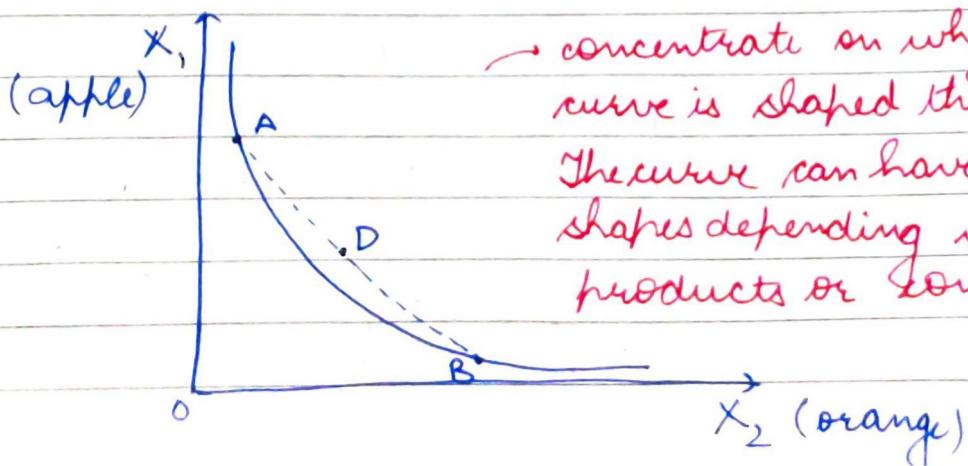


hna. & hns chapter - 1
int mech . no Consumers
Biharshik

→ CONSUMER BEHAVIOUR

→ ORDINAL THEORY

- The theory which aims to quantify the desire of a consumer for a particular product is ordinal theory.
- It basically includes the following attributes of a consumer:
 - non-satiety - The property of a consumer, where she/he is not satisfied with the amount of product that is given is called non-satiety
 - Convex-preference - Consider 2 products : apple and orange. We will graph a kink curve on x_1 apples vs orange, given which a consumer will be happy / satisfied. This curve is believed to be convex in nature



→ concentrate on why the curve is shaped this way. The curve can have different shapes depending on both products or consumers

Now consider 2 points A and B, and if we take a weighted average, then the average will always be more desirable

$$t(A) + (1-t)B > A \text{ or } B$$

3. **Completeness** - Completeness in a consumer is when she/he decides to stick to a specific preference of products. The more the number of products the greater the confusion. But if a consumer takes a decision, she/he is likely to stick to it later on.

4. **Transitivity** - Consider 3 products x, y, z
If preference is $x > y$ & $y > z$, then $x > z$ for sure.

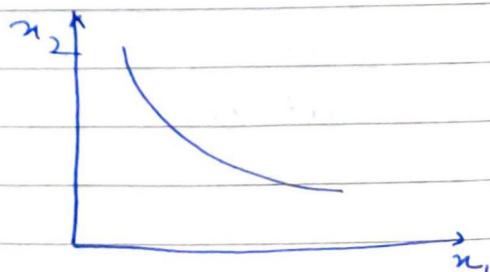
NOTE: Alfred Marshall and Paul Samuelson contributed to the ordinal theory.

→ TOTAL AND MARGINAL UTILITY

$$U = U(x_1, x_2)$$

Total utility

$$dU = U_1 dx_1 + U_2 dx_2$$

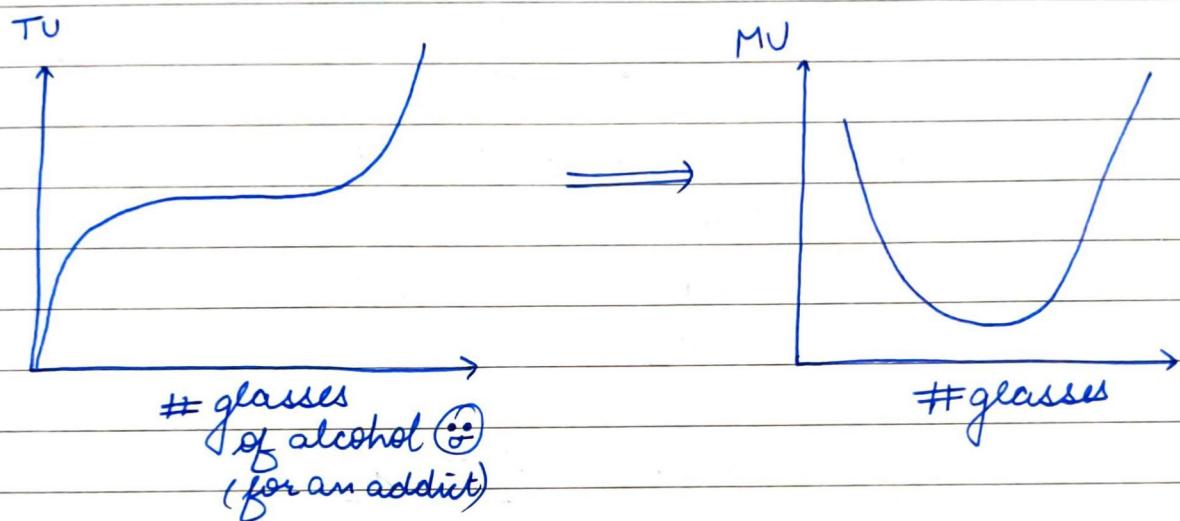


$$0 = U_1 dx_1 + U_2 dx_2 \rightarrow \text{Total utility becomes const. for indifference curve} \therefore dU=0$$

$$\Rightarrow \frac{dx_2}{dx_1} = -\frac{U_1}{U_2}$$

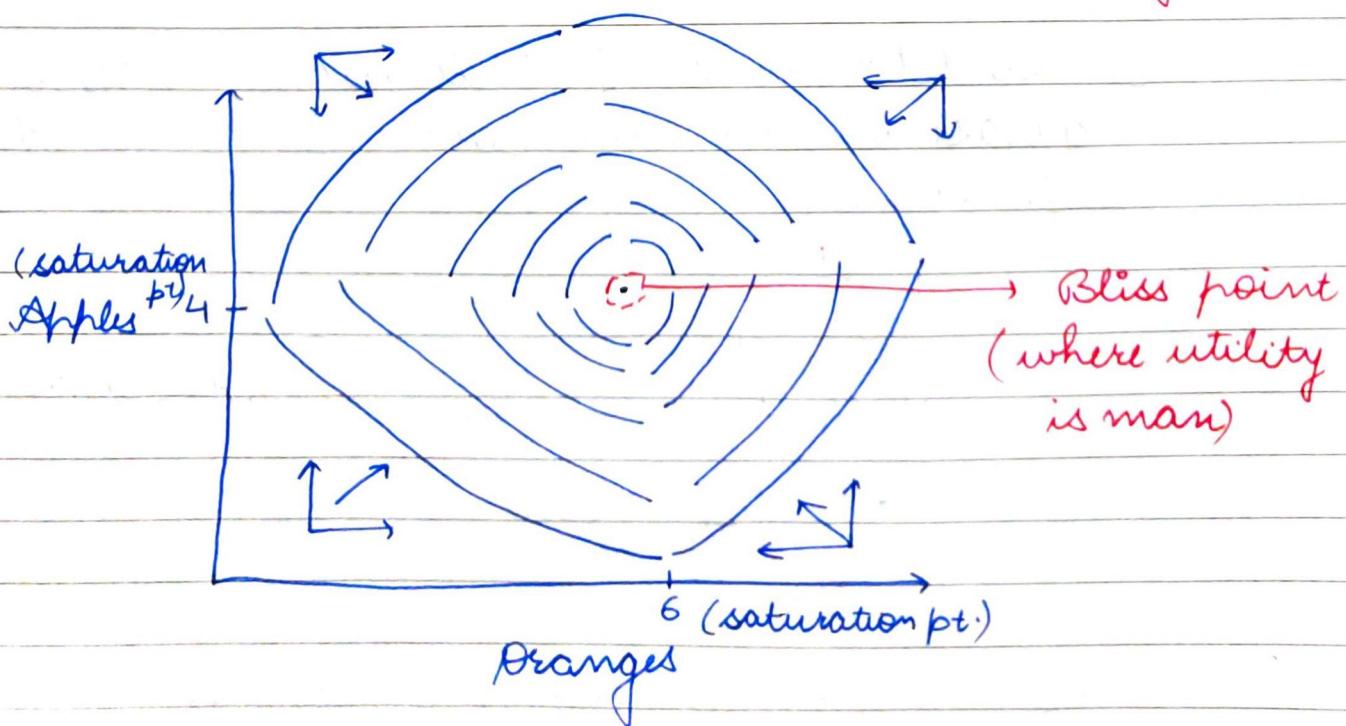
U_i = marginal utility
 $i = 1, 2$

marginal utility (for a product) is the slope of total utility vs the product curve



$$\text{marginal utility of } x_1 = \frac{\partial U}{\partial x_1}$$

Actual Utility Curve for Apples vs. Oranges



- In above graph, if we plot utility on z axis, we get a quasi-concave curve.

Consider

$$U = x_1^\alpha x_2^\beta \quad ; 0 < \alpha, \beta < 1$$

$$U_1 = \frac{\partial U}{\partial x_1} = \alpha x_1^{\alpha-1} x_2^\beta$$

$$U_2 = \frac{\partial U}{\partial x_2} = \beta x_1^\alpha x_2^{\beta-1}$$

$$U_{11} = \alpha(\alpha-1) x_1^{\alpha-2} x_2^\beta$$

$$U_{12} = \alpha \beta x_1^{\alpha-1} x_2^{\beta-1}$$

$$U_{22} = \beta(\beta-1) x_1^\alpha x_2^{\beta-2}$$

To determine if U is quasi concave or quasiconvex, we form a Bordered Hessian

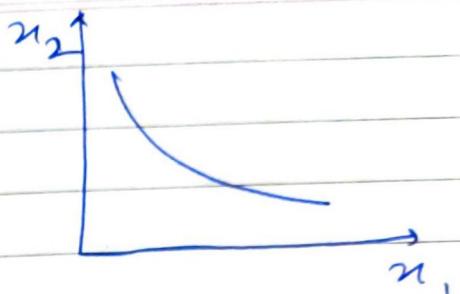
$$\begin{vmatrix} B_1 & & \\ \left(\begin{matrix} 0 & -U_{11} & -U_{12} \\ -U_{11} & U_{11} & U_{12} \\ -U_{12} & U_{12} & U_{22} \end{matrix} \right) & U_{12} & \\ & U_{12} & B_2 \end{vmatrix} \Rightarrow \text{Bordered Hessian}$$

If $B_1 \leq 0$
 $B_2 > 0$] curve is quasiconcave

(If no equality sign, $B_1 < 0$ & $B_2 > 0$, curve is strictly quasiconcave)

now, for a curve like
 $U = U(n_1, n_2)$

$$dU = U_1 dn_1 + U_2 dn_2$$



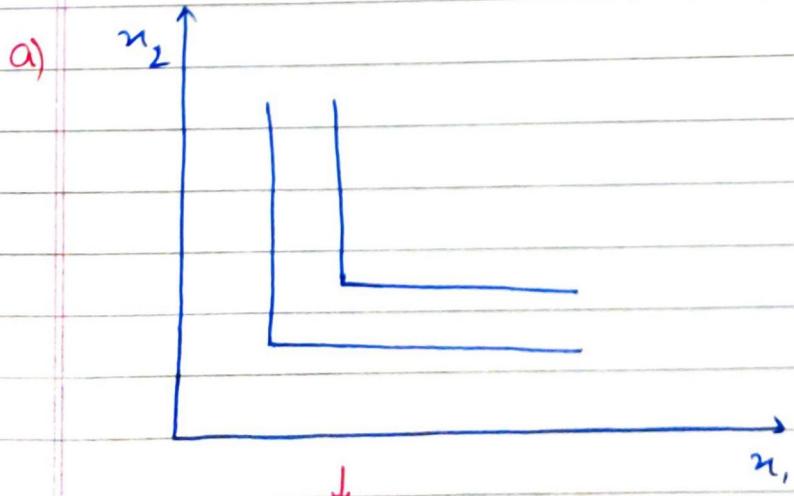
$$\frac{dn_2}{dn_1} = -\frac{U_1(n_1, n_2)}{U_2(n_1, n_2)} \quad -(i)$$

$$\boxed{\frac{d^2n_2}{dn_1^2} > 0}$$

now we will diff. (i) w.r.t. n_1 .

$$\frac{d^2n_2}{dn_1^2} = -\left[\frac{U_2 U_{11} - U_1 U_{21}}{U_2^2} \right]$$

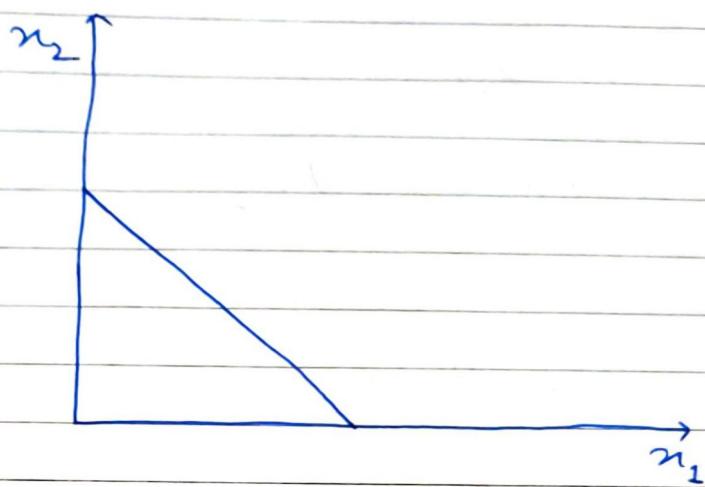
• Other types of indifference curves



Leontief curve

↓
 Perfect complements (n_1 & n_2)

b)



Perfect substitutes

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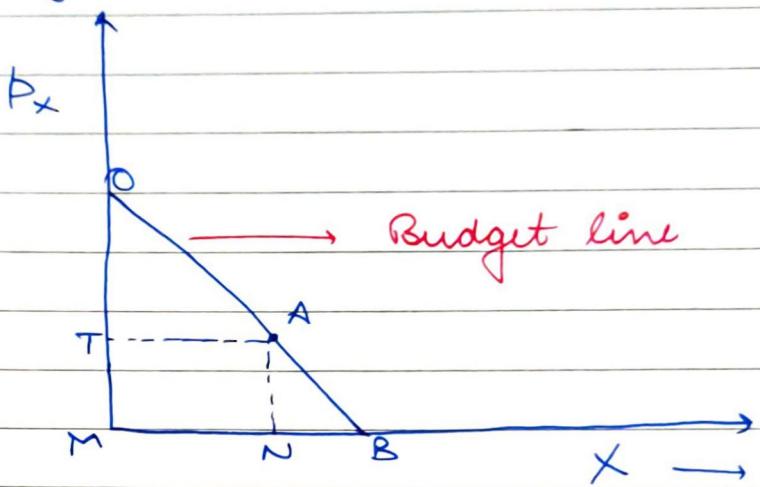
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- In graph for price vs quantity,



Now if we need to find elasticity at point A,

$$\Sigma = \frac{\Delta X}{\Delta P_x} \times \frac{P_x}{X}$$

$$= \frac{BM}{MO} \times \frac{MT}{MN}$$

$$\Rightarrow E = \frac{BA}{AO}$$

When A is mid, $E=1$

Above A $E > 1$

Below A $E < 1$

at B, $E=0$

at O, $E=\infty$

- If Q is demand & M is income of the consumer
then $\frac{\partial Q}{\partial M} \times \frac{M}{Q}$ is price of a product

$$\frac{\partial Q}{\partial M} \times \frac{M}{Q} > 1 \Rightarrow \text{Luxury good}$$

$$\frac{\partial Q}{\partial M} \times \frac{M}{Q} < 0 \Rightarrow \text{Inferior good}$$

$$0 < \frac{\partial Q}{\partial M} \times \frac{M}{Q} < 1 \Rightarrow \text{Normal good}$$

Q: $M = p_n X + p_y Y$ given. Prove that both ~~X~~ X and Y can't be luxury goods. (p_n & p_y are const.)

Ans. $\frac{dM}{dM} \neq p_n \frac{dx}{dM} + p_y \frac{dy}{dM}$

$$\frac{dM}{dM} = p_n \frac{\partial X}{\partial M} + p_y \frac{\partial Y}{\partial M} = 1$$

Taking derivative on both sides

$$dM = p_n dx + p_y dy$$

$$\frac{dM}{M} = p_n \frac{dx}{M} + p_y \frac{dy}{M}$$

$$\Rightarrow 1 = p_n \frac{dx}{dM} + p_y \frac{dy}{dM}$$

$$\Rightarrow 1 = \frac{p_n X}{M} \frac{dX \times M}{dM} + \frac{p_y Y}{M} \frac{dY \times M}{dM}$$

$$\Rightarrow 1 = \eta_x \frac{p_n x}{M} + \eta_y \frac{p_n y}{M}$$

Let $\frac{p_n x}{M} = \alpha$ then $\frac{p_n y}{M} = 1 - \alpha$

$$\therefore 1 = \eta_x \alpha + \eta_y (1 - \alpha)$$

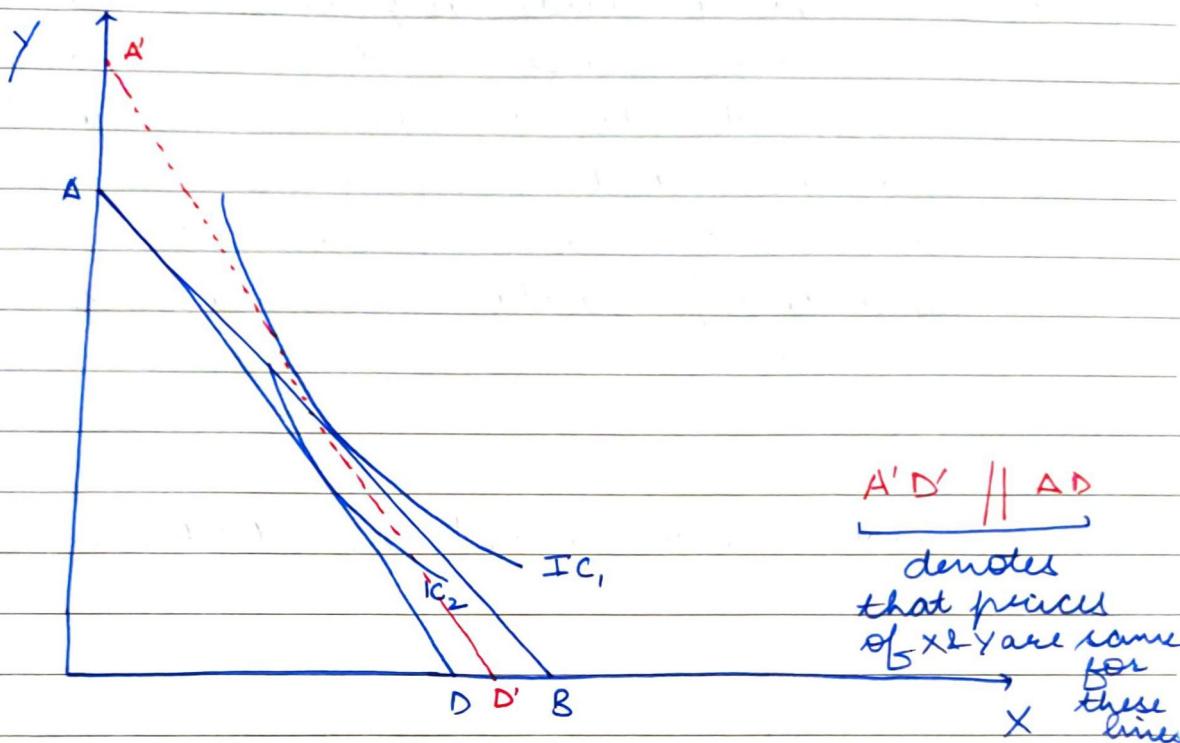
\therefore Clearly η_x & η_y can't both be > 1 or else the eqⁿ won't hold. \therefore both can't be luxury. Hence proved.



SUBSIDY

- There are different theories as to in what manner subsidies can be given to the consumers: in cash or in kind.
- Microeconomic theories by Slutsky and Hicks proved that cash form of subsidy can be better.
- Consider 2 products X and Y. We have a budget line as per ~~per~~ the income of consumer & an indifference curve. Where the indifference curve touches the budget line, it is called optimum point.

AB - Budget line (Initial)



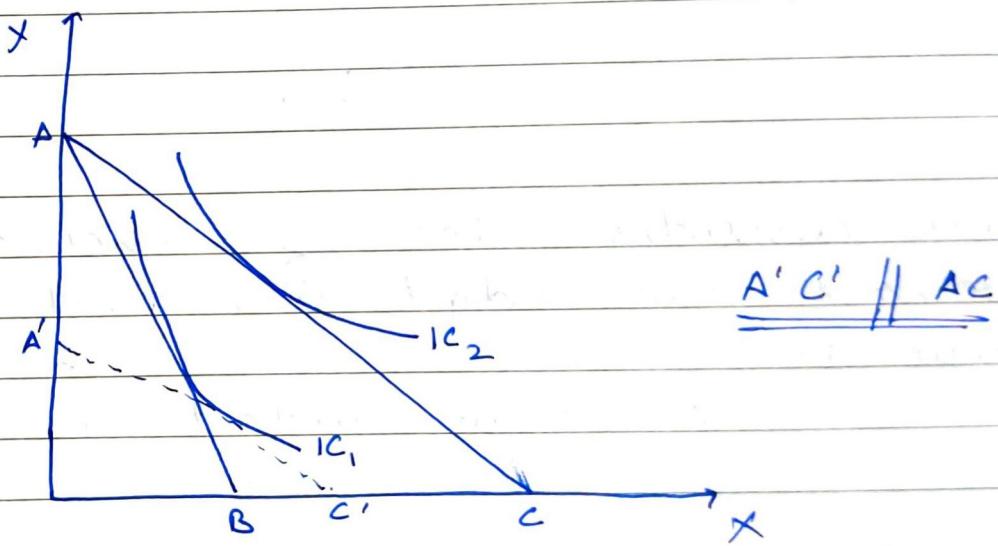
- now consider price of x increases, then we have new budget line and consequently new IC

AD - new budget line after hike in x

- Hicksian theory suggests that we give that amount of money to the consumer as subsidy such that the new budget line after subsidy will touch original IC.

$A'D'$ - new budget line after subsidy

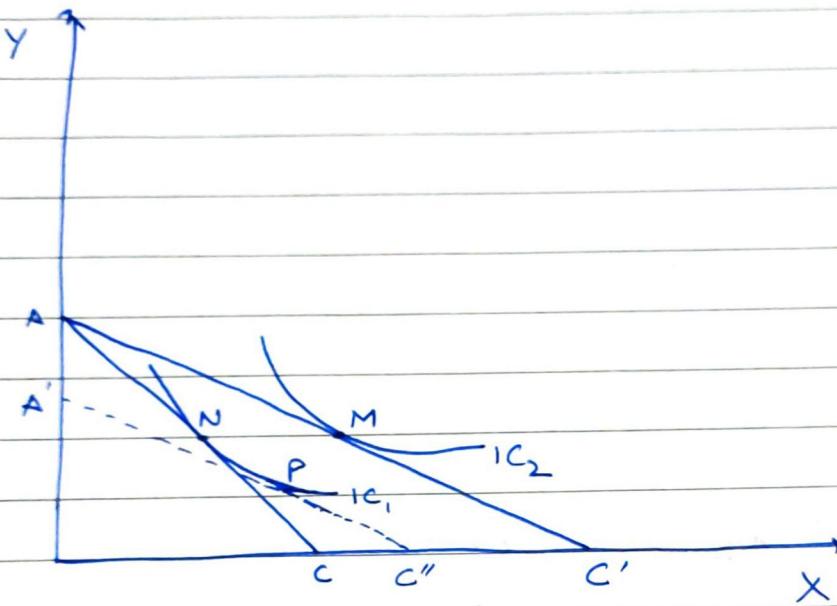
- The theory also applies on fall of prices in which case govt' increases taxes. This needs to be done because, there is a limited supply of the product, i.e. we don't have unlimited reserves to cope up with increasing demands
 ∵ ~~Prices~~ demand needs to be taken down. e.g. oil.
- ∴ we have a representation like



IC_1 = old IC

IC_2 = new IC after price change (no tax like)

- consider the previous case



$$NM = \bar{NP} + \bar{PM}$$

↓
price
effect

↓
income effect

↓
substitution
effect

↓
price of products
is const.

$\left| \frac{\partial x}{\partial p_n} \right|_{p_1 \text{ and } M \text{ are constant}}$ = price effect

PROOF: (First read note on next page)

$$\mathcal{L} = f(q_1, q_2) + \lambda [y_0 - p_1 q_1 - p_2 q_2]$$

Lagrange eqn

utility function

budget line

$$\frac{\partial \mathcal{L}}{\partial q_1} = \mathcal{L}_1 = \underbrace{f_1}_{B_1} - \lambda p_1 = 0 \quad (i)$$

$$\frac{\partial \mathcal{L}}{\partial q_2} = \mathcal{L}_2 = \underbrace{f_2}_{B_2} - \lambda p_2 = 0 \quad (ii)$$

$$\frac{\partial \mathcal{L}}{\partial \lambda} = \mathcal{L}_3 = y_0 - p_1 q_1 - p_2 q_2 = 0 \quad (iii)$$

proof continued 3 pages later

NOTE:

Proof continued

Consider $f(q_1, q_2) = q_1 q_2$ Ques:

$$U = x_1^{1/3} x_2^{2/3}; p_1 = 5 \text{ & } p_2 = 3 \quad y = 100$$

 Find optimal value ~~dimensions~~ of x_1 and x_2

Ans:

$$V = x_1^{1/3} x_2^{2/3} + \lambda(y - p_1 x_1 - p_2 x_2)$$

$$\frac{\partial V}{\partial x_1} = v_1 = \frac{1}{3} x_1^{-2/3} x_2^{2/3} + -\lambda p_1 = 0$$

$$\frac{\partial V}{\partial x_2} = v_2 = \frac{2}{3} x_2^{-1/3} x_1^{1/3} - \lambda p_2 = 0$$

$$\frac{\partial V}{\partial \lambda} = v_3 = y - p_1 x_1 - p_2 x_2 = 0$$

$$x_1^{1/3} = \frac{3\lambda p_1}{v_1}, \quad x_2 = (3\lambda p_1 v_1^{2/3})^{3/2}$$

$$y - p_1 v_1 - (3\lambda p_1)^{3/2} p_2 v_1 = 0$$

$$v_1 = \frac{y}{p_1 + (3\lambda p_1)^{3/2} p_2}$$

$$\frac{1}{3} n_1^{2/3} n_2^{2/3} = \lambda p_1$$

$$\frac{2}{3} n_2^{-1/3} n_1^{1/3} = \lambda p_2$$

$$\Rightarrow \frac{n_2}{2n_1} = \frac{p_1}{p_2}$$

$$\Rightarrow n_2 = 2n_1 \frac{p_1}{p_2}$$

$$y - p_1 n_1 - p_2 \frac{2n_1 p_1}{p_2} = 0$$

\Rightarrow

$$n_1 = \frac{y}{\frac{2}{3} p_1}$$

$$n_2 = \frac{2y}{3p_2}$$



Demand curves

$$\lambda p_1 = \left(\frac{1}{3}\right)^{1/3} \left(\frac{2}{3}\right)^{2/3}$$

$$\frac{1}{3} \left(\frac{2p_1}{y}\right)^{2/3} \left(\frac{2}{3}\right)^{2/3} = \lambda(p_1)^{1/3}$$

$$\Rightarrow \lambda = \frac{2}{3}^{2/3} \left(\frac{1}{p_2}\right)^{2/3} \left(\frac{1}{p_1}\right)^{1/3}$$

λ is called Marshallian.

PROOF: contd

We take derivative of (i), (ii) and (iii)

$$(i) f_{11} dq_1 + f_{12} dq_2 - b_1 d\lambda = \lambda dp_1$$

$$(ii) f_{21} dq_1 + f_{22} dq_2 - b_2 d\lambda = \lambda dp_2$$

$$(iii) -b_1 dq_1 - b_2 dq_2 + 0 = -dy_0 + q_1 dp_1 + q_2 dp_2$$

using Cramer's rule

$$dq_1 = \begin{bmatrix} \lambda dp_1 & f_{12} & -b_1 \\ \lambda dp_2 & f_{22} & -b_2 \\ -dy_0 + q_1 dp_1 + q_2 dp_2 & -b_2 & 0 \end{bmatrix}$$

D

$$dq_1 = \frac{\lambda dp_1 D_{11} + \lambda dp_2 D_{12} + (-dy_0 + q_1 dp_1 + q_2 dp_2) D_{13}}{D}$$

D

For income effect $dp_1 = dp_2 = 0$

$$\frac{dq_1}{\partial y_0} = -\frac{D_{13}}{D} \rightarrow \text{income effect} \Rightarrow dp_1 = dp_2 = 0$$

For substitution effect

$$U = f(q_1, q_2)$$

$$dU = 0 = f_1 dq_1 + f_2 dq_2$$

$$\Rightarrow \frac{dq_2}{dq_1} = -\frac{f_1}{f_2}$$

Also income is constant for substitution.

$$\therefore p_1 dq_1 + p_2 dq_2 = dy = 0$$

$$\therefore \text{in } \underline{\text{re}}, -dy_0 + q_1 dp_1 + q_2 dp_2 = 0$$

\therefore ~~Qs x Qd~~

$$dq_1 = \cancel{\lambda dp_1 D_{11} + \lambda dp_2 D_{12}} + (-dy_0 + q_1 dp_1 + \dots)$$

since $dp_2 = 0$ (price of q_2 never changes)

$$\boxed{\frac{dq_1}{dp_1} = \frac{\lambda D_{11}}{D}} \rightarrow \text{substitution effect}$$

For price effect

Price of first good and income does not change

$$dq_1 = \frac{\lambda dp_1 D_{11}}{D} + \frac{q_1 dp_1 D_{21}}{D}$$

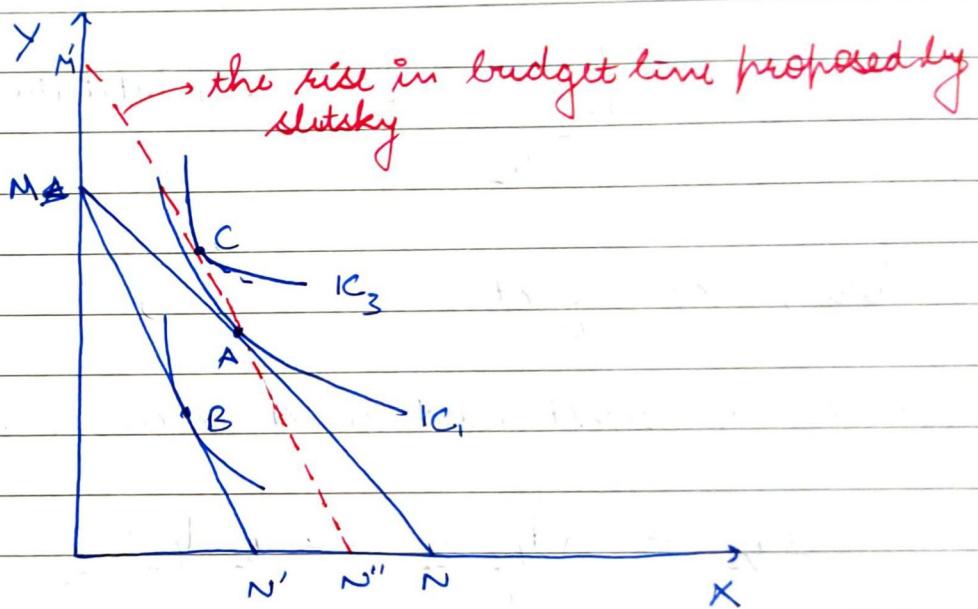
$$\boxed{\frac{dq_1}{dp_1} = \frac{\lambda D_{11}}{D} + \frac{q_1 D_{21}}{D}} \rightarrow \text{price effect}$$

\downarrow \downarrow

substitution effect income effect

→ SLUTSKY THEORY FOR SUBSIDY

- Slutsky suggested that the amount of subsidy to be given should be of that amount such that the consumer can buy the old combination of items



- When we put up a Slutsky rise in budget line by giving subsidy, it is possible to obtain higher utility by going to IC_3 at point C. But it is also possible for consumer to stay at A.
 \therefore the consumer can go at any point b/w A and C. But this ~~would~~ movement only be possible if we have a cash subsidy given to the consumer which increases her/his options. \therefore Cash subsidy for compensating upto point A is ideally better than Hicksian Theory.

- Practically, a gift card is of greater utility to consumer than a specific gift.

Ques: $U = x^\alpha y^\beta$ $M = p_x x + p_y y$ $0 < \alpha, \beta < 1$

maximising utility w.r.t. budget constraint

Sols: $Z = x^\alpha y^\beta + \lambda (M - p_x x - p_y y)$

$$\frac{\partial Z}{\partial x} = z_x = \alpha x^{\alpha-1} y^\beta - \lambda p_x = 0$$

$$\frac{\partial Z}{\partial y} = z_y = \beta y^{\beta-1} x^\alpha - \lambda p_y = 0$$

$$\frac{\partial Z}{\partial \lambda} = z_\lambda = M - p_x x - p_y y = 0$$

Solving, we get soln

$$x^* = \frac{M\lambda}{(\alpha+\beta)p_x}$$

$$y^* = \frac{M\beta}{(\alpha+\beta)p_y}$$

$$\therefore \text{max utility} = U^* = (x^*)^\alpha (y^*)^\beta$$

$$= \left(\frac{M\alpha}{(\alpha+\beta)p_x} \right)^\alpha \left(\frac{M\beta}{(\alpha+\beta)p_y} \right)^\beta$$

- From answer to previous question

$$\frac{\frac{\partial U^*}{\partial p_n}}{\frac{\partial U^*}{\partial M}} = \frac{x^* (p_n)^\alpha (-\alpha) p_n^{-\alpha-1}}{\frac{x^*}{M^{\alpha+\beta}} (\alpha+\beta) M^{(\alpha+\beta)-1}}$$

$$= -\frac{\alpha M}{p_n(\alpha+\beta)} = -x^*$$

$$\frac{\frac{\partial U^*}{\partial p_n}}{\frac{\partial U^*}{\partial M}} = -\frac{\alpha M}{p_n(\alpha+\beta)} = -x^*$$

demand curve

- Like we maximised U wrt budget, we can also be asked to minimize budget wrt. given U^*

minimize $p_1 n_1 + p_2 n_2$ subject to $U^* = n_1 n_2$

For this we use Lagrange again

$$L = p_1 n_1 + p_2 n_2 + \mu [U^* - n_1 n_2]$$

$$\frac{\partial L}{\partial x_2} = p_1 - \mu x_2 = 0$$

$$\frac{\partial L}{\partial x_1} = p_2 - \mu x_1 = 0$$

$$\frac{\partial L}{\partial \mu} = U^* - x_1 x_2 = 0$$

From above eqⁿs,

$$x_1^* = \sqrt{\frac{p_2}{p_1} U^*}$$

$$x_2^* = \sqrt{\frac{p_1}{p_2} U^*}$$

now we find expenditure (budget) as calculated optimally

$$E^* = p_1 x_1^* + p_2 x_2^*$$

$$\cancel{E^*} = \cancel{p_1} \cancel{x_1^*} + \cancel{p_2} \cancel{x_2^*}$$

$$\Rightarrow E^* = 2 \sqrt{p_1 p_2 U^*}$$

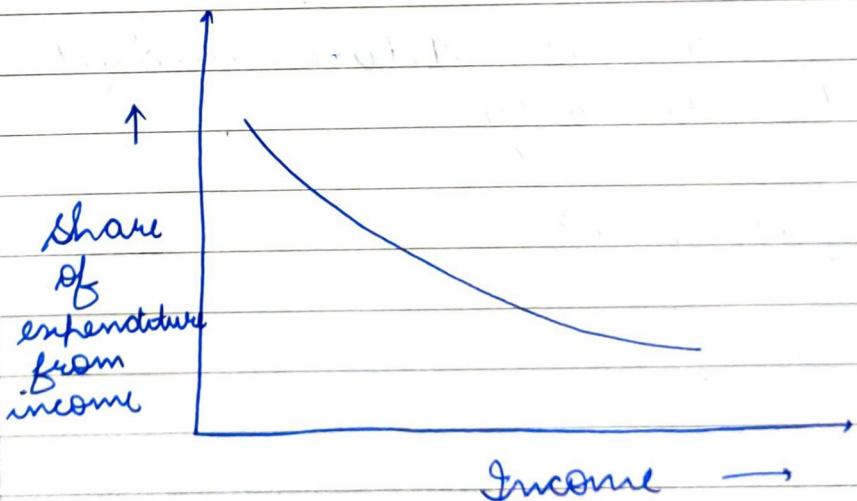
From this,

$$\frac{\partial E^*}{\partial p_1} = x_1^* = \sqrt{\frac{p_2}{p_1} U^*}$$

→ Shephard's Lemma

→ ENGEL CURVE (INCOME RISE AND CONSUMPTION) F

- For a poor man, he/she spends a high % amount of money ^{earned} on food.
- But as income rises, that percentage decreases (given that the food requirements are met). If the percentage rises, this shows insufficiency in amount of food for the individual.
- On a society/community level, for a good economy, this percentage (for all the population combined) must decrease with income.



This is Engel's Law.

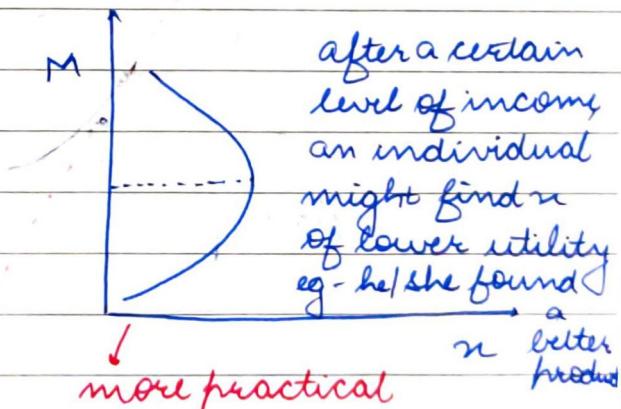
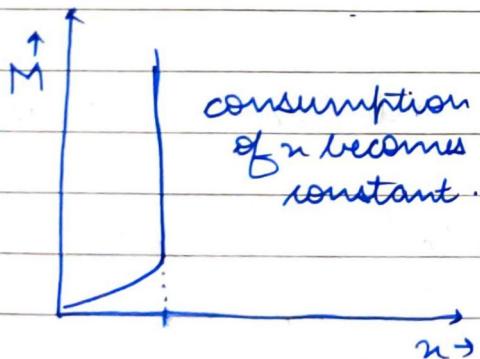
Ques: Own price elasticity of $n = 0.3$ $= \frac{dn}{dp_n} \frac{p_n}{n}$

Share of expenditure on $n = 70\%$ $= \frac{p_n n}{M} = 0.7$

Cross ~~price~~ price elasticity b/w n and $y = ?$

$$\frac{dn}{dpy} \frac{p_y}{n}$$

- **Engel curve:** It is a curve b/w the income versus consumption of a good for an individual. It can be of different shapes.



Ques: Draw a demand curve for which elasticity remains constant.

Ans: $\frac{dn}{dp_n} \frac{p_n}{n} = -c$

Integrating
 $\Rightarrow \ln n = -c \ln p_n + \ln c'$

$$\Rightarrow n = c'/p_n^c$$

$$\Rightarrow np_n^c = c'$$

→ CONSUMPTION VS LEISURE LINE

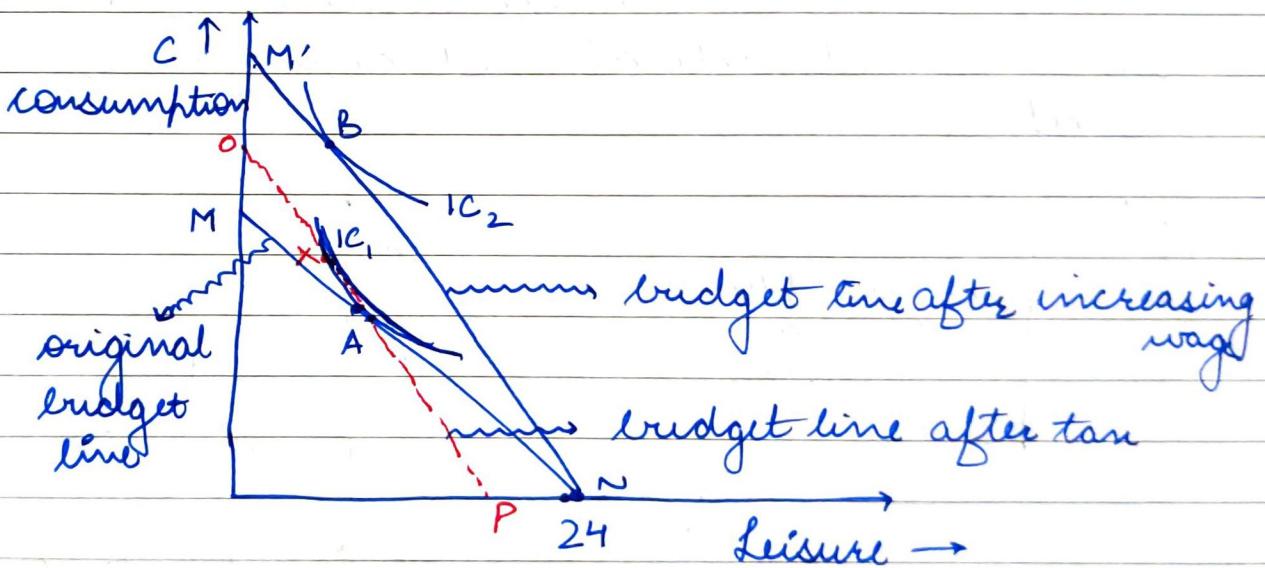
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$$pc = M + (24 - L)w$$

consumption

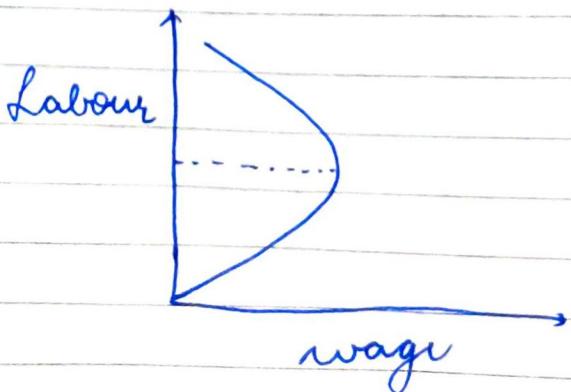
money from
savings/hereditary L = Leisure hours w = wage/hour

Any increase in wage increases consumption



$\vec{AX} \Rightarrow$ subⁿ effect }
 $\vec{XB} \Rightarrow$ Income effect } $\Rightarrow \vec{AB}$ = total effect

•



Ques: H.W wala

Ans: given

Own price elasticity = $0.3 = e_x$
 share of expenditure on $x = 70\%$
 cross price elasticity b/w x and y

now

$$M^* = p_x n + p_y y \quad (p_y \text{ & } M \text{ are const.})$$

$$\frac{dM}{dp_x} = n + \frac{dn}{dp_x} p_x + \frac{dy}{dp_x} p_y + 0$$

$$0 = n + \frac{dn}{dp_x} p_x + \frac{dy}{dp_x} p_y$$

$$\Rightarrow 0 = 1 + \frac{dn}{dp_x} \frac{p_x}{n} + \frac{dy}{dp_x} \frac{p_y}{n}$$

Multiply both sides by $\frac{n p_x}{M}$

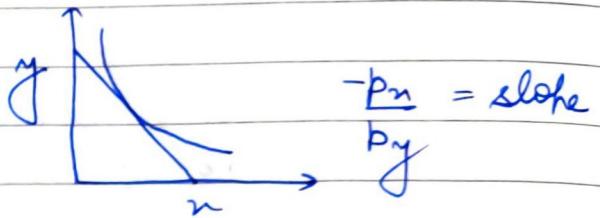
$$0 = \frac{n p_x}{M} + \frac{dn}{dp_x} \frac{p_x^2}{M} + \frac{dy}{dp_x} \frac{p_y p_x}{M}$$

use

$$\alpha n_1 + (1-\alpha) n_2 = 1$$

• REVISION

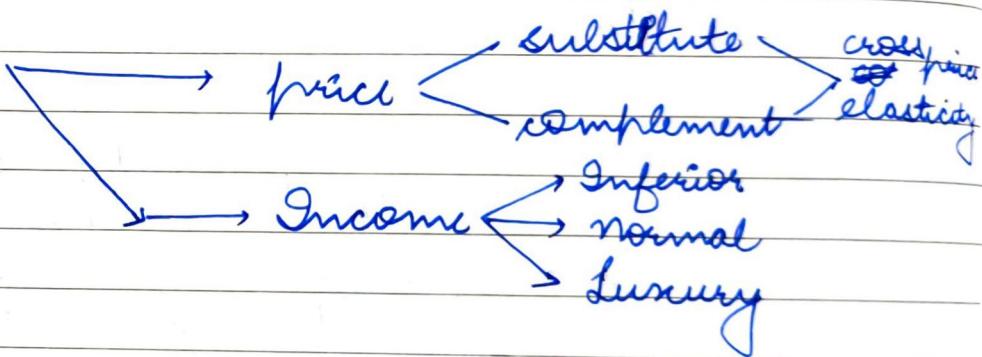
i) Indifference curve



ii) Lagrange \rightarrow Optimization under linear budget constraint.

iii) Demand curve $\rightarrow x, y$

iv) Elasticity



v) Engel curve

$$\text{vi) } TE / PE = SE + IE$$

vii) Backward bending individual labour supply curve

viii) Consumer surplus.

→ EXCEPTIONS TO LAW OF DEMAND

- i) **Bandwagon effect**: every consumer nearly is consuming it, so an individual consumer blindly consumes it. It is also called **herd effect**. eg - placement chahiye
kyuki salko chahiye
- ii) **Snob effect**: whatever others ~~are~~ are consuming, an individual does not want it anymore. eg - "I don't want placement whatsoever. See the case"
- iii) **Conspicuous consumption (Veblen effect)**: An individual wants an expensive object just for the sake of things like social status. It is different from bandwagon in terms of price which is not a factor in Bandwagon effect. eg - people buying an expensive phone.
- iv) **Giffen good**: In Ireland, during 1920's potatoes started getting expensive. But since it is a staple diet there, ~~prices~~ demand did not fall. Rather it increased (for not very concrete reasons).

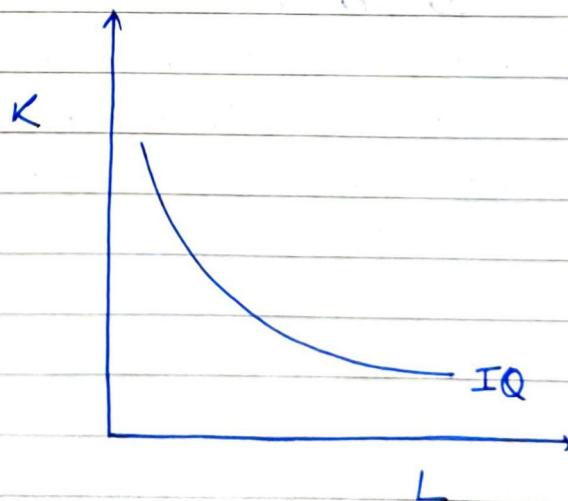
Chapter-2 Production

→ ISOQUANT

- Anything which can be used in production of a product can be divided into 2 categories
 - K (capital) - (machinery, money, ^{intell.})
 - L (Labour) - (effort, men/women)
- Output or production is dependent on these 2 factors

$$Q = f(K, L)$$

- A curve on K vs L graph for which Q or output remains the same is called isoquant



NOTE: Short run - A period in which we can vary only one of K & L if there is a constraint
 Long run - we can vary both K & L

NOTE: Isoquant is analogous to indifference curve

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Page _____

- $Q = f(K, L)$

$$dQ = f_K dK + f_L dL$$

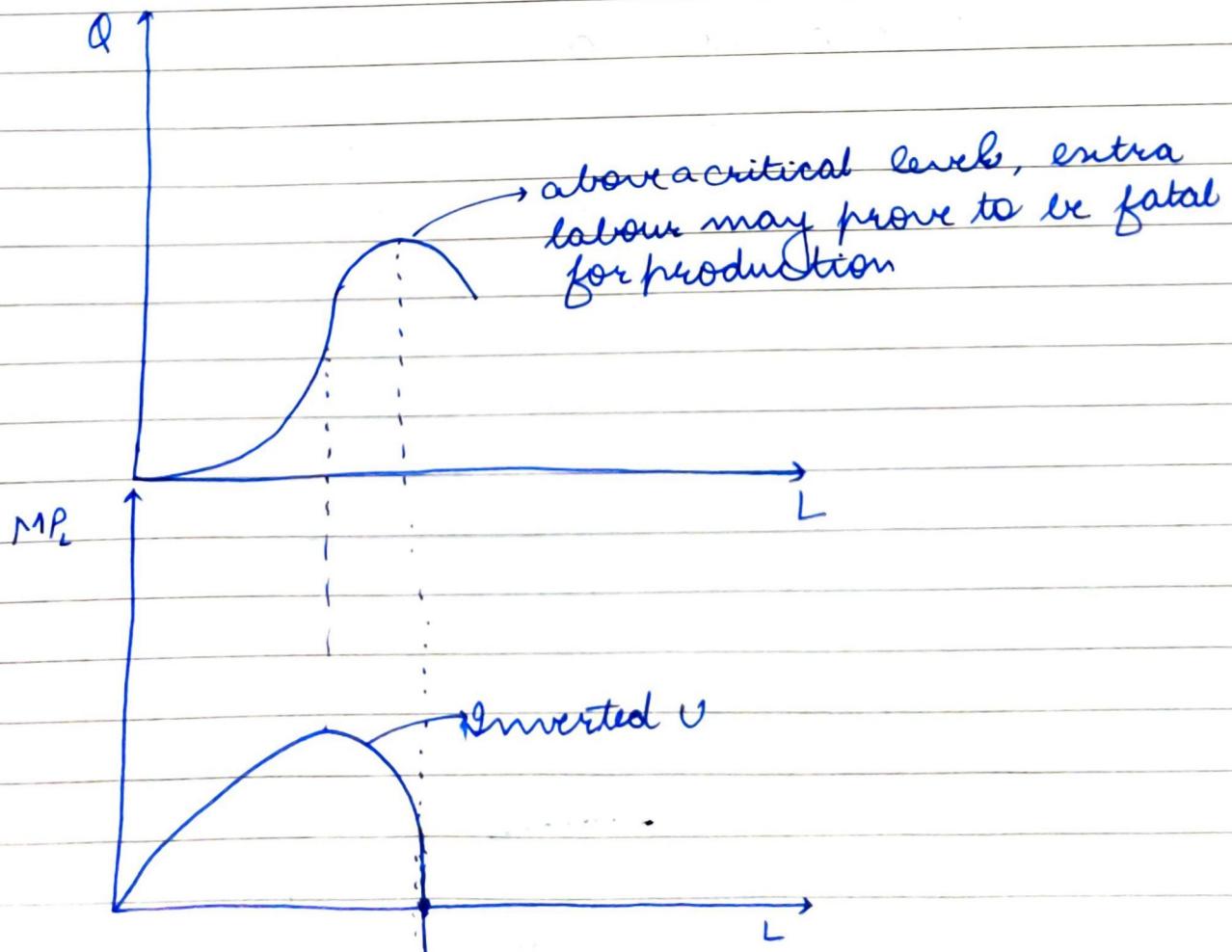
$$\boxed{\frac{dK}{dL} = -\frac{f_L}{f_K}}$$

\rightarrow MRTS (marginal Rate of technical substitution)

$$f_L = \frac{\partial f}{\partial L} = MP_L \rightarrow \text{marginal product of } L$$

$$f_K = \frac{\partial f}{\partial K} = MP_K \rightarrow \text{marginal product of } K$$

- consider the case of short run, lets say K is fixed then lets draw Q vs L & MP_L vs L



Average Product

$$AP = Q/L$$

To draw its graph (vs L), we check

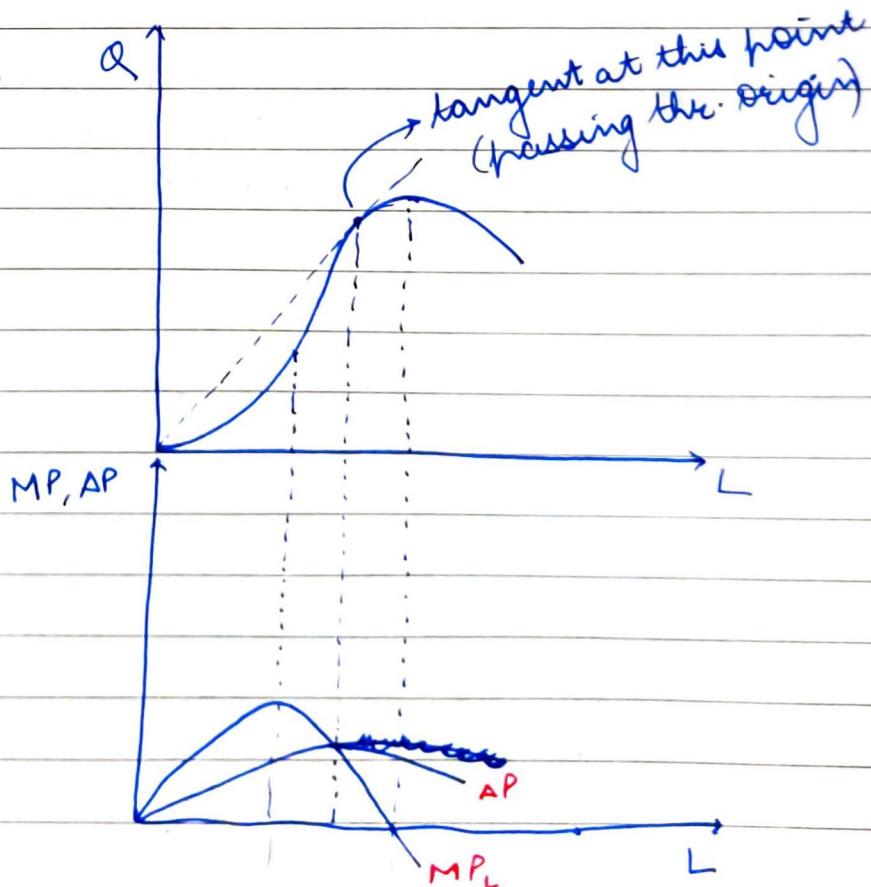
$$AP = Q/L$$

$$\frac{d(AP)}{dL} = \frac{d(Q/L)}{dL} = \frac{L \frac{\partial Q}{\partial L} - Q \frac{\partial L}{\partial L}}{L^2}$$

$$= \frac{1}{L} \left(\frac{\partial Q}{\partial L} - \frac{Q}{L} \right)$$

$$= \frac{1}{L} (MP_L - AP)$$

∴ AP reaches max when $AP = MP$



Ques: Zone 3 $\rightarrow MP_L < 0$

Zone 2 $\rightarrow \frac{dAP}{dL} < 0$

Zone 1 $\rightarrow \frac{dAP}{dL} > 0$

Where will you produce?

Ans: Not zone 3 because MP_L falls

Not zone 1 either because $\frac{dAP}{dL} > 0$ i.e.
we have better production possibility.

\therefore we produce in zone 2.

→ RETURN TO SCALE

- It refers to the change in Q w.r.t. change in K & L

- $Q = f(K, L)$

$$\lambda^k Q = (\cancel{\lambda} K, \cancel{\lambda} L) \rightarrow k > 1 \text{ increasing return to scale}$$

$$k = 1 \text{ const. Return to scale (CRS)}$$

$$k < 1 \text{ Decreasing Return to Scale (DRS)}$$

~~now~~
Ques: Identify IRS, CRS, ~~or~~ DRS for

$$Q = K + L^2$$

• NOTE: $(U = \ln x_1 + x_2)$, $p_1 x_1 + p_2 x_2 = M$

Quasi-linear utility $L = \ln x_1 + x_2 + \lambda [M - p_1 x_1 - p_2 x_2]$

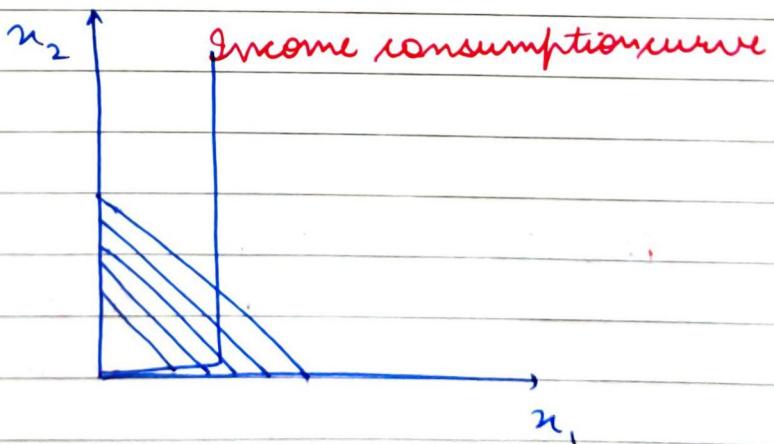
$$\frac{\partial L}{\partial x_1} = \frac{1}{x_1} - \lambda p_1 = 0$$

$$\frac{\partial L}{\partial x_2} = 1 - \lambda p_2 = 0$$

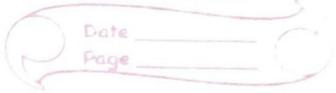
$$\frac{\partial L}{\partial \lambda} = M - p_1 x_1 - p_2 x_2 = 0$$

$$\therefore x_1^* = \frac{p_2}{p_1}; x_2^* = \frac{M - p_2}{p_2}$$

Here x_i^* does not depend on M . The reason for this is the $f^n U$



NOTE: Like budget constraint, we have cost constraint for producer.



→ PRODUCTION COSTS

K
 rent
 r
 L
 wage
 w

$$\boxed{\text{cost}(c) = wL + rK}$$

→ OPPORTUNITY COST

- Consider we have 2 options A & B only one of which we can execute. Then the opportunity cost of B would be equal to what it would cost us to not to execute B.

NOTE: Any producer looks to maximize

$$Q = L^\alpha K^{1-\alpha} \quad \text{such that } C = wL + rK$$

$\left. \begin{matrix} \\ \end{matrix} \right\}$ production ↓
 cost constraint

using Lagrange

$$L = L^\alpha K^{1-\alpha} + \lambda (C - wL - rK)$$

$$\frac{\partial L}{\partial L} = \alpha L^{\alpha-1} K^{1-\alpha} - \lambda w = 0 \quad (i)$$

$$\frac{\partial L}{\partial K} = (1-\alpha) L^\alpha K^{-\alpha} - \lambda r = 0 \quad (ii)$$

$$\frac{\partial L}{\partial \lambda} = -wL - rK + C = 0 \quad (iii)$$

Solving (i), (ii) and (iii)

~~Maximize~~

$$L^* = \frac{Cx}{w}$$

$$K^* = \frac{C(1-\alpha)}{r}$$

$$\therefore Q^* = \frac{C \alpha^{\alpha} (1-\alpha)^{1-\alpha}}{w^{\alpha} r^{1-\alpha}}$$

→ optimal production

Ques:

$$Q = L + 2K \quad \text{s.t.} \quad C = wL + rK$$

Ans.

$$L = L + 2K + \lambda (C - wL - rK)$$

$$\frac{\partial L}{\partial L} = 1 - \lambda w = 0$$

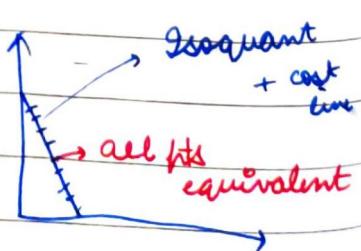
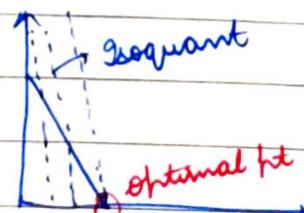
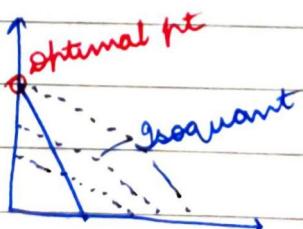
$$\frac{\partial L}{\partial K} = 2 - \lambda r = 0$$

$$\frac{\partial L}{\partial \lambda} = C - wL - rK = 0$$

Both the cases

This is unsolvable as such

3 cases may arise



→ COSTS IN BUSINESS

- Before starting a business, there is a fixed cost involved to start it. There is a variable cost after that depending on output.

$$\text{Total Cost} = \text{Fixed Cost} + \text{Variable cost}$$

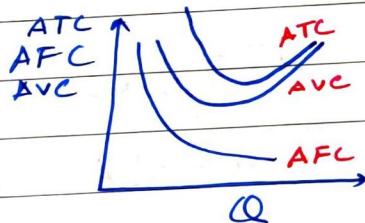
$$\frac{TC}{Q} = \frac{FC}{Q} + \frac{VC(Q)}{Q}$$

; Q = Output produced

$$ATC = AFC + AVC$$

average total cost average fixed cost average variable cost

$$AFC = \frac{TFC}{Q}$$



$$TC = WL + \bar{K}$$

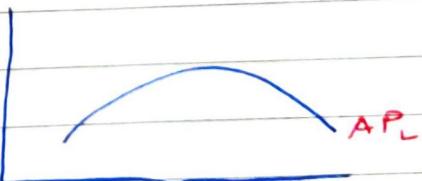
(consider $K = \text{const}$ for short run)

$$\Rightarrow TC = TVC + TFC$$

$$\Rightarrow \frac{IVC}{Q} = \frac{WL}{Q}$$

$$\Rightarrow AVC = \frac{W}{Q/L}$$

$$\boxed{AVC = \frac{W}{APL}}$$



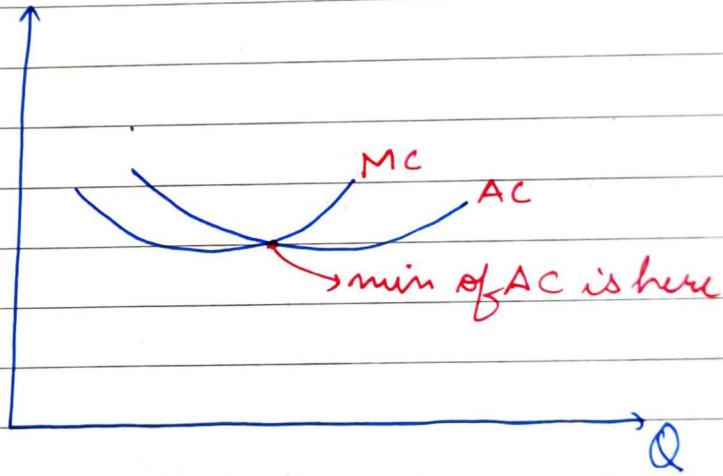
$$MC = \frac{\partial C}{\partial Q}$$

$$AC = C/Q$$

$$\underline{AC} = C/Q$$

$$\Rightarrow \frac{d(AC)}{dQ} = \frac{1}{Q} [MC - AC]$$

$$\Rightarrow \boxed{\frac{d(AC)}{dQ} = \frac{1}{Q} [MC - AC]}$$



→ PROFIT MAXIMIZATION

- Total revenue $(TR) = p \times q$ → quantity

$$\text{Total cost} = C(Q) = wL + rK$$

- $\pi = \text{profit} = p \times Q - C(Q)$

$$\Rightarrow \pi(Q) = p(Q)Q - C(Q)$$

For maximizing profit, we take derivative w.r.t. Q

$$\frac{\partial \pi}{\partial Q} = \underbrace{Qp'(Q) + p(Q)}_{\text{marginal revenue}} - C'(Q), \text{ where } p'(Q) = \frac{dp}{dQ}$$

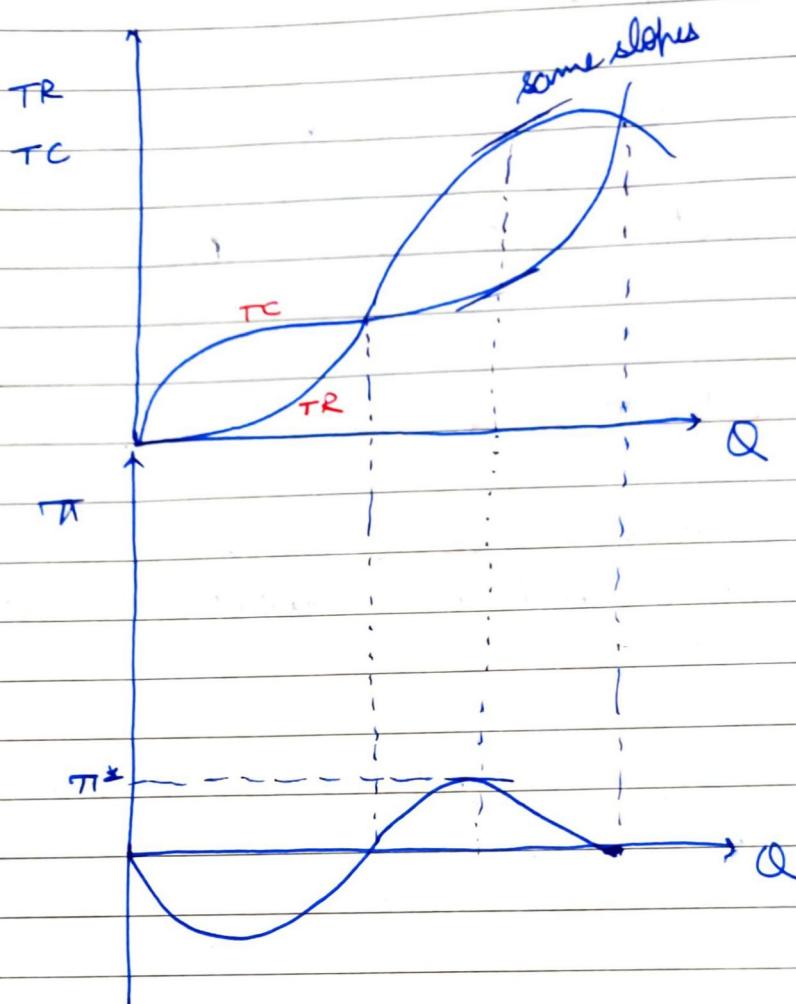
$$C'(Q) = \frac{\partial C}{\partial Q} \\ = MC$$

$$\therefore \frac{\partial \pi}{\partial Q} = MR - MC$$

For subsissa, maxima,

$$0 = MR - MC$$

$$\therefore MR = MC \text{ for maxima}$$

Ques:

$$P = 10 - 5Q$$

$$C = 10Q + 2Q^2$$

Tell optimal profit.

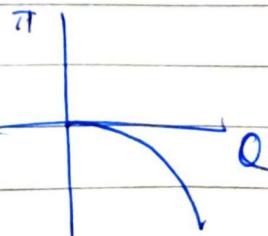
~~$$\text{Ans: } \Pi = 10Q - 5Q^2 - 10Q - 2Q^2$$~~

$$\Pi = -7Q^2$$

$$\frac{\partial \Pi}{\partial Q} = -14Q = 0$$

at $Q=0$

$$\therefore \Pi = 0$$



Ques: elasticity = -1.5
 $C = Q^2 - 10Q + 10$

Ans. $\frac{dQ}{dP} \times \frac{P}{Q} = -1.5$

$$\Rightarrow \ln Q = -1.5 \ln P + C' \quad (\text{where } C' \text{ is a constant})$$

$$\Rightarrow \ln\left(\frac{Q}{C'}\right) = -1.5 \ln P$$

$$\therefore \left(\frac{Q}{C'}\right) = P^{-1.5}$$

$$\left(\frac{K}{Q}\right)^{2/3} = P$$

$$\pi = K^{2/3} Q^{1/3} - Q^2 + 10Q - 10$$

$$\frac{1}{3} \left(\frac{K}{Q}\right)^{2/3} - 2Q + 10 = 0$$

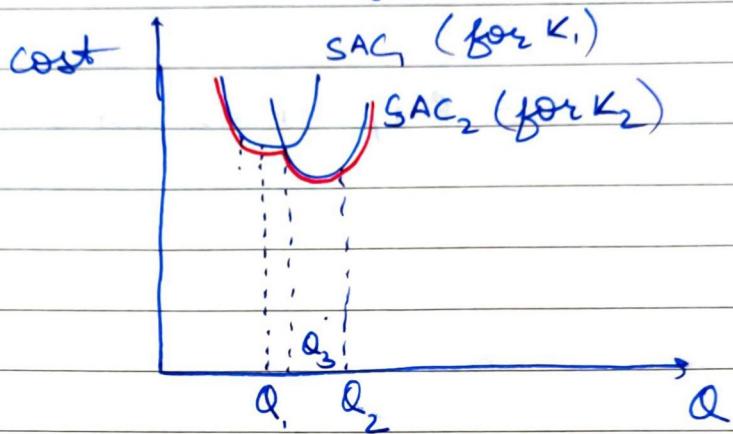
solve now \therefore (nahi hoga, bahut ganda hai $\odot\odot$)

PTO



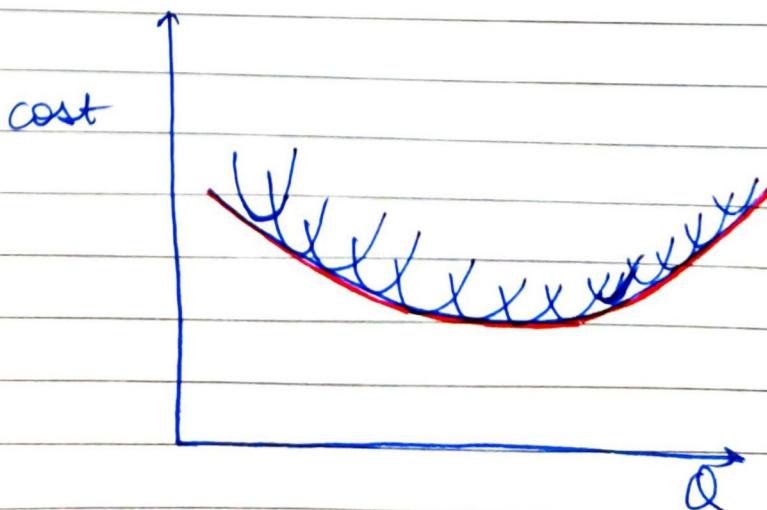
→ LONG RUN PRODUCTION

- For 2 diff. values of K , let's draw short run avg cost curves



If we are allowed to shift b/w these curves, the red one will be preferred.

- ∴ if both L & K are variable, we will have ∞ amt. of such curves and we are allowed to shift b/w them. Thus our long run cost vs quantity will look like



economics of Scope :

A
 Q_1
 $c(Q_1)$

B (2 diffⁿ locations)
 Q_2
 $c(Q_2)$

Total cost by firm = $c(Q_1) + c(Q_2) > c(Q_1 + Q_2)$
 producing in diffⁿ locations producing in same location

This is referred as economies of scope i.e., producing at one place to minimise cost.

$c(Q_1) + c(Q_2) = c(Q_1 + Q_2)$ doesn't make any diff in term of cost.

economics of Scale .

$$\underline{IC(Q_2)} - \underline{IC(Q_1)} = c(Q_1, Q_2) - c(Q_1, 0)$$

Incremental cost

$$AIC_{Q_2} = \frac{c(Q_1, Q_2) - c(Q_1, 0)}{Q_2}$$

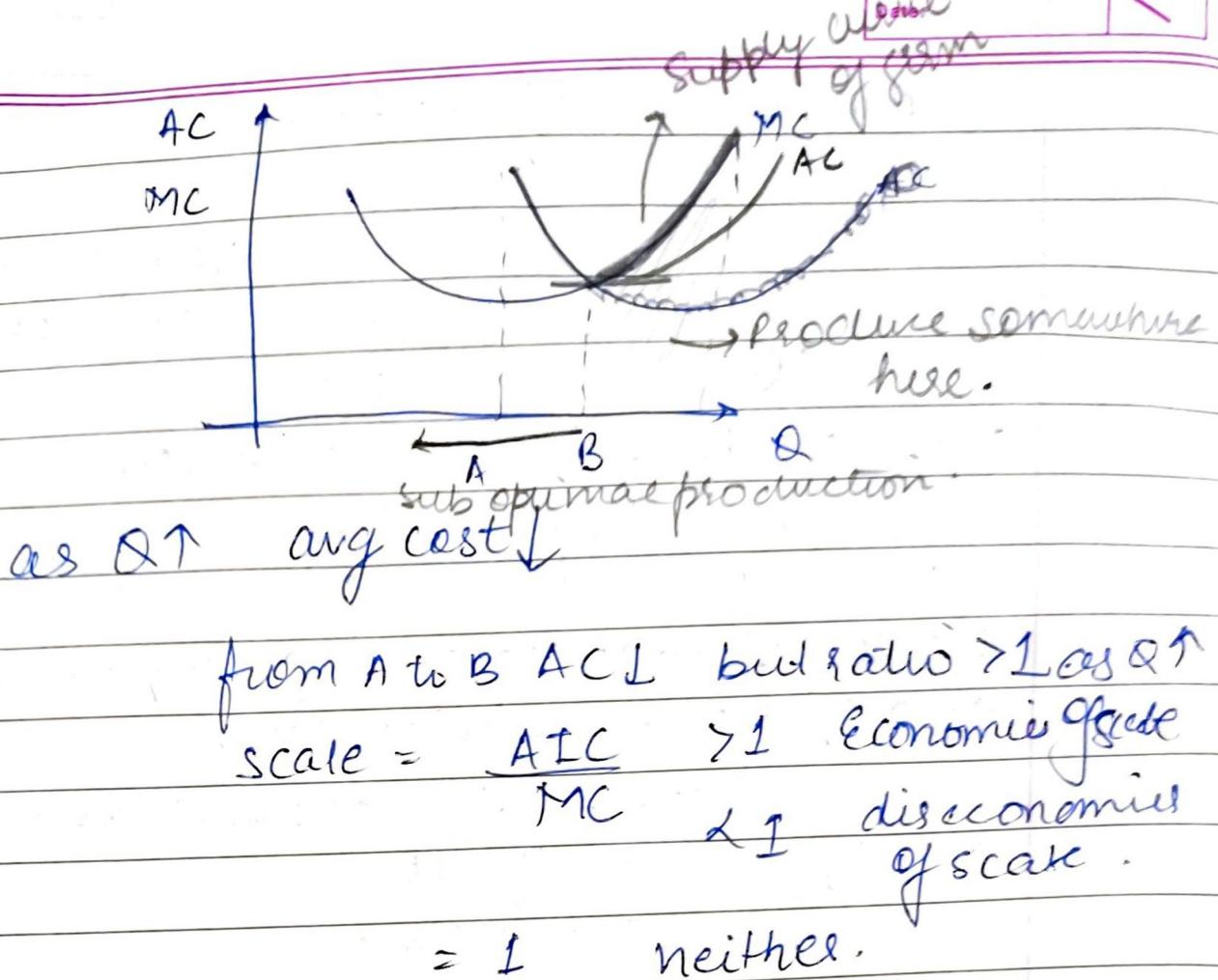
avg incremental cost for production of Q_2 .

$$MC = \frac{\Delta C}{\Delta Q_2}$$

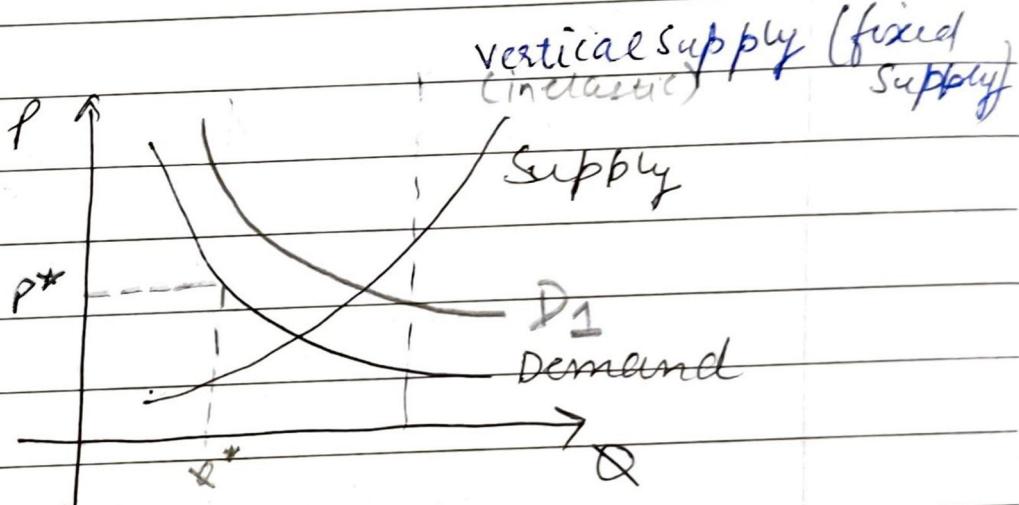
$$\text{scale} = \frac{AIC}{MC}$$

< 1	> 1
$= 1$	

economics of scale \Leftrightarrow cost fall if production ↑.

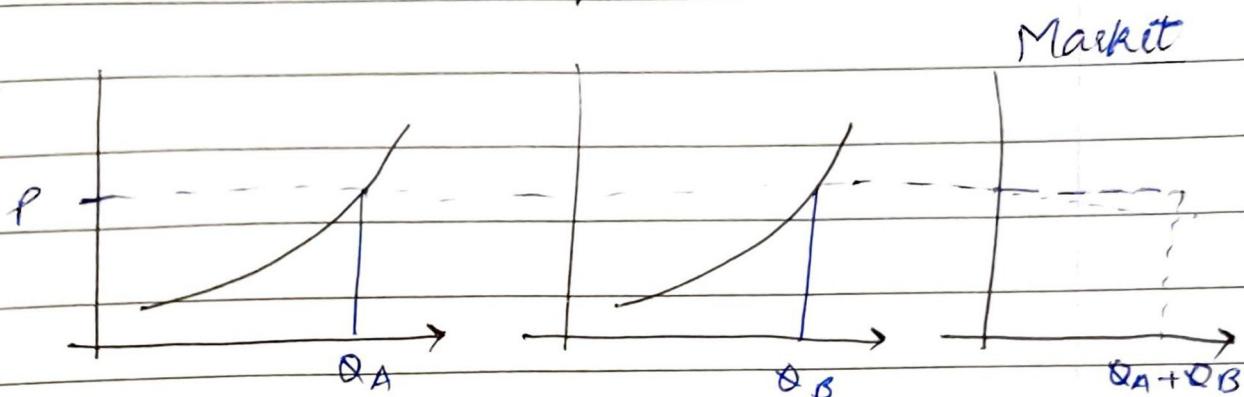


Monopoly.



$$\frac{dQ}{dP} \times \frac{P}{Q} = 0 \quad \text{for fixed supply} \quad (\because d\phi = 0)$$

when there are two suppliers.



Q :

$$Q_D = a - bp$$

quantity demanded

$$a - bp = c + dp$$

$$\frac{a - c}{b+d} = p. \quad (\text{equilibrium})$$

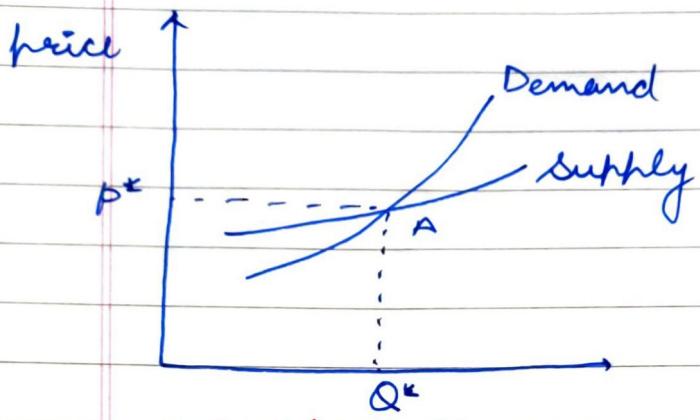
$$Q_D = a - b \left(\frac{a - c}{b+d} \right)$$

$$Q_S = c + d \left(\frac{a - c}{b+d} \right)$$

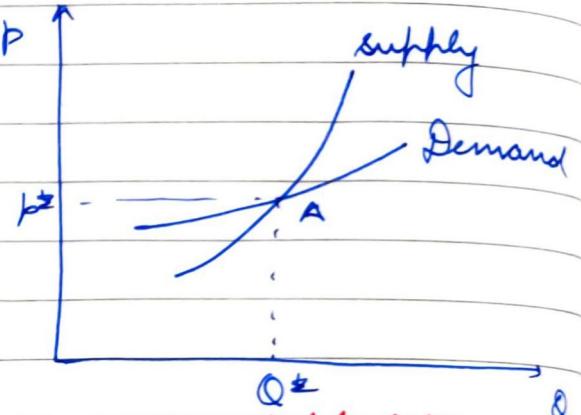
$$Q_F = \frac{ab + ad - ab + bc}{b+d} = \frac{ad + bc}{b+d} \quad Q_S = \frac{bc + ad}{b+d}$$

Cobweb model

- consider situation with +vely sloped demand curve & +vely sloped supply curve



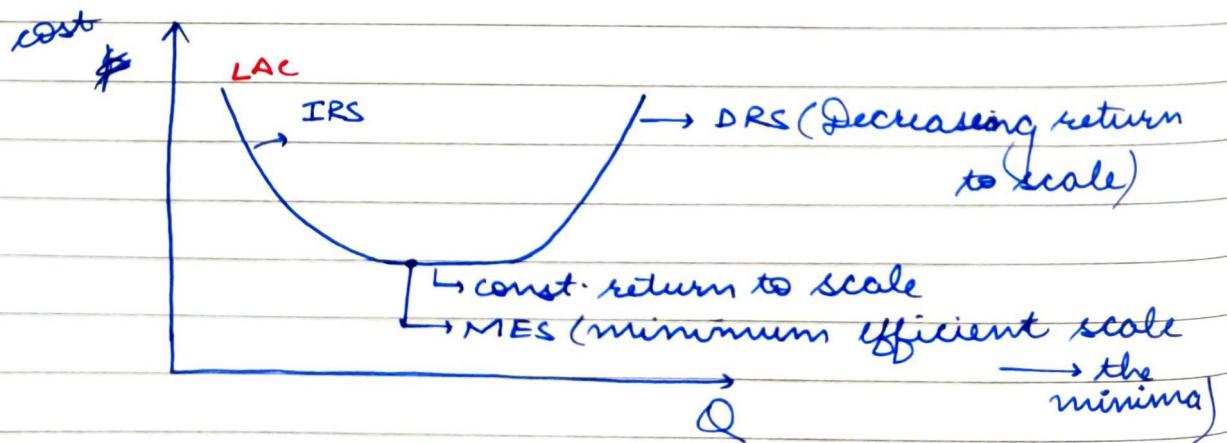
stable eq^m
above A, Demand
exceeds ∵ price
increases ↗ vice-versa



unstable eq^m
above A, demand
is low ∵ price
decrease must be
seen ∵ unstable.

- Pending topic
 $C = wL + rK$

$$AC = \frac{wL + rK}{Q} = K(wL + rK)$$



→ MARKET

- market is controlled by the sellers and their properties

• Perfect competition

monopolistic
compⁿ

monopoly

Oligopoly
(handful
of sellers
control the
market)

Duopoly
(2 sellers)

→ PERFECT COMPETITION

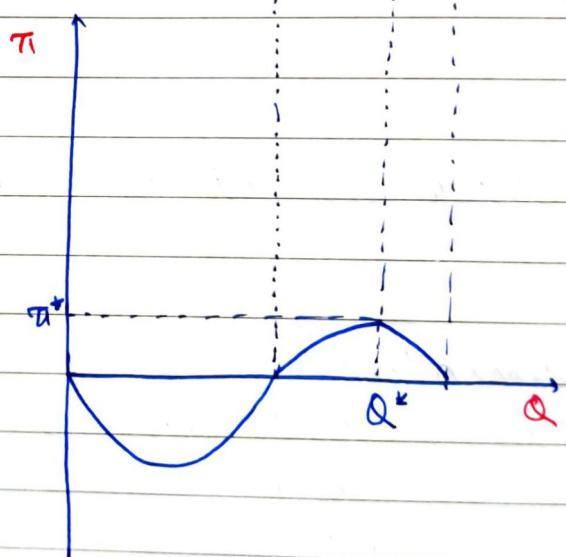
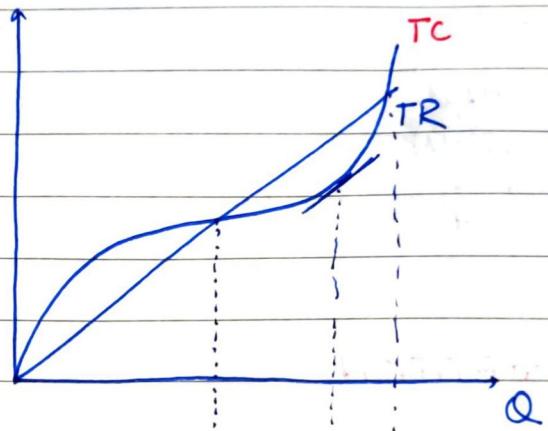
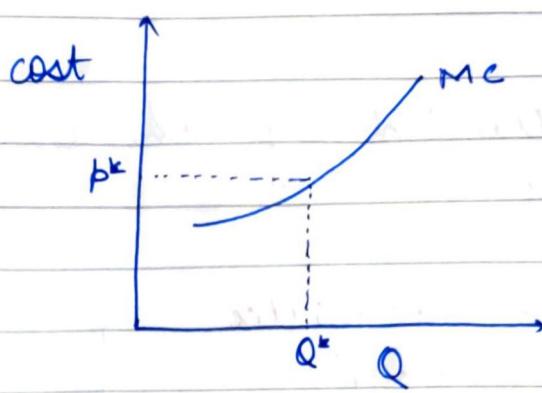
• PROPERTIES

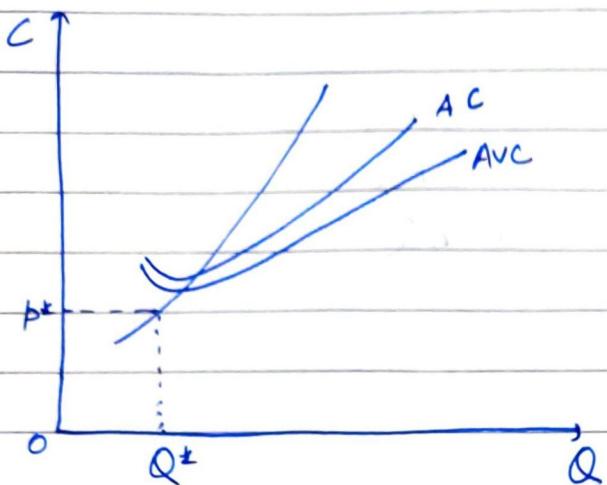
- anyone can enter or exit the market as sellers freely
 - many sellers
 - perfect information
 - every seller is a price taker (ie no one controls the price)
 - homogeneous product
- The price is more or less fixed in such a case for a product. ∴ profit can be written as

$$\pi = p^* Q - C(Q)$$

$$\therefore \frac{\partial \pi}{\partial Q} = p^* - C'(Q) = 0$$

$$\therefore p^* = \frac{\partial C}{\partial Q} = MC$$





avg cost

$$p > AC \Rightarrow \pi > 0$$

$$p < AC \Rightarrow \pi < 0$$

$$p = AC \Rightarrow \pi = 0$$

→ MONOPOLY

• PROPERTIES

- Exclusive Access to resources
- Patents
- Cartel (Discouraging new entrants using methods like bringing down prices artificially even if it gives you losses)
- economies of scale

- $p = a - bQ$

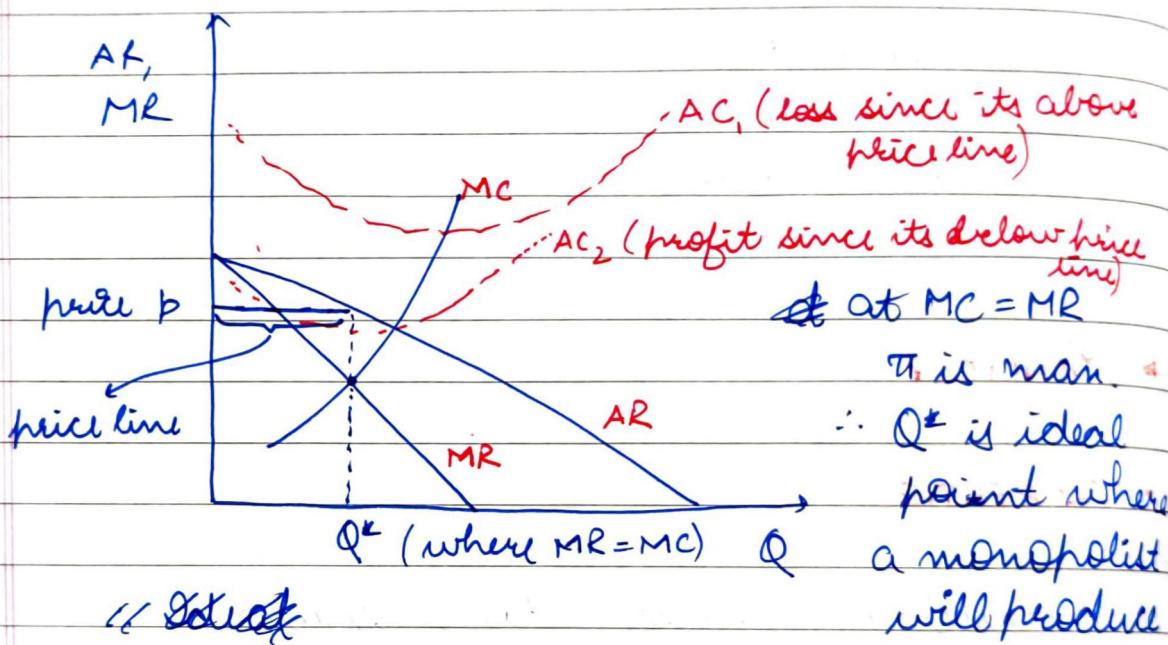
$$TR = pQ = aQ - bQ^2$$

$$MR = a - 2bQ$$

$$AR = a - bQ$$

$$TC = C(Q)$$

$$MC = c'(Q)$$



- Now

$$TR = p(Q)Q$$

$$MR = \frac{dp(Q)}{dQ}Q + p(Q)x_1$$

$$MR = p(Q) \left[\frac{dp}{dQ} \frac{Q}{P} + 1 \right]$$

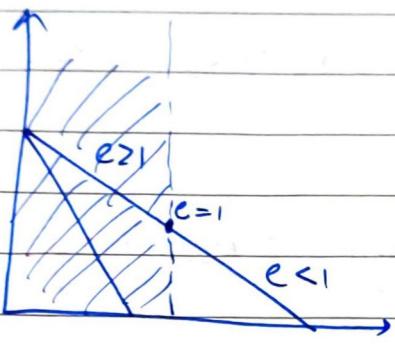
$$\cancel{MR = C(Q)}$$

$$MR = p(Q) \left[1 - \frac{1}{e} \right]$$

-(i)

NOTE: ~~Break even~~ point: The point of production where monopolist incurs no loss/profit when AC intersects with price line on AR line.

- From (i) we can say that a monopolist will like to produce at $e > 1$



$\therefore MC = MR \rightarrow$ this point must be within shaded region

• PRICE DISCRIMINATION

- First degree - For different no. of units, different prices are charged. All units are released one by one & whoever pays the highest product is sold
- Second degree - Upto a certain quantity, there is one price after which price starts changing. eg - electricity bill
- Third degree - Based on biasing among consumers. eg - metro tickets for old people.

- For discrimination consider we have 2 price fns $p_1(Q)$ & $p_2(Q)$

$$p_1(Q_1) \quad p_2(Q_2)$$

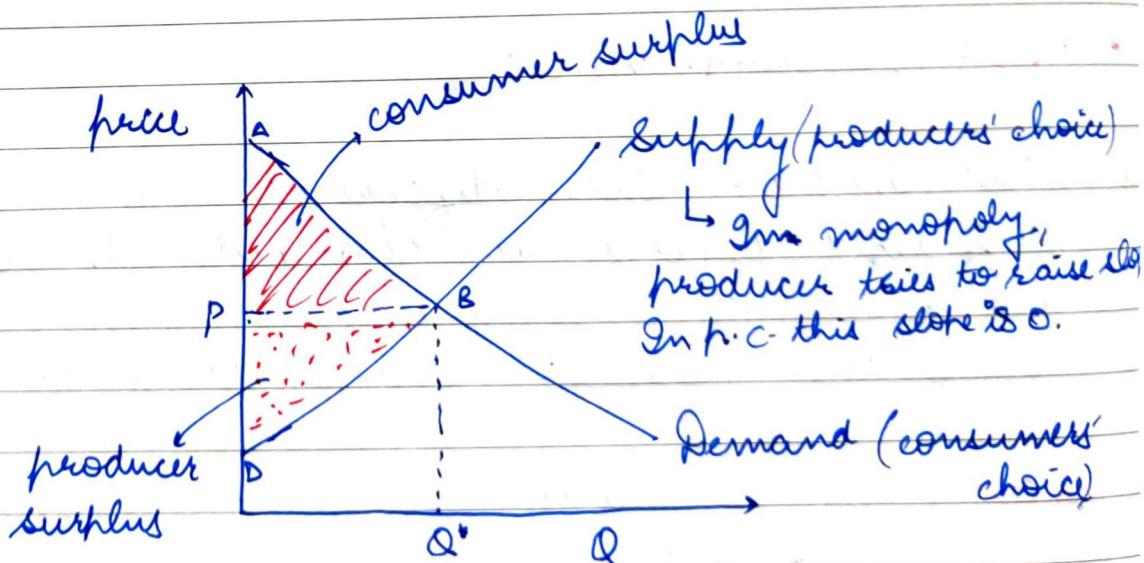
$$c(Q_1 + Q_2)$$

$$\pi = p_1(Q_1)Q_1 + p_2(Q_2)Q_2 - c(Q_1 + Q_2)$$

$$\frac{\partial \pi}{\partial Q_1} = MR_1 = MR_2 = MC$$

$$\Rightarrow p_1 \left[1 - \frac{1}{e_1} \right] = p_2 \left[1 - \frac{1}{e_2} \right] = MC$$

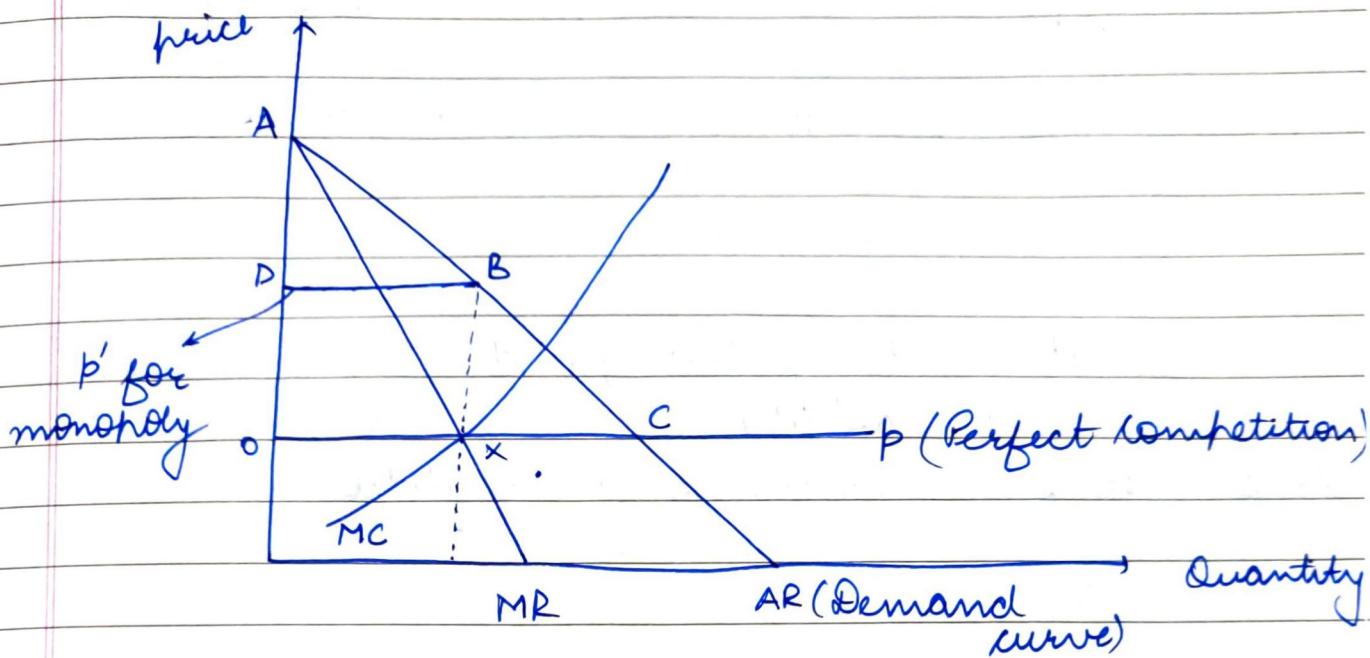
- Why monopolistic environment is not beneficial



This is a general scenario.

~~Answer now,~~

We'll incorporate 2 situations in below graph perfectly comp. and monopolistic



In perfect comp. consumer surplus was

$\Delta \times BC$ and in monopoly consumer surplus is ΔADB and ~~$\Delta DOXB$~~ becomes producer surplus.

∴ Net surplus in monopoly $\Delta ADB + \Delta DOXB$ which is less than ΔAOC .

∴ If we see carefully, $\Delta \times BC$ somehow vanishes from surplus.

• this $\Delta \times BC$ is called deadweight loss to the economy

Ques:

For a product X

$$C = 8X + 100$$

Demand for 2 groups

$$\begin{cases} X_1 = 100 - 0.5p, \\ X_2 = 40 - p_2 \end{cases}$$

→ first group of consumers

→ second group

$$X_1 + X_2 = X$$

What are the prices paid by 2 groups?
 & find elasticity

Ans: Profit maximising condition

$$(MR_1 = MR_2 = MC)$$

$$p_1 = 200 - 2X_1$$

$$p_2 = 40 - X_2$$

Total revenue

$$p_1 X_1 = 200 X_1 - 2X_1^2$$

$$p_2 X_2 = 40 X_2 - X_2^2$$

$$MR_1 = \cancel{\frac{\partial TR}{\partial X}} = 200 - 4X_1$$

$$MR_2 = 40 - 2X_2$$

$$MC = \frac{\partial C}{\partial X} = 8$$

$$8 = 40 - 2x_2$$

$$\Rightarrow x_2 = 16$$

8

$$200 - 4x_1 = 8$$

$$\Rightarrow x_1 = 48$$

$$\begin{array}{|l} \hline p_1 = 104 \\ \hline p_2 = 24 \\ \hline \end{array}$$

Now for elasticities

$$e_1 = \frac{\partial x_1}{\partial p_1} \cdot \frac{p_1}{x_1} = -0.5 \times \frac{104}{48} = -1.08$$

$$e_2 = \frac{\partial x_2}{\partial p_2} \cdot \frac{p_2}{x_2} = -1 \times \frac{24}{16} = -1.5$$

Ans.

$$p = 100 - 3q + 4\sqrt{A}$$

$$C = 4q^2 + 10q + A$$

A is advertising cost & q is quantity.

maximize profit.

Ans.

$$\Pi = pq - C$$

$$\Pi = 100q - 3q^2 + 4\sqrt{A}q - 4q^2 - 10q - A$$

$$\Rightarrow \Pi = 90q - 7q^2 + 4\sqrt{A}q - A$$

For maximizing, $f(n, q)$ we put $\frac{\partial f}{\partial n} = 0$ & $\frac{\partial f}{\partial q} = 0$

$$\frac{\partial \Pi}{\partial q} = 90 - 14q + 4\sqrt{A} = 0$$

$$\Rightarrow 90 + 4\sqrt{A} = 14q$$

~~2~~

$$\frac{\partial \Pi}{\partial A} = \frac{2q}{\sqrt{A}} - 1 = 0$$

$$\Rightarrow A = 4q^2$$

$$90 + 8q = 14q$$

$$\Rightarrow q = 15$$

Find profit with values

Ques Long run cost f^m is given by for an individual firm

$$C_i = q^3 - 4q^2 + 8q \rightarrow \text{for all firms}$$

There are n firms

$$\therefore \text{total product} = n \cdot q$$

Demand (total in market)

$$D = 2000 - 100b$$

Find b, q, n :

Ans:

$$D = n * q$$

$$\therefore n \times q = 2000 - 100p$$

When $p < AC$, ~~profit~~ producer is in loss. \therefore

$$AC_i = \frac{2q}{q} + \frac{C_i}{q}$$

for producer to produce,
 p should at least be
at AC .

$$\Rightarrow AC_i = q^2 - 4q + 8$$

Now we find min of AC

$$\frac{dAC_i}{dq} = 2q - 4 = 0$$

$$\Rightarrow q = 2$$

$$AC_{\min} = 4 - 8 + 8 = 4$$

$\therefore p \geq AC_{\min}$ for producer to produce

but since we can see that its perfectly competitive,

$$p = AC_{\min}$$

$$\therefore p = 4.$$

$$\& n * q = 2000 - 400 = 1600$$

$$\Rightarrow n = \frac{1600}{2} = 800$$

Ours

→ MONOPOLISTIC COMPETITION

- monopolistic competition is a market structure in which there are many firms selling differentiated products. The products may have some difference but it is same type of product.
eg - mobile phones - 2 different companies

* These are:

• PROPERTIES

- There are few barriers to entry in market
- Some difference in same type of product
- Gives producers a chance to come up with quality products and ~~advertisements~~ advertisements. eg - improving smartphone advertisements which entice etc.
- act independently & thinking.

NOTE:

→ OLIGOPOLY (Introduction)

- Oligopoly is a market in which there are a few interdependent firms

→ MONOPOLISTIC COMPETITION: CHARACTERISTICS *

- Four distinguishing characteristics
 - a) Many sellers: There are many sellers which do not take into account rivals' reactions.
 - b) Product differentiation where the goods that are sold aren't homogeneous
 - c) Multiple dimensions of competition make it harder to analyze a specific industry, but these methods of competition follow the same two decision rules as price competition.
 - d) Ease of entry of new firms in the long run: because there are now significant barriers to entry.

- OUTPUT, PRICE → from slides.
- GRAPHS → from slides
- DIFF. B/W MONOPOLY AND MONOPOLISTIC COMP.
↓
from slides
- ADVERTISING → from slides

→ OLIGOPOLY

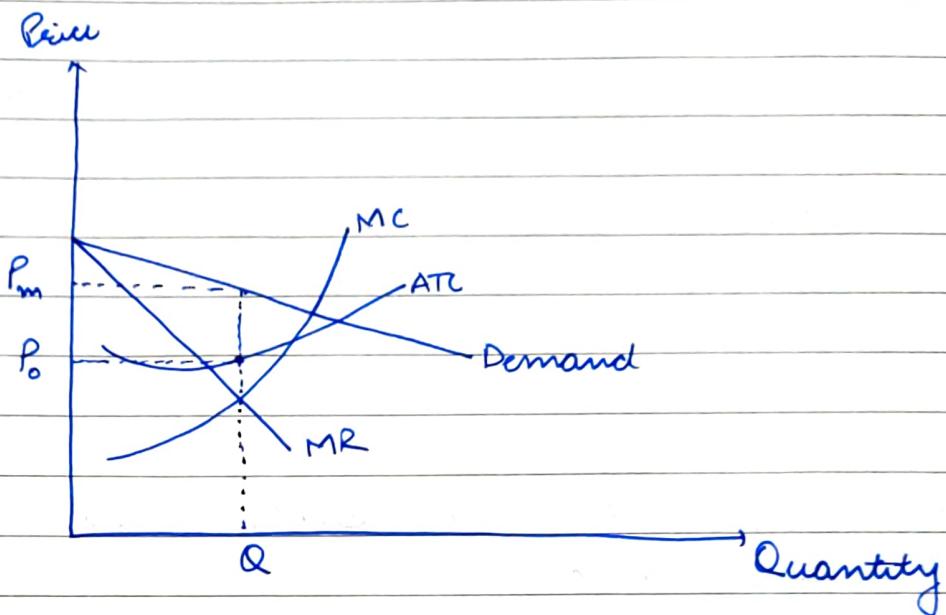
- A market structure in which a small number of firms has a large majority of market share is called oligopoly.
- It is similar to a monopoly, except that rather than 1 firm, a small no. of firms control the market.
- There is no exact upper limit to the number of firms in an oligopoly.
- But the number of firms are low enough that the actions of one firm significantly impact and influence the others.
- In oligopoly, the previous point is different from monopolistic competition because it in that case firms worry about product quality & make decisions independently. But that is not the case in oligopoly.
- Examples -
 - a) Google, Microsoft and Apple
 - b) Pepsi and Coca-Cola
 - c) Auto industry

- Products can either be homogenous or differentiated products
- Interdependence in terms of policies exist.
- Substantial barriers to entry. e.g. - new softwares need to be different from existing ones & may have very low demand if launched.
- Another example is British Airways and Air France.

→ COLLUSION AND COMPETITION

- **Collusion** is when 2 or more firms decide to fix price of a similar product(s) (e.g. a burger) to create a monopolistic situation and generate positive profit or to prevent entry of other firms.
- Collusion is illegal, i.e. it can't be drafted as a legal agreement.
- **Competition** is when firms enter competition and lower prices and come to a point of zero profit.

→ PRICE DETERMINATION FOR OLIGOPOLY



P_m - monopolistic price

P_0 - price of zero profit

- In oligopistic environment, in case of **collusion**, firms can easily charge at P_m ie monopolistic price.
- In case of **competition**, oligopistic firms charge P_0 and earn no profit or such.
- **Failure of Collusions:** Collusions are easy to fail, when firms cheat on each other and slightly cut their prices down to earn more secretly. Collusions are less likely to succeed when,
 - secret price cuts are difficult and costly

to detect. (Quality changes are difficult to monitor) (Sourcing of quality is undesirable to both the customers and other firms.)

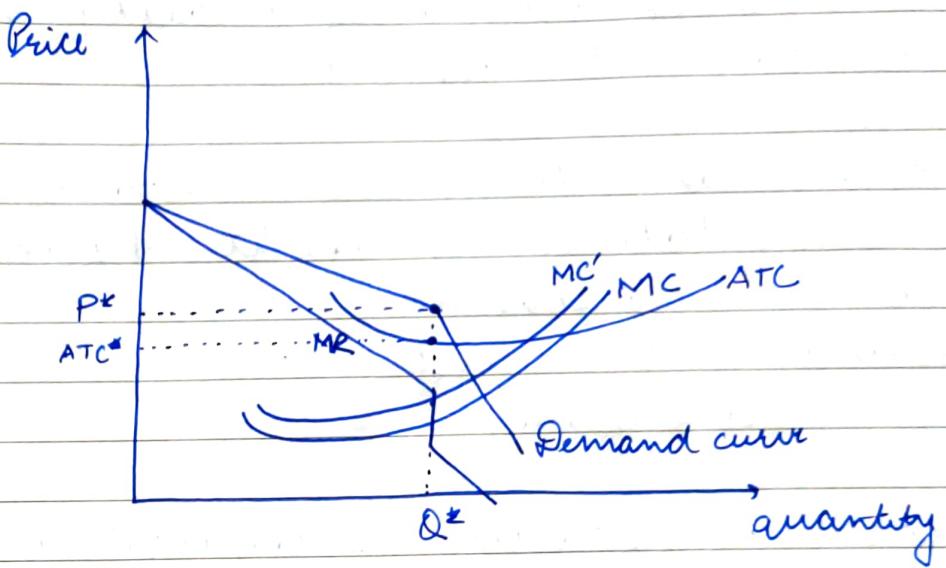
- market conditions are unstable. (Differences in expectations make it difficult to reach an agreement)
- vigorous anti-trust actions increase the cost of collusion.
- In cases of failure of collusions price may be b/w P_o and P_m

NOTE: Some oligopolistic markets operate in a situation of **price leadership**.

A single firm sets industry price and the remaining firms charge the same price as the leader.

→ SWEETY'S KINKED DEMAND CURVE MODEL OF OLIGOPOLY

- Assumptions:
 1. If a firm raises prices, other firms won't follow and the firm loses a lot of business.
 2. If a firm lowers prices, other firms follow and the firm doesn't gain much business.



- if cost (MC) shifts up slightly even then, $MC \cap MR$ intersect at same quantity.
 \therefore the price remains same. The reason for this **rigidity** is that producers are very concerned about the price at which they sell the product since any changes in price may prove heavy to revenue.
- This rigidity of price creates a discontinuity in demand curve

NOTE:

Oligopolistic markets show this Sweary's model, for eg, in case of separate geographic locations of market. The prices in this case are of monopolistic form ie at P^*

→ PROFIT POSSIBILITIES FOR OLIGOPOLY

- short run: profit, losses or even breaking even
- long run: profit or breaking even.

→ FOUR FIRM CONCENTRATION RATIO

- It is the sum of % market share of top 4 firms in the market
- read in detail from slides.

→ HERFINDAHL INDEX (H)

- It measures the extent to which a market is dominated by a few firms.
- It is calculated as sum of square of % shares of all firms in the market

$$H = \alpha_1^2 + \alpha_2^2 + \dots + \alpha_n^2$$

- H can be close to 0 in case of many, small firms.

- Justice Department guidelines (US)
- A market is considered concentrated if $H > 1800$
- A market is considered unconcentrated if $H < 1000$
- * read about concentrated & unconcentrated markets in slides
- * read about horizontal, vertical and conglomerate merger from slides.

Chapter - 3. market Failure

→ DEFINITION

- market failure is when a market left to itself does not allocate resources efficiently (labour & capital) or the condition where the allocation of goods and services by a market is not efficient is called market failure.

→ 4 SORTS OF MARKET FAILURE

- a) The abuse of market power, which can occur whenever a single buyer or seller can exert significant influence over prices or output (see monopoly and monopsony)
- b) Externalities : when the market does not take into account the impact of an economic activity on outsiders. For example, the market may ignore the costs imposed on outsiders by a firm polluting the environment.
- c) Public goods: such as national defence. How much defence would be provided if it were left to the market.

Public goods are non-rivalrous (in consumption) and nonexcludable (its usage is not limited to private entity)

d) where there is incomplete or asymmetric information or uncertainty

→ MARKET DISEQUILIBRIUM DUE TO SURPLUS →

- read from slides & look at graphs too

classmate

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→ FACTOR MARKETS

→ FACTORS OF PRODUCTION

a) Used to produce output

→ FACTOR MARKET

- A market for a factor of production
- A factor market facilitates the purchase and sale of services of factors of production
- eg- The market for construction workers brings together buyers and sellers of construction workers services.

NOTE: Derived demand: The demand for an input is derived from demand in output which the input helps to prepare.

NOTE: A firm might be a perfect competitor in the product market and might not be a perfect competitor in the factor market, or vice versa.

- Four possibilities for factor markets

	Product market	Factor market
a)	Perfectly competitive	not PC
b)	PC	not PC
c)	not PC	PC
d)	not PC	not PC

e.g- The local water company is the only company in the area & it hires one of the companies hiring accountants.

In this e.g, product market is not PC and factor market is PC.

e.g- a small mill town is owned by a textile company. The company is the only employer in town.

In this e.g, textile market may be PC but labour market is not PC

→ PRICE TAKING IN FACTOR MARKET →



1. What is the difference between a

2. What is the difference between a

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Questions

Ques: Suppose that a typical firm in a monopolistically competitive industry faces a demand curve given by $q = 60 - \frac{1}{2}p$, where q is quantity sold per week. The firm's MC curve is given by $MC = 60$.

- a) How much will it produce in short run?
- b) What price will it charge.

Ans:

$$a) q = 60 - \frac{1}{2}p$$

$$\Rightarrow 120 - 2q = p$$

$$\Rightarrow R = p \times q = 120q - 2q^2$$

$$MR = \frac{\partial R}{\partial q} = 120 - 4q$$

$MR = MC$ for profit max

$$\Rightarrow 120 - 4q = 60$$

$$\Rightarrow q = 15$$

$$b) p = 120 - 2q$$

$$\Rightarrow p = 120 - 30$$

$$\Rightarrow p = 90$$

NOTE: calculate MPP, MRC, MRP per day