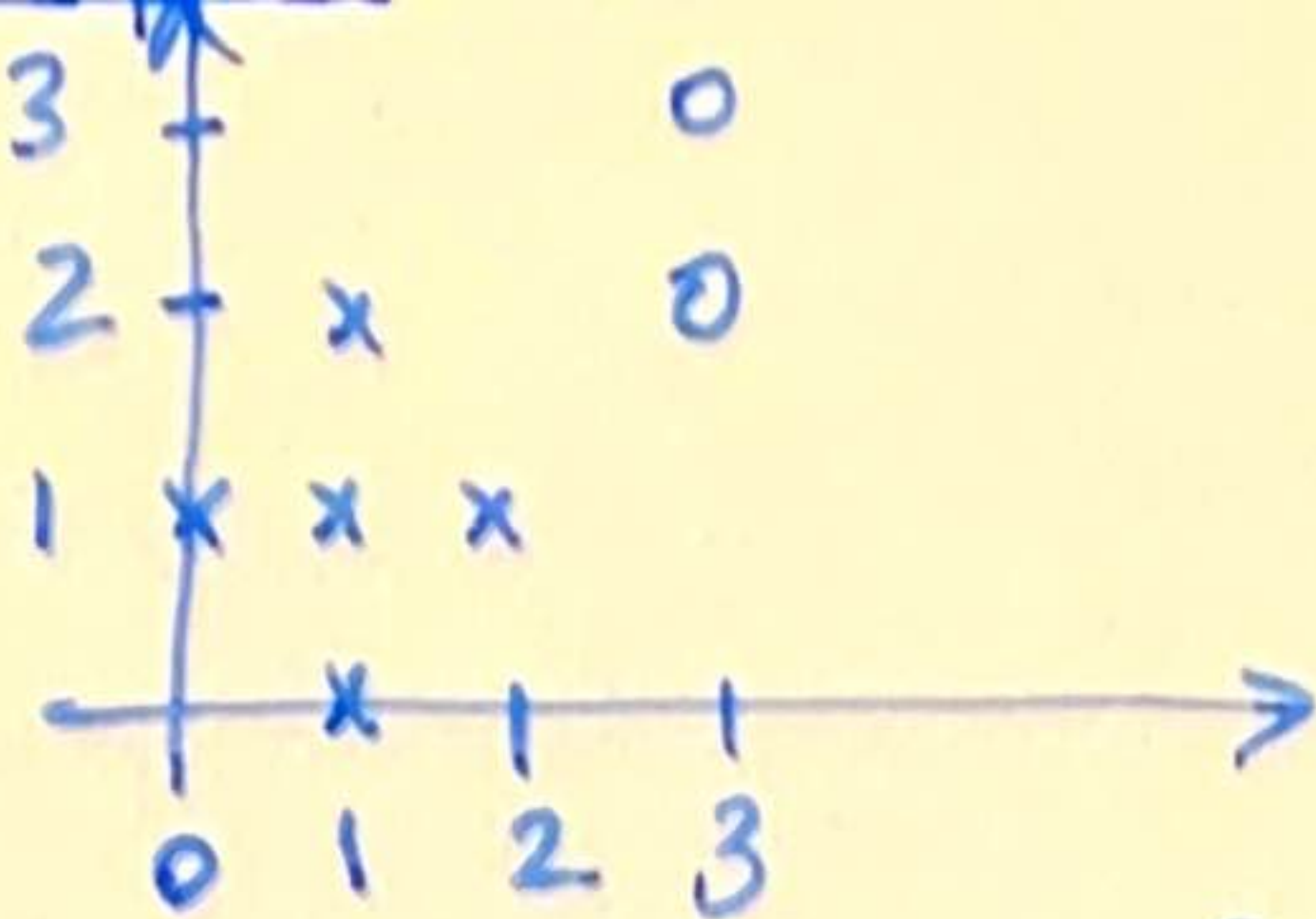


Given the data

There are two classes but we don't know their labels.



We only know $x = \left\{ \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \begin{bmatrix} 2 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 2 \end{bmatrix}, \begin{bmatrix} 3 \\ 2 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \end{bmatrix} \right\}$

Let $K=2$: ~~*~~ of classes.

Let $\mu_1 = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ and $\mu_2 = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$ (Initial center of mass vectors)

• Vectors $\begin{bmatrix} 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 0 \end{bmatrix}, \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ and $\begin{bmatrix} 1 \\ 2 \end{bmatrix}$ are close to μ_1 compared to μ_2 . Therefore the new μ_1 will be $\mu_1 = \frac{1}{5} \left(\begin{bmatrix} 1 \\ 1 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 2 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 \\ 2 \end{bmatrix} \right) = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$.

• Vectors $\begin{bmatrix} 3 \\ 2 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \end{bmatrix}$ are close to $\mu_2 = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$. So the new vector $\mu_2 = \frac{1}{2} \left(\begin{bmatrix} 3 \\ 2 \end{bmatrix} + \begin{bmatrix} 3 \\ 3 \end{bmatrix} \right) = \begin{bmatrix} 3 \\ 3/2 \end{bmatrix}$

• Vectors $\begin{bmatrix} 1 \\ 1 \end{bmatrix}, \begin{bmatrix} 0 \\ 1 \end{bmatrix}, \dots, \begin{bmatrix} 1 \\ 2 \end{bmatrix}$ are close to $\mu_1 = \begin{bmatrix} 1 & 1 \end{bmatrix}^T$
" $\begin{bmatrix} 3 \\ 2 \end{bmatrix}, \begin{bmatrix} 3 \\ 3 \end{bmatrix}$ " " $\mu_2 = \begin{bmatrix} 3 & 3/2 \end{bmatrix}^T$

So, we stop the iterative process.

Test
Given $x = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$ will it be in class 1 or 2?

distance $d\left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 1 \\ 1 \end{bmatrix}\right) = \sqrt{1^2 + 1^2} = \sqrt{2} < \text{dist}\left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 3 \\ 3/2 \end{bmatrix}\right) = \sqrt{3^2 + \left(\frac{3}{2}\right)^2}$

Therefore $\begin{bmatrix} 0 \\ 0 \end{bmatrix}$ is in class 1.