

**In Exercises 91–100, find all points (if any) of horizontal and vertical tangency to the curve. Use a graphing utility to confirm your results.**

91.  $x = 1 - t, \quad y = t^2$

92.  $x = t + 1, \quad y = t^2 + 3t$

93.  $x = 1 - t, \quad y = t^3 - 3t$

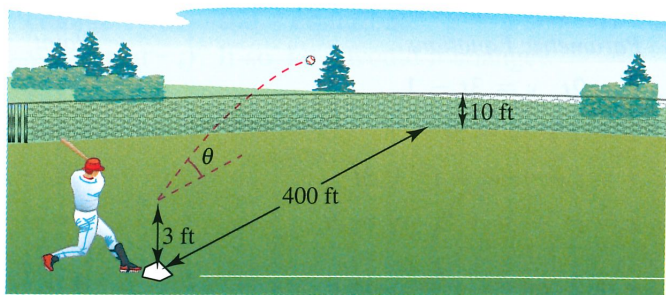
94.  $x = t^2 - t + 2, \quad y = t^3 - 3t$



**101. Archery** An archer releases an arrow from a bow 5 feet above the ground. The arrow leaves the bow at an angle of  $10^\circ$  with the horizontal and at an initial speed of 240 feet per second.

- Write a set of parametric equations for the path of the arrow.
- Assuming the ground is level, find the distance the arrow travels before it hits the ground. (Ignore air resistance.)
- Graph the path of the arrow and approximate its maximum height. Verify your result analytically.
- Find the time the arrow is in the air.

**102. Baseball** The center field fence in a ballpark is 10 feet high and 400 feet from home plate. The baseball is hit 3 feet above the ground. It leaves the bat at an angle of  $\theta$  degrees with the horizontal at a speed of 100 miles per hour (see figure).



- Write a set of parametric equations for the path of the baseball.
- Use a graphing utility to sketch the path of the baseball if  $\theta = 15^\circ$ . Is the hit a home run?
- Use a graphing utility to sketch the path of the baseball if  $\theta = 23^\circ$ . Is the hit a home run?
- Find the minimum angle required for the hit to be a home run.

**103. Projectile Motion** The position function for the path of a projectile is modeled by the parametric equations

$$x = (v_0 \cos \theta)t$$

and

$$y = h + (v_0 \sin \theta)t - 16t^2,$$



**104. Path of a Projectile** The path of a projectile is given by the rectangular equation

$$y = 7 + x - 0.02x^2.$$

- Use the result of Exercise 103 to find  $h$ ,  $v_0$ , and  $\theta$ . Find the parametric equations of the path.
- Use a graphing utility to graph the rectangular equation for the path of the projectile. Confirm your answer in part (a) by sketching the curve represented by the parametric equations.
- Use a graphing utility to approximate the maximum height of the projectile and its range.

**True or False?** In Exercises 105–108, determine whether the statement is true or false. If it is false, explain why or give an example that shows it is false.

**105.** The sets of parametric equations

$$x = t$$

$$y = t^2 + 1$$

and

$$x = 3t$$

$$y = 9t^2 + 1$$

have the same rectangular equation.

**106.** The graph of the parametric equations  $x = t^2$  and  $y = t^2$  is the line  $y = x$ .

**107.** Only one set of parametric equations can represent the line  $y = 3 - 2x$ .

**108.** The graph of the set of parametric equations

$$x = 2 \tan t$$

$$y = \sec t$$

is a hyperbola.