Data Analysis with augmentedRCBD

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1 Overview

The software augmentedRCBD is built on the R statistical programming language as an add-on (or 'package' in the R lingua franca). It performs the analysis of data generated from experiments in augmented randomised complete block design according to Federer, W.T. (1956b, 1956a, 1961; 1976). It also computes analysis of variance, adjusted means, descriptive statistics, genetic variability statistics etc. and includes options for data visualization and report generation.

This tutorial aims to educate the users in utilising this package for performing such analysis. Utilising augmentedRCBD for data analysis requires a basic knowledge of R programming language. However, as many of the intended end-users may not be familiar with R, sections 2 to 4 give a 'gentle' introduction to R, especially those aspects which are necessary to get augmentedRCBD up and running for performing data analysis in a Windows environment. Users already familiar with R can feel free to skip to section 5.



2 R software

It is a free software environment for statistical computing and graphics. It is free and open source, platform independent (works on Linux, Windows or MacOS), very flexible, comprehensive with robust interfaces for all the popular programming languages as well as databases. It is strengthened by its diverse library of



add-on packages extending its ability as well as the incredible community support. It is one of the most popular tools being used in academia today (Tippmann, 2015).

3 Getting Started

This section details the steps required to set up the R programming environment under a third-party interface called RStudio in Windows.

3.1 Installing R

New features in this version

Download and install R for Windows from http://cran.r-project.org/bin/windows/base/.

R-3.5.1 for Windows (32/64 bit)

Download R 3.5.1 for Windows (62 megabytes, 32/64 bit)

Installation and other instructions

If you want to double-check that the package you have downloaded matches the package distributed by CRAN, you can compare the md5sum of the .exe to the fingerprint on the master server. You will need a version of md5sum for windows: both graphical and command line versions are available.

Frequently asked questions

- Does R run under my version of Windows?
- How do I update packages in my previous version of R?
- Should I run 32-bit or 64-bit R?

Please see the RFAQ for general information about R and the RWindows FAQ for Windows-specific information

Other builds

- Patches to this release are incorporated in the <u>r-patched snapshot build</u>.
- A build of the development version (which will eventually become the next major release of R) is available in the r-devel snapshot build.
- Previous releases

Note to webmasters: A stable link which will redirect to the current Windows binary release is <cre>CRAN MIRROR>/bin/windows/base/release.htm.

Last change: 2018-07-02

Fig. 1: The R download location.

3.2 Installing RStudio

The basic command line interface in native R is rather limiting. There are several interfaces which enhance it's functionality and ease of use, RStudio being one of the most popular among R programmers.

 $Download\ and\ install\ RStudio\ for\ Windows\ from\ https://www.rstudio.com/products/rstudio/download/\ \#download$

Installers for Supported Platforms

Installers	Size	Date	MD5
RStudio 1.1.456 - Windows Vista/7/8/10	85.8 MB	2018-07-19	24ca3fe0dad8187aabd4bfbb9dc2b5ad
RStudio 1.1.456 - Mac OS X 10.6+ (64-bit)	74.5 MB	2018-07-19	4fc4f4f70845b142bf96dc1a5b1dc556
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (32-bit)	89.3 MB	2018-07-19	3493f9d5839e3a3d697f40b7bb1ce961
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (64-bit)	97.4 MB	2018-07-19	863ae806120358fa0146e4d14cd75be4
RStudio 1.1.456 - Ubuntu 16.04+/Debian 9+ (64-bit)	64.9 MB	2018-07-19	d96e63548c2add890bac633bdb883f32
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (32-bit)	88.1 MB	2018-07-19	1df56c7cd80e2634f8a9fdd11ca1fb2d
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (64-bit)	90.6 MB	2018-07-19	5e77094a88fdbddddddd0d35708752462

Zip/Tarballs

Zip/tar archives	Size	Date	MD5
RStudio 1.1.456 - Windows Vista/7/8/10	122.9 MB	2018-07-19	659d6bfe716d8c97acbe501270d89fa3
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (32-bit)	90 MB	2018-07-19	63117c159deca4d01221a8069bd45373
RStudio 1.1.456 - Ubuntu 12.04-15.10/Debian 8 (64-bit)	98.3 MB	2018-07-19	c53c32a71a400c6571e36c573f83dfde
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (32-bit)	88.8 MB	2018-07-19	f4ba2509fb00e30c91414c6821f1c85f
RStudio 1.1.456 - Fedora 19+/RedHat 7+/openSUSE 13.1+ (64-bit)	91.4 MB	2018-07-19	c60db6467421aa86c772227da0945a13

Source Code

A tarball containing source code for RStudio v1.1.456 can be downloaded from here

Fig. 2: The RStudio download location.

3.3 The RStudio Interface

On opening RStudio, the default interface with four panes/windows is visible as follows. Few panes have different tabs.

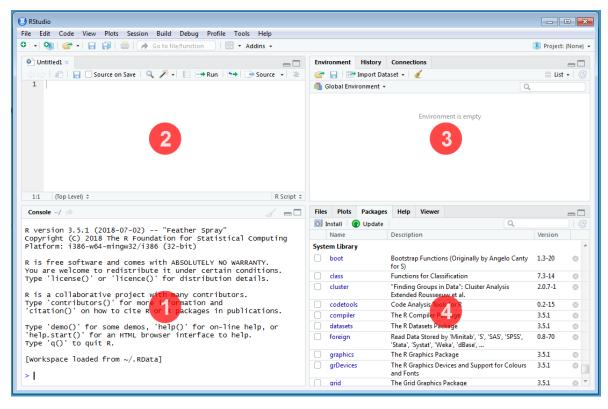


Fig. 3: The default RStudio interface with the four panes.

3.3.1 Console

This is where the action happens. Here any authentic R code typed after the '>' prompt will be executed after pressing 'Enter' to generate the output.

For example, type 1+1 in the console and press 'Enter.'

1+1

[1] 2

3.3.2 Source

This is where R Scripts (collection of code) can be created and edited. R scripts are text files with a .R extension. R Code for analysis can be typed and saved in such R scripts. New scripts can be opened by clicking 'File|New File' and selecting 'R Script.' Code can be selected from R Scripts and sent to console for evaluation by clicking 'Run' on the 'Source' pane or by pressing 'Ctrl + Enter.'

3.3.3 Environment | History | Connections

The 'Environment' tab shows the list of all the 'objects' (see section 4.3) defined in the current R session. It has also some buttons up top to open, save and clear the environment as well as few options for import of data under Import Dataset.

The 'History' tab shows a history of all the code that was previously evaluated. This is useful, if you want to go back to some code.

The 'Connections' tab helps to establish and manage connections with different databases and data sources.

3.3.4 Files|Plots|Packages|Help|Viewer

The 'Files' tab shows a sleek file browser to access the file directory in the computer with options to manage the working directory (see section 4.1) under the More button.

The 'Plots' tab shows all the plots generated in R with buttons to delete unnecessary ones and export useful ones as a pdf file or as an image file.

The 'Packages' tab shows a list of all the R add-on packages installed. The check box on the left shows whether they are loaded or not. There are also buttons to install and update R packages.

The 'Viewer' tab shows any web content output generated by an R code.

4 Some Basics

This section describes some basics to enable the users to have a working knowledge in R in order to use augmentedRCBD.

4.1 Working Directory

It is a file path to a folder on the computer which is recognised by R as the default location to read files from or write files to. The code getwd() shows the current working directory, while setwd() can be used to change the existing working directory.

```
# Print current working directory
getwd()

[1] "C:/Users/Computer/Documents"

# Set new working directory
setwd("C:/Data Analysis/")
```

[1] "C:/Data Analysis/"

getwd()

[1] 3

One key detail is that file paths in R uses forward slashes (/) as in MacOS or Linux, unlike backward slashes (\) in Windows. This needs to be considered while copying paths from default Windows file explorer.

4.2 Expression and Assignment

Expressions are instructions in the form of code to be entered after the > prompt in the console. Expressions can be a constant, an arithmetic or a condition. A more advanced and most useful expression is a function call (see section 4.3).

```
# Constant
123
[1] 123
# Arithmetic (add two numbers)
1 + 2
```

```
# Condition
34 > 25

[1] TRUE
1 == 2

[1] FALSE
# Function call (mean of a series of numbers)
mean(c(25,56,89,35))
```

[1] 51.25

Information from an expression can be stored as an 'object' (see section 4.3) by assigning a name using the operator '<-.'

```
# Assign the result of the expression 1 + 2 to an object 'a' a <- 1 + 2 a
```

[1] 3

It is recommended to add comments to explain the code by using the '#' sign. Any code after the '#' sign will be ignored by R.

4.3 Objects and Functions

R is an object-oriented programming language (OOP). Any kind or construct created in R is an 'object.' Each object has a 'class' (shown using the class() function) and different 'attributes' which defines what operations can be done on that object. There are different types of data structure objects in R such as vectors, matrices, factors, data frames, and lists. A 'function' is also an object, which defines a procedure or a sequence of expressions.

4.3.1 Vector

A vector is a collection of elements of a single type (or 'mode'). The common vector modes are 'numeric,' 'integer,' 'character' and 'logical.' The c() function is used to create vectors. The functions class(), str() and length() show the attributes of vectors.

Vector modes 'numeric' stores real numbers, while 'integer' stores integers, which can be enforced by suffixing elements with 'L.'

```
# A numeric vector
a <- c(1, 2, 3.3)
class(a)

[1] "numeric"
str(a)
num [1:3] 1 2 3.3
length(a)

[1] 3
# An integer vector
b <- c(1L, 2L, 3L)
class(b)
```

```
[1] "integer"
str(b)
 int [1:3] 1 2 3
length(b)
[1] 3
The vector mode 'character' store text.
# A character vector
c <- c("one","two","three")</pre>
class(c)
[1] "character"
str(c)
 chr [1:3] "one" "two" "three"
length(c)
[1] 3
The vector mode 'logical' stores 'TRUE' OR 'FALSE' logical data.
#logical vector
d <- c(TRUE,TRUE,TRUE,FALSE,TRUE,FALSE)</pre>
class(d)
[1] "logical"
str(d)
 logi [1:6] TRUE TRUE TRUE FALSE TRUE FALSE
length(d)
[1] 6
4.3.2 Factor
A 'factor' in R stores data from categorical data in variables as different levels.
catg <- c("male", "female", "female", "male", "male")</pre>
catg
[1] "male"
              "female" "female" "male"
                                             "male"
is.factor(catg)
[1] FALSE
# Apply the factor function
factor_catg <- factor(catg)</pre>
factor_catg
```

```
[1] male
            female female male
                                   male
Levels: female male
is.factor(factor_catg)
[1] TRUE
class(factor_catg)
[1] "factor"
str(factor_catg)
 Factor w/ 2 levels "female", "male": 2 1 1 2 2
A character, numeric or integer vector can be transformed to a factor by using the as.factor()
# Conversion of numeric to factor
a \leftarrow c(1, 2, 3.3)
class(a)
[1] "numeric"
str(a)
num [1:3] 1 2 3.3
fac_a <- as.factor(a)</pre>
class(fac_a)
[1] "factor"
str(fac_a)
Factor w/ 3 levels "1", "2", "3.3": 1 2 3
# Conversion of integer to factor
b \leftarrow c(1L, 2L, 3L)
class(b)
[1] "integer"
str(b)
 int [1:3] 1 2 3
fac_b <- as.factor(b)</pre>
class(fac_b)
[1] "factor"
str(fac_b)
 Factor w/ 3 levels "1", "2", "3": 1 2 3
# Conversion of character to factor
c <- c("one","two","three")</pre>
class(c)
[1] "character"
```

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```
str(c)
 chr [1:3] "one" "two" "three"
fac_c <- as.factor(c)</pre>
class(fac_c)
[1] "factor"
str(fac_c)
 Factor w/ 3 levels "one", "three", ...: 1 3 2
4.3.3 Matrix
A 'matrix' in R is a vector with the attributes 'nrow' and 'ncol.'
# Generate 5 * 4 numeric matrix
m \leftarrow matrix(1:20, nrow = 5, ncol = 4)
      [,1] [,2] [,3] [,4]
[1,]
        1
              6
                  11
[2,]
        2
              7
                  12
                        17
[3,]
        3
            8
                 13
                        18
         4
              9
[4,]
                  14
                        19
[5,]
         5
             10
                  15
                        20
class(m)
[1] "matrix" "array"
typeof(m)
[1] "integer"
# Dimensions of m
dim(m)
```

[1] 5 4

4.3.4 List

A 'list' is a container containing different objects. The contents of list need not be of the same type or mode. A list can encompass a mixture of data types such as vectors, matrices, data frames, other lists or any other data structure.

```
w <- list(a, m, d, list(b, c))
class(w)

[1] "list"

str(w)

List of 4
$ : num [1:3] 1 2 3.3
$ : int [1:5, 1:4] 1 2 3 4 5 6 7 8 9 10 ...
$ : logi [1:6] TRUE TRUE FALSE TRUE FALSE
$ :List of 2</pre>
```

```
..$ : int [1:3] 1 2 3
..$ : chr [1:3] "one" "two" "three"
```

4.3.5 Data Frame

A 'data frame' in R is a special kind of list with every element having equal length. It is very important for handling tabular data in R. It is a array like structure with rows and columns. Each column needs to be of a single data type, however data type can vary between columns.

```
L <- LETTERS[1:4]
y <- 1:4
z <- c("This", "is", "a", "data frame")</pre>
df \leftarrow data.frame(L, x = 1, y, z)
df
  Lxy
                 z
1 A 1 1
              This
2 B 1 2
                is
3 C 1 3
4 D 1 4 data frame
str(df)
'data.frame': 4 obs. of 4 variables:
 $ L: chr "A" "B" "C" "D"
 $ x: num 1 1 1 1
 $ y: int 1 2 3 4
 $ z: chr "This" "is" "a" "data frame"
attributes(df)
$names
[1] "L" "x" "y" "z"
$class
[1] "data.frame"
$row.names
[1] 1 2 3 4
rownames(df)
[1] "1" "2" "3" "4"
colnames(df)
[1] "L" "x" "y" "z"
```

4.3.6 Functions

All of the work in R is done by functions. It is an object defining a procedure which takes one or more objects as input (or 'arguments'), performs some action on them and finally gives a new object as output (or 'return'). class(), mean(), getwd(), +, etc. are all functions.

For example the function mean() takes a numeric vector as argument and returns the mean as a numeric vector.

```
a <- c(1, 2, 3.3)
mean(a)
```

[1] 2.1

The user can also create custom functions. For example the function foo adds two numbers and gives the result.

```
foo <- function(n1, n2) {
  out <- n1 + n2
  return(out)
}
foo(2,3)</pre>
```

[1] 5

4.4 Special Elements

In addition to numbers and text, there are some special elements which can be included in different data objects.

NA (not available) indicates missing data.

```
x <- c(2.5, NA, 8.6)
y <- c(TRUE, FALSE, NA)
z <- c("k", NA, "m", "n", "o")
is.na(x)</pre>
```

[1] FALSE TRUE FALSE

is.na(z)

[1] FALSE TRUE FALSE FALSE

anyNA(x)

[1] TRUE

a

[1] 1.0 2.0 3.3

is.na(a)

[1] FALSE FALSE FALSE

Inf indicates infinity.

1/0

[1] Inf

NaN (Not a Number) indicates any undefined value.

0/0

[1] NaN

4.5 Indexing

The [function is used to extract elements of an object by indexing (numeric or logical). Named elements in lists and data frames can be extracted by using the \$ operator.

```
Consider a vector a.
```

```
a \leftarrow c(1, 2, 3.3, 2.8, 6.7)
# Numeric indexing
# Extract first element
a[1]
[1] 1
# Extract elements 2:3
a[2:3]
[1] 2.0 3.3
# Logical indexing
a[a > 3]
[1] 3.3 6.7
Consider a matrix m.
m <- matrix(1:9, nrow = 3, ncol = 3, byrow = TRUE)
colnames(m) <- c('a', 'b', 'c')</pre>
     a\ b\ c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
# Extract elements
m[,2] # 2nd column of matrix
[1] 2 5 8
m[3,] # 3rd row of matrix
a b c
7 8 9
m[2:3, 1:3] # rows 2,3 of columns 1,2,3
     a b c
[1,] 4 5 6
[2,] 7 8 9
m[2,2] # Element in 2nd column of 2nd row
b
5
m[, 'b'] # Column 'b'
[1] 2 5 8
```

```
m[, c('a', 'c')] # Column 'a' and 'c'
    a c
[1,] 1 3
[2,] 4 6
[3,] 7 9
Consider a list w.
w <- list(vec = a, mat = m, data = df, alist = list(b, c))</pre>
# Indexing by number
w[2] # As list structure
$mat
    a b c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
w[[2]] # Without list structure
    a b c
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9
# Indexing by name
w$vec
[1] 1.0 2.0 3.3 2.8 6.7
w$data
 Lxy
1 A 1 1
            This
2 B 1 2
                is
3 C 1 3
                 a
4 D 1 4 data frame
Consider a data frame df.
df
 Lxy
                 z
            This
1 A 1 1
2 B 1 2
              is
3 C 1 3
4 D 1 4 data frame
# Indexing by number
df[,2] # 2nd column of data frame
[1] 1 1 1 1
df[2] # 2nd column of data frame
 х
1 1
```

```
2 1
3 1
4 1
df[3,] # 3rd row of data frame
  Lxyz
3 C 1 3 a
df[2:3, 1:3] # rows 2,3 of columns 1,2,3
  Lxy
2 B 1 2
3 C 1 3
df[2,2] # Element in 2nd column of 2nd row
[1] 1
# Indexing by name
df$L
[1] "A" "B" "C" "D"
df$z
                               "a"
[1] "This"
                 "is"
                                            "data frame"
```

4.6 Help Documentation

The help documentation regarding any function can be viewed using the ? or help() function. The help documentation shows the default usage of the function including, the arguments that are taken by the function and the type of output object returned ('Value').

```
?ls
help(ls)
?mean
?setwd
```

4.7 Packages

Packages in R are collections of R functions, data, and compiled code in a well-defined format. They are add-ons which extend the functionality of R and at present, there are 17408 packages available for deployment and use at the official repository, the Comprehensive R Archive Network (CRAN).

Valid packages from CRAN can be installed by using the install.packages() command.

```
# Install the package 'readxl' for importing data from excel install.packages(readxl)
```

Installed packages can be loaded using the function library().

```
# Install the package 'readxl' for importing data from excel
library(readxl)
```

4.8 Importing and Exporting Tabular Data

Tabular data from a spreadsheet can be imported into R in different ways. Consider some data such as in Table 1. Copy this data in to a spreadsheet editor such as MS Excel and save it as augdata.csv, a comma-separated-value file and augdata.xlsx, an Excel file in the working directory (getwd()).

Table 1: Example data from an experiment in augmented RCBD design.

I 12 II

Π

 Π

ΙΙ

Π

Π

III

III

III

str(data)

'data.frame': 20 obs. of 4 variables:

\$ y1 : num 92 79 87 81 96 89 82 79 81 81 ...

\$ y2 : num 258 224 238 278 347 300 289 260 220 237 ...

\$ blk: chr "I" "I" "I" "I" ...
\$ trt: num 1 2 3 4 7 11 12 1 2 3 ...

```
3
78
268
III
4
78
287
Ш
8
70
226
III
6
75
395
III
10
74
450
The augdata.csv file can be imported into R using the read.csv() function or the read_csv() function
in the readr package.
data <- read.csv(file = "augdata.csv")</pre>
str(data)
'data.frame': 20 obs. of 4 variables:
 $ blk: Factor w/ 3 levels "I","II","III": 1 1 1 1 1 1 2 2 2 ...
 $ trt: num 1 2 3 4 7 11 12 1 2 3 ...
 $ y1 : num 92 79 87 81 96 89 82 79 81 81 ...
 $ y2 : num 258 224 238 278 347 300 289 260 220 237 ...
The argument stringsAsFactors = FALSE reads the text columns as of type character instead of
the default factor.
data <- read.csv(file = "augdata.csv", stringsAsFactors = FALSE)</pre>
```

The augdata.xlsx file can be imported into R using the read_excel() function in the readxl package.

4.9 Additional Resources

To learn more about R, there are umpteen number of online tutorials as well as free courses available. Queries about various aspects can be put to the active and vibrant 'R community online.

- Online tutorials
 - http://www.cran.r-project.org/other-docs.html
 - https://bookdown.org/ndphillips/YaRrr/
- Free online courses
 - http://tryr.codeschool.com/
 - https://www.datacamp.com/courses/free-introduction-to-r
- R community support
 - http://stackoverflow.com/
 - R help mailing lists: http://www.r-project.org/mail.html

5 Installation of augmentedRCBD

The package augmentedRCBD can be installed using the following functions.

```
# Install from CRAN
install.packages('augmentedRCBD', dependencies=TRUE)

# Install development version from Github
if (!require('devtools')) install.packages('devtools')
library(devtools)
install_github("aravind-j/augmentedRCBD")
```

The stable release is hosted in CRAN (see section 4.7), while the under-development version is hosted as a Github repository. To install from github, you need to use the install_github() function from 'devtools package.

Then the package can be loaded using the function

```
library(augmentedRCBD)
```

The current version of the package is 0.1.4. The previous versions are as follows.

Table 2. Version history of augmentedRCBD R package.

Version

Date

0.1.0

2018-07-10

0.1.1

2019-07-21

0.1.2

2020-03-19

0.1.3

2020-07-27

To know detailed history of changes use news(package='augmentedRCBD').

6 Data Format

Certain details need to be considered for arranging experimental data for analysis using the augmentedRCBD package.

The data should be in long/vertical form, where each row has the data from one genotype per block. For example, consider the following data (Table 3) recorded for a trait from an experiment laid out in an augmented block design with 3 blocks and 12 genotypes(or treatment) with 6 to 7 genotypes/block. 8 genotypes (Test, G 5 to G 12) are not replicated, while 4 genotypes (Check, G 1 to G 4) are replicated.

Table 3: Data from an experiment in augmented RCBD design.

Block I

G12

G4

G11

G2

G1

G7

G3

82

81

89

79

92

96

87

${\bf Block\ II}$

G5

G9

 $\mathbf{G3}$ G1G2G479 78 81 79 81 91 **Block III** G4G2G1G6G10 G3G878 77 83 7574 78 70 This data needs to be arranged with columns showing block, genotype (or treatment) and the data of the trait for each genotype per block (Table 4).

Table 4: Data from an experiment in augmented RCBD design arranged in long-form.

 Block

 ${\bf Treatment}$

 ${\bf Trait}$

Block I

G 1

92

Block I G 2 79

Block I G 3 87

Block I
G 4
81
Block I
G 7
96
Block I
G 11
89
Block I
G 12
82
Block II
G 1
79
Block II
G 2
81
Block II
G 3
81
Block II
G 4
91
Block II
G 5
79
Block II

G 9 78 Block III G 1 83 Block III G 277 Block III G 378 Block III G 478 Block III G 8 70 Block III G 6 75 Block III G 10 74 The data for block and genotype (or treatment) can also be depicted as numbers (Table 5). Table 5: Data from an experiment in augmented RCBD design arranged in long-form (Block and Treatment as numbers). Block Treatment Trait 1 1 922 79

_

83
3
2
77
3
3
78
3
4
78
3
8
70
3
6
75
3
10
74
Multiple traits can be added as additional columns (Table 6).
Table 6: Data from an experiment in augmented RCBD design arranged in long-form (Multiple traits)
Block
Treatment
Trait1
Trait2
Block I
G 1
92
258
Block I
G 2
79
224
Block I
G 3

238
Block I
G 4
81
278
Block I
G 7
96
347
Block I
G 11
89
300
Block I
G 12
82
289
Block II
G 1
79
260
Block II
G 2
81
220
Block II
G 3
81
237
Block II
G 4
91
227
Block II

Block	Π
G 9	
78	
311	
Block	III
G 1	
83	
250	
Block	III
G 2	
77	
240	
Block	III
G 3	
78	
268	
Block	III
G 4	
78	
287	
Block	III
G 8	
70	
226	
Block	III
G 6	
75	
395	
Block	III
G 10	
74	
450	

Data should preferably be balanced i.e. all the check genotypes should be present in all the blocks. If not, a warning is issued. The number of test genotypes can vary within a block. There should not be any missing values. Rows of genotypes with missing values for one or more traits should be removed.

Such a tabular data should be imported (see section 7.8) into R as a data frame object (see section 4.3.5). The columns with the block and treatment categorical data should of the type factor (see section 4.3.2), while the column(s) with the trait data should be of the type integer or numeric (see section 4.3.1).

7 Data Analysis for a Single Trait

Analysis of data for a single trait can be performed by using augmentedRCBD function. It generates an object of class augmentedRCBD. Such an object can then be taken as input by the several functions to print the results to console (print.augmentedRCBD), generate descriptive statistics from adjusted means (describe.augmentedRCBD), plot frequency distribution (freqdist.augmentedRCBD) and computed genetic variability statistics (gva.augmentedRCBD). All these outputs can also be exported as a MS Word report using the report.augmentedRCBD function.

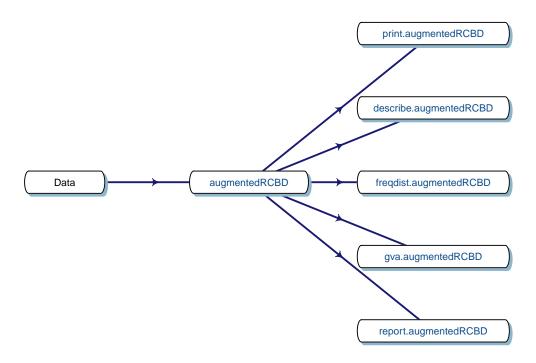


Fig. 4. Workflow for analysis of single traits with augmentedRCBD.

7.1 augmentedRCBD()

Consider the data in Table 1. The data can be imported into R as vectors as follows.

```
blk <- c(1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 3, 3)
trt <- c(1, 2, 3, 4, 7, 11, 12, 1, 2, 3, 4, 5, 9, 1, 2, 3, 4, 8, 6, 10)
```

```
y1 <- c(92, 79, 87, 81, 96, 89, 82, 79, 81, 81, 91, 79, 78, 83, 77, 78, 78,
        70, 75, 74)
y2 <- c(258, 224, 238, 278, 347, 300, 289, 260, 220, 237, 227, 281, 311, 250,
        240, 268, 287, 226, 395, 450)
```

The blk and trt vectors with the block and treatment data need to be converted into factors as follows before analysis.

```
# Convert block and treatment to factors
blk <- as.factor(blk)</pre>
trt <- as.factor(trt)</pre>
```

With the data in appropriate format, the analysis can be performed as follows for the trait y1 as follows.

```
out1 <- augmentedRCBD(blk, trt, y1, method.comp = "lsd",</pre>
                       alpha = 0.05, group = TRUE, console = TRUE)
```

Augmented Design Details

```
Number of blocks
                           11311
Number of treatments
                           "12"
Number of check treatments "4"
```

Number of test treatments "8"

Check treatments "1, 2, 3, 4"

ANOVA, Treatment Adjusted

```
Df Sum Sq Mean Sq F value Pr(>F)
Block (ignoring Treatments)
                                   2 360.1 180.04 6.675 0.0298 *
Treatment (eliminating Blocks)
                                  11 285.1
                                             25.92
                                                    0.961 0.5499
                                   3 52.9 17.64 0.654 0.6092
 Treatment: Check
 Treatment: Test and Test vs. Check 8 232.2
                                             29.02
                                                    1.076 0.4779
Residuals
                                   6 161.8
                                             26.97
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

===========

```
Df Sum Sq Mean Sq F value Pr(>F)
Treatment (ignoring Blocks)
                                        52.33
                                              1.940 0.215
                            11 575.7
 Treatment: Check
                             3
                                52.9
                                        17.64
                                               0.654 0.609
 Treatment: Test
                             7 505.9
                                              2.679 0.125
                                        72.27
 Treatment: Test vs. Check
                            1 16.9
                                        16.87
                                               0.626 0.459
Block (eliminating Treatments) 2 69.5
                                        34.75
                                               1.288 0.342
Residuals
                             6 161.8
                                        26.97
```

Treatment Means

```
Treatment Block
                  Means
                             SE r Min Max Adjusted Means
             84.66667 3.844188 3 79 92 84.66667
1
        1
2
        10
              3 74.00000 NA 1 74 74
                                             77.25000
3
             1 89.00000
                             NA 1 89 89
        11
                                             86.50000
```

4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			4.240458	10.37603
Two Test Treatments (Same Block)			7.344688	17.97180
Two Test Treatments (Different Blocks)			8.211611	20.09309
A Test Treatment and a Control Treatment			6.704752	16.40594

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12
7	7	93.50000	5.609598	6	79.77381	107.22619	2

class(out1)

[1] "augmentedRCBD"

Similarly the analysis for the trait y2 can be computed as follows.

Augmented Design Details

Number of blocks "3"
Number of treatments "12"
Number of check treatments "4"
Number of test treatments "8"

Check treatments "1, 2, 3, 4"

ANOVA, Treatment Adjusted

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Treatment Means

==========

	Treatment	Block	Means	SE	r	${\tt Min}$	Max	Adjusted Means
1	1		256.0000	3.055050	3	250	260	256.0000
2	10	3	450.0000	NA	1	450	450	437.6667
3	11	1	300.0000	NA	1	300	300	299.4167
4	12	1	289.0000	NA	1	289	289	288.4167
5	2		228.0000	6.110101	3	220	240	228.0000
6	3		247.6667	10.170764	3	237	268	247.6667
7	4		264.0000	18.681542	3	227	287	264.0000
8	5	2	281.0000	NA	1	281	281	293.9167
9	6	3	395.0000	NA	1	395	395	382.6667
10	7	1	347.0000	NA	1	347	347	346.4167
11	8	3	226.0000	NA	1	226	226	213.6667
12	9	2	311.0000	NA	1	311	311	323.9167

Coefficient of Variation

6.057617

```
Overall Adjusted Mean
```

298.4792

Standard Errors

==============

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			13.81424	33.80224
Two Test Treatments (Same Block)			23.92697	58.54719
Two Test Treatments (Different Blocks)			26.75117	65.45775
A Test Treatment and a Control Treatment			21.84224	53.44603

Treatment Groups

Method : lsd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1
3	3	247.6667	9.768146	6	223.7649	271.5685	123
1	1	256.0000	9.768146	6	232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345
11	11	299.4167	18.274527	6	254.7005	344.1328	45
9	9	323.9167	18.274527	6	279.2005	368.6328	56
7	7	346.4167	18.274527	6	301.7005	391.1328	56
6	6	382.6667	18.274527	6	337.9505	427.3828	67
10	10	437.6667	18.274527	6	392.9505	482.3828	7

class(out2)

[1] "augmentedRCBD"

The data can also be imported as a data frame and then used for analysis. Consider the data frame data imported from Table 1 according to the instructions in section 4.8.

str(data)

Augmented Design Details

Number of blocks "3"
Number of treatments "12"
Number of check treatments "4"
Number of test treatments "8"

Check treatments "1, 2, 3, 4"

ANOVA, Treatment Adjusted

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Treatment Means

==========

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

${\tt Treatment\ Groups}$

Method : lsd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12
7	7	93.50000	5.609598	6	79.77381	107.22619	2

class(out1)

[1] "augmentedRCBD"

```
# Results for variable y2
out2 <- augmentedRCBD(data$blk, data$trt, data$y2, method.comp = "lsd",</pre>
```

alpha = 0.05, group = TRUE, console = TRUE)

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

Residuals 6 1717 286

Treatment: Test and Test vs. Check 8 56815

7102 24.810 0.000473 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
Treatment (ignoring Blocks)	11	64708	5883	20.550	0.000707	***
Treatment: Check	3	2150	717	2.504	0.156116	
Treatment: Test	7	34863	4980	17.399	0.001366	**
Treatment: Test vs. Check	1	27694	27694	96.749	6.36e-05	***
Block (eliminating Treatments)	2	1277	639	2.231	0.188645	
Residuals	6	1718	286			

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Treatment Means

===========

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		256.0000	3.055050	3	250	260	256.0000
2	10	3	450.0000	NA	1	450	450	437.6667
3	11	1	300.0000	NA	1	300	300	299.4167
4	12	1	289.0000	NA	1	289	289	288.4167
5	2		228.0000	6.110101	3	220	240	228.0000
6	3		247.6667	10.170764	3	237	268	247.6667
7	4		264.0000	18.681542	3	227	287	264.0000
8	5	2	281.0000	NA	1	281	281	293.9167
9	6	3	395.0000	NA	1	395	395	382.6667
10	7	1	347.0000	NA	1	347	347	346.4167
11	8	3	226.0000	NA	1	226	226	213.6667
12	9	2	311.0000	NA	1	311	311	323.9167

Coefficient of Variation

6.057617

Overall Adjusted Mean

298.4792

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			13.81424	33.80224
Two Test Treatments (Same Block)			23.92697	58.54719
Two Test Treatments (Different Blocks)			26.75117	65.45775
${\tt A}$ Test Treatment and a Control Treatment			21.84224	53.44603

Treatment Groups

==========

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group	
8	8	213.6667	18.274527	6	168.9505	258.3828	12	
2	2	228.0000	9.768146	6	204.0982	251.9018	1	
3	3	247.6667	9.768146	6	223.7649	271.5685	123	
1	1	256.0000	9.768146	6	232.0982	279.9018	1234	
4	4	264.0000	9.768146	6	240.0982	287.9018	234	
12	12	288.4167	18.274527	6	243.7005	333.1328	345	
5	5	293.9167	18.274527	6	249.2005	338.6328	345	
11	11	299.4167	18.274527	6	254.7005	344.1328	45	
9	9	323.9167	18.274527	6	279.2005	368.6328	56	
7	7	346.4167	18.274527	6	301.7005	391.1328	56	
6	6	382.6667	18.274527	6	337.9505	427.3828	67	
10	10	437.6667	18.274527	6	392.9505	482.3828	7	
cl	ass(out2)							

[1] "augmentedRCBD"

Check genotypes are inferred by default on the basis of number of replications. However, if some test genotypes are also replicated, they may also be falsely detected as checks. To avoid this, the checks can be specified by the checks argument.

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

Df Sum Sq Mean Sq F value Pr(>F) Block (ignoring Treatments) 2 360.1 180.04 6.675 0.0298 * Treatment (eliminating Blocks) 11 285.1 25.92 0.961 0.5499 Treatment: Check 3 52.9 17.64 0.654 0.6092 Treatment: Test and Test vs. Check 8 232.2 29.02 1.076 0.4779 Residuals 6 161.8 26.97

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Df Sum Sq Mean Sq F value Pr(>F) Treatment (ignoring Blocks) 11 575.7 52.33 1.940 0.215 Treatment: Check 52.9 17.64 0.654 0.609 7 505.9 Treatment: Test 72.27 2.679 0.125 Treatment: Test vs. Check 16.9 16.87 0.626 0.459 Block (eliminating Treatments) 2 69.5 34.75 1.288 0.342 Residuals 6 161.8 26.97

Treatment Means

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

 ${\tt Coefficient\ of\ Variation}$

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

 Std. Error of Diff.
 CD (5%)

 Control Treatment Means
 4.240458 10.37603

 Two Test Treatments (Same Block)
 7.344688 17.97180

 Two Test Treatments (Different Blocks)
 8.211611 20.09309

 A Test Treatment and a Control Treatment
 6.704752 16.40594

${\tt Treatment\ Groups}$

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	73.25000	5.609598	6	59.52381	86.97619	1
9	9	77.25000	5.609598	6	63.52381	90.97619	12
10	10	77.25000	5.609598	6	63.52381	90.97619	12
5	5	78.25000	5.609598	6	64.52381	91.97619	12
6	6	78.25000	5.609598	6	64.52381	91.97619	12
2	2	79.00000	2.998456	6	71.66304	86.33696	12
12	12	79.50000	5.609598	6	65.77381	93.22619	12
3	3	82.00000	2.998456	6	74.66304	89.33696	12
4	4	83.33333	2.998456	6	75.99637	90.67029	12
1	1	84.66667	2.998456	6	77.32971	92.00363	12
11	11	86.50000	5.609598	6	72.77381	100.22619	12

```
7
          7
                  93.50000 5.609598 6 79.77381 107.22619
# Results for variable y2 (checks specified)
out2 <- augmentedRCBD(data$blk, data$trt, data$y2, method.comp = "lsd",
                    alpha = 0.05, group = TRUE, console = TRUE,
                    checks = c("1", "2", "3", "4"))
Augmented Design Details
"3"
Number of blocks
Number of treatments
                         "12"
Number of check treatments "4"
Number of test treatments "8"
Check treatments
                         "1, 2, 3, 4"
ANOVA, Treatment Adjusted
Df Sum Sq Mean Sq F value
                                                             Pr(>F)
Block (ignoring Treatments)
                                               3510 12.261 0.007597 **
                                   2
                                      7019
Treatment (eliminating Blocks)
                                               5360 18.727 0.000920 ***
                                  11 58965
 Treatment: Check
                                   3
                                       2150
                                               717
                                                    2.504 0.156116
 Treatment: Test and Test vs. Check 8 56815
                                               7102 24.810 0.000473 ***
Residuals
                                    6
                                      1717
                                                286
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
ANOVA, Block Adjusted
Df Sum Sq Mean Sq F value Pr(>F)
Treatment (ignoring Blocks)
                             11 64708
                                         5883 20.550 0.000707 ***
 Treatment: Check
                              3
                                2150
                                          717
                                              2.504 0.156116
 Treatment: Test
                              7 34863
                                         4980 17.399 0.001366 **
 Treatment: Test vs. Check
                              1 27694
                                        27694 96.749 6.36e-05 ***
Block (eliminating Treatments)
                                              2.231 0.188645
                              2 1277
                                          639
                                 1718
Residuals
                              6
                                          286
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Treatment Means
  Treatment Block
                    Means
                                 SE r Min Max Adjusted Means
                  256.0000 3.055050 3 250 260
                                                   256.0000
1
         1
2
         10
                3 450.0000
                                NA 1 450 450
                                                   437.6667
                                NA 1 300 300
3
         11
                1 300.0000
                                                  299.4167
4
         12
                1 289.0000
                                NA 1 289 289
                                                  288.4167
5
          2
                 228.0000 6.110101 3 220 240
                                                  228.0000
6
          3
                 247.6667 10.170764 3 237 268
                                                  247.6667
7
          4
                 264.0000 18.681542 3 227 287
                                                  264.0000
8
          5
                2 281.0000
                                NA 1 281 281
                                                  293.9167
9
                                NA 1 395 395
                                                  382.6667
          6
                3 395.0000
          7
               1 347.0000
                                NA 1 347 347
10
                                                  346.4167
```

11	8	3 226.0000	NA 1 226 226	213.6667
12	9	2 311.0000	NA 1 311 311	323.9167

Coefficient of Variation

6.057617

Overall Adjusted Mean

298.4792

Standard Errors

	Std.	Error	of Diff.	CD (5%)
Control Treatment Means			13.81424	33.80224
Two Test Treatments (Same Block)			23.92697	58.54719
Two Test Treatments (Different Blocks)			26.75117	65.45775
A Test Treatment and a Control Treatment			21.84224	53.44603

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1
3	3	247.6667	9.768146	6	223.7649	271.5685	123
1	1	256.0000	9.768146	6	232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345
11	11	299.4167	18.274527	6	254.7005	344.1328	45
9	9	323.9167	18.274527	6	279.2005	368.6328	56
7	7	346.4167	18.274527	6	301.7005	391.1328	56
6	6	382.6667	18.274527	6	337.9505	427.3828	67
10	10	437.6667	18.274527	6	392.9505	482.3828	7

In case the large number of treatments or genotypes, it is advisable to avoid treatment comparisons with the <code>group = FALSE</code> argument as it will be memory and processor intensive. Further it is advised to simplify output with <code>simplify = TRUE</code> in order to reduce output object size.

7.2 print.augmentedRCBD()

The results of analysis in an object of class augmented RCBD can be printed to the console as follows.

```
# Print results for variable y1
print(out1)
```

Augmented Design Details

Number of blocks "3"

```
Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"
```

ANOVA, Treatment Adjusted

	\mathtt{Df}	Sum Sq	Mean Sq	F value	Pr(>F)
Block (ignoring Treatments)	2	360.1	180.04	6.675	0.0298 *
Treatment (eliminating Blocks)	11	285.1	25.92	0.961	0.5499
Treatment: Check	3	52.9	17.64	0.654	0.6092
Treatment: Test and Test vs. Check	8	232.2	29.02	1.076	0.4779
Residuals	6	161.8	26.97		

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

${\tt ANOVA}\text{, Block Adjusted}$

	Df	Sum Sq	Mean Sq	${\tt F} \ {\tt value}$	Pr(>F)
Treatment (ignoring Blocks)	11	575.7	52.33	1.940	0.215
Treatment: Check	3	52.9	17.64	0.654	0.609
Treatment: Test	7	505.9	72.27	2.679	0.125
Treatment: Test vs. Check	1	16.9	16.87	0.626	0.459
<pre>Block (eliminating Treatments)</pre>	2	69.5	34.75	1.288	0.342
Residuals	6	161.8	26.97		

Treatment Means

	Treatment	Block	Means	SE	r	Min	Max	Adjusted Means
1	1		84.66667	3.844188	3	79	92	84.66667
2	10	3	74.00000	NA	1	74	74	77.25000
3	11	1	89.00000	NA	1	89	89	86.50000
4	12	1	82.00000	NA	1	82	82	79.50000
5	2		79.00000	1.154701	3	77	81	79.00000
6	3		82.00000	2.645751	3	78	87	82.00000
7	4		83.33333	3.929942	3	78	91	83.33333
8	5	2	79.00000	NA	1	79	79	78.25000
9	6	3	75.00000	NA	1	75	75	78.25000
10	7	1	96.00000	NA	1	96	96	93.50000
11	8	3	70.00000	NA	1	70	70	73.25000
12	9	2	78.00000	NA	1	78	78	77.25000

Coefficient of Variation

6.372367

Overall Adjusted Mean

81.0625

Standard Errors

```
Std. Error of Diff. CD (5%)
Control Treatment Means
                                                4.240458 10.37603
Two Test Treatments (Same Block)
                                                7.344688 17.97180
Two Test Treatments (Different Blocks)
                                                8.211611 20.09309
A Test Treatment and a Control Treatment
                                                6.704752 16.40594
Treatment Groups
______
Method : lsd
  Treatment Adjusted Means
                               SE df lower.CL upper.CL Group
              73.25000 5.609598 6 59.52381 86.97619
8
          8
                                                          1
9
          9
                 77.25000 5.609598 6 63.52381 90.97619
                                                          12
10
         10
                77.25000 5.609598 6 63.52381 90.97619
                                                          12
         5
                78.25000 5.609598 6 64.52381 91.97619
5
                                                          12
6
         6
                78.25000 5.609598 6 64.52381 91.97619
                                                          12
2
         2
                 79.00000 2.998456 6 71.66304 86.33696
                                                          12
              79.50000 5.609598 6 65.77381 93.22619
12
        12
                                                          12
3
         3
                82.00000 2.998456 6 74.66304 89.33696
4
          4
                83.33333 2.998456 6 75.99637 90.67029
                                                          12
                84.66667 2.998456 6 77.32971 92.00363
1
          1
                                                          12
11
         11
                86.50000 5.609598 6 72.77381 100.22619
                                                          12
7
          7
                 93.50000 5.609598 6 79.77381 107.22619
                                                           2
# Print results for variable y2
print(out2)
Augmented Design Details
"3"
Number of blocks
Number of treatments
                         "12"
Number of check treatments "4"
Number of test treatments "8"
                         "1, 2, 3, 4"
Check treatments
ANOVA, Treatment Adjusted
                                  Df Sum Sq Mean Sq F value Pr(>F)
Block (ignoring Treatments)
                                   2 7019
                                              3510 12.261 0.007597 **
Treatment (eliminating Blocks)
                                  11 58965
                                              5360 18.727 0.000920 ***
  Treatment: Check
                                   3 2150
                                              717 2.504 0.156116
                                              7102 24.810 0.000473 ***
  Treatment: Test and Test vs. Check 8 56815
Residuals
                                              286
                                      1717
```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

ANOVA, Block Adjusted

Df Sum Sq Mean Sq F value Pr(>F)
Treatment (ignoring Blocks) 11 64708 5883 20.550 0.000707 ***
Treatment: Check 3 2150 717 2.504 0.156116

323.9167

7 34863 Treatment: Test 4980 17.399 0.001366 ** Treatment: Test vs. Check 1 27694 27694 96.749 6.36e-05 *** Block (eliminating Treatments) 2 1277 639 2.231 0.188645 6 1718 286 Residuals

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Treatment Means ==========

Treatment Block Means SE r Min Max Adjusted Means 1 256.0000 3.055050 3 250 260 256.0000 1 2 10 3 450.0000 NA 1 450 450 437.6667 NA 1 300 300 3 11 1 300.0000 299.4167 1 289.0000 4 12 NA 1 289 289 288.4167 228.0000 6.110101 3 220 240 2 228.0000 5 247.6667 10.170764 3 237 268 264.0000 18.681542 3 227 287 6 3 247.6667 7 4 264.0000 2 281.0000 NA 1 281 281 8 5 293.9167 9 6 3 395.0000 NA 1 395 395 382.6667 7 1 347.0000 NA 1 347 347 10 346.4167 8 3 226.0000 NA 1 226 226 213.6667 11 NA 1 311 311

Coefficient of Variation

9

2 311.0000

6.057617

12

Overall Adjusted Mean

================

298.4792

Standard Errors

Std. Error of Diff. CD (5%) Control Treatment Means 13.81424 33.80224 Two Test Treatments (Same Block) 23.92697 58.54719 Two Test Treatments (Different Blocks) 26.75117 65.45775 A Test Treatment and a Control Treatment 21.84224 53.44603

Treatment Groups

Method : 1sd

	Treatment	Adjusted Means	SE	df	lower.CL	upper.CL	Group
8	8	213.6667	18.274527	6	168.9505	258.3828	12
2	2	228.0000	9.768146	6	204.0982	251.9018	1
3	3	247.6667	9.768146	6	223.7649	271.5685	123
1	1	256.0000	9.768146	6	232.0982	279.9018	1234
4	4	264.0000	9.768146	6	240.0982	287.9018	234
12	12	288.4167	18.274527	6	243.7005	333.1328	345
5	5	293.9167	18.274527	6	249.2005	338.6328	345

11	11	299.4167 18.274527	6 254.7005 344.1328	45
9	9	323.9167 18.274527	6 279.2005 368.6328	56
7	7	346.4167 18.274527	6 301.7005 391.1328	56
6	6	382.6667 18.274527	6 337.9505 427.3828	67
10	10	437.6667 18.274527	6 392.9505 482.3828	7

7.3 describe.augmentedRCBD()

The descriptive statistics such as count, mean, standard error, minimum, maximum, skewness (with p-value from D'Agostino test of skewness (D'Agostino (1970))) and kurtosis (with p-value from Anscombe-Glynn test of kurtosis (Anscombe and Glynn (1983))) for the adjusted means from the results in an object of class augmentedRCBD can be computed as follows.

```
# Descriptive statistics for variable y1
describe.augmentedRCBD(out1)
$Count
[1] 12
$Mean
[1] 81.0625
$Std.Error
[1] 1.547002
$Std.Deviation
[1] 5.358973
$Min
[1] 73.25
$Max
[1] 93.5
$`Skewness(statistic)`
     skew
0.9250344 1.6745760
$`Skewness(p.value)`
[1] 0.09401746
$`Kurtosis(statistic)`
    kurt
3.522807 1.282305
$`Kurtosis(p.value)`
[1] 0.1997357
# Descriptive statistics for variable y2
describe.augmentedRCBD(out2)
```

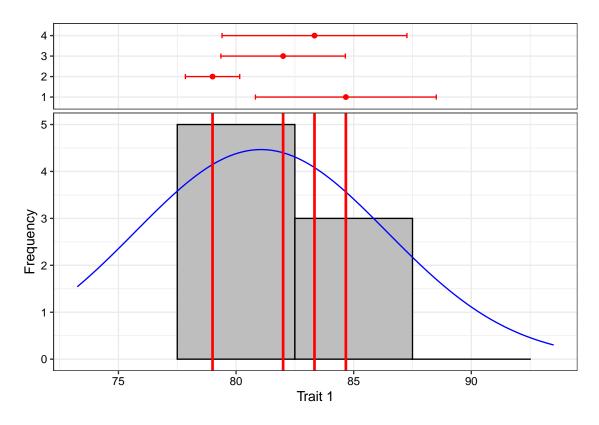
\$Count [1] 12

```
$Mean
[1] 298.4792
$Std.Error
[1] 18.92257
$Std.Deviation
[1] 65.5497
$Min
[1] 213.6667
$Max
[1] 437.6667
$`Skewness(statistic)`
     skew
0.7449405 1.3680211
$`Skewness(p.value)`
[1] 0.1713055
$`Kurtosis(statistic)`
    kurt
2.787997 0.536812
$`Kurtosis(p.value)`
[1] 0.5913975
```

7.4 freqdist.augmentedRCBD()

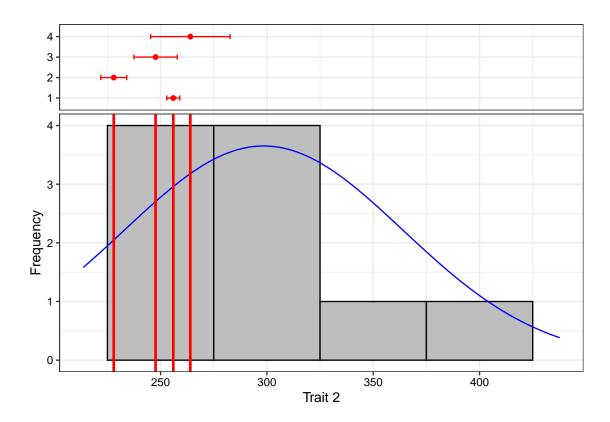
The frequency distribution of the adjusted means from the results in an object of class augmentedRCBD can be plotted as follows.

```
# Frequency distribution for variable y1
freq1 <- freqdist.augmentedRCBD(out1, xlab = "Trait 1")
Warning: Removed 2 rows containing missing values (geom_bar).
plot(freq1)</pre>
```



Frequency distribution for variable y2
freq2 <- freqdist.augmentedRCBD(out2, xlab = "Trait 2")</pre>

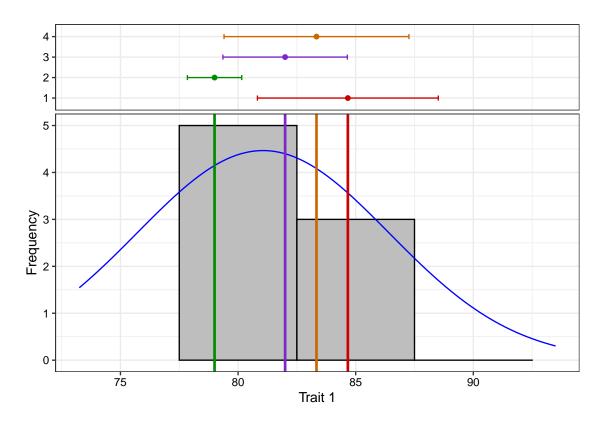
Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)



The colours for the check values may be specified using the argument check.col.

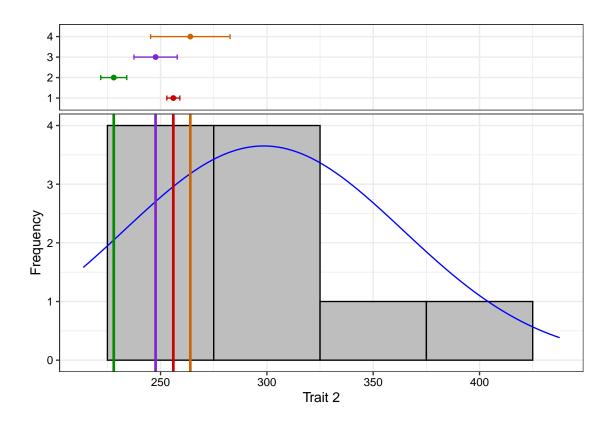
```
colset <- c("red3", "green4", "purple3", "darkorange3")
# Frequency distribution for variable y1
freq1 <- freqdist.augmentedRCBD(out1, xlab = "Trait 1", check.col = colset)</pre>
```

Warning: Removed 2 rows containing missing values (geom_bar). plot(freq1)



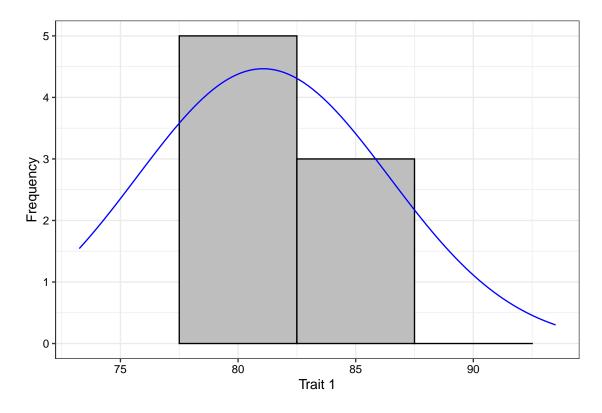
Frequency distribution for variable y2
freq2 <- freqdist.augmentedRCBD(out2, xlab = "Trait 2", check.col = colset)</pre>

Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)

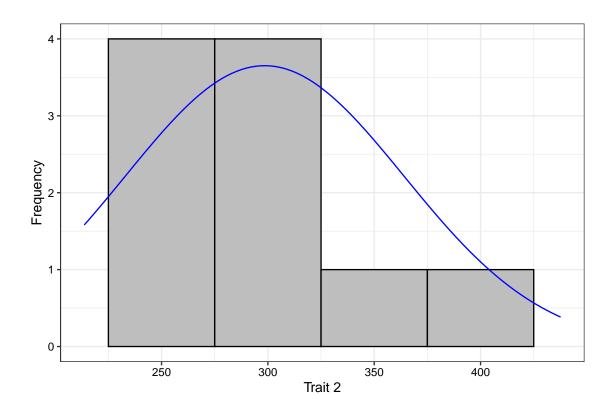


The default the check highlighting can be avoided using the argument highlight.check = FALSE.

Warning: Removed 2 rows containing missing values (geom_bar). plot(freq1)



Warning: Removed 2 rows containing missing values (geom_bar). plot(freq2)



7.5 gva.augmentedRCBD()

The genetic variability statistics such as mean, phenotypic, genotypic and environmental variation (Federer and Searle (1976)), phenotypic, genotypic and environmental coefficient of variation (Burton (1951), Burton (1952)), category of phenotypic and genotypic coefficient of variation according to Sivasubramaniam and Madhavamenon (1973), broad-sense heritability (H^2) (Lush (1940)), H^2 category according to Robinson (1966), Genetic advance (GA), genetic advance as per cent of mean (GAM) and GAM category according to Johnson et al. (1955) are computed from an object of class augmentedRCBD as follows.

Genetic variability statistics for variable y1 gva.augmentedRCBD(out1)

```
$Mean
[1] 81.0625

$PV
[1] 72.26786

$GV
[1] 45.29563

$EV
[1] 26.97222

$GCV
```

```
[1] 8.302487
$`GCV category`
[1] "Low"
$PCV
[1] 10.48703
$`PCV category`
[1] "Medium"
$ECV
[1] 6.406759
$hBS
[1] 62.67743
$`hBS category`
[1] "High"
$GA
[1] 10.99216
$GAM
[1] 13.5601
$`GAM category`
[1] "Medium"
# Genetic variability statistics for variable y2
gva.augmentedRCBD(out2)
$Mean
[1] 298.4792
$PV
[1] 4980.411
$GV
[1] 4694.161
$EV
[1] 286.25
$GCV
[1] 22.95435
$`GCV category`
[1] "High"
$PCV
[1] 23.64387
```

```
$`PCV category`
[1] "High"

$ECV
[1] 5.668377

$hBS
[1] 94.25248

$`hBS category`
[1] "High"

$GA
[1] 137.2223

$GAM
[1] 45.97382

$`GAM category`
[1] "High"
```

7.5 report.augmentedRCBD()

The results generated by the analysis can be exported to a MS Word file as follows.

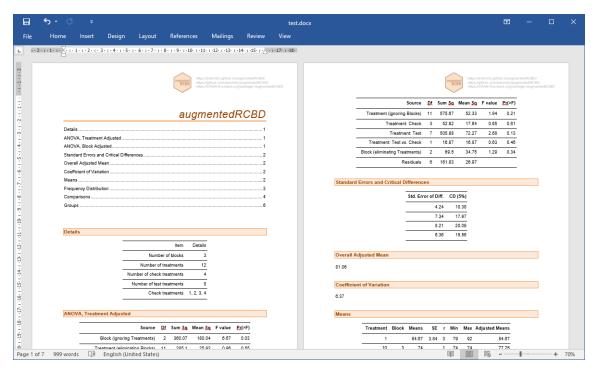


Fig. 6: MS Word report generated with report.agumentedRCBD function.

8 Data Analysis for a Multiple Traits

Analysis of data for a multiple traits simultaneously can be performed by using augmentedRCBD.bulk function. It generates an object of class augmentedRCBD.bulk. Such an object can then be taken as input by print.augmentedRCBD.bulk to print the results to console. The results can also be exported as a MS Word report using the report.augmentedRCBD.bulk function.

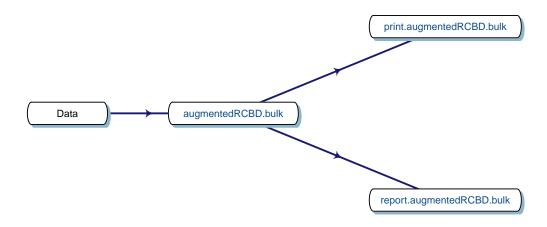


Fig. 7. Workflow for analysis of multiple traits with augmented RCBD.

8.1 augmentedRCBD.bulk()

Consider the data frame data imported from Table 1 according to the instructions in section 4.8. str(data)

```
'data.frame': 20 obs. of 4 variables:

$ blk: Factor w/ 3 levels "1","2","3": 1 1 1 1 1 1 1 2 2 2 ...

$ trt: Factor w/ 12 levels "1","2","3","4",..: 1 2 3 4 7 11 12 1 2 3 ...

$ y1 : num 92 79 87 81 96 89 82 79 81 81 ...

$ y2 : num 258 224 238 278 347 300 289 260 220 237 ...

# Convert block and treatment to factors
data$blk <- as.factor(data$blk)
data$trt <- as.factor(data$trt)
```

Rather than performing the analysis individually for each variable/trait separately using augmentedRCBD, the analysis can be performed simultaneously for for both the traits using augmentedRCBD.bulk function. It is a wrapper around the augmentedRCBD core function and its associated helper functions.

However in this case treatment comparisons/grouping by least significant difference or Tukey's honest significant difference method is not computed. Also the output object size is reduced using the simplify = TRUE argument in the augmentedRCBD function.

The logical arguments describe, freqdist and gva can be used to specify whether to generate the descriptive statistics, frequency distribution plots and genetic variability statistics respectively. If gva =

TRUE, then plots to compare phenotypic and genotypic coefficient of variation, broad sense heritability and genetic advance over mean between traits are also generated.

```
bout <- augmentedRCBD.bulk(data = data, block = "blk",</pre>
                         treatment = "trt", traits = c("y1", "y2"),
                         checks = NULL, alpha = 0.05, describe = TRUE,
                         freqdist = TRUE, gva = TRUE,
                         check.col = c("brown", "darkcyan",
                                    "forestgreen", "purple"),
                         console = TRUE)
ANOVA for y1 computed (1/2)
ANOVA for y2 computed (2/2)
Augmented Design Details
_____
                         "3"
Number of blocks
Number of treatments
                         "12"
Number of check treatments "4"
Number of test treatments "8"
Check treatments
                         "1, 2, 3, 4"
Number of traits
                         "2"
                         "y1, y2"
Traits
ANOVA, Treatment Adjusted
                            Source Df
                                             у1
        Block (ignoring Treatments) 2 180.04 *
                                                3509.67 **
1
2
     Treatment (eliminating Blocks) 11 25.92 ns 5360.49 **
3
                  Treatment: Check 3 17.64 ns
                                                716.75 ns
4 Treatment: Test and Test vs. Check 8 29.02 ns 7101.89 **
                         Residuals 6 26.97
                                                 286.25
ANOVA, Block Adjusted
_____
                        Source Df
                                        у1
                                                     y2
    Treatment (ignoring Blocks) 11 52.33 ns
1
                                             5882.5 **
2
               Treatment: Check 3 17.64 ns
                                            716.75 ns
3
      Treatment: Test vs. Check 1 16.87 ns 27694.41 **
                Treatment: Test 7 72.27 ns 4980.41 **
5 Block (eliminating Treatments) 2 34.75 ns
                                             638.58 ns
6
                     Residuals 6 26.97
                                             286.25
Coefficient of Variation
______
  Trait CV
1
    y1 6.37
```

Overall Adjusted Mean

y2 6.06

Standard Errors

Comparison y1 y2

1 A Test Treatment and a Control Treatment 6.7 21.84

2 Control Treatment Means 4.24 13.81

3 Two Test Treatments (Different Blocks) 8.21 26.75

4 Two Test Treatments (Same Block) 7.34 23.93

Critical Difference

alpha = 0.05 Comparison y1 y2

1 A Test Treatment and a Control Treatment 16.41 53.45

2 Control Treatment Means 10.38 33.8

3 Two Test Treatments (Different Blocks) 20.09 65.46

4 Two Test Treatments (Same Block) 17.97 58.55

Descriptive Statistics

Trait Count Mean Std.Error Std.Deviation Min Max Skewness Kurtosis skew...1 y1 12 81.06 1.55 5.36 73.25 93.5 0.93 ns 3.52 ns skew...2 y2 12 298.48 18.92 65.55 213.67 437.67 0.74 ns 2.79 ns

Genetic Variability Analysis

Trait Mean PV GV EV GCV.category PCV.category ECV hBS hBS.category
1 y1 81.06 72.27 45.3 26.97 8.3 Low 10.49 Medium 6.41 62.68 High
2 y2 298.48 4980.41 4694.16 286.25 22.95 High 23.64 High 5.67 94.25 High 1

Warning Messages

y1

Removed 2 rows containing missing values (geom_bar).

у2

Removed 2 rows containing missing values (geom_bar).

Treatment Means

Treatment y1 y2
1 1 84.67 256
2 10 77.25 437.67
3 11 86.5 299.42
4 12 79.5 288.42

```
5
                79
                      228
6
           3
                82 247.67
7
           4 83.33
                      264
           5 78.25 293.92
8
9
           6 78.25 382.67
           7 93.5 346.42
10
11
           8 73.25 213.67
12
           9 77.25 323.92
```

8.2 print.augmentedRCBD.bulk()

The results of analysis in an object of class augmentedRCBD.bulk can be printed to the console as follows.

```
# Print results
print(bout)
```

Augmented Design Details

```
Number of blocks "3"

Number of treatments "12"

Number of check treatments "4"

Number of test treatments "8"

Check treatments "1, 2, 3, 4"

Number of traits "2"

Traits "y1, y2"
```

ANOVA, Treatment Adjusted

```
Source Df y1 y2

1 Block (ignoring Treatments) 2 180.04 * 3509.67 **

2 Treatment (eliminating Blocks) 11 25.92 ns 5360.49 **

3 Treatment: Check 3 17.64 ns 716.75 ns

4 Treatment: Test and Test vs. Check 8 29.02 ns 7101.89 **

5 Residuals 6 26.97 286.25
```

ANOVA, Block Adjusted

```
Source Df
                                          у1
                                                      у2
1
    Treatment (ignoring Blocks) 11 52.33 ns
                                               5882.5 **
2
               Treatment: Check 3 17.64 ns
                                              716.75 ns
3
      Treatment: Test vs. Check 1 16.87 ns 27694.41 **
                Treatment: Test 7 72.27 ns
                                              4980.41 **
5 Block (eliminating Treatments) 2 34.75 ns
                                              638.58 ns
                      Residuals 6 26.97
                                              286.25
```

Coefficient of Variation

```
_____
```

```
Trait CV
1 y1 6.37
2 y2 6.06
```

Overall Adjusted Mean

Trait Overall.adjusted.mean

1 y1

81.06

y2

298.48

Standard Errors

============

Comparison y1 y2

- 1 A Test Treatment and a Control Treatment 6.7 21.84
- Control Treatment Means 4.24 13.81
- 3 Two Test Treatments (Different Blocks) 8.21 26.75
- 4 Two Test Treatments (Same Block) 7.34 23.93

Critical Difference

==========

alpha = 0.05 Comparison y1 y2

- 1 A Test Treatment and a Control Treatment $16.41\ 53.45$
- 2 Control Treatment Means 10.38 33.8
- 3 Two Test Treatments (Different Blocks) 20.09 65.46
- 4 Two Test Treatments (Same Block) 17.97 58.55

Descriptive Statistics

Trait Count Mean Std.Error Std.Deviation Min Max Skewness Kurtosis skew...1 y1 12 81.06 1.55 5.36 73.25 93.5 0.93 ns 3.52 ns skew...2 y2 12 298.48 18.92 65.55 213.67 437.67 0.74 ns 2.79 ns

Genetic Variability Analysis

Trait Mean PV ${\tt GV}$ GCV GCV.category PCV PCV.category ECV hBS hBS.category ΕV y1 81.06 72.27 45.3 26.97 8.3 Low 10.49 Medium 6.41 62.68 High y2 298.48 4980.41 4694.16 286.25 22.95 High 23.64 High 5.67 94.25 High 1

Warning Messages

y 1

Removed 2 rows containing missing values (geom_bar).

у2

Removed 2 rows containing missing values (geom_bar).

Treatment Means

=========

Treatment y1 y2
1 1 84.67 256
2 10 77.25 437.67

```
3
          11 86.5 299.42
4
          12 79.5 288.42
5
                79
                       228
6
           3
                82 247.67
7
           4 83.33
                       264
           5 78.25 293.92
8
9
           6 78.25 382.67
10
           7 93.5 346.42
           8 73.25 213.67
11
           9 77.25 323.92
12
```

8.3 report.augmentedRCBD.bulk()

The results generated by the analysis can be exported to a MS Word file as follows.

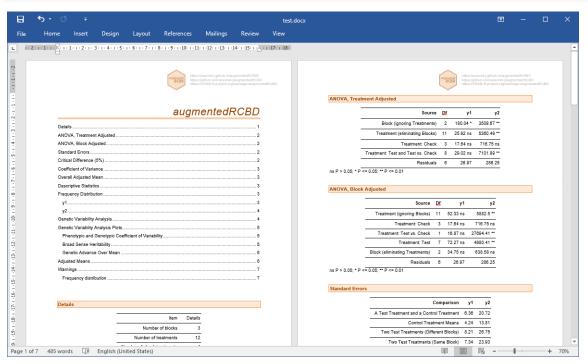


Fig. 8: MS Word report generated with report.agumentedRCBD.bulk function.

9 Citing augmentedRCBD

To cite the R package 'augmentedRCBD' in publications use:

Aravind, J., Mukesh Sankar, S., Wankhede, D. P., and Kaur, V. (2021). augmentedRCBD: Analysis of A Complete Block Designs. R package version 0.1.4.9000,

 $\verb|https://aravind-j.github.io/augmentedRCBD/https://cran.r-project.org/package=augmentedRCBD.||$

[64] xmlparsedata_1.0.5 curl_4.3

[71] gdtools_0.2.3

[85] evaluate_0.14

[92] magrittr_2.0.1

[99] withr_2.4.1

[106] utf8_1.2.1

[78] zip_2.1.1

```
A BibTeX entry for LaTeX users is
  @Manual{,
    title = {augmentedRCBD: Analysis of Augmented Randomised Complete Block Designs},
    author = {J. Aravind and S. {Mukesh Sankar} and Dhammaprakash Pandhari Wankhede and Vikender Kaur
    year = \{2021\},\
    note = {R package version 0.1.4.9000},
    note = {https://aravind-j.github.io/augmentedRCBD/},
    note = {https://cran.r-project.org/package=augmentedRCBD},
This free and open-source software implements academic research by the authors and co-workers. If you
support the project by citing the package.
10 Session Info
sessionInfo()
R Under development (unstable) (2021-04-01 r80137)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19042)
Matrix products: default
locale:
[1] LC_COLLATE=English_India.1252 LC_CTYPE=English_India.1252
                                                                   LC_MONETARY=English_India.1252 LC_N
[5] LC_TIME=English_India.1252
attached base packages:
[1] stats
              graphics grDevices utils
                                             datasets methods
                                                                 base
other attached packages:
[1] diagram_1.6.5
                             shape_1.4.5
                                                       augmentedRCBD_0.1.4.9000 kableExtra_1.3.4
loaded via a namespace (and not attached):
  [1] TH.data_1.0-10
                         colorspace_2.0-0
                                             ellipsis_0.3.1
                                                                rprojroot_2.0.2
                                                                                    estimability_1.3
  [8] fs_1.5.0
                         rstudioapi_0.13
                                             farver_2.1.0
                                                                roxygen2_7.1.1
                                                                                    remotes_2.3.0
 [15] xml2_1.3.2
                         codetools_0.2-18
                                             splines_4.1.0
                                                                cachem_1.0.4
                                                                                    knitr_1.31
                         whoami_1.3.0
                                             compiler_4.1.0
                                                                httr_1.4.2
 [22] rematch_1.0.1
                                                                                    emmeans_1.5.5-1
 [29] fastmap_1.1.0
                         lazyeval_0.2.2
                                             cli_2.3.1
                                                                htmltools_0.5.1.1
                                                                                   prettyunits_1.1.1
 [36] gtable_0.3.0
                         glue_1.4.2
                                             reshape2_1.4.4
                                                                dplyr_1.0.5
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                                                                svglite_2.0.0
 [43] xopen_1.0.0
                         vctrs_0.3.7
                                             debugme_1.1.0
                                                                                   xfun_0.22
 [50] ps_1.6.0
                         testthat_3.0.2
                                             rvest_1.0.0
                                                                parsedate_1.2.0
                                                                                   lifecycle_1.0.0
 [57] goodpractice_1.0.2 MASS_7.3-53.1
                                             zoo_1.8-9
                                                                                    clisymbols_1.2.0
                                                                scales_1.1.1
```

yaml_2.2.1

stringi_1.5.3

 ${\tt generics_0.1.0}$

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Rdpack_2.1.1

purrr_0.3.4

memoise_2.0.0

rlang_0.4.10

tibble_3.1.0

officer_0.3.18

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highr_0.8

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pkgconfig_2.0.3

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usethis_2.0.1

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bitops_1.0-6

R6_2.5.0

rhub_1.1.1

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References

- Anscombe, F. J., and Glynn, W. J. (1983). Distribution of the kurtosis statistic b_2 for normal samples. Biometrika 70, 227–234. doi:10.1093/biomet/70.1.227.
- Burton, G. W. (1951). Quantitative inheritance in pearl millet (*Pennisetum glaucum*). Agronomy Journal 43, 409–417. doi:10.2134/agronj1951.00021962004300090001x.
- Burton, G. W. (1952). Qualitative inheritance in grasses. Vol. 1. in *Proceedings of the 6th International Grassland Congress, Pennsylvania State College*, 17–23.
- D'Agostino, R. B. (1970). Transformation to normality of the null distribution of g_1 . Biometrika 57, 679–681. doi:10.1093/biomet/57.3.679.
- Federer, W. T. (1956b). Augmented (or Hoonuiaku) designs. The Hawaiian Planters' Record LV(2), 191–208.
- Federer, W. T. (1956a). Augmented (or Hoonuiaku) Designs. Cornell University, New York Available at: https://ecommons.cornell.edu/handle/1813/32841.
- Federer, W. T. (1961). Augmented designs with one-way elimination of heterogeneity. *Biometrics* 17, 447–473. doi:10.2307/2527837.
- Federer, W. T., and Searle, S. R. (1976). Model Considerations and Variance Component Estimation in Augmented Completely Randomized and Randomized Complete Blocks Designs-Preliminary Version. Cornell University, New York Available at: https://hdl.handle.net/1813/32691.
- Johnson, H. W., Robinson, H. F., and Comstock, R. E. (1955). Estimates of genetic and environmental variability in soybeans. *Agronomy journal* 47, 314–318. doi:10.2134/agronj1955.00021962004700070009x.
- Lush, J. L. (1940). Intra-sire correlations or regressions of offspring on dam as a method of estimating heritability of characteristics. *Proceedings of the American Society of Animal Nutrition* 1940, 293–301. doi:10.2527/jas1940.19401293x.
- Robinson, H. F. (1966). Quantitative genetics in relation to breeding on centennial of Mendelism. *Indian Journal of Genetics and Plant Breeding*, 171.
- Sivasubramaniam, S., and Madhavamenon, P. (1973). Genotypic and phenotypic variability in rice. *The Madras Agricultural Journal* 60, 1093–1096.
- Tippmann, S. (2015). Programming tools: Adventures with R. Nature News 517, 109. doi:10.1038/517109a.