

$$\Delta x = \frac{L}{2}$$

$$\text{and, } \Delta p \geq \frac{h}{a}$$

The momentum p must be of this order, so

$$K = \frac{p^2}{2m} \sim \frac{(\Delta p)^2}{2m}$$

or

$$K \gtrsim \frac{h^2}{2ma^2}$$

$$\therefore K_{\min} = \frac{h^2}{2ma^2} \approx 4 \text{ eV}$$