

### **ESQUEMAS NÚMERICOS AM1:**

- **RUNGE-KUTTA 2.**

$$\begin{aligned}k_1 &= F(x_i, t_i) \\k_2 &= F(x_i + \delta t \cdot k_1, t_i + \delta t) \\x_{i+1} &= x_i + \frac{\delta t}{2}(k_1 + k_2)\end{aligned}$$

- **RUNGE-KUTTA3.**

$$\begin{aligned}k_1 &= F(x_i, t_i) \\k_2 &= F(x_i + \frac{\delta t}{3}k_1, t_i + \frac{\delta t}{3}) \\k_3 &= F(x_i + \frac{2\delta t}{3}k_2, t_i + \frac{2\delta t}{3}) \\x_{i+1} &= x_i + \frac{\delta t}{4}(k_1 + 3k_3)\end{aligned}$$

- **RUNGE-KUTTA 4.**

$$\begin{aligned}k_1 &= F(x_i, t_i) \\k_2 &= F(x_i + \frac{\delta t}{2}k_1, t_i + \frac{\delta t}{2}) \\k_3 &= F(x_i + \frac{\delta t}{2}k_2, t_i + \frac{\delta t}{2}) \\k_4 &= F(x_i + \delta t \cdot k_3, t_i + \delta t) \\x_{i+1} &= x_i + \frac{\delta t}{6}(k_1 + 2k_2 + 2k_3 + k_4)\end{aligned}$$