

$$11. y = -6 \sin 3x$$

$$12. f(x) = 4 \cos(-5x)$$

$$13. \frac{d}{dx}(\cos^4 7x)$$

$$14. \frac{d}{dx}(\sin^9 13x)$$

$$15. f(x) = 24 \sin^{5/3} 4x$$

$$16. f(x) = -100 \sin^{6/5}(-9x)$$

$$17. f(x) = (5x + 3)^7$$

$$18. f(x) = (x^2 + 8)^9$$

$$19. y = (4x^3 - 7)^{-6}$$

$$20. y = (x^2 + 3x - 7)^{-5}$$

$$21. y = [\cos(x^2 + 3)]^{100}$$

$$22. y = [\cos(5x + 3)^4]^5$$

$$23. \text{ Find } \frac{d^2 y}{dx^2} \text{ if } y = 4 \cos 5x.$$

$$24. \text{ Find } \frac{d^2 y}{dx^2} \text{ if } y = 7 \sin(2x + 5).$$

$$25. \text{ If } f'(x) = \cos 5x, \text{ find an antiderivative } f(x).$$

$$26. \text{ If } f'(x) = 10 \sin 2x, \text{ find an antiderivative } f(x).$$

27. *Graphical Verification Problem:* For  $f(x) = 5 \cos 0.2x$ , plot the graph of function  $f$ . Where  $x = 3$ , plot a line on the graph with slope equal to  $f'(3)$ . Is the line really tangent to the graph?

28. *Beanstalk Problem:* Jack's beanstalk grows in spurts. Its height,  $y$ , in feet above the ground, at time  $t$ , in hours since he planted it, is given by

$$y = 7 \sin \pi t + 12t^{1.2}$$

Write an equation for  $dy/dt$ . Plot the graph of  $y$  and the velocity graph on the same screen. Use a window with  $[0, 10]$  for  $t$ . Do there appear to be times when the beanstalk is shrinking? Justify your answer.

29. *Balloon Volume Problem:* A spherical balloon is being inflated with air (see Figure 3-7c). The volume of the sphere depends on the radius, and the radius depends on time. Thus, the volume is a composite function of time.

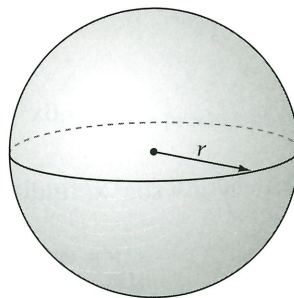


Figure 3-7c

- The volume of a sphere is  $V = (4\pi/3)r^3$ , where  $r$  is the radius in cm. Find an equation for  $dV/dr$ . What are the units of  $dV/dr$ ?
  - At time  $t = 0$ , the radius is 10 cm. If  $r$  increases at 6 cm/min, write  $r$  as a function of  $t$ .
  - Find an equation for  $dr/dt$ . Surprising? What are the units of  $dr/dt$ ?
  - By appropriate use of the chain rule, find  $dV/dt$  when  $t = 5$  min. Based on the units of  $dV/dr$  and  $dr/dt$ , explain why the units of  $dV/dt$  are  $\text{cm}^3/\text{min}$ .
  - Find  $dV/dt$  directly by substituting  $r$  from part b into the equation for  $V$ . Show that you get the same answer you did in part d for  $dV/dt$  when  $t = 5$ .
30.  *$\Delta u$  and  $\Delta x$  Problem:* The derivation of the chain rule states that if  $u$  is a continuous function of  $x$ , then  $\Delta x \rightarrow 0$  implies  $\Delta u \rightarrow 0$ .
- Sketch a graph showing that this may not be true if  $u$  has a step discontinuity.
  - Sketch a graph showing why this is true if  $u$  is continuous.