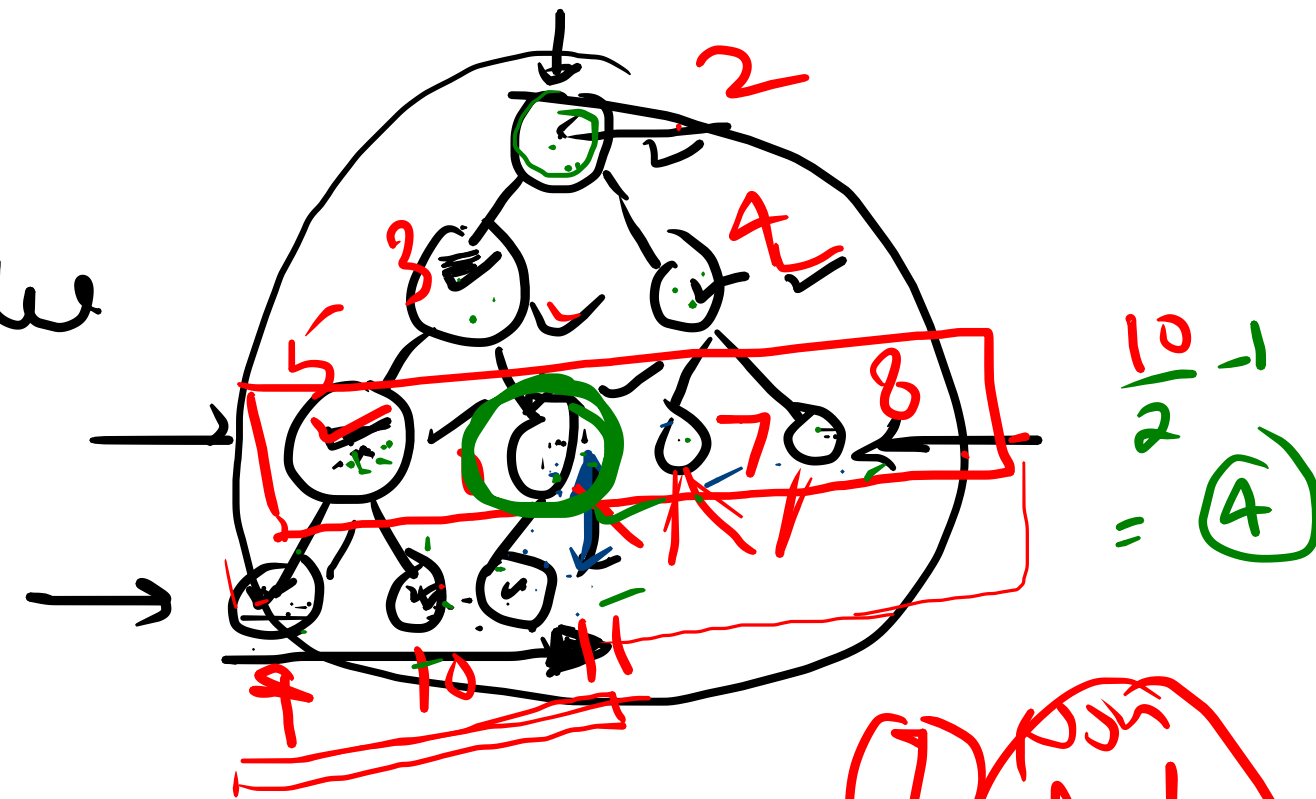


Heap :- Binary Heap - Tree Structure

↳ Complete Binary Tree

↳ Max Heap → value of node > left value + right value
↳ Min Heap → Node value < left value + right value



Application

Heap Sorting = $O(n \log n)$

Priority Queue

Operating System

→ Creation of Heap ✓

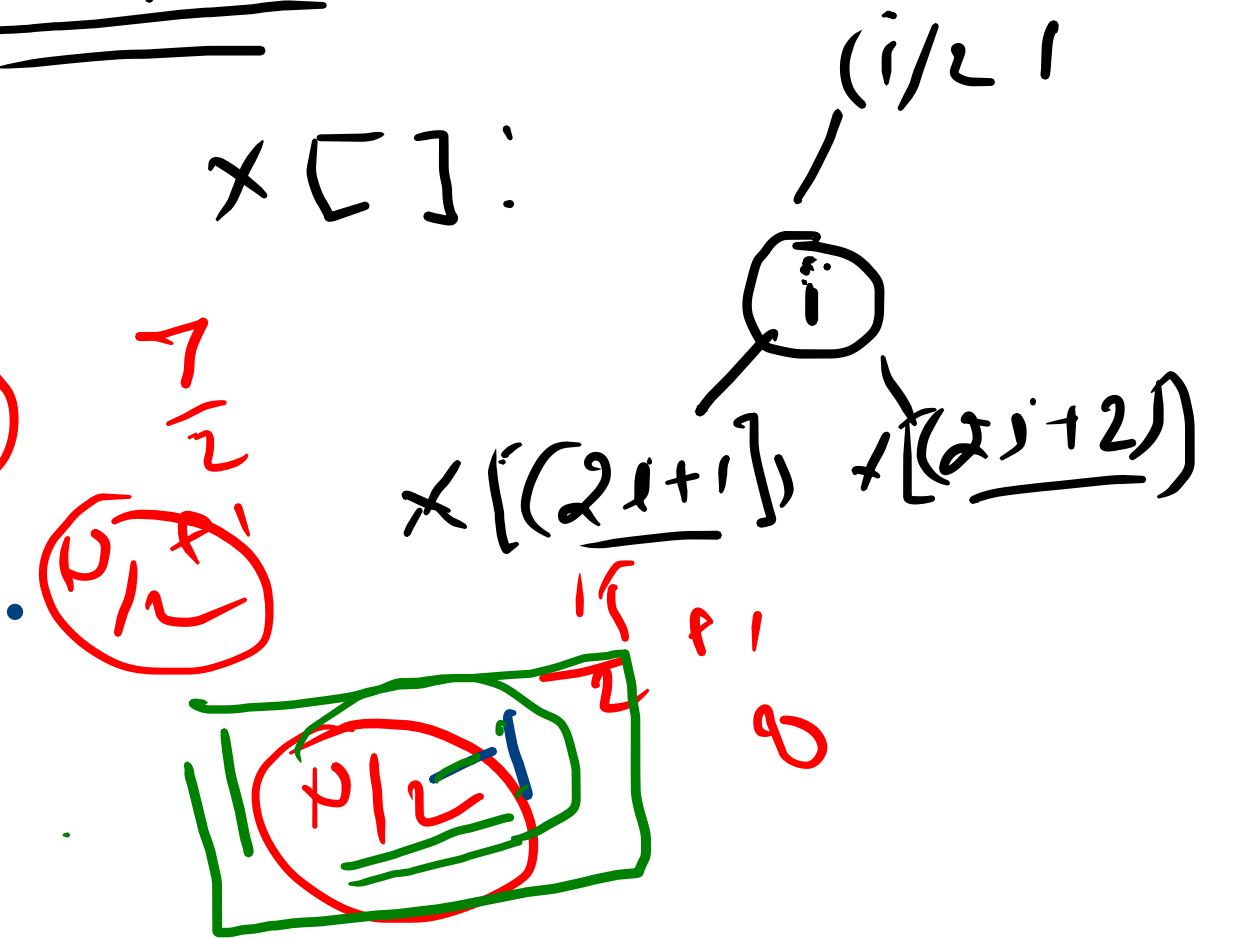
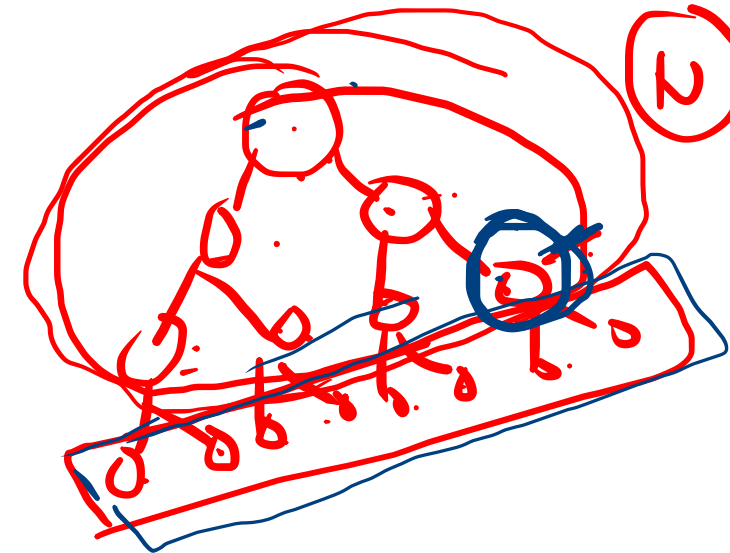
→ Insertion ✓

→ ~~Deletion~~ ✓

→ Traverse = Binary Tree

→ Heap Sort

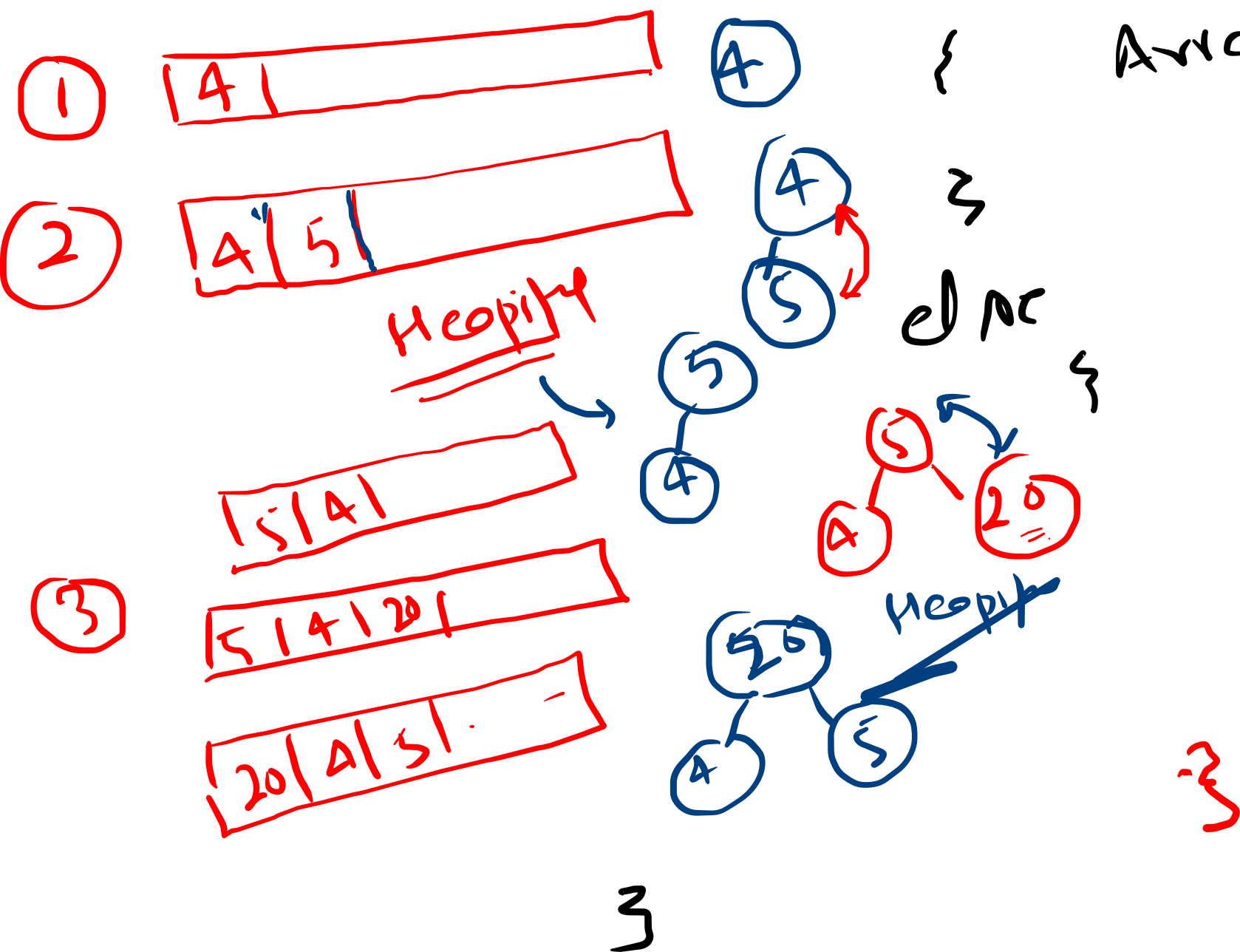
Heapify → Array $x[]$:



① Creation of Heap! → [Data is given in] Array

→ ARRAY implementation

```
Void HeapInsert ( int Array[], int value )  
{  
    if ( size == 0 )  
        Array [ size ] = value;  
        size ++;  
}
```



```
Array [ size - 1 ] = value;  
size --;
```

```
for ( int i = size / 2 - 1; i >= 0; i-- )
```

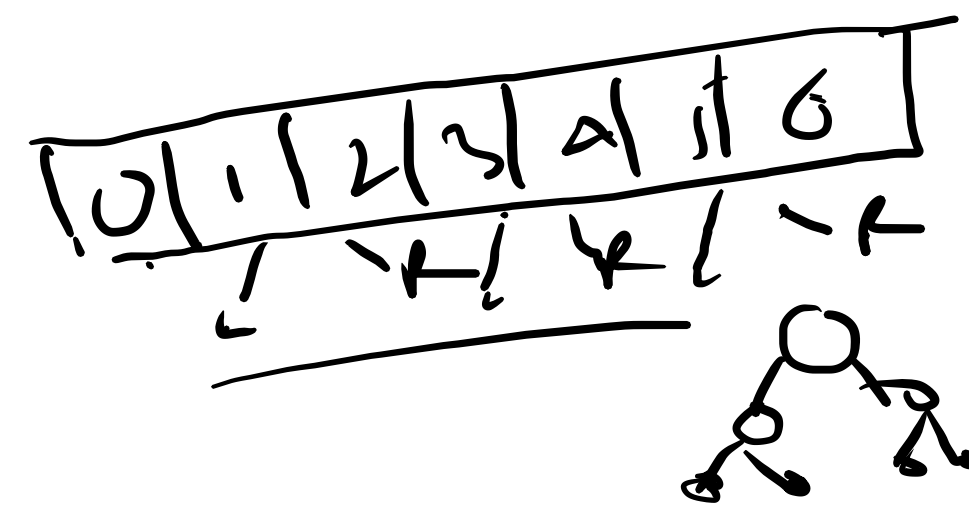
```
    Heapify ( Array, size, i );
```

```
int size = 0;  
int main  
{  
    int n = 10;  
    int x [ N ];
```

```
    HeapInsert ( x, 4 );  
    HeapInsert ( x, 5 );  
    HeapInsert ( x, 10 );  
    HeapInsert ( x, 20 );  
}
```

Let's say pool

$\boxed{N/2 - 1}$



Heapify (int x[], int size, int index)

```
{
    if (size == 1)
        return;
    else
```

```
{
    int Largest = index;
```

```
    int L = 2 * index + 1;
```

```
    int R = 2 * index + 2;
```

```
    if (L < size && x[L] > x[Largest])
```

```
        Largest = L;
```

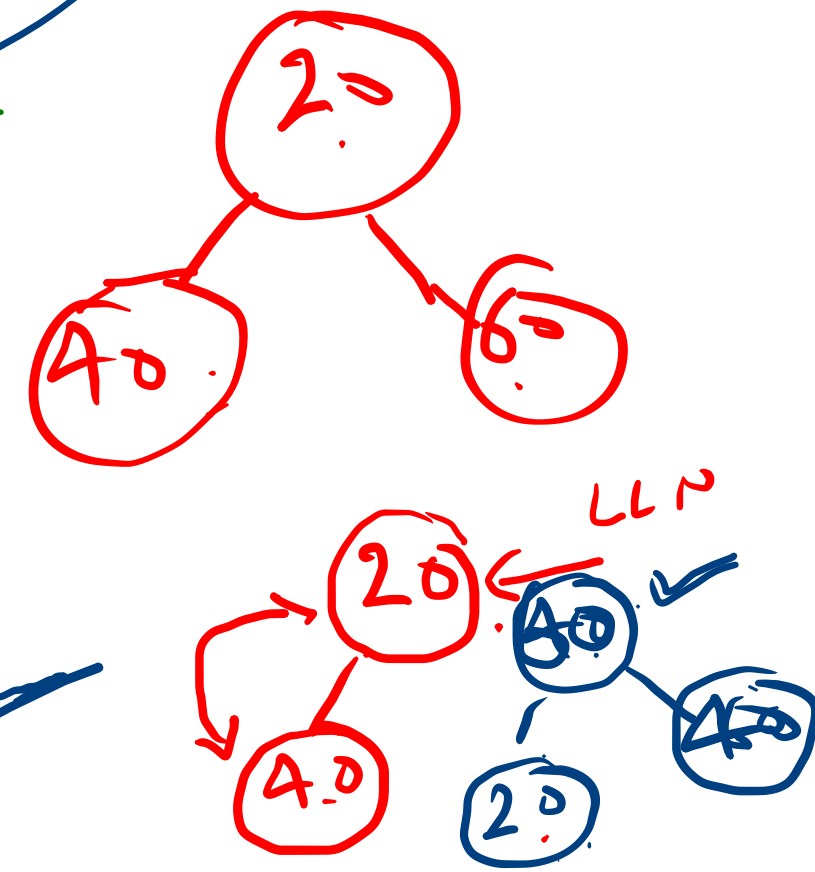
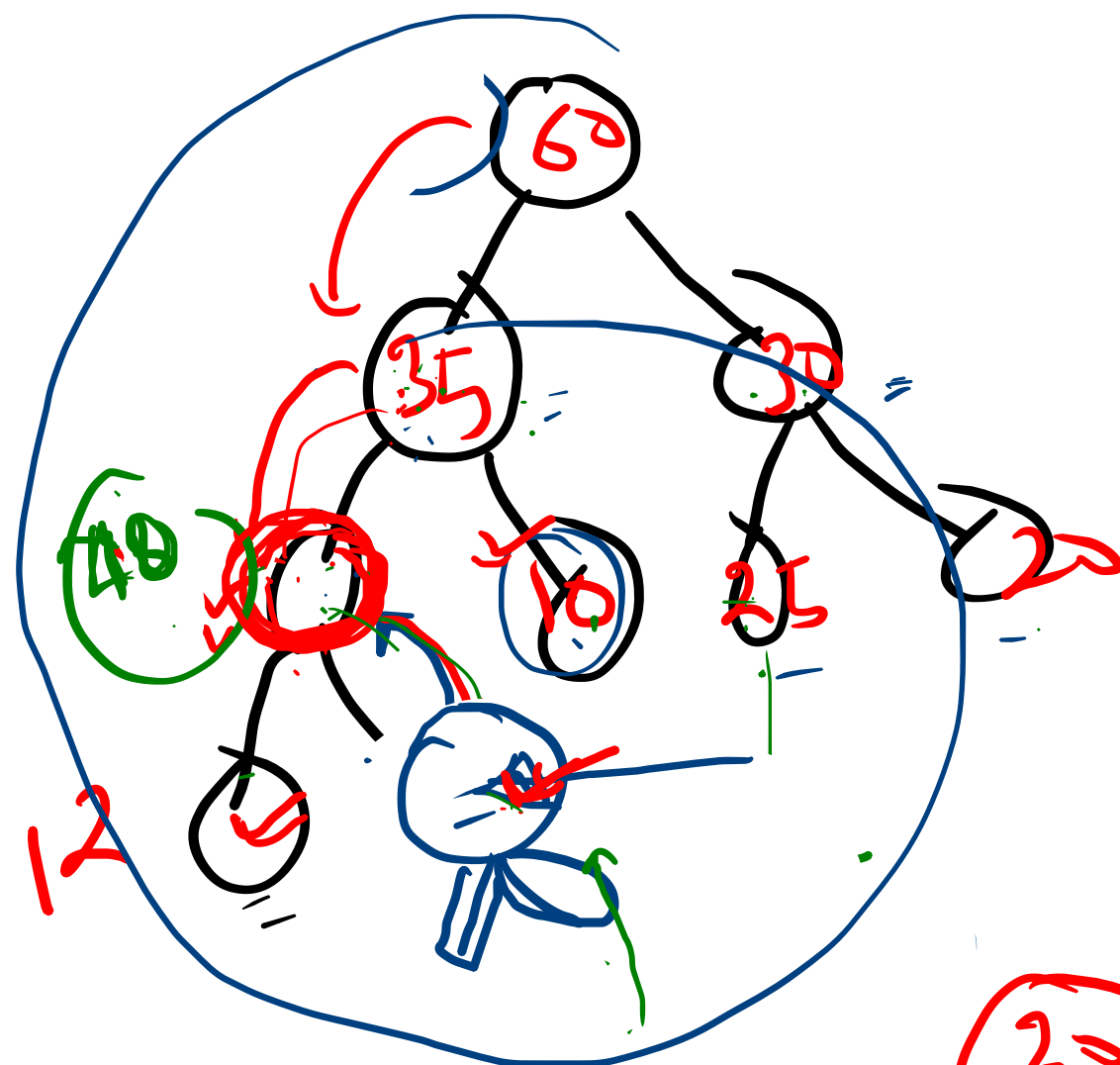
```
    if (R < size && x[R] > x[Largest])
```

```
        Largest = R;
```

```
    if (Largest != index)
```

```
        swap(x[index], x[Largest]);
```

```
    Heapify(x, size, Largest);
```



```

void Delete ( int x[], int value )
{
    int i = 0
    for ( i = 0, i < size : i++)
    {
        if ( value == x[i] )
            break;
    }

    swap ( x[i], x[size-1] )
    size = size - 1

    for ( i = size/2 - 1 ; i > 0 ; i--)
        heapify ( x, i )
}

```

```

{
    int i = 0;
    for (i = 0; i < size; i++)
    {
        if (value = x[i])
            break;
    }

    swap (x[i], x[size - 1])
    size = size - 1;

    for (i = size / 2 - 1; i > 0; i--)
        heapify (x, i);

}

```

```

    swap (x[i], x[size-1]);
    size = size-1;
    for (i = size-1; i > 0; i--)
        heapify (x, size, i);
}

```

size = size - 1

for (i = $\frac{\text{size}}{2} - 1$; i > 0; i--)

Heapify(x, size, i);

3


$$\widehat{40}$$

main ()

{

int x = { 2, 3, 1, 10, 15, 4 };

int size = sizeof x / sizeof x[0];

for (i = size - 1; i > 0; i--)

Heapify (x, size, i);

HeapSort (x, size);

}

HeapSort (int x[], int size)

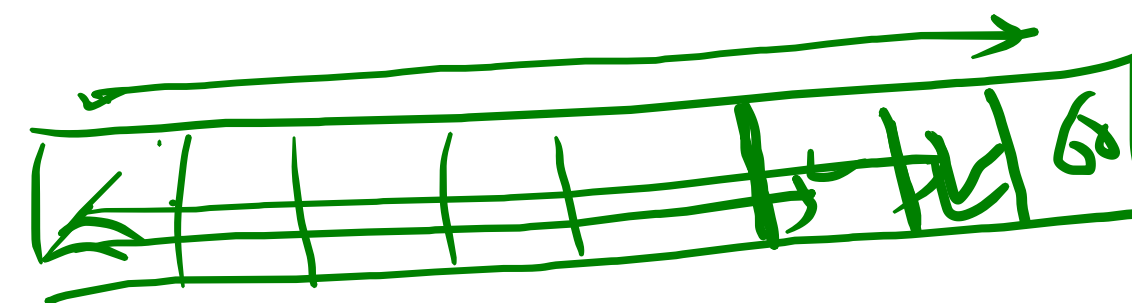
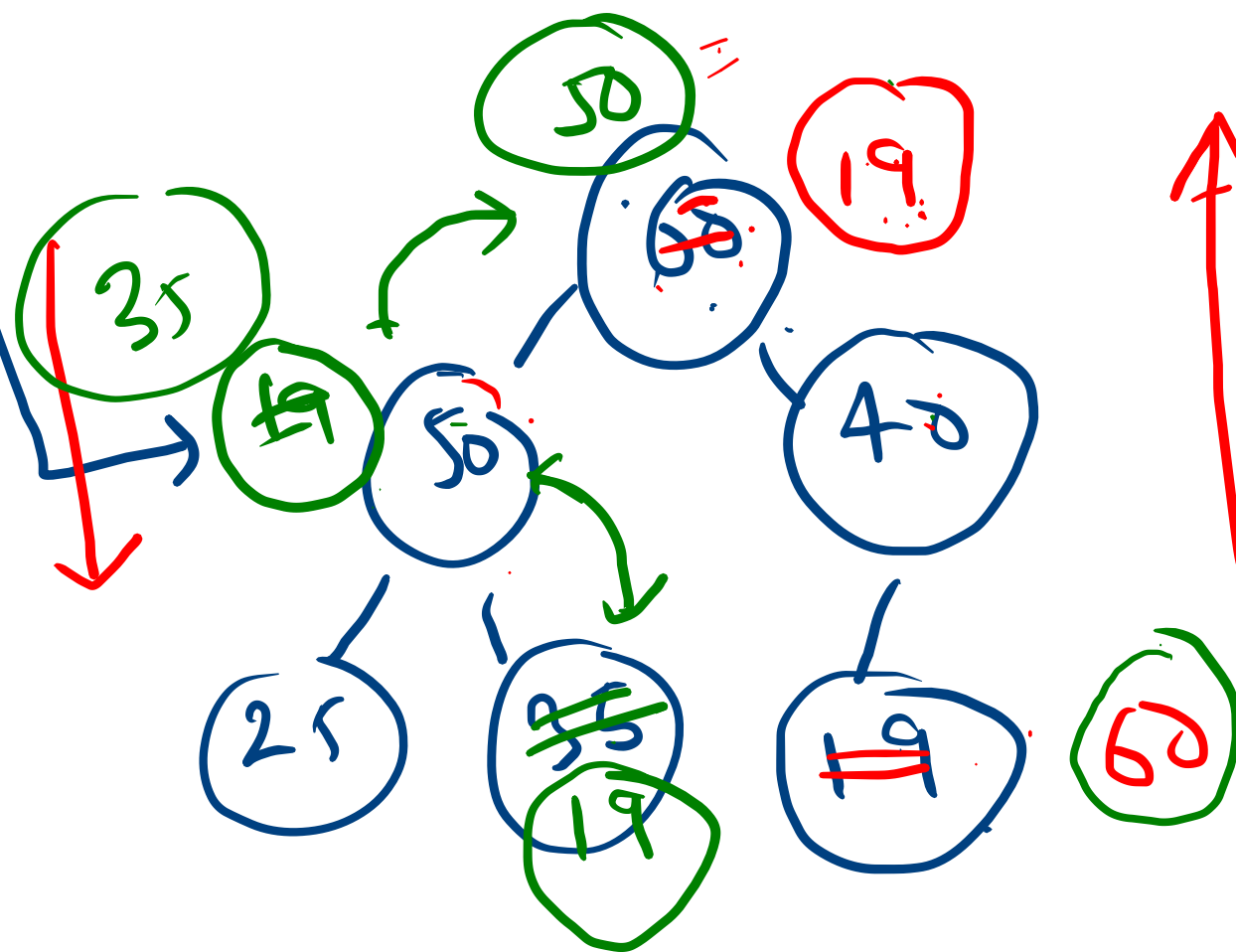
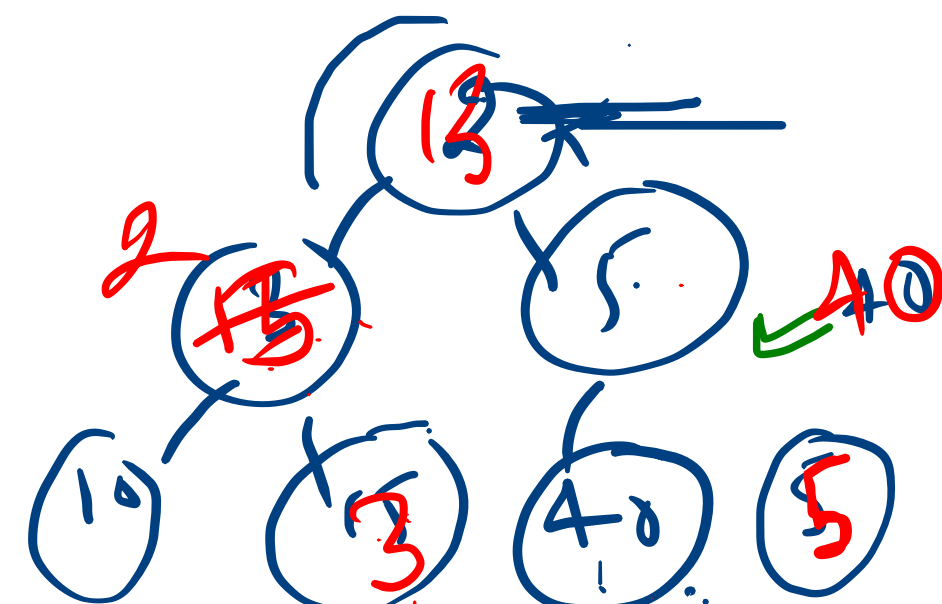
{

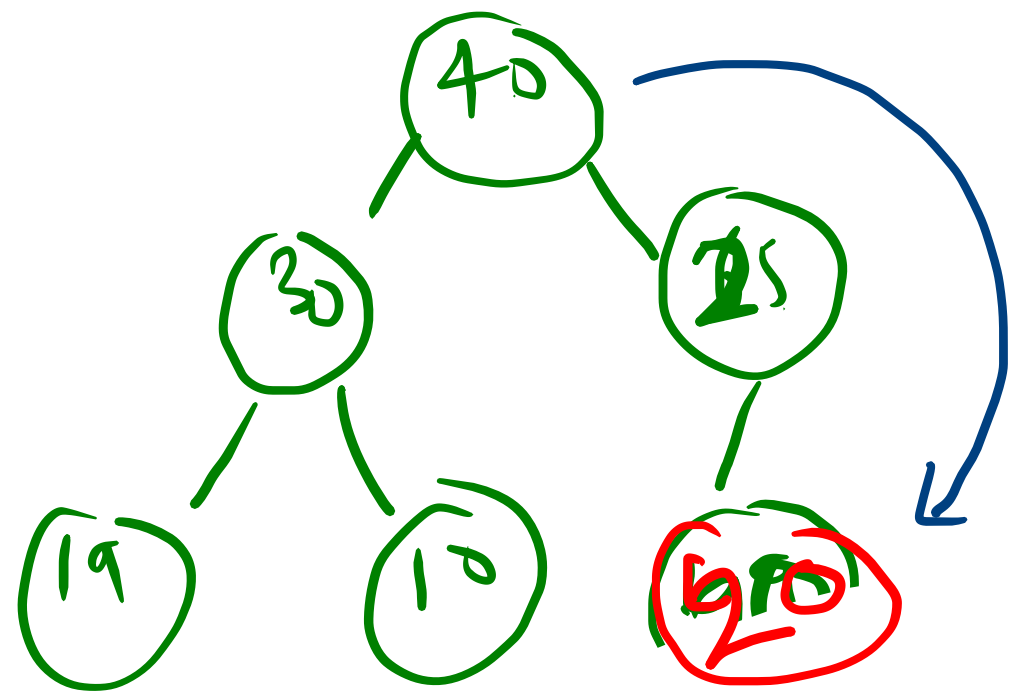
for (i = size - 1; i > 0; i--)

swap (x[0], x[i]);

Heapify (x, 1, 0);

}





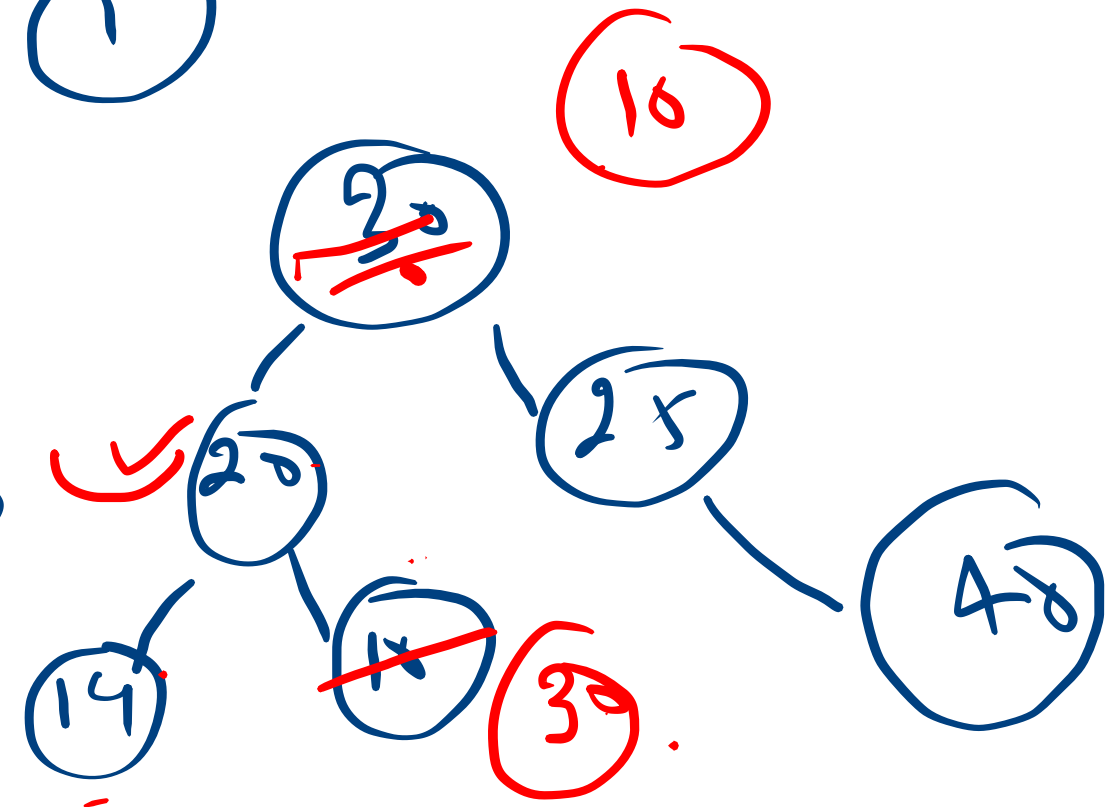
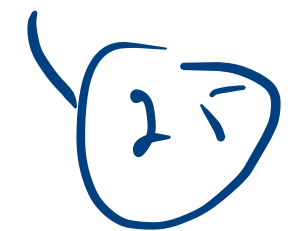
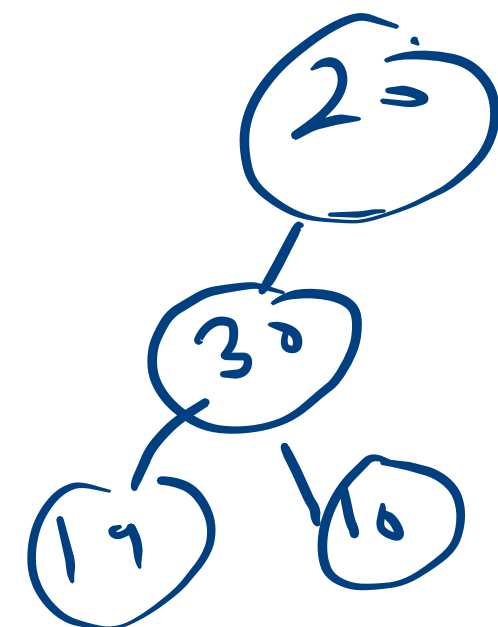
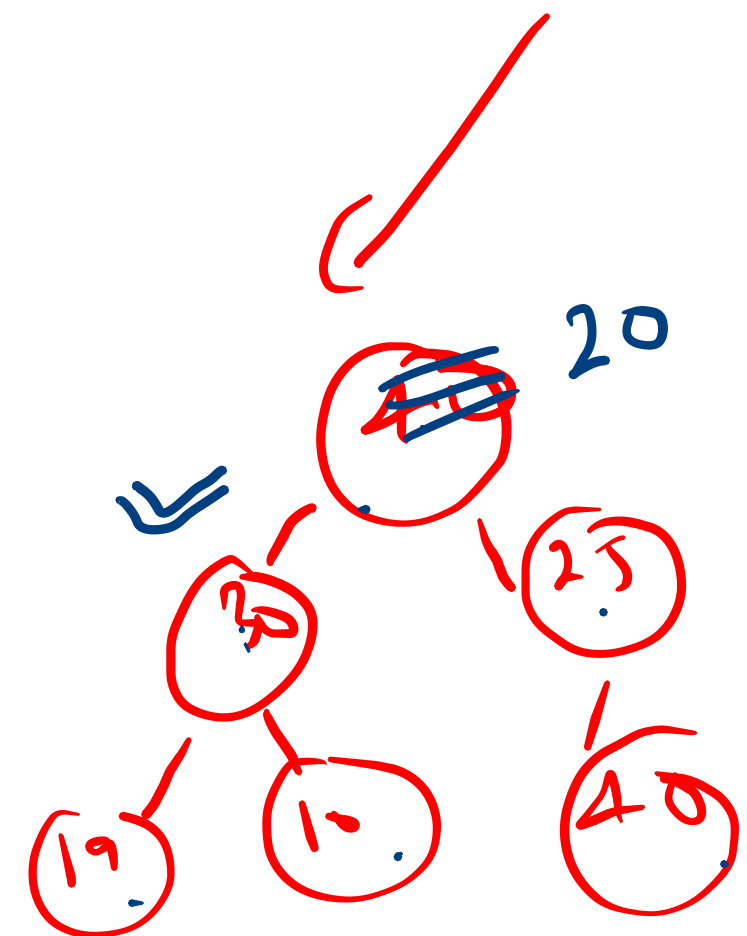
Size = 5

$$5/2 - 1 = 1$$

Size: 4

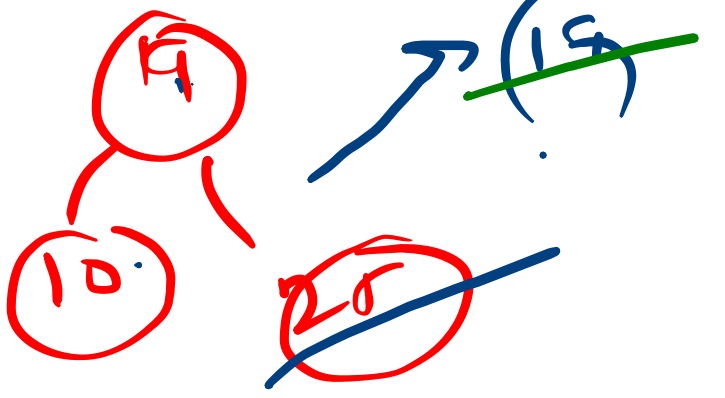
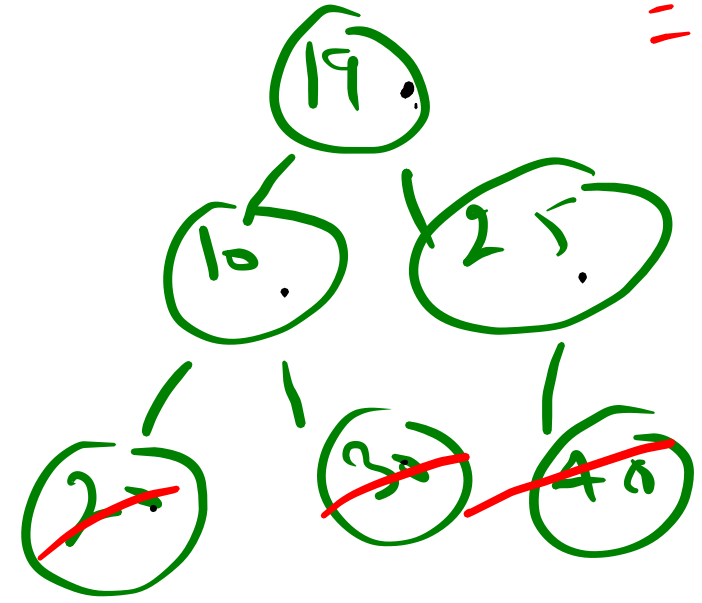
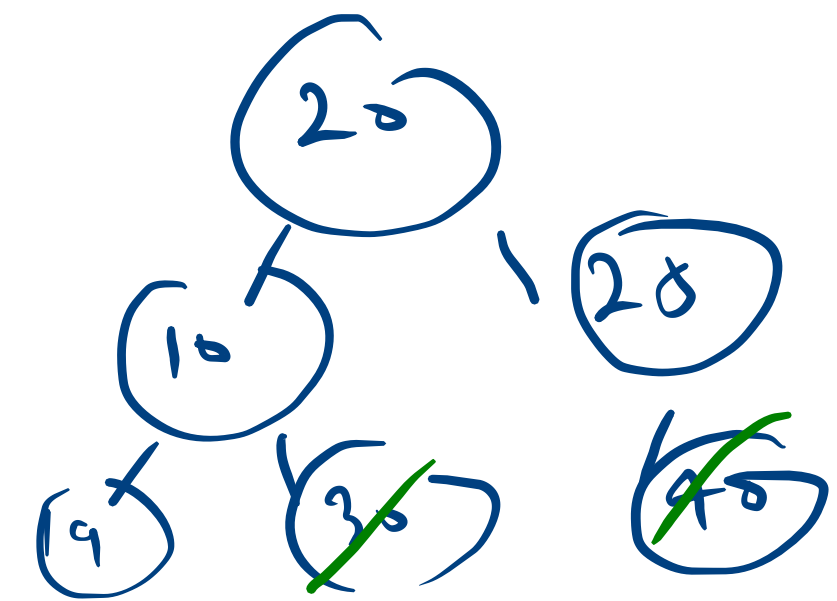
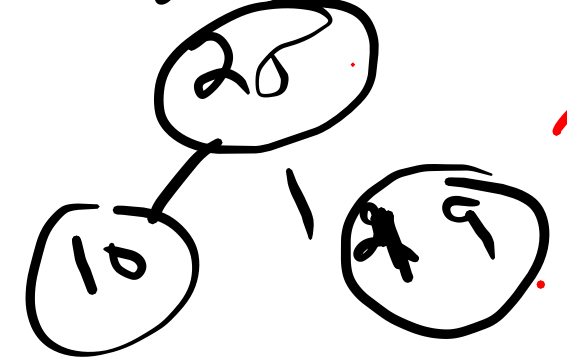
$$7/2 - 1 = 1$$

$$1$$



Size = 3

$$3/2 - 1 = 0$$



① Binom Tree \rightarrow Heap??

Node* createHeap (Node* Root, int value);
{
 if (Root == NULL)
 {
 ~~Node~~ Node* (createNode (value) |
 return (Node);
 }
}

else

}