# Proximity-informed robot control through whole-body artificial skin

by

# A. Aranburu Fernndez

B.A., UPV/EHU Euskal Herriko Unibertsitatea, 2017M.S., UPC Universitat Politecnica de Catalunya, 2020

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Aranburu Fernndez, A. (M.S., Industrial Engineering)

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Human-Robot Interaction is the field of robotics dedicated to the understanding, design, and evaluation of robotic systems for use by or with humans. Safety is one of the most important aspects this field will have to deal with in the years to come. In this work, pre-contact safety is adressed through the use of an artificial skin developed in our lab that integrates proximity sensing. Proximity sensor readings are transformed into 3D data, which will later inform the control algorithms. Two different avoidance controls have been implemented: "A Depth Space Approach to Human-Robot Collision Avoidance" [1] and "Collision Avoidance with Proximity Servoing for Redundant Serial Robot Manipulators" [2]. The implementations of these two controllers form, with the addition of a third controller that improves upon both of them, a framework for the comparison and improvement of the current state of art in safe robot controllers.

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#### Chapter 1

# Introduction

#### 1.1 Human-Robot Interaction

We are on the threshold of a new era in robotic technology that will bring breaking improvements into our lives. Simple household robots, such as the vacuuming robot Roomba<sup>®</sup> [3] or the kitchen robot thermomix<sup>®</sup> [4], are starting to do some of human's the most time consuming tasks. But this is just the beginning and robots will soon be more extended in our daily lives. This robotic revolution we are talking about has the potential to surpass the ubiquity and usefulness of the computer revolution, if only because robots can change not only our virtual world, but the physical world also.

Human-robot interaction (HRI) is a field of study dedicated to understanding, designing, and evaluating robotic systems for use by or with humans. It is one of the main fields of research working towards the revolution presented in the first paragraph and it is focused on expanding robot's abilities to interact with the physical world, integrating robots in human-populated environments. There are a number of ways in which robotics can be impactful to society in the short- mid- term. Some examples:

Hospital robots will check on patients and report their status to nurses, saving time and improving patient outcomes. One current example is the Moxi<sup>®</sup> hospital assistant robot
[5]. It can already accomplish tasks such us gathering supplies and bringing them to patient rooms and delivering lab samples.

- Childcare robots will help parents with chores such as assisting at diaper changing or feeding, so that families can spend high-quality time together. iPAL<sup>®</sup> [6] is a sneak peak of what is to come.
- Manufacturing robots will collaborate with people to assemble complex objects on reconfigurable assembly lines, increasing the efficiency and flexibility of factory floors.

Nowadays robots in the industry live in restricted access areas and interaction with humans is avoided. The transition of robots from these restricted access areas to human-populated environments comes with a number of problems that need to be overcome. One of the key issues is that human safety is compromised. Traditionally, safety in industrial robots has been achieved isolating the robotic platforms in a cell with safety interlocks to prevent direct interaction. HRI contributions will only be feasible once the coexistence of robots and humans does not come with serious injury risk.

### 1.2 Human senses and sensors in robotics

In order to achieve the safe requirements of HRI, robots are expected to adapt to the changes in their environment the way humans do. This is why it is important to study how humans interact with their environment.

Interaction between a human being and its environment is accomplished through its senses. One important aspect research in robotics has focused on has been to look for ways to emulate and exploit these human senses. For example, visual sensing has been widely explored in this field. One of the reasons is the development of new low-cost depth sensors such as the Microsoft Kinect TM that meet the requirements of computer vision application at an affordable price. These depth sensors are capable of acquiring 2D images as well as the distances of the objects that each of the cameras pixels views. The usual way visual data is used is to reassemble representations of obstacles in a robot-oriented space.

However, other human senses are of great importance for the acquisition of data relevant

to the interaction with their surroundings. Touch is one of them. Tactile sensing is the most fundamental sense when interacting with the external world and it is the biggest and oldest of the sensorial organs. An experiment that consisted of exploring objects after anesthetizing the hands of a control group demonstrated that the simple task of maintaining a stable grasp of objects becomes surprisingly difficult when sense of touch is suppressed. Their hand movements were inaccurate and unstable [7]. In another experiment carried out by astronauts at the International Space Station, sense of touch was proven to be an important indicator of direction and spatial disorientation [8]. Sense of touch is crucial when experiencing object properties, such as size, shape, texture, and temperature. It informs about slip. It is essential to develop awareness of the body and in consequence, to differentiate ones body from the rest of ones surroundings. The absence of touch seriously hinders the interaction of an individual with its environment [9].

Nonetheless, tactile sensing in robotics has not been able to achieve the impact this evidence suggests it should have had. In traditional industrial robots, tactile sensing has been ignored. Engineers have been able to avoid the issue of developing a artificial sensor that emulates touch by using prior knowledge about the object to be manipulated and the environment. The limitations of this approach are obvious: robots are only capable of working in structured and controlled environments.

The result is that research and technology in artificial tactile sensors is not as well developed as other perception modalities. Tactile sensors in robotic applications are represented by:

- Pressure sensing arrays. A pressure sensor matrix that provides information about the location and amount of pressure exerted on a surface.
- Force-torque sensors. Gives feedback about the forces and torques that are applied on a given point in the 3 geometric axes.
- Optical sensors placed under a flexible gel substrate. See chapter 2 for more information on these.

# 1.3 Whole-body artificial skins

Current research is focused on developing tactile skins that cover robot end effectors and hands with a number of tactile sensors, in parallel with devising new algorithms that make use of these new sensors for dexterous object manipulation ([10], [11]).

Even though we know about the importance of human skin covering all the body, whole-body artificial skins have not gained the same attention as end effector coverings. In fact, these types of skins can be of great importance in the transition of robots to operating alongside humans and the new safety issues that arise with it.

Traditional robots have been designed for precision and performance at expenses of safety and the ability to adapt to the surroundings. The two paradigms that try to find a solution to this issue, different but not mutually exclusive, are: **passive** and **active compliance**. Passive compliance aims to achieve safety through physical adaptation to the environment. There are two different strategies to accomplish that. On the one hand, there is the use of flexible parts and mechanisms. On the other hand, limitation of the performance capabilities of the robot, such us speed, can also be enough to achieve safety. Active compliance, in contrast, relies on algorithms and control laws for reactive interaction with the environment.

Both approaches have some important limitations, though. Passive compliance achieves safety at the cost of reducing accuracy, in the case of using flexible parts, and agility when the capabilities of the robot are reduced. As far as active compliance is concerned, sensors that are used are far from being perfect for the control. Some sensors provide either a high amount of low-quality information regarding the task, as in the case of the aforementioned depth cameras or a limited amount of relevant data, as force-torque sensors located at the robots joints. In addition, both solutions are currently lacking in flexibility. New problems require completely new designs. These are important enough reasons that explain why none of the solutions have become the established standard in robotics.

Whole-body artificial skins have the potential to solve all the issues present in active and

passive compliance. It does so providing high-density relevant information, information that is much more relevant to the task of collision avoidance. At the same time, it can also be designed to be mechanically compliant to the environment.

In addition, the skin can be equipped with heterogeneous sensing so that a greater amount of high-quality information is collected. Tactile data is only useful when contact has been established between the robot and the environment. However, collisions can be actively avoided before establishing undesired contact by choosing suitable pre-impact strategies. That is why proximity sensing opens up new possibilities for the task of collision avoidance. The addition of proximity sensors allows a compact, external motion capture free system, with highly informative prior-to-contact data. This combined with lighter data, makes proximity sensing the perfect sensing system for the solution of the collision avoidance problem.

#### 1.4 Control and collision avoidance

From the control perspective, using proximity data for the safe movement of a robot might prevent performing the task commanded to a robot, that is, the original trajectory when there were no impediments that prevented the desired movement commanded to perform a certain task. When any undesired object obstructed the desired trajectory of a robot, it is not difficult to see that the performance of that main task could be hindered. Nonetheless, this does not have to be the case for a certain type of robots called redundant robots.

A robot is task redundant if the number of degrees of freedom (DoF) n it has is greater than the degrees of freedom needed for the task m. For example, if the specifications of a given task only require positioning the end-effector of a robot at a certain point, i.e. m=3 a robot with n=3 DoF would be able to accomplish the task and one with n=4 DoF would be task redundant. A redundant robot has the advantage of being able to accomplish the task in infinitely many possible ways.

The ability to perform a certain movement of the end effector in infinitely many different ways means that safe motion control does not imply stopping the main task and in fact, the main task should only halt when there is no way to make use of redundancy to avoid a collision while completing it.

# 1.5 Objectives and scope

- Review the literature of avoidance controllers. Implement the most relevant ones and integrate them with proximity data.
- Actively communicate with the other teams in the lab. Inform the design of the skin and receive input from the results of calibration to ensure the feasibility of the project.
- Start building a new improved controller upon those previously implemented.
- Qualitatively test the control algorithms in simulation.
- Check the algorithms on the real robot platform as far as possible.

#### Chapter 2

#### Related Work

In this section, we describe the main research areas related to this work and place it in context. We have organized the content in two sections. Section 2.1 contains the previous publications made in the field of whole body artificial skins. Section 2.2 describes the work previously done in collision avoiding robot control.

### 2.1 Whole-body articial skins

One of the first whole-body artificial skin technologies was the iCub skin ([12], [13]). It made use of an array of capacitive touch sensors for tactile sensing. The arrays were covered by a flexible soft material and later placed on the robotic arms.

A different approach to tactile sensing was made by HEX-o-SKIN ([14]) and CellulARSKIN ([15], [16]). Their skins offer not only pressure sensors, but accelerometers, temperature and proximity sensors too. In spite of these new capabilities, their potential sensor density, that is, their amount of sensors per unit area, was lower. This was due to the fact that the modules were big and difficult to place on high curvature areas.

Another technology that has been utilized for tactile sensing has been the approach followed by Gelsight ([17]), Fingervision ([18]), SoftBubble ([19]). These implementations use optical sensors that are placed under a flexible gel substrate. The benefits of this technology is that the density is very high. However, the limitations come in form of limited scalability for whole-body sensing. The computational power required to process images is enormous. In fact, it is a good technology

for end effector tactile sensing and it has been used for dexterous manipulation applications.

In [20], they present a set of cuffs that can be placed around a robots arms. The cuffs contain proximity and capacitive sensors. Tactile sensing is not covered by this approach. Even their control methods have been inspiring in this project (see 2.2), we believe that their density is not high enough for the pre-contact collision avoidance task. The rigidity of the cuffs also make them fragile and not compliant.

In the HIRO lab, we are building our own skin upon the characteristics of the different approaches cited until now. From the iCub skin, we focus on its flexibility and high density of sensors. From HEX-o-SKIN and CellulARSKIN we focus on the the heterogeneity of different sensor technologies. In fact, we are adding a human sensor that indicates if the proximity sensor reading comes from a human or not. We are also looking for an approach of individual skin units instead of one large skin patch. This makes the system more modular.

### 2.2 Avoidance control

Collision avoidance can be done at different layers: motion planning and control. Control methods allow robots to reactively respond to sudden changes in the environment.

Most of the collision avoidance control methods are based on a potential fields approach. Artificial repulsive forces associated to obstacles are exerted on the robot. These modify the robot's trajectory in order to avoid obstacles. [1] implements one of this method and it has been implemented as a method for comparison in this work. See section 3.3.2 for an in depth explanation of the paper.

The formulation of the avoidance control in terms of mathematical optimization has allowed for the introduction of complex behaviours. [21] suggests a method that prioritizes the avoidance of parts of the human body that are more susceptible of serious damage, such as the head. In [2] they make use of proximity data to solve the problem. The formulation of the problem via mathematical optimization introduces a new way of forcing repulsive actions, through the addition of restrictions. This last work will be implemented in this work and it is explained in section 3.3.3.

The final controller we proposed is based on their publication.

#### Chapter 3

## Technical Approach

In this chapter, we will explain the technical means by which the objective of this thesis has been approached. Firstly, in section 3.1 we start talking about the basic elements that have been used during the development this work, such us the robot platform employed and software libraries. In order to make the robot avoid obstacles with proximity data, obstacles need to be located with respect to the robots kinematic chain. That's why, in section 3.2 we present a method to sense the environment through proximity sensing. Lastly, in section 3.3 the methods for collision avoidance are explained.

#### 3.1 Required resources

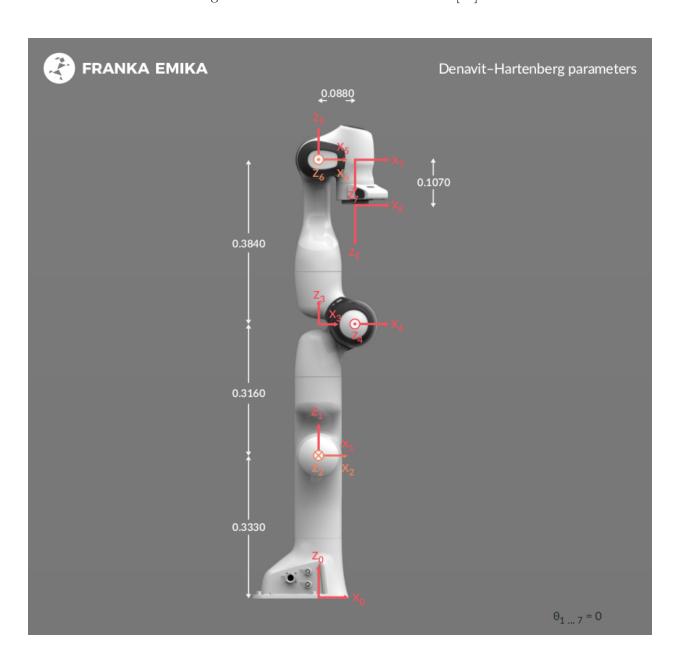
In this section we present the various tools that have employed throughout the process. We start presenting the robotic platform employed for carrying on the experiments. Then we define what robotic middleware is, why it is useful and we present the specific robotic middleware that has been employed: ROS. We finish this section by presenting the several software libraries that have been useful in the implementation of the concepts and ideas that will be elaborated on in the sections that follow.

#### 3.1.1 Robot platform

The robot utilized for the development of the ideas presented in this work has been the Panda, manufactured by the company Franka Emika based in Munich, Germany. It is well known for its performance and usability as well as for its affordability, starting at \$10,000.

The Franka Emika Panda (FEP) is equipped with 7 revolute joints, i.e. it has 7 degrees of freedom (DOF). Each of the revolute joints mounts a torque sensor. The total weight of FEP is around 18 kg. It can handle payloads of up to 3 kg.

Figure 3.1: FEP: Joints and dimensions [22].



It has a control interface that provides access to joint positions  $\mathbf{q}$  and velocities  $\dot{\mathbf{q}}$  and link side torques vector  $\tau$ , with a refresh rate of 1 kHz. The control interface also provides numerical values of the inertia matrix  $\bar{\mathbf{M}}(\mathbf{q})$ , the gravity vector  $\bar{\mathbf{g}}(\mathbf{q})$ , the end effector Jacobian matrix  $\bar{\mathbf{J}}(\mathbf{q})$  and the Coriolis term  $\bar{\mathbf{c}}(\mathbf{q}, \dot{\mathbf{q}})$ .

There are 3 control modes available. At the lowest level, there is the torque-mode  $\tau_{\mathbf{d}}$ . The joint velocity  $\dot{\mathbf{q}}_{\mathbf{d}}$  and joint position  $\mathbf{q}_{\mathbf{d}}$  modes provide a higher level control and are the ones that are going to be used throughout this work.

The Denavit Hartenberg (DH) parameters provided by the manufacturer [22] and depicted in figure 3.1 are shown in table 3.1.

Table 3.1: Denavit Hartenberg parameters [22]

Joint	<b>a</b> (m)	<b>d</b> (m)	$\alpha$ (rad)	$\boldsymbol{\theta}$ (rad)
1	0	0.333	0	$\theta_1$
2	0	0	$-\frac{\pi}{2}$	$\theta_2$
3	0	0.316	$\frac{\pi}{2}$	$\theta_3$
4	0.0825	0	$\frac{\pi}{2}$	$\theta_4$
5	-0.0825	0.384	$-\frac{\pi}{2}$	$\theta_5$
6	0	0	$\frac{\pi}{2}$	$\theta_6$
7	0.088	0	$\frac{\pi}{2}$	$\theta_7$
F	0	0.107	0	0

The manufacturer also provides the physical limits of the robot, both in the joint and the cartesian spaces (tables 3.2 and 3.3 respectively).

Table 3.2: Joint space limits [22]

	Joint 1	Joint 2	Joint 3	Joi1nt 4	Joint 5	Joint 6	Joint 7	
$\mathbf{q}_{\mathbf{max}}$	+2.8973	+1.7628	+2.8973	-0.0698	+2.8973	+3.7525	+2.8973	rad
$\mathbf{q_{min}}$	-2.8973	-1.7628	-2.8973	-3.0718	-2.8973	-0.0175	-2.8973	rad
$\dot{\mathbf{q}}_{\mathbf{max}}$	2.1750	2.1750	2.1750	2.1750	2.6100	2.6100	2.6100	$\frac{\text{rad}}{\text{s}}$
$\ddot{\mathbf{q}}_{ ext{max}}$	15	7.5	10	12.5	15	20	20	$\frac{\text{rad}}{\text{s}^2}$

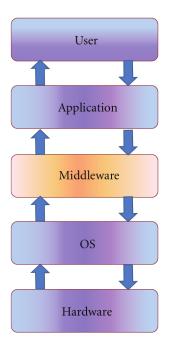
Table 3.3: Cartesian space limits [22]

	Translation	Rotation	Elbow
$\dot{\mathbf{p}}_{ ext{max}}$	$1.7000 \frac{m}{s}$	$2.5000 \frac{\text{rad}}{\text{s}}$	$2.1750 \frac{rad}{s}$
$\ddot{\mathbf{p}}_{ ext{max}}$	$13.0000 \frac{\text{m}}{\text{s}^2}$	$25.0000 \frac{\text{rad}}{\text{s}^2}$	$10.0000  \frac{rad}{s^2}$

### 3.1.2 ROS

The Robot Operating System (ROS) is an open source robot middleware, robot framework or robot development environment (RDE), one of many available in the market. Robot middleware [23] is an abstraction layer that resides between the operating system (OS) and software applications (figure 3.2). Its purpose is to provide a framework and take care of several important parts of applications development, so that the developer needs only to build the logic or algorithm as a component.

Figure 3.2: Robotic middleware [23]



The main goal of ROS in particular is to provide a framework for easy code reuse in research.

This is why ROS is mostly used in an academic context. It also provides APIs for Python and C++ and code written in both languages can be used interchangeably and at the same time.

ROSs main concept is its runtime graph: a peer-to-peer network of loosely coupled components or nodes that use the ROS communication infrastructure. ROS implements two main communication types:

- Topics. A publisher node publishes a message to a topic. Another node subscribes to this topic, meaning that every time there is a new message published in the topic this subscriber node will receive it and therefore will we able to utilize and manipulate the data. Several nodes can publish to a given topic, and subscribe to topics of the same name.
- Services. Sometimes the asynchronous model topics provided are not suitable for an application. When synchronous behavior is desired services are the way to go. Services have two sides: client and service. From the client side calling a service is equivalent to

calling a function. However, this function is managed in a different node: the server side.

In figure 3.3 the runtime graph of this work is presented as an example. The real robot is replaced by a simulation. The /gazebo node is calculating the physics of the real robot, as well as sensor readings. /CartesianPositionController is subscribed to the topic /joint\_states, as it needs this information for control purposes. Sensor data is processed in the /proximity\_listener node and then is published to the topic /live\_points. This topic has two subscribers in this example. On the one hand, /proximity\_visualizer uses the data published in /live\_points to visualize the sensor data in rviz (the 3D visualization tool provided by ROS to visualize several types of visual data). On the other hand, /CartesianPositionController uses the data for collision avoidance control, as explained later in this chapter (section 3.3).

/robot\_state\_publisher is an example of the benefits of the framework ROS provides for easy code reuse. This node is part of a widely used ROS package that uses the robots description (described in a .urdf file) and messages published in /joint\_states to provide transformation matrices between any two joints in the robots kinematic chain. It publishes this data in /tf topics.

/controller\_spawner

//gazebo\_gui

//gazebo\_gui

//proximity\_visualizer

//proximity\_data149

//controller\_spawner\_hand

//f\_static

//proximity\_listener

//proximity\_data149

//controller\_spawner\_hand

//f\_static

//controller\_spawn

//controller\_spawn

//controller\_spawn

//controller\_spawn

//controller\_spawn

//controller\_spawn

Figure 3.3: ROS graph

In addition, bags in ROS enable real data storage coming from sensors on the robot. These allow developers to test their algorithms with real data without having to collect new data every time they need to run their code.

The ROS Master node enables nodes to find each other and to communicate. It also holds the parameter server, which provides a central storage location for data that is relevant for several nodes. It serves, broadly speaking, as a place where global variables can be stored and retrieved by nodes. Examples of variables that are stored in the parameter server are PID control parameters, the robots urdf description, and frequencies at which different components living in the graph work.

Last, it should be mentioned that despite the fact that ROS is widely used in the academic context, it lacks the reliability and robustness of safety-critical systems in industrial or commercial contexts require. Some industrial fields, such as the automotive and aerospace, have their own standards for development of safety-critical software. These standards need to be certified for every software component written in any of these fields. ROS was not developed to any of these standards and it depends on many libraries that were not developed to these standards. ROS 2, in contrast, is based on components that are safety-certified (DDL communication) that make ROS 2 certifiable. Indeed, Apex.AI is working on Apex.OS: an API compatible to ROS 2 that is being certified ISO 26262 for safe automotive applications [24].

#### 3.1.3 Simulation and Visualization

According to the Cambridge Dictionary, a simulation is a situation in which a particular set of conditions is created artificially in order to study or experience something that could exist in reality. Simulations are therefore very useful for research and especially for robotics, where the following issues are prevalent:

- Robotic hardware is usually **costy**.
- Prototyping can be **dangerous**, since bugs that appear when testing and debugging can lead to damage in the real world, as opposed to programs that only affect the virtual world.
- Development can be slow.

Robot simulation is an adequate solution to address each of these. This work has been prototyped in simulation. This has enabled parallel development of the artificial skin and its

electronics on the one side and the control design on the other. The simulation software package employed is *Gazebo*.

Gazebo [25] is a 3D robot simulator. It features dynamics simulation, advanced 3D graphics, indoor and outdoor environments and simulation of several sensors with noise that make the virtual readings realistic. It is a standalone software package, but offers integration with ROS through the gazebo\_ros\_pkgs ROS packages.

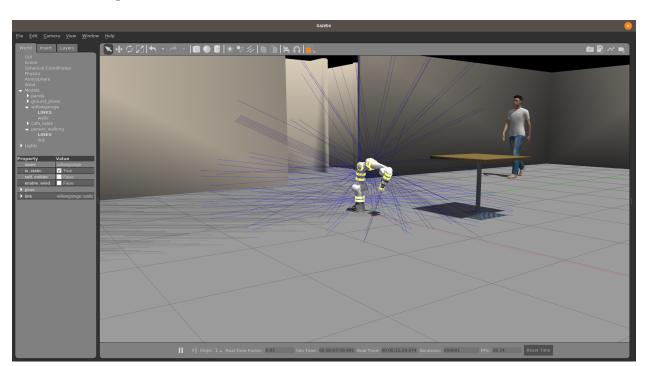


Figure 3.4: Franka Panda Emika in Gazebo's simulation environment.

On the other hand, ROS offers a useful vizualization tool called *rviz* [26], short for *ROS Visualization*. Several kinds of data can be visualized in *rviz*, which allow the user to see what the robot is seeing, thinking, and planning. These visualization capabilities make it an extremely useful tool for application debugging.

The difference between *Gazebo* and *rviz* is that even though both offer some kind of a graphics visualization, *Gazebo* is mainly focused on simulating the physics whereas *rviz* is mainly useful for visualizing any kind of information concerning the robot's state and its knowledge about the

environment. Note that rviz has the same role in both real and simulated environments.

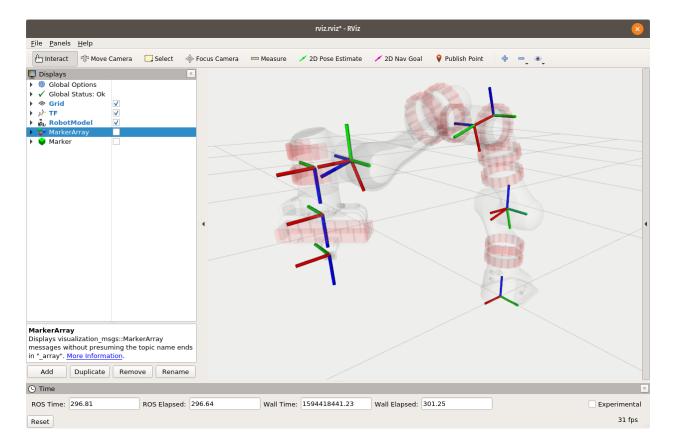


Figure 3.5: Joint frames in Franka Panda Emika as seen in rviz.

### 3.1.4 Mathematical Optimization and Quadratic Programming

Mathematical Optimization, also called Mathematical Programming, is the set of principal methods used to determine the best solutions to mathematically described problems.

Formally speaking, Mathematical Optimization is the process of formulation and solution of a optimization problem of the general mathematical form:

$$\underset{\text{w.r.t. } \mathbf{x}}{\text{minimize}} f(\mathbf{x}), \mathbf{x} = [x_1, x_2, \dots, x_n]^T \in \mathbb{R}^n$$

subject to the constraints:

$$g_j(\mathbf{x}) \le 0, \quad j = 1, 2, \dots, m$$

$$h_j(\mathbf{x}) = 0, \quad j = 1, 2, \dots, r$$

 $f(\mathbf{x})$ ,  $g_j(\mathbf{x})$  and  $h_j(\mathbf{x})$  are scalar functions of a vectorial variable  $\mathbf{x}$ . The components  $x_i$  of  $\mathbf{x}$  are called the variables of the optimization problem,  $f(\mathbf{x})$  is the objective function,  $g_j(\mathbf{x})$  are the inequality constraint functions and  $h_j(\mathbf{x})$  are the equality constraint functions. The optimum vector  $\mathbf{x}$  that solves the optimization problem is denoted with an asterisk  $\mathbf{x}^*$  and the corresponding optimal objective function value is  $f(\mathbf{x}^*)$ .

Optimization problems are usually solved using *optimization algorithms*. These optimization algorithms are tailored to particular types of optimization problems. This is why classification of optimization models is a crucial part in the optimization problem.

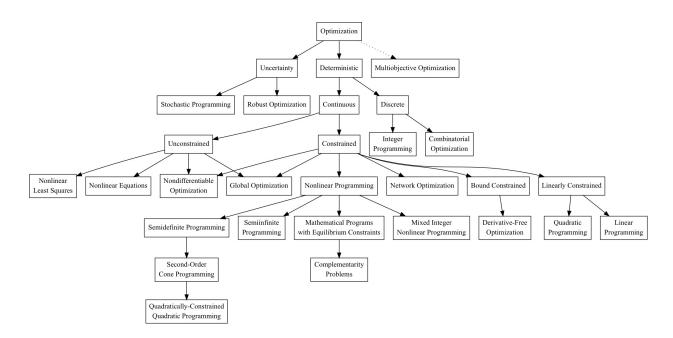
One important optimization problem type is the **Quadratic Programming** (QP) problem. It is an important class of problems on its own and also a subproblem for more general constrained optimization problems (sequential quadratic programming (SQP), augmented Lagrangian methods). These are the characteristics of QP problems:

- One objective function. The most common case is the problem being defined by a single objective function, but there are also problems that can be modeled with no objective functions or using many of them.
- **Deterministic optimization**. Depending on the nature of the data, an optimization problem can be either *deterministic* or *stochastic*. Due to measurement errors or more importantly because the data being used is data that represents the future, uncertainty has to be incorpored to the model. In this case we are talking about stochastic optimization. On the other hand, if data is assumed to be known with accuracy we are talking about deterministic optimization.
- Continuous optimization problem. For some problems, the variables of the optimization problem can only take values from a discrete set, often a subset of integers, whereas for

other problems they can take any value in  $\mathbb{R}$ . The former are called *discrete optimization* problems and the latter are called *continuous optimization problems*. Continuous optimization problems tend to be easier to solve because the continuity of the functions involved can be used to obtain information about the neighbourhood of the current value.

• Constrained optimization. Sometimes the problem does not require to specify constraints for the variables of the optimization. When this is the case we are talking about unconstrained optimization. If the problem requires a certain constraints to be fulfilled it is called constrained optimization.

Figure 3.6: Optimization models taxonomy, with an emphasis on deterministic optimization problems.



Moreover, a problem has to meet some more requirements so that it can be written as a QP problem:

• The objective function cannot be any function, it needs to be a quadratic function that can

be rewritten as follows:

$$f(\mathbf{x}) = \frac{1}{2}\mathbf{x}^T\mathbf{Q}\mathbf{x} + \mathbf{c}^T\mathbf{x}$$

where **Q** is a symmetric  $n \times n$  matrix and  $\mathbf{c} \in \mathbb{R}^{n \times 1}$ .

• The constraints must be described by a linear set of equations and inequations:

$$\mathbf{A}\mathbf{x} \leq \mathbf{0}, \quad \mathbf{A} \in \mathbb{R}^{m \times n}$$
  $\mathbf{A}_{eq}\mathbf{x} = \mathbf{0}, \quad \mathbf{A}_{eq} \in \mathbb{R}^{r \times n}$ 

• Depending on the characteristics of the matrix **Q** the problem can be easily solved using polynomial-time algorithms. This is only possible if **Q** is positive definite, that is, if all its eigenvalues are greater than or equal to 0. When **Q** is positive definite, the problem is a *convex QP problem*. In the contrary case, the problem is *non-convex* and only local minimums can be found.

So, the quadratic problem can be formulated as follows:

minimize 
$$\frac{1}{2}\mathbf{x}^T\mathbf{Q}\mathbf{x} + \mathbf{c}^T\mathbf{x}$$
  
subject to  $\mathbf{A}\mathbf{x} \leq \mathbf{0}$ ,  $\mathbf{A} \in \mathbb{R}^{m \times n}$  (3.1)  
 $\mathbf{A}_{eq}\mathbf{x} = \mathbf{0}$ ,  $\mathbf{A}_{eq} \in \mathbb{R}^{r \times n}$ 

#### 3.1.5 Software Libraries

In this section we describe the software libraries chosen to fulfill the needs that have arisen during the implementation of the perception and control parts of this work. C++ is the language in which all the final code is written, so the libraries mentioned in this section are C++ Libraries. Other languages (Python and Matlab) have also been employed in the code prototyping phase, but as their importance is less prevalent the software components employed in those languages will be mentioned in the specific parts they have been used, in section 3.3.

#### 3.1.5.1 Robot Kinematics

The Kinematics and Dynamics Library (KDL) [27] is a framework that provides the tools to describe robot kinematic chains and solutions to the most usual problems: forward and inverse kinematics, jacobian solvers, etc.

For that purpose, KDL implements classes that represent kinematic primitives such as vectors, rotations and frames as well as classes that represent the whole kinematic chain, built from segments defined by kinematic primitives. The classes that represent the whole kinematic chain are KDL::Chain and KDL::Tree, being KDL::Tree a container of KDL::Chains. Various generic forward and inverse kinematic algorithms that take inputs of these classes are provided also.

For more information on the elements mentioned in this section see section 3.3.1, where the fundamental elements for basic kinematic control are discussed.

#### 3.1.5.2 Linear Algebra

Eigen [28] is a template library for linear algebra, meaning that every component in the Eigen is a C++ template, that is, a component whose functionality can be adapted to more than one C++ type. In this case, Eigen supports all the C++ standard numeric types. It is the ecosystem of KDL (3.1.5.1).

It supports fixed and dynamicly sized matrices and vectors and all the basic operations and common matrix decompositions. It does all its operations in an efficient, optimized, elegant and reliable fashion.

#### 3.1.5.3 Mathematical Optimization

ALGLIB [29] is a numerical analysis and data processing library, which includes optimization algorithms among other tools. Its goal is to make high quality numerical code available to industry and academic worlds. The library is offered in a free version and in a commercial paid version, which is highly optimized. The free version, however offers access to the full library and has proved a good enough performance for this work.

# 3.2 Perception via proximity sensing

Proximity sensors embedded in artificial skin provide distance information about the surroundings of the robot. These readings are one dimensional distance readings, which means that the readings of isolated individual sensors are not very useful if our objetive is to obtain information about the 3D euclidean space in which the robot's operations take place.

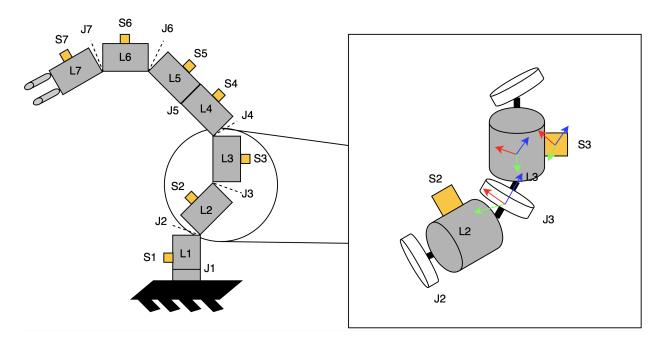
In this section we describe the method developed in this work to create a 3D point cloud from proximity distance data. The first step is the kinematic calibration of the skin units that contain the proximity sensors. Kinematic calibration makes an automatic estimation of the position and orientation of each sensor. The method is described in section 3.2.1. It is a conceptual and not detailed description, since it has been developed in a parallel project and is an essential part that makes the control methods employed in this work possible. Section 3.2.3 describes the point cloud creation algorithm. Finally, section 3.2.4 shows how the obtained data is visualized in *rviz*.

#### 3.2.1 Kinematic Calibration

This section describes a framework for automatic kinematic calibration that leverages an Inertial Measurement Unit (IMU) sensor to accurately estimate the position and orientation of a skin unit (SU) along the surface of a robot.

To automatically locate skin units along the surface of a robot, angular velocity and linear acceleration measurements from the IMUs are used. The position and orientation of an SU are estimated using a modified version of Denavit-Hartenberg (DH) parameters (see section 3.3.1.1), as illustrated in figure 3.7. The position and orientation of each SU with respect to the previous joint in the kinematic chain is estimated by six DH parameters: four parameters from the joint to a virtual joint, and two additional parameters from the virtual joint to the SU (the other two parameters are set to 0). This virtual joint is located within the link that is orthogonal to the joints z axis and the SUs z axis. This solution is necessary to adhere to the DH notation, so that each transformation can be expressed with no more than four parameters.

Figure 3.7: Depiction of multiple skin units (S) placed on the robots links (L) and separated by joints (J). We estimate the Denavit-Hartenberg parameters of each joint in order to calculate the pose of each skin unit along the surface of the robot.



The optimization algorithm is composed of the following **four steps**:

(1) Initialize a kinematic chain with randomized values. Each skin unit frame is represented using an homogeneous transformation matrix (see section 3.3.1.2).

$${}^{0}T_{SU_{i}} = {}^{0}T_{1} \cdot {}^{1}T_{2} \dots {}^{i-1}T_{i} \cdot {}^{i}T_{SU_{i}}, \quad \forall i \in \{1, 2, \dots, n\}$$

- (2) Collect Data. First, static forces applied to the IMU (that is, the constant acceleration due to gravity) are measured and compensated for. Then, each reference joint is moved through its operational range in a constant rotation pattern and the resulting acceleration as measured by the IMU is stored.
- (3) **Define an error function.** Acceleration exerted on each SU  ${}^{SU_i}a_{u,d}$  can be estimated as a composition of local acceleration  ${}^{0}\mathbf{g}$ , tangential acceleration  ${}^{0}\mathbf{a}_{tan_{u,d}}$  and centripetal

acceleration  ${}^{0}\mathbf{a}_{cp_{u,d}}$ :

$${}^{0}\mathbf{a}_{tan_{u,d}} = {}^{0}\boldsymbol{\alpha}_{d} \times {}^{0}\mathbf{r}_{u,d}$$

$$^{0}\mathbf{a}_{cp_{u,d}}=^{0}oldsymbol{\omega}_{d} imes\left(^{0}oldsymbol{\omega}_{d} imes^{0}\mathbf{r}_{u,d}
ight)$$

$$^{SU_{i}}\mathbf{a}_{u,d} = ^{SU_{i}}\mathbf{R}_{0} \cdot \left(^{0}\mathbf{g} + ^{0}\mathbf{a}_{tan_{u},d} + ^{0}\mathbf{a}_{cp_{u,d}}\right).$$

Angular velocity  ${}^{0}\boldsymbol{\omega}_{d}$  and angular acceleration  ${}^{0}\boldsymbol{\alpha}_{d}$  are measured during data collection, whereas rotation matrix  ${}^{SU_{i}}\mathbf{R}_{0}$  and position vector  ${}^{0}\mathbf{r}_{u,d}$  can be computed using the currently estimated DH parameters.

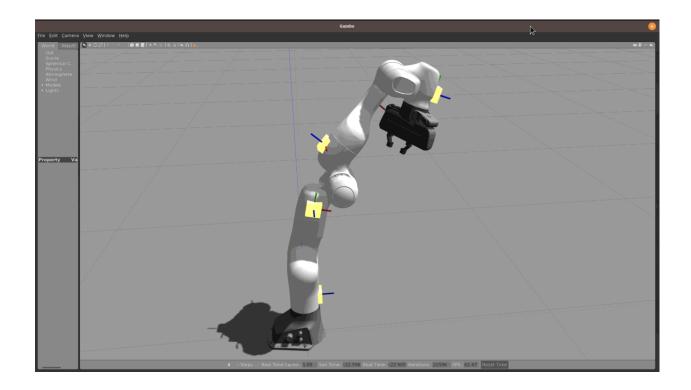
(4) Minimize the error function with a global optimizer. A global optimizer optimizes the DH parameters by minimizing a given error function. One example error function could be seen as the error between the measured accelerations from the IMUs and the estimated accelerations using the kinematic chain model for  $n_{pose}$  poses:

$$E = \sum_{i=1}^{n_{pose}} \sum_{i=1}^{n_{joint}} ||a_{i,j}^{model} - a_{i,j}^{IMU}||^2$$

Several different error functions are used to estimate both rotational and translational parameters.

The final result after calibration can be seen in figure 3.8.. Once the calibration is completed, the positions and orientation of the SU's are known. In the next section we will describe how 3D located points can be obtained from the positions and orientations of the sensors plus their readings.

Figure 3.8: Calibrated IMU positions on a simulated Franka Emika Panda robot.



## 3.2.2 Simulation of proximity sensors

We start by describing the algorithm's implementation with simulated sensors. There are some important differences compared to using real sensors:

- The sensors' positions and orientations are assumed to be known. A perfect outcome from calibration is assumed.
- The number of sensors that we can place on the robot's surface is unlimited.
- Sensor noise can be contolled.

In order to add proximity sensors to the robot suface in simulation XML macros (xacro) are utilized. Xacro's allow to write shorter, easier to maintain and more readable XML files. One xacro macro expand into a larger XML expression. Moreover, it allows math, which is useful as we will see in the following lines.

We start by describing how to set up the behaviour of the proximity sensors in Gazebo. Gazebo provides the ability to add new functionalities to the *urdf* models through the use of plugins. More specificly, it is sensor plugins that provide sensor simulation functionalities. Sensor plugins are inserted in the *urdf* description of the robot model in <gazebo> tags. Since the sensors are meant to be attached to a link, this tag must include a reference to indicate the link in which the sensor is inserted, as seen in line 1 in the code below.

```
<gazebo reference="proximity_link${proximity_id}">
                                                                           1
    <material > Gazebo / YellowGlow </material >
                                                                           2
                                                                           3
    <sensor type="ray" name="proximity_sensor${proximity_id}">
        <pose>0 0 0 0 0 0</pose>
                                                                           4
                                                                           5
        <visualize>true</visualize>
                                                                           6
        <update_rate>${freq}</update_rate>
                                                                           7
        <ray>
             <scan>
                                                                           8
                                                                           9
                 <horizontal>
                     <samples>1</samples>
                                                                           10
                     <resolution>1</resolution>
                                                                           11
                     <min_angle > -0.0001 </min_angle >
                                                                           12
                     <max_angle > 0.0001 </max_angle >
                                                                           13
                 </horizontal>
                                                                           14
             </scan>
                                                                           15
             <range>
                                                                           16
                 <min > 0.02 </min >
                                                                           17
                 < max > 2.0 < / max >
                                                                           18
                 <resolution>0.01</resolution>
                                                                           19
                                                                           20
             </range>
        </ray>
                                                                           21
        <plugin filename="libgazebo_ros_laser.so"</pre>
                                                                           22
                                                                           23
                 name="proximity_plugin${proximity_id}">
             <topicName>proximity_data${proximity_id}</topicName>
                                                                           24
                                                                           25
             <bodyName>proximity_link${proximity_id}</bodyName>
             <updateRateHZ>${freq}</updateRateHZ>
                                                                           26
                                                                           27
             <gaussianNoise > 0.0 </gaussianNoise >
             <xyzOffset>0.0 0.0 0.0
                                                                           28
             <rpyOffset>0 0 0</rpyOffset>
                                                                           29
             <frameName>proximity_link${proximity_id}</frameName>
                                                                           30
        </plugin>
                                                                           31
    </sensor>
                                                                           32
</gazebo>
                                                                           33
```

Listing 3.1: Setting up a ray sensor for Gazebo simulation.

Gazebo provides several sensor plugins [30], such as depth cameras, IMU's or force sensors.

The proximity sensing capabilities are provided in *laser* sensors. These are originally thought to simulate *LIDAR* sensors, where a number of distance sensors are installed in one module. However, in order to simulate a single proximity sensor we only need an individual laser beam. The final configuration that accomplishes this is shown between in the <ray> tag.

The sensor messages are published to the topic /proximity\_data# and the type of the messages published is sensor\_msgs/LaserScan, which is structured as follows:

```
std_msgs/Header header
    uint32 seq
    time stamp
    string frame_id

float32 angle_min

float32 angle_max

float32 angle_increment

float32 time_increment

float32 scan_time

float32 range_min

float32 range_max

float32[] ranges

float32[] intensities
```

Listing 3.2: LaserScan message structure.

Once we know how to set up the sensors, we need to place them in the robotic arm. Since the arms are mainly cylindrical, cylindrical coordinate systems  $(r, \theta, z)$  are a more suitable solution to refer to points on the surface than regular cartesian (x, y, z). urdf only allows to express positions in (x, y, z), but math provided by xacro can be utilized to express cylindrical coordinates in those required cartesian coordinates.

$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$z = z$$
(3.2)

Therefore, the proximity sensor macro allows to use cylindrical coordinates to create a new link attached to the surface of the robot that simulates a new proximity sensor. The interface to the macro is defined by the arguments it takes. This is a list of the arguments:

- **proximity\_id**: It is important to define a unique name for the link and joint. Trying to use an already defined name will result in an error.
- connected\_to: It is used to select the link in which the sensor is placed. The link's coordinate frame's z axis must be oriented in the direction of the arm cylinder. In other words, link's whose coordinate frames are not oriented in this way are not valid.
- **type**: It allows to specify the joint type: fixed, revolute or prismatic. In this case, it could have been previously set to fixed.
- $\mathbf{x0}$ ,  $\mathbf{y0}$ : If the z axis is not centered in the desired cylinder  $\mathbf{x0}$  and  $\mathbf{y0}$  can apply an offset to place the origin where it is needed.
- radius, theta, z0: The cylindrical coordinates presented in equation 3.2.

The actual implementation of the macro can be seen in the following fragment of a *xacro* code. Cylindrical coordinates are implemented in the *<origin>* tag at line 6.

```
<!-- Connect proximity sensor to ${connected_to} -->
                                                                                    1
<joint name="proximity${proximity_id}_to_${connected_to}"</pre>
                                                                                    2
         type="${type}">
                                                                                    3
    <parent link="${connected_to}"/>
    <child link="proximity_link${proximity_id}"/>
                                                                                    5
                                                                                    6
         xyz="\{x0+radius*sin(theta)\}_{\sqcup}\{y0+radius*cos(theta)\}_{\sqcup}\{z0\}"
                                                                                    7
         rpy="0_{\sqcup}0_{\sqcup}\$\{pi/2_{\sqcup}-theta\}"/>
                                                                                    8
                                                                                    9
</joint>
```

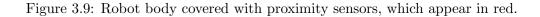
Listing 3.3: <joint> element in the proximity macro, where the position of new sensor is set up given some arguments.

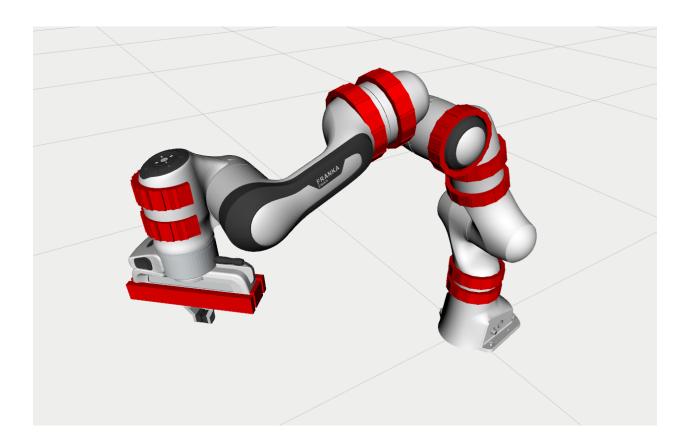
We can use this macro to place sensors through a number of rings to cover the body of the robot and simulate the artificial skin. radius specifies the selected link's radius and z0 decides the longitudinal position in which we want to place the sensor. With radius and z0 fixed, changing theta can place sensors through the entire ring radius and z0 define. The following code places 4 equally spaced sensors in a ring located in panda link 3.

```
1
<xacro:property name="sensors_per_ring" value="4"/>
                                                                           2
<xacro:property name="ring_id" value="0"/>
<xacro:property name="radius" value="0.06"/>
                                                                           3
<xacro:property name="z0" value="-0.13"/>
                                                                           4
<xacro:property name="connected_to" value="panda_link3"/>
                                                                           5
                                                                           6
<xacro:proximity proximity_id="${sensors_per_ring*ring_id+0}"</pre>
                  radius="${radius}"
                                                                           7
                  theta="${2*pi/sensors_per_ring*u0}"
                                                                           8
                  z0="${z0}" connected_to="${connected_to}"/>
                                                                           9
<xacro:proximity proximity_id="${sensors_per_ring*ring_id+1}"</pre>
                                                                           10
                  radius="${radius}"
                                                                           11
                  theta="${2*pi/sensors_per_ring*<sub>□</sub>1}"
                                                                           12
                  z0="${z0}" connected_to="${connected_to}"/>
                                                                           13
<xacro:proximity proximity_id="${sensors_per_ring*ring_id+2}"</pre>
                                                                           14
                  radius="${radius}"
                                                                           15
                  theta="${2*pi/sensors_per_ring*u2}"
                                                                           16
                  z0="${z0}" connected_to="${connected_to}"/>
                                                                           17
<xacro:proximity proximity_id="${sensors_per_ring*ring_id+3}"</pre>
                                                                           18
                  radius="${radius}"
                                                                           19
                  theta="${2*pi/sensors_per_ring*u3}"
                                                                           20
                  z0="${z0}" connected_to="${connected_to}"/>
                                                                           21
```

Listing 3.4: Using the proximity macro to place sensors in a robot arm.

The final appearance of the new sensor links added to the surface of the robot is shown in figure 3.9, where the new links are shown as red parallelepipeds. The final amount of sensors added for simulation counts 162.



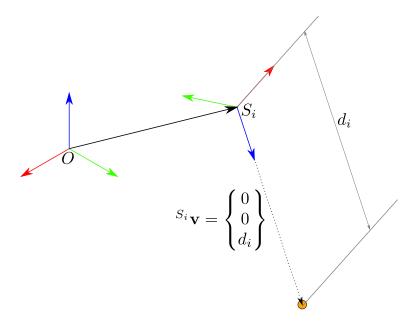


# 3.2.3 Point localization algorithm

The question answered in this section is: How do we convert the unidimensional reading of the proximity sensors embedded in the skin into a 3D point cloud in the cartesian space.

The diagram in figure 3.10 shows the relationship between the unidimensional reading  $d_i$  and the position vector of the corresponding point with respect to the base frame O.

Figure 3.10: Diagram showing the conversion of a proximity sensor reading into a 3D point in space.



The position of orientation  ${}^{j}\mathbf{T}_{S_{i}}$  of the sensor  $S_{i}$  with respect to the joint j in which its located are obtained after the calibration process presented in section 3.2.1. This allows to obtain the position and orientation  ${}^{0}\mathbf{T}_{S_{i}}$  of the sensor  $S_{i}$  with respect to the base frame O, through forward kinematics (explained in section 3.3.1.2).

$${}^0\mathbf{T}_{S_i} = {}^0\mathbf{T}_j \cdot {}^j\mathbf{T}_{S_i}$$

Once  ${}^{0}\mathbf{T}_{S_{i}}$  is known, the next step is calculating the position vector of obstacle associated to the sensor  $S_{i}$  with respect to the base frame. The distance  $d_{i}$  is read in the z axis of  $S_{i}$  (coloured in blue in the diagram in 3.10). Therefore, the position of the point detected written in the  $S_{i}$  coordinate frame has the following form:

$$S_i \mathbf{v} = \left\{ \begin{array}{c} 0 \\ 0 \\ d_i \end{array} \right\}$$

Again, simple forward kinematics allow us to transform that vector in order to express in in the base coordinate frame O.

$${}^0\mathbf{v} = {}^0\mathbf{T}_{S_i} \, {}^{S_i}\mathbf{v}$$

Expanding the expression having into account the form of homogeneous transformation matrices,  ${}^{0}\mathbf{v}$  results in:

$${}^{0}\mathbf{v} = {}^{0}\mathbf{p}_{S_{i}} + {}^{0}\mathbf{R}_{S_{i}} {}^{S_{i}}\mathbf{v} \tag{3.3}$$

As stated in section 3.2.2, each proximity sensor publishes a LaserScan type message to the topic /proximity\_data#. We have implemented a ROS node that deals with the transformations presented in this section when new messages are published to the topics and we have named it proximity\_listener. The node's activity can be summarized in 3 steps:

- (1) Listen to changes in the topics to which proximity sensors send data.
- (2) Transform the unidimensional sensor readings into 3D position vectors.
- (3) Publish the updated 3D position vectors with a certain periodicity. Also, allow saving old obstacle points for a while, so that a memory of the last reading is kept.

In the following paragraphs we expand on these steps. First, the callback function is explained, where steps (1) and (2) are carried out. Then, the publication of messages and buffer implementation are detailed in step (3).

ROS suscribers implement a callback function, which allows them to process the data published in the subscribed topics. This callback function is called every time a new message arrives to the topic. The callback that receives the proximity sensor data is presented below.

```
1
void sensorCallback(const sensor_msgs::LaserScan::ConstPtr& scan)
{
                                                                           2
                                                                           3
int sensor_number =
                                                                           4
    std::stoi
                                                                           5
    (
        scan->header.frame_id.substr
                                                                           6
                                                                           7
                                                                           8
             scan->header.frame_id.find_first_of("0123456789"),
             scan->header.frame_id.length() -1
                                                                           9
                                                                           10
        )
    );
                                                                           11
                                                                           12
                                                                           13
try
                                                                           14
                                                                           15
    listener.lookupTransform
    (
                                                                           16
        "/world",
                                                                           17
        "/proximity_link" + std::to_string(sensor_number),
                                                                           18
        ros::Time(0),
                                                                           19
        transform[sensor_number]
                                                                           20
    );
                                                                           21
                                                                           22
    translation1[sensor_number] <<</pre>
        transform[sensor_number].getOrigin().getX(),
                                                                           23
        transform[sensor_number].getOrigin().getY(),
                                                                           24
                                                                           25
        transform[sensor_number].getOrigin().getZ();
    translation2[sensor_number] << 0.0,</pre>
                                                                           26
                                                                           27
                                                                           28
                                      scan->ranges[0];
    rotation[sensor_number].w() =
                                                                           29
        transform[sensor_number].getRotation().getW();
                                                                           30
    rotation[sensor_number].x() =
                                                                           31
        transform[sensor_number].getRotation().getX();
                                                                           32
    rotation[sensor_number].y() =
                                                                           33
        transform[sensor_number].getRotation().getY();
                                                                           34
    rotation[sensor_number].z() =
                                                                           35
        transform[sensor_number].getRotation().getZ();
                                                                           36
                                                                           37
    live_points[sensor_number] =
                                                                           38
        translation1[sensor_number] +
                                                                           39
        (rotation[sensor_number] * translation2[sensor_number]);
                                                                           40
}
                                                                           41
                                                                           42
catch (tf::TransformException ex)
                                                                           43
    ROS_ERROR("%s",ex.what());
                                                                           44
    ros::Duration(1.0).sleep();
                                                                           45
}
                                                                           46
}
                                                                           47
```

Listing 3.5: Point localization C++ algorithm.

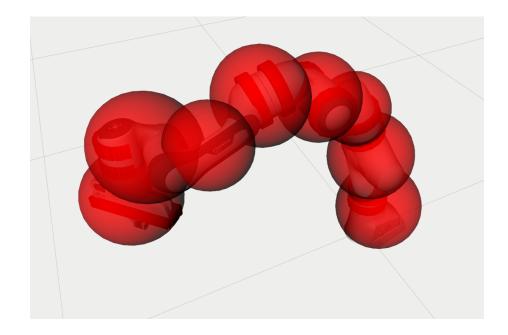
The first thing the callback function does is read the sensor from which it is receiving the message. This is done in line 3. There is a single callback for all the sensors, so this step is crucial.

Then, the sensor's position and orientation are obtained through a function that the tf library provides: lookupTransform. Also,  $S_i$ v is created through the distance readings packaged in the ranges member of the message received. Note that as mentioned in section 3.2.2, LaserScan messages have the potential capability to include several sensors in one, as in LIDAR's. However, in this case each sensor publishes a separate message, so ranges contains a unique element, indexed by ranges [0].

Last, line 38 implements equation 3.3. The obtained vector is saved in the position corresponding to the sensor that is sending the message of the std::vector live\_points.

As far as the publication of this processed data is concerned, there are two things that need to be taken into account. On the one hand, sensed points that come from the robot itself's need to be removed. We do this by covering the whole robot body with a set of spheres, shown in figure 3.11, and checking if the points are inside those spheres. This is done in isInSphere in line 10 of listing 3.6.

Figure 3.11: Sphere coverage of the robot for removal of the points detected its the surface.



```
1
geometry_msgs::Point point;
                                                                            2
ros_robotic_skin::PointArray msg;
                                                                            3
ros::Rate rate(50.0);
                                                                            4
while (ros::ok())
                                                                            5
                                                                            6
{
    for (int i = 0; i < num_sensors; i++)</pre>
                                                                            7
    {
                                                                            8
        if (std::isnan(live_points[i].x()) ||
                                                                            9
             isInSphere(live_points[i]) ||
                                                                            10
             (live_points[i].z() < floor_threshold) && removeFloor);</pre>
                                                                            11
        else
                                                                            12
        {
                                                                            13
             point.x = live_points[i].x();
                                                                            14
             point.y = live_points[i].y();
                                                                            15
             point.z = live_points[i].z();
                                                                            16
             msg.points.push_back(point);
                                                                            17
        }
                                                                            18
                                                                            19
    pub.publish<ros_robotic_skin::PointArray>(msg);
                                                                            20
                                                                            21
    msg.points.clear();
                                                                            22
    rate.sleep();
                                                                            23
}
```

Listing 3.6: Body and floor points removal and publication C++ algorithm.

Another optional filter that can be applied to the perveived points is that if the boolean variable removeFloor is set to true, points that are lower than a certain threshold floor\_threshold), in meters, will also be removed. Also, if a sensor i does not perceive any point in the range for which it is set up, live\_point[i] will be

and the point will not be added to the message.

The points are packed in a custom created message called ros\_robotic\_skin::PointArray, whose only field is an array of geometry\_msgs::Points. This is done at 100 Hz, or what is the same, every 10 ms.

Moreover, the points obtained at each of the iterations are saved in a control buffer. This is the portion of the proximity listener that implements this behaviour, where buffer is a data structure of type std::vector<Eigen::Vector3d>.

```
if (buffer.size() == 10)
{
    buffer.pop_back();
}
buffer.insert(buffer.begin(), final_points);
```

Listing 3.7: Implementation of the buffer in the Proximity Listener

# 3.2.4 Visualization in rviz

In this section we extoplain the last step of the perception part: visualization. Visualization of the data perveived by the robot is a very intuitive way of seeing what is going on, both on the perception and control algorithms. We will see how to visualize the data processed by the proximity\_listener node in rviz.

There are several dysplay types that can be visualized in rviz. We use Marker Arrays [31] to visualize the point cloud generated.

We have called the class that implements the visualization ProximityVisualizer. In the

initializer of the class, shown in listing 3.8, the node is suscribed to the data published in the topic live\_points by proximity\_listener. The data received in that topic will be processed in ProximityVisualizer::Callback. Next, the publication of messages of type MarkerArray in the topic visualization\_marker\_array is set up. The general properties that are kept through all of the Markers that will be added to the MarkerArray are also set up and the rest of the properties are initialized.

Note that these properties allow to set up the Marker's shape, the size, the color, the coordinates in which it will be located, as well as the frame in which those coordinates are written and the orientation. namespace allows organization within the same topic so that Markers can be further classified. The id of the marker is unique and whenever a new marker with the same id is published, the previous one is deleted. Finally, action can be ADD, DELETE or DELETEALL.

```
ProximityVisualizer::ProximityVisualizer()
                                                                         1
                                                                         2
                                                                         3
                                                                         4
    sub = n.subscribe < ros_robotic_skin::PointArray >
        ("live_points", 1, &ProximityVisualizer::Callback, this);
                                                                         5
    pub = n.advertise < visualization_msgs::MarkerArray >
                                                                         6
        ("visualization_marker_array", 1);
                                                                         7
    // Marker properties that are the same for all the points
                                                                         8
                                                                         9
    marker.ns = "Live_Points";
    marker.action = visualization_msgs::Marker::ADD;
                                                                         10
    marker.scale.x = 0.05;
                                                                         11
    marker.scale.y = 0.05;
                                                                         12
    marker.scale.z = 0.05;
                                                                         13
    marker.color.r = 1.0;
                                                                         14
    marker.color.g = 0.0;
                                                                         15
    marker.color.b = 0.0;
                                                                         16
    marker.color.a = 1.0;
                                                                         17
    marker.header.frame_id = "/world";
                                                                         18
    marker.type = visualization_msgs::Marker::SPHERE;
                                                                         19
    marker.pose.orientation.x = 0.0;
                                                                         20
                                                                         21
    marker.pose.orientation.y = 0.0;
                                                                         22
    marker.pose.orientation.z = 0.0;
    marker.pose.orientation.w = 1.0;
                                                                         23
    // Marker properties that depend on the point
                                                                         24
    marker.header.stamp = ros::Time::now();
                                                                         25
                                                                         26
    marker.id = 0;
    marker.pose.position.x = 0.0;
                                                                         27
    marker.pose.position.y = 0.0;
                                                                         28
```

Listing 3.8: Initializer of the Proximity Visualizer class

Every time a new message arrives to the live\_points topic in runtime, the callback will add the new points received to a MarkerArray. This is shown in listing 3.9.

The sequence when a new message arrives is as follows. First, all the previously published markers are deleted publishing a MarkerArray that contains a Marker whose action is DELETEALL. Then, the new points received are packed into a Marker and pushed back in a MarkerArray. Finally, this MarkerArray is published.

```
1
void ProximityVisualizer::Callback(
    const ros_robotic_skin::PointArray::ConstPtr& msg)
                                                                     2
{
                                                                     3
    // Delete all points from previous callback
                                                                     4
    marker.action = visualization_msgs::Marker::DELETEALL;
                                                                     5
                                                                     6
    marker_array.markers.push_back(marker);
                                                                     7
    pub.publish < visualization_msgs::MarkerArray > (marker_array);
                                                                     8
    marker_array.markers.clear();
                                                                     9
                                                                     10
    // Add new points
    marker.action = visualization_msgs::Marker::ADD;
                                                                     11
    marker.header.stamp = ros::Time::now();
                                                                     12
    for (int i = 0; i < msg->points.size(); i++)
                                                                     13
                                                                     14
    {
        // Check that it's not 'nan' or 'inf'
                                                                     15
        marker.id = i;
                                                                     16
                                                                     17
        marker.pose.position.x = msg->points[i].x;
        marker.pose.position.y = msg->points[i].y;
                                                                     18
        marker.pose.position.z = msg->points[i].z;
                                                                     19
        marker_array.markers.push_back(marker);
                                                                     20
                                                                     21
    pub.publish < visualization_msgs::MarkerArray > (marker_array);
                                                                     22
    marker_array.markers.clear();
                                                                     23
                                                                     24
}
```

Listing 3.9: Callback of the Proximity Visualizer class

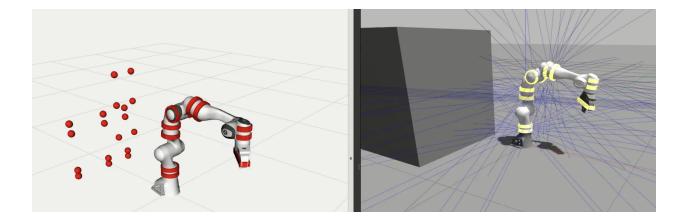
In order to visualize the MarkerArray, a subscription to the topic has to be added in *rviz*, as shown in figure 3.12. Since the Namespaces field is empty, all the points in the received MarkerArray will be visualized, with no exception.

Figure 3.12: Menu of the Marker Array plugin in rviz.



The points are seen in rviz as shown in figure 4.1, where a wall in front of the robot is being perceived.

Figure 3.13: Final visualization of the perceived points in rviz.



# 3.3 Control

This is the main section of this work. Here we present all the concepts necessary for safe motion control, from fundamental robot kinematics to obstacle avoidance algorithms and different means by which robot redundancy can be leveraged.

# 3.3.1 The Kinematic Control Problem

In this section one of the most fundamental problems in robotics will be defined and solved: the Kinematic Control Problem. It can be formulated as the problem of obtaining a joint space trajectory  $\mathbf{q}(t)$  that satisfies a desired trajectory in the cartesian space  $\mathbf{x}(t)$ .

This problem contains several elements required in order to solve the collision avoidance problem in subsequent sections. Moreover, the collision avoidance will be built as a modification to the more fundamental method described in this section.

## 3.3.1.1 Geometric representation of the kinematic chain of a robot

Kinematics is the branch of physics that studies the motion of the bodies. It does so with no consideration of the causes that originate the motion, forces, and torques. Kinematics is required and fundamental in robotics for design, analysis, control, and simulation.

In order to study the kinematics of a robot its geometric representation must be defined mathematically beforehand. Rigid body kinematics deals with the problem of studying relative movement of two non-deformable elements by attaching a coordinate frame to each of them. Robot manipulators and robots in general can be seen as a series of rigid links connected by joints. Therefore, attaching a frame to each of the links of a robot in a convenient manner is how robots' geometry is usually represented.

However, there are infinitely many ways in which this 3-dimensional frames can be assigned to the links. The origin and rotation of the frames could be located anywhere in space as long as its movement was fixed to the respective links.

That is where conventions for geometric representation come in place. The most well known and extended convention was introduced by Denavit and Hartenberg (DH) in 1955 [32]. Although there have been numerous adaptations, the representations serve the same purpose and DH parameters are still widely used. In fact, the manufacturer of the robot employed in this work (3.1.1) provides DH parameters in its documentation [22].

DH suggest a set of rules to place the frames corresponding to each robot link:

- The n links of the mechanism are numbered from 0 to N, being link 0 the fixed base.
- The n joints of the mechanism are numbered from 1 to N, with joint i located between

links i-1 and i.

- The  $\mathbf{z_i}$  axis is located along the axis of joint *i*.
- The  $x_{i-1}$  axis is located along the common perpendicular between  $z_{i-1}$  and  $z_i$  axis.

Then, they define 4 parameters that completely define the position and rotation of a link with respect to the previous one. Note that full position and orientation are usually defined by at least 6 parameters. However, geometric constraints inherent to robotic arms allow us to define them with just 4 parameters.

The four parameters are:

- $a_i$ : the distance from  $z_{i-1}$  to  $z_i$  along  $x_{i-1}$ .
- $\alpha_i$ : the angle from  $\mathbf{z_{i-1}}$  to  $\mathbf{z_i}$  about  $\mathbf{x_{i-1}}$ .
- $\mathbf{d_i}$ : the distance from  $\mathbf{x_{i-1}}$  to  $\mathbf{x_i}$  along  $\mathbf{z_i}$ .
- $\theta_i$ : the angle from  $\mathbf{x_{i-1}}$  to  $\mathbf{x_i}$  about  $\mathbf{z_i}$ .

Most common joint types in robot manipulators are revolute and prismatic joints. In the case of **revolute joints** all the parameters but  $\theta_{\mathbf{i}}$  are defined by the geometric design of the robot, while  $\theta_{\mathbf{i}}$  is the variable of the movement. If the joint is **prismatic**, all the parameters but  $\mathbf{d}_{\mathbf{i}}$  are defined by the geometry of the robot, while  $\mathbf{d}_{\mathbf{i}}$  is the variable of the movement.

Franka Panda Emika (described in section 3.1.1) is equipped with 7 revolute joints. Its DH parameters are given by the manufacturer and shown in figure 3.1.

In ROS, the robots' geometry is internally described in *urdf* files. *urdf* files make use of Extensible Markup Language (XML), the same markup language that is used for web pages in html files. The following fragment taken from the complete descripion of Franka Panda (by justagist [33]) Emika describes the transformation from frame 6 to frame 7.

```
k_velocity="40.0"
                                                                 3
                       soft_lower_limit="-2.8973"
                                                                 4
                       soft_upper_limit="2.8973"/>
                                                                 5
     6
     <parent link="${arm_id}_link6"/>
                                                                 7
     <child link="${arm_id}_link7"/>
                                                                 8
     < axis xyz = "0 0 1"/>
                                                                 9
     limit effort="12" lower="-2.8973"
                                                                 10
                       upper="2.8973"
                                                                 11
                       velocity="2.6100"/>
                                                                 12
     <dynamics damping="1.0" friction="0.5"/>
                                                                 13
</joint>
                                                                 14
```

Listing 3.10: Fragment of panda\_arm.urdf

The relative positions and orientations are defined under the tag  $\langle origin/\rangle$  in line 6. DH parameters are not used in this tag, even though urdf could be adapted to use them through the language xacro, that permits to do math inside textiturdf. Rotation is defined through Euler Angles: rotations are defined by applying rotation about x, y and z axes, in this order. Translation is defined with a  $3 \times 1$  vector that goes from frame i-1 to frame i, from 6 to 7 in this case.

The use of DH parameters would have been beneficial and less error prone through the process of writing the urdf description.

In the next section we will make use of the geometric representation of the robot to locate the different elements of the robot.

### 3.3.1.2 Forward Kinematics

Forward kinematics provides a mathematical tool that allows to find the position and orientation of the end effector or any other point in the kinematic chain given all the joint variables' values. These are ( $\theta_i$ s for revolute joints and  $\mathbf{d_i}$ s for prismatic joints.

A common way to represent the rotation and translation from one axis to another are homogeneous transformation matrices. They are  $4 \times 4$  matrices defined as in equation 3.4.

$${}^{i-1}\mathbf{T}_i = \begin{pmatrix} {}^{i-1}\mathbf{R}_i & {}^{i-1}\boldsymbol{p}_i \\ \mathbf{0}^{\mathrm{T}} & 1 \end{pmatrix}$$
(3.4)

The top left  $3 \times 3$  matrix  $^{i-1}\mathbf{R}_i$  defines the rotation from axis i-1 to axis i.  $^{i-1}\mathbf{R}_i$  is an orthogonal matrix, this meaning that the basis formed by its columns is orthonormal. Each of the column vectors are required to have unit length. One nice property of orthogonal matrices is that their inverse is exactly the same as their transpose:

$$(^{i-1}\mathbf{R}_i)^{-1} = ^i \mathbf{R}_{i-1} = (^{i-1}\mathbf{R}_i)^{\mathsf{T}}$$

On the other hand, the top right  $3 \times 1$  position vector  $i^{-1}\mathbf{p}_i$  defines the translation vector from axis i-1 to axis i.

Homogeneous transformation matrices are an easy and convenient way to calculate several linked transformations.  $^{i-2}\mathbf{T}_i$  would be calculated as follows:

$$^{i-2}\mathbf{T}_{i} = ^{i-2}\mathbf{T}_{i-1}^{i-1}\mathbf{T}_{i} = \left(\begin{array}{cc}^{i-2}\mathbf{R}_{i-1} & ^{i-2}\boldsymbol{p}_{i-1} \\ \mathbf{0}^{\mathrm{T}} & 1 \end{array}\right) \left(\begin{array}{cc}^{i-1}\mathbf{R}_{i} & ^{i-1}\boldsymbol{p}_{i} \\ \mathbf{0}^{\mathrm{T}} & 1 \end{array}\right) = \left(\begin{array}{cc}^{i-2}\mathbf{R}_{i-1}^{i-1}\mathbf{R}_{i} & (^{i-2}\boldsymbol{p}_{i-1} + ^{i-2}\mathbf{R}_{i-1}^{i-1}\boldsymbol{p}_{i}) \\ \mathbf{0}^{\mathrm{T}} & 1 \end{array}\right)$$

This is the desired behaviour because  ${}^{i-2}\mathbf{R}_{i-1}^{i-1}\mathbf{R}_i$  represents the combination of applying the rotation  ${}^{i-2}\mathbf{R}_{i-1}$  first and  ${}^{i-1}\mathbf{R}_i$  after.  $({}^{i-2}\boldsymbol{p}_{i-1} + {}^{i-2}\mathbf{R}_{i-1}^{i-1}\boldsymbol{p}_i)$  takes the vector  ${}^{i-1}\boldsymbol{p}_i$  to the i-2 basis and them it sums the origin of the frame i-1,  ${}^{i-2}\boldsymbol{p}_{i-1}$ , already written in the i-2 axis.

The homogeneous transformation matrix  $^{i-1}\mathbf{T}_i$  can be built from the DH parameters representation with  $\mathbf{a_i}$ ,  $\alpha_i$ ,  $\mathbf{d_i}$  and  $\theta_i$ . For that purpose the following steps are combined in order:

- (1)  $\alpha_i$  rotation about the axis  $x_{i-1}$ .
- (2)  $\mathbf{a_i}$  translation through the axis  $x_{i-1}$ .
- (3)  $\theta_i$  rotation about the axis  $z_i$ .
- (4)  $\mathbf{d_i}$  translation about the axis  $z_i$ .

$$i^{-1}\mathbf{T}_{i} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \alpha_{i} & -\sin \alpha_{i} & 0 \\ 0 & \sin \alpha_{i} & \cos \alpha_{i} & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 & a_{i} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} \cos \theta_{i} & -\sin \theta_{i} & 0 & 0 \\ \sin \theta_{i} & \cos \theta_{i} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_{i} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
$$\begin{pmatrix} \cos \theta_{i} & -\sin \theta_{i} & 0 & a_{i} \\ -\sin \theta_{i} & 0 & a_{i} \end{pmatrix}$$

$$= \begin{pmatrix} \cos \theta_i & -\sin \theta_i & 0 & a_i \\ \sin \theta_i \cos \alpha_i & \cos \theta_i \cos \alpha_i & -\sin \alpha_i & -\sin \alpha_i d_i \\ \sin \theta_i \sin \alpha_i & \cos \theta_i \sin \alpha_i & \cos \alpha_i & \cos \alpha_i d_i \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

Once all the transformation matrices  $i^{-1}\mathbf{T}_i$  are defined for  $i=1,\ldots,n$ , the full transformation from the base i=0 to the end effector i=n transformation can easily be calculated:

$${}^{0}\mathbf{T}_{n} = {}^{0}\mathbf{T}_{1}^{1}\mathbf{T}_{2}\dots {}^{n-1}\mathbf{T}_{n}$$

Forward Kinematics are calculated in the robot\_state\_publisher package [34]. The robot's description is read from a *urdf* file loaded in the parameter server. Then, the joints' values are read from a topic named /joint\_states and used to compute forward kinematics of all the joints. The results are published in a topic named /tf.

# 3.3.1.3 Inverse Kinematics

The inverse Kinematics problem is the opposite to the one of Forward Kinematics (section 3.3.1.2). The objective in this case is not to locate the robot's parts for known joint values, but to find the joint values given the end effector (or any other point in the kinematic chain) position and orientation.

Given the nature of the homogeneous transformation matrices defined in section 3.3.1.2, whose elements contain sin and cos functions, the problem requires to solve a set of non linear equations defined by:

$${}^{0}\mathbf{T}_{n}(q_{1},\ldots,q_{n})=({}^{0}\mathbf{T}_{n})^{d}$$

It is trivial to see that solving the position  ${}^{0}\boldsymbol{p}_{n}(q_{1},\ldots,q_{n})=({}^{0}\boldsymbol{p}_{n})^{d}$  describes 3 equations. On the other hand, since rotation matrices provide six auxiliary relationships (3 coming from the fact that column vectors to have unit length, and 3 coming from the requirement of its column vectors being mutually orthogonal), and they contain 9 elements, 9-6=3 more equations coming from  ${}^{0}\mathbf{R}_{n}(q_{1},\ldots,q_{n})=({}^{0}\mathbf{R}_{n})^{d}$ .

In order for a solution to exist, the desired location and rotation  $({}^{0}\mathbf{T}_{n})^{d}$  needs to be in the robot's workspace.

A closed form of the equation does not always exist. In fact, in the common case there is no way to do this. Consequently, numerical methods are needed.

For Franka Panda Emika n = 7, there are infinitely many joint values that satisfy the Inverse Kinematics equations.

### 3.3.1.4 Forward Instantaneous Kinematics

Forward instataneous Kinematics relates the motion rates of joints  $\mathbf{q} = \begin{bmatrix} q_1 & \dots & q_n \end{bmatrix}^\mathsf{T}$  with the velocities in the 3D Cartesian Space of the end effector.

Note that everything defined for the specific point in the kinematic chain end effector will also be adaptable to any other point in the kinematic chain, by simply considering a reduced kinematic chain that goes from the base to joint i, instead of to the end effector.

We start by redefining what we got in section 3.3.1.2. This was our final result, given in the form of homogeneous transformation matrices:

$${}^0\mathbf{T}_n = {}^0\mathbf{T}_1^1\mathbf{T}_2\dots^{n-1}\mathbf{T}_n = \left(egin{array}{cc} {}^0\mathbf{R}_n & {}^0oldsymbol{p}_n \ \mathbf{0}^\mathrm{T} & 1 \end{array}
ight)$$

The position of the end effector is well defined by the position vector  ${}^{0}\boldsymbol{p}_{n}$ . However, the rotation matrix  ${}^{0}\boldsymbol{p}_{n}$ , by definition of rotation matrix, contains six auxiliary relationships (3.3.1.2).

In consequence, rotation matrices are not minimal representations. For Forward Instantaneous Kinematics we will use a minimal representation of orientation, such as Euler angles (3.3.1.1), where orientation is completely described with just three elements.

$$\mathbf{t}(t) = \mathbf{f}(t) = egin{bmatrix} f_1(t) \ f_2(t) \ f_3(t) \ f_4(t) \ f_5(t) \ f_6(t) \end{bmatrix}$$
 r vector function.  $f_1(t), f_2(t),$ 

**f** is a differentiable nonlinear vector function.  $f_1(t)$ ,  $f_2(t)$ , and  $f_3(t)$  describe the position of the end effector and  $f_4(t)$ ,  $f_5(t)$ , and  $f_6(t)$  its orientation.

Thus, the rate of change of this parameters is given by  $\dot{\mathbf{t}}(t)$ ,

$$\dot{t}_i(t) = \frac{dt_i(t)}{dt} = \sum_{i=1}^n \frac{\partial t_i}{\partial q_i} \cdot \frac{dq_i}{dt} = (\nabla_{\mathbf{q}} t_i)^{\mathsf{T}} \cdot \dot{\mathbf{q}}$$

In matrix form,

$$\dot{\mathbf{t}} = \frac{d\mathbf{t}}{dt} = \left[\frac{\partial \mathbf{t}}{\partial \mathbf{q}}\right] \cdot \dot{\mathbf{q}} = \mathbf{J_t}(\mathbf{q}) \cdot \dot{\mathbf{q}}$$

 $\mathbf{J_t}(\mathbf{q}) \in \mathbb{R}^{6 \times n}$  is called the *Jacobian*. It relates joint space velocities to cartesian space velocities and it is a function of the joint angles (or distances in the case of prismatic joints)  $\mathbf{q}$ . Its *i*th row is the gradient of the component i in  $\mathbf{t}(t) \nabla_{\mathbf{q}} t_i$ .

It is convenient to remark that, with this formulation, the components of the velocity vector  $\dot{\mathbf{t}}(t)$  express the rate of change of the parameters that form the minimal representation vector  $\mathbf{t}(t)$ . In Rigid Body Kinematics, the velocities of all the points in a rigid body (a link in our case) are completely defined by two vectors [35].

(1) The angular velocity of the body  $\omega$ .

(2) The velocity of one point pertaining to the body  $\mathbf{v}_O$ .

Given those two vectors the velocity  $\mathbf{v}_P$  of any other point P pertaining to the same body can be calculated as:

$$\mathbf{v}_P = \mathbf{v}_O + \boldsymbol{\omega} \times \overrightarrow{\mathbf{OP}} \tag{3.5}$$

However, while the end effector velocity represented by the first three elements of  $\dot{\mathbf{t}}(t)$  is suitable for  $\mathbf{v}_O$ , the last three elements of  $\dot{\mathbf{t}}(t)$  don't express the angular velocity  $\boldsymbol{\omega}$  of the end effector link. They represent the rate of change of Euler Angles or any other minimal representation parameters chosen to describe orientation.

The actual Jacobian that relates the joint space velocities to  $\dot{\mathbf{x}} = \begin{bmatrix} \mathbf{v}_{\mathrm{end~effector}} \\ \boldsymbol{\omega}_{\mathrm{end~effector}} \end{bmatrix}$  is:

$$\mathbf{J}(\mathbf{q}) = \mathbf{T}(t) \cdot \mathbf{J_t}(\mathbf{q})$$

$$\mathbf{T}(t) = egin{bmatrix} \mathbf{I} & \mathbf{0} \ \mathbf{0} & \mathbf{R}(t) \end{bmatrix}$$

 $\mathbf{T}(t)$  only depends on time t and its expression depends on the minimal representation chosen to describe orientation. The resulting equation is:

$$\dot{\mathbf{x}} = \mathbf{J}(\mathbf{q}) \cdot \dot{\mathbf{q}} \tag{3.6}$$

There are many methods that compute the values of the jacobian matrix  $\mathbf{J}(\mathbf{q})$  [36]. The general idea underlying is similar in all of them, with differences in efficiency.

$$\mathbf{J}(\mathbf{q}) = egin{bmatrix} oldsymbol{\mathcal{J}}_{P1} & oldsymbol{\mathcal{J}}_{P2} & \dots & oldsymbol{\mathcal{J}}_{Pn} \ oldsymbol{\mathcal{J}}_{O1} & oldsymbol{\mathcal{J}}_{O2} & \dots & oldsymbol{\mathcal{J}}_{On} \end{bmatrix}$$

 $\mathcal{J}_{Pi} \in \mathbb{R}^{3\times 1}$  denotes the contribution of  $\dot{q}_i$  per radian to  $\mathbf{v}_{\mathrm{end\ effector}}$ .  $\mathcal{J}_{Oi} \in \mathbb{R}^{3\times 1}$  denotes the contribution of  $\dot{q}_i$  per radian to  $\boldsymbol{\omega}_{\mathrm{end\ effector}}$ . Their value is computed as follows:

$$m{J}_{Pi} = egin{cases} ^0 \mathbf{z}_{i-1} & ext{if joint } i ext{ is prismatic} \ ^0 \mathbf{z}_{i-1} imes ^{i-1} m{p}_{ ext{end effector}} & ext{if joint } i ext{ is revolute} \ \\ m{J}_{Oi} = egin{cases} \mathbf{0} & ext{if joint } i ext{ is prismatic} \ ^0 \mathbf{z}_{i-1} & ext{if joint } i ext{ is revolute} \end{cases}$$

As described in section 3.3.1.1,  ${}^{0}\mathbf{z}_{i-1}$  is joint *i*'s *z* axis, which is a unitary vector in the direction of the joint.  ${}^{0}\mathbf{z}_{i-1}$  coincides both the direction in which a prismatic joint contributes to the end effector velocity  $\mathbf{v}_{\text{end effector}}$  and with the contribution of a revolute joint to the angular velocity of the end effector  $\boldsymbol{\omega}_{\text{end effector}}$ . The magnitude  $\mathbf{z}_{i-1} \times^{i-1} \boldsymbol{p}_{\text{end effector}}$  is due to the  $\boldsymbol{\omega} \times \overrightarrow{\mathbf{OP}}$  part in equation 3.5. It is obvious that the contribution of a prismatic joint to  $\boldsymbol{\omega}_{\text{end effector}}$  is  $\mathbf{0}$ .

In section 3.1.5.1 we presented KDL as the library we use to deal with problems fundamental to robot kinematics. This is how the robotic jacobian is obtained in KDL:

```
Eigen::MatrixXd KDLSolver::computeJacobian
                                                                         1
                                                                         ^2
                                                                         3
    std::string linkName,
    Eigen::VectorXd q
                                                                         4
)
                                                                         5
{
                                                                         6
    // Obtain the description of the robot up to link linkName
                                                                         7
                                                                         8
    KDL::Chain kdlChain;
    kdlTree.getChain("panda_link0", linkName, kdlChain);
                                                                         9
    int number_joints = kdlChain.getNrOfJoints();
                                                                         10
    // Construct the jacobian solver with the description obtained
                                                                         11
    KDL::ChainJntToJacSolver JSolver =
                                                                         12
        KDL::ChainJntToJacSolver(kdlChain);
                                                                         13
    // Prepare the data for the solver
                                                                         14
    KDL::Jacobian J;
                                                                         15
    J.resize(number_joints);
                                                                         16
    KDL::JntArray KDLJointArray(7);
                                                                         17
    KDLJointArray.data = q;
                                                                         18
    KDLJointArray.resize(number_joints);
                                                                         19
    // Obtain the jacobian
                                                                         20
    JSolver.JntToJac(KDLJointArray, J);
                                                                         21
    return J.data;
                                                                         22
}
                                                                          23
```

Listing 3.11: Implementation of the function computeJacobian.

Note that linkName lets us decide which is the link for we want to obtain the jacobian. If the link is other than the end effector we will call it partial jacobian.

Later, in section 3.3.3 we will upgrade this function so that it will let us obtain the jacobian for any point attached to a link and not only the one corresponding to the joints.

### 3.3.1.5 Inverse Instantaneous Kinematics

As defined at the beginning of 3.3.1, the kinematic control problem deals with the problem of obtaining a joint space trajectory  $\mathbf{q}(t)$  that satisfies a desired trajectory in the cartesian space  $\mathbf{x}(t)$ . Several approaches can be taken in order to find a solution to this problem, but according to [37], the most relevant ones for redundant manipulators (sections 3.1.1 and 3.3.1.2) solve the problem at the joint velocity level.

Therefore, joint space velocities  $\dot{\mathbf{q}}(t)$  that result in end effector velocities  $\dot{\mathbf{x}}_{\mathbf{d}}$  that satisfy a desired trajectory in the cartesian space  $\mathbf{x}_{\mathbf{d}}(t)$  must be found. This is the opposite problem to the one presented in the previous section (3.3.1.4) that was resolved in equation 3.6. The equation presents a linear system of equations in the unknowns  $\dot{\mathbf{q}}$ . This contrasts with the fact that, as stated in section 3.3.1.3, the Inverse Kinematics problem is non-linear. The jacobian  $\mathbf{J}(\mathbf{q})$  is a local linearization of the instantaneous problem, which is valid only for the specific time instant t and joint values  $\mathbf{q}$  for which it was calculated. In the general task this is represented by m variables:

$$\mathbf{J}(\mathbf{q}) \cdot \dot{\mathbf{q}} = \dot{\mathbf{x}}_{\mathbf{d}} \\ {m \times n} \quad {n \times 1} \quad {m \times 1}$$
 (3.7)

It is important to note that the maximum number of variables a task can be identified with is m = 6. This implies that for a redundant robot for which n >= 7, m > n will always remain true.

In the following paragraphs we will utilize some definitions and theorems of Linear Algebra to verify that the linear system of equations defined by equation 3.7 has a set of solutions that can only be either empty or infinite. We also verify that when the  $\mathbf{J}(\mathbf{q})$  is full rank, i.e. when its rank

is exactly m, the vector space of solutions has dimension (m-n). When the rank is < m, there exists no solution.

We start by listing some definitions and theorems of Linear Algebra (taken from [38]. However this are well known results and definitions and can be found in any general linear algebra book).

Definition 1. The row space/column space of a matrix is the span of the set of its rows/columns.

The row rank/column rank is the dimension of this space, the number of linearly independent rows/columns.

**Theorem 2.** For any matrix, the row rank and column rank are equal.

**Definition 3.** The rank of a matrix is its row rank or its column rank.

**Theorem 4.** No linearly independent set can have a size greater than the dimension of the enclosing space.

Therefore, because of this last theorem, it is obvious that the maximum rank for a given matrix  $\mathbf{A} \in \mathbb{R}^{m \times n}$  is the minimum value between m and n. The rank of this matrix can only be equal to or less than that maximum rank. In the case of redundant robots, the maximum rank  $\mathbf{J}(\mathbf{q})$  will always be given by the dimension of the row space m, that is, the number of variables needed to define the task.

**Theorem 5.** Any linear system's solution set has the form

$$\left\{ \vec{p} + c_1 \vec{\beta}_1 + \dots + c_k \vec{\beta}_k \mid c_1, \dots, c_k \in \mathbb{R} \right\}$$

where  $\vec{p}$  is any particular solution and where the number of vectors  $\vec{\beta}_1, \ldots, \vec{\beta}_k$  equals the dimension of the space of solutions associated to homogeneous system.

**Theorem 6.** For linear systems with n unknowns and with matrix of coefficients A, the statements

- (1) the rank of  $\mathbf{A}$  is r
- (2) the vector space of solutions of the associated homogeneous system has dimension (n-r)

are equivalent.

Consequently, the homogeneous system associated to equation 3.7,  $\mathbf{J}(\mathbf{q}) \cdot \dot{\mathbf{q}} = \mathbf{0}$ , has a solution space of dimension  $(n-r) \geq (n-\max(r)) = (n-m)$ . In the case of Panda Franka Emika, the solution space of the associated homogeneous system will always be greater than or equal to 1:  $(n-r) \geq (n-\max(m)) = (7-6)$  and in consequence, if a solution exists equation 3.7 will have infinitely many solutions.

However, the existence of solution to the actual system of equations, and not its associated homogeneous system, is not guaranteed:

**Theorem 7.** For a linear system of equations Ax = b, a solution exists for all b if and only if the rank of A is equal to the dimension of b, i.e, A is full rank.

This means that every time  $\mathbf{J}(\mathbf{q})$  loses a rank, r < m, equation 3.7 won't have a solution for all  $\dot{x}_d$  and the ability to control one axis either of translation or rotation will lost. The positions q in which this situation is given are called singularities.

In table 3.4, we can see that all the possible situations for equation 3.7 are summarized by the last column. If a solution exists there are infinitely many solutions, with dimension n - m.

Table 3.4: Number of solutions of a linear system

		number of solution of	
		the homogeneous system?	
		one	infinitely many
a particular	yes	unique solution	infinitely many solutions
solution exists?	no	no solutions	no solutions

Summing up, the kinematic control problem has been defined as a set of linear equations (equation 3.7) and the existence of the solutions has been studied until now. Next, we must find a solution to the set of equations.

The most widely used tool to find this solution is the **Moore-Penrose pseudoinverse** of the jacobian  $\mathbf{J}^+(\mathbf{q})$ , where  $\mathbf{J}^+(\mathbf{q}) = \mathbf{J}^\top (\mathbf{q})(\mathbf{J}(\mathbf{q})\mathbf{J}^\top(\mathbf{q}))^{-1}$ . The complete set of solutions can be described as:

$$\dot{\mathbf{q}} = \mathbf{J}^{+}(\mathbf{q})\dot{\mathbf{x}}_{\mathbf{d}} + (\mathbf{I} - \mathbf{J}^{+}(\mathbf{q})\mathbf{J}(\mathbf{q}))\,\boldsymbol{\xi} \tag{3.8}$$

 $\boldsymbol{\xi} \in \mathbb{R}^{n \times 1}$  is the free variable that lets us choose between different  $\dot{\mathbf{q}}$  to obtain the same end effector velocity  $\dot{\mathbf{x}}_{\mathbf{d}}$ . This is possible because  $(\mathbf{I} - \mathbf{J}^+(\mathbf{q})\mathbf{J}(\mathbf{q}))$  is the null space projection matrix of  $\mathbf{J}(\mathbf{q})$ , meaning that it projects any vector into its null space. This implies that it doesn't change the final desired velocity.

This solution give us all the posible solutions for the least squares problem, which aims to minimize  $\|\dot{\mathbf{x}}_{\mathbf{d}} - \mathbf{J}(\mathbf{q})\dot{\mathbf{q}}\|$ . More specifically, if  $\boldsymbol{\xi} = \mathbf{0}$ ,  $\dot{\mathbf{q}} = \mathbf{J}^+(\mathbf{q})\dot{\mathbf{x}}_{\mathbf{d}}$  is the minimum norm solution to the least squares problem.

However, there are some problems with this solution. As mentioned before,  $\mathbf{J}(\mathbf{q})$  not being full rank implies the control over one of the motion axes is lost. This happens at certain joint configurations  $\mathbf{q}$  called singularities. Not only is reaching one of these configurations a problem, but near to singularity configurations are also problematic. This is true because even though a solution is possible, at these near to singularity configurations excessive joint space velocities are required to move the end effector in the axis that is close from being uncontrolable.

The reader may think that it would be useful to have a measure of how close the configuration of the robot is from a singularity. One possible solution is the one introduced by [39]:

$$\sqrt{\det(\mathbf{J}^\intercal \cdot \mathbf{J})}$$

This measure indicates how close a robot is from a singularity. It is the equivalent to the determinant of a square matrix. When it approaches 0 it indicates  $\mathbf{J}$  is close from loosing a rank.

Some method needs to be used to avoid reaching a singularity configuration. Recall that there are infinitely many solutions to the joint velocities that accomplish the desired end effector velocity  $\dot{\mathbf{x}}_{\mathbf{d}}$ , so if the addecuate joint velocities are chosen singularities can be avoided.

[40] presented a method that makes use of the Lagrange multipliers to minimize a certain objective function h(q). This method says that introducing the following expression in  $\xi$  in equation 3.8 will decrease the value of the chosen objective function:

$$\boldsymbol{\xi} = -\alpha \, \nabla_{\mathbf{q}} h(\boldsymbol{q})$$

where  $\alpha$  is a weight that allows to increase or decrease the effect of this second term on the final solution. Small values of  $\alpha$  will be unnoticeable, while if the values are too big the value of h(q) could even increase, since the gradient is only valid in the surroundings of the configuration at a certain time.

One possible objective function that can avoid singularities is:

$$h(\boldsymbol{q}) = \frac{1}{2} \sum_{i=1}^{n} \left( \frac{q_i - q_{i,\text{mid}}}{q_{i,\text{max}} - q_{i,\text{min}}} \right)^2$$

This function approaches 0 as the joints are close to their mid range value. The reason why this is a valid approach is that singularities usually appear when joints are close their limits.

# 3.3.1.6 End effector Position Control through Inverse Instantaneous Kinematics

In this section we present a simple algorithm that moves the end effector to a desired position in cartesian space, shown in the function moveToPosition in listing 3.12. The mathematical elements presented in previous sections are an essential part of the code.

```
void moveToPosition(const Eigen::Vector3d xd)
                                                                          1
                                                                          2
                                                                          3
    Eigen::VectorXd qDot;
    positionErrorVector = xd - x;
                                                                          4
                                                                          5
    while (positionErrorVector.norm() > position_error_threshold
                                                                          6
                                                                          7
            && ros::ok())
    {
                                                                          8
        readEndEffectorPosition();
                                                                          9
        readControlPointPositions();
                                                                          10
        positionErrorVector = xd - x;
                                                                          11
```

```
xdDot = pGain * positionErrorVector;
                                                                         12
        ros::spinOnce();
                                                                         13
        qDot = IIK(xdDot)
                                                                         14
        jointVelocityController.sendVelocities(qDot);
                                                                         15
        rate.sleep();
                                                                         16
    }
                                                                         17
    qDot = Eigen::VectorXd::Constant(7, 0.0);
                                                                         18
    jointVelocityController.sendVelocities(qDot);
                                                                         19
}
                                                                         20
                                                                          21
Eigen::VectorXd IIK(Eigen::Vector3d xdDot)
                                                                          22
                                                                         23
    J = kdlSolver.computeJacobian("end_effector", q);
                                                                         24
    Jpinv = J.completeOrthogonalDecomposition().pseudoInverse();
                                                                         25
    Eigen::VectorXd qDot1, qDot2;
                                                                         26
    qDot1 = Jpinv * xdDot;
                                                                         27
    qDot2 = secondaryTaskGain *
                                                                         28
             ((Eigen::MatrixXd::Identity(7,7) - Jpinv*J) *
                                                                         29
             secondaryTaskFunctionGradient(q));
                                                                         30
    return qDot1 + qDot2;
                                                                         31
}
                                                                         32
                                                                         33
Eigen::VectorXd secondaryTaskFunctionGradient(Eigen::VectorXd q)
                                                                         34
{
                                                                         35
    Eigen::VectorXd qMid, qRanges;
                                                                         36
    qMid = 0.5 * (jointLimitsMax + jointLimitsMin);
                                                                         37
    qRanges = jointLimitsMax - jointLimitsMin;
                                                                         38
    return 2.0/7.0 * (q - qMid).cwiseQuotient(qRanges);
                                                                         39
                                                                          40
}
```

Listing 3.12: CartesianPositionController.cpp

Note that the velocity we command at every control loop is  $(\mathbf{x_d} - \mathbf{x})$ , that is a vector that points from the current end effector possition to the desired objective point. This means that the trajectory of the end effector will be a straight line that goes from the initial point to the objective point.

This simple method will be used as the base desired velocity for all the avoidance control methods.

# 3.3.2 Collision avoidance algorithm based on potential field methods and joint velocity constraints

The method presented in this section is an adaptation of the academic article "A Depth Space Approach to Human-Robot Collision Avoidance" [1], published by F. Flacco et al. in 2012. The paper presents an avoidance algorithm that takes depth images as inputs. In this work we have implemented the same functionality leveraging the perception via proximity sensing presented in section 3.2 instead. Moreover, the resolution of the equations is done via optimization, whereas in the original work it was done using a more complex algorithmic approach that leveraged inverse instantaneous kinematics explained in 3.3.1.5.

The main task of robot control usually deals with the motion of the end effector. The objective of the collision avoidance control algorithm is to maintain the original main task as long as collision can be avoided.

In consequence, a discrintion is made between a discrete set of points in the body of the robot and the end effector. The points in the **body** are taken to avoid the collision of any part of the robot with an object in its surroundings. On the one hand, the **end effector** is given special attention due to its aforementioned importance.

The end effector algorithm is based on a **potential field** approach, where artificially generated repulsive fields avoid getting closer to a possible collision. This algorithm is explained in detail in section 3.3.2.4.

The body control points are treated as cartesian constraints that are translated into **joint** velocity constraints. This constraints can be satisfied thanks to task redundancy, that is, there are different joint velocities that move the end effector at the same velocity. The authors state that if they had considered the same approach as for the end effector, they would have had to prioritize some points over the rest so that the problem turned feasible. However, doing this is problematic in their own words: giving priority to the end effector the collision safety of the points in the body would not be guaranteed, whereas not prioritizing it would result in random end effector trajectories

that would not accomplish the task. The obtainment of these joint velocity constraints is addressed in section 3.3.2.2.

# 3.3.2.1 Potential field method approach applied to the effector obstacle avoidance

Let  $\dot{\mathbf{x}}_{\mathbf{d}}$  be the desired velocity for the end effector. This velocity can be coming from different sources, but one example is the velocity that points to the next point in a cartesian position control 3.3.1.6. The location of the end effector is described by the position vector relative to the base frame  $\mathbf{x}_{ee}$ . In addition, the robot is surrounded by a set of m obstacles, represented by their position vectors relative to the base frame of the robot  $\mathbf{h}_{i}$ , for i = 1, 2, ..., m.

The algorithm presented in this section will adapt this velocity to be reactive to obstacles, thanks to the generation of an artificial repulsive vector  $\dot{\mathbf{x}}_{rep}$ . This repulsive vector will be used to generate the final control velocity  $\dot{\mathbf{x}}_{c}$ :

$$\mathbf{\dot{x}_c} = \mathbf{\dot{x}_d} - \mathbf{\dot{x}_{rep}}$$

In order to obtain  $\dot{\mathbf{x}}_{\mathbf{rep}}$ , firstly the distance vectors for all the obstacles are calculated:

$$d_i = h_i - x_{ee}$$

Among all these vectors, the smallest one is selected. This vector is denoted with  $\mathbf{d_{min}}$  and it is the only factor that affects direction and norm of  $\dot{\mathbf{x}}_{rep}$ .

$$\dot{\mathbf{x}}_{rep} = V \cdot \frac{1}{1 + e^{\alpha(2\frac{\|\mathbf{d}_{min}\|}{D} - 1)}} \cdot \frac{\mathbf{d}_{min}}{\|\mathbf{d}_{min}\|}$$
(3.9)

The direction of the vector is exactly the same as that of  $\mathbf{d_{min}}$ . The parameters that affect the shape of the curve that describes the norm of the repulsive vector are V, D and  $\alpha$ .

• V is the maximum value the norm of the repulsive vector can take, since  $\frac{1}{1+e^{\alpha(2\frac{\|\mathbf{d_{min}}\|}{D}-1)}}$  is bounded between 0 and 1.

- D is the minimum distance at which the norm of the repulsive vectors starts increasing.

  For distances greater than D the norm is 0.
- $\alpha$  defines the form of the curve. As  $\alpha$  tends to  $\infty$ , the shape of the curve tends to that of of a step function.

This interactive graph allows fine tuning of the parameters.

### 3.3.2.2 Joint velocity constraints to avoid collision of any point in the robot

The robot body must also avoid obstacles. For that purpose, each of the control points that describe the robot body will provide a set of joint velocity limits.

Let one of those control points be described by its position vector with respect to the base frame  $c_i$ . The set of obstacles is the same as in the previous section.

The procedure to obtain the joint velocity limits for a given control point  $\mathbf{c_j}$  starts in the same way as in the end effector, that is, finding the closest obstacle to  $\mathbf{c_j}$  and obtaining the corresponding distance vector  $\mathbf{d_{min}}$ .

Then f is calculated. This expression is identical to part of equation 3.9.

$$f = \frac{1}{1 + e^{\alpha(2\frac{\|\mathbf{d_{\min}}\|}{D} - 1)}}$$

This value is bounded between 0 and 1 and is close to 1 when the probability of hitting an object is high. The shape of the curve that defines f is exactly the same as that of the curve from the previous section.

Then, vector  $\mathbf{s}$  is calculated:

$$\mathbf{s} = \mathbf{J_{c_i}}^+ \frac{\mathbf{d_{min}}}{\|\mathbf{d_{min}}\|} f$$

 $\mathbf{J_{c_i}}$  is the partial jacobian of the kinematic chain that goes from the base to  $\mathbf{c_j}$ . Not all the joints necessarily influence the movement of that control point. For instance, if the control point is located in link 2 (see Denavit-Hartenberg notation in 3.3.1.1 for more information on link

numbering) only joints 1 and 2 affect the movement of that point. Therefore, the size of  $J_{c_i}$  and, in consequence, of s depend on the location of the specific control point we are talking about.

The *i*th value of  $\mathbf{s} \in \mathbb{R}^{n \times 1}$  represents the influence on the movement of that specific joint i has in moving  $\mathbf{c_j}$  as indicated by the vector  $\frac{\mathbf{d_{min}}}{\|\mathbf{d_{min}}\|}$ . The sign of  $s_i$  represents the direction of rotation of that joint that leads to that movement. If  $s_i > 0$ , moving that joint counterclockwise would contribute to a collision. On the other hand, if  $s_i < 0$  hte clockwise rotation of the joint is the one that has to be limited.

The amount by which joint velocities are limited depends on the value of f and the physical limits of the robot (joint velocity limits impose that  $-\dot{\mathbf{q}}_{\text{max}} \leq \dot{\mathbf{q}} \leq \dot{\mathbf{q}}_{\text{max}}$ , see 3.1.1):

if 
$$s_i \ge 0$$
,  $\dot{q}_{\max,body,i}^j = \dot{q}_{\max,i} (1 - f)$   
else  $\dot{q}_{\min,body,i}^j = -\dot{q}_{\max,i} (1 - f)$ 

Once  $\dot{\mathbf{q}}_{\min,\mathbf{body}}^{\mathbf{j}}$  and  $\dot{\mathbf{q}}_{\max,\mathbf{body}}^{\mathbf{j}}$  have been obtained for all control points, the final restrictions  $\dot{\mathbf{q}}_{\min,\mathbf{body}}$  and  $\dot{\mathbf{q}}_{\max,\mathbf{body}}$  need to be set as the the most restrictive.

$$\begin{split} \dot{q}_{\min,body,i} &= \max\{\dot{q}_{\min,body,i}^{\ j}\} \\ \dot{q}_{\max,body,i} &= \min\{\dot{q}_{\max,body,i}^{\ j}\} \end{split}$$

## 3.3.2.3 Imposing joint position, velocity and acceleration limits

The aforementioned approach doesn't take into account the physical limitations of the robot. Positions of the joints are limited, as mentioned in section 3.1.1. In addition, repulsive vectors can sometimes provoke unpredictable sudden changes in the motion of the robot. This can be avoided limiting the accelerations of the joints. The previous section has explained how joint velocity limitations can be used to avoid obstacles.

To limit joint positions, and accelerations, we assume that the restrictions that these can be written as follows:

$$\mathbf{q}_{\min} \leq \mathbf{q} \leq \mathbf{q}_{\max}$$
  $-\ddot{\mathbf{q}}_{\max} \leq \ddot{\mathbf{q}} \leq \ddot{\mathbf{q}}_{\max}$ 

Position and acceleration restrictions can be brought to the velocity level  $\dot{\mathbf{q}}$ . This is a necessary step since, as presented in the next section, the whole problem will be defined as a joint velocity optimization problem. In [41], they present a method to express these limits in the velocity level:

Position limits 
$$\frac{q_{\min,i} - q_i}{T} \le \dot{q}_i \le \frac{q_{\max,i} - q_i}{T}$$
Acceleration limits 
$$-\sqrt{2\ddot{q}_{\max,i} \left(q_i - q_{\min,i}\right)} \le \dot{q}_i \le \sqrt{2\ddot{q}_{\max,i} \left(q_{\max,i} - q_i\right)}$$
(3.10)

where  $q_i$  is the current position of joint i and the is T is the control period.

Finally, the most restrictive values between position, acceleration and the body algorithm restrictions need to be selected.

$$\dot{q}_{\min,i} = \max\left\{\frac{q_{\min,i} - q_i}{T}, \dot{q}_{\min,body,i}, -\sqrt{2\ddot{q}_{\max,i}\left(q_i - q_{\min,i}\right)}\right\} 
\dot{q}_{\max,i} = \min\left\{\frac{q_{\max,i} - q_i}{T}, \dot{q}_{\max,body,i}, \sqrt{2\ddot{q}_{\max,i}\left(q_{\max,i} - q_i\right)}\right\}$$
(3.11)

## 3.3.2.4 Setting up the optimization problem

Although this paper was not originally implemented using optimization, we believe that this is an easier and more intuitive way of describing the desired end effector velocity and the joint velocity descriptions.

Therefore, the purpose of this section is to define the optimization problem that takes the modified end effector velocity  $\dot{\mathbf{x_c}}$  obtained in section 3.3.2.4 and the restrictions obtained in section 3.3.2.2 as inputs and outputs the joint velocities  $\dot{\mathbf{q}}$ .

Firstly, we need to describe the objective function in 3.1. The optimal  $\dot{\mathbf{q}}^*$  that minimizes the objective function must be one that moves the end effector with the desired velocity  $\dot{\mathbf{x_c}}$ . This is the proposed form for the objective function (from now on we will denote  $\dot{\mathbf{x_c}}$  with simply  $\dot{\mathbf{x}}$ ):

$$f(\dot{\mathbf{q}}) = \underbrace{\frac{1}{2}(\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}})^{\mathbf{T}}(\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}})}_{\mathbf{1}} + \underbrace{\frac{\mu}{2}\dot{\mathbf{q}}^{\mathbf{T}}\dot{\mathbf{q}}}_{\mathbf{2}}$$

(1) This is the quadratic error between the robot's target velocity and its actual motion given the optimization variables  $\dot{\mathbf{q}}$ .

$$\frac{1}{2} \left( \dot{\mathbf{x}} - \mathbf{J} \dot{\mathbf{q}} \right)^{\mathrm{T}} \left( \dot{\mathbf{x}} - \mathbf{J} \dot{\mathbf{q}} \right) = \frac{1}{2} \| \dot{\mathbf{x}} - \mathbf{J} \dot{\mathbf{q}} \|^{2}$$

Observe above that  $\dot{\mathbf{x}}$  represents the desired motion, while  $\mathbf{J}\dot{\mathbf{q}}$  represents the actual motion determined by the jacobian  $\mathbf{J}$  presented in section 3.3.1.4. Therefore,  $\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}}$  is the difference between the desired and actual motions. Performing the actual matrix math on the first term gives us the scalar on the right in the equation above, which happens to be the square of the norm of the error, hence the quadratic error.

Note that the solution to the optimization problem  $\dot{\mathbf{q}}$  would be the result of doing  $\dot{\mathbf{q}} = \mathbf{J}^{\dagger}\dot{\mathbf{x}}$ , as explained in section 3.3.1.5 if no further constraints where applied to the optimization problem. That is,  $\dot{\mathbf{q}} = \mathbf{J}^{\dagger}\dot{\mathbf{x}}$  would be the smallest value vector to solve  $\dot{\mathbf{x}} = \mathbf{J}\dot{\mathbf{q}}$  and minimize the term  $||\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}}||$ .

(2) As mentioned in section 3.3.1.5, problems appear with the jacobian when near singularities.

This second term is used to solve this issue using the **Damped Least Squares** method [42] [43].

The value of  $\mu$  is calculated as follows, based in the manipulability measure (section 3.3.1.5):

$$w = \sqrt{\det(\mathbf{J}\mathbf{J}^{\top})}$$

$$\mu = \begin{cases} \mu_0 \left(1 - \frac{w}{w_0}\right)^2, & w < w_0 \\ 0, & w \ge w_0 \end{cases}$$

.

This expression needs to be expanded to meet the quadratic form of the objective function in 3.1.

$$\begin{split} f(\dot{\mathbf{q}}) &= \frac{1}{2} (\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}})^{\top} (\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}}) + \frac{\mu}{2}\dot{\mathbf{q}}^{\top}\dot{\mathbf{q}} \\ &= \frac{1}{2} \underbrace{(\dot{\mathbf{x}}^{\top} - (\mathbf{J}\dot{\mathbf{q}})^{\top})}_{(\mathbf{A} + \mathbf{B})^{\top} = \mathbf{A}^{\top} + \mathbf{B}^{\top}} (\dot{\mathbf{x}} - \mathbf{J}\dot{\mathbf{q}}) + \frac{\mu}{2}\dot{\mathbf{q}}^{\top}\dot{\mathbf{q}} \\ &= \frac{1}{2} [\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}} - \underbrace{\dot{\mathbf{x}}^{\top}\mathbf{J}\dot{\mathbf{q}} - (\mathbf{J}\dot{\mathbf{q}})^{\top}\dot{\mathbf{x}}}_{\mathbf{Both \ equivalent \ to:}} + (\mathbf{J}\dot{\mathbf{q}})^{\top}(\mathbf{J}\dot{\mathbf{q}})] + \frac{\mu}{2}\dot{\mathbf{q}}^{\top}\dot{\mathbf{q}} \\ &= \frac{1}{2} (\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}} - 2\dot{\mathbf{x}}^{\top}\mathbf{J}\dot{\mathbf{q}} + \underbrace{\dot{\mathbf{q}}^{\top}\mathbf{J}^{\top}}_{\mathbf{A}^{\top}}\mathbf{J}\dot{\mathbf{q}}) + \frac{1}{2}\dot{\mathbf{q}}^{\top}\mu\mathbf{I}\dot{\mathbf{q}} \\ &= \frac{1}{2} (\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}} - 2\dot{\mathbf{x}}^{\top}\mathbf{J}\dot{\mathbf{q}} + \underbrace{\dot{\mathbf{q}}^{\top}\mathbf{J}^{\top}}_{\mathbf{A}^{\top}}\mathbf{J}\dot{\mathbf{q}}) + \frac{1}{2}\dot{\mathbf{q}}^{\top}\mu\mathbf{I}\dot{\mathbf{q}} \\ &= \frac{1}{2}\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}} - \dot{\mathbf{x}}^{\top}\mathbf{J}\dot{\mathbf{q}} + \frac{1}{2}\dot{\mathbf{q}}^{\top}(\mathbf{J}^{\top}\mathbf{J} + \mu\mathbf{I})\dot{\mathbf{q}} \\ &= \frac{1}{2}\dot{\mathbf{q}}^{\top}\left(\mathbf{J}^{\top}\mathbf{J} + \mu\mathbf{I}\right)\dot{\mathbf{q}} - \dot{\mathbf{x}}^{\top}\mathbf{J}\dot{\mathbf{q}} + \frac{1}{2}\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}} \end{split}$$

 $\frac{1}{2}\dot{\mathbf{x}}^{\top}\dot{\mathbf{x}}$  is a constant w.r.t. the optimization variables in  $\dot{\mathbf{q}}$ , so even though it will change the inal value of the objective function, it does not affect  $\dot{\mathbf{q}}^*$ . Since the resulting  $\dot{\mathbf{q}}^*$  is the only important output of the optimization process regarding our application, we can get rid of this term, resulting in the final expression:

$$f(\dot{\mathbf{q}}) = \frac{1}{2} \dot{\mathbf{q}}^{\top} \left( \mathbf{J}^{\top} \mathbf{J} + \mu \mathbf{I} \right) \dot{\mathbf{q}} - \dot{\mathbf{x}}^{\top} \mathbf{J} \dot{\mathbf{q}}$$

Comparing this expanded expression to 3.1, we have that:

$$\mathbf{Q} = \mathbf{J}^{\top} \mathbf{J} + \mu \mathbf{I}$$
$$\mathbf{c}^{\top} = -\dot{\mathbf{x}}^{\top} \mathbf{J}$$

As stated in section 3.1.4, the problem needs to be convex in order to be able to find a global optimal solution in a minimum amount of time. This will only be the case if we can verify  $\mathbf{Q}$  will always be semi-positive definite, or what is the same, its eigenvalues will be non-negative.

**Theorem 8.** Let  $\mathbf{A} \in \mathbb{R}^{m \times n}$ . Then,  $\mathbf{A}\mathbf{A}^{\top}$  is a positive semi-definite matrix.

**Theorem 9.** The sum of any two (semi)positive definite matrices of the same size is (semi)positive definite.

 $\mu$ **I** is semi-positive definite because it is a diagonal matrix with non-negative coefficients and the eigenvalues of a diagonal matrices are the coefficients themselves.  $\mathbf{J}^{\mathsf{T}}\mathbf{J}$  because of theorem 8. Then, by theorem 9 we know that **Q** is semi-positive definite.

On the other hand, the restrictions presented in section 3.3.2.2 could be rewritten as 4 linear equations to meet the structure in equation 3.1. However, Quadratic Programming optimization algorithms can deal more efficiently with a different kind of constraint for this specific kind of restrictions, where only upper and lower boundaries for the optimization variables are required. This type of constraints are called **box constraints** and can be expressed as:

$$\dot{\mathbf{q}}_{\min} \leq \dot{\mathbf{q}} \leq \dot{\mathbf{q}}_{\max}$$

where the components of  $\dot{\mathbf{q}}_{\min}$  and  $\dot{\mathbf{q}}_{\max}$  are calculated with the expression 3.10.

Once the end effector velocity is set up in the objective funtion and the restrictions are applied, the resolution of the Quadratic Programming problem presented in 3.1 returns the best joint velocities that solve all the specifications presented in this section.

### 3.3.3 Alternative approach to collision avoidance based on linear inequalities

In this section we implement the academic article "Collision Avoidance with Proximity Servoing for Redundant Serial Robot Manipulators" [2], published by Y. Ding and U. Thomas in May 2020. In their approach box constraints are reserved to the task of maintaining the limits in joint positions, velocities and accelerations. The hierarchy between the algorithms applied to the end effector and the rest of the body is not used any more. Control points are calculated dynamically (section 3.3.3.1). The commanded velocity is not modified by a repulsive vector. Instead, each obstacle point defines a restriction on the movement of the closest point in the kinematic chain (section 3.3.3.2). An extra restriction makes the overall distance to the obstacles increase over time

(section 3.3.3.3).

# 3.3.3.1 Assigning a control point in the kinematic chain of the robot to each of the obstacles

In this section control points are not predefined as in section 3.3.2. All the obstacle points are dynamically assigned a point in the robot's kinematic chain instead. The point is chosen to be the one closest to the obstacle.

The method implemented to obtain the closest point is presented in [44]. These are the steps proposed:

- (1) Let the robot be represented by a series of segments defined by pairs of points. Let P be the obstacle point to which we want to assign the closest point in the robot.
- (2) For each segment that goes from A to B:
  - (a) Write the vector between P and a point that is t from A to B. (When t = 0, the point is A; when t = 1, the point is B.)

$$f(t) = (1 - t)A + tB - P (3.12)$$

- (b) Now let  $g(t) = ||f(t)||^2$ , which is norm of that vector squared. We want to find the value of t that minimizes g(t).
- (c) Develop expression 3.12,

$$g(t) = ||f(t)||^{2}$$

$$= ((1-t)A + tB - P)^{T} \cdot (1-t)A + tB - P$$

$$= (t(B-A) + A - P)^{T} \cdot (t(B-A) + (A-P))$$

Let v = B - A and u = A - P,

$$g(t) = ||f(t)||^{2}$$

$$= (tv + u)^{T} \cdot (tv + u)$$

$$= t^{2}||v||^{2} + 2t(v \cdot u) + ||u||^{2}$$

(d) Calculate g'(t),

$$g'(t) = 2t||v||^2 + 2(v \cdot u) = 2t(v \cdot v) + 2(v \cdot u). \tag{3.13}$$

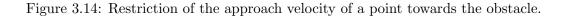
(e) Set to zero and solve to get the value of t that minimizes g(t). This particular function has only one minimum, so if you find a critical point you know it is a minimum value.

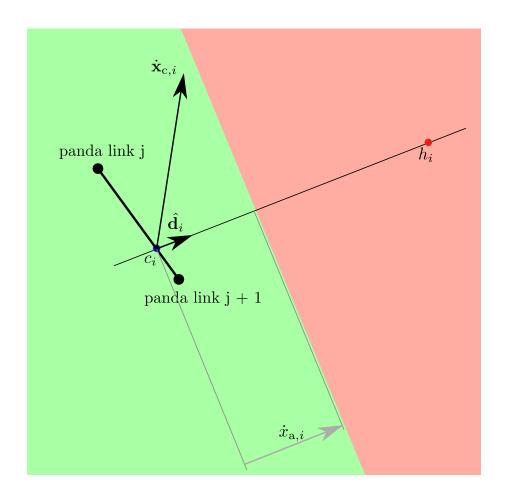
$$t = -\frac{v \cdot u}{v \cdot v}.$$

- (f) Once the value of t is computed, if it is between 0 and 1, then the closest point is (1-t)A+tB. If it is not, A or B are the closest points, depending on which f(0) or f(1) is the smaller.
- (3) From the list of points associated to each of the segments, choose the one corresponding to the minimum distance.

## 3.3.3.2 Limiting the approach velocity to the obstacles

The expression described in this section will restrict the approach velocity of the point assigned in section 3.3.3.1 towards the obstacle. The restriction is described graphically in figure 3.14.



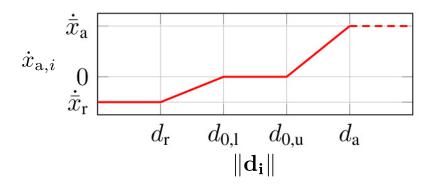


Given a position of an obstacle  $h_i$ , the orthogonal projection of the final velocity  $\dot{\mathbf{x}}_{c,i}$  will be limited by a certain amount  $\dot{x}_{a,i}$ . Every  $\dot{\mathbf{x}}_{c,i}$  whose arrowhead is within the green area will be permitted.

Moreover, if the value of  $\dot{x}_{a,i}$  is negative, then the red boundary between the green and red areas will be moved to the opposite site of  $\hat{\mathbf{d}}_i$ , forcing a repulsive action.

Consequently, the value of  $\dot{x}_{a,i}$  defines how the behaviour of a given point is restricted. In [2] they propose a piecewise defined function to calculate the value, based on the distance at which the obstacle is located with respect to the robotic arm, shown in figure 3.15.

Figure 3.15: Determination of  $\dot{x}_{a,i}$  as a function of  $\|\mathbf{d}_{\mathbf{i}}\|$ .



Formally speaking, the restriction for one obstacle is formulated as follows:

$$\hat{\mathbf{d}}_i^{\top}\dot{\mathbf{x}}_{\mathrm{c},i} = \hat{\mathbf{d}}^{\top}\mathbf{J}_{\mathrm{p}_{\mathrm{c},i}}\dot{\mathbf{q}} \leq \dot{x}_{\mathrm{a},i}$$

This defines one linear inequation, where  $\hat{\mathbf{d}}^{\top}\mathbf{J}_{\mathrm{pc},i} \in \mathbb{R}^{1\times n}$  is the coefficients vector,  $\dot{\mathbf{q}} \in \mathbb{R}^{n\times 1}$  are the unknowns and  $\dot{x}_{\mathrm{a},i} \in \mathbb{R}$  is the right side of the inequation. As one obstacle defines one new restriction, for m obstacle points, m rows will be added to elements  $\mathbf{A}$  and  $\mathbf{b}$  in the Quadratic Programming problem definition in 3.1.

It has to be noted that the restrictions for several points can be contradictory sometimes. This turns the optimization unfeasible. When this happens, the repulsive actions are set to 0 and the optimization is run again.

#### 3.3.3.3 Increasing the overall distance to the obstacles over time

In this section a new restriction is described, which forces an overall increase over time of the distance between the obstacles and the robot. This restriction complements the one presented in section 3.3.3.2.

In terms of mathematical analysis, a continuous function is increasing in time when its

derivative with respect to time is positive. By the chain rule, this is how the derivative of a single distance norm with respect to time would be calculated:

$$\frac{d\|\mathbf{d_i}\|}{dt} = \frac{\partial \|\mathbf{d_i}\|}{\partial \mathbf{q}} \frac{d\mathbf{q}}{dt} = \nabla_{\mathbf{q}} \|\mathbf{d_i}\| \dot{\mathbf{q}}$$

As what we want is an overall increase of the distance instead of increasing just one distance, a weight based formulation can be employed:

$$\begin{bmatrix} w_1 & \cdots & w_m \end{bmatrix} \begin{bmatrix} \frac{d\|\mathbf{d_1}\|}{dt} \\ \cdots \\ \frac{d\|\mathbf{d_m}\|}{dt} \end{bmatrix} = \begin{bmatrix} w_1 & \cdots & w_m \end{bmatrix} \begin{bmatrix} \nabla_{\mathbf{q}} \|\mathbf{d_1}\| \\ \cdots \\ \nabla_{\mathbf{q}} \|\mathbf{d_m}\| \end{bmatrix} \dot{\mathbf{q}} \ge 0$$

The weights are set to be indirectly proportional to the distance, so that closest obstacles have highest priority:

$$w_i = \frac{1}{\|\mathbf{d_i}\|}$$

This constraint adds one last row to **A** and **b**.

# Chapter 4

#### Results

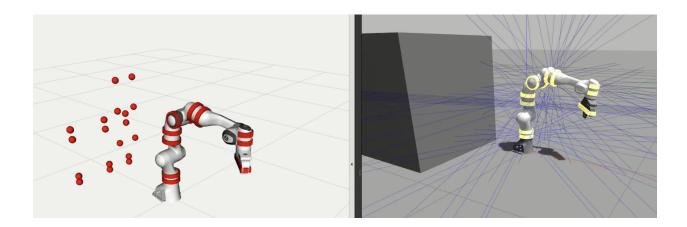
In this section we present the results of the implementation of all the elements presented in chapter 3.

# 4.1 Perception

The culmination of the proximity sensor transformation explained in section 3.2, in addition to the work done in calibration by the calibration group in the HIRO Lab, led by Kandai Watanabe, will allow to the robot to sense its surroundings.

In simulation, we show below that proximity sensors placed in the robot body (marked in red in figure 3.9) can detect objects in simulation. In figure 4.1, rviz is placed on the left and the simulation in Gazebo on the right. A black box is moved around in Gazebo and the robot's perception, result of the transformation algorithm proposed in this work, is seen in rviz.

Figure 4.1: Final visualization of the perceived points in rviz.



This video shows the same result in movement. Note that the perception is instantaneous. Gazebo updates the position of the box when the left button of the mouse is released and this is the precise time that the old red spheres are deleted from perception and the new ones are created.

The update rate achieved in simulation has been 100 Hz. In practical applications the rate is limited by the specific sensor's capabilities, as opposed to the fact that the limiting factor is the computer's processing time for depth sensors, sensors that traditionally have been use for the obstacle avoidance control.

The buffer size in the demonstration is 10. At  $100\,\mathrm{Hz}$ , this buffer size means it holds the data for  $100\,\mathrm{ms}$ .

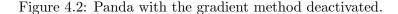
# 4.2 End effector position control using the general solution of Instantaneous Forward Kinematics

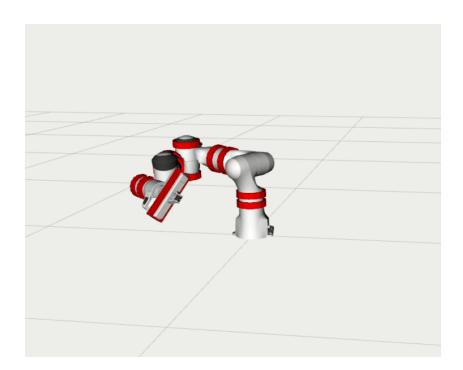
Cartesian position control, final code has been shown in section 3.3.1.6, was a necessary step to implement the rest of the avoidance algorithms. We have used many elements implemented in this controller as a foundation and to inform the movement of all subsequent controllers.

This video presents the control in action. The desired trajectory is composed of 4 points that pertain to a circumference in the x = 0.5 m plane. This video presents the experiment that will be

conducted for a first evaluation of the avoidance algorithm. The red point represents an obstacle and obviously it is not avoided in the case of this simple controller.

The gradient of the objective function that represents how close the joints are with respect to their mid range value, that goes into the second term of equation 3.8, is a key element in this controller. If this them was omitted, weird joint configurations can be reached. As shown in figure 4.2 and This video, starting from a good initial position everything seems to work well in the beginning. However, at the second half of the video the arm reaches an undesired configuration in which it is near to hit the ground. This happens because of all posible joint velocities the minimum is being selected and this does not always involve the best solution. For a more detailed explanation on how the gradient works see section 3.3.1.5.





Another important result is that, in listing 3.12, if the threshold that decides if the main position control loop is complete is too small, the sensor update interval is not fast enough to ensure

that level of precision. The velocity commanded to the end effector also needs to be considered, since for higher velocities a greater amount of distance is covered in the same amount of time. For example, when this threshold is set to less than  $1\,\mathrm{cm}$  for an end effector speed of  $0.35\,\mathrm{m/s}$ , the final part of the trajectory sometimes becomes sloppy.

This threshold method is not the best one to solve the problem of trajectory control. A more advanced control method has been developed for the future development of the project. In contrast, it is a valid method for an initial checking of the behavior of the avoidance algorithms.

# 4.3 Collision avoidance algorithm based on potential field methods and joint velocity constraints

The approach explained in section 3.3.2 divided the avoidance control into two parts. One for the end effector and another one for the rest of the robot's body. We will demonstrate how this approach works in two parts. Firstly, the end effector algorithm will be tested independently. Then, the experiment presented in section 4.2

In this video we show an example of the repulsive vector modifying the trajectory of the end effector. The experiment is simple: the end effector is commanded an iterative movement between two points in a line parallel to the x axis. An obstacle is placed in the trajectory.

The result is that the repulsive vector modifies the trajectory in the beginning and successfully moves around the object. When moving torwards the second objective the end effector stops when the desired velocity and the repulsive vector are exactly the same but with opposite directions. This represents a local minimum of the problem, since the desired position is actually reachable while avoiding the obstacle.

In this other video, the repulsive method is combined with the joint restriction method and tested with the aforementioned experiment (following a trajectory between 4 points). The obstacle is now successfully avoided. However, it can be observed how the joint restrictions sometimes limit movements that do not have to be limited.

Acceleration limits (section 3.3.2.3) have also been proven to be an important part of the

correct behavior of the control. In the process of implementation, fast changes in the repulsive vector's direction resulted in jerky movements. Limiting acceleration has been proven to be a suitable solution to this fact.

The methods demonstrated in the next sections will improve this limitation imposed by the restrictions that prevent collision.

#### 4.4 Alternative approach to collision avoidance based on linear inequalities

The approach explained in section 3.3.3 is different in two main ways with respect to Flacco. Control points where dynamically calculated for every obstacle point. The original desired end effector velocity was maintained as long as possible, as opposed to using repulsive vectors.

In this video the behaviour of the controller is shown. The first time the robot arm approaches the obstacle the avoidance is satisfactory. The second time something different happens. The movement torwards the next trajectory point is not allowed by the restrictions. The reason why this takes place is obvious if we analyze the second restriction (section 3.3.3.3). As we explained there, an overall increase in the distance to the obstacles is pursued by that restriction. In this case, as there is one single obstacle, it is the distance to that obstacle that is forced to increase. That is why the robot arm is not allowed to advance in the trajectory, there is no way to do so while satisfying the restriction.

On the other hand, another anomaly can be observed in the movement of the robot. After avoiding the obstacle for the first time, the position of the arm stays in the position adopted in order to avoid the obstacle. This effect was also observable in the previous control approach. What makes the robot approach the ground in figure 4.2 is the reason why this happens. The general solution shown in equation 3.8 and the gradient that minimizes the distance from the joint angles to their mid ranges are not being used in this section. In fact, the optimization selects the minimum norm joint velocity. This is exactly what happened if the second term of the general solution was deleted.

In addition, acceleration limitation is also very important in this section. The behaviour

thanks to these limitations is more predictable and safer.

#### 4.5 Improvements to the collision avoidance control

The restriction that causes the undesired behaviour in the previous test can be deleted. We have shown its implications are not convenient. Furthermore, we think that the restriction of the approach velocity is enough for if exploited properly. In section 3.3.3.2, we explained why the form of these restrictions are a suitable way of describing the avoidance problem. They allow setting up a repulsive action for any point in the robot when needed. This implies that the implications of the repulsive vectors applied to the end effector in section 3.3.2 can be extended to the rest of the body.

The original problem of maintaining the task as long as it is possible is also better described by this formulation, since the commanded velocity will be the original task velocity. That is, no repulsive vectors will modify the original task velocity. Since this goes in the optimization function, when it is not possible to maintain the original velocity, the closest possible velocity will be commanded.

In conclusion, the control proposed in this work is similar to the one presented in section 3.3.3, but it is a more fundamental formulation of the original description of the problem.

The graph used to model the repulsive actions in the original publication (figure 3.15) has been enhanced for a more natural behaviour (figure 4.3). See this interactive graph for a deeper understanding of the parameters. Instead of using a linear graph we propose using exponential functions. In addition we propose that there are two thresholds for making decisions: the distance at which the control starts taking into account the obstacle:  $d_{noticeable}$  and the distance at which repulsive actions start to be considered  $d_{critical}$ .

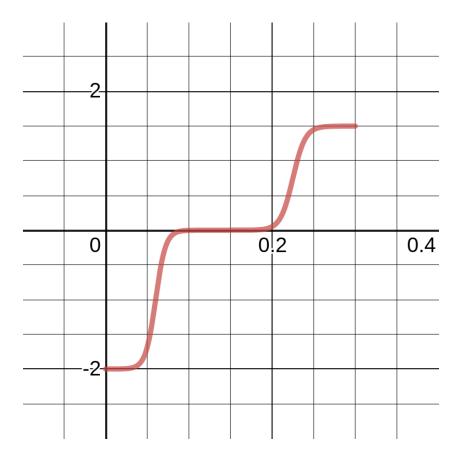


Figure 4.3: Enhanced determination of  $\dot{x}_{a,i}$  as a function of  $\|\mathbf{d}_{\mathbf{i}}\|$ .

The result of this enhanced approach can be observed in this video.

# 4.6 Collision avoidance control in the real robot

All the implementations and experiments described in the document so far have been done in simulation. The final will be to verify all the control algorithms work as well in the real Franka Panda Emika.

This video shows the same experiment carried on in the last section, but in real life.

The perception algorithm explained in 3.2 has not been tested. The development of the artificial skin has been parallel to this work and as of the day of completion, the electronics of the sensors are in their third version and waiting to be tested. The kinematic calibration method, in contrast, has been successfully tested using individual *IMU* sensors.

The obstacle in the video has been placed manually via de command line tool rostopic pub.

We show the location of the point with our hand.

#### Chapter 5

#### Conclusions

Human-Robot Interaction is the field of robotics dedicated to the understanding, design, and evaluation of robotic systems for use by or with humans. Safety is one of the most important aspects this field will have to deal with in the years to come. In this work, pre-contact safety is adressed through the use of a artificial skin that is being developed in the HIRO Lab. To be more specific, the artificial skin integrates a set of proximity sensors and has the potential to cover all the links of any robotic arm.

Proximity sensor readings are transformed into 3D data, which will later inform the control algorithms. An important step in this transformation is the kinematic calibration developed by another team in the HIRO Lab.

The main objective has been to adapt and integrate previous literature to the collision avoidance control through proximity sensors. Two different approaches have been implemented.

On the one hand, "A Depth Space Approach to Human-Robot Collision Avoidance" [1], published by F. Flacco et al. in 2012, makes use of two different methods to solve the problem of avoidance control. A repulsive field method is used to modify the end effector's velocity and. For the rest of the robot's body, a set of control points are used to avoid collisions. Each of the control points generates a set of joint velocity restrictions that ensures the safety for all the points that surround that point.

On the other hand, in "Collision Avoidance with Proximity Servoing for Redundant Serial Robot Manipulators" [2], published by Y. Ding and U. Thomas in May 2020, the end effector

velocity is not modified. The optimization algorithm will try to minimize the quadratic error between the desired task velocity and the the final commanded velocity, but the minimization will be subject to some constraints. These constraints ensure the safety of motion. For the generation of the constraints each obstacle is assigned a control point on the robotic arm. Then, the approach velocity of each of the control points to their respective obstacle is limited. The same formulation can also be used to force a repulsive movement. In addition, one last restriction forces an weighted increase in the overall distance to obstacles.

The implementations of these two controllers form, with the addition of a third controller that improves upon both of them, a framework for the comparison and improvement of the current state of art in safe robot controllers.

As far as future work is concerned, the first thing will be to design an experiment in simulation that allows a better evaluation of the different control methods. The choice of suitable quantitative tools will also be of great importance for this evaluation. This is a list of already implemented and future ideas for improvement:

- Build on the controller shown in section 4.5.
- Improve and test the graph shown in figure 4.3 and compare it against the original piecewise graph (figure 3.15).
- Integrate the second term of the general equation and the gradient that minimizes the distance to the mid-range of the joints in the optimization approach.
- Make use of a human sensor that will be integrated in the skin to avoid show alternative behaviours when obstacles are human beings.
- Account for the thickness of the robotic arm for a more accurate response to distance.
   Right now, distances are measured from obstacles to the dynamic control points located in the axis of the robotic limbs.

#### **Bibliography**

- [1] Fabrizio Flacco, Torsten Kröger, Alessandro De Luca, and Oussama Khatib. A depth space approach to human-robot collision avoidance. In <u>2012 IEEE International Conference on</u> Robotics and Automation, pages 338–345. IEEE, 2012.
- [2] Yitao Ding and Ulrike Thomas. Collision avoidance with proximity servoing for redundant serial robot manipulators.
- [3] iRobot. Roomba vacuuming robot, 2020. https://www.irobot.com/.
- [4] thermomix. thermomix cooking robot, 2020. https:
  //www.thermomix.com/tm6/?utm\_source=google&utm\_medium=cpc&
  utm\_term=thermomix&utm\_campaign=brand&utm\_content=ETA&gclid=
  Cj0KCQjwjer4BRCZARIsABK4QeWxAdizt1-6N-cJk1-wB0jGrsYqi0lptmd7M8yAm1P-vG1YVJzZtyEaAkGjEALw\_wcB.
- [5] Diligent Robots. Moxi hospital robot assistant, 2020. https://diligentrobots.com/moxi.
- [6] Avatarmind. ipal robot family, 2020. https://www.ipalrobot.com/.
- [7] G Westling and RS Johansson. Factors influencing the force control during precision grip. Experimental brain research, 53(2):277–284, 1984.
- [8] Jan BF van Erp and Hendrik AHC van Veen. Touch down: the effect of artificial touch cues on orientation in microgravity. Neuroscience Letters, 404(1-2):78–82, 2006.
- [9] Ravinder S Dahiya, Giorgio Metta, Maurizio Valle, and Giulio Sandini. Tactile sensingfrom humans to humanoids. IEEE transactions on robotics, 26(1):1–20, 2009.
- [10] S. Tian, F. Ebert, D. Jayaraman, M. Mudigonda, C. Finn, R. Calandra, and S. Levine. Manipulation by feel: Touch-based control with deep predictive models. In <u>2019 International</u> Conference on Robotics and Automation (ICRA), pages 818–824, 2019.
- [11] Achu Wilson, Shaoxiong Wang, Branden Romero, and Edward Adelson. Design of a fully actuated robotic hand with multiple gelsight tactile sensors. arXiv preprint arXiv:2002.02474, 2020.
- [12] Giorgio Metta, Lorenzo Natale, Francesco Nori, Giulio Sandini, David Vernon, Luciano Fadiga, Claes Von Hofsten, Kerstin Rosander, Manuel Lopes, José Santos-Victor, et al. The icub humanoid robot: An open-systems platform for research in cognitive development. <u>Neural</u> networks, 23(8-9):1125-1134, 2010.

- [13] Alexander Schmitz, Perla Maiolino, Marco Maggiali, Lorenzo Natale, Giorgio Cannata, and Giorgio Metta. Methods and technologies for the implementation of large-scale robot tactile sensors. IEEE Transactions on Robotics, 27(3):389–400, 2011.
- [14] E. Dean-Leon, K. Ramirez-Amaro, F. Bergner, I. Dianov, P. Lanillos, and G. Cheng. Robotic technologies for fast deployment of industrial robot systems. In <u>IECON 2016 42nd Annual</u> Conference of the IEEE Industrial Electronics Society, pages 6900–6907, 2016.
- [15] P. Mittendorfer and G. Cheng. Humanoid multimodal tactile-sensing modules. <u>IEEE</u> Transactions on Robotics, 27(3):401–410, 2011.
- [16] Philipp Mittendorfer, Eiichi Yoshida, and Gordon Cheng. Realizing whole-body tactile interactions with a self-organizing, multi-modal artificial skin on a humanoid robot. Advanced Robotics, 29(1):51–67, 2015.
- [17] Wenzhen Yuan, Siyuan Dong, and Edward H Adelson. Gelsight: High-resolution robot tactile sensors for estimating geometry and force. Sensors, 17(12):2762, 2017.
- [18] Akihiko Yamaguchi and Christopher G Atkeson. Implementing tactile behaviors using fingervision. In 2017 IEEE-RAS 17th International Conference on Humanoid Robotics (Humanoids), pages 241–248. IEEE, 2017.
- [19] Alex Alspach, Kunimatsu Hashimoto, Naveen Kuppuswarny, and Russ Tedrake. Soft-bubble: A highly compliant dense geometry tactile sensor for robot manipulation. In <u>2019 2nd IEEE</u> International Conference on Soft Robotics (RoboSoft), pages 597–604. IEEE, <u>2019</u>.
- [20] Yitao Ding, Felix Wilhelm, Leonhard Faulhammer, and Ulrike Thomas. With proximity servoing towards safe human-robot-interaction. In 2019 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pages 4907–4912. IEEE, 2019.
- [21] Dong Hai Phuong Nguyen, Matej Hoffmann, Alessandro Roncone, Ugo Pattacini, and Giorgio Metta. Compact real-time avoidance on a humanoid robot for human-robot interaction. In Proceedings of the 2018 ACM/IEEE International Conference on Human-Robot Interaction, pages 416–424, 2018.
- [22] Franka Emika. Franka emika panda robot and interface specifications, 2020. https://frankaemika.github.io/docs/control\_parameters.html#.
- [23] Ayssam Elkady and Tarek Sobh. Robotics middleware: A comprehensive literature survey and attribute-based bibliography. Journal of Robotics, 2012, 05 2012.
- [24] Apex.AI. Apex.OS  $^{\rm R}$ , 2020. https://www.apex.ai/apex-os.
- [25] Open Source Robotics Foundation. Gazebo simulator, 2020. http://gazebosim.org/.
- [26] David Hershberger, David Gossow, and Josh Faust. rviz, 2020. http://wiki.ros.org/rviz.
- [27] Orocos kdl, 2020. https://www.orocos.org/wiki/orocos/kdl-wiki.
- [28] Eigen, 2020. http://eigen.tuxfamily.org.
- [29] ALGLIB Project. Alglib, 2020. https://www.alglib.net/.

- [30] Open Source Robotics Foundation. Gazebo plugins, 2020. http://gazebosim.org/tutorials?tut=ros\_gzplugins#Pluginsavailableingazebo\_plugins.
- [31] Josh Faust Dave Hershberger, David Gossow. rviz marker display type, 2020. http://wiki.ros.org/rviz/DisplayTypes/Marker.
- [32] Richard S Hartenberg and Jacques Denavit. A kinematic notation for lower pair mechanisms based on matrices. Journal of applied mechanics, 77(2):215–221, 1955.
- [33] justagist. Franka emika panda robot description, 2020. https://github.com/justagist/franka\_panda\_description.
- [34] Robot state publisher ros package, 2020. wiki.ros.org/robot\_state\_publisher.
- [35] José María Goicolea Ruigómez. Curso de Mecánica. 2010.
- [36] David E. Orin and William W. Schrader. Efficient Computation of the Jacobian for Robot Manipulators. The International Journal of Robotics Research, 3(4):66–75, 1984.
- [37] Bruno Siciliano. Kinematic control of redundant robot manipulators: A tutorial. <u>Journal of intelligent and robotic systems</u>, 3(3):201–212, 1990.
- [38] Jim Hefferon. Linear algebra, 3rd.
- [39] Tsuneo Yoshikawa. Dynamic manipulability of robot manipulators. <u>Transactions of the Society</u> of Instrument and Control Engineers, 21(9):970–975, 1985.
- [40] Alain Liegeois et al. Automatic supervisory control of the configuration and behavior of multibody mechanisms. <u>IEEE transactions on systems, man, and cybernetics</u>, 7(12):868–871, 1977.
- [41] Fabrizio Flacco, Alessandro De Luca, and Oussama Khatib. Motion control of redundant robots under joint constraints: Saturation in the null space. In <u>2012 IEEE International</u> Conference on Robotics and Automation, pages 285–292. IEEE, 2012.
- [42] Yoshihiko Nakamura and Hideo Hanafusa. Inverse kinematic solutions with singularity robustness for robot manipulator control. 1986.
- [43] Charles W Wampler. Manipulator inverse kinematic solutions based on vector formulations and damped least-squares methods. <u>IEEE Transactions on Systems, Man, and Cybernetics</u>, 16(1):93–101, 1986.
- [44] John Hughes (https://math.stackexchange.com/users/114036/john-hughes). Find a point on a line segment which is the closest to other point not on the line segment. Mathematics Stack Exchange. https://math.stackexchange.com/q/2193733.
- [45] Sami Haddadin, Alessandro De Luca, and Alin Albu-Schäffer. Robot collisions: A survey on detection, isolation, and identification. <u>IEEE Transactions on Robotics</u>, 33(6):1292–1312, 2017.
- [46] S. Haddadin, A. Albu-Schaffer, A. De Luca, and G. Hirzinger. Collision detection and reaction: A contribution to safe physical human-robot interaction. In <u>2008 IEEE/RSJ International</u> Conference on Intelligent Robots and Systems, pages 3356–3363, 2008.
- [47] Numpy, 2020. https://numpy.org/.