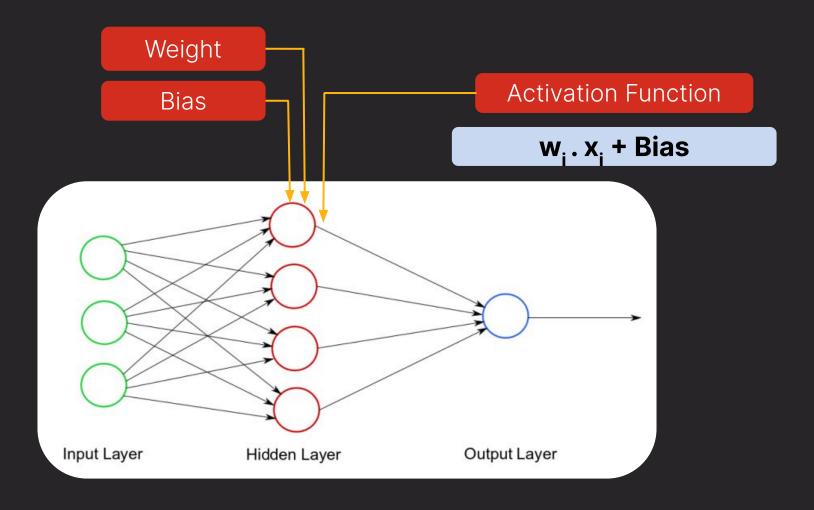




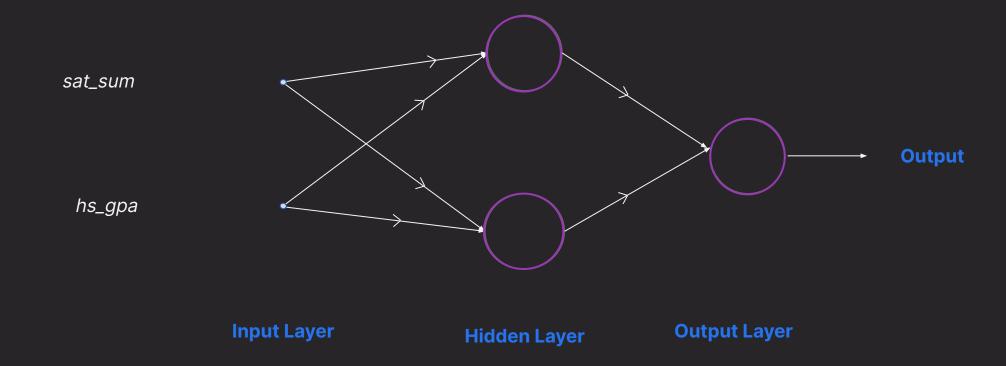
#### Introduction

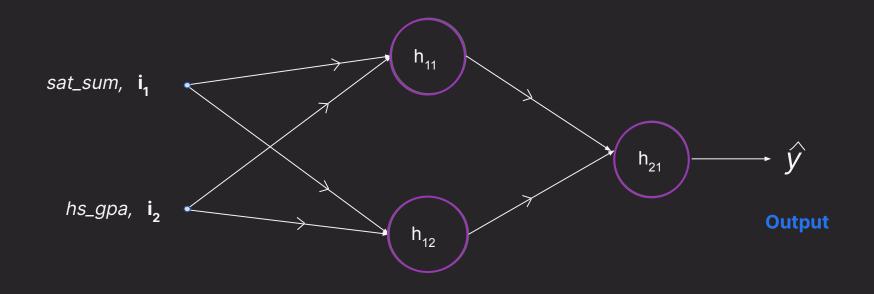




#### Predict 1st year college grades from high school SAT and GPA scores.

sat_sum	hs_gpa	fy_gpa	Targe
727	3.40	3.18	
722	4.00	3.33	
716	3.75	3.25	

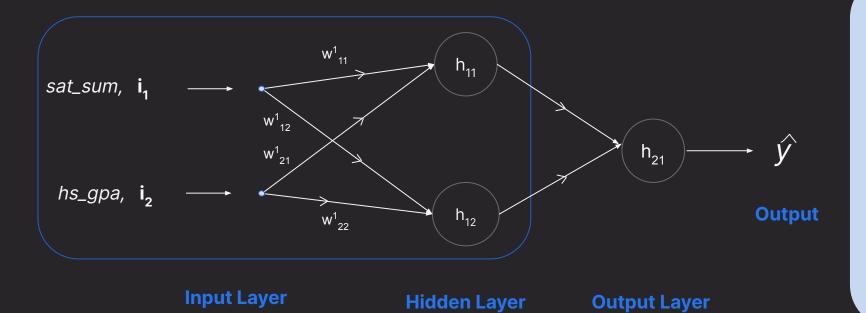




**Input Layer** 

**Hidden Layer** 

**Output Layer** 



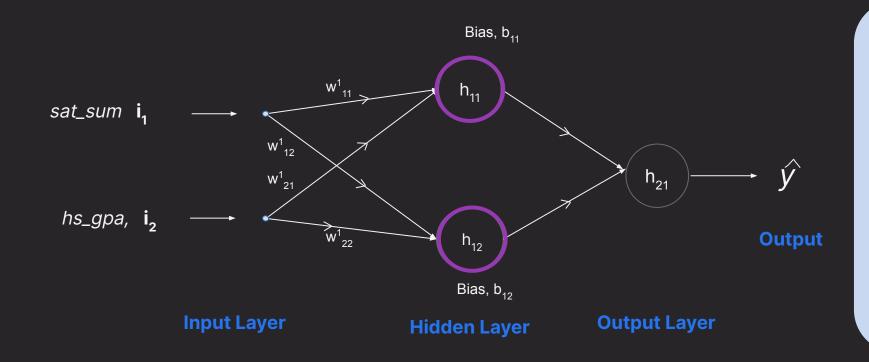
Nodes in Input and Hidden layer = 2 Each

Connections = 2\*2 = 4

4 Weights

 $\mathbf{w_{11}^1}, \mathbf{w_{12}^1}, \mathbf{w_{21}^1}, \mathbf{w_{22}^1}$ 





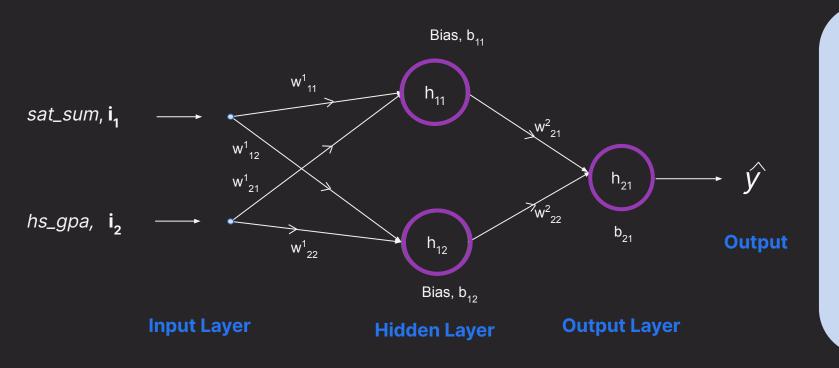
Connections = 2\*2 = 4

Nodes = 2

Biases = 4 + 2

6 Dependent Parameters

 $\mathbf{w_{11}^{1}}, \mathbf{w_{12}^{1}}, \mathbf{w_{21}^{1}}, \mathbf{w_{22}^{1}}, \mathbf{b_{11}^{1}}, \mathbf{b_{12}^{1}}$ 



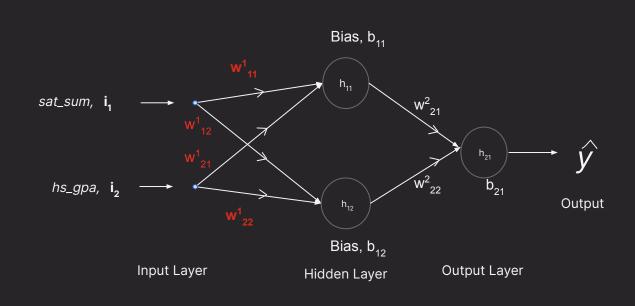
6 Dependent Parameters
+

**3 New Parameters** 

**9 Dependent Parameters** 



#### 1. Calculate the weighted sum of the inputs



$$\mathbf{I} = \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} \qquad \mathbf{b} = \begin{bmatrix} b_{11} \\ b_{12} \end{bmatrix}$$

$$\mathbf{w}_1 = \begin{bmatrix} \mathbf{w}^1_{11} \\ \mathbf{w}^1_{11} \end{bmatrix}$$

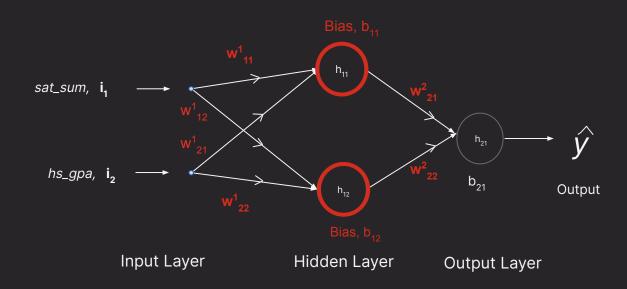
$$\mathbf{b} = \begin{bmatrix} b_{11} \\ b_{12} \end{bmatrix}$$

$$\mathbf{w_2} = \left[ \begin{array}{c} \mathbf{w^1}_{21} \\ \mathbf{w^1}_{22} \end{array} \right]$$

$$\mathbf{w} = \begin{bmatrix} \mathbf{w}_{11} & \mathbf{w}_{21} \\ \mathbf{w}_{12} & \mathbf{w}_{22} \end{bmatrix}$$



## 2. Apply activation function to get outputs

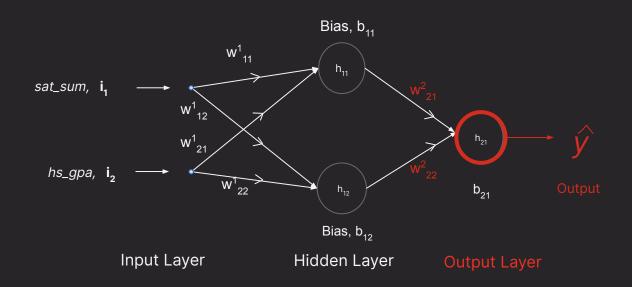


$$O_1 = Sigmoid (w_{11}^1 * i_1 + w_{21}^1 * i_2 + b_{11})$$

$$O_2 = Sigmoid (w_{12}^1 * i_1 + w_{22}^1 * i_2 + b_{12})$$



#### 3. Outputs act as input for the next layer

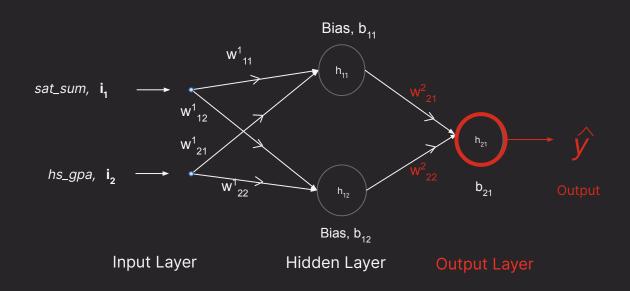


$$O_1 = Sigmoid (w_{11}^1 * i_1 + w_{21}^1 * i_2 + b_{11})$$

$$O_2 = Sigmoid (w_{12}^1 * i_1 + w_{22}^1 * i_2 + b_{12})$$



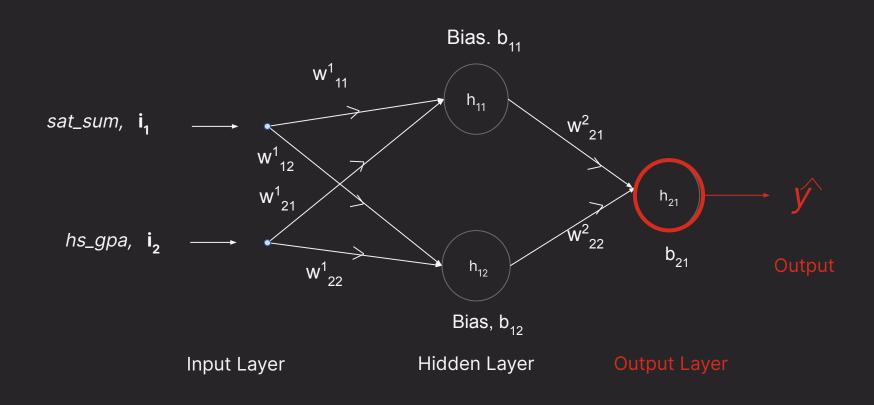
#### 4. Calculate weighted sum of outputs



$$W_{21}^2 * O_1 + W_{22}^2 * O_2 + b_{21}$$



### 5. Apply Activation Function to get Output



Y = Activation Function 
$$(W_{21}^2 * O_1 + W_{22}^2 * O_2 + b_{21})$$



# **Activation Function of Last Layer: Regression Problems**

$$Y = Activation Function (W_{21}^2 * O_1 + W_{22}^2 * O_2 + b_{21})$$

**Linear Activation Function** 



Regression Problems with negative output

**Example: Temperature Prediction** 

**ReLu Activation Function** 



Regression Problems with positive output

Example: House price Prediction



#### **Activation Function of Last Layer: Classification Problems**

$$Y = Activation Function (W_{21}^2 * O_1 + W_{22}^2 * O_2 + b_{21})$$

Sigmoid Function

**Softmax Function** 





Multi Classification Problems