

Erosion:

Shrinks connected sets of 1's of binary image

Used for:

1) Shrinking features

2) Removing bridges, protrusions etc & branches



3) Foreground holes are enlarged

4) $f \ominus s \rightarrow$ Representation

Min filter

Dilation:

→ Expands foreground objects

→ foreground holes are shrunk

→ Representation: $f \oplus \hat{s}$

→ Max filter

→ No change in SE after reflection if symmetric

Boundary extraction:

Ex. Boundary: $(A \oplus B) - A$

In. Boundary: $A - (A \ominus B)$

Morphological operation $(A \oplus B) - (A \ominus B)$

Opening: (Erosion then dilation) $f \circ s = (f \ominus s) \oplus s$
 Closing: (Dilation then erosion) $f \cdot s = (f \oplus s) \ominus s$

Idempotent
 &
 Dual
 Repeats has no effect

Morphological smoothing can be achieved by opening followed by closing

Dilation & Closing are extending operations

Erosion & Opening are narrowing operations

Erosion can be used for pattern matching [fixed template case]

Hit or miss transforms

→ Look for particular patterns of foreground & bg pixels

→ Use don't care (X) cases

→ If matched set pixel = 1

→ Representation: $A \otimes B = (A \ominus B_1) \cap (A^c \ominus B_2)$

↑ Associated with fg
 ↑ Associated with bg
 ↓ Hit
 ↓ Miss
 Shape Detection

→ Distance transforms

→ Intensities in fg now show distance from each point to closest background/boundary pixel

→ L_∞ = Chessboard distance metric

$$DT(p)[x] = \min_{y \in P} D(x, y)$$

$$D_{\text{chess}}((a, b, c), (x, y, z)) = \max(|a-x|, |b-y|, |c-z|)$$

→ Inefficient way:
Successive erasures

Application: Skeletonisation

Two pass algorithm:

Look at top and side labels and assign new labels accordingly. Go row by row to identify connected components.

Execute this loop again by replacing child label with root label

→ Uses union-find data structure ensures 'find' -ing $O(\log^* n)$
converges to $O(1)$ for repeated calls

Flood fill:

→ Old colored pixels with fill target colors

→ 4 or 8 connectivity

→ Parameters

Target fill, old colors, coordinates

→ Recursively call fn

Geometric operations:

- Zooming images, ...
- Computer graphics
- Coordinates are changed rather than pixel intensities

$$I(x, y) \rightarrow I'(x', y')$$

→ Example Shifting

$$\begin{aligned} x' &= f_x(x, y) \\ y' &= f_y(x, y) \end{aligned} \Rightarrow I(x, y) \Rightarrow I(x', y')$$

→ Operations:

→ Scale

→ Rotate

→ Reflect

→ Translate

→ Shear

$$\begin{aligned} T_x &: x' = x + b_x y \\ T_y &: y' = y + b_y x \end{aligned}$$

→ Affine transformation

$$T_x: x' = S_x x$$

$$T_y: y' = S_y y$$

$$T_x: x' = x + dx$$

$$T_y: y' = y + dy$$

where s_x, s_y are scaling factors

Shrinking:

Removing certain pixels via pixel selection or interpolation

Stretching:

pixels are added via replication (or) interpolation

Homogenous coordinates:

→ Useful for converting scaling, translation, rotation into point-matrix multiplication

$$x = \begin{pmatrix} x \\ y \end{pmatrix} \text{ converted to } \hat{x} = \begin{pmatrix} \hat{x} \\ \hat{y} \\ \hat{h} \end{pmatrix} = \begin{pmatrix} hx \\ hy \\ h \end{pmatrix}$$