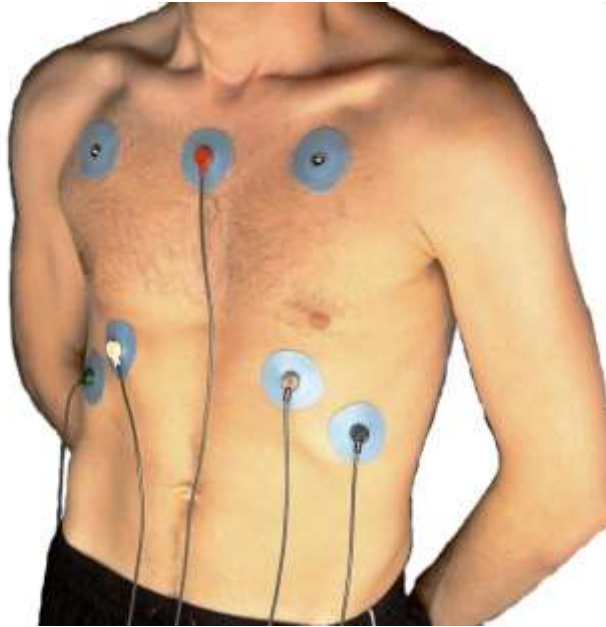


# Looking into the body non-invasively.

A [medical procedure](#) is defined as *non-invasive* when no break in the skin is created and there is no contact with the mucosa, or skin break, or internal body cavity beyond a natural or artificial body orifice. : [Non-invasive procedure - Wikipedia](#)



Biopotential: electrical signal



Biopotential: electrical signal



Sound signal

[14101766166\\_c78919676e\\_b.jpg](#)  
(850×760) (staticflickr.com)

[EEG\\_cap.jpg \(289×423\) \(wikimedia.org\)](#)

[Finding the Error Activity: Infant Apical Pulse – Answer – Vital Sign Measurement Across the Lifespan – 1st Canadian edition \(pressbooks.pub\)](#)

# Looking into the body non-invasively.

[https://en.wikipedia.org/wiki/CT\\_scan](https://en.wikipedia.org/wiki/CT_scan)

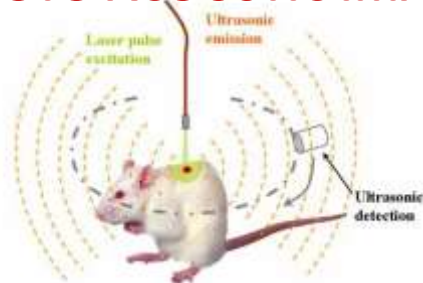


**NIR IMAGING**



[https://en.wikipedia.org/wiki/Photoacoustic\\_imaging](https://en.wikipedia.org/wiki/Photoacoustic_imaging)

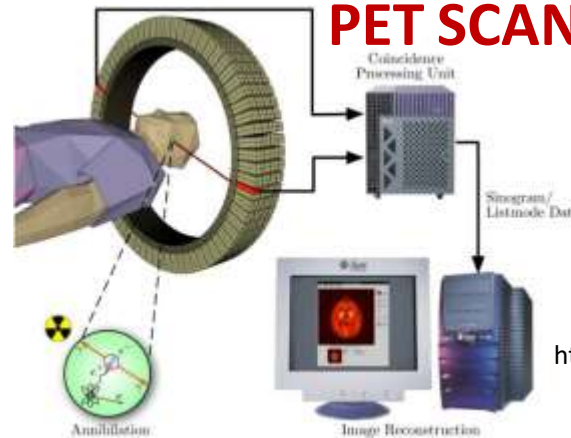
**PHOTO ACOUSTIC IMAGING**



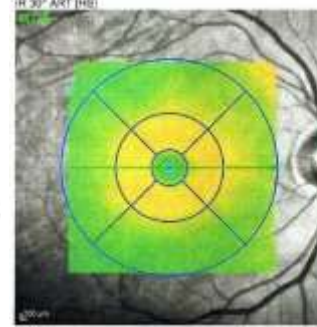
<https://en.wikipedia.org/wiki/Ultrasound>



[https://en.wikipedia.org/wiki/Positron\\_emission\\_tomography](https://en.wikipedia.org/wiki/Positron_emission_tomography)



**PET SCAN**



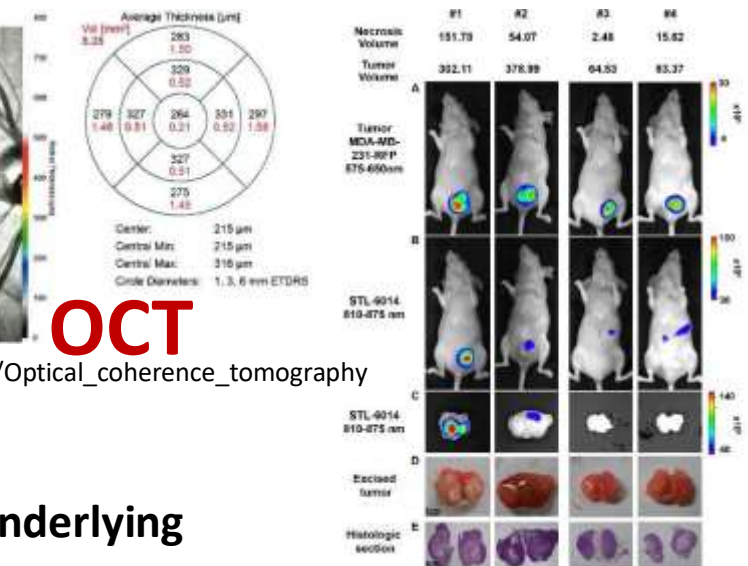
[https://en.wikipedia.org/wiki/Optical\\_coherence\\_tomography](https://en.wikipedia.org/wiki/Optical_coherence_tomography)

**OCT**

[https://en.wikipedia.org/wiki/Magnetic\\_resonance\\_imaging](https://en.wikipedia.org/wiki/Magnetic_resonance_imaging)



**MRI**



**FLOURESCENCE IMAGING**

[https://commons.wikimedia.org/wiki/File:Fluorescence\\_Imaging\\_07.jpg](https://commons.wikimedia.org/wiki/File:Fluorescence_Imaging_07.jpg)

- Different imaging modalities have different underlying physical principles.
- Look for common features of each imaging modalities.
- A common platform or theory to many imaging modalities.

Hari M Varma, BSBE, IIT Bombay (harivarma@iitb.ac.in)

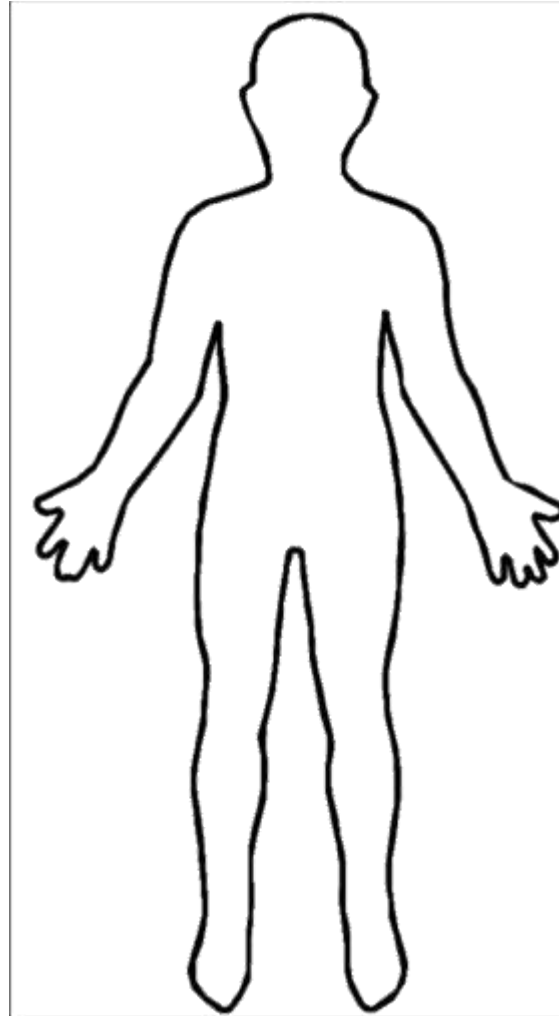
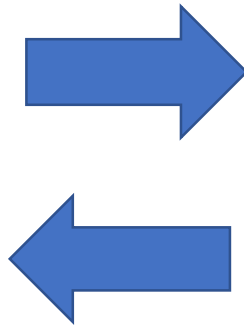
# Looking into the body non-invasively.

Measure externally irradiated Probing signals after interacting with the body.

Eg: X Ray, CT, Ultrasound  
MRI, NIRS, OCT etc



<https://en.wikipedia.org/wiki/Ultrasound>



[human body wiki - Bing images](#)

Hari M Varma, BSBE, IIT Bombay (harivarma@iitb.ac.in)

Measure Bio Signals emanating from the body:

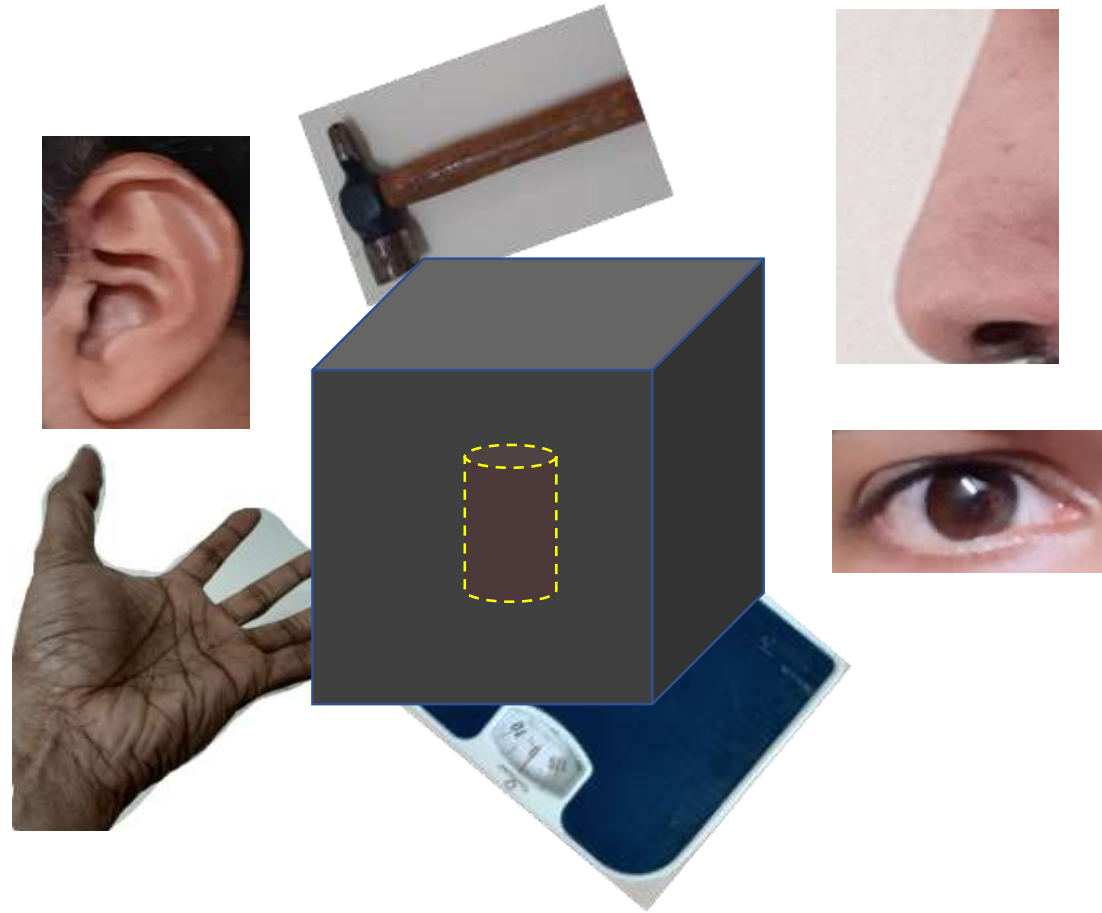
Eg: ECG, EEG, EMG, EKG,  
Phonocardiography, body temperature  
etc.



[Finding the Error Activity: Infant Apical Pulse – Answer – Vital Sign Measurement Across the Lifespan – 1st Canadian edition \(pressbooks.pub\)](#)

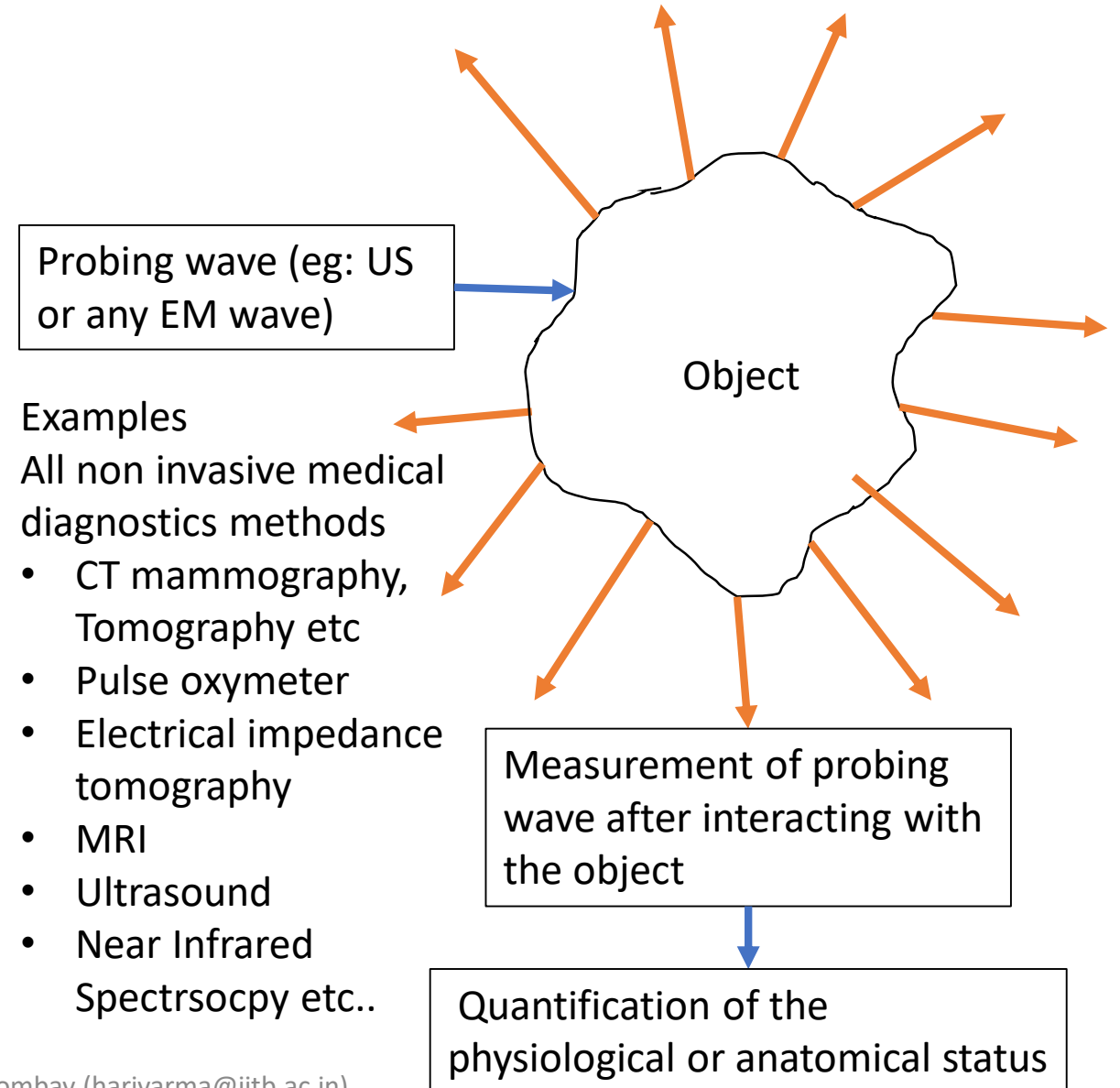
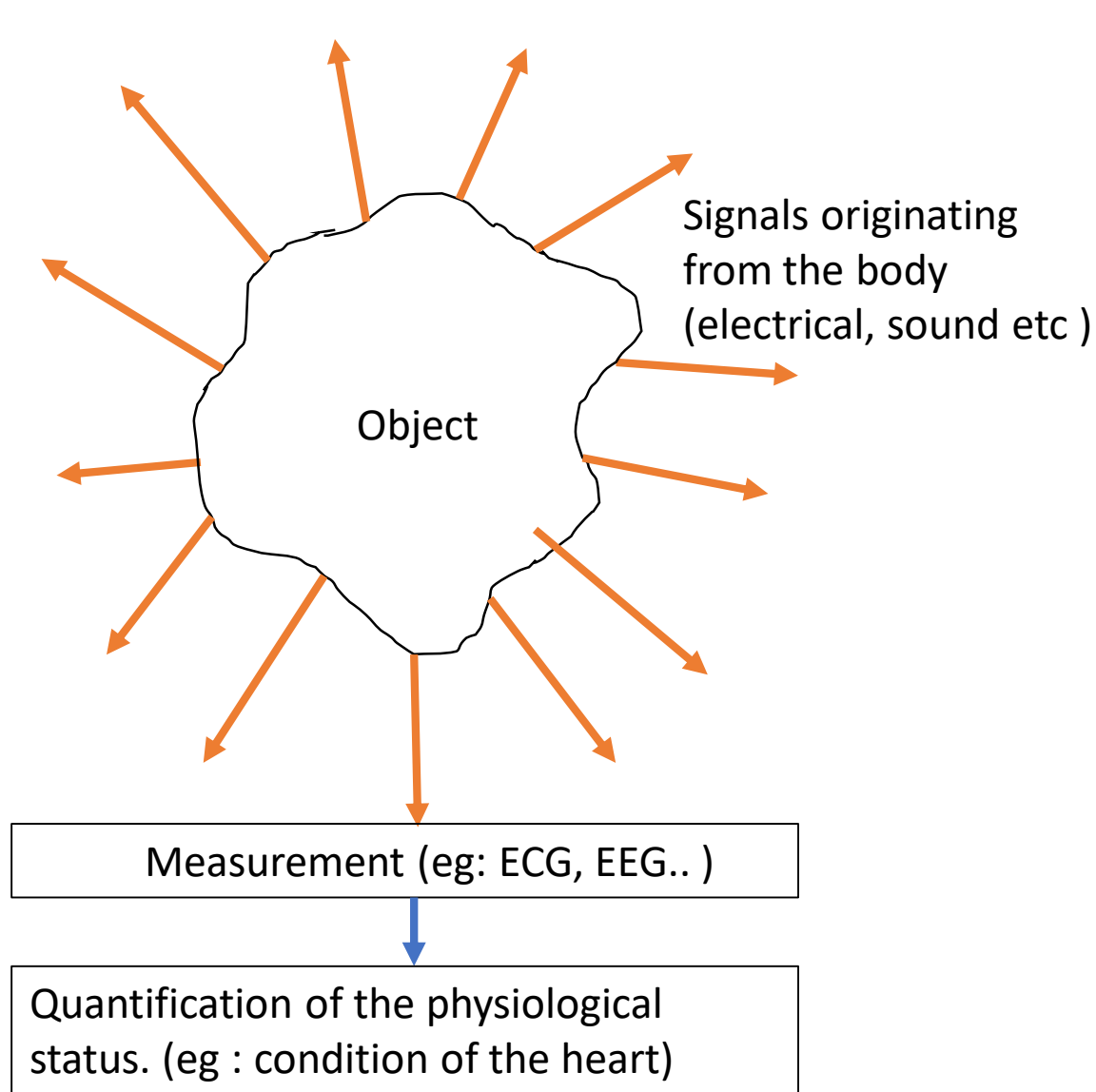


# Looking at the body : A black box approach



## A BLACK BOX WITH A HIDDEN OBJECT

# Signals originating from body and signals created by probing waves





# Forward and inverse problem

## Signals from the body

### Forward Model/Problem

A physical/mathematical model explaining how signal is originated and then propagated through the object.

Eg: how Neuron action potential is originated and then manifest as EEG at the body surface

### Measurement Model

A physically realizable measurement of the signals from the object at appropriate places in the surface of the body.

### Inverse Model/Problem

Given the forward model and the measurement model, find the object property.

(eg: physiological status of the heart or functional activation studies using EEG etc. )

## Probing signals coming out from the body after interaction

### Forward Model/Problem

A physical/mathematical model explaining how probing wave interacts with the object.

Eg: how X-rays interacts with human body (Beer Lamberts Law)

### Measurement Model

A physically realizable measurement of the probing wave after interacting with the object.

### Inverse Model/Problem

Given the forward model and the measurement model, find the object property. (eg: the absorption coefficient of the tissue as a 3D map in CT scan. )

# Origin of signals from the body : the forward model.

- Origin of Bio electric potentials : membrane potential and action potential
- Neuron : signalling and origin of EEG
- Cardiac system : working of heart and origin of ECG.
- Emphasis on the engineering concepts in above phenomenon's :



# How body interacts with probing signals applied externally (non- invasively) : imaging problem

- X ray propagation inside the human body : Beers Lamberts Law.
- Concept of computed tomography to create three dimensional anatomical images.
- Image reconstruction method (INVERSE PROBLEMS): simple back projection and its implementation in Matlab.
- Concept of Fourier Transform
- Quick introduction to Magnetic Resonance Imaging.
- Why Fourier Transforms are indispensable tool for CT and MRI ?

# INTRODUCTION TO IMAGING USING IMAGES



HARIDWAR

# DIFFERENT IMAGING MODALITIES

[https://en.wikipedia.org/wiki/CT\\_scan](https://en.wikipedia.org/wiki/CT_scan)



**CT SCAN**

<https://en.wikipedia.org/wiki/Ultrasound>



**ULTRASOUND**

[https://en.wikipedia.org/wiki/Magnetic\\_resonance\\_imaging](https://en.wikipedia.org/wiki/Magnetic_resonance_imaging)



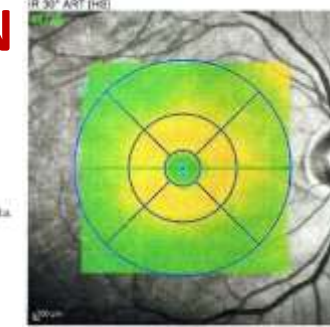
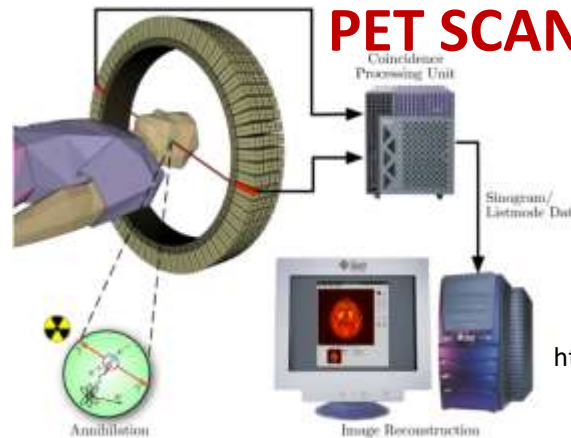
**MRI**

**NIR IMAGING**



[https://www.wikiwand.com/en/Near-infrared\\_spectroscopy](https://www.wikiwand.com/en/Near-infrared_spectroscopy)

[https://en.wikipedia.org/wiki/Positron\\_emission\\_tomography](https://en.wikipedia.org/wiki/Positron_emission_tomography)

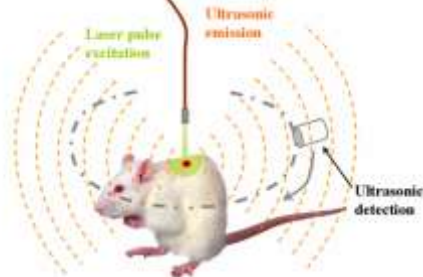


**OCT**

[https://en.wikipedia.org/wiki/Optical\\_coherence\\_tomography](https://en.wikipedia.org/wiki/Optical_coherence_tomography)

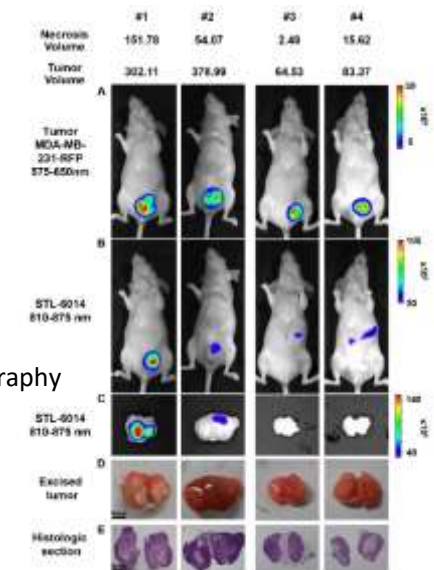
[https://en.wikipedia.org/wiki/Photoacoustic\\_imaging](https://en.wikipedia.org/wiki/Photoacoustic_imaging)

**PHOTO ACOUSTIC IMAGING**



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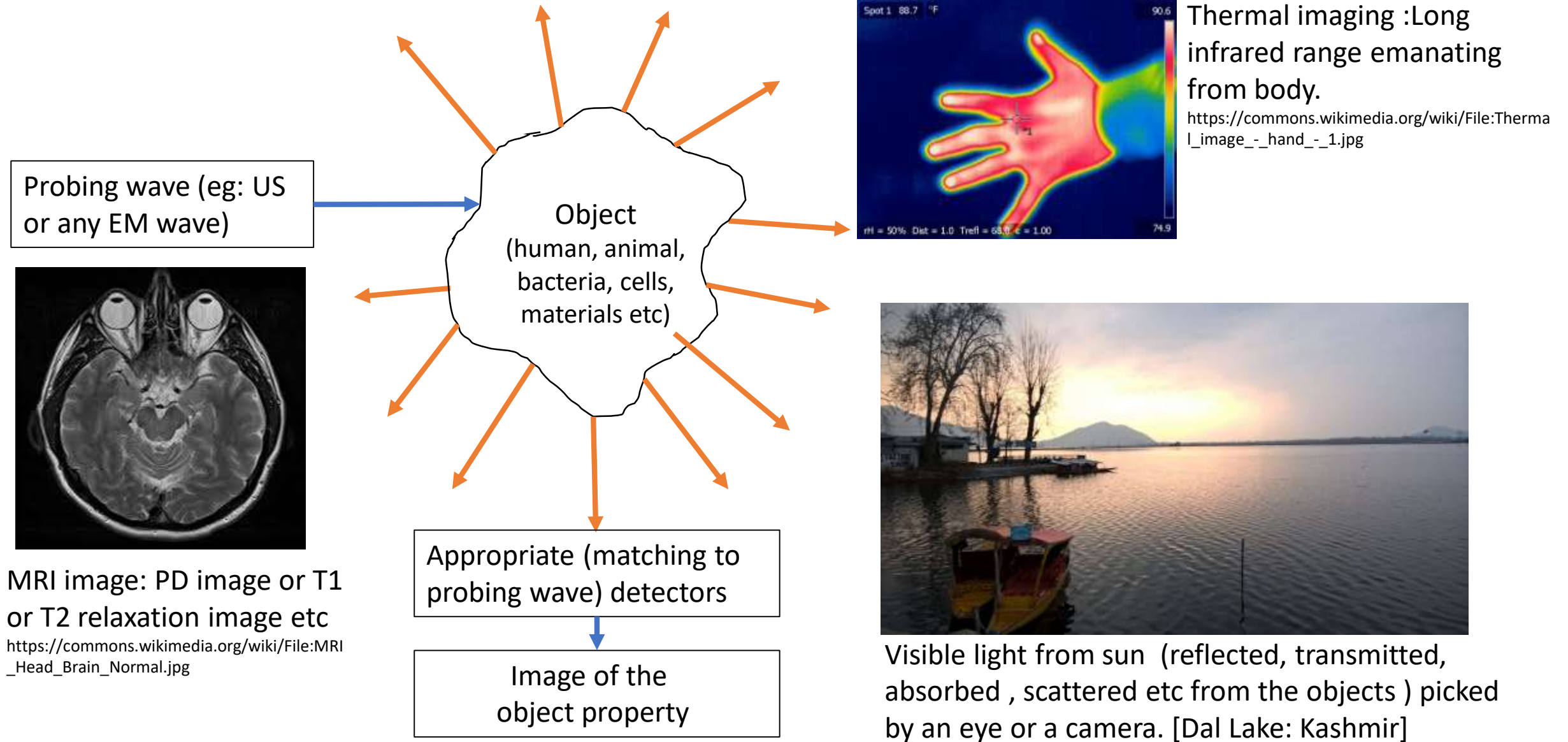
Hari M Varma, BSBE, IIT Bombay (harivarma@iitb.ac.in)



**FLOURESCENCE IMAGING**

[https://commons.wikimedia.org/wiki/File:Fluorescence\\_Imaging\\_07.jpg](https://commons.wikimedia.org/wiki/File:Fluorescence_Imaging_07.jpg)

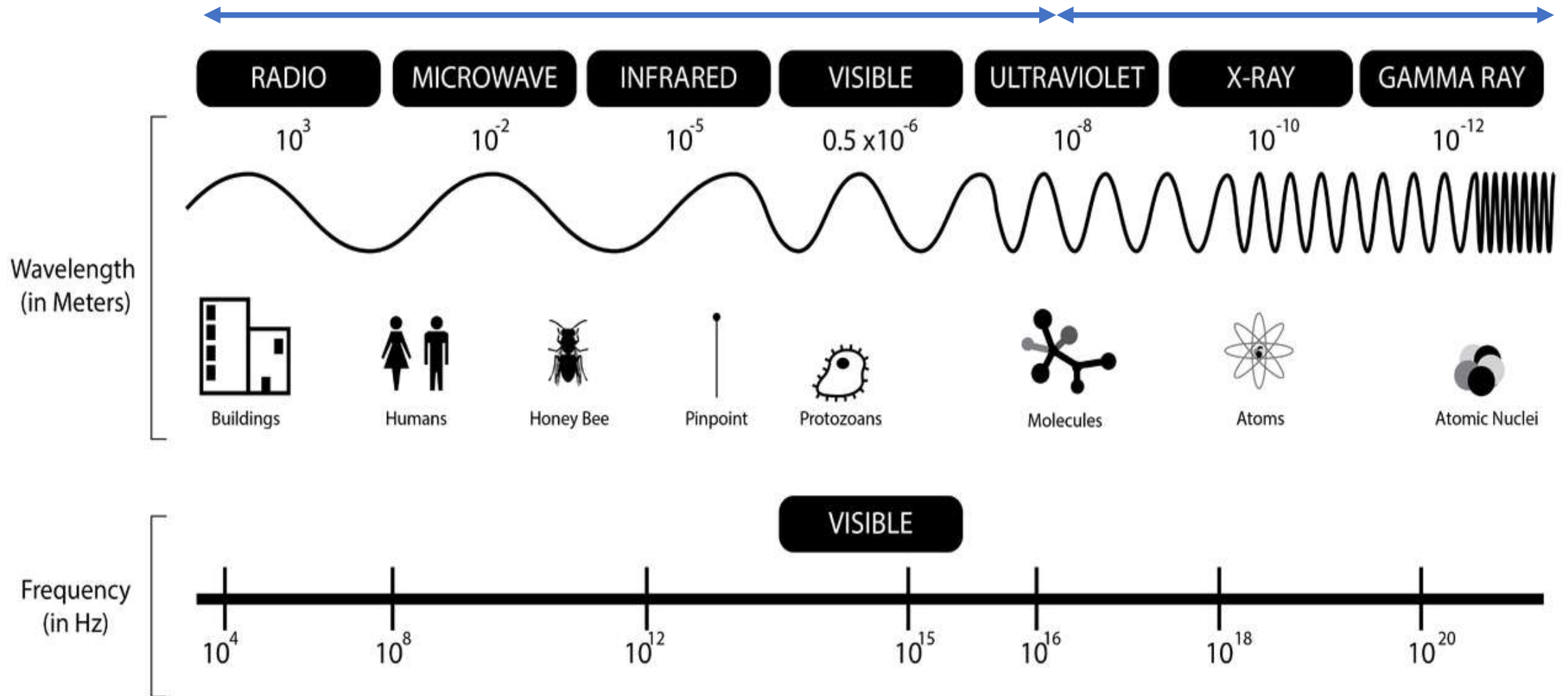
# What is an Image ???



# ELECTROMAGNETIC SPECTRUM

NON IONIZING

IONIZING



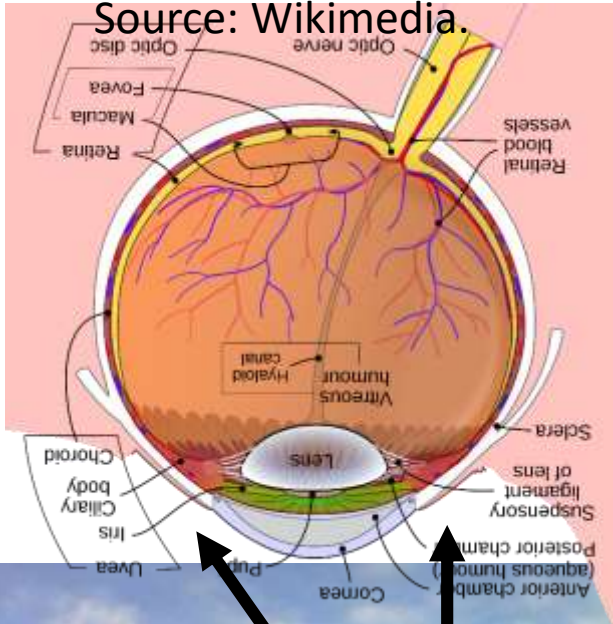
Source: [https://commons.wikimedia.org/wiki/File:BW\\_EM\\_spectrum.png](https://commons.wikimedia.org/wiki/File:BW_EM_spectrum.png)

Hari M Varma, BSBE, IIT Bombay (harivarma@iitb.ac.in)



# IMAGE , IMAGING AND IMAGE PROCESSING

Source: Wikimedia.



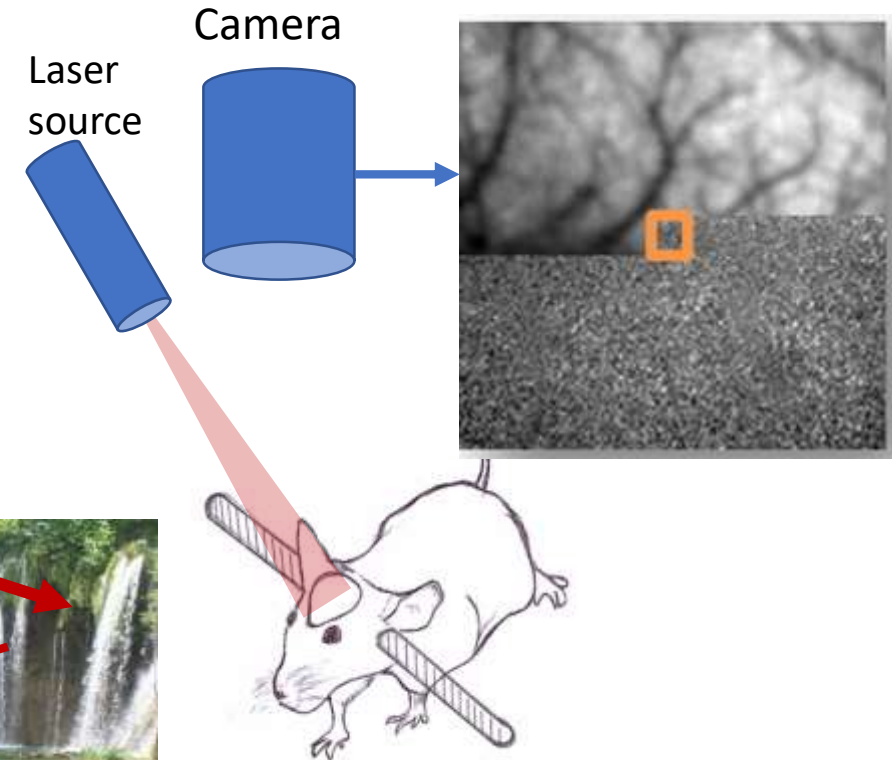
<https://en.wikipedia.org/wiki/Eye>



Helsinki, Finland



Plitvice National Park, Croatia

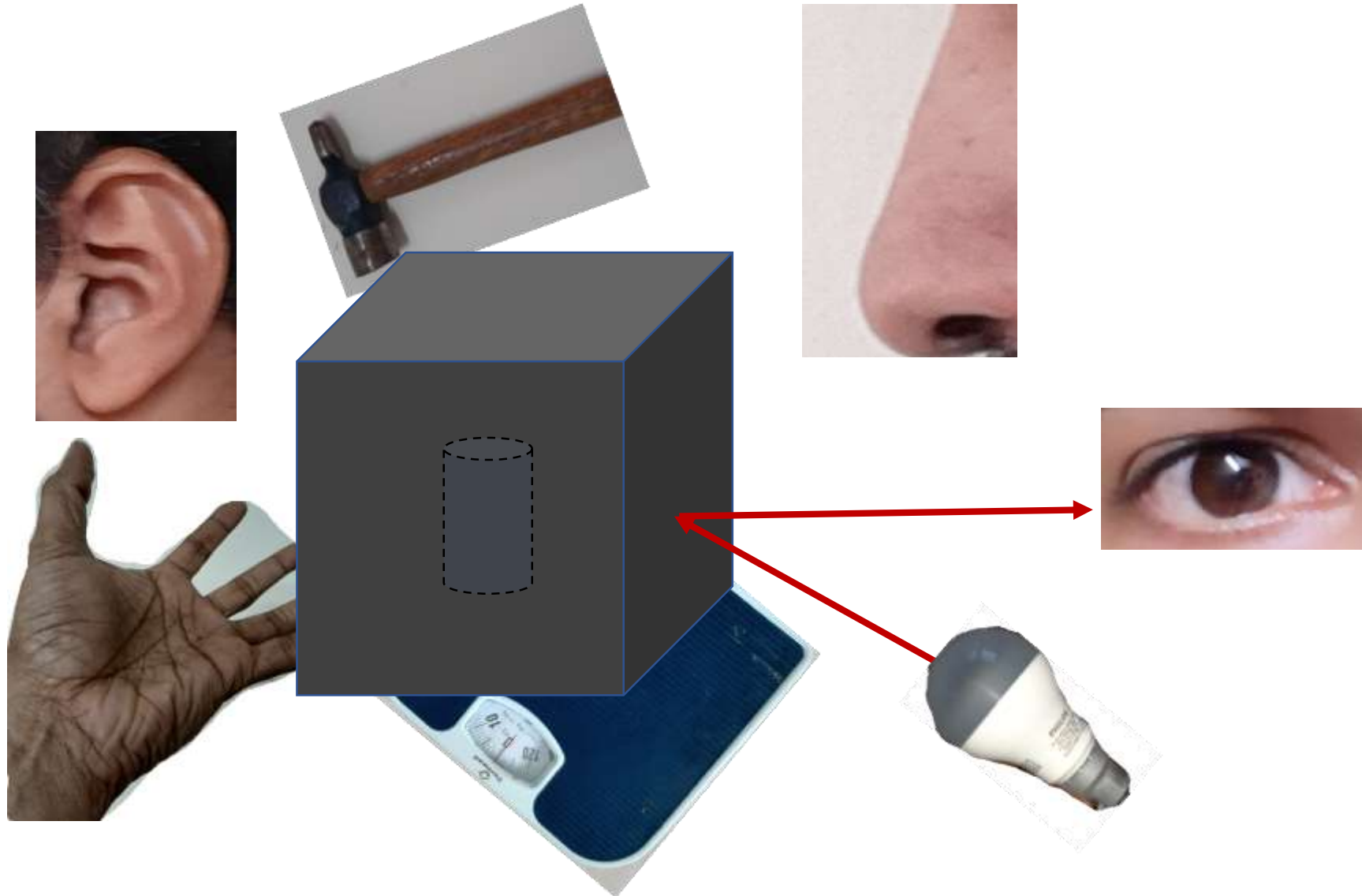


D. Briers et. al., J. Biomed. Opt. 18, 066018 (2013).  
A. K. Dunn, Ann. Biomed. Engg. 40, 367–377 (2012).  
R. Bandyopadhyay et al, Rev. sci. instrum. 76, 2005

Eg: Laser Speckle Imaging



# NEED OF A COMMON THEORY

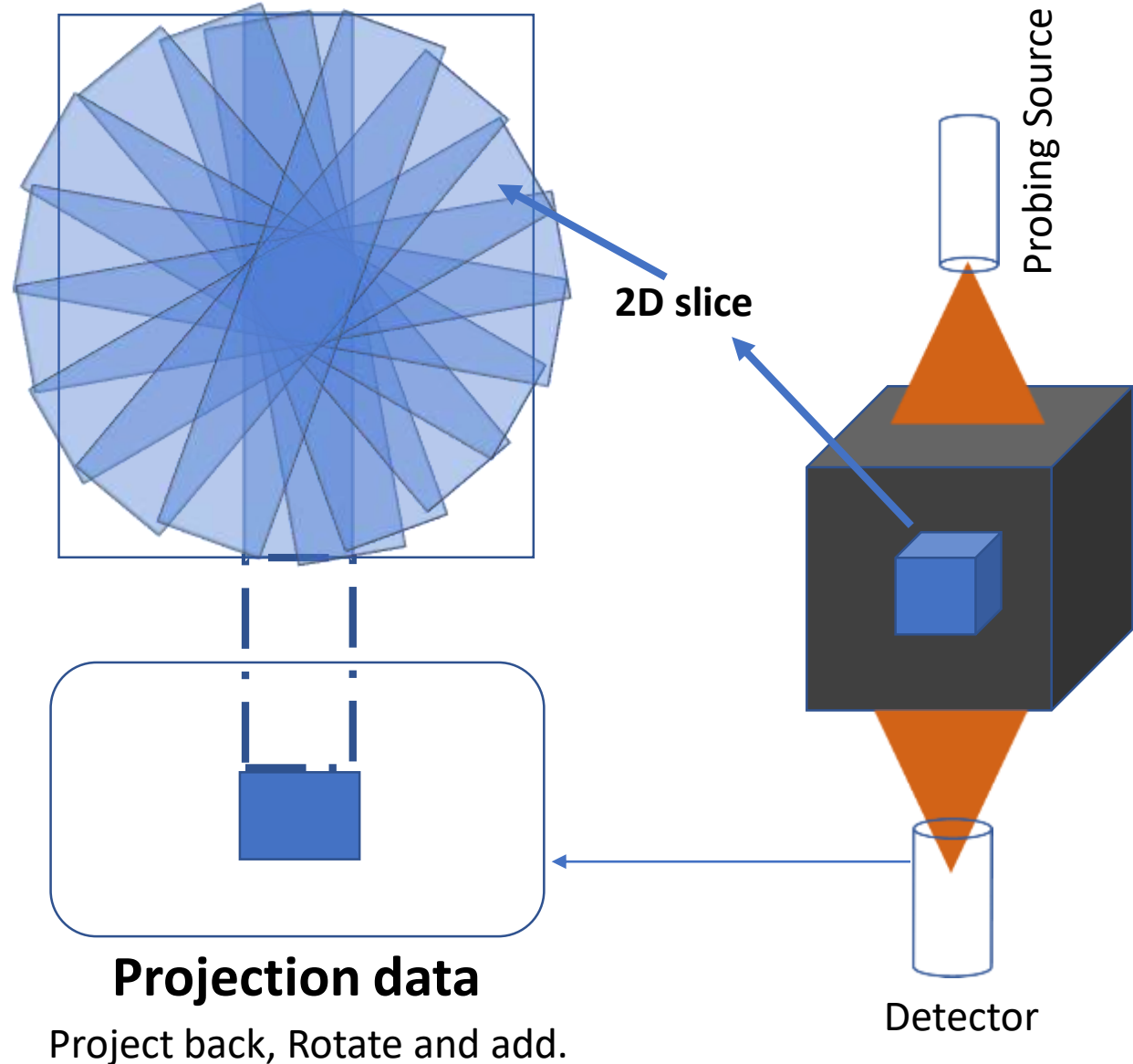


# HOW TO TACKLE THIS PROBLEM

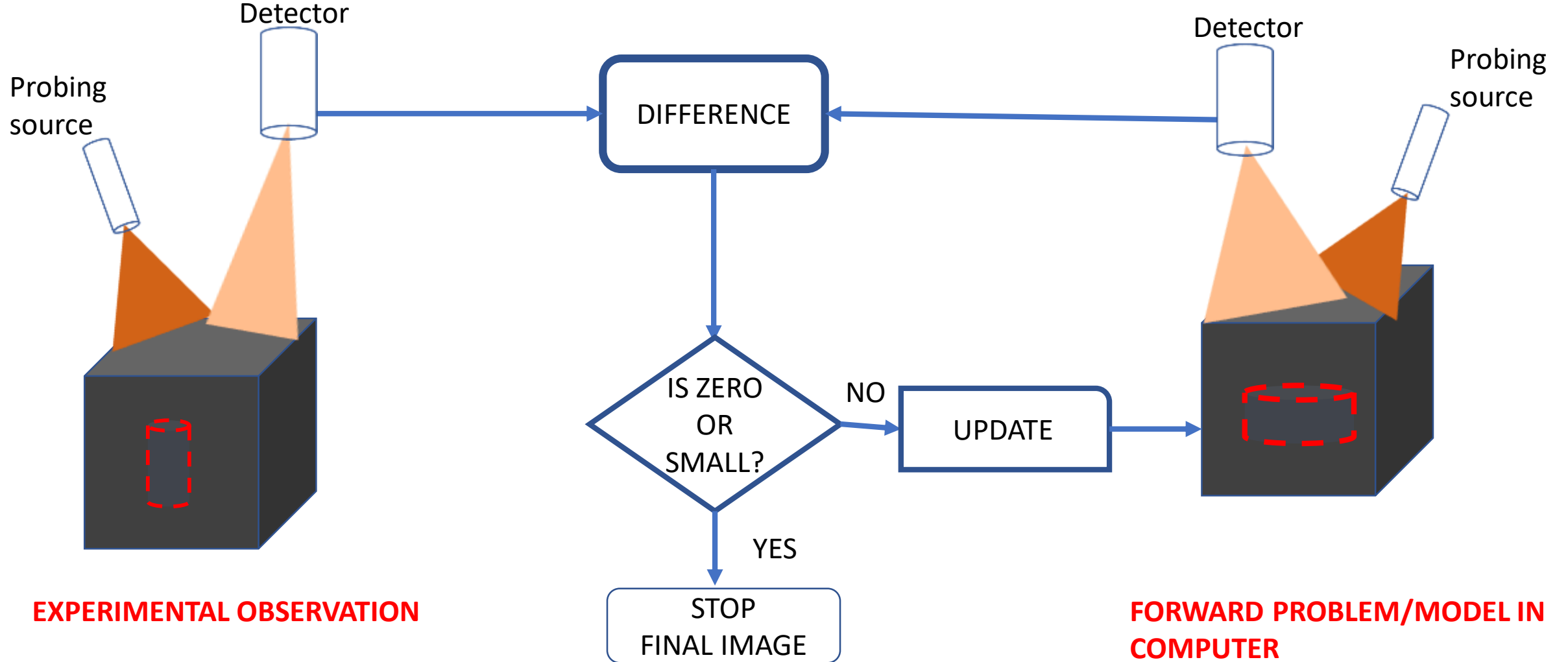


**SHADOW OF THE HIDDEN OBJECT:  
CAN YOU IDENTIFY PERSON FROM THE  
SHADOW?**

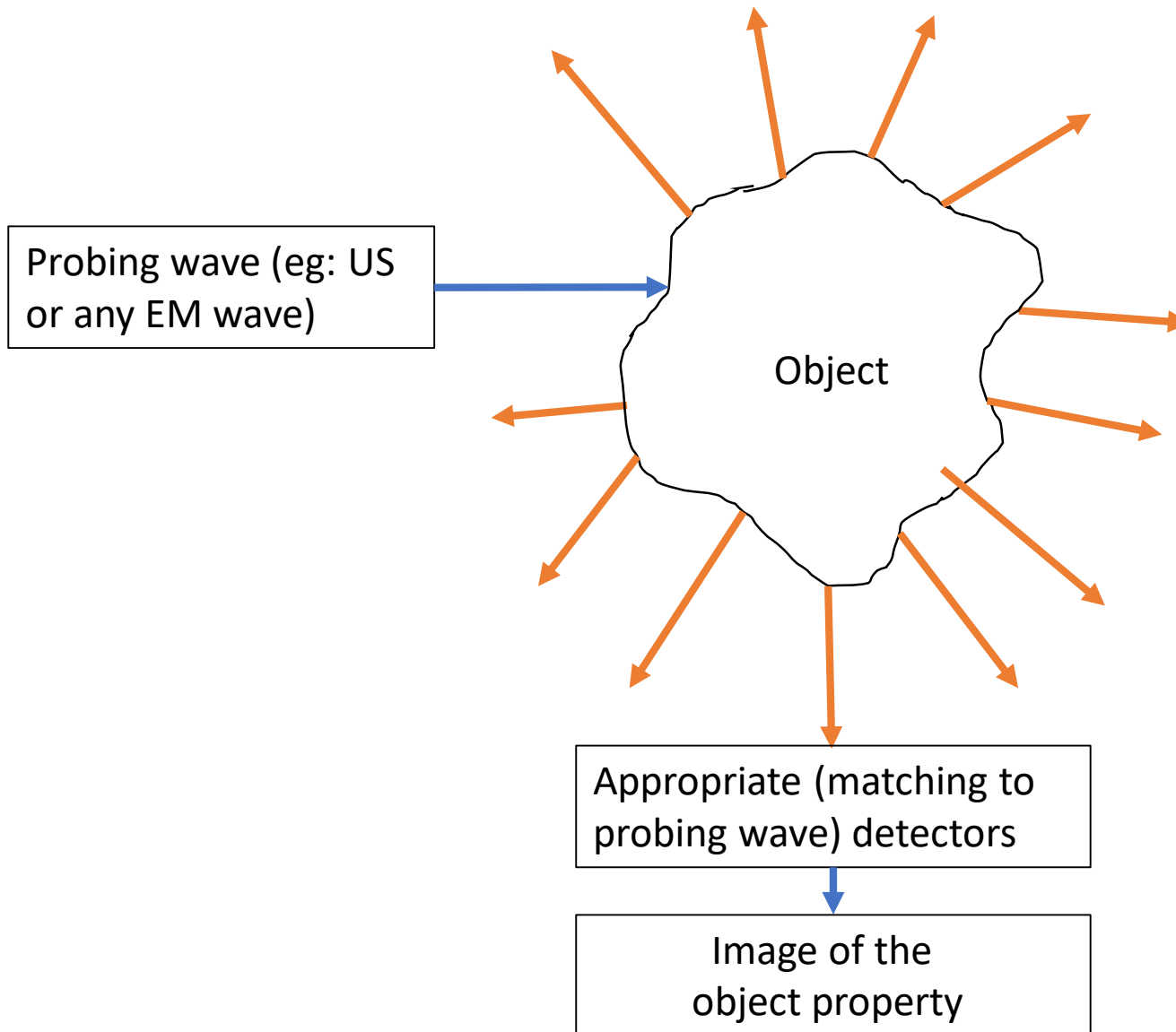
**Dali Theatre-Museum, Figueres, Girona,  
Spain**



# Projection may not be possible in all cases



# Forward and inverse problem



## Forward Model/Problem

A physical/mathematical model explaining how probing wave interacts with the object.  
Eg: how X-rays interacts with human body (Beer Lamberts Law)

## Measurement Model

A physically realizable measurement of the probing wave after interacting with the object.

## Inverse Model/Problem

Given the forward model and the measurement model, find the object property.  
(eg: the absorption coefficient of the tissue as a 3D map in CT scan. )

# Relate these concepts to the real life examples.

Identify the forward and inverse problems associated with the following photographs (need not be imaging problems. Some examples are forced ones while others are direct/obvious)



Zagreb, Croatia.

- The movement of the duck leaves behind a wave pattern.
- Is this pattern unique to a duck?
- Given the pattern can you identify the duck?





- Each food is associated with a unique aroma.?
- Can you identify the food from its aroma?

Castelldefels, Barcelona, Spain.





- Mumbai roads are infamous for Manholes.
- While we walk in the beautiful Mumbai Monsoon, can you identify the manhole? If so, how?

Chandivali, Mumbai.

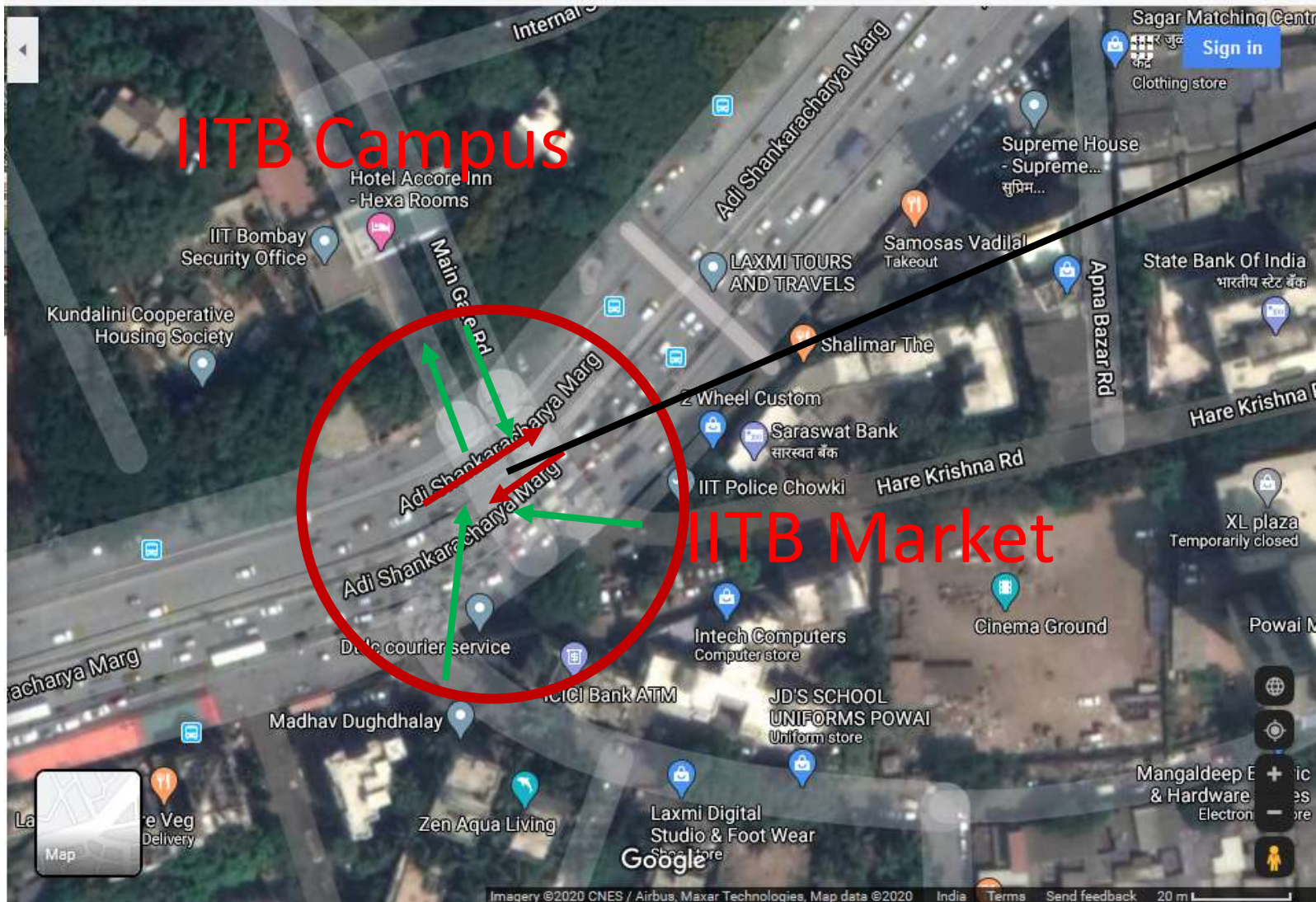


Near AIIMS, Rishikesh.

## ECHOLOCATION:

- Bats use sound to navigate.
- Sound waves are emitted which on reflection from the object is picked up the ear and processed in the brain to find location, size and shape of the object.
- Is this an inverse problem?





IITB main gate

- From IITB main campus, we can cross the road to the market through the junction as circled. The green arrows shows the vehicle movement during the “walk” sign.
- We take measurements of vehicle movements from all sides and decide to cross, change directions, stop etc.
- The problem is even tougher during night when the signal is off so that vehicles with red arrows also moves without stops.



This simplifies the problem (have to worry about law offenders )





- Driving in a rainy or misty day/night in heavy traffic. How many inverse problems we instantly solve in the brain? If the location is familiar then it simplifies the problem (apriori information).
- Note that the usual traffic rules and driving rules acts as the forward model along with the local habits (it is very common in Mumbai to overtake from left by two wheelers), local terrain etc.



Mumbai Taxis , Autos and the Monsoon.



Monsoon in IITB campus

## Learning process in children

- They observe and make forward models.
- Eg: One of the developmental milestones from 12-18 months is to find hidden objects. Is this can be categorized as some sort of inverse problem?





- There are musicians who compose film music based on ragas. Can you identify the raga by hearing the film song?
- Can you catch the copy cats?

Eg: T. Sreenidhi

[https://wikivisually.com/wiki/T.\\_Sreenidhi](https://wikivisually.com/wiki/T._Sreenidhi)

Powai Fine Arts, Nahar, Chandivali, Mumbai



# Can One Hear the Shape of a Drum?

## Mark Kac



Can One Hear the Shape of a Drum? Author(s): Mark Kac  
Reviewed work(s): Source: The American Mathematical  
Monthly, Vol. 73, No. 4, Part 2: Papers in Analysis  
(Apr., 1966), pp. 1-23



- How many images are formed by a pair of mirrors?
- Count the image and find the number of mirrors used, relative orientation etc?

Helsinki, Finland.

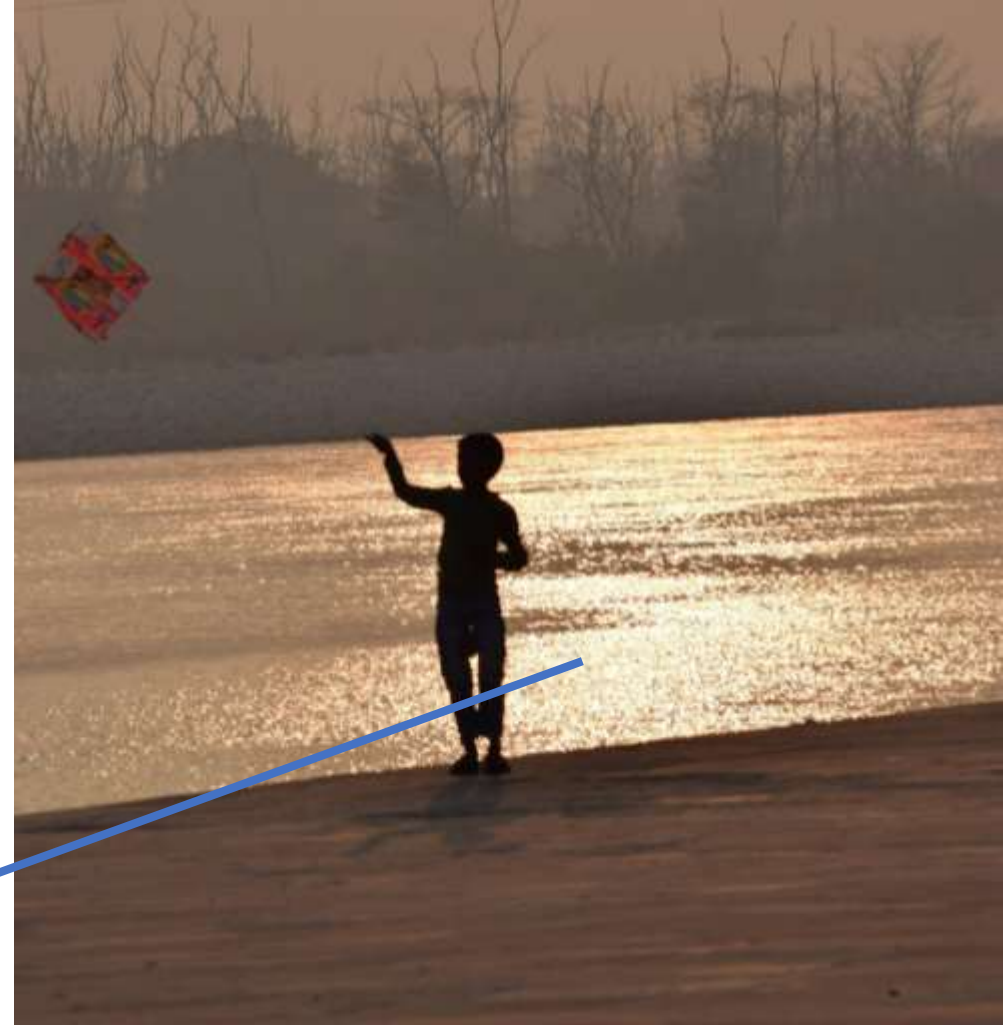


# Deblurring



Vashi Bridge, Navi Mumbai

- Bridge is distorted by the moving rain drops in the window glass of a moving train.
- Can you find the velocity of the train or the velocity of the rain drops?
- It is very common to see the light reflected from the water body to fade while wind blows.
- Can you find the wind velocity from the blurred image?



River Ganga, Haridwar





[https://commons.wikimedia.org/wiki/File:OxyWatch\\_C20\\_Pulse\\_Oximeter.png](https://commons.wikimedia.org/wiki/File:OxyWatch_C20_Pulse_Oximeter.png)

### Pulse oximeter

- Near Infrared light can penetrate human body and can carry information about absorption coefficient of tissue.
- This can then be “inverted” to find the tissue oxygen saturation.



- X ray imaging: 2d projection of dental cavity.
- Here it is just the projection measurement on film: Intra Oral Periapical radiograph.
- The inverse problem associated is carried out by the dentist by looking at the measurement.
- CBCT (cone beam computed tomography) of teeth gives a 3D image.

My own report: lost one teeth which served 38 years



# Airports/sensitive buildings



- Non destructive testing (NDT)  
Eg: baggage check using X-rays.
- Full body scanner for travellers in airports.

[https://commons.wikimedia.org/wiki/File:Check\\_in\\_area\\_and\\_Baggage\\_screening\\_at\\_Jodhpur\\_Airport.jpg](https://commons.wikimedia.org/wiki/File:Check_in_area_and_Baggage_screening_at_Jodhpur_Airport.jpg)

# Near infrared spectroscopy of painting



Mona Lisa, Louvre Museum, Paris.

- The final art of any artist involve a lot of corrections.
- The corrections are made one above the other thus having different layers.
- The outer layer is the finished work.
- Is it possible to reconstruct each layer so that we can get an idea of how a beautiful work evolve in the mind of an artist.

# Forensics or crime scene reconstruction, archaeology

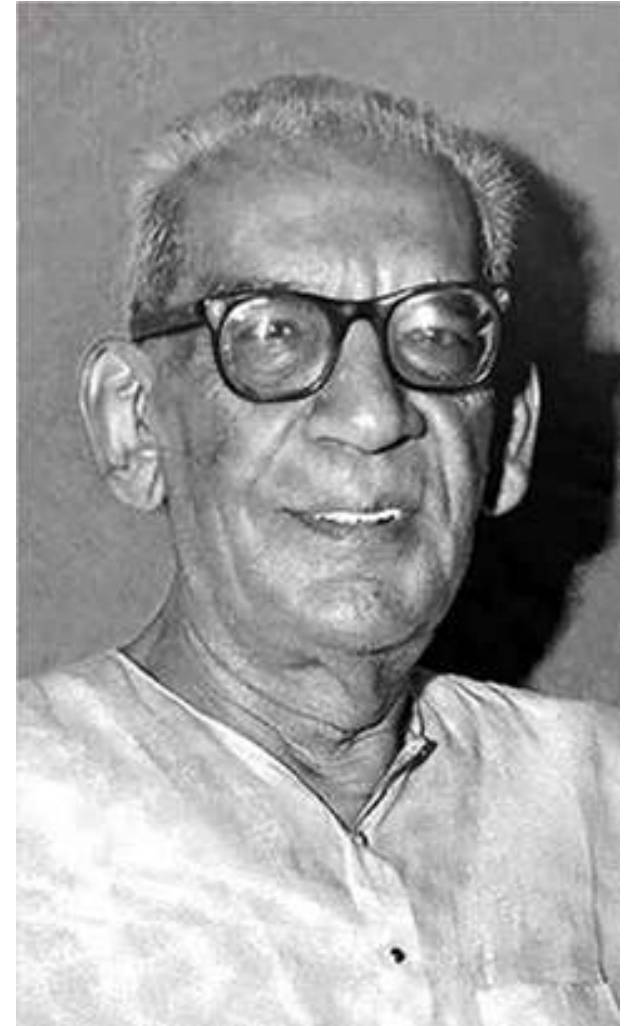
**Arthur Conan Doyle:**  
creator of Sherlock  
Holmes and Dr. Watson.

**Sharadindu Bandyopadhyay:**  
Creator of Byomkesh Bakshi.

Experience + intelligent observation = forward model



Catacombs of Paris





# Police Dogs



- Train them: forward model is created in brain.
- In crime scene: measurement is taken.
- An inverse problem is attempted in its brain to get the criminal .

**Rishikesh.**

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# Kitchen



Gas levels of cylinders, Food quality testing: vegetables and fruits, milk etc...



# Alcohol detection

- Transdermal alcohol concentration
- Breath analyzer: Henrys Law.



<http://chdtransport.gov.in/Webpages/DrunkenDriving.html>

# Politics: Opinion Polls

Critical states in Political Trends. How much reliable is a poll on Twitter? A study by means of the Potts Model  
<https://arxiv.org/abs/1901.10984>



<https://eci.gov.in/about/about-eci/the-functions-electoral-system-of-india-r2/>

# Sudoku

	1	2		3	4	5	6	7
	3	4	5		6	1	8	2
		1		5	8	2		6
		8	6					1
	2				7		5	
		3	7		5		2	8
	8			6		7		
2		7		8	3	6	1	5

Generating Sudoku Puzzles as an Inverse Problem

<https://sites.math.washington.edu/~morrow/mcm/team2306.pdf>.

Each row , column and 3x3 sub matrices should be filled with 1 to 9 without repetition starting from a partially filled matrix.

[https://commons.wikimedia.org/wiki/File:Minimal\\_9x9\\_Sudoku\\_with\\_40\\_givens.svg](https://commons.wikimedia.org/wiki/File:Minimal_9x9_Sudoku_with_40_givens.svg)

# Cards and chess



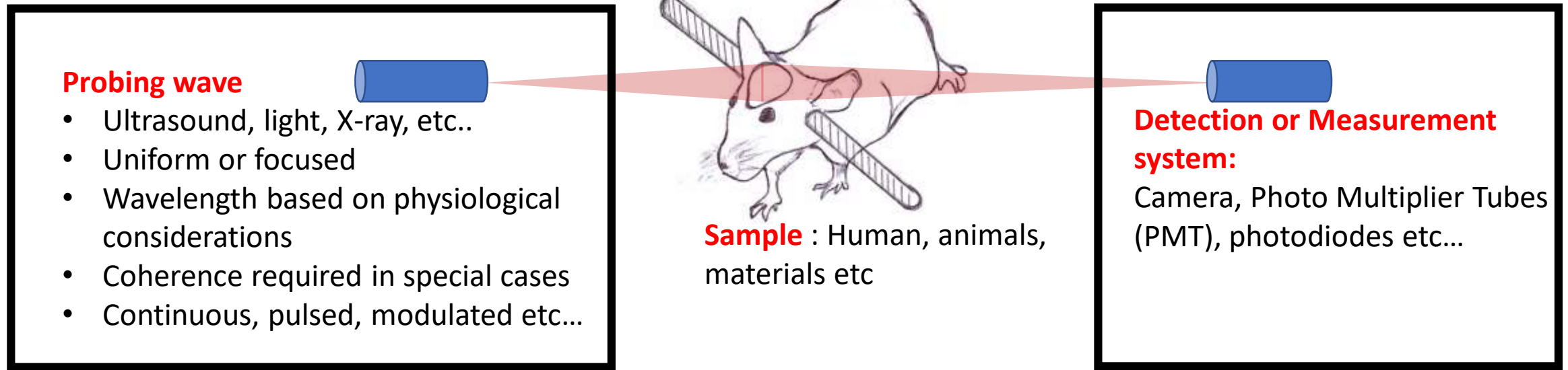
Gymkhana, Indian Institute of Science

Indian Card Game 28  
or 56: guessing the  
cards in opponents  
hands

Search “Inverse Chess”

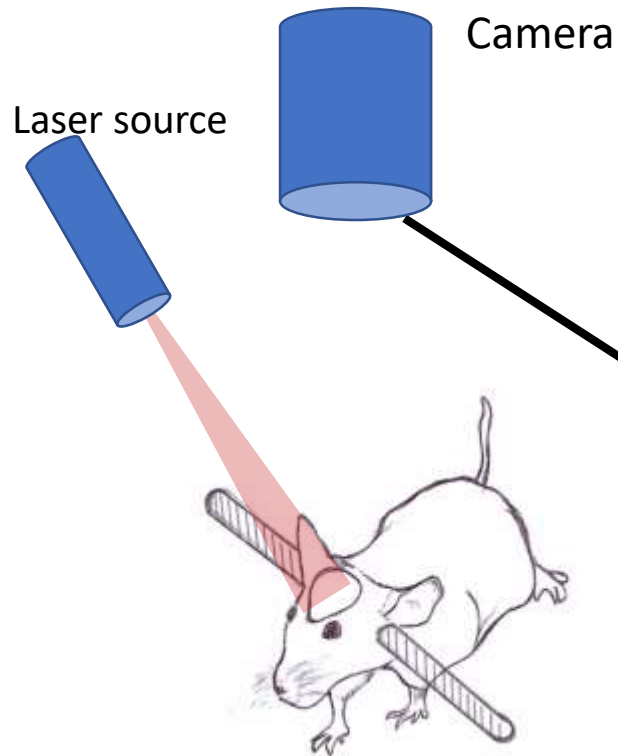


# Imaging system



- How do we select the sources and the detectors?
- What energy..X ray, US, light etc...
- What wavelength? How much intensity?
- White light? LED's? lasers?- If so, CW or pulsed? Focussed or uniform illumination??
- Detectors: should match the source: sensitivity (Quantum efficiency), area detector etc..
- Sample: invitro, invivo?? Size? Which probe to use? Info like the physiological window etc..
- Imaging: spectroscopy (no spatial but an average information) or tomography? Forward models?? Inversion models: computational costs (real time ???) Speed etc...

# An example of imaging

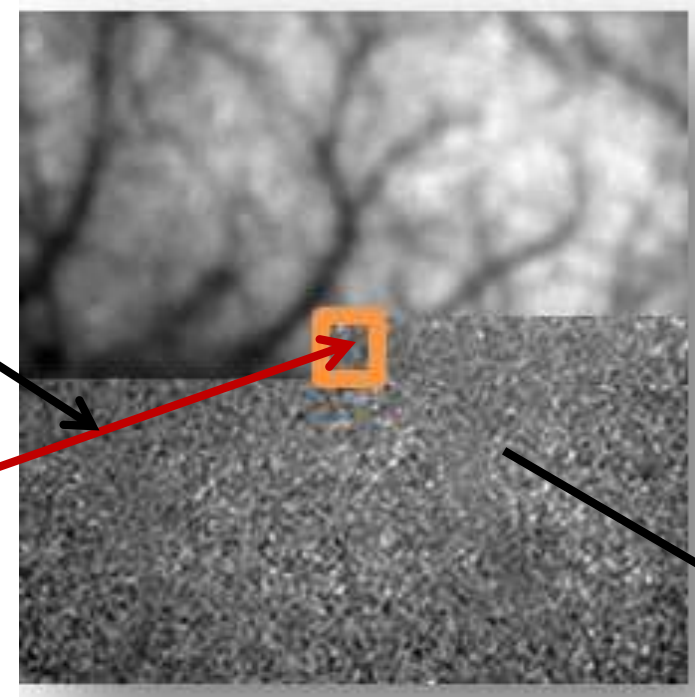


$$\text{Speckle contrast, } \kappa(r, T) = \frac{\sigma}{\langle I \rangle}$$

$\sigma$  = standard deviation of intensity

$\langle I \rangle$  = mean of intensity

Image processing? Yes, but how do we arrive at quantity speckle contrast??? How do we relate it to say blood flow??? Physics????



Intensity speckles

This is what you get from camera..! So called images..

D. Briers et. al., J. Biomed. Opt. 18, 066018 (2013).  
A. K. Dunn, Ann. Biomed. Engg. 40, 367–377 (2012).  
R. Bandyopadhyay et al, Rev. sci. instrum. 76, 2005