examples

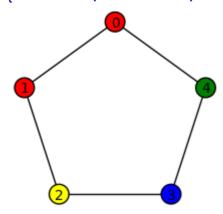
```
attach "/Users/araichev/graph_dynamics/graph_dynamics.py"

# For a list of Sage's graph generators, see
http://wiki.sagemath.org/graph_generators.
```

```
# Example: Use color()

G = graphs.CycleGraph(5)
coloring = color(G, ['red', 'red', 'yellow', 'blue', 'green'])
print(coloring)
G.show(vertex_colors=invert_dict(coloring), figsize=3)
```

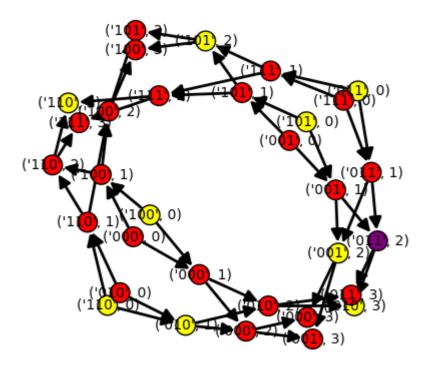
{0: 'red', 1: 'red', 2: 'yellow', 3: 'blue', 4: 'green'}



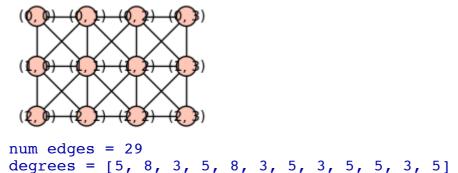
```
# Example: Use color_randomly() and color_count()

G = digraphs.ButterflyGraph(3)
coloring = color_randomly(G, {'red': 0.6, 'yellow': 0.3,
'purple': 1/10})
print(coloring)
print('Color count = {!s}'.format(color_count(coloring)))
G.show(vertex_colors=invert_dict(coloring), figsize=5)
```

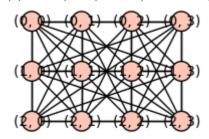
```
{('101', 1): 'red', ('111', 3): 'red', ('001', 2): 'yellow',
0): 'yellow', ('110', 2): 'red', ('010', 2): 'red', ('000', 2
'red', ('011', 3): 'red', ('101', 0): 'yellow', ('001', 3): '
('100', 1): 'red', ('110', 1): 'red', ('010', 3): 'yellow', (
0): 'red', ('011', 2): 'purple', ('000', 1): 'red', ('101', 3
'red', ('001', 0): 'red', ('110', 0): 'yellow', ('111', 1): '
('011', 1): 'red', ('100', 2): 'red', ('010', 0): 'red', ('00', 1): 'red', ('111', 2): '
('011', 0): 'yellow', ('100', 3): 'red', ('110', 3): 'yellow'
('010', 1): 'yellow', ('000', 3): 'red'}
Color count = Counter({'red': 22, 'yellow': 9, 'purple': 1})
```



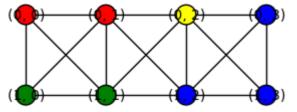
```
# Test the Moore lattice generator
G = moore_lattice(3, 4)
G.show(figsize=2)
print('num edges = {!s}'.format(G.num edges()))
print('degrees = %s' % G.degree())
print(G.edges())
G = moore lattice(3, 4, toroidal=True)
G.show(figsize=2)
print('num edges = %s' % G.num_edges())
print('degrees = %s' % G.degree())
print(G.edges())
G = moore lattice(2, 4)
coloring = color(G, ['red', 'red', 'yellow', 'blue', 'green',
'green', 'blue', 'blue'])
G.show(vertex_colors=invert_dict(coloring), figsize=3)
print(coloring)
```



[((0, 0), (0, 1), None), ((0, 0), (1, 0), None), ((0, 0), (1, None), ((0, 1), (0, 2), None), ((0, 1), (1, 0), None), ((0, 1), 1), None), ((0, 1), (1, 2), None), ((0, 2), (0, 3), None), ((1, 1), None), ((0, 2), (1, 2), None), ((0, 2), (1, 3), None), ((1, 1), None), ((0, 3), (1, 3), None), ((1, 0), (1, 1), None), ((1, 0), (2, 1), None), ((1, 1), (1, None), ((1, 1), (2, 0), None), ((1, 1), (2, 1), None), ((1, 1), (2), None), ((1, 2), (1, 3), None), ((1, 2), (2, 1), None), ((2, 2), None), ((1, 2), (2, 3), None), ((2, 1), None), ((2, 2), None), ((2, 2), None)]



num edges = 48degrees = [8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8] [((0, 0), (0, 1), None), ((0, 0), (0, 3), None), ((0, 0), (1, 0))]None), ((0, 0), (1, 1), None), ((0, 0), (1, 3), None), ((0, 0), None), ((0, 0), (2, 1), None), ((0, 0), (2, 3), None)(0, 2), None), ((0, 1), (1, 0), None), ((0, 1), (1, 1), None) 1), (1, 2), None), ((0, 1), (2, 0), None), ((0, 1), (2, 1), None) ((0, 1), (2, 2), None), ((0, 2), (0, 3), None), ((0, 2), (1, 2), (1, 3), (1,None), ((0, 2), (1, 2), None), ((0, 2), (1, 3), (1, 3), (1, 3), ((0, 2), (1, 3), ((0, 2), (1, 3), ((0, 2), ((1), None), ((0, 2), (2, 2), None), ((0, 2), (2, 3), None), ((1, 0), None), ((0, 3), (1, 2), None), ((0, 3), (1, 3), None) 3), (2, 0), None), ((0, 3), (2, 2), None), ((0, 3), (2, 3), N ((1, 0), (1, 1), None), ((1, 0), (1, 3), None), ((1, 0), (2, 1))None), ((1, 0), (2, 1), None), ((1, 0), (2, 3), None), ((1, 1 2), None), ((1, 1), (2, 0), None), ((1, 1), (2, 1), None), (((2, 2), None), ((1, 2), (1, 3), None), ((1, 2), (2, 1), None) 2), (2, 2), None), ((1, 2), (2, 3), None), ((1, 3), (2, 0), None) ((1, 3), (2, 2), None), ((1, 3), (2, 3), None), ((2, 0), (2, 3), (2,None), ((2, 0), (2, 3), None), ((2, 1), (2, 2), None), ((2, 2), (2,3), None)]



{(0, 1): 'red', (1, 2): 'blue', (0, 0): 'red', (0, 2): 'yellc'; 'blue', (1, 0): 'green', (0, 3): 'blue', (1, 1): 'green'}

```
# Test the triangular lattice generator

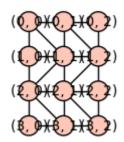
G = triangular_lattice(4, 3)

G.show(figsize=2)
print('num edges = {!s}'.format(G.num_edges()))
```

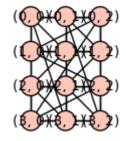
```
print('degrees = %s' % G.degree())
print(G.edges())

G = triangular_lattice(4, 3, toroidal=True)
G.show(figsize=2)
print('num edges = %s' % G.num_edges())
print('degrees = %s' % G.degree())
print(G.edges())

G = triangular_lattice(2, 4)
coloring = color(G, ['red', 'red', 'yellow', 'blue', 'green', 'green', 'blue', 'blue'])
G.show(vertex_colors=invert_dict(coloring), figsize=3)
print(coloring)
```



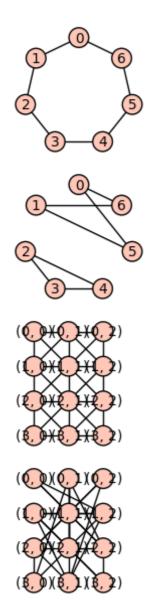
num edges = 23
degrees = [4, 5, 3, 3, 2, 4, 6, 6, 5, 3, 3, 2]
[((0, 0), (0, 1), None), ((0, 0), (1, 0), None), ((0, 0), (1, None), ((0, 1), (0, 2), None), ((0, 1), (1, 1), None), ((0, 1
2), None), ((0, 2), (1, 2), None), ((1, 0), (1, 1), None), ((2, 0), None), ((1, 1), (1, 2), None), ((1, 1), (2, 0), None)
1), (2, 1), None), ((1, 2), (2, 1), None), ((1, 2), (2, 2), None), ((2, 0), (2, 1), None), ((2, 0), (3, 0), None), ((2, 0), (3, None), ((2, 1), (2, 2), None), ((2, 1), (3, 1), None), ((2, 1), None), ((3, 2), None)]



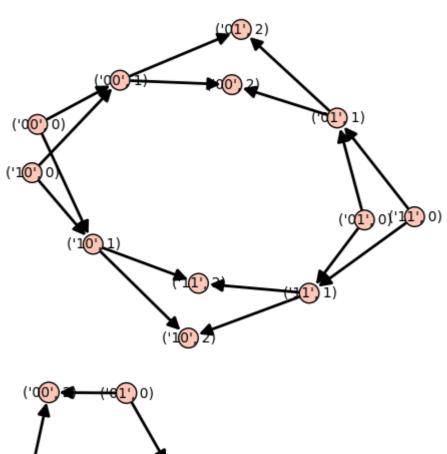
```
2), None), ((1, 1), (2, 0), None), ((1, 1), (2, 1), None), ((
    (2, 1), None), ((1, 2), (2, 2), None), ((2, 0), (2, 1), None)
   0), (2, 2), None), ((2, 0), (3, 0), None), ((2, 0), (3, 1), None)
   ((2, 1), (2, 2), None), ((2, 1), (3, 1), None), ((2, 1), (3,
   None), ((2, 2), (3, 0), None), ((2, 2), (3, 2), None), ((3, (
   1), None), ((3, 0), (3, 2), None), ((3, 1), (3, 2), None)]
   {(0, 1): 'red', (1, 2): 'blue', (0, 0): 'red', (0, 2): 'yellc
   3): 'blue', (1, 0): 'green', (0, 3): 'blue', (1, 1): 'green'}
# Test the Maslov-Sneppen rewiring method
G = graphs.CycleGraph(7)
G.show(figsize=2)
H = maslov sneppen(G)
H.show(figsize=2)
G = moore lattice(4, 3)
G.show(figsize=2)
H = maslov sneppen(G)
H.show(figsize=2)
print(G.num verts() == H.num verts())
print(G.num_edges() == H.num_edges())
print(G.degree() == H.degree())
G = graphs.RandomBarabasiAlbert(50, 5)
H = maslov sneppen(G)
print(G.num_verts() == H.num_verts())
print(G.num edges() == H.num edges())
print(G.degree() == H.degree())
G = digraphs.ButterflyGraph(2)
G.show(figsize=5)
H = maslov sneppen(G)
H.show(figsize=5)
```

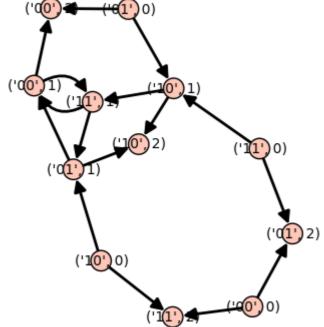
print(G.num_verts() == H.num_verts())
print(G.num edges() == H.num edges())

print(G.degree() == H.degree())



True True True True True True





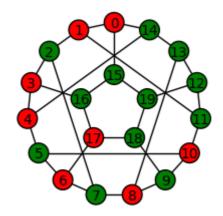
True True True

```
# Example: Run the majority rule

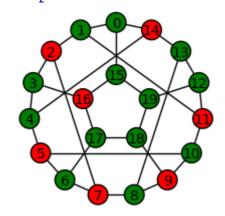
G = graphs.FlowerSnark()
color_bias = {'green': 0.7, 'red': 0.3}
ur = majority_rule
ur_kwargs = {}
initial_coloring = color_randomly(G, color_bias)
s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
```

```
print('Stabilized?\n %s' % stabilized)
print(s)
show_colorings(G, s, vertex_labels=True)
```

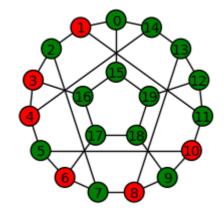
Stabilized? False [{0: 'red', 1: 'red', 2: 'green', 3: 'red', 4: 'red', 5: 'gre 'red', 7: 'green', 8: 'red', 9: 'green', 10: 'red', 11: 'gree 'green', 13: 'green', 14: 'green', 15: 'green', 16: 'green', 'red', 18: 'green', 19: 'green'}, {0: 'green', 1: 'green', 2: 3: 'green', 4: 'green', 5: 'red', 6: 'green', 7: 'red', 8: 'c 9: 'red', 10: 'green', 11: 'red', 12: 'green', 13: 'green', 1 'red', 15: 'green', 16: 'red', 17: 'green', 18: 'green', 19: 'green'}, {0: 'green', 1: 'red', 2: 'green', 3: 'red', 4: 're 'green', 6: 'red', 7: 'green', 8: 'red', 9: 'green', 10: 'red 'green', 12: 'green', 13: 'green', 14: 'green', 15: 'green', 'green', 17: 'green', 18: 'green', 19: 'green'}, {0: 'green', 'green', 2: 'red', 3: 'green', 4: 'green', 5: 'red', 6: 'gree 'red', 8: 'green', 9: 'red', 10: 'green', 11: 'red', 12: 'gre 13: 'green', 14: 'green', 15: 'green', 16: 'green', 17: 'gree 'green', 19: 'green'}, {0: 'green', 1: 'red', 2: 'green', 3: 'green', 4: 'green', 5: 'green', 6: 'red', 7: 'green', 8: 're 'green', 10: 'red', 11: 'green', 12: 'green', 13: 'green', 14 'green', 15: 'green', 16: 'green', 17: 'green', 18: 'green', 'green'}, {0: 'green', 1: 'green', 2: 'green', 3: 'green', 4: 'green', 5: 'red', 6: 'green', 7: 'red', 8: 'green', 9: 'red' 'green', 11: 'red', 12: 'green', 13: 'green', 14: 'green', 15 'green', 16: 'green', 17: 'green', 18: 'green', 19: 'green'}, 'green', 1: 'green', 2: 'green', 3: 'green', 4: 'green', 5: ' 6: 'red', 7: 'green', 8: 'red', 9: 'green', 10: 'red', 11: 'c 12: 'green', 13: 'green', 14: 'green', 15: 'green', 16: 'gree 'green', 18: 'green', 19: 'green'}, {0: 'green', 1: 'green', 'green', 3: 'green', 4: 'green', 5: 'red', 6: 'green', 7: 're 'green', 9: 'red', 10: 'green', 11: 'green', 12: 'green', 13: 'green', 14: 'green', 15: 'green', 16: 'green', 17: 'green', 'green', 19: 'green', {0: 'green', 1: 'green', 2: 'green', 3 'green', 4: 'green', 5: 'green', 6: 'red', 7: 'green', 8: 're 'green', 10: 'red', 11: 'green', 12: 'green', 13: 'green', 14 'green', 15: 'green', 16: 'green', 17: 'green', 18: 'green', 'green', {0: 'green', 1: 'green', 2: 'green', 3: 'green', 4: 'green', 5: 'red', 6: 'green', 7: 'red', 8: 'green', 9: 'red' 'green', 11: 'green', 12: 'green', 13: 'green', 14: 'green', 'green', 16: 'green', 17: 'green', 18: 'green', 19: 'green'}, 'green', 1: 'green', 2: 'green', 3: 'green', 4: 'green', 5: ' 6: 'red', 7: 'green', 8: 'red', 9: 'green', 10: 'red', 11: 'c 12: 'green', 13: 'green', 14: 'green', 15: 'green', 16: 'gree 'green', 18: 'green', 19: 'green'}] Step 0



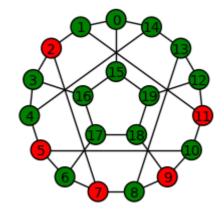
Step 1



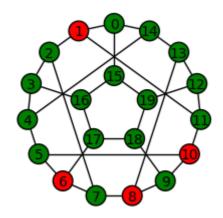
Step 2



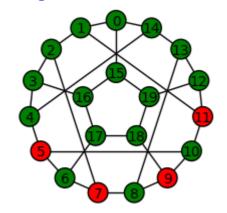
Step 3



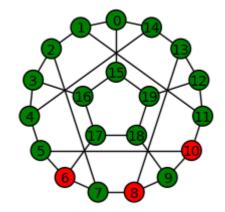
Step 4



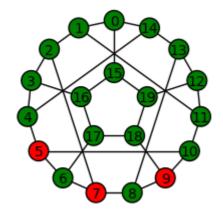
Step 5



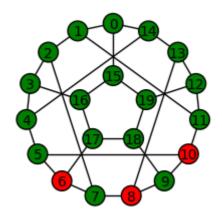
Step 6



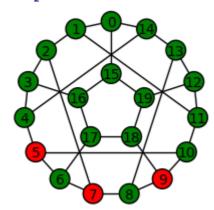
Step 7



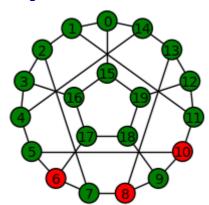
Step 8



Step 9



Step 10

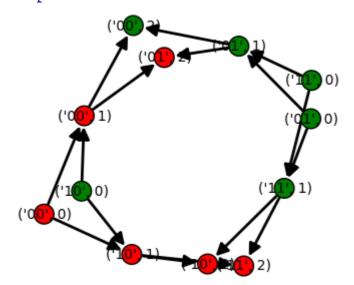


```
# Example: Run the majority rule on a directed graph

G = digraphs.ButterflyGraph(2)
color_bias = {'green': 0.7, 'red': 0.3}
ur = majority_rule
ur_kwargs = {}
initial_coloring = color_randomly(G, color_bias)
s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
print(s)
show_colorings(G, s, vertex_labels=True, figsize=4)
```

Stabilized? True

```
[{('11', 1): 'green', ('10', 2): 'red', ('01', 2): 'red', ('1 'green', ('01', 0): 'green', ('01', 1): 'green', ('00', 1): '('11', 2): 'red', ('00', 0): 'red', ('00', 2): 'green', ('10' 'green', ('10', 1): 'red'}]
Step 0
```

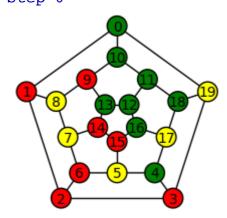


```
# Example: Run the plurality rule.

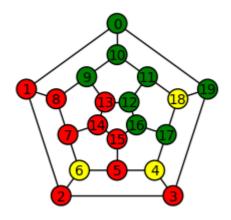
G = graphs.DodecahedralGraph()
ur = plurality_rule
ur_kwargs = {}
color_bias = {'green': 0.6, 'red': 0.3, 'yellow': 0.1}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s, vertex_labels=True)
```

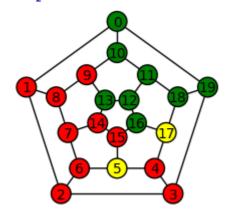
Stabilized? False Step 0



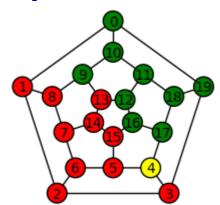
Step 1



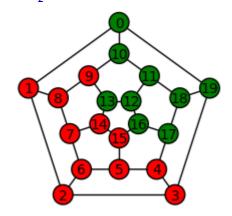
Step 2



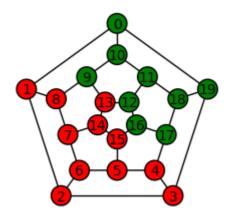
Step 3



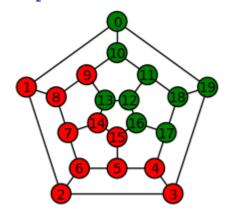
Step 4



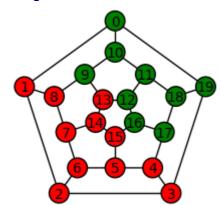
Step 5



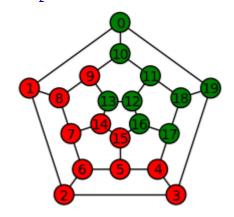
Step 6



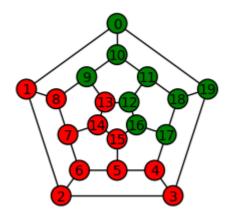
Step 7



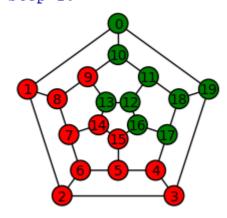
Step 8



Step 9



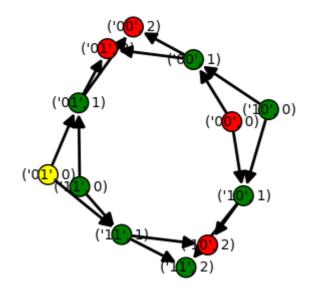
Step 10



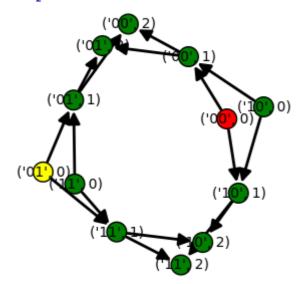
```
# Example: Run the plurality rule.

G = digraphs.ButterflyGraph(2)
ur = plurality_rule
ur_kwargs = {}
color_bias = {'green': 0.6, 'red': 0.3, 'yellow': 0.1}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s, vertex_labels=True, figsize=4)
```



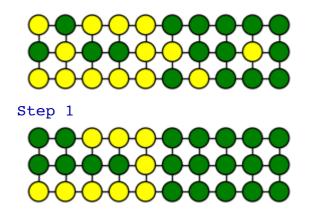
Step 1



```
# Example: Run the GSL2 rule.

G = graphs.Grid2dGraph(3, 10)
color_bias = {'green': 0.6, 'yellow': 0.4}
ur = gsl2_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.7}
initial_coloring = color_randomly(G, color_bias)

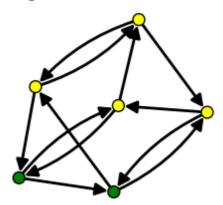
s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s)
```



```
# Example: Run the GSL2 rule.

G = digraphs.Kautz(2, 2)
color_bias = {'green': 0.6, 'yellow': 0.4}
ur = gsl2_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.7}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s)
```



```
# Example: Run the GSL3 rule.

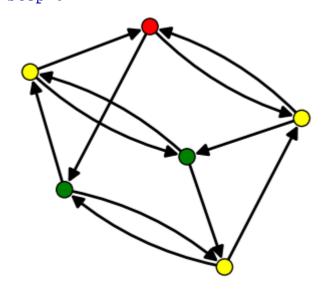
G = graphs.Grid2dGraph(3, 10)
color_bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = gsl3_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.6}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s)
```

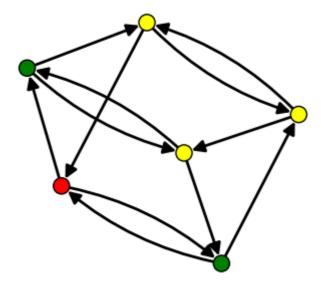
Stabilized? True Step 0 Step 1 Step 2 Step 3 Step 4 Step 5 Step 6 Step 7

```
G = digraphs.Kautz(2, 2)
color_bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = gsl3_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.6}
initial_coloring = color_randomly(G, color_bias)

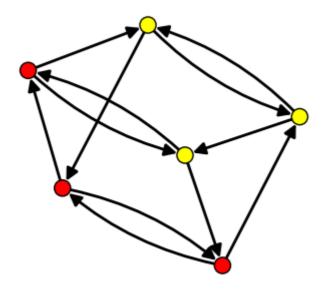
s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s, figsize=4)
```



Step 1



Step 2

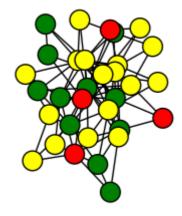


```
# Example: Run the GSL3 rule on a random graph

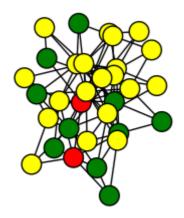
gg = graphs.RandomBarabasiAlbert
print(gg)
G = gg(32, 3)
color_bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = gsl3_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.6}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s)
```

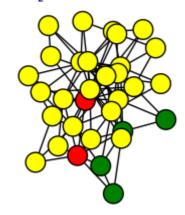
<function RandomBarabasiAlbert at 0x10c58e1b8>
Stabilized?
True
Step 0



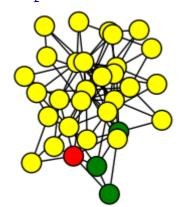
Step 1



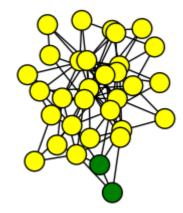
Step 2



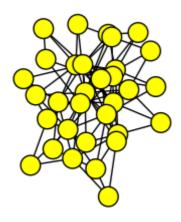
Step 3



Step 4



Step 5

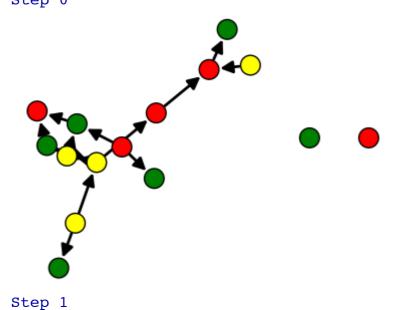


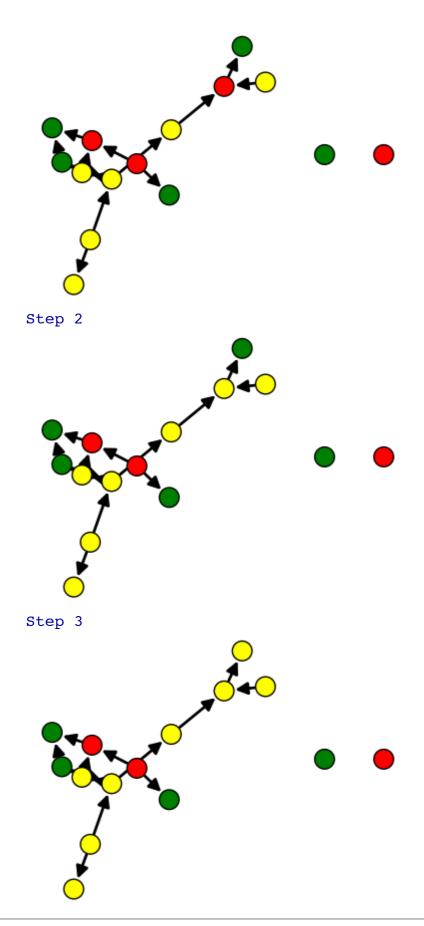
```
# Example: Run the GSL3 rule on a random graph

gg = digraphs.RandomDirectedGNP
print(gg)
G = gg(15, .1)
color_bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = gsl3_rule
ur_kwargs = {'palette': color_bias.keys(), 'T': 0.6}
initial_coloring = color_randomly(G, color_bias)

s, stabilized = run_rule(ur, ur_kwargs, G, initial_coloring)
print('Stabilized?\n %s' % stabilized)
show_colorings(G, s, figsize=4)
```

<bound method DiGraphGenerators.RandomDirectedGNP of
<sage.graphs.digraph_generators.DiGraphGenerators instance at
0x10b1cd4d0>>
Stabilized?
 True
Step 0





Example: Use run_rule_many_times() on one graph

```
color bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = qs13 rule
urk = {'palette': color bias.keys()}
gg = moore lattice
ggk = {'r': 8, 'c': 16, 'toroidal': True}
cf = color randomly
cfk = {'bias': color bias}
num runs = 1000
num stabilized, mean_steps, mean_initial, mean_final =
run rule many times(ur, urk, qq, qqk, cf, cfk,
num runs=num runs)
   <function gsl3 rule at 0x10c4c3848>
   <function moore lattice at 0x10c4c38c0>
   <function color_randomly at 0x10c4c3668>
   _____
   Number of runs: 1000
   Number of runs that stabilized: 736
   Mean number of steps required to stabilize: 6.53
   Mean initial color counts:
       green: 42.5
       red: 43
       yellow: 42.6
   Mean final color counts:
       green: 43.7
       red: 39.2
       yellow: 45
# Example: Use run rule many times() on many instances of a
random graph
color_bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = qs13 rule
urk = {'palette': color bias.keys(), 'T': 0.5, 't': 0.25, 's':
0.25}
gg = maslov sneppen
ml = moore lattice(r=8, c=16, toroidal=True)
ggk = {'graph': ml} # Warning: Maslov-Sneppon does 4096 (=
4*num edges) steps on this graph. Slow!
cf = color randomly
cfk = {'bias': color_bias}
num runs = 10
num stabilized, mean steps, mean initial, mean final =
run rule many times(ur, urk, gg, ggk, cf, cfk,
num runs=num runs)
   <function gsl3 rule at 0x10c4c3848>
   <function maslov sneppen at 0x10c4c39b0>
   <function color randomly at 0x10c4c3668>
   ______
   Number of runs: 10
```

```
Number of runs that stabilized: 9
   Mean number of steps required to stabilize: 4
   Mean initial color counts:
       green: 46.2
       red: 39.7
       yellow: 42.1
   Mean final color counts:
       green: 50.1
       red: 41.9
       yellow: 36
# Exploring the random Barabasi Albert graph
G = graphs.RandomBarabasiAlbert(128, 4)
n = G.num verts()
degrees = G.degree()
ave degree = sum(degrees)/n
print('nvertices = {!s}'.format(n))
print('degrees = {!s}'.format(degrees))
print('ave degree = {:.3f}'.format(ave degree))
   nvertices = 128
   degrees = [5, 7, 23, 34, 46, 26, 21, 20, 27, 29, 11, 14, 12,
   16, 8, 12, 9, 11, 11, 10, 12, 4, 7, 11, 11, 10, 14, 7, 7, 9,
   8, 8, 11, 4, 13, 5, 4, 7, 9, 7, 7, 4, 5, 7, 7, 14, 6, 4, 7, 4
   7, 4, 5, 4, 8, 6, 6, 5, 6, 4, 7, 4, 5, 5, 4, 4, 6, 4, 4, 5,
   5, 5, 6, 5, 5, 4, 6, 4, 6, 4, 5, 4, 5, 6, 6, 6, 4, 5, 6, 4, 5
   4, 4, 4, 4, 5, 4, 4, 5, 4, 4, 5, 4, 4, 4, 4, 4, 4, 4, 4, 4
   4, 4, 4]
   ave degree = 7.000
# Example: Use run_rule_many_times() on many instances of a
random graph
color bias = {'green': 1/3, 'red': 1/3, 'yellow': 1/3}
ur = qs13 rule
urk = {'palette': color_bias.keys(), 'T': 0.5, 't': 0.25, 's':
gg = graphs.RandomBarabasiAlbert
qqk = \{'n': 128, 'm': 4\}
cf = color randomly
cfk = {'bias': color bias}
num runs = 1000
num stabilized, mean_steps, mean_initial, mean_final =
run rule many times(ur, urk, gg, ggk, cf, cfk,
num runs=num runs)
   <function gsl3 rule at 0x10c4c3848>
   <function RandomBarabasiAlbert at 0x10c58e1b8>
   <function color randomly at 0x10c4c3668>
```

```
Number of runs: 1000
Number of runs that stabilized: 911
Mean number of steps required to stabilize: 4.96
Mean initial color counts:
    green: 42.5
    red: 42.6
    yellow: 42.9
Mean final color counts:
    green: 43.1
    red: 38.7
    yellow: 46.2
```