



$$m \frac{dv}{dt} = F_{\text{net}} = F - F_d = F - r v$$

$$\text{or, } m \frac{dv}{dt} + r v = F$$

Given at  $t=0$ ,  $F=0$  and  $v=v_0$

$$\Rightarrow m \frac{dv}{dt} = -r v$$

$$\text{or } \frac{dv}{v} = -\frac{r}{m} dt$$

$$\Rightarrow \int_{v_0}^v \frac{dv}{v} = -\frac{r}{m} \int_0^t dt$$

$$[\ln v]_{v_0}^v = -\frac{r}{m} [t]_0^t$$

$$\ln \frac{v}{v_0} = -\frac{r}{m} t$$

$$\Rightarrow \boxed{v = v_0 e^{-\frac{r}{m} t} = v_0 e^{-t/\tau}}$$

$$\text{where } \tau = \frac{m}{r}$$

$$\text{Now } \tau = \frac{m}{r} = \frac{2 \times 5 \times 10^{-3} \times 0.5 \times 10^{-6} \times 0.5 \times 10^{-6}}{3 \times 10^{-3} \times 9 \times 10^{-3}} = \frac{2}{9} \frac{\rho r^2}{\eta}$$

$$\text{for bacterium } \tau = \frac{2 \times 5 \times 10^{-3} \times 0.5 \times 10^{-6} \times 0.5 \times 10^{-6}}{9 \times 10^{-3}} = \frac{2.5 \times 10^{-15}}{9 \times 10^{-3}} = \frac{2.5}{9} \times 10^{-12} \text{ s} \approx 0.28 \mu\text{s}$$

$$\text{for pufferfish } \tau = \frac{2 \times 5 \times 10^{-3} \times 0.5 \times 10^{-3} \times 0.5 \times 10^{-3}}{9 \times 10^{-3}} = \frac{2.5 \times 10^{-9}}{9 \times 10^{-3}} = \frac{2.5}{9} \times 10^{-6} \text{ s} \approx 0.28 \text{ s}$$

Distance travelled before stopping is given by

$$x = \int_0^\infty v dt = v_0 \int_0^\infty e^{-t/\tau} dt = [-v_0 \tau e^{-t/\tau}]_0^\infty = -v_0 \tau e^{-\infty} - (-v_0 \tau e^{-0}) = v_0 \tau$$

$$\therefore \text{stopping distance for bacterium} = 10 \times 10^{-6} \frac{\text{m}}{\text{s}} \times 0.28 \times 10^{-6} \text{ s} = 2.8 \times 10^{-12} \text{ m} \\ = 0.028 \times 10^{-10} \text{ m} \approx 0.028 \text{ \AA}$$

$$\text{stopping distance for pufferfish} = 10 \times 10^{-3} \frac{\text{m}}{\text{s}} \times 0.28 = 2.8 \times 10^{-3} \text{ m} \\ = 2.8 \text{ mm}$$