1 Expressions

1.1 Expressions

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\begin{split} e &\coloneqq x \quad (\mathbf{variable}) \\ &\parallel \lambda \quad (\mathbf{literal}) \\ &\parallel [e_1, ..., e_n] \\ &\parallel \{k_1 : e_1 \; ; \; ... \; ; \; k_n : e_n\} \\ &\parallel (x_1, ..., x_n) \rightarrow e \\ &\parallel e_1[e_2] \\ &\parallel f(e_1, ..., e_n) \\ &\parallel \text{ if } e \text{ elif } f_1... \text{ elif } f_n \text{ else } g \text{ end} \\ &\parallel \text{ match } e \; ; \; p_1 \Rightarrow e_1 \; ; \; ... \; ; \; p_n \Rightarrow e_n \text{ end} \\ &\parallel (e : \tau) \\ &\parallel e \text{ as } \tau \end{split}
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2 Typing

2.1 Types

$$\begin{split} \tau &\coloneqq T \quad \text{(type variable)} \\ &\parallel \lambda \quad \text{(literal)} \\ &\parallel int \parallel number \parallel string \parallel bool \parallel null \parallel void \\ &\parallel [\tau_1, ..., \tau_n] \parallel \tau[] \\ &\parallel \{k_1 : \tau_1 \ ; \ ... \ ; \ k_n : \tau_n\} \\ &\parallel \tau_1 \mid \tau_2 \\ &\parallel (\tau_1, ..., \tau_n) \to \sigma \\ &\parallel any \parallel some \end{split}$$

2.2 Type Equivalence

$$(au_0 \mid au_1) \mid au_2 \overset{c}{\sim} au_0 \mid (au_1 \mid au_2)$$
 $au_0 \mid au_1 \overset{c}{\sim} au_1 \mid au_0$
 $au \mid au \overset{c}{\sim} au$
 $any \mid au \overset{c}{\sim} au$
 $any \mid au \overset{c}{\sim} au$
 $any \mid au \overset{c}{\sim} au$

2.3 Subtype Relation

2.4 Expression Typing

$$\overline{\Gamma,x:\tau\vdash x:\tau}$$

$$\overline{\Gamma\vdash \lambda:\operatorname{typeof}(\lambda)}$$

$$\frac{\Gamma\vdash e_1:\tau_1 \quad \dots \quad \Gamma\vdash e_n:\tau_n}{\Gamma\vdash [e_1,\dots,e_n]:[\tau_1,\dots,\tau_n]}$$

$$\frac{\Gamma\vdash e_1:\tau_1 \quad \dots \quad \Gamma\vdash e_n:\tau_n}{\Gamma\vdash \{k_1:e_1:\dots : k_n:e_n\}:\{k_1:\tau_1:\dots : k_n:\tau_n\}}$$

$$\frac{\Gamma\vdash \{k_1:e_1:\dots : k_n:e_n\}:\{k_1:\tau_1:\dots : k_n:\tau_n\}}{\Gamma\vdash \{k_1:\tau_1,\dots,x_n:\tau_n\vdash e:\rho}$$

$$\overline{\Gamma\vdash \{k_1:\tau_1,\dots,x_n:\tau_n\}} \quad \Gamma\vdash e_2:\rho$$

$$\frac{\Gamma\vdash e_1:[\tau_1,\dots,\tau_n] \quad \Gamma\vdash e_2:i}{\Gamma\vdash e_1[e_2]:\tau_i}$$

$$\frac{\Gamma\vdash e_1:[\tau_1,\dots,\tau_n] \quad \Gamma\vdash e_2:\sigma \quad \sigma\preceq int}{\Gamma\vdash e_1[e_2]:\tau_1\mid\dots\mid\tau_n}$$

$$\frac{\Gamma\vdash e_1:any}{\Gamma\vdash e_1[e_2]:any}$$

$$\underline{\Gamma\vdash f:(\sigma_1,\dots,\sigma_n)\to\rho \quad \Gamma\vdash e_1:\tau_1 \quad \dots \quad \Gamma\vdash e_n:\tau_n \quad \tau_1\preceq\sigma_1 \quad \dots \quad \tau_n\preceq\sigma_n}}{\Gamma\vdash f(e_1,\dots,e_n):\rho}$$

$$\underline{\Gamma\vdash e:bool \quad \Gamma\vdash f_1:\tau_1 \quad \dots \quad \Gamma\vdash f_n:\tau_n \quad \Gamma\vdash g:\tau'}{\Gamma\vdash if e \text{ elif }f_1\dots \text{ elif }f_n \text{ else }g \text{ end }:\tau_1\mid\dots\mid\tau_n\mid\tau'}}$$

$$\underline{\Gamma\vdash e:bool \quad \Gamma\vdash f_1:\tau_1 \quad \dots \quad \Gamma\vdash f_n:\tau_n}}{\Gamma\vdash e:bool \quad \Gamma\vdash f_1:\tau_1 \quad \dots \quad \Gamma\vdash f_n:\tau_n}$$

$$\underline{\Gamma\vdash e:bool \quad \Gamma\vdash f_1:\tau_1 \quad \dots \quad \Gamma\vdash f_n:\tau_n}}{\Gamma\vdash e:bool \quad \Gamma\vdash f_1:\tau_1 \quad \dots \quad \Gamma\vdash f_n:\tau_n}$$

$$\underline{\Gamma\vdash e:\tau \quad \Gamma\vdash \tau\preceq\sigma}}{\Gamma\vdash e:\sigma:\sigma:\tau}$$

$$\underline{\Gamma\vdash e:\tau \quad \Gamma\vdash \tau\preceq\sigma}}{\Gamma\vdash (e:\sigma):\sigma}$$