

(c) evidence of substituting into
$$\frac{\sum f(x)}{125}$$
 (M1)

 $e.g. \frac{15(11)+16(21)+17(33)+18(34)+19(18)+20(8)}{125}, \frac{2176}{125}$

mean = 17.4

A1 N2

9.) (a) median m = 32 A1 N1

 $40 \le t < 50$

 $50 \le t < 60$

(b) lower quartile $Q_1 = 22$, upper quartile $Q_3 = 40$ (A1)(A1) interquartile range = 18 A1 N3

14

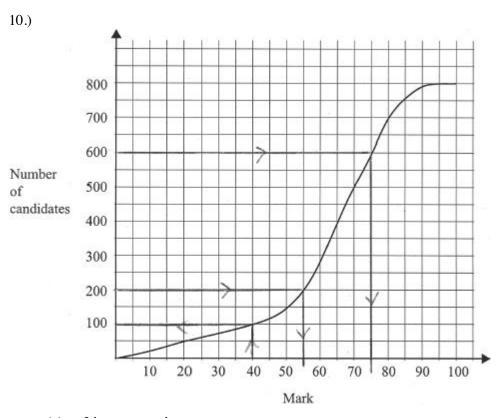
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(c) Time (minutes) Number of students $0 \le t < 10 \qquad 5$ $10 \le t < 20 \qquad 11$ $20 \le t < 30 \qquad 20$ $30 \le t < 40 \qquad 24$

A1A1 N2 [6]

(M1)

A1N2



(a) Lines on graph
100 students score 40 marks or fewer.

$$eg \ \frac{1200 - 50z}{42 + z} = 30,1200 + 50z = 1260 + 30z$$

z = 3

$$x = 5$$
 A1 N3

(c) Setting up their inequality

Correct substitution A1

$$eg \ \frac{98 + 276 + 416 + 41(10 + y) + 400}{50 + y} < 33, \frac{1600 - 41y}{50 + y} < 33$$

$$1600 + 41y < 1650 + 33y \tag{A1}$$

$$8y < 50 \ (y < 6.25)$$

6 A1 N1

Note: If candidates don't use the mid-interval values, but assume that all the new boxes weigh the minimum amount for Class D, award marks as follows:

Setting up **their** inequality M1

Correct substitution A1

$$eg \ \frac{1600 - 36.5y}{50 + y} < 33$$

$$1600 + 36.5y < 1650 + 33y \tag{A1}$$

$$3.5y < 50 \ (y < 14.28...)$$
 A1

14 A1 N1

14.) (a)

Age range	Frequency	Mid - interval value		
$0 \le age < 20$	40	10		
$20 \le age < 40$	70	30		
40 ≤ age < 60	100	50		
60 ≤ age < 80	50	70		
$80 \le age \le 100$	10	90		

A1A1 N2

M1

(b) For attempting to find
$$\sum f x$$
 (M1)

 $eg\ 40 \times 10 + ... + 10 \times 90 = 11900$

For dividing by 270 (M1)

$$eg \frac{11900}{270}$$

Mean = 44.1 A1 N4

[12]

15.)
$$b = 3, c = 3$$
 AIAI N2

using mean $\left(\frac{a+b+c+d}{4} = 4\right)$ M1

using range $(d-a=6)$ M1

 $a = 2, d = 8$ AIAI N2

(ii) $r = 10$ A2 N2

(ii) $s = 13$ A2 N2

(b) Using $\frac{\sum x}{12} = 10$ A1

 $t = 18$ AI N1

(b) B A C AIAIAI N3

(c) Recognizing the link between 6 and the upper quartile eg 25% scored greater than 6, 0.25 × 32 (A1)

8 A1 N3

[6]

19.) (a) (i) 50 (accept 49, "fewer than 50") A1 N1

(ii) Cumulative frequency $(7) = 90$ (A1)

 $90 - 50$ (M1)

 $90 - 50$ (M1)

(c)

(i)

t (minutes)	$0 \le t < 2$	$2 \le t < 4$	4 ≤ <i>t</i> < 6	6 ≤ <i>t</i> < 8	8 ≤ <i>t</i> < 10	$10 \le t < 12$
Frequency	10	23	37	38	27	15

N3 A1A1A1

(ii) Evidence of using all correct mid-interval values (1, 3, 5, 7, 9, 11) A1

mean =
$$\left(\frac{1 \times 10 + 3 \times 23 + 5 \times 37 + 7 \times 38 + 9 \times 27 + 11 \times 15}{150}\right)$$

$$= 6.25 \text{ (min)}, 6 \text{ min } 15 \text{ secs}$$

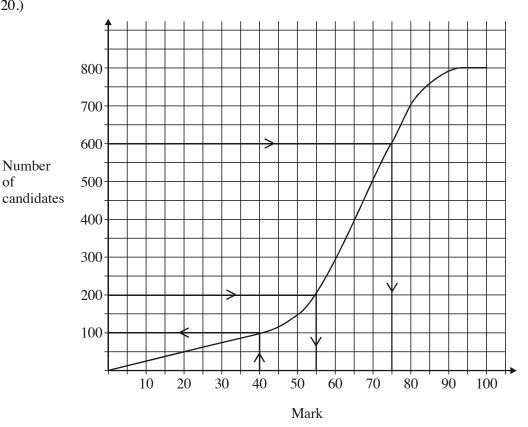
A1 N1

[14]

20.)

Number

of



Lines on graph (a) 100 students score 40 marks or fewer. (M1)

A1

(A1) (C2)

2

4

(b) Identifying 200 and 600 Lines on graph. a = 55, b = 75.

A1

(M1)

A1A1

[6]

21.) (a) mean =
$$\sum \frac{x}{n} \left(= \frac{2230}{45} \right)$$
 (M1)

$$\overline{x} = 49.6$$
 (Accept 50)

(b)
$$\overline{y} = \frac{\sum y}{n+2}$$
 (may be implied) (M1)

$$\sum y = 2230 + 37 + 30 \tag{A1}$$

$$\bar{y} = \frac{2297}{47} \tag{A1}$$

$$=48.9 \text{ (Accept 49)}$$
 (A1) (C4)

22.) (a) Mean = $\frac{\sum f x}{\sum f}$

$$\sum f x = (1) (0) + (2) (4) + (3) (6) + (4) (k) + (5) (8) + (6)$$
(6) + (7) (6) (A1)

$$\sum f \quad k + 30 \tag{A1}$$

Using mean
$$4.6 = \frac{144 + 4k}{k + 30}$$
 (M1)

$$4.6k + 138 = 144 + 4k \tag{A1}$$

0.6k = 6

$$k = 10 \tag{A1)(C5)}$$

(b) Mode = 4 (A1) (C1) (accept 5, if k < 8)

23.) (a) 76 (mice) (A1) (N1)

(c)
$$p = 76 - (16 + 22) = 38 \text{(allow ft from (ii) (a))}$$
 (A1) (N1)

$$q = 132 - 76 = 56$$
 (A1) (N1)

(ii)
$$x = \frac{7.5 \times 16 + \dots 14.5 \times 23}{16 + \dots 23} \qquad \left(= \frac{3363}{300} \right)$$
 (M1)

$$= 11.2 \quad (accept 11.21)$$
 (A1) (N2)

24.) (a)

Mark (x)	$0 \le x < 20$	$20 \le x < 40$	$40 \le x < 60$	$60 \le x < 80$	$80 \le x < 100$
Number of Students	22	50 (±1)	66 (±1)	42 (±1)	20

(A1)(A1)(A1) (C3)

[6]

[6]

(b) 40th Percentile
$$\Rightarrow$$
 80th student fails, (mark 42%) (M2)
Pass mark 43% (Accept mark > 42.) (A1) (C3)

25.) List of frequencies with p in the middle

$$eg \ 5 + 10, p, 6 + 2 \Rightarrow 15, 8, \text{ or } 15 < \frac{23 + p}{2}, \text{ or } p > 7.$$
 (M1)

Consideration that p < 10 because 2 is the mode or discretionary for further processing. (M1)

Possible values of p are 8 and 9

(A2)(A2) (C6)

[6]

26.) (a) line(s) on graph (M1) median is 183 (A1) (C2)

(b) Lower quartile
$$Q_1 = 175$$
 (A1)

Upper quartile
$$Q_3 = 189$$
 (A1)

IQR is 14

[6]

[6]

27.)
$$d = 11$$
; $c = 11$ (A1)(A1) (C1)(C1)

$$d-a=8 \text{ (or } 11-a=8)$$
 (A1)
 $a=3$ (A1) (C2)

$$\frac{3+b+11+11}{4} = 8 \left(\text{or } \frac{\text{sum}}{4} = 8 \right)$$
 (A1)

$$b = 7 \tag{A1}$$

28.)

x	f	Σf
4	2	2
5	5	7
6	4	11
7	3	14
8	4	18
10	2	20
12	1	21

```
m = 6
      (a)
                                                                                           (A2) (C2)
      (b)
             Q_1 = 5
                                                                                           (A2) (C2)
                                                                                           (A1)
      (c)
              Q_3 = 8
             IQR = 8 - 5
                                                                                           (M1)
                   = 3 (accept 5 - 8 or [5, 8])
                                                                                                  (C2)
                                                                                                                  [6]
29.)
                   90
                   80
               Cumulative frequency
                   70
                   60
                   50
                   40
                   30
                   20
                   10
                    0
                               5
                                       10
                                          LQ = 15
                                                      M = 20 \text{ UQ} = 24
                                                                                  35
                      0
                                                                                          40
                                                                                                   45
                                                     Diameter (mm)
                                                   Correct lines drawn on graph,(A1)(C1)
      (a)
                    (i)
                    median = 20
                                                                        (A1)(C1)
             (ii)
                    Correct lines drawn on graph,
                                                                                      (A1)(C1)
                    UQ = Q_3 = 24
                                                                                      (A1)(C1)
             IQR = Q_3 - Q_1 (or UQ - LQ)
      (b)
                                                                                           (M1)
             = 10 (accept 14 to 24)
                                                                                           (A1) (C2)
                           Note: Accept 14 to 24, 24 to 14, 14 – 24
                           or 24 -14.
                                                                                                                  [6]
30.)
                         \Sigma = 630 \times 9 = 5670
        Jan-Sept
                                                   (M1)(A1)
Oct-Dec
                 \Sigma = 810 \times 3 = 2430
                                           (M1)(A1)
        \bar{x} = \frac{5670 + 2430}{}
                                  (M1)
mean = 675
                 (A1)
                         (C6)
                                                                                                                  [6]
31.)
        (a)
                 (i)
                         median fare = $24 (\pm 0.5)
                                                            (A1)
                    fare \leq $35 => number of cabs is 154 (or 153)
                                                                                           (A1)
                                                                                                      2
       (b)
             40\% of cabs = 80 cabs
                                                                                           (A1)
             fares up to $22
                                                                                           (A1)
             distance = $22 \div $0.55
                                                                                           (M1)
                     a = 40 \text{ km}
                                                                                                      4
                                                                                           (A1)
       (c)
             Distance 90 km \Rightarrow fare = 90 \times \$0.55
```

= \$49.50

(A1)

Fare
$$$49.50 \Rightarrow$$
 number of cabs = $200 - 186$ (M1)
= 14 (A1)

Thus percentage is
$$\frac{14}{200} = 7\%$$
 (A1)

[10]

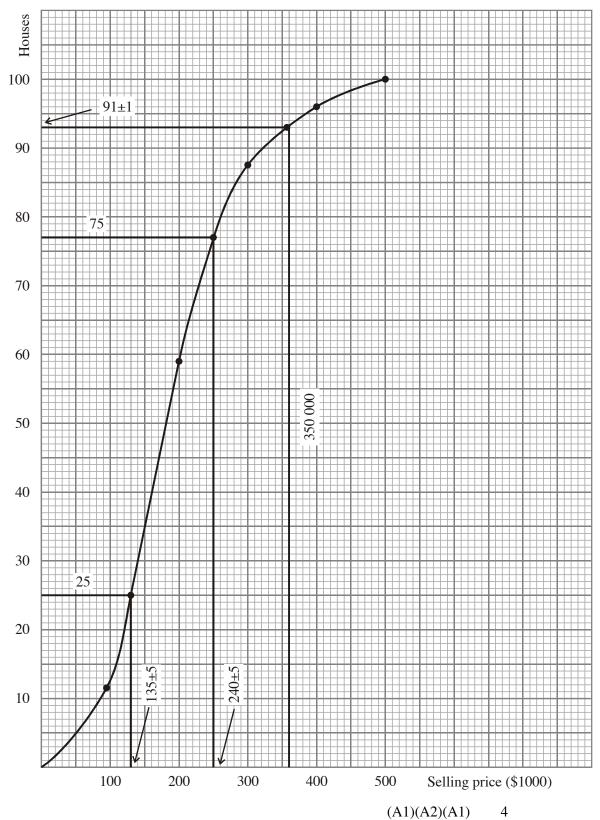
32.) Median = middle value
$$\Rightarrow b = 11$$
 (A1)

Mean =
$$\frac{a+b+c}{3}$$
 = $\frac{a+11+c}{3}$ = 9 => $a+11+c=27$ (M1)

$$\Rightarrow a + c = 16$$
 (A1)
Range = $c - a = 10$ (M1)(A1)

Solving equations simultaneously gives
$$a = 3$$
 (A1) (C6)

[6]



Notes: Award (A1) for correct axes, scales and labelling, (A1) for correctly plotted points.

Award (A2) for good curve correctly drawn, (A1) for badly drawn, correct curve.

Award (A1) for a correct polygon.

(b) $Q_1 = 135 \pm 5$ $Q_3 = 240 \pm 5$ (M1)(A1)

Interquartile range = 105 ± 10 . (Accept 135 - 240 or 240 - 135.) (A1) 3 *Note:* Award (M1) for the correct lines on the graph.

(c)
$$a = 94 - 87 = 7$$
, $b = 100 - 94 = 6$ (A1)(A1) 2

(d) $mean = \frac{12(50) + 46(150) + 29(250) + 7(350) + 6(450)}{100}$ (M1)

 $= 199 \text{ or } \$199000$ (A1)

OR

 $mean = 199 \text{ or } \$199000$ (G2) 2

(e) (i) $\$350000 \Rightarrow 91.5$ (M1)

 $= 9 \text{ or } \$$ (A1)

(ii) $P(both > 400000) = \frac{6}{9}(\frac{5}{8}) = \frac{5}{12} \text{ or } \frac{6}{8}(\frac{5}{7}) = \frac{15}{28}$ (M1)(A1) 4

Note: Award (M1)(A0) for the answers $\frac{4}{9}$ or $\frac{9}{16}$ obtained from correct independent probabilities.

(a) Median = middle number of 75 (M1)

 $= 38th \text{ number}$
 $= 4$ (A1) (C2)

(b) Mean = $\frac{5 + 18 + 48 + 72 + 100 + 42}{75}$ (M1)

 $= \frac{285}{75}$
 $= 3.8$ (A1) (C2)

35.)

34.)

Weight (W)	<i>W</i> ≤ 85	<i>W</i> ≤ 90	<i>W</i> ≤ 95	<i>W</i> ≤ 100	<i>W</i> ≤ 105	<i>W</i> ≤ 110	<i>W</i> ≤ 115
Number of packets	5	15	30	56	69	76	80

(A1)1 [15]

[4]

- From the graph, the median is approximately 96.8. (c) Answer: 97 (nearest gram).
 - (ii) From the graph, the upper or third quartile is approximately 101.2. Answer: 101 (nearest gram). (A2)4
- (d) Sum = 0, since the sum of the deviations from the mean is zero. (A2)

$$\sum (W_i - \overline{W}) = \sum W_i - \left(80 \frac{\sum W_i}{80}\right) = 0 \tag{M1)(A1)}$$

(e) Let *A* be the event:
$$W > 100$$
, and *B* the event: $85 < W \le 110$

$$P(A \mid B) = \frac{P(A \cap B)}{P(B)}$$
(M1)

$$P(A \cap B) = \frac{20}{80} \tag{A1}$$

$$P(B) = \frac{71}{80} \tag{A1}$$

$$P(A \mid B) = 0.282$$
 (A1)

OR

71 packets with weight $85 < W \le 110$. (M1)

Of these, 20 packets have weight W > 100. (M1)

Required probability =
$$\frac{20}{71}$$
 (A1)

$$= 0.282$$
 (A1) 4

Notes: Award (A2) for a correct final answer with no reasoning.

Award up to (M2) for correct reasoning or method.

[14]

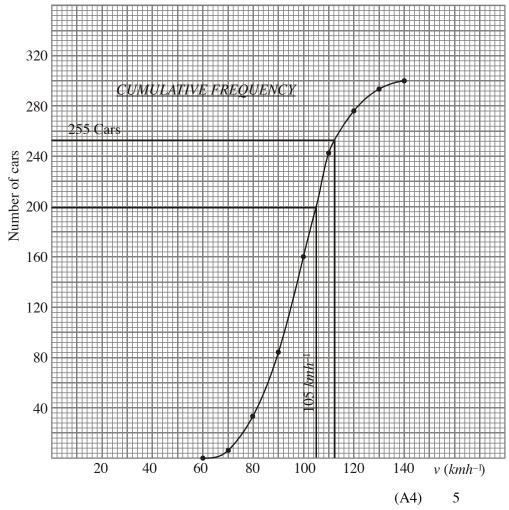
36.) (a) (Using mid-intervals)
$$\bar{v} = \frac{65(7) + 75(25) + ... + 135(5)}{7 + 25 + ... + 5}$$
(M1)
$$= \frac{29450}{300} = 98.2 \text{ km h}^{-1}(\text{A1})$$

OR

$$\overline{v} = 98.2 \tag{G2}$$

(b)
$$a = 165, b = 275$$
 (A1)

(ii)



Note: Award (A1) for properly marked scales and axes, (A2) for 9 correctly plotted points, (A1) for 7 or 8 points, (A1) for a smooth curve through the points.

(c) (i) Vertical line on graph at
$$105 \text{ km h}^{-1}$$
 (M1)
$$\frac{300 - 200}{300} \times 100\% = 33.3(\pm 1.3\%)$$
 (A1)

OR

$$33.3(\pm 1.3\%)$$
 (A2)

(ii) 15% of 300 = 45 300 - 45 = 255Horizontal line on graph at 255 cars (M1) Speed = $114(\pm 2 \text{ km h}^{-1})$ (A1)

OR

Speed =
$$114(\pm 2 \text{ km h}^{-1})$$
 (A2) 4 [11]

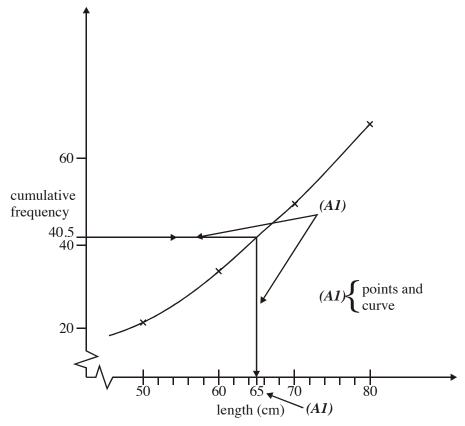
37.) (a) (i)
$$10$$
 (A1) (A1) (A1) $14 + 10 = 24$ (A1) 2

Note: Award (A0) for using the mid-interval values of 14.5, 24.5 etc.

(i)
$$\square = 63$$
 (A1)

(ii)
$$\Box = 20.5 (3 \text{ sf})$$
 (A1) 4

(d)



OR Median =
$$65$$
 (A3) 3

Note: This answer assumes appropriate use of a calculator with correct arguments.

3

OR Linear interpolation on the table: (M1)

$$\left(\frac{48-40.5}{48-32}\right) \times 60 + \left(\frac{40.5-32}{48-32}\right) \times 70 = 65 \text{ (2sf)}$$
 (A1)(A1)

[10]

5

(A4)

(M1)

38.) (a)
$$\bar{x} = $59$$
 (G2)

OR

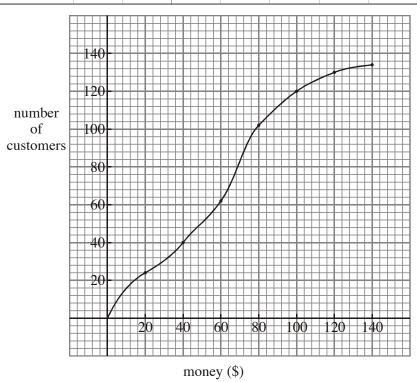
$$\overline{x} = \frac{10 \times 24 + 30 \times 16 + \dots + 110 \times 10 + 130 \times 4}{24 + 16 + \dots + 10 + 4}$$
 (M1)

$$=\frac{7860}{134}$$

$$= $59$$
 (A1) 2

(b)

Money (\$)	<20	<40	<60	<80	<100	<120	<140	
Customers	24	40	62	102	120	130	134	(A1)



Note: Award (A1) for the correct scale, (A1) for the points, and (A2) for the curve.

(c) (i)
$$t = 2d^{2/3} + 3$$

Mean $d = 59$

Mean
$$t \approx 2 \times (59)^{2/3} + 3$$
 (M1)

$$\approx 33.3 \text{ min.} (3 \text{ sf}) (\text{accept } 33.2)$$
 (A1)

(ii)
$$t > 37 \Rightarrow 2d^{2/3} + 3 > 37$$
 (M1) $2d^{2/3} > 34$

$$d^{2/3} > 17 (A1)$$

 $d > (17)^{3/2}$ d > 70.1

From the graph, when
$$d = 70.1$$
, $n = 82$ (A1)

number of shoppers =
$$134 - 82$$
 (A1)

$$= 52 \tag{A1}$$

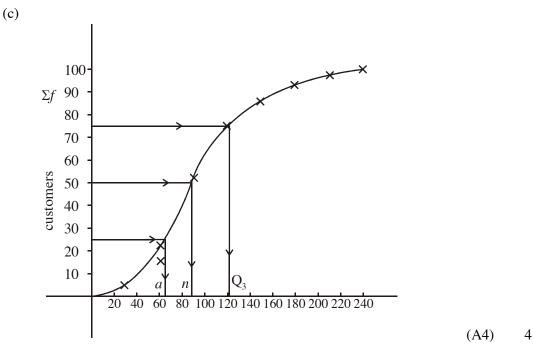
39.)
$$\frac{(10 \times 1) + (20 \times 2) + (30 \times 5) + (40 \times k) + (50 \times 3)}{k + 11} = 34 \quad (M1)(A1)$$

$$\frac{40k + 350}{k + 11} = 34(A1)$$

$$\Rightarrow k = 4 \quad (A1) \quad (C4)$$

40.) (a)
$$\frac{x}{f} = 97.2 \text{ (exactly)}$$
 (a)
$$\frac{x}{x} = 97.2 \text{ (exactly)}$$
 (A1)
$$\frac{x}{x} = 97.2 \text{ (exactly)}$$

Note: Award (A1) for correct values for x, $\sum f$.



Notes: Award (A2) for 6 or more points correct, (A1) for 4/5 points correct.

Award (A1) for a reasonable graph, (A1) for the correct axes and the given scales.

(d) Median =
$$87 \pm 2$$
 (A1)

Lower quartile =
$$65 \pm 2$$
 (A1)

Upper quartile =
$$123 \pm 2$$
 (A1) 3

[10]

[15]

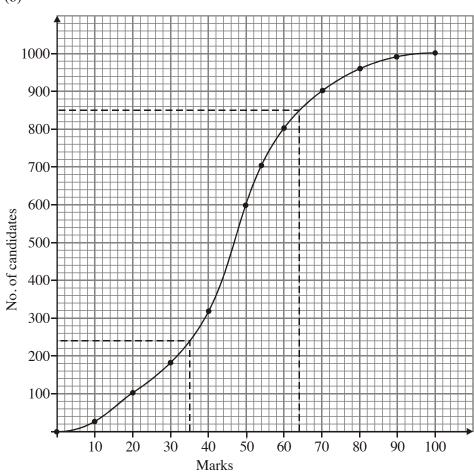
41.) (a)

Mark	≤ 10	≤ 20	≤ 30	≤ 40	≤ 50	≤ 60	≤ 70	≤ 80	≤ 90	≤ 100
No. of Candidates	15	65	165	335	595	815	905	950	980	1000

(A3) 3

Note: Award (A1) for 165, (A1) for 1000, (A1) if all other entries are correct.

(b)



(A5) 5

Notes: Vertical axis and scale (A1)

Horizontal axis and scale (A1)
Points (A1)

Curve (allow polygon) (A2)

(c) Median = 46(M1)(A1)

(ii) Scores < 35: 240 candidates (M1)(A2)

(iii) Top $15\% \Rightarrow Mark \ge 63$ (M1)(A1)(A1) 8

Notes: Accept the answers from the **student's** graph. In each part, award (M1) for the dotted lines on the graph.

42.) Mean =
$$\frac{(72 \times 1.79) + (28 \times 1.62)}{100}$$
 (M1)(M1)(M1)
= 1.7424 (= 1.74 to 3 sf) (A1) (C4)

43.) (a)
$$m = \frac{300}{25}$$
 (M1)
= 12 (A1) (C2)
(b) $s = \sqrt{\frac{625}{25}}$ (M1)
= 5 (A1) (C2)

[4]