

# Agent for Bazar Blot

G. Hovhannisyan A. Abrahamyan  
M. Khachatryan, M. Davtyan

December 3, 2024

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Table of contents

## Introduction

## Cheating Mini-Max

Expectimax

Mini-Max

## Simulation Results

## Numerical Methods for Solving the SIR

Euler's Method

Backward Euler's Method

## Simulation Results on Real-World Data

Active Cases

Simulations on USA's COVID-19 Data

Simulations on Armenia's COVID-19 Data

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

## Introduction

### Introduction

#### Cheating Mini-Max

Expectimax

Mini-Max

#### Simulation Results

#### Numerical Methods for Solving the SIR

Euler's Method

Backward Euler's Method

#### Simulation Results on Real-World Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Introduction

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

- ▶ The Origin of the Game
- ▶ General Rules

- ▶ Bidding
- ▶ Playing

Card	Trump	Regular	No-Trumps
A	11	11	19
K	4	4	4
Q	3	3	3
J	20	2	2
10	10	10	10
9	14	0	0
8	0	0	0
7	0	0	0

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Introduction

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

## Introduction

### Cheating Mini-Max

Expectimax

Mini-Max

### Simulation Results

#### Numerical Methods for Solving the SIR

Euler's Method

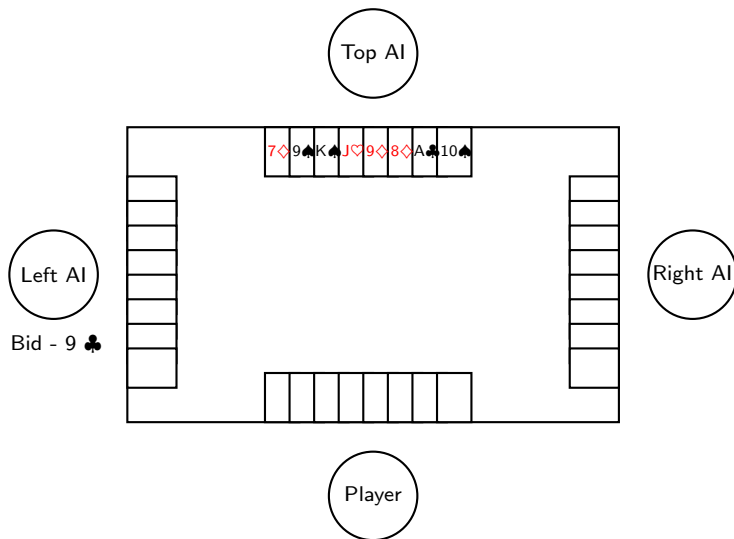
Backward Euler's Method

### Simulation Results on Real-World Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



Bid - 9 ♣

First Player, Bid - 8 ♠

# Cheating Mini-Max

## Cheating Mini-Max

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

**Cheating Mini-Max**

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

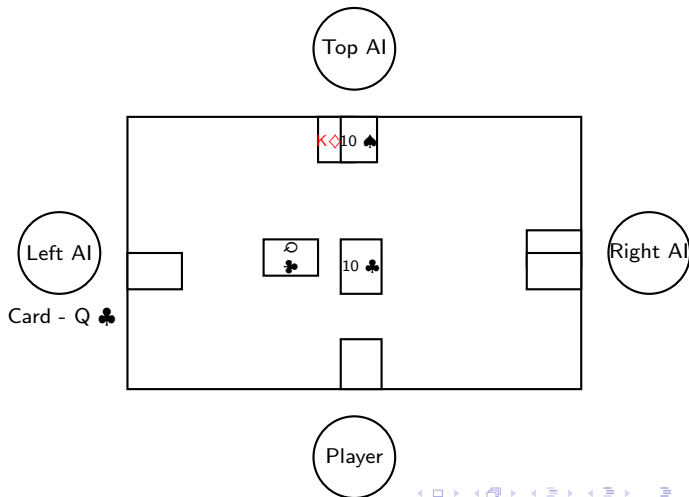
Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Expectimax

Without resorting to cheating we will have  $\binom{24}{8}$  nodes in our first depth!

Figure: Example of a Game



Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

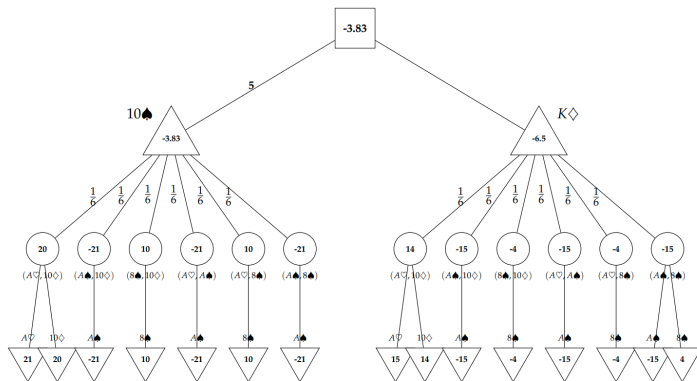
Simulations on Armenia's  
COVID-19 Data

# Expectimax

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Figure: Example of Expectimax tree



Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



# Mini-Max

- ▶ Assuming we know everyone's cards what's the approximate number of terminal states?

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Mini-Max

- ▶ Assuming we know everyone's cards what's the approximate number of terminal states?
- ▶  $(8!)^4$
- ▶ We can't use normal Mini-Max either even with alpha-beta pruning.

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Depth-Limited Cheating Mini-Max

- ▶ Depth is limited to 12.
- ▶ Uses alpha-beta pruning.
- ▶ Heuristic is the current score / 10.
- ▶ It plays slightly worse than a random bot.

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

## Simulation Results

# Minimax vs Random Without Auction (Three hand version)

Agent for Bazar Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

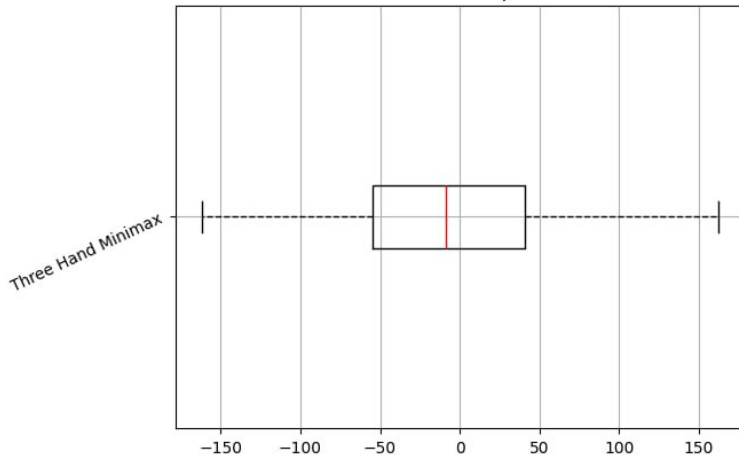
Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

MiniMax Boxplot



# Minimax vs Random Without Auction (One hand version)

Agent for Bazar Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

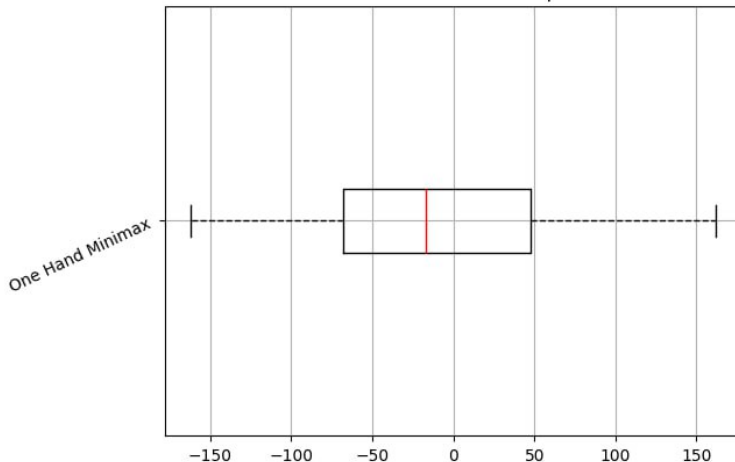
Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

One Hand MiniMax Boxplot



# Random vs Random Without Auction (Control)

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

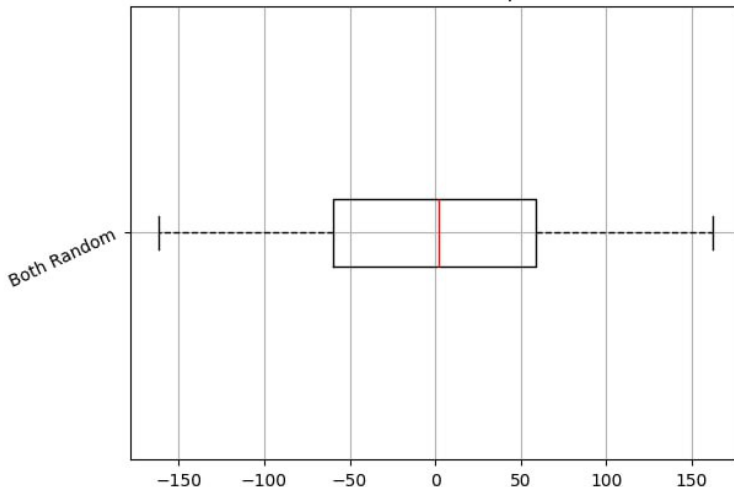
Simulation Results  
on Real-World  
Data

Active Cases

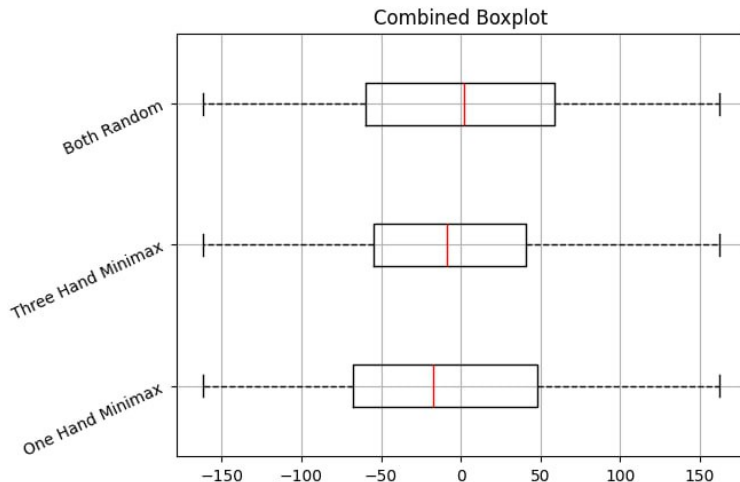
Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

Both Random Boxplot



# Combined Plot of the Three Versions



Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



# Game Results With Auction (Control)

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

## Introduction

### Cheating Mini-Max

Expectimax

Mini-Max

## Simulation Results

### Numerical Methods for Solving the SIR

Euler's Method

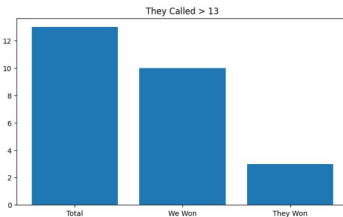
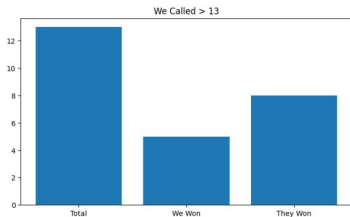
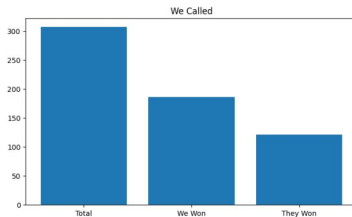
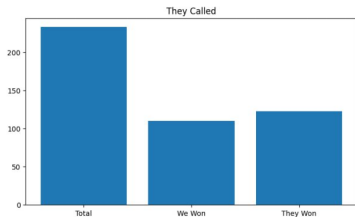
Backward Euler's Method

## Simulation Results on Real-World Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



# Game Results With Auction (V1 vs V2)

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

## Introduction

### Cheating Mini-Max

Expectimax

Mini-Max

## Simulation Results

### Numerical Methods for Solving the SIR

Euler's Method

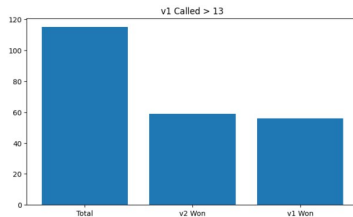
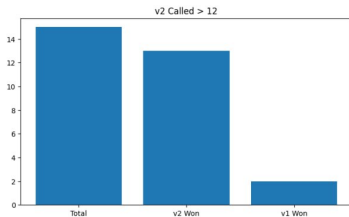
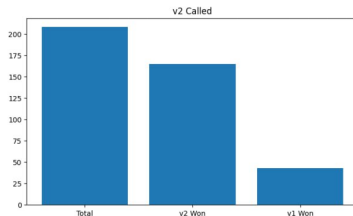
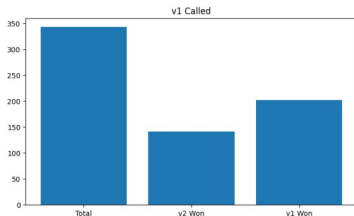
Backward Euler's Method

## Simulation Results on Real-World Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



# Numerical Solutions

- ▶ Euler's Method
- ▶ Backward Euler's Method

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Euler's Method

By using the extension  $y'(x) \approx \frac{y_{k+1}-y_k}{h}$  and having the  $y_0$ , we can iteratively predict the  $y_{k+1} = y(x+h)$ , by using the system

$$\begin{cases} y_{k+1} = y_k + h \cdot f(x_k, y_k) \\ y(x_0) = y_0 \end{cases}$$

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Euler's Method

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

**Euler's Method**

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Euler's Method

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

In case of SIR, we are solving 3 ODE's, hence we are solving a system for  $s_{k+1}$ ,  $i_{k+1}$ , and  $r_{k+1}$ , given the  $s_0, i_0, r_0$

$$\begin{cases} s_{k+1} = s_k - \beta \cdot h \cdot s_k \cdot i_k \\ i_{k+1} = i_k + (\beta \cdot s_k \cdot i_k - \gamma \cdot i_k) \cdot h \\ r_{k+1} = r_k + \gamma \cdot h \cdot i_k \end{cases}$$

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Backward Euler's Method

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

This time, the Method uses a different approach, namely

$$y'(x) \approx \frac{y_k - y_{k+1}}{h}$$

Plugging the SIR ODE's, we will get the system

$$\begin{cases} s_{t+1} = s_t - h \cdot \beta s_{t+1} i_{t+1} \\ i_{t+1} = i_t + h \cdot (\beta s_{t+1} i_{t+1} - \gamma i_{t+1}) \\ r_{t+1} = r_t + h \cdot \gamma i_{t+1} \end{cases}$$

By solving each one of these SLE's, we will get the next approximations for  $s_k, i_k, r_k$

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Backward Euler's Method

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

**Backward Euler's Method**

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data



## Simulations on USA's COVID-19 Data

### Introduction

### Cheating Mini-Max

Expectimax

Mini-Max

### Simulation Results

### Numerical Methods for Solving the SIR

Euler's Method

Backward Euler's Method

### Simulation Results on Real-World Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Active Cases

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

**Active Cases**

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

# Simulations on USA's COVID-19 Data

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

**Simulations on USA's  
COVID-19 Data**

Simulations on Armenia's  
COVID-19 Data

# Simulations on Armenia's COVID-19 Data

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data

Thank You For Attention!  
More Information is available at Our  
Github Repository

Agent for Bazar  
Blot

G. Hovhannisyan  
A. Abrahamyan  
M. Khachatryan,  
M. Davtyan

Introduction

Cheating Mini-Max

Expectimax

Mini-Max

Simulation Results

Numerical  
Methods for  
Solving the SIR

Euler's Method

Backward Euler's Method

Simulation Results  
on Real-World  
Data

Active Cases

Simulations on USA's  
COVID-19 Data

Simulations on Armenia's  
COVID-19 Data