

1C  $I = \int_0^5 \frac{dx}{2\sqrt{x}}$  observe singularity @  $x=4$

lets try intervals  $0 \leq x \leq 3.999$  &  $4.001 \leq x \leq 5$

$$\int_a^b f(x) dx \approx \frac{h}{3} [f(x_0) + 4f(x_1) + 2f(x_2) + \dots + f(x_n)]$$

coeffs  $\rightarrow 1, 4, 2, 4, 2, \dots, 4, 2, 4, 1 \rightarrow n+1$  points

let  $h = \frac{b-a}{n}$  where  $n$  is even

$$h_1 = \frac{3.999 - 0}{4} = 0.99975$$

$$h_2 = \frac{5 - 4.001}{4} = 0.24975$$

$$\int_0^{3.99} \frac{h}{3} (f(0) \dots f(3.99))$$

$$+ \int_{4.001}^5 \frac{h}{3} (f(4.001) \dots f(5))$$

$$f(x_1)_1 = \frac{1}{2\sqrt{0.99975}} \approx 0.999875$$

$$f(x_2)_1 = 1.7066$$

$$f(x_3)_1 = 3.729$$

$$f(x_4)_1 = 399.7498$$

$$f(x_1)_2 = \frac{1}{2\sqrt{0.24975}} \approx 0.6665$$

$$f(x_2)_2 = 0.773$$

$$f(x_3)_2 = 0.8815$$

$$f(x_4)_2 = 0.9995$$

$$\frac{0.99975}{3} \left( f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + f(x_4) \right)$$

$$+ \frac{0.24975}{3} \left( -4000.25 + 4(0.6665) + 2(0.773) + 4(0.8815) + 0.9995 \right)$$

$$209.9864 + |-448| \approx 658$$