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Project 2

Algorithm 1: Target terms or Substrings

a. Pseudocode

```
Algorithm1(inputA, inputB)
  // Step 1: Initialization
  full string = inputA[0]
  output order = []
                     // Will hold the starting index of each found word
                       // Will hold the actual matched words
  output array = []
  // Step 2: Search for each word in inputB within full string
  for each word in inputB {
    index = full string.find(word) // Find the starting index of the word
    if index \neq -1 {
                              // If the word is found
       output order.append(index) // Add the index to output order
       output array.append(word) // Add the word to output array
    }
  }
  // Step 3: Combine and sort results by index
  combined = zip(output order, output array) // Create list of (index, word) pairs
  sort(combined)
                                    // Sort pairs by index (ascending)
  // Step 4: Unzip sorted results into separate arrays
  if combined is not empty {
    output order, output array = unzip(combined)
    return output order, output array
  else {
    return empty list, empty list
```

b. Analysis and Efficiency class

The algorithm runs efficiently with a time complexity of $O(m \times n + m \log m)$, where m is the number of target words and n is the length of the input string. Each word is searched using Python's find() method in linear time O(1), and the results are sorted using Timsort $O(n \log n)$, which is highly efficient. Space complexity is O(m),

c. Output

```
/usr/bin/python3 "/Users/quantruong/CSU Fullerton Dropbox/Hung Truong/CPSC 335
Algo/CPSC335_Project2/target_terms.py"
--- Result for array 1 ---
Output_order: [34, 38, 44, 51]
Output_array: ['brea', 'corona', 'modesto', 'clovis']
--- Result for array 2 ---
Output_order: [12, 25, 43, 49]
Output_array: ['fremont', 'fullerton', 'fresno', 'chino']
--- Result for array 3 ---
Output_order: [21, 26, 43, 59]
Output_array: ['marco', 'oxnard', 'irvine', 'orange']
```

Algorithm 2: Run Encoding Problem

a. Pseudocode:

```
Algorithm string run encoding(string)
  If S is empty Then
     Return an empty string
  result \leftarrow empty list
  count \leftarrow 1
  For i from 1 to Length(S) - 1 Do
     If S[i] == S[i - 1] Then
       Increment count
     Else
       If count > 1 Then
          Append count and S[i - 1] to result
       Else
          Append S[i - 1] to result
       End If
       count \leftarrow 1
     End If
  End for
```

```
# Process last run
If count > 1 Then
   Append count and S[length(S) - 1] to result
Else
   Append S[length(S) - 1] to result
End If
```

Return concatenation of all elements in result End

b. Analysis and Efficiency Class

- 1. Checking if the string is empty \rightarrow O(1)
- 2. Initialize variables \rightarrow O(1)
- 3. For loop iterating over string (n-1 times where n is the length of S) \rightarrow O(n) Inside the loop:
 - a. Comparison and increment \rightarrow O(1)
 - b. Else, comparison and append \rightarrow O(1)
 - c. Reset count \rightarrow O(1)
- 4. Last run, if comparison and append \rightarrow O(1)
- 5. Return statement \rightarrow O(n)

The dominant term in the analysis is O(n) from the main loop and the final string concatenation, and since we ignore the constants, the final efficiency class is O(n).

c. Output

```
quantruong@Quans-MacBook-Air CPSC335_Project2 % python3 string_run_encoding.py "ddd" becomes "3d" "heloooooooo there" becomes "hel8o there" "choosemeeky and tuition-free" becomes "ch2osem2eky and tuition-fr2e"
```

Algorithm 3: Merging Techniques

a. Pseudocode

```
Algorithm merging_array(list_of_arrays)

min_heap = [] // Create a min-heap to store the current smallest elements

merged_list = [] // Create an empty list to hold the final sorted output

// Step 1: Push the first element of each list into the min_heap

For i from 0 to length of list_of_arrays - 1:

current list = list of arrays[i]
```

```
If current_list is not empty:
    value = current_list[0]
    Push (value, i, 0) into min_heap
    // (value, list_index, element_index)

// Step 2: Process the min_heap

While min_heap is not empty:
    Pop (value, list_index, element_index) from min_heap
    Append value to merged_list

// If there's a next element in the same list

If element_index + 1 < length of list_of_arrays[list_index]:
    next_value = list_of_arrays[list_index][element_index + 1]

    Push (next_value, list_index, element_index + 1) into min_heap

Return merged_list
```

b. Analysis and Efficiency class

The merge_sorted_list algorithm uses a min-heap to merge k sorted lists with N elements. It first inserts the first element of each list into the heap in O(k log k) time. Then, for each of the N elements, it performs a heap pop and possibly a push, each taking O(log k) time. This results in a merging phase that runs in O(N log k) time. Overall, the algorithm runs in O(N log k) time, making it efficient for merging multiple sorted lists, especially when k is much smaller than N.

c. Output

```
quantruong@Quans-MacBook-Air CPSC335_Project2 % python3 merging_techniques.py
Array_1: [-10, -1, 0, 2, 2, 4, 5, 6, 9, 12, 20, 21, 81, 121, 150]
Array_2: [-3, 0, 3, 7, 8, 9, 10, 11, 11, 12, 17, 18, 19, 21, 29, 29, 81, 88, 121, 131]
Array_3: [-4, -2, 0, 2, 4, 5, 6, 6, 7, 10, 10, 12, 14, 15, 20, 24, 25]
```