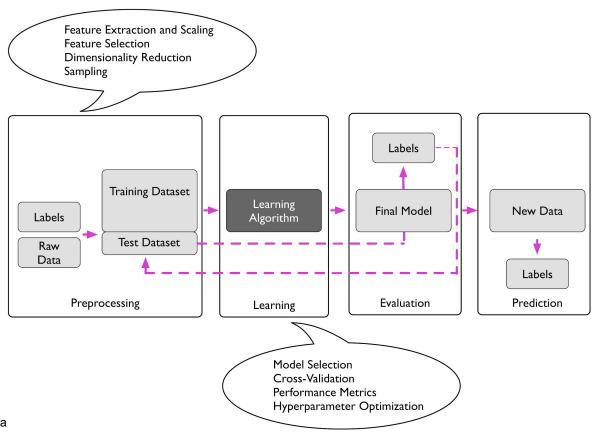
#### Lecture 12

### **Decision trees**

https://github.com/dalcimar/MA28CP-Intro-to-Machine-Learning
UTFPR - Federal University of Technology - Paraná
https://www.dalcimar.com/

## Machine learning pipeline

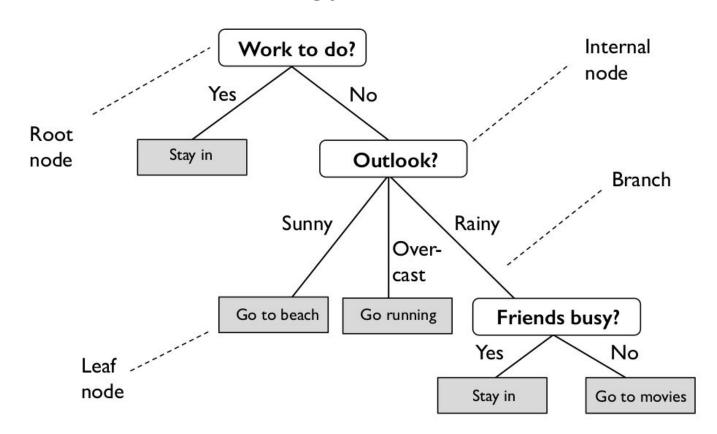


Python Machine Learning by Sebastian Raschka

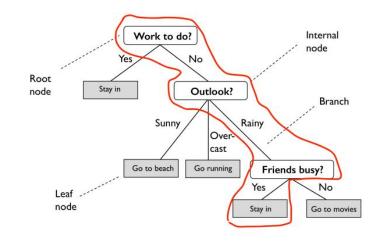
### Topics

- Intro to decision trees
- 2. Recursive and divide & conquer strategy
- 3. Types of decision trees
- 4. Splitting criteria
- 5. Gini & Entropy vs misclassification error
- 6. Improvements & dealing with overfitting
- 7. Code example

### Decision tree terminology



#### Decision tree as rulersets



IF \_\_\_\_\_\_

2<del>-1--</del>: <del>2-1--</del>--

THEN \_\_\_\_\_

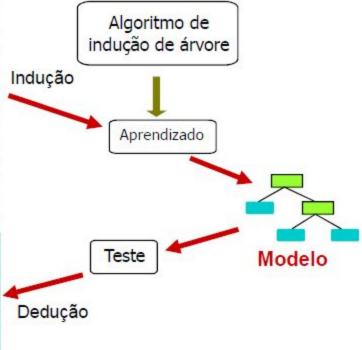
### Decision tree pipeline

Conjunto de treinamento

ld	E Credor	Estado Civil	Salário	Calote
1	Sim	Solteiro	125K	Não
2	Não	Casado	100K	Não
3	Não	Solteiro	70K	Não
4	Sim	Casado	120K	Não
5	Não	Divorciado	95K	Sim
6	Não	Casado	60K	Não
7	Sim	Divorciado	220K	Não
8	Não	Solteiro	85K	Sim
9	Não	Casado	75K	Não
10	Não	Solteiro	90K	Sim

Conjunto de teste

ld	E Credor	Estado Civil	Salário	Calote
11	Não	Casado	80K	?
12	Não	Solteiro	100K	?
13	Sim	Solteiro	100K	?
14	Não	Casado	120K	?
15	Sim	Solteiro	80K	?



### **Training**

- Works on categorical (binary, nominal or ordinal) and
- Works also with numeric (continuos) attributes

Id	E	Estado	Salário	Calote
	Credor	Civil		
1	Sim	Solteiro	125K	Não
2	Não	Casado	100K	Não
3	Não	Solteiro	70K	Não
4	Sim	Casado	120K	Não
5	Não	Divorciado	95K	Sim
6	Não	Casado	60K	Não
7	Sim	Divorciado	220K	Não
8	Não	Solteiro	85K	Sim
9	Não	Casado	75K	Não
10	Não	Solteiro	90K	Sim

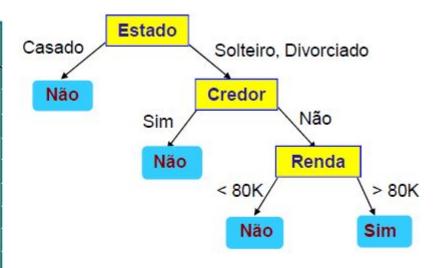
Atributos de Decisão Credor Sim Não Não Estado Casado Solteiro, Divorciado Renda Não < 80K > 80K Não Sim

**Dados de Treinamento** 

Modelo: Árvore de Decisão

## Training

ld	E Credor	Estado Civil	Salário	Calote
1	Sim	Solteiro	125K	Não
2	Não	Casado	100K	Não
3	Não	Solteiro	70K	Não
4	Sim	Casado	120K	Não
5	Não	Divorciado	95K	Sim
6	Não	Casado	60K	Não
7	Sim	Divorciado	220K	Não
8	Não	Solteiro	85K	Sim
9	Não	Casado	75K	Não
10	Não	Solteiro	90K	Sim



Diferentes árvores podem ser ajustadas para os mesmos dados !

### Decision tree on Iris dataset (2 features)

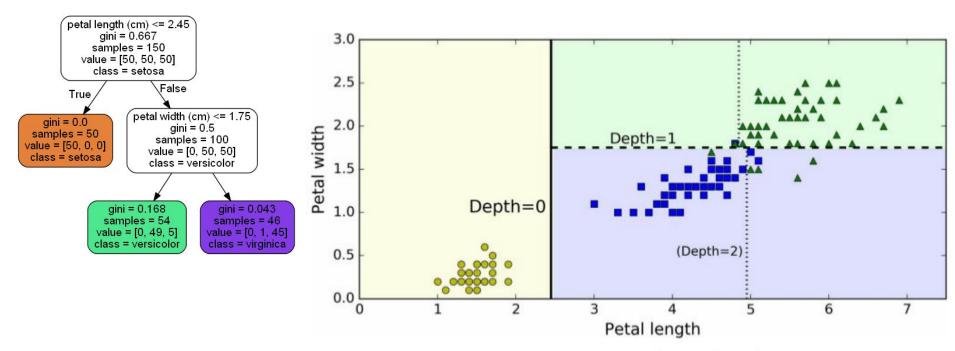
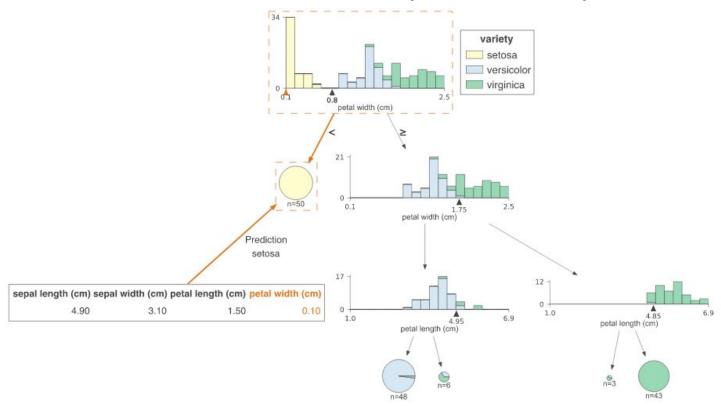
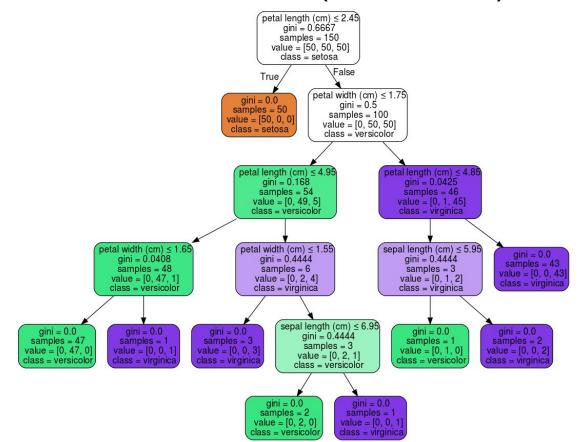


Figure 6-2. Decision Tree decision boundaries

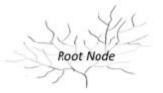
### Decision tree on Iris dataset (2 features)

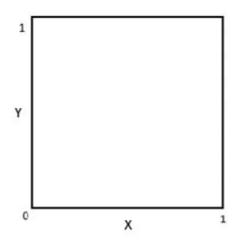


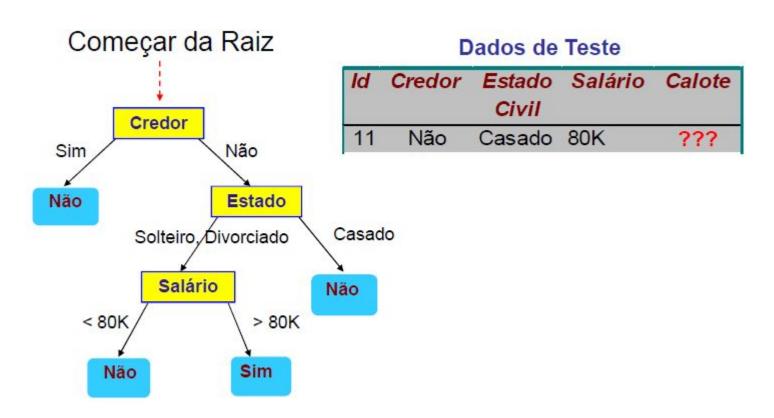
### Decision tree on Iris dataset (4 features)

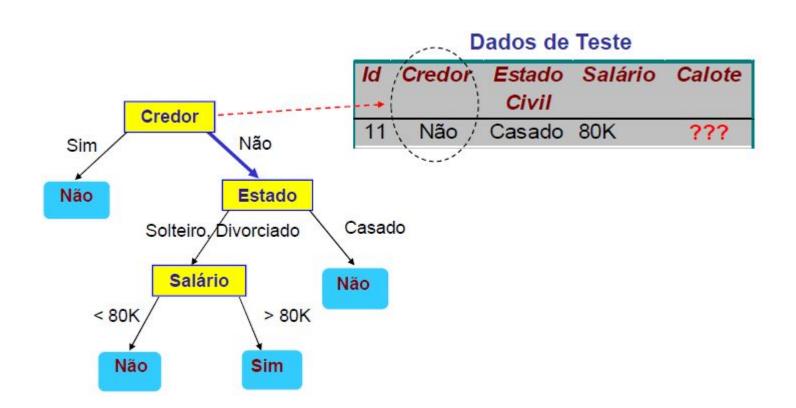


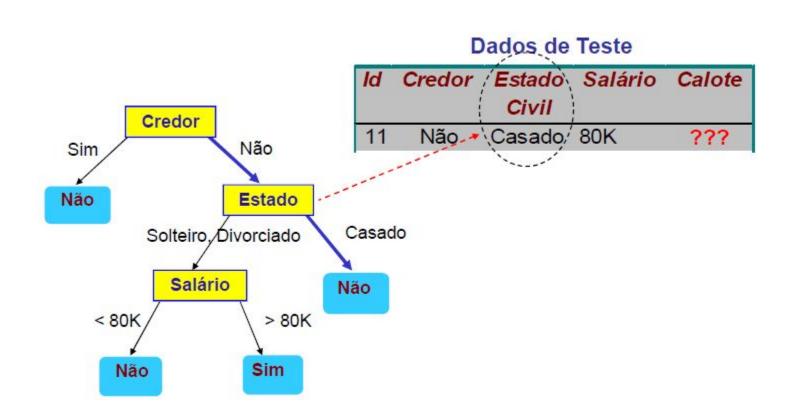
## Growing depth process

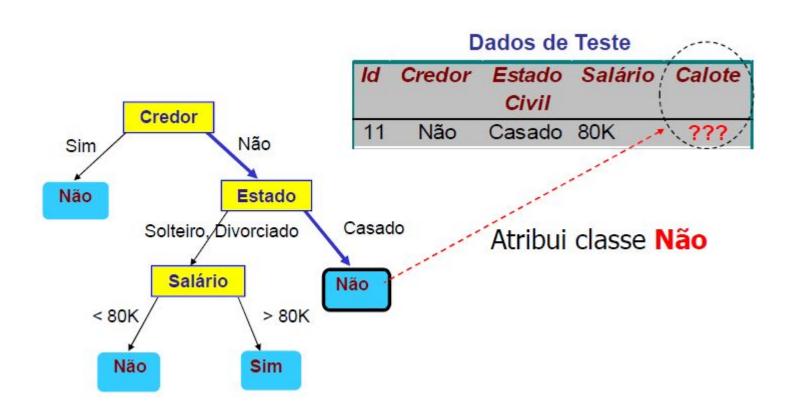












### Tree depth overfitting

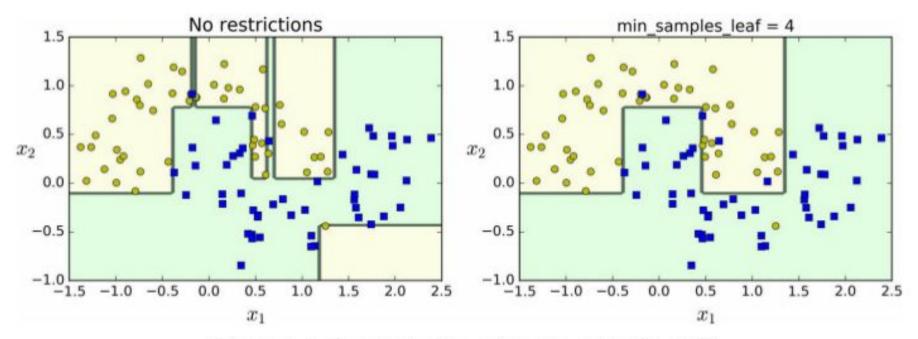


Figure 6-3. Regularization using min\_samples\_leaf

#### **Animations**

Amazing animation of decision tree

http://www.r2d3.us/visual-intro-to-machine-learning-part-1/

### **Topics**

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### Recursion / Recursive Algorithms

What does this function do?

```
1 def some_fun (x):
2    if x == []:
3       return 0
4    else:
5     return 1 + some_fun (x[1:])
```

# Divide & Conquer Algorithms: Quicksort

```
def quicksort(array):
       if len(array) < 2:
            return array
       else:
            pivot = array[0]
6
            smaller, bigger = [], []
            for ele in array[1:]:
                if ele <= pivot:
                    smaller.append(ele)
9
10
                else:
11
                    bigger.append(ele)
            return quicksort(smaller) + [pivot] + quicksort(bigger)
12
```

### Divide & Conquer Algorithms: Quicksort

```
1 def quicksort(array):
       if len(array) < 2:
           return array
       else:
           pivot = array[0]
           smaller, bigger = [], []
           for ele in array[1:]:
               if ele <= pivot:
                   smaller.append(ele)
10
               else:
11
                   bigger.append(ele)
12
           return quicksort(smaller) + [pivot] + quicksort(bigger)
```

### Time complexity of quicksort

#### O(n log n)

```
def quicksort(array):
        if len(array) < 2:
            return array
 4
       else:
            pivot = array[0]
            smaller, bigger = [], []
 6
            for ele in array[1:]:
                if ele <= pivot:
8
9
                    smaller.append(ele)
10
                else:
                    bigger.append(ele)
11
12
            return quicksort(smaller) + [pivot] + quicksort(bigger)
```

## Time and space complexity of sorting algorithms

Algorithm	Time Complexity			Space Complexity
	Best	Average	Worst	Worst
Quicksort	$\Omega(n \log(n))$	O(n log(n))	0(n^2)	O(log(n))
Mergesort	$\Omega(n \log(n))$	O(n log(n))	O(n log(n))	0(n)
Timsort	$\Omega(n)$	O(n log(n))	O(n log(n))	0(n)
<u>Heapsort</u>	$\Omega(n \log(n))$	Θ(n log(n))	O(n log(n))	0(1)
Bubble Sort	$\Omega(n)$	0(n^2)	0(n^2)	0(1)
Insertion Sort	$\Omega(n)$	Θ(n^2)	0(n^2)	0(1)
Selection Sort	$\Omega(n^2)$	Θ(n^2)	0(n^2)	0(1)
Tree Sort	$\Omega(n \log(n))$	O(n log(n))	0(n^2)	0(n)
Shell Sort	$\Omega(n \log(n))$	$\Theta(n(\log(n))^2)$	O(n(log(n))^2)	0(1)
Bucket Sort	$\Omega(n+k)$	Θ(n+k)	0(n^2)	0(n)
Radix Sort	$\Omega(nk)$	Θ(nk)	O(nk)	0(n+k)
Counting Sort	$\Omega(n+k)$	O(n+k)	0(n+k)	0(k)
Cubesort	$\Omega(n)$	Θ(n log(n))	O(n log(n))	0(n)

### Decision Tree in Pseudocode

#### GenerateTree( $\mathcal{D}$ ):

- if  $y=1 \ \forall \ \langle \mathbf{x},\mathbf{y} \rangle \in \mathcal{D} \text{ or } y=0 \ \forall \ \langle \mathbf{x},y \rangle \in \mathcal{D}$  :
  - o return Tree
- else:
  - Pick best feature  $x_i$ :
    - $\mathcal{D}_0$  at Child $_0: x_i = 0 \; \forall \; \langle \mathbf{x}, y \rangle \in \mathcal{D}$
    - $\mathcal{D}_1$  at Child $_1: x_i = 1 \ \forall \ \langle \mathbf{x}, y \rangle \in \mathcal{D}$

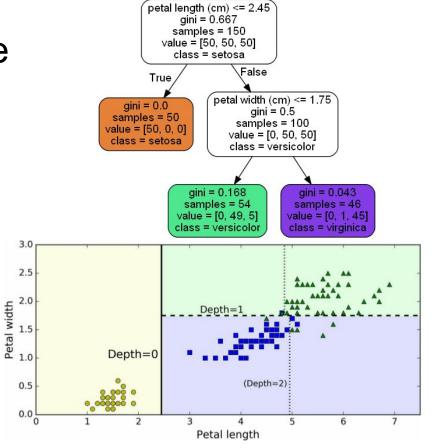


Figure 6-2. Decision Tree decision boundaries

return Node $(x_j, \text{GenerateTree}(\mathcal{D}_0), \text{GenerateTree}(\mathcal{D}_1))$ 

### Time complexity decision tree

Growing the tree (fit()):  $O(m*n^2log n)$ 

- Assuming we have continuous features and perform binary splits, the runtime of the decision tree construction is
- Sorting the values of continuous features helps with determining a decision threshold. If we have n examples, the sorting has time complexity O(n log n)
- If we have to compare sort m features, this becomes O(m\*n log n)
- Sorting step up to n/2 times O(m\*n²log n)

Querying the tree (**predict()**): O(log n)

depth of log<sub>2</sub>n

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