

Apply machine learning to Performance trend analysis

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- 1 Recall: Thesis objectives
- 2 Markov switching model
 - Markov switching autoregressive model
 - Model estimation
- 3 What has been done?
- 4 Next step

Objectives

- Detect the state of the CPU utilization (degrading, improving or steady state)
- Detect whether there is any change in the test environment that effects the CPU utilization

Markov switching model, [Hamilton, 1989]

- A technique uses for describing the evolution of the process at different period of time
- Model involves multiple structures that can characterize the time series behaviors in different states
- The switching mechanism between the states is assumed to be an unobserved Markov chain - a stochastic process which contains the probability of transition from one state to any other state

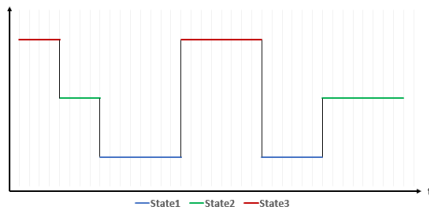


Figure: regime shift between states

Markov switching model, [Hamilton, 1989]

Assuming that S_t denote an unobservable state variable

$$y_t = X_t' \beta_{S_t} + \varepsilon_t, \quad \varepsilon_t \sim N(0, \sigma_{S_t}^2)$$

y_t is the observed value of time series at time t

X_t are the predictor variables of time series at time t

β_{S_t} are the coefficients in state S_t , where $S_t = 1, 2, \dots, k$

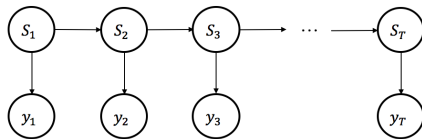


Figure: Model structure

Markov switching model

Given dataset,

$$y_t = X_t' \beta_{S_t} + \varepsilon_t, \quad \varepsilon_t \sim N(0, \sigma_{S_t}^2)$$

- y_t is CPU utilization
- X_t are components which have an impact on the CPU utilization
- Assume there are three states ($k = 3$): normal, good, bad

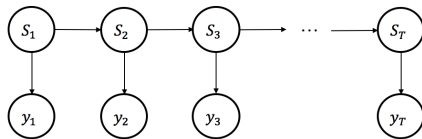


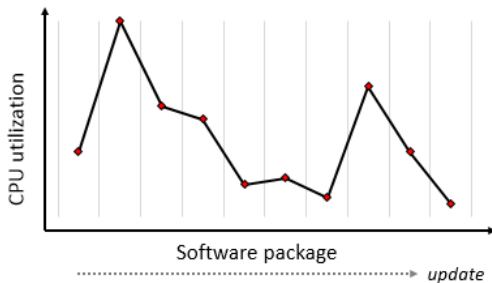
Figure: Model structure

Markov switching autoregressive model

Autoregressive model

$$y_t = c + \sum_{i=1}^p \phi_p y_{t-i} + \varepsilon_t$$

where c is constant, ϕ_p are parameters and ε_t is white noise



Markov switching autoregressive model

The observation are drawn from the first order autoregressive model, AR(1).

$$y_t = X_t' \beta_{S_t} + \phi_{1,S_t} y_{t-1} + \varepsilon_t$$

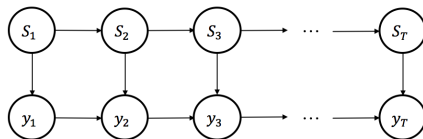


Figure: Model with additional dependencies at observation level

Model Likelihood

$$L(\theta; y_t) = f(y_t|\theta) = \sum_{t=1}^T \sum_{j=1}^k f(y_t|S_t = j; \theta) P(S_t = j)$$

and S_t is non-observable variable

What has been done?

One software product \Rightarrow many software packages

One software package \Rightarrow many different types of test cases

Data preprocessing

- Select a test case which has a minimum value of CPU utilization for each software package
- Multiple values separated by a tab character are stored together in column \Rightarrow split a tab-separated values to columns
- Remove incomplete test cases

ID	Variable1	Variable2	ID	Variable1	A	B	C
1	X	A=2 B=1 C=5	1	X	2	1	5
2	Y	A=4 B=2 C=8	2	Y	4	2	8
3	Z	A=1 C=6	3	Z	1	0	6
.
.
.

Figure: Data example

What has been done?

Study and review source code in the R package in detail

- MSwM: An univariate autoregressive Markov switching model for linear and generalized model by using the EM algorithm [Sanchez-Espigares, 2014]

What has been done?

Implement and modify code in the package

- Small typo in the code when computing residual variance
- Solve non-invertible Hessian using generalized inverse procedure [Gill, 2004]
- Extension for categorical predictor variables
- Deal with NA coefficients
 - Initial coefficients with random subsets
 - A single value or incomplete levels of variable
 - Matrix multiplication to compute conditional means \Rightarrow NAs

Solution: Remove variables with NAs coefficient before performing matrix multiplication

What has been done?

Results of fitting Markov switching autoregressive model

- Estimated parameters in each state
- For each observation,
 - State assignment
 - Probability assignment in each state
- Graphs show periods where the observation is in the specific state

Next step

- Model selection: Compare several models (e.g., number of states, number of parameters which have switching effects)
- State prediction: Find the most probable state for the new observation
- Making a state inference
- Fit model for other software products



James D Hamilton (1989)

A new approach to the economic analysis of nonstationary time series and the business cycle

Econometrica: Journal of the Econometric Society, pages 357-384.



Jeff Gill and Gary King (2004)

What to do when your hessian is not invertible: Alternatives to model respecification in nonlinear estimation

Sociological methods & research, 33(1):54-87.



Josep A. Sanchez-Espigares and Alberto Lopez-Moreno (2014)

MSwM: Fitting Markov Switching Models

CRAN R.