

# Apply machine learning to Performance trend analysis

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March 28, 2017

# Overview

- 1 Recall: Thesis objectives
- 2 Markov switching model
  - Markov switching autoregressive model
- 3 Model estimation
  - E-M algorithm
- 4 What has been done?
- 5 Next step

# Objectives

- Detect the state of the CPU utilization (degrading, improving or steady state)
- Detect whether there is any change in the test environment that effects the CPU utilization

# Markov switching model, [Hamilton, 1989]

- A technique uses for describing the evolution of the process at different period of time
- Model involves multiple structures that can characterize the time series behaviors in different states
- The switching mechanism between the states is assumed to be an unobserved Markov chain - a stochastic process which contains the probability of transition from one state to any other state

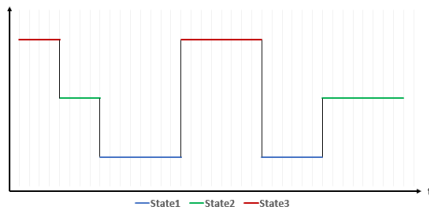


Figure: regime shift between states

# Markov switching model, [Hamilton, 1989]

Assuming that  $S_t$  denote an unobservable state variable

$$y_t = X_t' \beta_{S_t} + \varepsilon_t, \quad \varepsilon_t \sim N(0, \sigma_{S_t}^2)$$

$y_t$  is the observed value of time series at time  $t$

$X_t$  are the predictor variables of time series at time  $t$

$\beta_{S_t}$  are the coefficients in state  $S_t$ , where  $S_t = 1, 2, \dots, k$

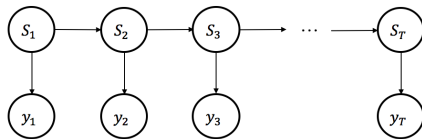


Figure: Model structure

# Markov switching model

Given dataset,

$$y_t = X_t' \beta_{S_t} + \varepsilon_t, \quad \varepsilon_t \sim N(0, \sigma_{S_t}^2)$$

- $y_t$  is CPU utilization
- $X_t$  are components which have an impact on the CPU utilization
- Assume there are three states ( $k = 3$ ): normal, good, bad

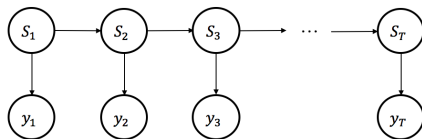


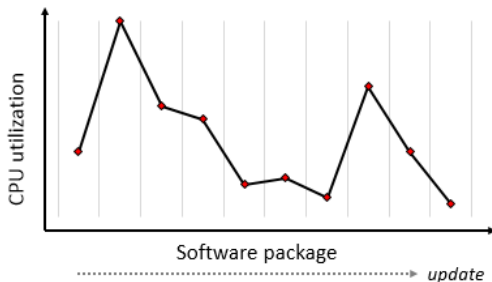
Figure: Model structure

# Markov switching autoregressive model

## Autoregressive model

$$y_t = c + \sum_{i=1}^p \phi_p y_{t-i} + \varepsilon_t$$

where  $c$  is constant,  $\phi_p$  are parameters and  $\varepsilon_t$  is white noise



# Markov switching autoregressive model

The observation are drawn from the first order autoregressive model, AR(1).

$$y_t = X_t' \beta_{S_t} + \phi_{1,S_t} y_{t-1} + \varepsilon_t$$

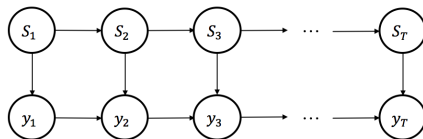


Figure: Model with additional dependencies at observation level



# Model estimation

## Model parameters

$$\theta = (\beta_{S_t}, \phi_{1,S_t}, \sigma_{S_t}^2, \pi_{S_t}, p_{ij})$$

where,

$\pi_{S_t}$  is initial probabilities in state  $S_t$

$p_{ij}$  is transition probabilities,  $p_{ij} = P(S_t = j | S_{t-1} = i) \quad 1 \leq i, j \leq k$   
and  $S_t$  is non-observable variable

## Model Likelihood

$$L(\theta; y_t) = f(y_t | \theta) = \sum_{t=1}^T \sum_{S_t=1}^k f(y_t | S_t; \theta) P(S_t)$$

## E-M algorithm

- Expectation step: Calculate the expectation of  $S_t$  given the observation under the current estimated parameters
- Maximization step: Obtain new estimates of the parameters by maximizing likelihood
- Repeat until converged

# What has been done?

One software product  $\Rightarrow$  many software packages

One software package  $\Rightarrow$  many different types of test cases

Data preprocessing

- Select a test case which has a minimum value of CPU utilization for each software package
- Multiple values separated by a tab character are stored together in column  $\Rightarrow$  split a tab-separated values to columns
- Remove incomplete test cases

ID	Variable1	Variable2	ID	Variable1	A	B	C
1	X	A=2 B=1 C=5	1	X	2	1	5
2	Y	A=4 B=2 C=8	2	Y	4	2	8
3	Z	A=1 C=6	3	Z	1	0	6
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.
.	.	.	.	.	.	.	.

Figure: Data example

# What has been done?

Study and review source code in the R package in detail

- MSwM: An univariate autoregressive Markov switching model for linear and generalized model by using the EM algorithm [Sanchez-Espigares, 2014]

# What has been done?

Implement and modify code in the package

- Small typo in the code when computing residual variance
- Solve non-invertible Hessian using generalized inverse procedure [Gill, 2004]
- Extension for categorical predictor variables
- Deal with NA coefficients
  - ⇒ Mostly occurs when predictor variables are categorical
  - ⇒ Initial coefficients with random subsets
  - ⇒ A single value or incomplete levels of variable

# What has been done?

## Results of fitting Markov switching autoregressive model

- Estimated parameters in each state
- For each observation,
  - ⇒ State assignment
  - ⇒ Probability assignment in each state
- Graphs show periods where the observation is in the specific state

# Next step

- Model selection: Compare several models (e.g., number of states, number of parameters which have switching effects)
- State prediction: Find the most probable state for the new observation
- Making a state inference
- Fit model for other software products



James D Hamilton (1989)

A new approach to the economic analysis of nonstationary time series and the business cycle

*Econometrica: Journal of the Econometric Society*, pages 357-384.



Jeff Gill and Gary King (2004)

What to do when your hessian is not invertible: Alternatives to model respecification in nonlinear estimation

*Sociological methods & research*, 33(1):54-87.



Josep A. Sanchez-Espigares and Alberto Lopez-Moreno (2014)

MSwM: Fitting Markov Switching Models

*CRAN R*.