

Homework 5

I pledge my honor that I have abided by the Stevens Honor System - esp

7.71 - Sadness & Spending

(a) The use of t -procedures could be appropriate because there is no apparent skewness/outliers. However, we don't know if it's normal which we should keep in mind

(b)

	Sample Size	Mean	Standard Dev
Neutral	14	0.571	0.73
Sad	17	2.12	1.24

(c) μ_1 = mean of Neutral Group $\left\{ \begin{array}{l} H_0: \mu_1 = \mu_2 \\ \mu_2 = \text{mean of Sad Group} \end{array} \right. H_a: \mu_1 \neq \mu_2$

(d) $\alpha = 0.05$ level \rightarrow Test Stat: $\frac{0.571 - 2.118}{\sqrt{\left(\frac{0.73^2}{14}\right) - \left(\frac{1.24^2}{17}\right)}} = -4.3$
degrees of freedom = 26

p-value = 0.0001 [We see a big difference in mean and there p-val is much smaller than sig-level 0.05
Therefore, reject H_0 & accept H_a]

(e) 95% Confidence Int

$$\rightarrow (0.571 - 2.12) \pm \sqrt{\frac{0.73^2}{14} - \frac{1.24^2}{17}} \times t_{42} = (-2.285, -8.08)$$

7.89 - Breast-Feeding vs Baby Formula

(a) μ_1 = breast-feed group $\left\{ \begin{array}{l} H_0: \mu_1 = \mu_2 \\ \mu_2 = \text{baby formula group} \end{array} \right. H_a: \mu_1 > \mu_2$

We get p-val = 0.053 so based on the significant level there's not a higher level if the level is 0.05. H_0 is not rejected.

$$s_{\text{comb}} = \sqrt{\frac{22 \times (1.7)^2 + 18 \times 3.24}{40}} = 1.746$$

$$\leftarrow \{ 1.66 = t = \frac{13.3 - 12.4}{1.746 \cdot \sqrt{\frac{1}{23} + \frac{1}{19}}} \}$$

(b) $(-0.202, 2.002)$

(c) We assume ~~it is~~ the samples involved are normal and simple random samples (SRS).

7.102 - Comparison of Standard Deviations

(a) $F = 2.6$

(b) $F(15, 10, 0.05) = 2.845$

(c) The 2 population standard deviations are equal

7.122 - Two-sample t test

(a) $\bar{x}_1 = 49.69$, $s_1 = 2.318$, $\bar{x}_2 = 50.545$, $s_2 = 1.924$
 degrees of freedom = 17, $t = -0.9$, $p\text{-val} = 0.3831$

(b) ~~$p\text{-val} = 0.3831$~~ $\bar{d} = -0.853$, $s = 1.2691$, $t = -2.13$
 $p\text{-val} = 0.0625$

(c) The p-values, t-stat are different resulting in accidental acceptance/rejection of H_0

8.71 - Gender Bias in Textbook

(a) Proportion female = 0.8, $SE_{\text{female}} = 0.052$

Proportion male = 0.39, $SE_{\text{male}} = 0.0425$

(b) 90% Conf $\rightarrow (0.2960, 0.5161)$

The mean difference of male to female is between 0.2960 - 0.5161.

(c) $H_0: \text{prop}_f = \text{prop}_{\text{male}}$, $p = 0.5101$

Standard Error = 0.0778

$$z = \frac{\text{prop}_{\text{female}} - \text{prop}_{\text{male}}}{0.0778} = 5.217$$

We reject null hypo H_0 because there is a big difference $P(z > 5.217) \approx 0$.