1.)	In	an arithmetic sequence, $u_1 = 2$ and $u_3 = 8$.	
	(a)	Find d .	(2)
	(b)	Find u_{20} .	(2)
	(c)	Find S_{20} .	(2)
			(Total 6 marks)
2.)	In a	an arithmetic sequence $u_1 = 7$, $u_{20} = 64$ and $u_n = 3709$.	
	(a)	Find the value of the common difference.	(3)
	(b)	Find the value of n .	(2)
			(2) (Total 5 marks)
3.)	Co	nsider the arithmetic sequence 3, 9, 15,, 1353.	
σ.,	(a)	Write down the common difference.	
	()		(1)
	(b)	Find the number of terms in the sequence.	(3)
	(c)	Find the sum of the sequence.	(2)
			(Total 6 marks)
4.)	An	arithmetic sequence, u_1 , u_2 , u_3 ,, has $d = 11$ and $u_{27} = 263$.	
	(a)	Find u_1 .	
			(2)
	(b)	(i) Given that $u_n = 516$, find the value of n .	
		(ii) For this value of n , find S_n .	(4) (Total 6 marks)
			(Total o marks)
5.)	Th	e first three terms of an infinite geometric sequence are 32, 16 and 8.	
	(a)	Write down the value of <i>r</i> .	(1)
	(b)	Find u_6 .	· · ·

(c) Find the sum to infinity of this sequence.

(2) (Total 5 marks)

- 6.) The n^{th} term of an arithmetic sequence is given by $u_n = 5 + 2n$.
 - (a) Write down the common difference.

(1)

- (b) (i) Given that the n^{th} term of this sequence is 115, find the value of n.
 - (ii) For this value of n, find the sum of the sequence.

(5)

(Total 6 marks)

- 7.) In an arithmetic series, the first term is –7 and the sum of the first 20 terms is 620.
 - (a) Find the common difference.

(3)

(b) Find the value of the 78th term.

(2)

(Total 5 marks)

- 8.) In a geometric series, $u_1 = \frac{1}{81}$ and $u_4 = \frac{1}{3}$.
 - (a) Find the value of r.

(3)

(b) Find the smallest value of n for which $S_n > 40$.

(4)

(Total 7 marks)

9.) (a) Expand $\sum_{r=4}^{7} 2^r$ as the sum of four terms.

(1)

- (b) (i) Find the value of $\sum_{r=4}^{30} 2^r$.
 - (ii) Explain why $\sum_{r=4}^{\infty} 2^r$ cannot be evaluated.

(6)

(Total 7 marks)

10.)	In a	an arithmetic sequence, $S_{40} = 1900$ and $u_{40} = 106$. Find the value of u_1 and of d .	(Total 6 marks)
11.)	Cor	nsider the arithmetic sequence 2, 5, 8, 11,	
	(a)	Find u_{101} .	(3)
	(b)	Find the value of n so that $u_n = 152$.	
			(3) (Total 6 marks)
12.)	Coı	nsider the infinite geometric sequence $3000, -1800, 1080, -648, \dots$	
	(a)	Find the common ratio.	(2)
	(b)	Find the 10 th term.	(2)
	(c)	Find the exact sum of the infinite sequence.	(2)
			(Total 6 marks)
13.)	Cor	nsider the infinite geometric sequence 3, $3(0.9)$, $3(0.9)^2$, $3(0.9)^3$,	
	(a)	Write down the 10 th term of the sequence. Do not simplify your answer.	(1)
	(b)	Find the sum of the infinite sequence.	(4)
			(4) (Total 5 marks)
14.)	In a	an arithmetic sequence $u_{21} = -37$ and $u_4 = -3$.	
	(a)	Find	
		(i) the common difference;	
		(ii) the first term.	(4)
	(b)	Find S_{10} .	
			(3) (Total 7 marks)

15.)	Let	$t u_n = 3 - 2n.$	
	(a)	Write down the value of u_1 , u_2 , and u_3 .	(3)
	(b)	Find $\sum_{n=1}^{20} (3-2n)$.	
			(3) (Total 6 marks)
16.) each		heatre has 20 rows of seats. There are 15 seats in the first row, 17 seats in the secons sive row of seats has two more seats in it than the previous row.	nd row, and
	(a)	Calculate the number of seats in the 20th row.	(4)
	(b)	Calculate the total number of seats.	(2) (Total 6 marks)
17.)	A sı	sum of \$ 5000 is invested at a compound interest rate of 6.3 % per annum.	
	(a)	Write down an expression for the value of the investment after n full years.	(1)
	(b)	What will be the value of the investment at the end of five years?	(1)
	(c)	The value of the investment will exceed $$10000$ after n full years.	
		(i) Write down an inequality to represent this information.	
		(ii) Calculate the minimum value of <i>n</i> .	(4) (Total 6 marks)
18.)	Cor	nsider the infinite geometric sequence 25, 5, 1, 0.2,	
	(a)	Find the common ratio.	
	(b)	Find	
		(i) the 10^{th} term;	
		(ii) an expression for the n^{th} term.	
	(c)	Find the sum of the infinite sequence.	(Total 6 marks)

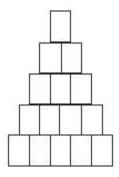
19.)	The	e first four terms of a sequence are 18, 54, 162, 486.	
	(a)	Use all four terms to show that this is a geometric sequence.	(2)
	(b)	(i) Find an expression for the n^{th} term of this geometric sequence.	
		(ii) If the n^{th} term of the sequence is 1062 882, find the value of n .	(4) (Total 6 marks)
20.)	(a)	Write down the first three terms of the sequence $u_n = 3n$, for $n \ge 1$.	(1)
	(b)	Find	
		(i) $\sum_{n=1}^{20} 3n$;	
		(ii) $\sum_{n=21}^{100} 3n$.	
		n=21	(5) (Total 6 marks)
21.)	Cor	nsider the infinite geometric series $405 + 270 + 180 +$	
	(a)	For this series, find the common ratio, giving your answer as a fraction in its simform.	plest
	(b)	Find the fifteenth term of this series.	
	(c)	Find the exact value of the sum of the infinite series.	(Total 6 marks)
22.)	(a)	Consider the geometric sequence –3, 6, –12, 24,	
		(i) Write down the common ratio.	
		(ii) Find the 15 th term.	
	Cons	sider the sequence $x - 3$, $x + 1$, $2x + 8$,	(3)
	(b)	When $x = 5$, the sequence is geometric.	
		(i) Write down the first three terms.	
		(ii) Find the common ratio.	(2)

	· /			(4)
	(d)	For th	his value of x , find	
		(i)	the common ratio;	
		(ii)	the sum of the infinite sequence.	(3)
				(Total 12 marks)
23.)	Let	S_n be t	he sum of the first n terms of the arithmetic series $2 + 4 + 6 + \dots$	
	(a)	Find		
		(i)	S_4 ;	
		(ii)	S_{100} .	(4)
	Let M	$\mathbf{I} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$.	· · · · · · · · · · · · · · · · · · ·
	(b)		(i) Find M^2 .	
		(ii)	Show that $\mathbf{M}^3 = \begin{pmatrix} 1 & 6 \\ 0 & 1 \end{pmatrix}$.	(5)
	It ma	y now	be assumed that $M^n = \begin{pmatrix} 1 & 2n \\ 0 & 1 \end{pmatrix}$, for $n \ge 4$. The sum T_n is defined by	
			$T_n = M^1 + M^2 + M^3 + + M^n$.	
	(c)		(i) Write down M^4 .	
		(ii)	Find T_4 .	(4)
	(d)	Using	g your results from part (a) (ii), find T_{100} .	(3) (Total 16 marks)

Find the other value of x for which the sequence is geometric.

(c)

24.) Clara organizes cans in triangular piles, where each row has one less can than the row below. For example, the pile of 15 cans shown has 5 cans in the bottom row and 4 cans in the row above it.



(a) A pile has 20 cans in the bottom row. Show that the pile contains 210 cans.

(4)

(b) There are 3240 cans in a pile. How many cans are in the bottom row?

(4)

- (c) (i) There are S cans and they are organized in a triangular pile with n cans in the bottom row. Show that $n^2 + n 2S = 0$.
 - (ii) Clara has 2100 cans. Explain why she cannot organize them in a triangular pile.

(6)

(Total 14 marks)

- 25.) A theatre has 20 rows of seats. There are 15 seats in the first row, 17 seats in the second row, and each successive row of seats has two more seats in it than the previous row.
 - (a) Calculate the number of seats in the 20th row.
 - (b) Calculate the **total** number of seats.

(Total 6 marks)

- 26.) A sum of \$5000 is invested at a compound interest rate of 6.3% per annum.
 - (a) Write down an expression for the value of the investment after n full years.
 - (b) What will be the value of the investment at the end of five years?
 - (c) The value of the investment will exceed \$10000 after n full years,
 - (i) Write down an inequality to represent this information.
 - (ii) Calculate the minimum value of n.

(Total 6 marks)

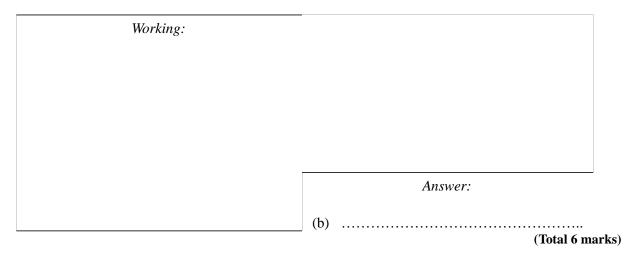
(a)	Write down u_1 .					
(b)	Calculate the common	difference of t	the sequence.			
(c)	Calculate u_4 .					
	Working:					
				Answers	<u> </u>	
			(a)	 		
			(b)	 		
			(c)	 		
			(c)	 		
ble se	e first term of an infinite quences. Find the sum of rking:		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w	third term is		(Total 6 n
ble se	quences. Find the sum of		uence is 18, w			(Total 6 n
ble se	quences. Find the sum of		uence is 18, w	third term is		(Total 6 n

Let S_n be the sum of the first n terms of an arithmetic sequence, whose first three terms are u_1 , u_2 and

- 29.) The following table shows four series of numbers. One of these series is geometric, one of the series is arithmetic and the other two are neither geometric nor arithmetic.
 - (a) Complete the table by stating the type of series that is shown.

Series		Type of series
(i)	1+11+111+1111+11111+	
(ii)	$1 + \frac{3}{4} + \frac{9}{16} + \frac{27}{64} + \dots$	
(iii)	$0.9 + 0.875 + 0.85 + 0.825 + 0.8 + \dots$	
(iv)	$\frac{1}{2} + \frac{2}{3} + \frac{3}{4} + \frac{4}{5} + \frac{5}{6} + \dots$	

(b) The geometric series can be summed to infinity. Find this sum.



30.) A company offers its employees a choice of two salary schemes A and B over a period of 10 years.

Scheme A offers a starting salary of \$11000 in the first year and then an annual increase of \$400 per year.

- (a) (i) Write down the salary paid in the second year and in the third year.
 - (ii) Calculate the **total** (amount of) salary paid over ten years.

Scheme B offers a starting salary of \$10000 dollars in the first year and then an annual increase of 7% of the previous year's salary.

- (b) (i) Write down the salary paid in the second year and in the third year.
 - (ii) Calculate the salary paid in the tenth year.

(4)

(3)

(c) Arturo works for *n* complete years under scheme A. Bill works for *n* complete years under scheme B. Find the minimum number of years so that the total earned by Bill exceeds the total earned by Arturo.

(4)

(Total 11 marks)

31.) Gwendolyn added the multiples of 3, from 3 to 3750 and found that

$$3 + 6 + 9 + \dots + 3750 = s$$
.

Calculate s.

Working:	
	Answer:
	(Total 6 marks

32.) The number of hours of sleep of 21 students are shown in the frequency table below.

Hours of sleep	Number of students
4	2
5	5
6	4
7	3
8	4
10	2
12	1

Find

- (a) the median;
- (b) the lower quartile;
- (c) the interquartile range.

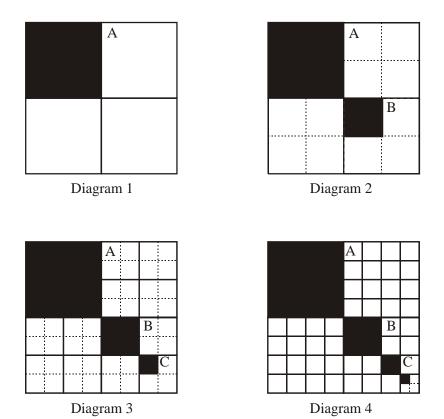
Working:	
	Answers:

(a)
(b)
(c)
(Total 6 marl

- 33.) Arturo goes swimming every week. He swims 200 metres in the first week. Each week he swims 30 metres more than the previous week. He continues for one year (52 weeks).
 - (a) How far does Arturo swim in the final week?
 - (b) How far does he swim altogether?

Working:	
	Answers:
	(a)
	(b)
	(Total 6 marks)

34.) The diagrams below show the first four squares in a sequence of squares which are subdivided in half. The area of the shaded square A is $\frac{1}{4}$.



- (a) (i) Find the area of square B and of square C.
 - (ii) Show that the areas of squares A, B and C are in geometric progression.
 - (iii) Write down the common ratio of the progression.

(5)

- (b) (i) Find the **total** area shaded in diagram 2.
 - (ii) Find the **total** area shaded in the 8th diagram of this sequence. Give your answer correct to six significant figures.

(4)

(c) The dividing and shading process illustrated is continued indefinitely. Find the total area shaded.

(2)

(Total 11 marks)

- 35.) In an arithmetic sequence, the first term is -2, the fourth term is 16, and the n^{th} term is 11998.
 - (a) Find the common difference d.
 - (b) Find the value of n.

Working:	
	Answers:
	(a)
	(b)
	(Total 6 marks

- 36.) Ashley and Billie are swimmers training for a competition.
 - (a) Ashley trains for 12 hours in the first week. She decides to increase the amount of time she spends training by 2 hours each week. Find the total number of hours she spends training during the first 15 weeks.

(3)

- (b) Billie also trains for 12 hours in the first week. She decides to train for 10% longer each week than the previous week.
 - (i) Show that in the third week she trains for 14.52 hours.
 - (ii) Find the total number of hours she spends training during the first 15 weeks.

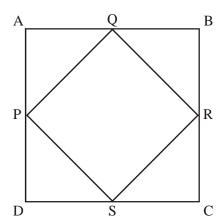
(4)

(c) In which week will the time Billie spends training first exceed 50 hours?

(4)

(Total 11 marks)

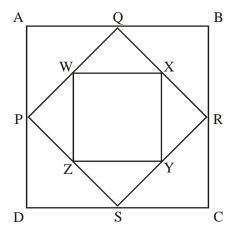
37.) The diagram shows a square ABCD of side 4 cm. The midpoints P, Q, R, S of the sides are joined to form a **second** square.



- (a) (i) Show that $PQ = 2\sqrt{2}$ cm.
 - (ii) Find the area of PQRS.

(3)

The midpoints W, X, Y, Z of the sides of PQRS are now joined to form a **third** square as shown.



- (b) (i) Write down the area of the **third** square, WXYZ.
 - (ii) Show that the areas of ABCD, PQRS, and WXYZ form a geometric sequence. Find the common ratio of this sequence.

(3)

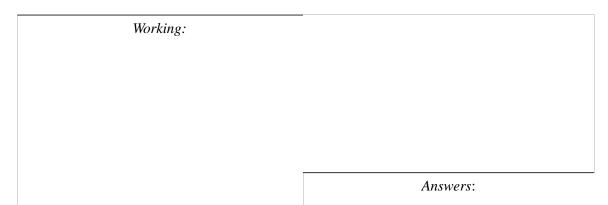
The process of forming smaller and smaller squares (by joining the midpoints) is **continued indefinitely**.

- (c) (i) Find the area of the 11th square.
 - (ii) Calculate the sum of the areas of **all** the squares.

(4)

(Total 10 marks)

- 38.) The first three terms of an arithmetic sequence are 7, 9.5, 12.
 - (a) What is the 41st term of the sequence?
 - (b) What is the sum of the first 101 terms of the sequence?



	(a)
	(b)
	(Total 4 mar
hla talanhanas ara first sald in the country	Collegaria in 1000 During 1000 the number of
sold is 160. In 1991, the number of units so	old is 240 and in 1992, the number of units sold
93 it was noticed that the annual sales form and 3rd terms being 240 and 360 respec	ned a geometric sequence with first term 160, tively.
What is the common ratio of this sequence	e?
me that this trend in sales continues.	
How many units will be sold during 2002	?
In what year does the number of units solo	d first exceed 5000?
een 1990 and 1992, the total number of uni	its sold is 760.
What is the total number of units sold bet	ween 1990 and 2002?
ng this period, the total population of Cellm	nania remains approximately 80 000.
Use this information to suggest a reason vecontinue.	why the geometric growth in sales would not
	(Total 11 mar
	ne first day she runs 1000 m, and then increases
On which day does she run a distan	nce of 10 km in training?
What is the total distance she will have ru answer exactly.	in in training by the end of that day? Give your
Working:	
	93 it was noticed that the annual sales form and 3rd terms being 240 and 360 respectively. What is the common ratio of this sequence that this trend in sales continues. How many units will be sold during 2002. In what year does the number of units sold een 1990 and 1992, the total number of units will be sold better that is the total number of units sold better that is the total number of units sold better that this information to suggest a reason we continue. day a runner trains for a 10 km race. On the istance by 250 m on each subsequent day. On which day does she run a distant what is the total distance she will have runner exactly.

	Answers:
	(a)
	(b)
	(Total 4 mark
In an arithmetic sequence, the first term is 5 and <i>Working:</i>	the fourth term is 40. Find the second term.
morking.	
	Answer:
	(Total 4 mar
Find the sum of the infinite geometric series	
$\frac{2}{3} - \frac{4}{9} + \frac{8}{27}$	16_+
3 9 27	7 81
Working:	
	Answer:

			posit of \$1000 and increases this by \$80 each t is \$1080, the next month it is \$1160 and so on.	
		Plan B, the investor again starts with \$100 ious month.	0 and each month deposits 6% more than the	
	(a)	Write down the amount of money invest	ed under Plan B in the second and third months.	(2)
	Give	your answers to parts (b) and (c) correct	to the nearest dollar.	
	(b)	Find the amount of the 12th deposit for o	each Plan.	(4)
	(c)	Find the total amount of money invested	during the first 12 months	
		(i) under Plan A;		(2)
		(ii) under Plan B.	(Total 10 ma	(2)
			(Total To ma	irks,
44.)	\$100	00 is invested at the beginning of each year	r for 10 years.	
	The	rate of interest is fixed at 7.5% per annum	. Interest is compounded annually.	
	Calc	culate, giving your answers to the nearest d	lollar	
	(a)	how much the first \$1000 is worth at the	e end of the ten years;	
	(b)	the total value of the investments at the	end of the ten years.	
		Working:		
			Answers:	
			(a)	
			(b)	
			(Total 4 ma	rks)

43.) The *Acme* insurance company sells two savings plans, Plan A and Plan B.

Working:	
	Answer:
	(Total
	(Total
	(Total
	The first term is 2 and the last term is 32. Find the sum of
an arithmetic series has five terms. ne series. Working:	
ne series.	The first term is 2 and the last term is 32. Find the sum of

45.) Find the sum of the arithmetic series