

Section 1.1

1. Find the value of y that corresponds to $x=3$ in $y = -2 + 4(x-3)$.

2. Find the value of x that corresponds to $y=3$ in $y = 3 - 2(x+1)$.

$$y = -2$$

$$3 = 3 - 2(x+1) \rightarrow 0 = -2(x+1)$$

$$x = -1$$

In Exercises 3 and 4, find the value of m that corresponds to the values of x and y .

$$3. \ x=5, \ y=2, \ m = \frac{y-3}{x-4} = \frac{-1}{1} = -1$$

$$4. \ x=-1, \ y=-3, \ m = \frac{2-y}{3-x} = \frac{5}{4}$$

In exercises 5 and 6, determine whether the ordered pair is a solution to the equation.

5. $3x - 4y = 5$

6. $y = -2x + 5$

a) $\left(2, \frac{1}{4}\right)$

b) $(3, -1)$

a) $(-1, 7)$

b) $(-2, 1)$

Yes

No

Yes

No

In exercises 7 and 8, find the distance between the points.

7. $(1, 0)$ and $(0, 1)$

8. $(2, 1)$ and $\left(1, -\frac{1}{3}\right)$

$$\begin{aligned} d &= \sqrt{(0-1)^2 + (1-0)^2} \\ &= \sqrt{1+1} \\ &= \sqrt{2} \end{aligned}$$

$$\begin{aligned} d &= \sqrt{(2-1)^2 + \left(1 - \left(-\frac{1}{3}\right)\right)^2} \\ &= \sqrt{1 + \frac{16}{9}} \\ &= \sqrt{\frac{25}{9}} = \frac{5}{3} \end{aligned}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

In Exercises 9 and 10, solve for y in terms of x .

9. $4x - 3y = 7$

$$-3y = 7 - 4x$$

$$y = -\frac{7}{3} + \frac{4}{3}x$$

10. $-2x + 5y = -3$

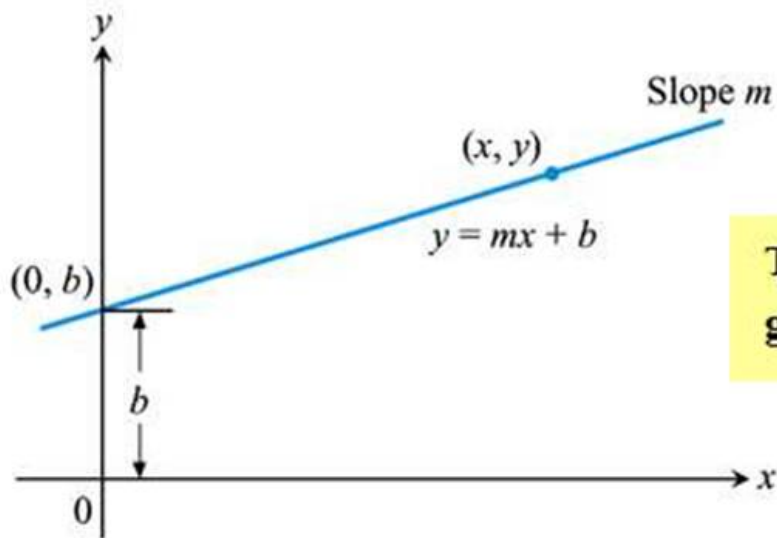
$$5y = 2x - 3$$

$$y = \frac{2}{5}x - \frac{3}{5}$$

The equation $y = m(x - x_1) + y_1$ is the **point - slope equation** of the line through the point (x_1, y_1) with slope m .

$$y - y_0 = m(x - x_0)$$

The equation $y = mx + b$ is the **slope - intercept equation** of the line with slope m and y -intercept b .



The equation $Ax + By = C$ (A and B not both 0) is a **general linear equation** in x and y .

In Exercises 1–6, solve for x .

Section 1.2

Functions and Graphs

① $3x - 1 \leq 5x + 3$

② $x(x - 2) > 0$

③ $|x - 3| \leq 4$

④ $|x - 2| \geq 5$

5. $x^2 < 16$

6. $9 - x^2 \geq 0$

②

x	$-$	$+$	$+$
$x-2$	$-$	$-$	$+$
	\oplus	\ominus	\oplus

$x < 0$ or $x > 2$

$(-\infty, 0) \cup (2, \infty)$

③

$$-4 \leq x - 3 \leq 4$$

$+3 \quad +3 \quad +3$

$$-1 \leq x \leq 7$$

$x - 2 \geq 5$ or $x - 2 \leq -5$

$x \geq 7$ or $x \leq -3$

①

$$3x - 1 \leq 5x + 3$$

$-5x \quad +1 \quad -5x \quad +1$

$$-2x \leq 4$$

$\div -2 \quad \div -2$

$x \geq -2$

Interval: $[-2, \infty)$

In Exercises 7 and 8, describe how the graph of f can be transformed to the graph of g .

7. $f(x) = x^2$, $g(x) = (x+2)^2 - 3$

8. $f(x) = |x|$, $g(x) = |x-5| + 2$

7. translate f 2 units left and 3 units down

8. translate $f(x)$ 5 right and 2 units up

In Exercises 9–12, find all real solutions to the equations.

9. $f(x) = x^2 - 5$

(a) $f(x) = 4$

10. $f(x) = \frac{1}{x}$

(a) $f(x) = -5$

10a

$$\frac{1}{x} = -5$$

$$x = -\frac{1}{5}$$

(b) $f(x) = -6$

9a

$$x^2 - 5 = 4$$

$$x^2 = 9$$

$$x = \pm 3$$

9b

$$x^2 - 5 = -6$$

$$x^2 = -1$$

$$x = \pm i$$

No real solution

(b) $f(x) = 0$

$$\frac{1}{x} = 0$$



No solution

$$11. f(x) = \sqrt{x+7}$$

$$(a) f(x) = 4 \quad ; x = 9 \quad (b) f(x) = 1 \quad x = -6$$

$$12. f(x) = \sqrt[3]{x-1}$$

$$(a) f(x) = -2$$

$$\sqrt[3]{x-1} = -2$$

$$x-1 = -8$$

$$x = -7$$

$$(b) f(x) = 3$$

$$\sqrt[3]{x-1} = 3$$

$$x-1 = 27$$

$$x = 28$$

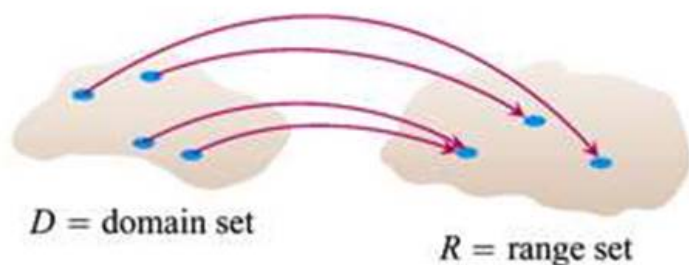
Functions

A rule that assigns to each element in one set a unique element in another set is called a *function*. A function is like a machine that assigns a unique output to every allowable input. The inputs make up the *domain* of the function; the outputs make up the *range*.

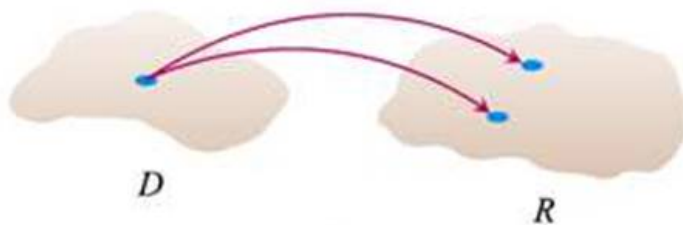


A **function** from a set D to a set R is a rule that assigns a unique element in R to each element in D .

In this definition, D is the domain of the function and R is a set containing the range.



(a)



(b)

Not
a function

- The domains and ranges of many real-valued functions of a real variable are intervals or combinations of intervals. The intervals may be **open**, **closed** or **half-open**, **finite** or **infinite**.
- The endpoints of an interval make up the interval's **boundary** and are called **boundary points**.
- The remaining points make up the interval's **interior** and are called **interior points**.

- **Closed intervals** contain their boundary points.
- **Open intervals** contain no boundary points



Name: Open interval ab

Notation: $a < x < b$ or (a, b)



Closed at a and open at b

Notation: $a \leq x < b$ or $[a, b)$



Name: Closed interval ab

Notation: $a \leq x \leq b$ or $[a, b]$



Open at a and closed at b

Notation: $a < x \leq b$ or $(a, b]$



Name: The set of all real numbers

Notation: $-\infty < x < \infty$ or $(-\infty, \infty)$



Name: The set of numbers greater than a

Notation: $a < x$ or (a, ∞)



Name: The set of numbers greater than or equal to a

Notation: $a \leq x$ or $[a, \infty)$



Name: The set of numbers less than b

Notation: $x < b$ or $(-\infty, b)$



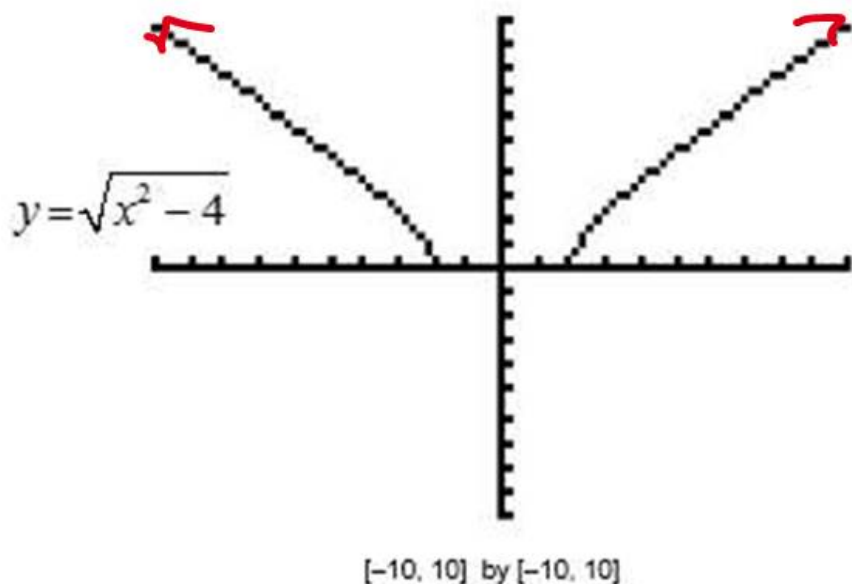
Name: The set of numbers less than or equal to b

Notation: $x \leq b$ or $(-\infty, b]$

Identify the domain and range and use a grapher to graph the function $y = \sqrt{x^2 - 4}$

Domain: The function gives a real value of y for each value of $|x| \geq 2$ so the domain is $(-\infty, -2] \cup [2, \infty)$.

Range: Every value of the domain, x , gives a real, positive value of y so the range is $[0, \infty)$.



- The graphs of *even* and *odd* functions have important symmetry properties.

A function $y = f(x)$ is a

even function of x if $f(-x) = f(x)$

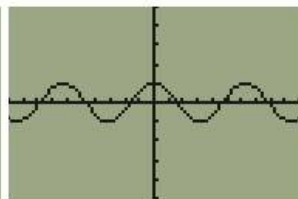
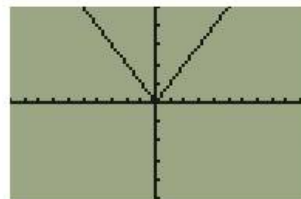
odd function of x if $f(-x) = -f(x)$

for every x in the function's domain.

```

Plot1 Plot2 Plot3
Y1=abs(X)
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=

```



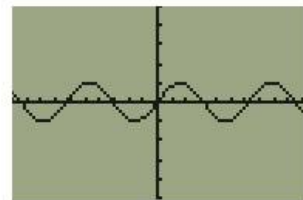
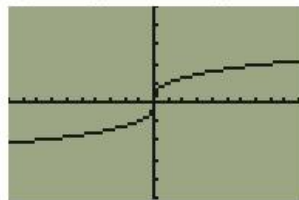
Even functions have y-axis symmetry

Odd functions have origin symmetry.

```

Plot1 Plot2 Plot3
Y1=sqrt(X)
Y2=
Y3=
Y4=
Y5=
Y6=
Y7=

```



- The graph of an **even** function is **symmetric about the y-axis**. A point (x,y) lies on the graph if and only if the point $(-x,y)$ lies on the graph.
- The graph of an **odd** function is **symmetric about the origin**. A point (x,y) lies on the graph if and only if the point $(-x,-y)$ lies on the graph.

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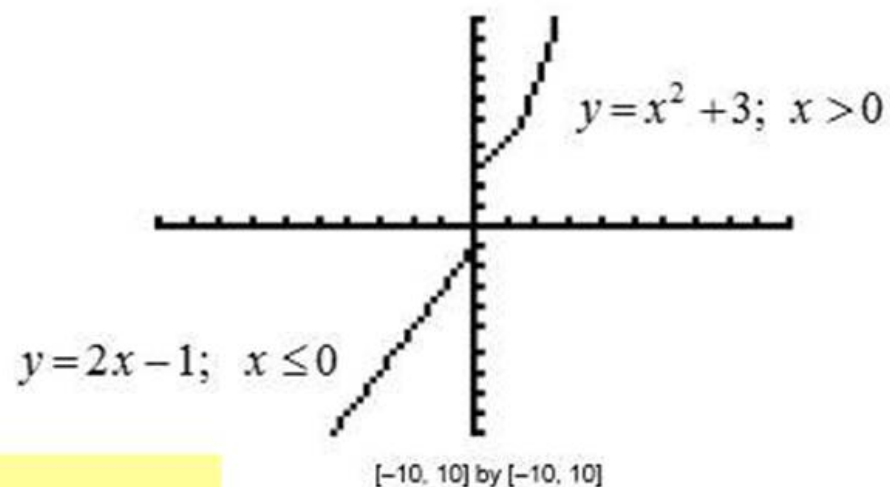
Plot1 Plot2 Plot3
Y1=(2X-1)(X≤0)
Y2=(X²+3)(X>0)
Y3=
Y4=
Y5=
Y6=
Y7=

```



Use a grapher to graph the following piecewise function:

$$f(x) = \begin{cases} 2x - 1 & x \leq 0 \\ x^2 + 3 & x > 0 \end{cases}$$



The absolute value function $y = |x|$ is defined piecewise by the formula

$$|x| = \begin{cases} -x, & x < 0 \\ x, & x \geq 0 \end{cases}$$

Given $f(x) = 2x - 3$ and $g(x) = 5x$, find $f \circ g$.

$$\begin{aligned} &= f(g(x)) \\ &= f(5x) \\ &= 2(5x) - 3 \\ &= 10x - 3 \end{aligned}$$

$$\underbrace{f \circ f \circ g \circ f}(2) =$$

$$f \circ f \circ g(2(2) - 3) = f \circ f \circ g(1) = f \circ f(5)$$

$$= f(2(5) - 3) = f(7) = 2(7) - 3 = 11$$

Standardized Test Questions

47. **True or False** The slope of a vertical line is zero. Justify your answer.

48. **True or False** The slope of a line perpendicular to the line $y = mx + b$ is $1/m$. Justify your answer.

49. **Multiple Choice** Which of the following is an equation of the line through $(-3, 4)$ with slope $1/2$?

(A) $y - 4 = \frac{1}{2}(x + 3)$ (B) $y + 3 = \frac{1}{2}(x - 4)$

(C) $y - 4 = -2(x + 3)$ (D) $y - 4 = 2(x + 3)$

(E) $y + 3 = 2(x - 4)$

50. **Multiple Choice** Which of the following is an equation of the vertical line through $(-2, 4)$?

(A) $y = 4$ (B) $x = 2$ (C) $y = -4$

(D) $x = 0$ (E) $x = -2$

51. **Multiple Choice** Which of the following is the x -intercept of the line $y = 2x - 5$?

(A) $x = -5$ (B) $x = 5$ (C) $x = 0$

(D) $x = 5/2$ (E) $x = -5/2$

52. **Multiple Choice** Which of the following is an equation of the line through $(-2, -1)$ parallel to the line $y = -3x + 1$?

(A) $y = -3x + 5$ (B) $y = -3x - 7$ (C) $y = \frac{1}{3}x - \frac{1}{3}$

(D) $y = -3x + 1$ (E) $y = -3x - 4$

False, because $m = \frac{dy}{dx}$
and $dx = 0$ in a vertical
line making m undefined.

False, because $m(\frac{1}{m}) = 1 \neq -1$

$$y - -1 = -3(x - -2)$$
$$y = -3x - 6 - 1$$

59. **Multiple Choice** Which of the following gives the domain of

$$f(x) = \frac{x}{\sqrt{9-x^2}}?$$

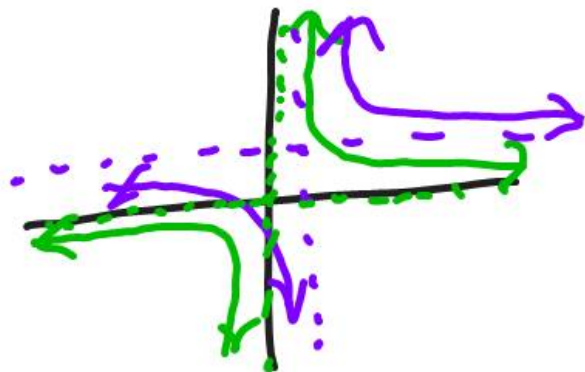
- (A) $x \neq \pm 3$ (B) $(-3, 3)$ (C) $[-3, 3]$
 (D) $(-\infty, -3) \cup (3, \infty)$ (E) $(3, \infty)$

60. **Multiple Choice** Which of the following gives the range of

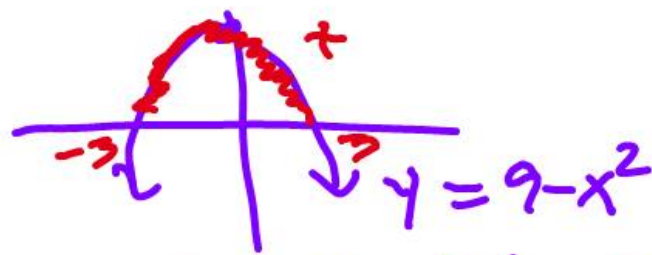
* $f(x) = 1 + \frac{1}{x-1}?$

$g(x) = 1/x$

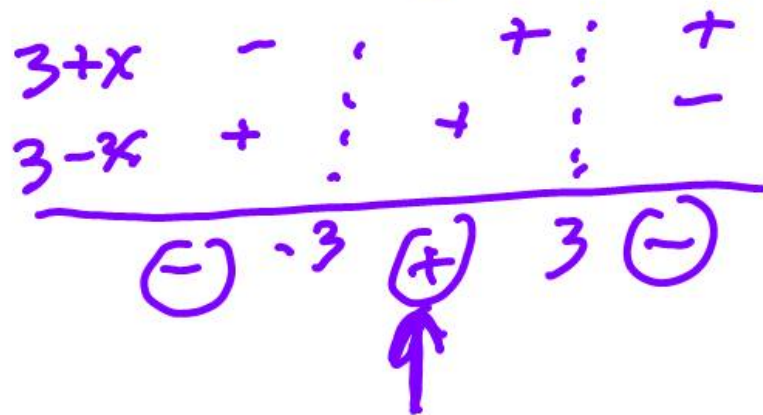
- (A) $(-\infty, 1) \cup (1, \infty)$ (B) $x \neq 1$ (C) all real numbers
 (D) $(-\infty, 0) \cup (0, \infty)$ (E) $x \neq 0$



$$9-x^2 > 0$$



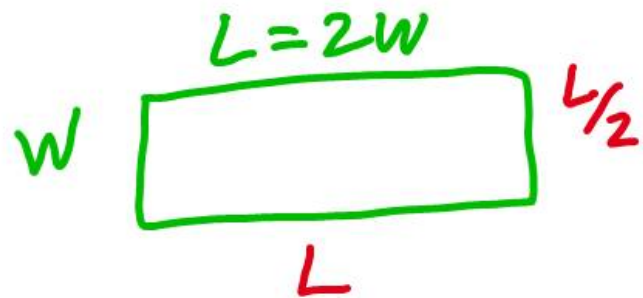
$$9-x^2 = (3+x)(3-x)$$



- 61. Multiple Choice** If $f(x) = 2x - 1$ and $g(x) = x + 3$, which of the following gives $(f \circ g)(2)$? $f(g(2)) = f(5) = 10 - 1 = 9$
- (A) 2 (B) 6 (C) 7 (D) 9 (E) 10

- 62. Multiple Choice** The length L of a rectangle is twice as long as its width W . Which of the following gives the area A of the rectangle as a function of its width?

- (A) $A(W) = 3W$ (B) $A(W) = \frac{1}{2}W^2$ (C) $A(W) = 2W^2$
- (D) $A(W) = W^2 + 2W$ (E) $A(W) = W^2 - 2W$



$$A(w) = 2w^2$$

$$P(L) = 2L + 2\left(\frac{L}{2}\right) = 3L$$