

GRADE- 11

MATHEMATICS

FINAL EXAM

100 MARKS

Chapter(1)

1. $(x-2)$ is a factor of $x^{n+1} + 5x^n - 10x - 36$. Then $n =$

A.2

B.4.

C.3 ✓

D.5

2. When $(2x + k)^{2024} + (x - 1)^2$ is divided by $(1+x)$, the remainder is 5. Then $k =$

A.3

B.-3

C.3 or 1 ✓

D.3 or -1

3. If $f(x) = x^7 - 97x^6 - 199x^5 + 99x^4 - 2x + 199$ is divided by $(x-99)$, then the remainder is

A.16

B.10

C.-2

D.1 ✓

4. The remainder when $5x^4 - 3x^2 + 4$ is divided by $x^2 + 2$ is

A.30 ✓

B.-30

C.20

D.-20

5. Given that $2x^3 + ax^2 + bx + c$

leave the same remainder when divided by $x-2$ or $x-1$. Find $3a+b+14$ (3-marks)


$$3a+b+14=0 \quad \checkmark$$

Chapter(2)

6. In the expansion of $(2a^2 - 3a^3)^n$ if the fifth term does not contain a factor of a , what is the value of n .

- A.11  B.10 C.9 D.6

7. ${}^nC_0 + {}^nC_2 + {}^nC_4 + \dots$ is

- A. n^2 B. 2^n C. 2^{n+1} D. 2^{n-1} 


8. Find the last two digits of 3^{10} is

-  A.49 B.50 C.51 D.9

9. The number of terms in the expansion of $(1 - 2x + x^2)^{50}$ is

- A.51 B.52 C.100 D.101 

10. Given that $\left(p - \frac{1}{2}x\right)^6 = r - 96x + sx^2 + \dots$. Find p , r and s . (3-marks)

$p =$  A.2 B.-2 C.3 D.-3

$r =$ A.32 B.64  C.243 D.729

$s =$ A.15 B.30 C.45 D.60 

Chapter(3)

11. Given that $f(x)=x^2$, stretched by a factor of 2 , shifted vertically 3 units downward. The resulting function is

- A. $\frac{1}{2}x^2 - 3$ B. $2x^2 - 3$ ✓
C. $\frac{1}{2}x^2 + 3$ D. $2x^2 + 3$

13. The graph of $y=f(x)$ move nearer horizontally by scale factor $\frac{1}{q}$ to the Y-axis , when q is

- A. $0 < q < 1$ B. $q > 1$ ✓
C. $q < 1$ D. $q = 1$

12. The graph of an even function is symmetric with respect to


- A. X-axis B. origin
C. Y-axis ✓ D. neither

14. A point p is reflected in the origin. Coordinates of its images are $(-2,5)$, then p is


- A. $(2,-5)$ ✓ B. $(-2,-5)$ C. $(-2,5)$ D. $(2,5)$

(15) The transformation function, $f(x) = -2\left(\frac{1}{3}x - 1\right)^3 + 2$, answer the following questions. (5 marks)

(i) Which of the following is the parent function for $f(x)$?


- A. $y = x$  B. $y = x^3$ C. $y = |x|$ D. $y = \sqrt{x}$

(ii). Write a description for the two translations.

- A. translation 1 unit to the right and 2 units up 
 B. translation 1 unit to the right and 2 units down
 C. translation 1 unit to the left and 2 units up
 D. translation 1 unit to the left and 2 units down


(iii) If the point $A(0, 0)$ is on the original graph, then the respective point on the graph of

$$y = -2\left(\frac{1}{3}x - 1\right)^3 + 2 \text{ is}$$

- A. $(-2, 0)$  B. $(3, 2)$ C. $(-1, 0)$ D. $(3, -2)$

(iii) If the point $A(-2, -8)$ is on the original graph, then the respective point on the graph of

$$y = -2\left(\frac{1}{3}x - 1\right)^3 + 2 \text{ is}$$

-  A. $(-3, 18)$ B. $(3, 16)$ C. $(3, -18)$ D. $(3, -16)$

(iii) If the point $A(2, 8)$ is on the original graph, then the respective point on the graph of

$$y = -2\left(\frac{1}{3}x - 1\right)^3 + 2 \text{ is}$$

- A. $(-9, 14)$ B. $(9, 16)$  C. $(9, -14)$ D. $(9, -16)$

Chapter(4)

16. The smallest positive number in an AP 179, 173, 167, ...

is A.2 B.3 C.4 D.5 ✓

17. The product of 5 consecutive terms of a GP is 243, then the middle term is

A.9 B.4 C.5 D.3 ✓

18. The sum to infinity of $1 + 1 + \frac{1}{2} + \frac{1}{4} + \dots$ is

A.4 B.3 ✓ C. $\frac{1}{2}$ D.2

19. $(n - 2)^{th}$ term of an AP is $(n+2)$. Then $(n + 2)^{th}$ term is

A.n+4 B.n-4 C.n+6 ✓ D.n-6

20. Find the sum of the first n natural numbers. (3-marks)

a= A.0 B.1 ✓ C.2 D.-1

d= A.1 ✓ B.2 C.3 D.-1

$S_n =$

A. $\frac{1}{2}n$ B.2n

C. n^2 D. $\frac{1}{2}(n^2 + n)$ ✓

Chapter(5)

21. If $C = \begin{bmatrix} 1 & -2 & 0 \\ 3 & 4 & -1 \end{bmatrix}$, then which of the following is(are) true?

(1) $C_{21}=3$ (2) $C_{11} + C_{23} = C_{13}$ (3) $C_{22} - C_{12}=2$

A.1 only B.2 only

C.1 and 2  only D.1,2,3


22. If $\begin{bmatrix} b & 2-c \\ 4-d & a \end{bmatrix} = \begin{bmatrix} 3-a & b \\ c & 5-d \end{bmatrix}$, then $\mathbf{a + b + c + d =}$

A. 4 B. 5 C. 6 D. 7 ✓

23. Given that $\begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 2 \end{bmatrix}$, then $\begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} =$

A. $\begin{bmatrix} 0 \\ -1 \end{bmatrix}$ B. $\begin{bmatrix} 4 \\ 1 \end{bmatrix}$ C. $\begin{bmatrix} \frac{11}{2} \\ 2 \end{bmatrix}$ ✓ D. $\begin{bmatrix} 16 \\ 9 \end{bmatrix}$

24. If $Q = \begin{bmatrix} 3 & 7 \\ 2 & 5 \end{bmatrix}$, then $(Q^{-1})^T =$

A. $\begin{bmatrix} 5 & 2 \\ 7 & 3 \end{bmatrix}$ B. $\begin{bmatrix} 3 & -2 \\ -1 & 1 \end{bmatrix}$ C. $\begin{bmatrix} 3 & -1 \\ -2 & 1 \end{bmatrix}$ D.  $\begin{bmatrix} 5 & -2 \\ -7 & 3 \end{bmatrix}$

25. Given that $A = \begin{bmatrix} 1 & 0 \\ 3 & 4 \end{bmatrix}$ and $A - kI$ is singular then $k =$

A.-1 or 4 B.1 or -4

C.1 or 4 ✓ D.-1 or -4

26. $P = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$, $\det P = 14$, $ac = 8$ and $bd = 15$. Then

$Q = \begin{pmatrix} a^{-1} & b^{-1} \\ c^{-1} & d^{-1} \end{pmatrix}$. Find $\det Q$. (3-marks)

det P= A.ab-cd B.ab+cd

C.ad-bc ✓ D.ad+bc

$$\det Q =$$

A. $a^{-1}b^{-1} - c^{-1}d^{-1}$ B. $a^{-1}b^{-1} + c^{-1}d^{-1}$

C. $a^{-1}d^{-1} - b^{-1}c^{-1}$ ✓ D. $a^{-1}d^{-1} + b^{-1}c^{-1}$

$$\det Q =$$

A. $-\frac{7}{60}$  B. $\frac{7}{60}$ C. -120 D. 112

Chapter(6)

27. If the mean of 26, 19, 15, 24 and x is x , then the median of the data is

- A. 19 B. 20 C. 21 D. 22

28. Since the value of correlation coefficient is zero,

1. there is no relationship

2. there is no linear relationship

3. there is strong positive linear relationship

- A. 1-only B. 1 and 2-only C. 2-only D. 3-only

32. Consider the frequency of five observations $x-2, x-4, y, -2x, x$. If the cumulative frequency of fifth observation is 9, find the value of y and express the equation of regression line. (3-marks)

Cumulative frequency of fifth is

- A. x B. $-3x$ C. $-x+y$ D. $x-6+y$

29. The class mark of a class is 25 and if the upper limit of that class is 40, then its lower limit is

- A. 15 B. 20 C. 10 D. 5

30. If the variance of the data is 12.25, then the standard deviation is

- A. 3.5 B. 3.25 C. 3 D. 2.5

31. The variance of 10, 10, 10, 10, 10 is

- A. 0 B. 5 C. 10 D. $\sqrt{10}$

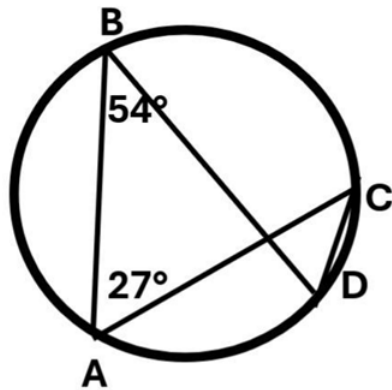
$y =$ A. 9 B. $-27-x$ C. $15-x$ D. $9-x$

The equation of regression line is

- A. $y = ax + b$ B. $y = a + bx$ C. $y = ax - b$ D. $y = a - bx$

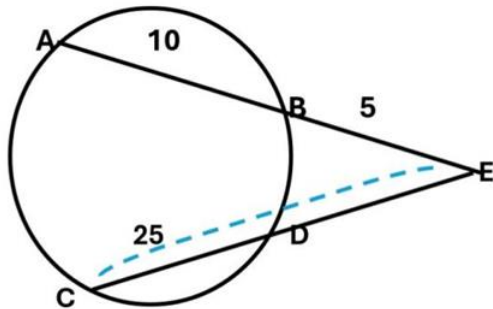
Chapter(7)

33. A,B,C,D are points on the circumference of a circle.If $\angle BAC = 27^\circ$ and $\angle ABD=54^\circ$, then $\angle ACD=$



- A. 27° B. 54° ✓ C. 60° D. 90°

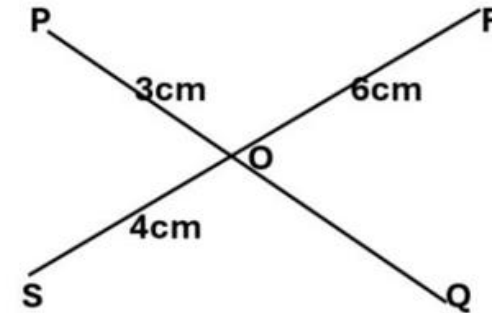
34. In the diagram if $AB=10\text{cm}$, $BE=5\text{cm}$ and $CE=25\text{cm}$, then $DE=$



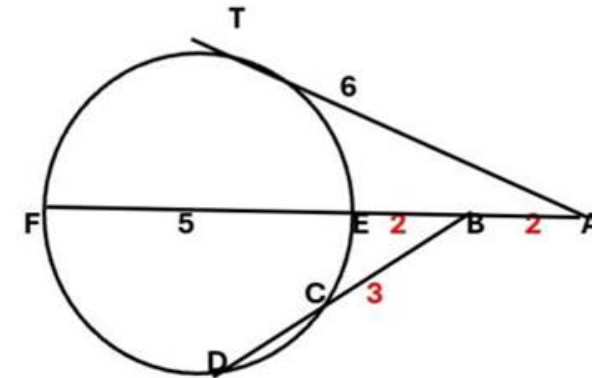
- A. 2cm B. 3cm ✓ C. 5cm D. 7cm

35. The points P,Q,R and S will be concyclic if $OQ=$

- A. 8cm ✓ B. 6cm C. 4cm D. 2cm



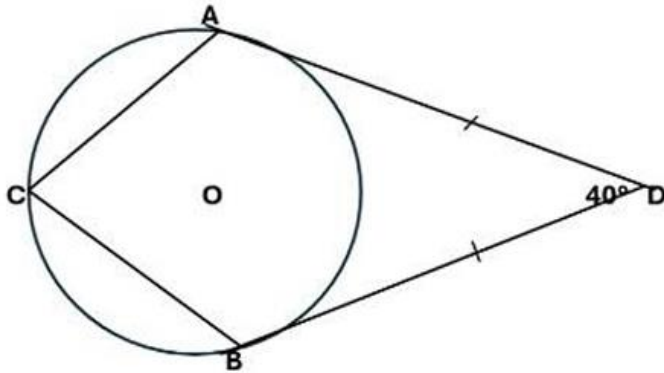
36. In the figure $CD=$



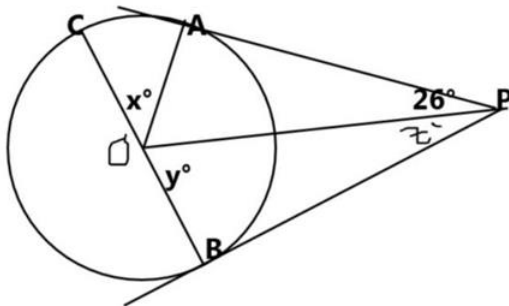
- ✓
A. 1.67 B. 4.13 C. 2.51 D. 4.12.

37. In the figure, DA and DB are tangents to the circle whose centre is O and $DA = DB$. If $\angle ADB = 40^\circ$ then $\angle ACB$ is

- A. 140° ☒ B. 70° C. 35° D. 55°



38. In the figure, PA and PB are tangent to circle O. Find the values of x, y and z. (3-marks)



PA and PB are tangents.

$\angle AOP =$

- A. 90° B. 52° ☒ C. 26° D. 13°

$\angle AOP = \angle BOP$ (OP bisects $\angle AOB$)

$\angle AOP = y$

In $\triangle OAP$, $\angle AOP + \angle OPA + \angle OAP = 180^\circ$

$y =$

- A. 26° ☒ B. 64° C. 45° D. 52°

BOC is a straight line.

$x =$

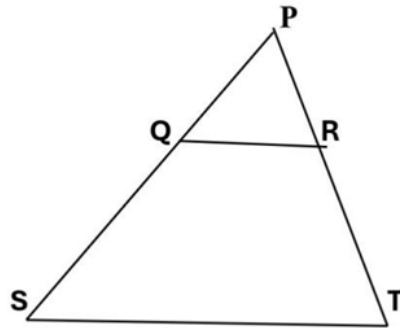
- A. 64° B. 45° C. 26° ☒ D. 52°

Chapter(8)

39. The area of two similar triangles are in the ratio 4:9. One side of smaller triangle is 4. The corresponding side of the other triangle is

- A.9 B.8 C.6 ✓ D.3

40. In the diagram, $QR \parallel ST$. If $\frac{\alpha(\Delta PQR)}{\alpha(\Delta PST)} = \frac{9}{64}$, then $PQ:QS =$



- A.3:8 B.3:5 ✓ C.5:3 D.2:5

41. Two chords of a circle PQ and RS intersect at O, $\alpha(\Delta POR) : \alpha(\Delta SOQ) =$

- A. $OP^2 : OS^2$ ✓ B. $PO^2 : OQ^2$
C. $OQ^2 : PR^2$ D. $OP^2 : OR^2$

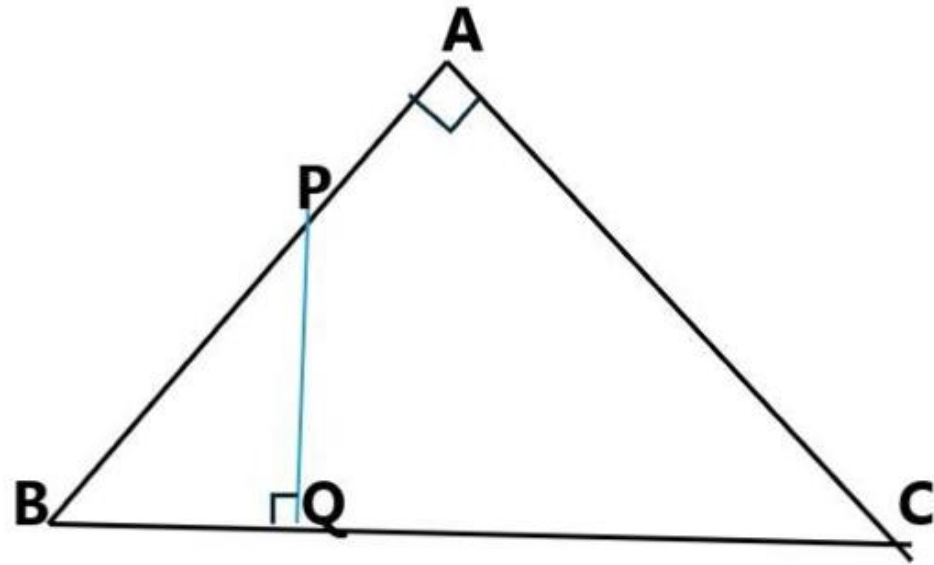
42. In the trapezium PQRS, $PQ \parallel SR$ and $SR = 2PQ$. PR and QS intersect at O. Given that $\alpha(\Delta POQ) = 5\text{cm}^2$ then $\alpha(\Delta SOR) =$

- A. 10cm^2 B. 15cm^2
C. 20cm^2 ✓ D. 25cm^2

43. The area of two similar triangles are in the ratio 4:9. One side of the smaller triangle is a-cm. The corresponding side of the other triangle is

- A. $2a$ B. $\frac{3a}{2}$ ✓ C. $3a$ D. $\frac{2a}{3}$

44. In $\triangle ABC$, $\angle A = 90^\circ$, $PQ \perp BC$, if $AC = 3$, $BC = 5$ and $CQ = 3$, find $\alpha(\triangle BPQ) : \alpha(\triangle PQC)$ [3 – marks]



In $\triangle ABC$, $\angle A = 90^\circ$

$AB =$

A. 3 B. 4 C. 5 D. 6

$\triangle BPQ \sim \triangle BCA$ (AA corollary)

$$\frac{\alpha(\triangle BPQ)}{\alpha(\triangle BCA)} =$$

A. $\frac{1}{2}$ B. $\frac{1}{3}$ C. $\frac{1}{4}$ D. $\frac{1}{6}$

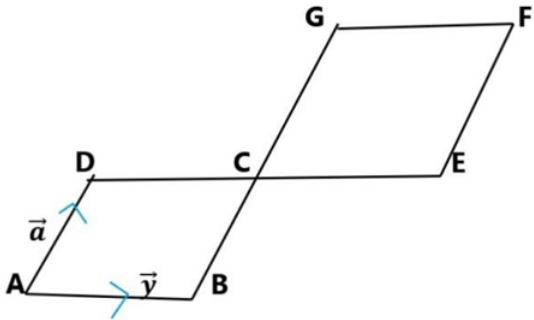
$$\frac{\alpha(\triangle BPQ)}{\alpha(\triangle PQC)} =$$

A. 1:2 B. 1:3 C. 1:4 D. 1:6

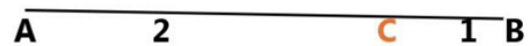
45. Parallelogram ABCD is translated to the position

CEFG so that DCE and BCG are straight lines. If $\overrightarrow{AD} = \vec{a}$, $\overrightarrow{AB} = \vec{y}$, then $\overrightarrow{GD} =$

- A. $\vec{a} + 2\vec{y}$ B. $\vec{a} + \vec{y}$
C. $-\vec{a} - \vec{y}$ ✓ D. $\vec{a} + 3\vec{b}$



46. If $\overrightarrow{AB} = -3\overrightarrow{BC}$, which of the following is(are) true?



1. $AB = -3BC$ 2. A, B, C are collinear 3. C
lies between A and B

- A. 1 only B. 2 only C. 3 only D. 2 and 3 only ✓

47. Given that $\vec{a} = 3\hat{i} + 4\hat{j}$. Then the vector with magnitude 20 units and in the direction of \vec{a} is

- A. $12\hat{i} + 6\hat{j}$ B. $60\hat{i} + 120\hat{j}$
C. $12\hat{i} + 16\hat{j}$ ✓ D. $-12\hat{i} - 16\hat{j}$

48. $P = (3, 4)$, $R = (8, 2)$ and O is the origin. If $\overrightarrow{OT} = \overrightarrow{OP} + \frac{1}{2}\overrightarrow{OR}$, then T =

- A. (11, 6) B. (5, -2) C. (5, 7)
D. (7, 5) ✓

49. If the vector $\begin{pmatrix} x \\ y \end{pmatrix} - \begin{pmatrix} 3 \\ 5 \end{pmatrix}$ is parallel to $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$ then

- A. $3x - y = 12$ B. $3x + y = 12$
C. $3y - x = 12$ ✓ D. $3y + x = 12$

Chapter(9)

50. The position vectors of A, B and C are $2\vec{p} - \vec{q}$, $k\vec{p} + \vec{q}$ and $12\vec{p} + 4\vec{q}$ respectively.

Calculate the value of k if A, B and C are collinear. (3- marks)

Solution

Let O be the origin,

$$\overrightarrow{OA} = 2\vec{p} - \vec{q}, \overrightarrow{OB} = k\vec{p} + \vec{q}, \overrightarrow{OC} = 12\vec{p} + 4\vec{q}$$

$$\overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{OA}$$

✓
A. $(k - 2)\vec{p} + 2\vec{q}$

B. $(k + 2)\vec{p} + 2\vec{q}$

C. $(k - 2)\vec{p} - 2\vec{q}$

D. $(k + 2)\vec{p} - 2\vec{q}$

$$\overrightarrow{AC} = \overrightarrow{OC} - \overrightarrow{OA}$$

A. $10\vec{p} - 5\vec{q}$

✓
B. $10\vec{p} + 5\vec{q}$

C. $-10\vec{p} + 5\vec{q}$

D. $-10\vec{p} - 5\vec{q}$

If A, B and C are collinear,

$$\overrightarrow{AB} = h \overrightarrow{AC}$$

$$(k - 2)\vec{p} + 2\vec{q} = 10h\vec{p} + 5h\vec{q}$$

$$k - 2 = 10h \quad \text{and} \quad 2 = 5h$$

$$k = ?$$

A. 2

B. 5

✓
C. 6

D. 10


Chapter(9)


(2) The vectors \overrightarrow{OP} has magnitude of 39 units and has the same direction as $\begin{bmatrix} 5 \\ 12 \end{bmatrix}$.


(5 marks)


The vectors \overrightarrow{OQ} has magnitude of 25 units and has the same direction as $\begin{bmatrix} 3 \\ 4 \end{bmatrix}$.

Express the vector \overrightarrow{OP} and \overrightarrow{OQ} as column vectors and find the unit vector of \overrightarrow{PQ} .

(i) $\hat{p} =$ A. $\frac{1}{13} \begin{bmatrix} -5 \\ 12 \end{bmatrix}$  B. $\frac{1}{13} \begin{bmatrix} 5 \\ 12 \end{bmatrix}$ C. $\frac{1}{13} \begin{bmatrix} -5 \\ -12 \end{bmatrix}$ D. $\frac{1}{13} \begin{bmatrix} 5 \\ -12 \end{bmatrix}$

(ii) $\overrightarrow{OP} =$  A. $\begin{bmatrix} 15 \\ 36 \end{bmatrix}$ B. $\begin{bmatrix} -15 \\ 36 \end{bmatrix}$ C. $\begin{bmatrix} -5 \\ -36 \end{bmatrix}$ D. $\begin{bmatrix} 15 \\ -36 \end{bmatrix}$

(iii) $\hat{q} =$ A. $-\frac{1}{5} \begin{bmatrix} 3 \\ 4 \end{bmatrix}$ B. $\frac{1}{5} \begin{bmatrix} -3 \\ 4 \end{bmatrix}$  C. $\frac{1}{5} \begin{bmatrix} 3 \\ 4 \end{bmatrix}$ D. $\frac{1}{5} \begin{bmatrix} 3 \\ -4 \end{bmatrix}$

(iv) $\overrightarrow{OQ} =$ A. $\begin{bmatrix} -15 \\ 20 \end{bmatrix}$ B. $\begin{bmatrix} -15 \\ -20 \end{bmatrix}$  C. $\begin{bmatrix} 15 \\ 20 \end{bmatrix}$ D. $\begin{bmatrix} 15 \\ -20 \end{bmatrix}$

(v) the unit vector of $\overrightarrow{PQ} =$ A. $\begin{bmatrix} 0 \\ 1 \end{bmatrix}$ B. $\begin{bmatrix} -1 \\ 0 \end{bmatrix}$ C. $\begin{bmatrix} 1 \\ 0 \end{bmatrix}$  D. $\begin{bmatrix} 0 \\ -1 \end{bmatrix}$

Chapter(10)

52. In $\triangle ABC$, $a : b : c = 1 : 3 : \sqrt{7}$ then $LC =$

- A. 30° B. 45° C. 60° Chapter(10) D. 90°

53. $\cos 4A - \cos 6A =$

- A. $\cos 2A$ B. $2\sin A \sin 5A$ Chapter(10)
C. $-2\sin A \sin 5A$ D. $2 \cos A \cos 5A$

54. $\sin(-90^\circ) + \tan 45^\circ + 2 \sin 30^\circ =$

- A. 0 B. 2 C. -1 D. 1 Chapter(10)

55. $\cos(30^\circ + x) - \sin(60^\circ - x) =$

- A. 0 B. 1 C. -1 D. $\frac{1}{2}$ Chapter(10)

56. $\csc A$ cannot be

- A. -50 B. 4 C. 0 Chapter(10) D. 1

57. Which of the following is(are) false?

1. $\sin 70^\circ = \cos 20^\circ$ 2. $\tan 45^\circ = \cot 45^\circ$
3. $\sec A = \csc(90^\circ - A)$
A. 1 only B. 2 only
C. 3 only D. 1 and 3 only Chapter(10)

58. Solve the $\triangle ABC$ with $a=2$, $c=\sqrt{6}$ and $LC=60^\circ$,

having given that $\sin 75^\circ = \frac{\sqrt{6} + \sqrt{2}}{4}$. (3 - marks)

Solution

$LA =$ A. 30° Chapter(10) B. 45° C. 60° D. 90°

$LB =$

A. 55° B. 65° Chapter(10) C. 75° D. 85°

$b =$

A. $\sqrt{3} - 1$ B. $-\sqrt{3} - 1$ Chapter(10) C. $\sqrt{3}$ D. $\sqrt{3} + 1$

59..Solve ΔABC with $a = \frac{1}{\sqrt{6}-\sqrt{2}}$, $b = \frac{1}{\sqrt{6}+\sqrt{2}}$, $LC = 60^\circ$.

Solution

By the law of Cosines, $c^2 =$

- ☒ A. $a^2 + b^2 - 2ab \cos C$ B. $a^2 - b^2 + 2ab \cos C$
 C. $a^2 - b^2 - 2ab \cos C$ D. $-a^2 - b^2 + 2ab \cos C$

The value of c , $c =$

- A. $\frac{1}{2}$ ☒ B. $\frac{\sqrt{3}}{2}$ C. $\frac{\sqrt{2}}{2}$ D. $\frac{3}{4}$

By the law of Sines,

$\sin A =$

- A. $c^2 \sin C$ B. $a^2 \sin C$ C. $\frac{c \sin C}{a}$ ☒ D. $\frac{a \sin C}{c}$

The value of LA , $LA =$

- A. 30° B. 45° ☒ C. 75° D. 60°

The value of LB , $LB =$

- A. 75° B. 30° ☒ C. 45° D. 60°

Chapter(11)

60. If $f(x) = \frac{1}{x^3+1}$, then $f'(1) =$

- A. $\frac{1}{2}$ B. $-\frac{1}{2}$ C. -1 D. $-\frac{3}{4}$ ✓

61. $\lim_{x \rightarrow \infty} (2x^5 + 3x^2 - 2)$

- A. ∞ ✓ B. $-\infty$ C. 0 D. 1

62. If $g(x) = \sqrt{x+2}$, g is continuous on its domain of

- A. $(-2, \infty)$ B. $[-2, -\infty)$ C. $(-2, \infty)$ D. $[-2, \infty)$ ✓

63. Given that the gradient of the curve $y = x^2 + ax + b$ at the point $(2, -1)$ is 1.

Find the values of a and b . (3-marks)

$$y = x^2 + ax + b \quad \frac{dy}{dx} =$$

- A. $2x+a$ ✓ B. $2x + a + b$ C. $2 + a$ D. $2x^2 + a$

$a =$

- A. 3 B. -3 ✓ C. 4 D. -4

$b =$

- A. 3 B. 2 C. 1 ✓ D. 0

64. Find the equation of the tangent line and normal line to the curve $x^2 - y^2 = 25$ at the point (1,3).

Solution

$$x^2 - y^2 = 25, \text{ then } \frac{dy}{dx} =$$

- ✓ A. $\frac{x}{y}$ B. xy C. $\sqrt{x^2 - 25}$ D. $25 + x^2$

The slope of the tangent line at the point (1,3) is

m=

- A. 3 B. 1 C. -1 ✓ D. $\frac{1}{3}$

The equation of the tangent line at the point (1,3) is

$$3y =$$

- A. $x+9$ ✓ B. $x+8$ C. $x+2$ D. $x-2$

The slope of the normal line is

m=

- A. -2 B. 2 C. 1 ✓ D. -3

The equation of the normal line at the point (1,3) is

y=

- A. $-x - 4$ B. $x - 4$ ✓ C. $-3x + 6$ D. $-x + 4$

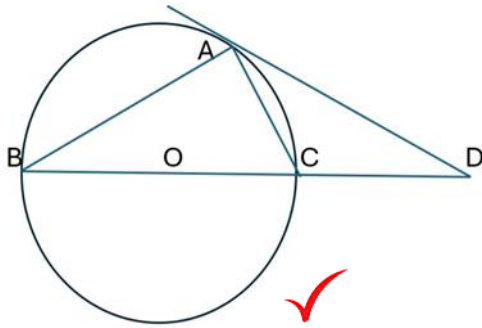


65. The opposite angles of a cyclic quadrilateral are in the ratio 3:7 .

The difference of their degree measure is

- A. 90° B. 72° C. 40° D. 30°

67. In circle O, $AD=6$, $AB=4$ and $AC=3$, then $CD=$



- A. 6 B. 5 C. 4 D. 3

69. Given that $\triangle ABC \sim \triangle PQR$,

$$\alpha(\triangle ABC) : \alpha(\triangle PQR) = 25 : 9,$$

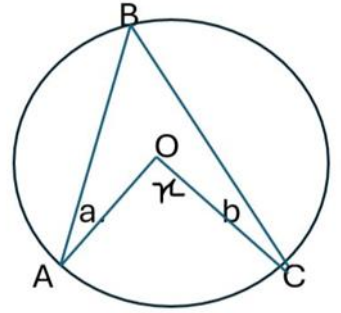
AB and PQ are corresponding sides and

$AB - PQ = 6\text{cm}$. Then $PQ =$

- A. 4 B. 6 C. 9 D. 12

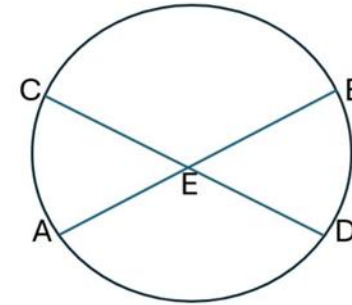
66. In the figure, O is centre of the circle , $x =$

- A. $2a + 2b$ B. $180^\circ - 2a$
C. $2a - 2b$ D. $a + b$



68. In the figure $CE=6$, $CD=24$ and $AE=4EB$, $AB=$

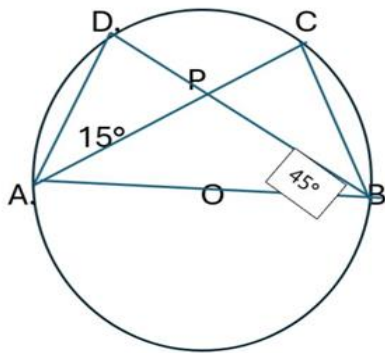
- A. $3\sqrt{3}$ B. $10\sqrt{3}$ C. $12\sqrt{3}$ D. $15\sqrt{3}$



70. Sum and difference of areas of two similar triangles are 234 and 90. The ratio of corresponding sides is

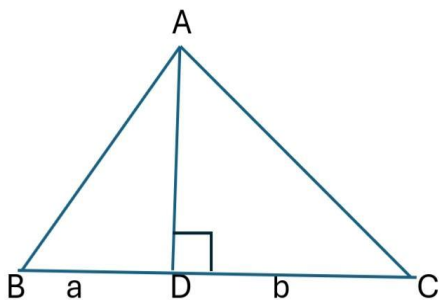
- A. 2:3 B. 3:5 C. 4:5 D. 5:8

71. In circle O, AB is a diameter, $\angle DAC = 15^\circ$ and $\angle ABD = 45^\circ$ then $\alpha(\triangle APD) : \alpha(\triangle BPC) =$



✓
A. 2:1 B. 3:1 C. 3:2 D. 9:1

72. In the figure, AD is perpendicular to BC, $\alpha(\triangle ABD) : \alpha(\triangle ACD) =$



✓
A. $a^2 : b^2$ B. $b^2 : a^2$ C. $b : a$ D. $a : b$

73. $\overrightarrow{AB} - \overrightarrow{CB} =$

✓
A. \overrightarrow{AB} B. \overrightarrow{AC} C. \overrightarrow{BC} D. \overrightarrow{CA}

74. \vec{a} and \vec{b} are non zero and non parallel vectors.

If $3\vec{a} + x(\vec{b} - \vec{a}) = y(2\vec{a} + \vec{b})$. Then $2x + 3y =$

A. 2 B. 3 C. 5 ✓ D. 7

75. If $P = (-1, 1)$ and $Q = (1, -1)$, then the length of \overrightarrow{PQ} is

A. 1 B. $\sqrt{2}$ C. $2\sqrt{2}$ ✓ D. 2

76. If $\vec{p} = 8\hat{i} + 7\hat{j}$, $\vec{q} = -3\hat{i} + 5\hat{j}$, then $|\vec{p} + \vec{q}| =$

A. 16 B. 15 C. 14 D. 13 ✓

77. If \overrightarrow{AB} is a unit vector, then $|\overrightarrow{AB}| =$

✓
A. -1 B. 1 C. $\sqrt{2}$ D. 0

78. If $\sin 20^\circ = x$, then $\sec 290^\circ =$

✓
A. x B. $-x$ C. $\frac{1}{x}$ ✓ D. $-\frac{1}{x}$

79. Given that $\sin \alpha = \frac{1}{2}$ and $\cos \beta = \frac{1}{2}$,

then the value of $(\alpha + \beta) =$

- A. 0° B. 30° C. 60° D. 90°

80. $\triangle ABC$ is right angle at C, the value of $\cos(A+B)$ is

- A. 0 B. 1 C. $\frac{1}{2}$ D. $\sqrt{3}$

81. If $\cot x = \sqrt{3}$, then $\tan(180^\circ - x) =$

- A. $\frac{1}{\sqrt{3}}$ B. $-\frac{1}{\sqrt{3}}$ C. $-\sqrt{3}$ D. $\sqrt{3}$

82. In $\triangle ABC$, $\alpha : \beta : \gamma = 3 : 4 : 5$, then $a : b =$

- A. $2 : \sqrt{3}$ B. $1 : \sqrt{3}$
C. $1 : \sqrt{2}$ D. $2 : \sqrt{6}$

83. $\lim_{x \rightarrow -3} \left(\frac{x^3 - 3^3}{x - 3} \right) =$

- A. 27 B. -27 C. 9 D. -9

84. If $f(x) = \frac{\sqrt{x}}{2x}$, then $f'(1) =$

- A. 1 B. $\frac{1}{2}$ C. -1 D. $-\frac{1}{4}$

85. The value of x at which f is not continuous $f(x) = \frac{x^2 - 9}{|x - 3|}$ is

- A. -3 B. 3 C. ∞ D. 9

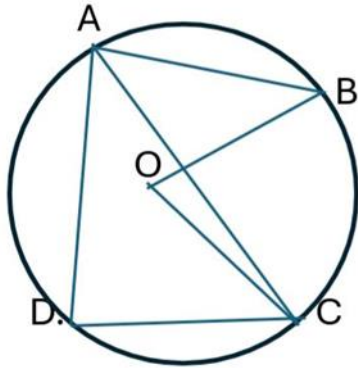
86. One sided limit of $\lim_{x \rightarrow 2^+} \left(\frac{x}{x^2 - 2x} \right)$ is

- A. 2 B. -2 C. ∞ D. $-\infty$

87. If $xy = 2$, $\frac{dy}{dx} =$

- A. $-\frac{y}{x}$ B. $\frac{y}{x}$ C. x D. y

88. In circle O, the circle through A, B, C, D. $\angle BOC = 100^\circ$ and $\angle OBA = 62^\circ$. Calculate $\angle BAC$, $\angle OCB$ and $\angle ADC$.



$\angle BAC =$

- A. 30° B. 40°
 ✓ C. 50° D. 60°

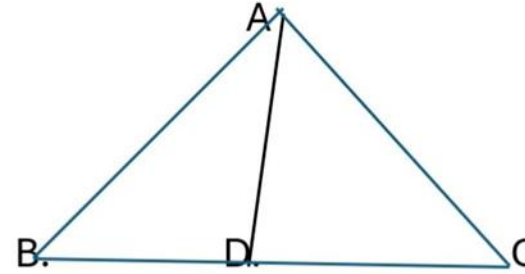
$\angle OCB =$

- A. 30° B. 40° ✓
 C. 50° D. 60°

$\angle ADC =$

- A. 68° B. 78° ✓
 C. 58° D. 88°

89. In $\triangle ABC$, $BD = 3$, $DC = 4$ and $\alpha(\triangle ABD) = 5$. Find $\alpha(\triangle ABC)$ and $\alpha(\triangle ADC)$.



$\alpha(\triangle ABD) : \alpha(\triangle ABC) =$

- A. $\frac{3}{4}$ ✓ B. $\frac{3}{7}$ C. $\frac{4}{3}$ D. $\frac{9}{16}$

$\alpha(\triangle ABC) =$

- A. 7 B. 4 C. 3 D. 11.67 ✓

$\alpha(\triangle ADC) =$

- A. 3 B. 4 C. 3.43 D. 6.67 ✓

90. Relative to an origin O, the position vector of the points A, B, C are $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$, $\begin{pmatrix} 1 \\ 3 \end{pmatrix}$ and $\begin{pmatrix} 8 \\ 9 \end{pmatrix}$ respectively.

If $m\vec{a} + n\vec{b} = \vec{c}$, find the value of m, n and \overrightarrow{AC} .

Solution

m =

A.1 B.2 C.3 D.4

n =

A.1 B.2 C.3 D.4

$\overrightarrow{AC} =$

A.(6,8) B.(-6,-8)
C.(7,6) D.(-7,-6)

91. In a triangle, $2 \sin^2 \alpha - \cos^2 \alpha = 2$, find α .

Solution

$(\cos^2 \alpha) =$

A. $1 + \sin \alpha$ C. $1 + (\sin^2 \alpha)$

B. $1 - \sin \alpha$ D. $1 - (\sin^2 \alpha)$

$\sin \alpha =$

A.1 B.-1 C. ± 1 D.0

$\alpha =$

A. 270° B. 90° C. 60° D. 0°

92. If $y = x^2 + 2x + 3$, find $(y')^2 + (y'')^3$

Solution

$y' =$

A. $2x + 2$ B. $2x - 2$
C. $2x + 2 + 3$ D. $2x - 2 + 3$

$y'' =$

A.-2 B.2 C.-4 D.4

$(y')^2 + (y'')^3 =$

A.y B.2y C.3y D.4y

93. Given that $\vec{a} = \begin{pmatrix} p \\ 3 \end{pmatrix}$ and $\vec{b} = \begin{pmatrix} 7 \\ 9 \end{pmatrix}$, find the value(s) of p if (i) \vec{a} is parallel to \vec{b} (ii) \vec{a} and \vec{b} are same magnitude.

Solution

\vec{a} is parallel to \vec{b}

$$\vec{a} = \text{A. } \vec{b} \quad \text{B. } -\vec{b} \quad \text{C. } k\vec{b} \quad \text{D. } -k\vec{b}$$

$$p =$$

$$\text{A. } 7 \quad \text{B. } 3 \quad \text{C. } \frac{3}{7} \quad \text{D. } \frac{7}{3}$$

$$k =$$

$$\text{A. } 1 \quad \text{B. } \frac{1}{3} \\ \text{C. } 3 \quad \text{D. } -\frac{1}{3}$$

\vec{a} and \vec{b} are same magnitude

$$\text{A. } |\vec{a}| = |\vec{b}| \quad \text{B. } \vec{a} = \vec{b}$$

$$\text{C. } |\vec{a}| = -|\vec{b}| \quad \text{D. } \vec{a} = \vec{b}$$

$$p =$$

$$\text{A. } 11 \quad \text{B. } -11 \quad \text{C. } \pm 11 \quad \text{D. } 0$$

94. Solve the triangle ABC with $\gamma = 60^\circ$, $a = 5$, $b = 8$.

And then find the area of $\triangle ABC$.

Solution

c=

A. ± 7 **B. 7** **C. ± 10** **D. 10**

$\alpha =$

A. $38^\circ 12'$ **B. $48^\circ 12'$**

C. $58^\circ 12'$ **D. $68^\circ 12'$**

$\beta =$

A. $71^\circ 48'$ **B. $81^\circ 48'$**

C. $61^\circ 48'$ **D. $51^\circ 48'$**

S=

A. 11.5 **B. 10.5** **A. 15.3** **B. 16.3**

C. 20 **D. 10** **C. 17.3** **D. 18.3**

Area of $\triangle ABC =$

95. Find the coordinate of the points on the curve $x^2 + y^2 = 32$ at which the tangent is perpendicular to the line $x + y = 1$.

$y' =$ **A. $-\frac{x}{y}$** **B. $\frac{x}{y}$** **C. $2x$** **D. $-2x$**

x=

A. y **B. $-y$** **C. $\frac{1}{2}y$** **D. $2y$**

y=

A. 4 **B. -4** **C. ± 4** **D. ± 2**

x = **A. 4** **B. -4** **C. ± 4** **D. ± 2**

Coordinates of the points are

A. $(-4, 4)$ and $(4, 4)$ **B. $(-4, -4)$ and $(4, 4)$**

C. $(4, -4)$ and $(-4, 4)$ **D. $(2, -2)$ and $(-2, 2)$**