

HW8

May 17, 2016

```
In [2]: import numpy as np
import cv2
%matplotlib inline
import matplotlib.pyplot as plt
import pandas as pd

In [3]: x = np.reshape([2,4,11,5,3,4,5,12,3,8,2,6,2,2,12,3,10,9,14,5,10,2,14,12,2],(5,5))
print len(np.unique(x))

11

In [4]: y = np.bincount(x.reshape((25,)))
ii = np.nonzero(y)[0]

In [5]: a = pd.Series(ii,name='value')
b = pd.Series(y[ii],name='Count')
df = pd.concat([a,b],axis=1)
df
```

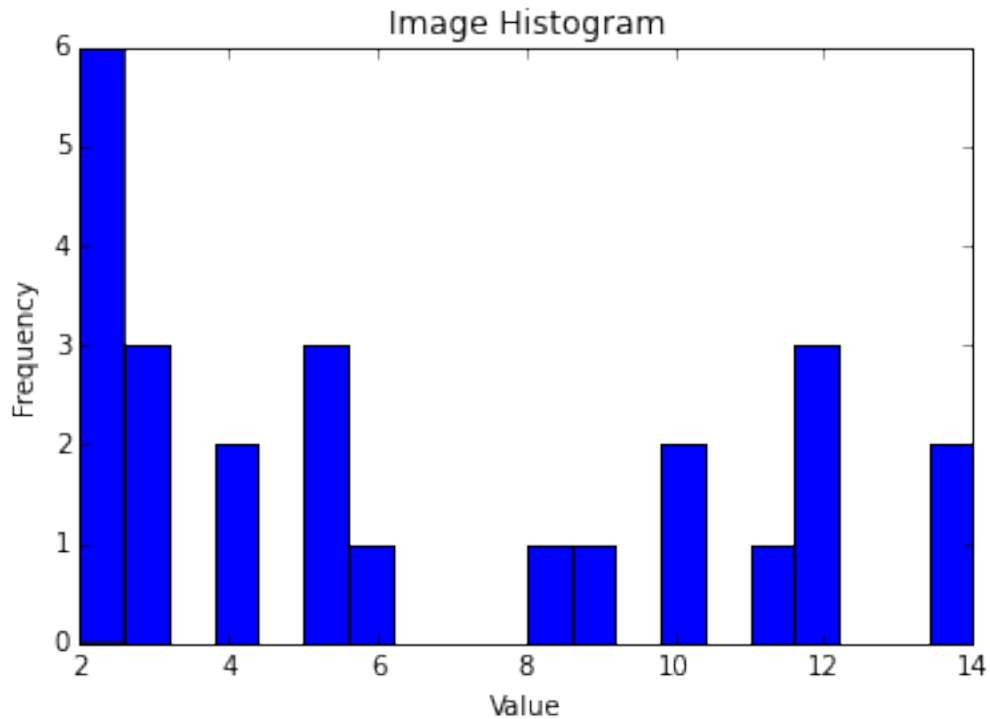
	value	Count
0	2	6
1	3	3
2	4	2
3	5	3
4	6	1
5	8	1
6	9	1
7	10	2
8	11	1
9	12	3
10	14	2

1 a)

Draw the histogram of this image

```
In [6]: plt.hist(x.reshape((25,)),bins=20)
plt.title("Image Histogram")
plt.xlabel("Value")
plt.ylabel("Frequency")
plt.xlim(np.min(x),np.max(x))

fig = plt.gcf()
plt.show()
```



2 b)

Find the output of HE and draw the histogram of equalized image

```
In [7]: table = zip(ii,y[ii])
p =map(lambda x:x[1]/float(25),table)
cdf = []
for i in range (len(p)):
    cdf.append(sum(p[:i+1]))
p =pd.Series(p,name='Probablitiy').to_frame()
cdf = pd.Series(cdf,name='CDF').to_frame()
df = df.join([p,cdf])
df
#table = zip(ii,y[ii],p,cdf)
#table
```

```
Out[7]:
```

	value	Count	Probablitiy	CDF
0	2	6	0.24	0.24
1	3	3	0.12	0.36
2	4	2	0.08	0.44
3	5	3	0.12	0.56
4	6	1	0.04	0.60
5	8	1	0.04	0.64
6	9	1	0.04	0.68
7	10	2	0.08	0.76
8	11	1	0.04	0.80

```

9      12      3      0.12  0.92
10     14      2      0.08  1.00

```

```
In [8]: df['HE'] = (((df.CDF-df.CDF.min())/(1-df.CDF.min())) *15).round()
```

```
In [9]: df
```

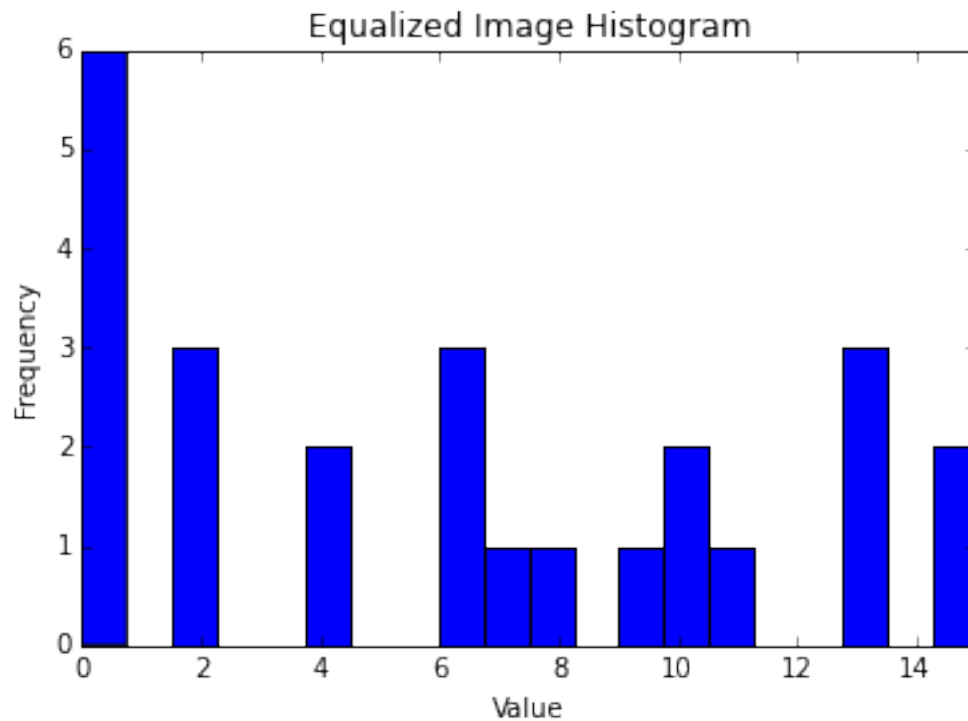
```
Out[9]:
```

	value	Count	Probablitiy	CDF	HE
0	2	6	0.24	0.24	0
1	3	3	0.12	0.36	2
2	4	2	0.08	0.44	4
3	5	3	0.12	0.56	6
4	6	1	0.04	0.60	7
5	8	1	0.04	0.64	8
6	9	1	0.04	0.68	9
7	10	2	0.08	0.76	10
8	11	1	0.04	0.80	11
9	12	3	0.12	0.92	13
10	14	2	0.08	1.00	15

```
In [10]: Eimg = map(lambda x:df[df.value==x].HE.values[0],x.reshape((25,)))
```

```
In [11]: plt.hist(Eimg,bins=20)
plt.title("Equalized Image Histogram")
plt.xlabel("Value")
plt.ylabel("Frequency")
plt.xlim(np.min(Eimg),np.max(Eimg))
```

```
fig = plt.gcf()
plt.show()
```



3 c)

If the equalized image in subject to compression by () Find the average length of the compression image.

```
In [12]: Ey = np.bincount(Eimg)
        Eii = np.nonzero(Ey)[0]
        Ea = pd.Series(Eii,name='value')
        Eb = pd.Series(Ey[Eii],name='Count')
        Edf = pd.concat([Ea,Eb],axis=1)
        Edf['Pr'] = Edf['Count']/25
        Edf = Edf.sort('Count',ascending=False)
        Edf
```

```
Out[12]:
```

	value	Count	Pr
0	0	6	0.24
1	2	3	0.12
3	6	3	0.12
9	13	3	0.12
2	4	2	0.08
7	10	2	0.08
10	15	2	0.08
4	7	1	0.04
5	8	1	0.04
6	9	1	0.04
8	11	1	0.04

```
In [39]: Ey = np.bincount(Eimg)
        Eii = np.nonzero(Ey)[0]
        Ea = pd.Series(Eii,name='value')
        Eb = pd.Series(Ey[Eii],name='Count')
        Edf = pd.concat([Ea,Eb],axis=1)
        Edf['Pr'] = Edf['Count']/25
        Edf.sort('Count',ascending=False, inplace=True)
        Edf = Edf.reset_index(drop=True)
        Edf['Code_Length'] = pd.Series([2,3,3,3,3,4,4,5,5,5,5])#2,3,3,3,3,4,4,5,5,5,5])
        Edf
```

```
Out[39]:
```

	value	Count	Pr	Code_Length
0	0	6	0.24	2
1	2	3	0.12	3
2	6	3	0.12	3
3	13	3	0.12	3
4	4	2	0.08	3
5	10	2	0.08	4
6	15	2	0.08	4
7	7	1	0.04	5
8	8	1	0.04	5
9	9	1	0.04	5
10	11	1	0.04	5

```
In [40]: np.sum( Edf['Pr']*Edf['Code_Length'])
```

```
Out[40]: 3.2400000000000007
```

4 d)

if a 3X3 laplacian with isotropy of 45 degree is applied to the pixel indicated in the circled of the equalized image find the new value.

```
In [41]: eimgnp = np.reshape(Eimg,(5,5))
         eimgnp
```

```
Out[41]: array([[ 0.,  4., 11.,  6.,  2.],
                [ 4.,  6., 13.,  2.,  8.],
                [ 0.,  7.,  0.,  0., 13.],
                [ 2., 10.,  9., 15.,  6.],
                [10.,  0., 15., 13.,  0.]])
```

```
In [42]: laplacian = np.reshape([1,1,1,1,-8,1,1,1,1],(3,3))
         imageImportantMatrix = np.reshape([6,13,2,7,0,0,10,9,15],(3,3))
```

```
In [43]: print laplacian
         print '======'
         print imageImportantMatrix
```

```
[[ 1  1  1]
 [ 1 -8  1]
 [ 1  1  1]]
====
[[ 6 13  2]
 [ 7  0  0]
 [10  9 15]]
```

Since we used negative center then we subtract :

```
In [44]: imageImportantMatrix[1,1] - (np.sum(laplacian*imageImportantMatrix))
```

```
Out[44]: -62
```