



# Day - 3

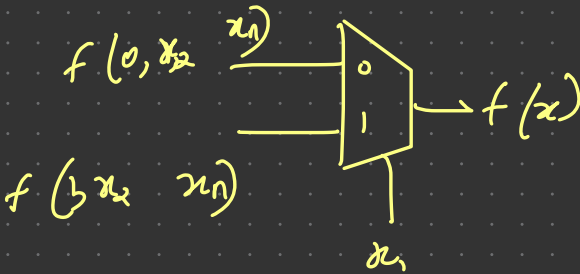
Switches  $\rightarrow$  To state inverter

$\rightarrow$  Implement comb, seq circuit

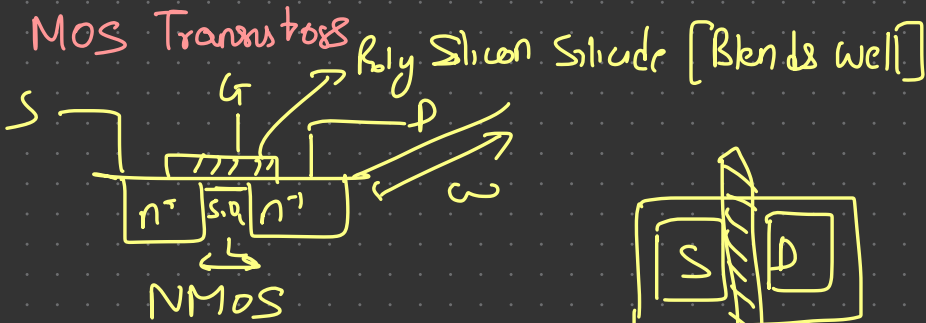
$\rightarrow$  2x1 MUX

SHANNON'S EXPANSION [can be done for multiple variable]  
 $f(x_1, x_2, \dots, x_n) = \bar{x}_1 f(0, x_2, \dots, x_n) + x_1 f(1, x_2, \dots, x_n)$

$$S(A, B) = \bar{A} S(0, B) + A S(1, B)$$



MOS Transistors

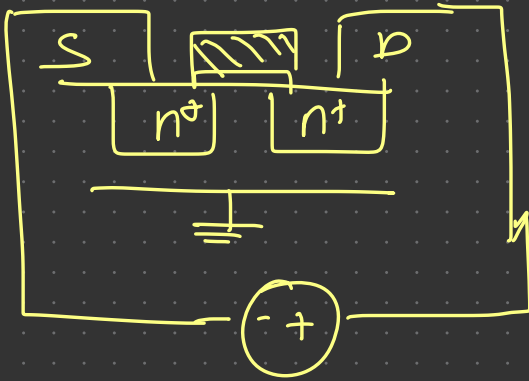


Cross-Sectional View



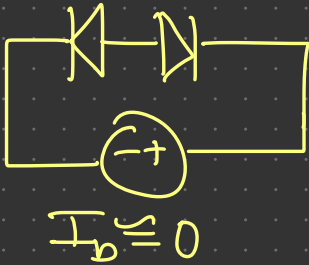
Top View

# MOS Operation



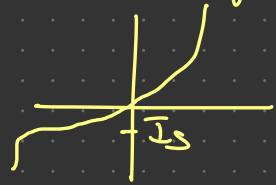
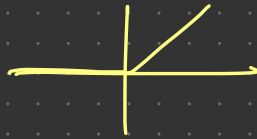
Back to back connected,  
No voltage at gate

→ Current governed by reverse diode



Ideally 0

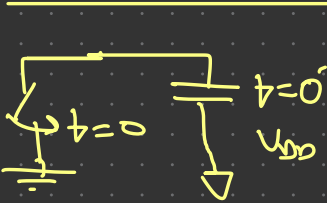
Realistically



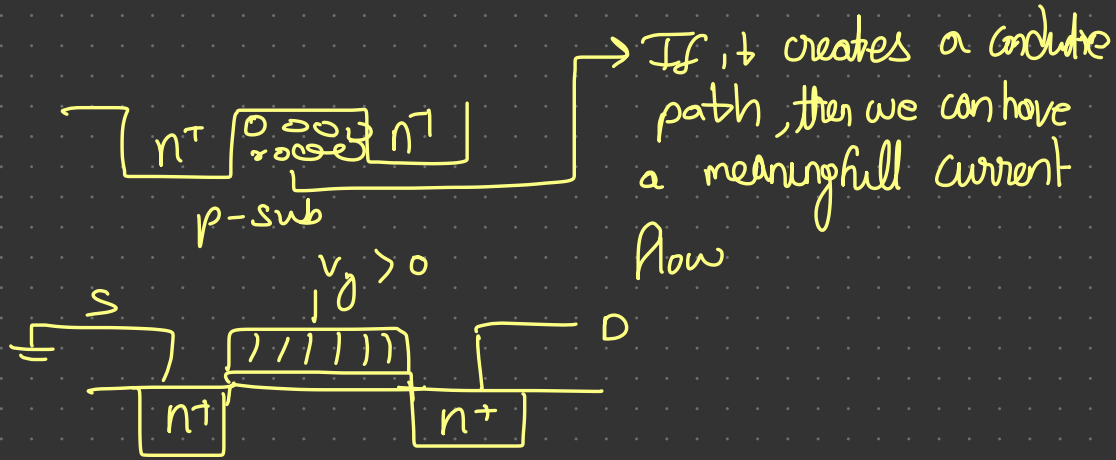
$$I_D = I_S (e^{V_D/nV_T} - 1)$$

↓  
Reverse Saturation Current

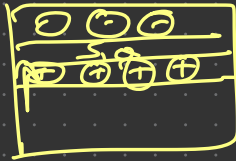
↓  
Leakage Current



To have sufficient conduction

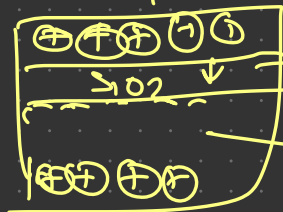


→ If  $V_{gs} < 0$ , try to induce -ve charge in b/w holes [ve] gets accumulated beneath gate called



accumulation mode

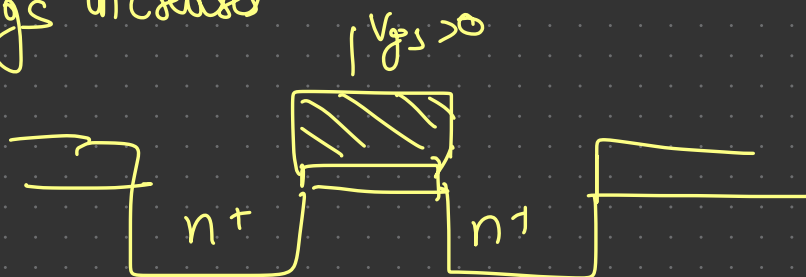
→ If  $V_{gs} > 0$ ,  $V_{gs}$  Depletion Mode



→ repelled

→ depleted of everything

→  $V_{gs}$  increases

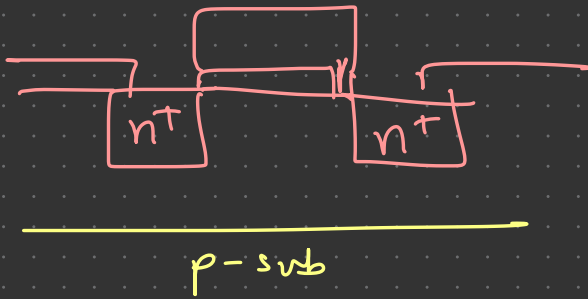


$n^+$  regions supply electrons and tries to  
invert behaviour by making inversion layer  
Inversion Mode

Inversion  $\begin{cases} \rightarrow \text{Weak Inversion} \\ \rightarrow \text{Strong Inversion} \end{cases}$

p-sub - Electrons are minor  
Minor carrier conc  
= Majority carrier  
conc in  
channel

⇒ Threshold Voltage → Channel is complete formed in  
strong inversion when  $V_{gs} > V_{th}$



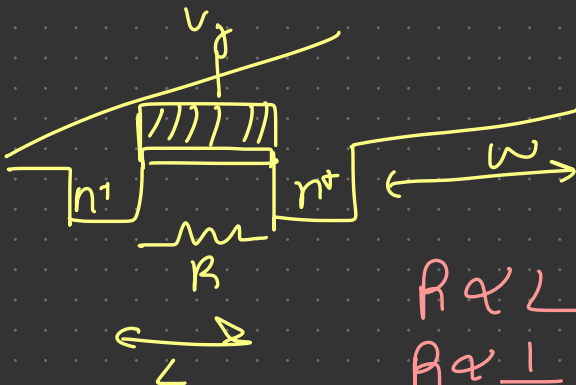
→ Bulk connected to ground

→ Bulk ~~not~~ connected to voltage [oppose as there would be lesser -ve charge]

→  $V_{BS} > 0$

→  $V_{BS} < 0$

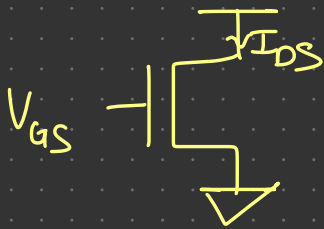
$V_{th}$  is a function of  $V_{BS}$



$R \propto L$   
 $R \propto \frac{1}{W}$  as  $R = \frac{\rho L}{A}$

By using wider transistors, we can conduct more current if other constraints are okay

Channel can act as resistor controlled by gate voltage  $[V_{GS}]$



VCCS

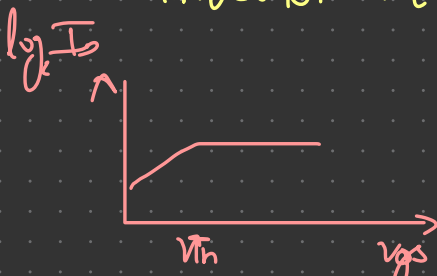
$$\begin{cases} V_{GS} < 0, I_D \approx 0 \\ V_{GS} > 0, I_{DS} = \text{finite} \end{cases}$$

MOSFETs Voltage Controlled Current Source

Accumulation  $\circ V_{GS} < 0$

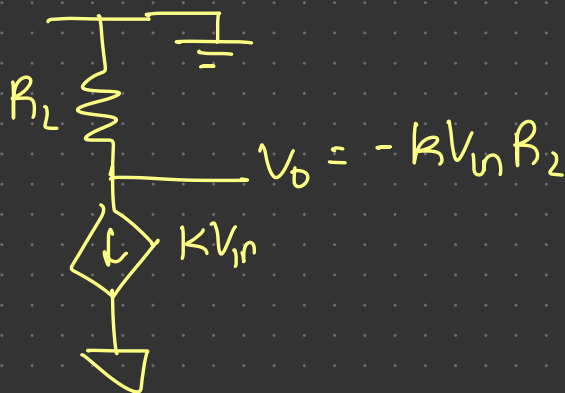
Depletion  $\circ 0 < V_{GS} < V_T$  Sub Threshold

Inversion Mode  $\circ$  Weak  $\circ 0 < V_{GS} < V_T$   
Strong  $\circ V_{GS} > V_T$



$$I_D \approx I_0 e^{V_{GS}/V_T}$$

Transconductance  $= \frac{I}{V}$  for small voltage we can get high current if  $\mu_{\text{trans}}$  is high

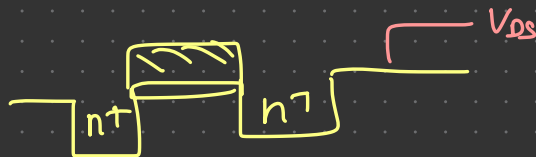


→ NMOS modes of op<sup>n</sup> with  $V_{DS}$

①  $V_{GS} < 0$ , for any finite  $V_{DS}$ ,  $I_{DS} \approx 0$

Cutoff Region

②  $V_{GS} > V_{Th}$  and finite  $V_{DS}$  [ $V_{DS} > 0$ ]



There will be electric field

$$E = \frac{V_{DS}}{L} \text{ with}$$

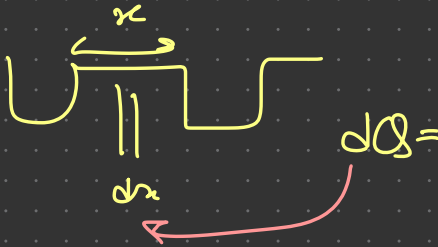
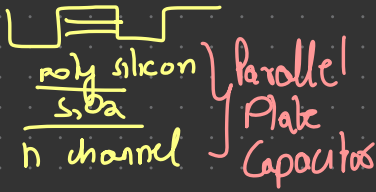
force on charge carrier



on an average they drift from one side to another called drift velocity

$$V_d = \mu E = \mu \frac{V_{DS}}{L}$$

ability to move in medium [Mobility]



$C_{ox}$  = Capacitance per unit area

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = \frac{\epsilon_o}{t_{ox}} = qF/\mu m^2$$

order of few nm

permittivity

$$dQ = C_{ox} (w dL) (V_{GS} - V_{th} - V_x)$$

$$I_{DS} = \frac{dQ}{dt} = C_{ox} W (V_{gs} - V_{th} - V_k) \frac{dx}{dt}$$

$$\frac{dx}{dt} = V_D = \mu F(x) = \mu \left( \underbrace{-\frac{dV}{dx}}_{\text{Field}} \right)$$

$$\int_0^L I_{DS} dx = \mu C_{ox} \frac{W}{L} \left[ (V_{gs} - V_{th}) - \frac{V_{DS}}{2} \right] V_{DS}$$

$$I_{DS} = \mu C_{ox} \left[ \frac{W}{L} \right] \left[ (V_{gs} - V_{th}) V_{DS} - \frac{V_{DS}^2}{2} \right]$$

If  $V_{GS} > V_{th}$   $V_{DS}$  Overdrive Voltage

If  $V_{DS} < V_{GS} - V_{th}$ , second term  $\frac{V_{DS}^2}{2}$  can be ignored

Linear Mode of Operation

$$I_{DS} \approx \mu C_{ox} \left[ \frac{W}{L} \right] (V_{GS} - V_{th}) V_{DS}$$



$$R = \frac{1}{\mu C_{ox} \left[ \frac{W}{L} \right] (V_{GS} - V_{th})}$$

Cutoff:  $V_{GS} < 0$

Linear:  $V_{DS} > V_{th}$ ,  $V_{DS} < V_{GS} - V_{th}$

$$V_{GD} = V_{GS} - V_{DS} = \underbrace{V_G - V_D}_{\text{Common Reference}}$$