

# SAT Math Equations

December 29, 2024

## Contents

<b>1</b>	<b>Quadratics</b>	<b>2</b>
1.1	FOIL . . . . .	2
1.2	Quadratic Formula . . . . .	2
1.2.1	Derivation . . . . .	2
1.2.2	Alternatives . . . . .	2
1.3	Discriminant . . . . .	3
1.4	Vertex . . . . .	3
1.5	Factoring . . . . .	3
1.5.1	Aquarc Method . . . . .	3
<b>2</b>	<b>Sets</b>	<b>3</b>
2.1	Domain and Range . . . . .	3
2.2	Standard Deviation . . . . .	3
<b>3</b>	<b>Word Problems</b>	<b>3</b>
<b>4</b>	<b>Trigonometry</b>	<b>3</b>

# 1 Quadratics

A quadratic is a function in the form

$$f(x) = ax^2 + bx + c$$

Where  $\{a, b, c\} \in \mathbb{R}$ .

Or in the vertex form:

$$f(x) = a(x - h)^2 + k$$

Where  $\{a, h, k\} \in \mathbb{R}$

Or in the roots form:

$$f(x) = a(x - r_1)(x - r_2)$$

Where  $\{a, r_1, r_2\} \in \mathbb{R}$

## 1.1 FOIL

FOIL stands for First Outer Inner Last. Meaning, when you have

$$f(x) = (a_1x - r_1)(a_2x - r_2)$$

You get:

$$a_1a_2x^2 - a_1r_2x - a_2r_1x + r_1r_2 = a_1a_2x^2 - (a_1r_1 + a_2r_2)x + (r_1r_2)$$

## 1.2 Quadratic Formula

### 1.2.1 Derivation

$$ax^2 + bx + c = 0 \implies ax^2 + bx = -c \implies \frac{1}{a}ax^2 + \frac{b}{a}x = -\frac{c}{a} \implies x^2 + \frac{b}{a}x = -\frac{c}{a}$$

Complete the square:

$$\begin{aligned} x^2 + \frac{b}{a}x + \frac{b^2}{4a^2} &= -\frac{c}{a} + \frac{b^2}{4a^2} \implies (x + \frac{b}{2a})^2 = -\frac{4ac}{4a^2} + \frac{b^2}{4a^2} \implies (x + \frac{b}{2a})^2 = \frac{b^2 - 4ac}{4a^2} \\ &\implies \sqrt{(x + \frac{b}{2a})^2} = \frac{\pm\sqrt{b^2 - 4ac}}{2a} \implies x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \end{aligned}$$

### 1.2.2 Alternatives

In some scenarios it may be easier to use systems of equations.

Given a quadratic in the form:

$$ax^2 + bx + c = 0$$

We want to find  $r_1$  and  $r_2$  such that:

$$r_1 + r_2 = b \quad r_1r_2 = c$$

You can easily substitute around until you get the answer. If  $a \neq 1$  then it is difficult to use this formula.

**1.3 Discriminant**

**1.4 Vertex**

**1.5 Factoring**

You can use the two equations to do it

**1.5.1 Aquarc Method**

The fancy X thing

## **2 Sets**

**2.1 Domain and Range**

**2.2 Standard Deviation**

## **3 Word Problems**

You can't really predict what these will be. For

## **4 Trigonometry**