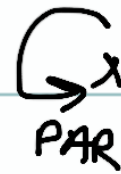
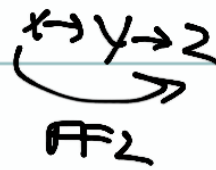


Overall: $4 \times$
NAR



Topics:

→ Response/Rise Time

→ Robustness [Effect of small noise/errors] / Steady State Accuracy

→ Filtering

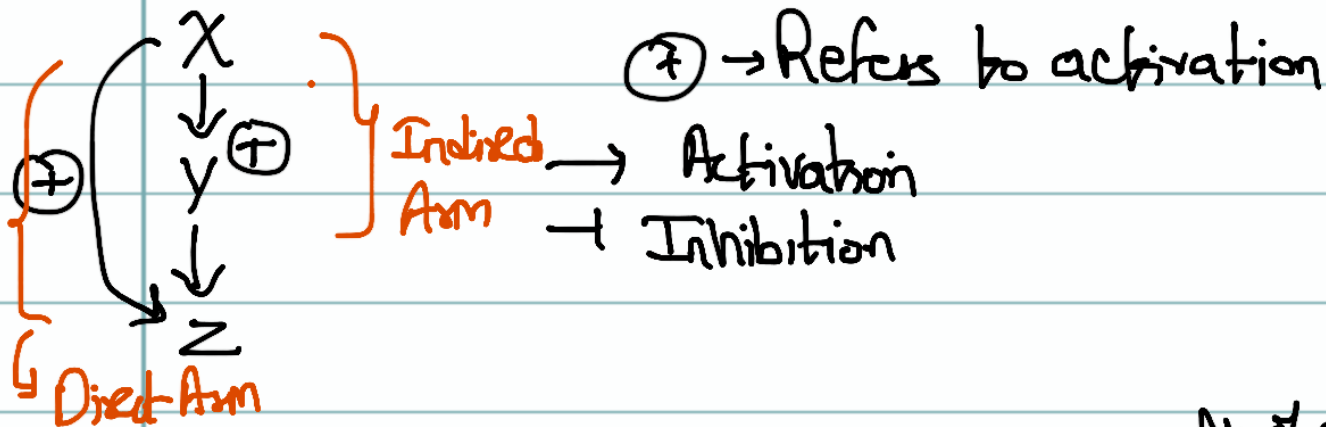
→ Sign-sensitive delay

→ Pulse Generation

∴

20th Oct, 2020

Feedforward Loop



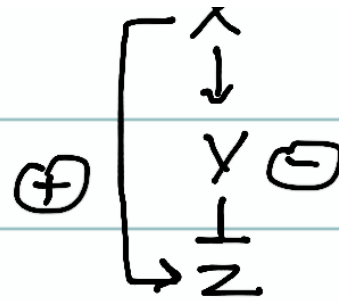
Total feed forward loops : 8 $[2^3 \rightarrow \text{No. of nodes}]$
 $[2 \rightarrow \text{No. of path}]$

Cohesent [C-FFL]

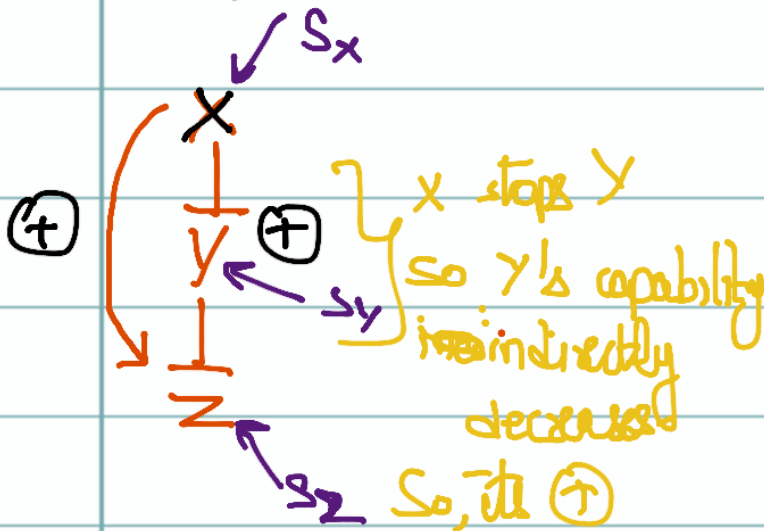
Incoherent



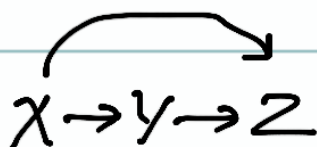
→ Same signs
 → 4 combinations
 (+, +), (-, -)



→ Different signs
 → 4 combinations
 (+, -), (-, +)



Coherent Feedforward loops :



$$\frac{dz}{dt} = k_{s_z} \underbrace{\theta(x > k_{x_z}) \theta(y > k_{y_z})}_{\text{AND Logic}} + k_{d_z} z$$

K_{xz}, K_{yz} are activation thresholds

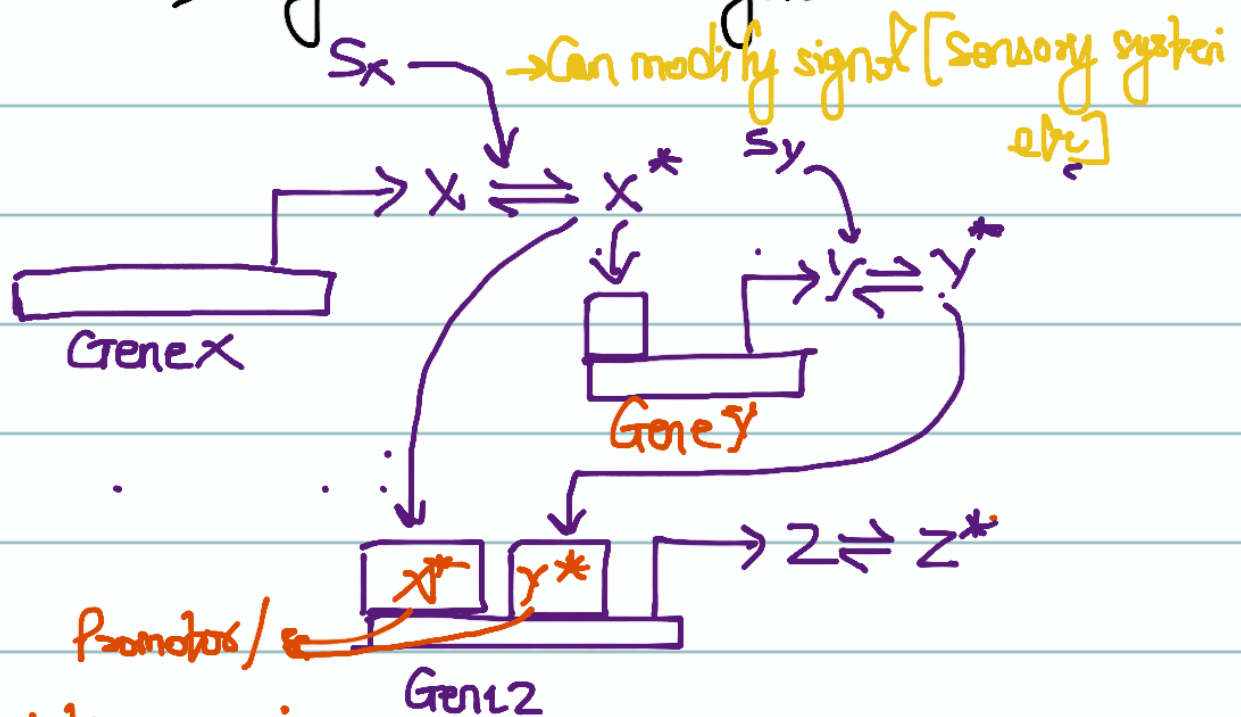
h_{sz} = Synthesis of Z

h_{dz} = Degradation of Z

S_x, S_y, S_z : Input signals

In C-FFL, they can receive signals

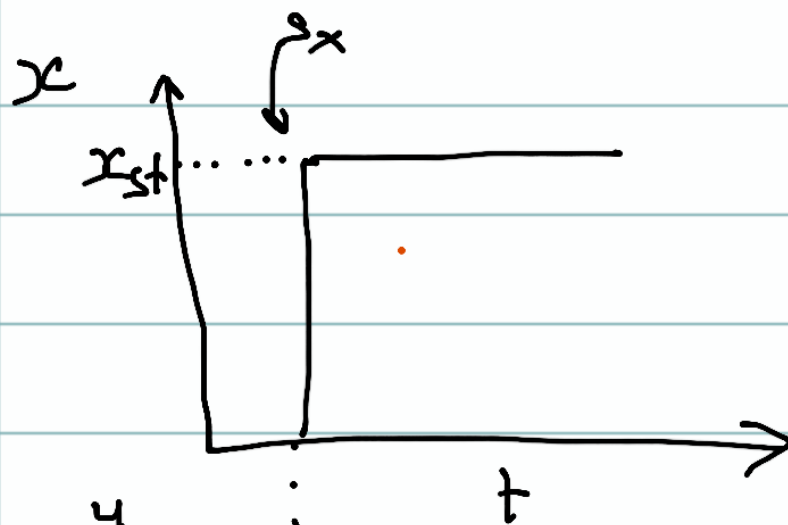
Mechanism



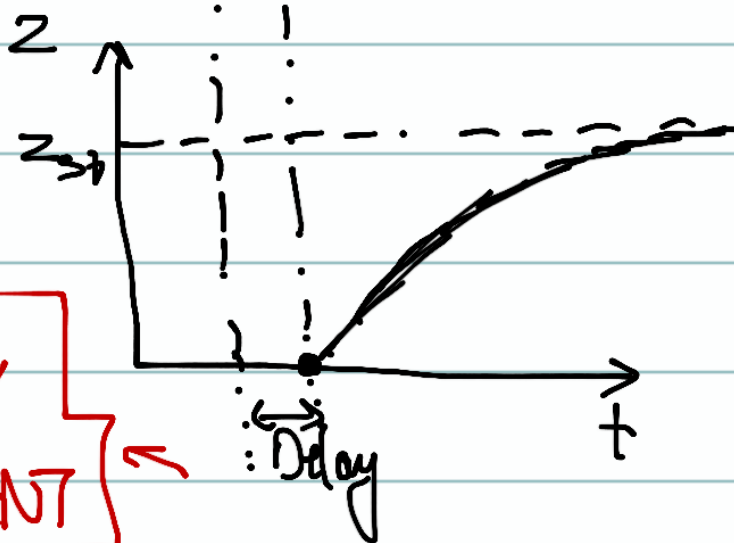
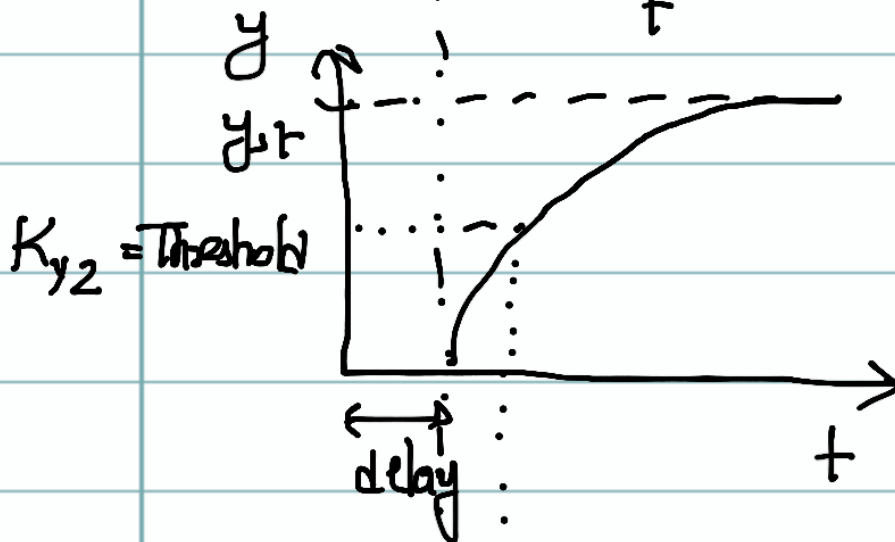
Transcription
activators that bind
to gene

x, y gets modified and help in
synthesis of z .

~~$\frac{dx}{dt} = K_x$~~ → Not possible, there's always s state

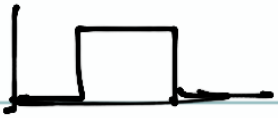


Assume X changes in step wise manner



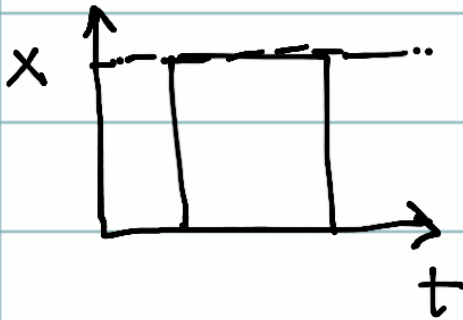
Ability to create delay

DELAY ELEMENT

If X is shut off after a point,  then Y, Z will immediately begin to fall without delay.

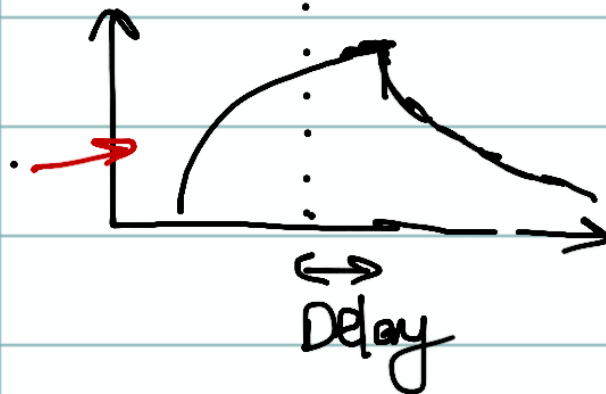


OR Logic :



→ Delay is in inactivation
→ Doesn't decrease for sometime

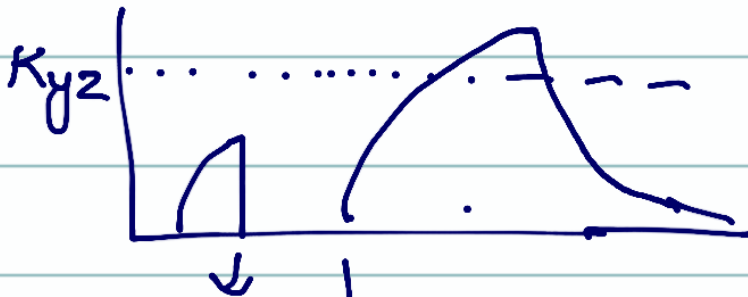
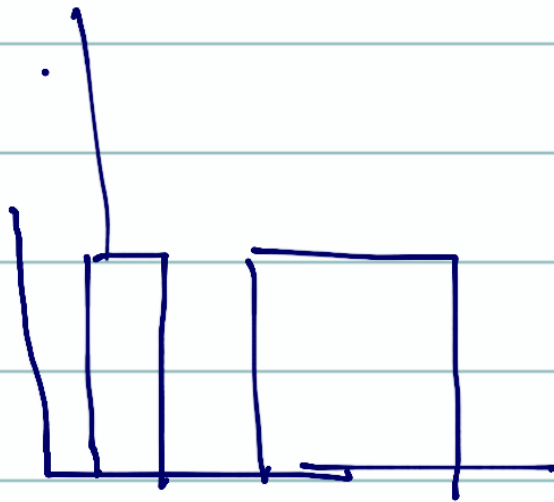
No delay



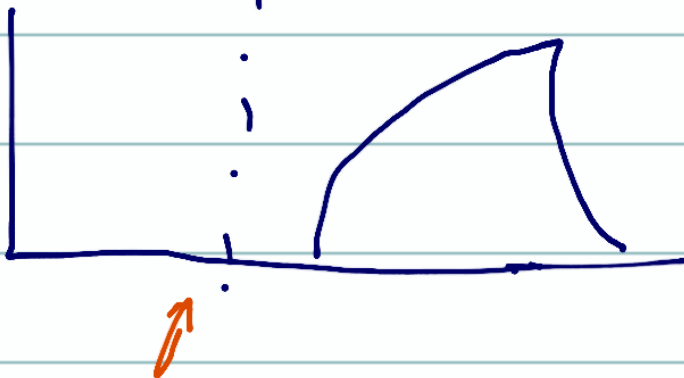
CALLLED SIGN SENSITIVE DELAY
ELEMENT (BASED ON AND/OR

Example: Elevator

↳ keeps hand open momentarily. [quick]
 ↳ If sensor hand, then slowly [slow]



If threshold is not reached, then y will immediately drop

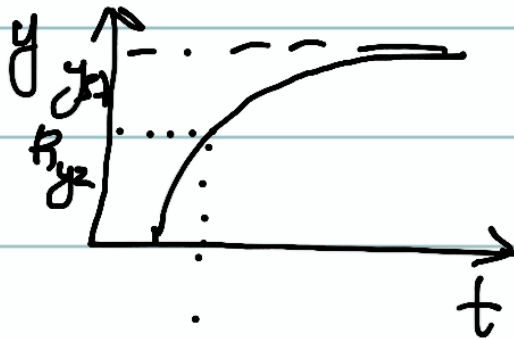


Coincidence detector

IMP
↑

Acts as a filter
 so it avoid all signals
 less than threshold and
 the system is sustained

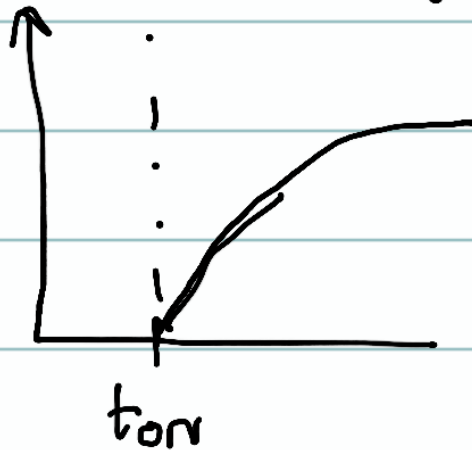
Calculate t_{on} ,



$$\frac{dy}{dt} = k_{sy} - k_{dy}y$$

$$\frac{dy}{dt} = k_{sy} - k_{dy}y$$

$$y = y_{st} (1 - e^{-k_{dy}t})$$

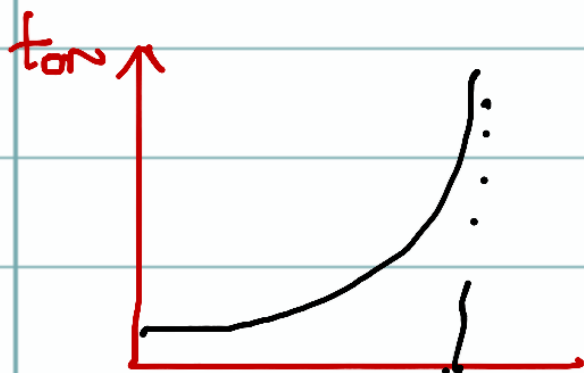


$$k_{y2} = y_{st} (1 - e^{-k_{dy}t})$$

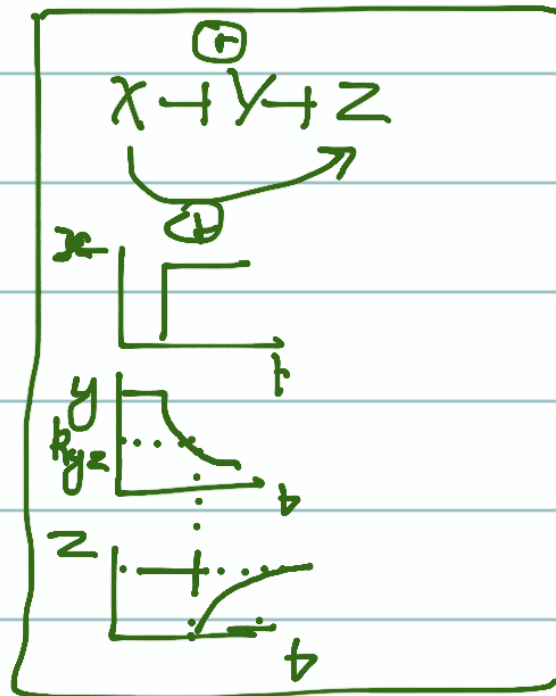
$$e^{-k_{dy}t} = 1 - \frac{k_{y2}}{y_{st}}$$

$$+k_{dy}t = \ln \left(\frac{y_{st}}{y_{st} - k_{y2}} \right)$$

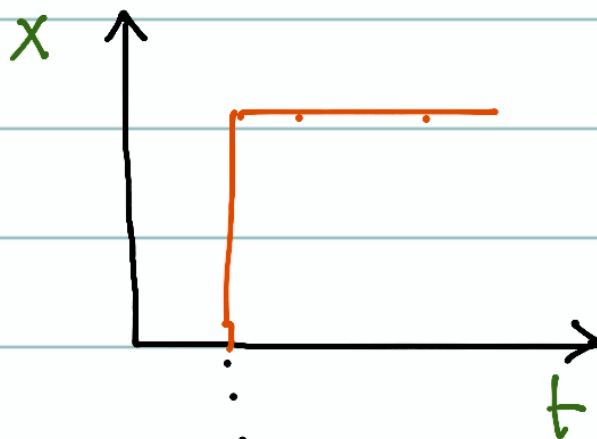
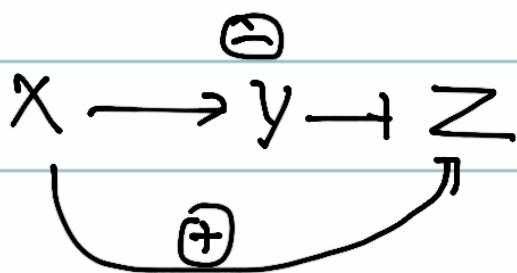
$$t_{on} = \frac{1}{k_{dy}} \ln \left[\frac{y_{st}}{y_{st} - k_{y2}} \right]$$



$$\left(\frac{K_{y2}}{y_{st}} \right)$$



Incoherent-FFL:



→ Increasing F , more depression so, lower steady state.

→ Increasing F will adjust steady state.



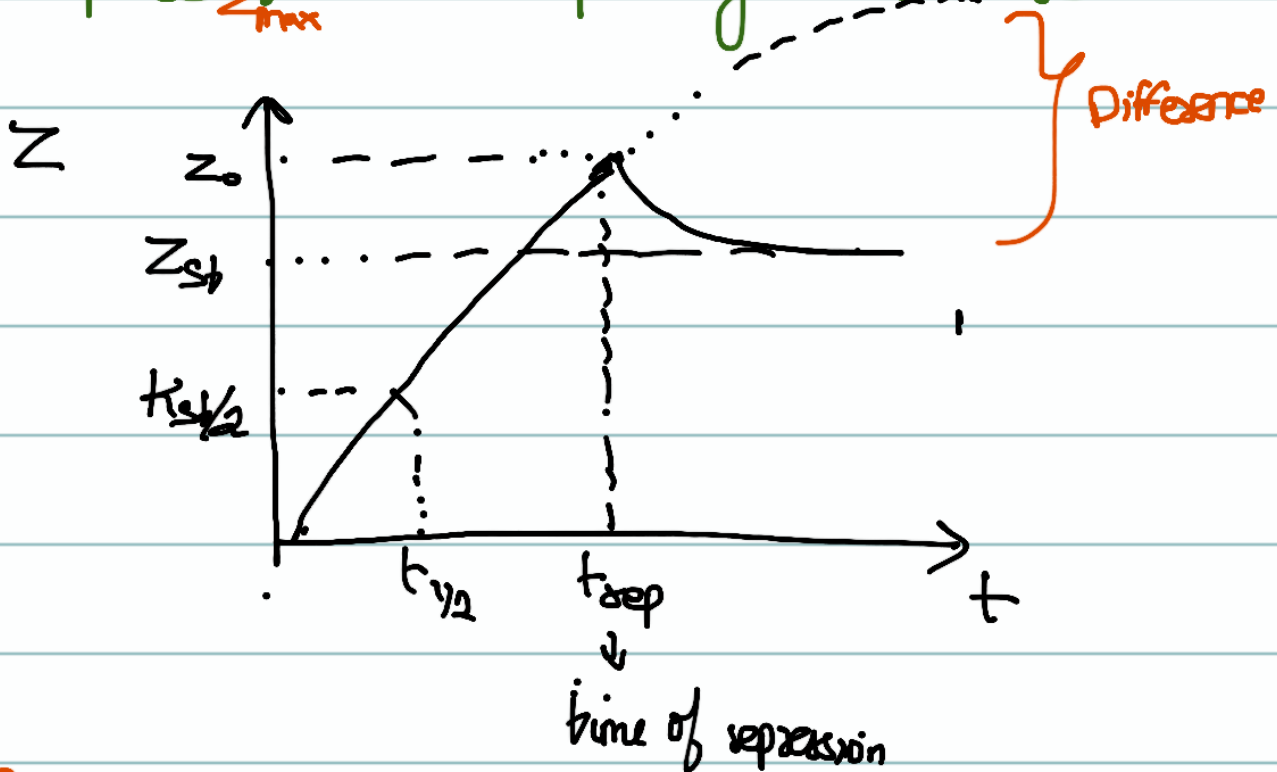
Pulse Generator



Depends on strength of inhibition



Response time for simple system increases



17:07:

Ability to increase quickly and shut down fast too

$$Z_{\text{Max}} = \frac{K_{S2}}{K_{D2}}, \quad Z_{\text{sb}} = \left(\frac{K_{S2}}{K_{D2}} \right)' \rightarrow \text{Repressed rate}$$

$$Z = Z_M [1 - e^{-K_{D2} b}]$$

$$Z_0 = Z_M [1 - e^{-K_{D2} t_{\text{rep}}}]$$

To find t_{rep} ,

$$K_{Y2} = Y_{\text{sb}} [1 - e^{-K_{D2} t_{\text{rep}}}]$$

$$t_{\text{rep}} = \frac{1}{K_{D2}} \ln \left[\frac{Y_{\text{sb}}}{Y_{\text{sb}} - K_{Y2}} \right]$$

↓
same as t_{on}

To calculate response time t_{Y2} ,

$$\frac{Z_{\text{sb}}}{2} = Z_M [1 - e^{-K_{D2} t_{Y2}}]$$

$$\left[\frac{K_{S2}'}{2 K_{D2}} \right] = \left[\frac{K_{S2}}{K_{D2}} \right] [1 - e^{-K_{D2} t_{Y2}}]$$

$$\frac{K_{S2}'}{2(K_{S2})} = 1 - e^{-K_{D2} t_{Y2}}$$

$$t_{y_2} = \frac{1}{K_{D2}} \ln \left[\frac{2(K_{S2})}{2(K_{S2}) - K_{D2}} \right] = \frac{1}{K_{D2}} \ln \left[\frac{1}{1 - \frac{K_{S2}}{2(K_{S2})}} \right]$$

If we take $F = \frac{Z_{M_1}}{Z_{S1}} = \frac{K_{S2}}{K_{D2}}$

$$t_{y_2} = \frac{1}{K_{D2}} \ln \left[\frac{2F}{2F-1} \right]$$

If $F=1, K_{S2} = K_{D2}$

$t_{y_2} = \frac{\ln 2}{K_{D2}}$

→ Same as standard case obt'd in previous

→ No inhibition $\left[\frac{K_S}{\rightarrow} \times \frac{K_D}{\rightarrow} \right]$

→ No control

