

The `germinationmetrics` Package: A Brief Introduction

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Overview

The package `germinationmetrics` is a collection of functions which implements various methods for describing the time-course of germination in terms of single-value germination indices as well as fitted curves.

The goal of this vignette is to introduce the users to these functions and get started in describing sequentially recorded germination count data. This document assumes a basic knowledge of R programming language.

Installation

The package can be installed using the following functions:

```
# Install from CRAN
install.packages('germinationmetrics', dependencies=TRUE)

# Install development version from Github
devtools::install_github("aravind-j/germinationmetrics")
```

Then the package can be loaded using the function

```
library(germinationmetrics)
```



Version History

The current version of the package is 0.1.9. The previous versions are as follows.

Table 1. Version history of `germinationmetrics` R package.

Version	Date
0.1.0	2018-04-17
0.1.1	2018-07-26
0.1.1.1	2018-10-16
0.1.2	2018-10-31
0.1.3	2019-01-19
0.1.4	2020-06-16
0.1.5	2021-02-17
0.1.6	2022-06-15
0.1.7	2022-08-28

To know detailed history of changes use `news(package='germinationmetrics')`.

Germination count data

Typically in a germination test, the germination count data of a fixed number of seeds is recorded at regular intervals for a definite period of time or until all the seeds have germinated. These germination count data can be either partial or cumulative (Table 2).

Table 2 : A typical germination count data.

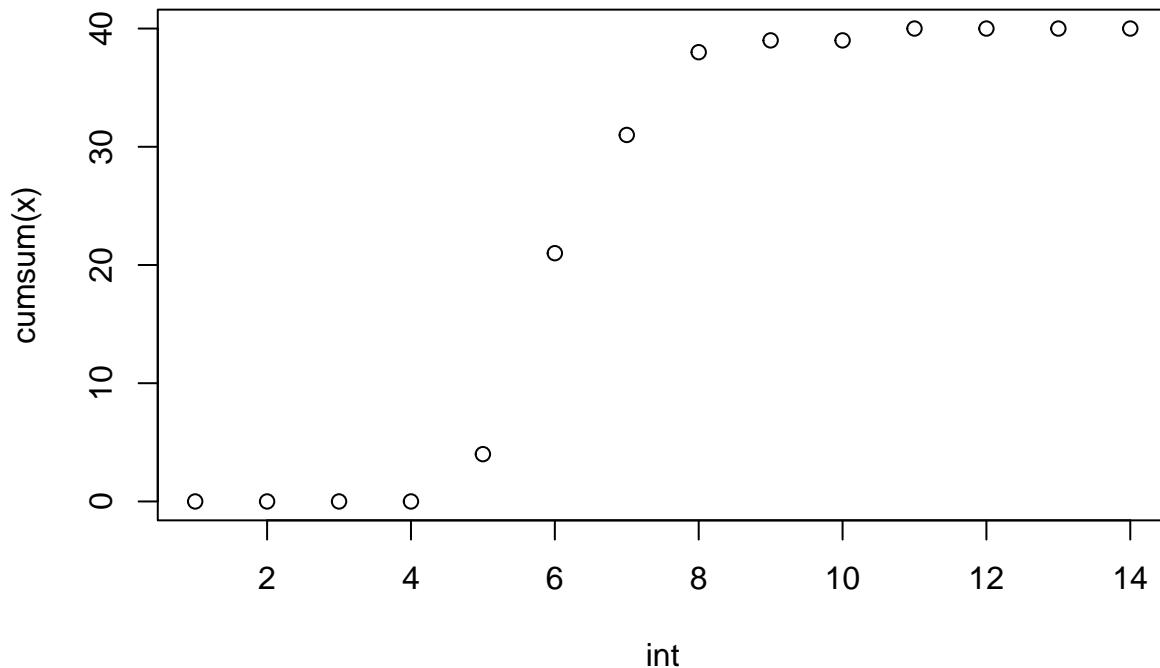
intervals	counts	cumulative.counts
1	0	0
2	0	0
3	0	0
4	0	0
5	4	4
6	17	21
7	10	31
8	7	38
9	1	39
10	0	39
11	1	40
12	0	40
13	0	40
14	0	40

The time-course of germination can be plotted as follows.

```
data <- data.frame(intervals = 1:14,
                    counts = c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0))

# Partial germination counts
x <- data$counts
# Cumulative germination counts
y <- cumsum(x)
# Time intervals of observations
```

```
int <- data$intervals  
plot(int, cumsum(x))
```



Single-value germination indices

The details about the single-value germination indices implemented in `germinationmetrics` are described in Table 3.

Table 3 : Single-value germination indices implemented in `germinationmetrics`.

Germination index	Function	Details	Unit	Measures	Reference
Germination percentage or Final germination percentage or Germinability (GP)	<code>GermPercent</code>	<p>It is computed as follows.</p> $GP = \frac{N_g}{N_t} \times 100$ <p>Where, N_g is the number of germinated seeds and N_t is the total number of seeds.</p>	Percentage (%)	Germination capacity	ISTA (2015)
Peak germination percentage (PGP)	<code>PeakGermPercent</code>	<p>It is computed as follows.</p> $PGP = \frac{N_{max}}{N_t} \times 100$ <p>Where, N_{max} is the maximum number of seeds germinated per interval.</p>	Percentage (%)	Germination capacity	Vallance (1950); Roh et al. (2004)
Time for the first germination or Germination time lag (t_0)	<code>FirstGermTime</code>	<p>It is the time for first germination to occur (e.g. First day of germination).</p> $t_0 = \min \{T_i : N_i \neq 0\}$ <p>Where, T_i is the time from the start of the experiment to the ith interval and N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval)</p>	time	Germination time	Edwards (1932); Czabator (1962); Goloff and Bazzaz (1975); Labouriau (1983a); Ranal (1999); Quintanilla et al. (2000)
Time for the last germination (t_g)	<code>LastGermTime</code>	<p>It is the time for last germination to occur (e.g. Last day of germination)</p> $t_g = \max \{T_i : N_i \neq 0\}$ <p>Where, T_i is the time from the start of the experiment to the ith interval and N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval)</p>	time	Germination time	Edwards (1932)
Time spread of germination or Germination distribution	<code>TimeSpreadGerm</code>	<p>It is the difference between time for last germination (t_g) and time for first germination (t_0).</p> $\text{Time spread of germination} = t_g - t_0$	time	Germination time	Al-Mudaris (1998); Schrader and Graves (2000); Kader (2005)
Peak period of germination or Modal time of germination (t_{peak})	<code>PeakGermTime</code>	<p>It is the time in which highest frequency of germinated seeds are observed and need not be unique.</p> $t_{peak} = \{T_i : N_i = N_{max}\}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval) and N_{max} is the maximum number of seeds germinated per interval.</p>	time	Germination time	Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Median germination time (t_{50}) (Coolbear)	<code>t50</code>	<p>It is the time to reach 50% of final/maximum germination. With argument <code>method</code> specified as "coolbear", it is computed as follows.</p> $t_{50} = T_i + \frac{\left(\frac{N+1}{2} - N_i\right)(T_j - T_i)}{N_j - N_i}$ <p>Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N+1}{2} < N_j$.</p>	time	Germination time	Coolbear et al. (1984)
Median germination time (t_{50}) (Farooq)	<code>t50</code>	<p>With argument <code>method</code> specified as "farooq", it is computed as follows.</p> $t_{50} = T_i + \frac{\left(\frac{N}{2} - N_i\right)(T_j - T_i)}{N_j - N_i}$ <p>Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N}{2} < N_j$.</p>	time	Germination time	Farooq et al. (2005)
Mean germination time or Mean length of incubation time (\bar{T}) or Germination resistance (GR) or Sprouting index (SI) or Emergence index (EI)	<code>MeanGermTime</code>	<p>It is the average length of time required for maximum germination of a seed lot and is estimated according to the following formula.</p> $\bar{T} = \frac{\sum_{i=1}^k N_i T_i}{\sum_{i=1}^k N_i}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p> <p>It is the inverse of mean germination rate (\bar{V}).</p> $\bar{T} = \frac{1}{\bar{V}}$	time	Germination time	Edmond and Drapala (1958); Czabator (1962); Smith and Millet (1964); Gordon (1969); Gordon (1971); Mock and Eberhart (1972); Ellis and Roberts (1980) Labouriau (1983a); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Variance of germination time (s_T^2)	VarGermTime	<p>It is computed according to the following formula.</p> $s_T^2 = \frac{\sum_{i=1}^k N_i(T_i - \bar{T})^2}{\sum_{i=1}^k N_i - 1}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p>	time ⁻¹	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Standard error of germination time ($s_{\bar{T}}$)	SEGermTime	<p>It signifies the accuracy of the calculation of the mean germination time.</p> <p>It is estimated according to the following formula:</p> $s_{\bar{T}} = \sqrt{\frac{s_T^2}{\sum_{i=1}^k N_i}}$ <p>Where, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval) and k is the total number of time intervals.</p>	time	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Mean germination rate (\bar{V})	MeanGermRate	<p>It is computed according to the following formula:</p> $\bar{V} = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p> <p>It is the inverse of mean germination time (\bar{T}).</p> $\bar{V} = \frac{1}{\bar{T}}$	time ⁻¹	Germination rate	Labouriau and Valadares (1976); Labouriau (1983b); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Coefficient of velocity of germination (<i>CVG</i>) or Coefficient of rate of germination (<i>CRG</i>) or Kotowski's coefficient of velocity	CVG	<p>It is estimated according to the following formula.</p> $CVG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i} \times 100$ $CVG = \bar{V} \times 100$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p>	% time ⁻¹	Germination rate	Kotowski (1926), Nichols and Heydecker (1968); Bewley and Black (1994); Labouriau (1983b); Scott et al. (1984)
Variance of germination rate (s_V^2)	VarGermRate	<p>It is calculated according to the following formula.</p> $s_V^2 = \bar{V}^4 \times s_T^2$ <p>Where, s_T^2 is the variance of germination time.</p>	time ⁻²	Germination rate	Labouriau (1983b); Ranal and Santana (2006)
Standard error of germination rate ($s_{\bar{V}}$)	SEGermRate	<p>It is estimated according to the following formula.</p> $s_{\bar{V}} = \sqrt{\frac{s_V^2}{\sum_{i=1}^k N_i}}$ <p>Where, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p>	time ⁻¹	Germination rate	Labouriau (1983b); Ranal and Santana (2006)
Germination rate as the reciprocal of the median time (v_{50})	GermRateRecip	<p>It is the reciprocal of the median germination time (t_{50}).</p> $v_{50} = \frac{1}{t_{50}}$	time ⁻¹	Germination rate	Went (1957); Labouriau (1983b); Ranal and Santana (2006)
Speed of germination (S) or Germination rate Index or index of velocity of germination or Emergence rate index (Allan, Vogel and Peterson; Erbach; Hsu and Nelson) or Germination index (AOSA)	GermSpeed	<p>It is the rate of germination in terms of the total number of seeds that germinate in a time interval. It is estimated as follows.</p> $S = \sum_{i=1}^k \frac{N_i}{T_i}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of germination.</p>	% time ⁻¹ or count time ⁻¹	Mixed	Throneberry and Smith (1955); Maguire (1962); Allan et al. (1962); Kendrick and Frankland (1969); Bouton et al. (1976); Erbach (1982); AOSA (1983); Khandakar and Bradbeer (1983); Hsu and Nelson (1986); Bradbeer (1988); Wardle et al. (1991)

Germination index	Function	Details	Unit	Measures	Reference
Speed of accumulated germination ($S_{\text{accumulated}}$)	GermSpeedAccumulate	<p>It is the rate of germination in terms of the accumulated/cumulative total number of seeds that germinate in a time interval.</p> <p>It is estimated as follows.</p> $S_{\text{accumulated}} = \sum_{i=1}^k \frac{\sum_{j=1}^i N_j}{T_i}$ <p>Where, T_i is the time from the start of the experiment to the ith interval, $\sum_{j=1}^i N_j$ is the cumulative/accumulated number of seeds germinated in the ith interval, and k is the total number of time intervals.</p> <p>Instead of germination counts, germination percentages may also be used for computation of speed of germination.</p>	% time ⁻¹ or count time ⁻¹	Mixed	Bradbeer (1988); Wardle et al. (1991); Haugland and Brandsaeter (1996); Santana and Ranal (2004)
Corrected speed of germination or Corrected germination rate index (\hat{S})	GermSpeedCorrected	<p>It is computed as follows.</p> $S_{\text{corrected}} = \frac{S}{FGP}$ <p>Where, S is the germination speed computed with germination percentage instead of counts and FGP is the final germination percentage or germinability.</p> <p>It can also be computed from speed of accumulated germination (computed with germination percentage).</p> $\hat{S}_{\text{accumulated}} = \frac{S_{\text{accumulated}}}{FGP}$ <p>Where, $S_{\text{accumulated}}$ is the speed of accumulated germination computed with germination percentage instead of counts and FGP is the final germination percentage or germinability.</p>	time ⁻¹	Mixed	Evetts and Burnside (1972)
Weighted germination percentage (WGP)	WeightGermPercent	<p>It is estimated as follows.</p> $WGP = \frac{\sum_{i=1}^k (k - i + 1)N_i}{k \times N} \times 100$ <p>Where, N_i is the number of seeds that germinated in the time interval i (not cumulative, but partial count), N is the total number of seeds tested, and k is the total number of time intervals.</p>	Percentage (%)	Mixed	Reddy et al. (1985); Reddy (1978)
Mean germination percentage per unit time (\overline{GP})	MeanGermPercent	<p>It is estimated as follows.</p> $\overline{GP} = \frac{GP}{T_k}$ <p>Where, GP is the final germination percentage, T_k is the time at the kth time interval, and k is the total number of time intervals required for final germination.</p>	% time ⁻¹	Mixed	Czabator (1962)

Germination index	Function	Details	Unit	Measures	Reference
Number of seeds germinated per unit time \bar{N}	<code>MeanGermNumber</code>	<p>It is estimated as follows.</p> $\bar{N} = \frac{N_g}{T_k}$ <p>Where, N_g is the number of germinated seeds at the end of the germination test, T_k is the time at the kth time interval, and k is the total number of time intervals required for final germination.</p>	count time ⁻¹	Mixed	Khamassi et al. (2013)
Timson's index [$\sum 10$ (Ten summation), $\sum 5$ or $\sum 20$] or Germination energy index (GEI)	<code>TimsonsIndex</code>	<p>It is the progressive total of cumulative germination percentage recorded at specific intervals for a set period of time and is estimated in terms of cumulative germination percentage (G_i) as follows.</p> $\Sigma k = \sum_{i=1}^k G_i$ <p>Where, G_i is the cumulative germination percentage in time interval i, and k is the total number of time intervals.</p> <p>It also estimated in terms of partial germination percentage as follows.</p> $\Sigma k = \sum_{i=1}^k g_i(k - j)$ <p>Where, g_i is the germination (not cumulative, but partial germination) in time interval i (i varying from 0 to k), k is the total number of time intervals, and $j = i - 1$.</p>	Percentage (%)	Mixed	Grose and Zimmer (1958); Timson (1965); Lyon and Coffelt (1966); Chaudhary and Ghildyal (1970); Negm and Smith (1978); Brown and Mayer (1988); Baskin and Baskin (1998); Goodchild and Walker (1971)
Modified Timson's index (Σk_{mod}) (Labouriau)	<code>TimsonsIndex</code>	<p>It is estimated as Timson's index Σk divided by the sum of partial germination percentages.</p> $\Sigma k_{mod} = \frac{\Sigma k}{\sum_{i=1}^k g_i}$	no unit	Mixed	Ranal and Santana (2006)
Modified Timson's index (Σk_{mod}) (Khan and Unger)	<code>TimsonsIndex</code>	<p>It is estimated as Timson's index (Σk) divided by the total time period of germination (T_k).</p> $\Sigma k_{mod} = \frac{\Sigma k}{T_k}$	% time ⁻¹	Mixed	Khan and Ungar (1984)

Germination index	Function	Details	Unit	Measures	Reference
George's index (GR)	<code>GermRateGeorge</code>	It is estimated as follows. $GR = \sum_{i=1}^k N_i K_i$ Where N_i is the number of seeds germinated by i th interval and K_i is the number of intervals(eg. days) until the end of the test, and k is the total number of time intervals.	count time	Mixed	George (1961); Tucker and Wright (1965); Nichols and Heydecker (1968);Chopra and Chaudhary (1980)
Germination Index (GI) (Melville)	<code>GermIndex</code>	It is estimated as follows. $GI = \sum_{i=1}^k \frac{ (T_k - T_i) N_i }{N_t}$ Where, T_i is the time from the start of the experiment to the i th interval (day for the example), N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), N_t is the total number of seeds used in the test, and k is the total number of time intervals.	time	Mixed	Melville et al. (1980)
Germination Index (GI_{mod}) (Melville; Santana and Ranal)	<code>GermIndex</code>	It is estimated as follows. $GI_{mod} = \sum_{i=1}^k \frac{ (T_k - T_i) N_i }{N_g}$ Where, T_i is the time from the start of the experiment to the i th interval (day for the example), N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), N_g is the total number of germinated seeds at the end of the test, and k is the total number of time intervals.	time	Mixed	Melville et al. (1980); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index (ERI) or Germination Rate Index (Shmueli and Goldberg)	<code>EmergenceRateIndex</code>	It is estimated as follows. $ERI = \sum_{i=i_0}^{k-1} N_i(k-i)$ Where, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.	count	Mixed	Shmueli and Goldberg (1971)

Germination index	Function	Details	Unit	Measures	Reference
Modified Emergence Rate Index (ERI_{mod}) or Modified Germination Rate Index (Shmueli and Goldberg; Santana and Ranal)	<code>EmergenceRateIndex</code>	<p>It is estimated by dividing Emergence rate index (ERI) by total number of emerged seedlings (or germinated seeds).</p> $ERI_{mod} = \frac{\sum_{i=i_0}^{k-1} N_i(k-i)}{N_g} = \frac{ERI}{N_g}$ <p>Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.</p>	no unit	Mixed	Shmueli and Goldberg (1971); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index (ERI) or Germination Rate Index (Bilbro & Wanjura)	<code>EmergenceRateIndex</code>	<p>It is the estimated as follows.</p> $ERI = \frac{\sum_{i=1}^k N_i}{\bar{T}} = \frac{N_g}{\bar{T}}$ <p>Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and \bar{T} is the mean germination time or mean emergence time.</p>	count time ⁻¹	Mixed	Bilbro and Wanjura (1982)
Emergence Rate Index (ERI) or Germination Rate Index (Fakorede)	<code>EmergenceRateIndex</code>	<p>It is estimated as follows.</p> $ERI = \frac{\bar{T}}{FGP/100}$ <p>Where, \bar{T} is the Mean germination time and FGP is the final germination time.</p>	time count ⁻¹	Mixed	Fakorede and Ayoola (1980); Fakorede and Ojo (1981); Fakorede and Agbana (1983)
Peak value(PV) (Czabator) or Emergence Energy (EE)	<code>PeakValue</code>	<p>It is the accumulated number of seeds germinated at the point on the germination curve at which the rate of germination starts to decrease. It is computed as the maximum quotient obtained by dividing successive cumulative germination values by the relevant incubation time.</p> $PV = \max \left(\frac{G_1}{T_1}, \frac{G_2}{T_2}, \dots, \frac{G_k}{T_k} \right)$ <p>Where, T_i is the time from the start of the experiment to the ith interval, G_i is the cumulative germination percentage in the ith time interval, and k is the total number of time intervals.</p>	% time ⁻¹	Mixed	Czabator (1962); Bonner (1967)

Germination index	Function	Details	Unit	Measures	Reference
Germination value (GV) (Czabator)	GermValue	<p>It is computed as follows.</p> $GV = PV \times MDG$ <p>Where, PV is the peak value and MDG is the mean daily germination percentage from the onset of germination.</p> <p>It can also be computed for other time intervals of successive germination counts, by replacing MDG with the mean germination percentage per unit time (GP).</p> <p>GV value can be modified (GV_{mod}), to consider the entire duration from the beginning of the test instead of just from the onset of germination.</p>	% ² time ⁻²	Mixed	Czabator (1962); Brown and Mayer (1988)
Germination value (GV) (Diavanshir and Pourbiek)	GermValue	<p>It is computed as follows.</p> $GV = \frac{\sum DGS}{N} \times GP \times c$ <p>Where, DGS is the daily germination speed computed by dividing cumulative germination percentage by the number of days since the onset of germination, N is the frequency or number of DGS calculated during the test, GP is the germination percentage expressed over 100, and c is a constant. The value of c is decided on the basis of average daily speed of germination ($\frac{\sum DGS}{N}$). If it is less than 10, then c value of 10 can be used and if it is more than 10, then value of 7 or 8 can be used for c.</p> <p>GV value can be modified (GV_{mod}), to consider the entire duration from the beginning of the test instead of just from the onset of germination.</p>	% ² time ⁻¹	Mixed	Djavanshir and Pourbeik (1976); Brown and Mayer (1988)
Coefficient of uniformity of germination (CUG)	CUGerm	<p>It is computed as follows.</p> $CUG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k (\bar{T} - T_i)^2 N_i}$ <p>Where, \bar{T} is the mean germination time, T_i is the time from the start of the experiment to the ith interval (day for the example), N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.</p>	time ⁻²	Germination uniformity	Heydecker (1972); Bewley and Black (1994)
Coefficient of variation of the germination time (CV _T)	CVGermTime	<p>It is estimated as follows.</p> $CV_T = \sqrt{\frac{s_T^2}{\bar{T}}}$ <p>Where, s_T^2 is the variance of germination time and \bar{T} is the mean germination time.</p>	no unit	Germination uniformity	Gomes (1960); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Synchronization index (\bar{E}) or Uncertainty of the germination process (U) or informational entropy (H)	GermUncertainty	<p>It is estimated as follows.</p> $\bar{E} = - \sum_{i=1}^k f_i \log_2 f_i$ <p>Where, f_i is the relative frequency of germination ($f_i = \frac{N_i}{\sum_{i=1}^k N_i}$), N_i is the number of seeds germinated on the ith time interval, and k is the total number of time intervals.</p>	bit	Germination synchrony	Shannon (1948); Labouriau and Valadares (1976); Labouriau (1983b)
Synchrony of germination (Z index)	GermSynchrony	<p>It is computed as follows.</p> $Z = \frac{\sum_{i=1}^k C_{N_i,2}}{C_{\Sigma N_i,2}}$ <p>Where, $C_{N_i,2}$ is the partial combination of the two germinated seeds from among N_i, the number of seeds germinated on the ith time interval (estimated as $C_{N_i,2} = \frac{N_i(N_i-1)}{2}$), and $C_{\Sigma N_i,2}$ is the partial combination of the two germinated seeds from among the total number of seeds germinated at the final count, assuming that all seeds that germinated did so simultaneously.</p>	no unit	Germination synchrony	Primack (1985); Ranal and Santana (2006)

Examples

```

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z <- c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)

# From partial germination counts
#-----
GermPercent(germ.counts = x, total.seeds = 50)

GermPercent()
[1] 80

PeakGermPercent(germ.counts = x, intervals = int, total.seeds = 50)
[1] 34

# For multiple peak germination times
PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50)

Warning in PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50): Multiple peak germination times exist.
[1] 22

# From cumulative germination counts
#-----
GermPercent(germ.counts = y, total.seeds = 50, partial = FALSE)

[1] 80

PeakGermPercent(germ.counts = y, intervals = int, total.seeds = 50,
                 partial = FALSE)
[1] 34

# For multiple peak germination times
PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50,
                 partial = FALSE)

Warning in PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50, : Multiple peak germination times exist.
[1] 22

# From number of germinated seeds
#-----
GermPercent(germinated.seeds = 40, total.seeds = 50)

[1] 80

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z <- c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)

# From partial germination counts

```

```

#-----
FirstGermTime(germ.counts = x, intervals = int)

FirstGermTime(), LastGermTime(), PeakGermTime(), TimeSpreadGerm()

[1] 5
LastGermTime(germ.counts = x, intervals = int)

[1] 11
TimeSpreadGerm(germ.counts = x, intervals = int)

[1] 6
PeakGermTime(germ.counts = x, intervals = int)

[1] 6
# For multiple peak germination times
PeakGermTime(germ.counts = z, intervals = int)

Warning in PeakGermTime(germ.counts = z, intervals = int): Multiple peak germination times exist.

[1] 5 6
# From cumulative germination counts
#-----
FirstGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 5
LastGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 11
TimeSpreadGerm(germ.counts = y, intervals = int, partial = FALSE)

[1] 6
PeakGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 6
# For multiple peak germination time
PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE)

Warning in PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE): Multiple peak germinations exist.

[1] 5 6

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----
t50(germ.counts = x, intervals = int, method = "coolbear")

t50()

```

```
[1] 5.970588
t50(germ.counts = x, intervals = int, method = "farooq")

[1] 5.941176
# From cumulative germination counts
#-----
t50(germ.counts = y, intervals = int, partial = FALSE, method = "coolbear")

[1] 5.970588
t50(germ.counts = y, intervals = int, partial = FALSE, method = "farooq")

[1] 5.941176

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----
MeanGermTime(germ.counts = x, intervals = int)

MeanGermTime(), VarGermTime(), SEGermTime(), CVGermTime()

[1] 6.7
VarGermTime(germ.counts = x, intervals = int)

[1] 1.446154
SEGermTime(germ.counts = x, intervals = int)

[1] 0.1901416
CVGermTime(germ.counts = x, intervals = int)

[1] 0.1794868

# From cumulative germination counts
#-----
MeanGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 6.7
VarGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 1.446154
SEGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 0.1901416
CVGermTime(germ.counts = y, intervals = int, partial = FALSE)

[1] 0.1794868

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
```

```

int <- 1:length(x)

# From partial germination counts
#-----
MeanGermRate(germ.counts = x, intervals = int)

MeanGermRate(), CVG(), VarGermRate(), SEGermRate(), GermRateRecip()

[1] 0.1492537

CVG(germ.counts = x, intervals = int)

[1] 14.92537

VarGermRate(germ.counts = x, intervals = int)

[1] 0.0007176543

SEGermRate(germ.counts = x, intervals = int)

[1] 0.004235724

GermRateRecip(germ.counts = x, intervals = int, method = "coolbear")

[1] 0.1674877

GermRateRecip(germ.counts = x, intervals = int, method = "farooq")

[1] 0.1683168

# From cumulative germination counts
#-----
MeanGermRate(germ.counts = y, intervals = int, partial = FALSE)

[1] 0.1492537

CVG(germ.counts = y, intervals = int, partial = FALSE)

[1] 14.92537

VarGermRate(germ.counts = y, intervals = int, partial = FALSE)

[1] 0.0007176543

SEGermRate(germ.counts = y, intervals = int, partial = FALSE)

[1] 0.004235724

GermRateRecip(germ.counts = y, intervals = int,
               method = "coolbear", partial = FALSE)

[1] 0.1674877

GermRateRecip(germ.counts = y, intervals = int,
               method = "farooq", partial = FALSE)

[1] 0.1683168

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

```

```
# From partial germination counts
#-----
GermSpeed(germ.counts = x, intervals = int)

GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)

[1] 34.61567
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                    method = "normal")

[1] 0.1534731
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                    method = "accumulated")

[1] 0.8653917

# From partial germination counts (with percentages instead of counts)
#-----
GermSpeed(germ.counts = x, intervals = int,
           percent = TRUE, total.seeds = 50)

[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                      percent = TRUE, total.seeds = 50)

[1] 69.23134
# From cumulative germination counts
#-----
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)

[1] 6.138925
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)

[1] 34.61567
GermSpeedCorrected(germ.counts = y, intervals = int,
                     partial = FALSE, total.seeds = 50, method = "normal")

[1] 0.1534731
GermSpeedCorrected(germ.counts = y, intervals = int,
                     partial = FALSE, total.seeds = 50, method = "accumulated")

[1] 0.8653917

# From cumulative germination counts (with percentages instead of counts)
#-----
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
           percent = TRUE, total.seeds = 50)

[1] 12.27785
```

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
                      percent = TRUE, total.seeds = 50)
```

```
[1] 69.23134
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
```

```
# From partial germination counts
#-----
WeightGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
```

```
WeightGermPercent()
```

```
[1] 47.42857
```

```
# From cumulative germination counts
#-----
```

```
WeightGermPercent(germ.counts = y, total.seeds = 50, intervals = int,
                  partial = FALSE)
```

```
[1] 47.42857
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
```

```
# From partial germination counts
#-----
```

```
MeanGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
```

```
MeanGermPercent(), MeanGermNumber()
```

```
[1] 5.714286
```

```
MeanGermNumber(germ.counts = x, intervals = int)
```

```
[1] 2.857143
```

```
# From cumulative germination counts
#-----
```

```
MeanGermPercent(germ.counts = y, total.seeds = 50, intervals = int, partial = FALSE)
```

```
[1] 5.714286
```

```
MeanGermNumber(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 2.857143
```

```
# From number of germinated seeds
#-----
```

```
MeanGermPercent(germinated.seeds = 40, total.seeds = 50, intervals = int)
```

```
[1] 5.714286
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----
# Without max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50)
```

```
TimsonsIndex(), GermRateGeorge()
```

```
[1] 664
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
modification = "none")
```

```
[1] 664
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
modification = "labouriau")
```

```
[1] 8.3
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
modification = "khanungar")
```

```
[1] 47.42857
```

```
GermRateGeorge(germ.counts = x, intervals = int)
```

```
[1] 332
```

```
# With max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50, max = 10)
```

```
[1] 344
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
max = 10, modification = "none")
```

```
[1] 344
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
max = 10, modification = "labouriau")
```

```
[1] 4.410256
```

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
max = 10, modification = "khanungar")
```

```
[1] 24.57143
```

```
GermRateGeorge(germ.counts = x, intervals = int, max = 10)
```

```
[1] 172
```

```
GermRateGeorge(germ.counts = x, intervals = int, max = 14)
```

```
[1] 332
```

```

# From cumulative germination counts
#-----
# Without max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50)

[1] 664

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "none")

[1] 664

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "labouriau")

[1] 8.3

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "khanungar")

[1] 47.42857

GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE)

[1] 332

# With max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50, max = 10)

[1] 344

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "none")

[1] 344

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "labouriau")

[1] 4.410256

TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "khanungar")

[1] 24.57143

GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 10)

[1] 172

GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 14)

```

```
[1] 332
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#-----
GermIndex(germ.counts = x, intervals = int, total.seeds = 50)
```

```
GermIndex()
```

```
[1] 5.84
```

```
GermIndex(germ.counts = x, intervals = int, total.seeds = 50,
           modification = "none")
```

```
[1] 5.84
```

```
GermIndex(germ.counts = x, intervals = int, total.seeds = 50,
           modification = "santanaranal")
```

```
[1] 7.3
```

```
# From cumulative germination counts
#-----
```

```
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
           total.seeds = 50)
```

```
[1] 5.84
```

```
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
           total.seeds = 50,
           modification = "none")
```

```
[1] 5.84
```

```
GermIndex(germ.counts = y, intervals = int, partial = FALSE,
           total.seeds = 50,
           modification = "santanaranal")
```

```
[1] 7.3
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
```

```
# From partial germination counts
#-----
```

```
EmergenceRateIndex(germ.counts = x, intervals = int, total.seeds = 50)
```

```
EmergenceRateIndex()
```

```
[1] 292
```

```
EmergenceRateIndex(germ.counts = x, intervals = int, total.seeds = 50,
                     method = "shmueligoldberg")
```

```
[1] 292
EmergenceRateIndex(germ.counts = x, intervals = int, total.seeds = 50,
                     method = "sgsantanaranal")

[1] 7.3
EmergenceRateIndex(germ.counts = x, intervals = int, total.seeds = 50,
                     method = "bilbrownanjura")

[1] 5.970149
EmergenceRateIndex(germ.counts = x, intervals = int, total.seeds = 50,
                     method = "fakorede")

[1] 8.375
# From cumulative germination counts
#-----
EmergenceRateIndex(germ.counts = y, intervals = int, total.seeds = 50,
                     partial = FALSE)

[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, total.seeds = 50,
                     partial = FALSE,
                     method = "shmueligoldberg")

[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, total.seeds = 50,
                     partial = FALSE,
                     method = "sgsantanaranal")

[1] 7.3
EmergenceRateIndex(germ.counts = y, intervals = int, total.seeds = 50,
                     partial = FALSE,
                     method = "bilbrownanjura")

[1] 5.970149
EmergenceRateIndex(germ.counts = y, intervals = int, total.seeds = 50,
                     partial = FALSE,
                     method = "fakorede")

[1] 8.375

x <- c(0, 0, 34, 40, 21, 10, 4, 5, 3, 5, 8, 7, 7, 6, 6, 4, 0, 2, 0, 2)
y <- c(0, 0, 34, 74, 95, 105, 109, 114, 117, 122, 130, 137, 144, 150,
      156, 160, 160, 162, 162, 164)
int <- 1:length(x)
total.seeds = 200

# From partial germination counts
#-----
PeakValue(germ.counts = x, intervals = int, total.seeds = 200)

PeakValue(), GermValue()
```

```
[1] 9.5
```

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
           method = "czabator")
```

```
$`Germination Value`
```

```
[1] 38.95
```

```
[[2]]
```

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34		17.0 5.666667
4	40	4	74		37.0 9.250000
5	21	5	95		47.5 9.500000
6	10	6	105		52.5 8.750000
7	4	7	109		54.5 7.785714
8	5	8	114		57.0 7.125000
9	3	9	117		58.5 6.500000
10	5	10	122		61.0 6.100000
11	8	11	130		65.0 5.909091
12	7	12	137		68.5 5.708333
13	7	13	144		72.0 5.538462
14	6	14	150		75.0 5.357143
15	6	15	156		78.0 5.200000
16	4	16	160		80.0 5.000000
17	0	17	160		80.0 4.705882
18	2	18	162		81.0 4.500000
19	0	19	162		81.0 4.263158
20	2	20	164		82.0 4.100000

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
           method = "dp", k = 10)
```

```
$`Germination Value`
```

```
[1] 53.36595
```

```
[[2]]
```

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	SumDGSbyN	GV
3	34	3	34		17.0 5.666667	5.666667	9.633333
4	40	4	74		37.0 9.250000	7.458333	27.595833
5	21	5	95		47.5 9.500000	8.138889	38.659722
6	10	6	105		52.5 8.750000	8.291667	43.531250
7	4	7	109		54.5 7.785714	8.190476	44.638095
8	5	8	114		57.0 7.125000	8.012897	45.673512
9	3	9	117		58.5 6.500000	7.796769	45.611097
10	5	10	122		61.0 6.100000	7.584673	46.266503
11	8	11	130		65.0 5.909091	7.398497	48.090230
12	7	12	137		68.5 5.708333	7.229481	49.521942
13	7	13	144		72.0 5.538462	7.075752	50.945411
14	6	14	150		75.0 5.357143	6.932534	51.994006
15	6	15	156		78.0 5.200000	6.799262	53.034246
16	4	16	160		80.0 5.000000	6.670744	53.365948
17	0	17	160		80.0 4.705882	6.539753	52.318022
18	2	18	162		81.0 4.500000	6.412268	51.939373
19	0	19	162		81.0 4.263158	6.285850	50.915385
20	2	20	164		82.0 4.100000	6.164414	50.548194

```
$testend
```

```
[1] 16
```

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
           method = "czabator", from.onset = FALSE)
```

```
$`Germination Value`
```

```
[1] 38.95
```

```
[[2]]
```

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
           method = "dp", k = 10, from.onset = FALSE)
```

```
$`Germination Value`
```

```
[1] 46.6952
```

```
[[2]]
```

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	SumDGSbyN	GV
1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111
4	40	4	74	37.0	9.250000	3.729167	13.797917
5	21	5	95	47.5	9.500000	4.883333	23.195833
6	10	6	105	52.5	8.750000	5.527778	29.020833
7	4	7	109	54.5	7.785714	5.850340	31.884354
8	5	8	114	57.0	7.125000	6.009673	34.255134
9	3	9	117	58.5	6.500000	6.064153	35.475298
10	5	10	122	61.0	6.100000	6.067738	37.013202
11	8	11	130	65.0	5.909091	6.053316	39.346552
12	7	12	137	68.5	5.708333	6.024567	41.268285
13	7	13	144	72.0	5.538462	5.987174	43.107655
14	6	14	150	75.0	5.357143	5.942172	44.566291

```

15      6      15      156      78.0 5.200000 5.892694 45.963013
16      4      16      160      80.0 5.000000 5.836901 46.695205
17      0      17      160      80.0 4.705882 5.770370 46.162961
18      2      18      162      81.0 4.500000 5.699794 46.168331
19      0      19      162      81.0 4.263158 5.624182 45.555871
20      2      20      164      82.0 4.100000 5.547972 45.493374

$testend
[1] 16

# From cumulative germination counts
#-
PeakValue(germ.counts = y, interval = int, total.seeds = 200,
           partial = FALSE)

[1] 9.5

GermValue(germ.counts = y, intervals = int, total.seeds = 200,
           partial = FALSE, method = "czabator")

$`Germination Value`
[1] 38.95

[[2]]
  germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent      DGS
3          34         3                  34                  17.0 5.666667
4          40         4                  74                  37.0 9.250000
5          21         5                  95                  47.5 9.500000
6          10         6                 105                  52.5 8.750000
7           4         7                  109                  54.5 7.785714
8           5         8                  114                  57.0 7.125000
9           3         9                  117                  58.5 6.500000
10          5        10                  122                  61.0 6.100000
11          8        11                  130                  65.0 5.909091
12          7        12                  137                  68.5 5.708333
13          7        13                  144                  72.0 5.538462
14          6        14                  150                  75.0 5.357143
15          6        15                  156                  78.0 5.200000
16          4        16                  160                  80.0 5.000000
17          0        17                  160                  80.0 4.705882
18          2        18                  162                  81.0 4.500000
19          0        19                  162                  81.0 4.263158
20          2        20                  164                  82.0 4.100000

GermValue(germ.counts = y, intervals = int, total.seeds = 200,
           partial = FALSE, method = "dp", k = 10)

$`Germination Value`
[1] 53.36595

[[2]]
  germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent      DGS SumDGSbyN      GV
3          34         3                  34                  17.0 5.666667 5.666667 9.633333
4          40         4                  74                  37.0 9.250000 7.458333 27.595833
5          21         5                  95                  47.5 9.500000 8.138889 38.659722
6          10         6                 105                  52.5 8.750000 8.291667 43.531250

```

```

7      4      7      109      54.5 7.785714 8.190476 44.638095
8      5      8      114      57.0 7.125000 8.012897 45.673512
9      3      9      117      58.5 6.500000 7.796769 45.611097
10     5     10      122      61.0 6.100000 7.584673 46.266503
11     8     11      130      65.0 5.909091 7.398497 48.090230
12     7     12      137      68.5 5.708333 7.229481 49.521942
13     7     13      144      72.0 5.538462 7.075752 50.945411
14     6     14      150      75.0 5.357143 6.932534 51.994006
15     6     15      156      78.0 5.200000 6.799262 53.034246
16     4     16      160      80.0 5.000000 6.670744 53.365948
17     0     17      160      80.0 4.705882 6.539753 52.318022
18     2     18      162      81.0 4.500000 6.412268 51.939373
19     0     19      162      81.0 4.263158 6.285850 50.915385
20     2     20      164      82.0 4.100000 6.164414 50.548194

$testend
[1] 16

GermValue(germ.counts = y, intervals = int, total.seeds = 200,
           partial = FALSE, method = "czabator", from.onset = FALSE)

``Germination Value``
[1] 38.95

[[2]]
  germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent      DGS
1          0         1                      0            0.0 0.000000
2          0         2                      0            0.0 0.000000
3         34         3                     34            17.0 5.666667
4         40         4                     74            37.0 9.250000
5         21         5                     95            47.5 9.500000
6         10         6                    105            52.5 8.750000
7          4         7                    109            54.5 7.785714
8          5         8                    114            57.0 7.125000
9          3         9                    117            58.5 6.500000
10         5        10                    122            61.0 6.100000
11         8        11                    130            65.0 5.909091
12         7        12                    137            68.5 5.708333
13         7        13                    144            72.0 5.538462
14         6        14                    150            75.0 5.357143
15         6        15                    156            78.0 5.200000
16         4        16                    160            80.0 5.000000
17         0        17                    160            80.0 4.705882
18         2        18                    162            81.0 4.500000
19         0        19                    162            81.0 4.263158
20         2        20                    164            82.0 4.100000

GermValue(germ.counts = y, intervals = int, total.seeds = 200,
           partial = FALSE, method = "dp", k = 10, from.onset = FALSE)

``Germination Value``
[1] 46.6952

[[2]]
  germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent      DGS SumDGSbyN      GV

```

1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111
4	40	4	74	37.0	9.250000	3.729167	13.797917
5	21	5	95	47.5	9.500000	4.883333	23.195833
6	10	6	105	52.5	8.750000	5.527778	29.020833
7	4	7	109	54.5	7.785714	5.850340	31.884354
8	5	8	114	57.0	7.125000	6.009673	34.255134
9	3	9	117	58.5	6.500000	6.064153	35.475298
10	5	10	122	61.0	6.100000	6.067738	37.013202
11	8	11	130	65.0	5.909091	6.053316	39.346552
12	7	12	137	68.5	5.708333	6.024567	41.268285
13	7	13	144	72.0	5.538462	5.987174	43.107655
14	6	14	150	75.0	5.357143	5.942172	44.566291
15	6	15	156	78.0	5.200000	5.892694	45.963013
16	4	16	160	80.0	5.000000	5.836901	46.695205
17	0	17	160	80.0	4.705882	5.770370	46.162961
18	2	18	162	81.0	4.500000	5.699794	46.168331
19	0	19	162	81.0	4.263158	5.624182	45.555871
20	2	20	164	82.0	4.100000	5.547972	45.493374

```
$testend
[1] 16
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40)
int <- 1:length(x)
```

```
# From partial germination counts
#-----
CUGerm(germ.counts = x, intervals = int)
```

```
CUGerm()
```

```
[1] 0.7092199
```

```
# From cumulative germination counts
#-----
```

```
CUGerm(germ.counts = y, intervals = int, partial = FALSE)
```

```
[1] 0.7092199
```

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40)
int <- 1:length(x)
```

```
# From partial germination counts
#-----
GermSynchrony(germ.counts = x, intervals = int)
```

```
GermSynchrony(), GermUncertainty()
```

```
[1] 0.2666667
```

```
GermUncertainty(germ.counts = x, intervals = int)
[1] 2.062987
# From cumulative germination counts
#-
GermSynchrony(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.2666667
GermUncertainty(germ.counts = y, intervals = int, partial = FALSE)
[1] 2.062987
```

Non-linear regression analysis

Several mathematical functions have been used to fit the cumulative germination count data and describe the germination process by non-linear regression analysis. They include functions such as Richard's, Weibull, logistic, log-logistic, gaussian, four-parameter hill function etc. Currently **germinationmetrics** implements the four-parameter hill function to fit the count data and computed various associated metrics.

Four-parameter hill function

The four-parameter hill function defined as follows (El-Kassaby et al., 2008).

$$f(x) = y = y_0 + \frac{ax^b}{x^b + c^b}$$

Where, y is the cumulative germination percentage at time x , y_0 is the intercept on the y axis, a is the asymptote, b is a mathematical parameter controlling the shape and steepness of the germination curve and c is the "half-maximal activation level".

this function can also be reparameterized by substituting b with e^β to constraint b to positive values only.

$$y = y_0 + \frac{ax^{e^\beta}}{c^{e^\beta} + x^{e^\beta}}$$

Where, $b = e^\beta$ and $\beta = \log_e(b)$.

The details of various parameters that are computed from this function are given in Table 4.

Table 4 Germination parameters estimated from the four-parameter hill function.

Germination parameters	Details	Unit	Measures
y intercept (y_0)	The intercept on the y axis.		
Asymptote (a)	It is the maximum cumulative germination percentage, which is equivalent to germination capacity.	%	Germination capacity
Shape and steepness (b)	Mathematical parameter controlling the shape and steepness of the germination curve. The larger the b , the steeper the rise toward the asymptote a , and the shorter the time between germination onset and maximum germination.		Germination rate
Half-maximal activation level (c)	Time required for 50% of viable seeds to germinate.	time	Germination time

Germination parameters	Details	Unit	Measures
<i>lag</i>	It is the time at germination onset and is computed by solving four-parameter hill function after setting <i>y</i> to 0 as follows. $lag = b \sqrt{\frac{-y_0 c^b}{a + y_0}}$	time	Germination time
D_{lag-50}	The duration between the time at germination onset (<i>lag</i>) and that at 50% germination (<i>c</i>).	time	Germination time
$t_{50_{total}}$	Time required for 50% of total seeds to germinate.	time	Germination time
$t_{50_{germinated}}$	Time required for 50% of viable/germinated seeds to germinate	time	Germination time
$t_{x_{total}}$	Time required for <i>x</i> % of total seeds to germinate.	time	Germination time
$t_{x_{germinated}}$	Time required for <i>x</i> % of viable/germinated seeds to germinate	time	Germination time
Uniformity ($U_{t_{max}-t_{min}}$)	It is the time interval between the percentages of viable seeds specified in the arguments <code>umin</code> and <code>umax</code> to germinate.	time	Germination time
Time at maximum germination rate (<i>TMGR</i>)	The partial derivative of the four-parameter hill function gives the instantaneous rate of germination (<i>s</i>) as follows. $s = \frac{\partial y}{\partial x} = \frac{abc^b x^{b-1}}{(c^b + x^b)^2}$ From this function for instantaneous rate of germination, <i>TMGR</i> can be estimated as follows. $TMGR = b \sqrt{\frac{c^b(b-1)}{b+1}}$	time	Germination time
Area under the curve (<i>AUC</i>)	It represents the point in time when the instantaneous rate of germination starts to decline.	Mixed	
<i>MGT</i>	Calculated by integration of the fitted curve and proper normalisation.	time	Germination time
<i>Skewness</i>	It is computed as follows. $\frac{MGT}{t_{50_{germinated}}}$		

Examples

```

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)
total.seeds = 50

# From partial germination counts
#-----
FourPHFFit(germ.counts = x, intervals = int, total.seeds = 50, tmax = 20)

```

FourPHFFit()

```

$data
  gp csgp intervals
1   0    0      1
2   0    0      2
3   0    0      3
4   0    0      4
5   8    8      5
6  34   42      6
7  20   62      7
8  14   76      8
9   2   78      9
10  0   78     10
11  2   80     11
12  0   80     12
13  0   80     13
14  0   80     14

$Parameters
  term estimate std.error statistic      p.value
1  bta  2.290709  0.05602634  40.88628 2.965932e-14
2    c  6.034954  0.03872162 155.85488 3.270089e-21

$Fit
  sigma isConv      finTol      logLik       AIC       BIC deviance df.residual nobs
1 1.61522  TRUE 7.105427e-14 -25.49868 56.99736 58.91453 31.30723                12    14

$a
[1] 80

$b
[1] 9.881937

$c
[1] 6.034954

$y0
[1] 0

$lag
[1] 0

$Dlag50

```

```
[1] 6.034954

$t50.total
[1] 6.355121

$txp.total
      10       60
4.956264 6.744598

$t50.Germinated
[1] 6.034954

$txp.Germinated
      10       60
4.831807 6.287724

$Uniformity
      90       10 uniformity
7.537690 4.831807 2.705882

$TMGR
[1] 5.912194

$AUC
[1] 1108.976

$MGT
[1] 6.632252

$Skewness
[1] 1.098973

$msg
[1] "#1. success "

$isConv
[1] TRUE

$model
Nonlinear regression model
model: csgp ~ FourPHF_fixa_fixy0(x = intervals, a = max(csgp), bta,      c)
  data: data
    bta      c
2.291 6.035
residual sum-of-squares: 31.31

Algorithm: multifit/levenberg-marquardt, (scaling: levenberg, solver: qr)

Number of iterations to convergence: 9
Achieved convergence tolerance: 7.105e-14

attr("class")
[1] "FourPHFFit" "list"
```

```

# From cumulative germination counts
#-----
FourPHFFit(germ.counts = y, intervals = int, total.seeds = 50, tmax = 20,
            partial = FALSE)

$data
  gp csgp intervals
1  0    0      1
2  0    0      2
3  0    0      3
4  0    0      4
5  8    8      5
6 34   42     6
7 20   62     7
8 14   76     8
9  2   78     9
10 0   78    10
11 2   80    11
12 0   80    12
13 0   80    13
14 0   80    14

$Parameters
  term estimate std.error statistic      p.value
1  bta 2.290709 0.05602634 40.88628 2.965932e-14
2    c 6.034954 0.03872162 155.85488 3.270089e-21

$Fit
  sigma isConv      finTol      logLik      AIC      BIC deviance df.residual nobs
1 1.61522  TRUE 7.105427e-14 -25.49868 56.99736 58.91453 31.30723           12    14

$a
[1] 80

$b
[1] 9.881937

$c
[1] 6.034954

$y0
[1] 0

$lag
[1] 0

$Dlag50
[1] 6.034954

$t50.total
[1] 6.355121

$txp.total
  10      60

```

```

4.956264 6.744598

$t50.Germinated
[1] 6.034954

$txp.Germinated
 10      60
4.831807 6.287724

$Uniformity
 90      10 uniformity
 7.537690  4.831807  2.705882

$TMGR
[1] 5.912194

$AUC
[1] 1108.976

$MGT
[1] 6.632252

$Skewness
[1] 1.098973

$msg
[1] "#1. success "

$isConv
[1] TRUE

$model
Nonlinear regression model
model: csgp ~ FourPHF_fixa_fixy0(x = intervals, a = max(csgp), bta,      c)
  data: data
    bta      c
2.291 6.035
residual sum-of-squares: 31.31

Algorithm: multifit/levenberg-marquardt, (scaling: levenberg, solver: qr)

Number of iterations to convergence: 9
Achieved convergence tolerance: 7.105e-14

attr(),"class")
[1] "FourPHFfit" "list"

x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40)
int <- 1:length(x)
total.seeds = 50

# From partial germination counts
#-----

```

```

fit1 <- FourPHFFit(germ.counts = x, intervals = int,
                     total.seeds = 50, tmax = 20)

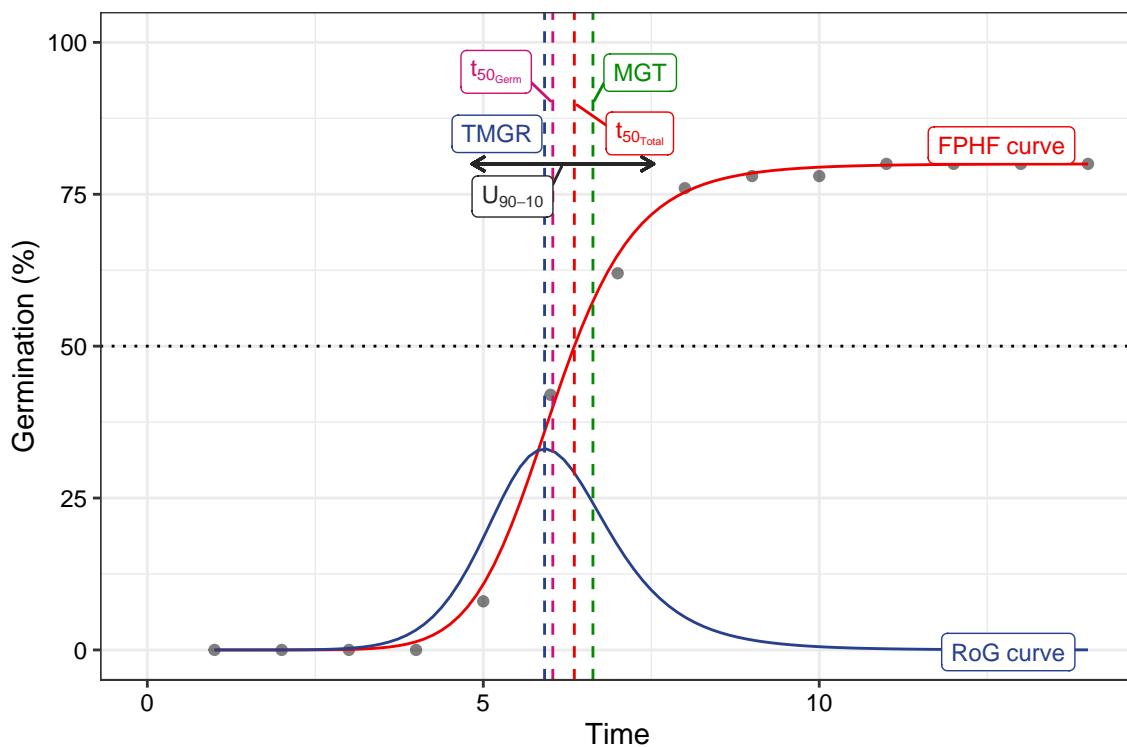
# From cumulative germination counts
#-----
fit2 <- FourPHFFit(germ.counts = y, intervals = int,
                     total.seeds = 50, tmax = 20, partial = FALSE)

# Default plots
plot(fit1)

```

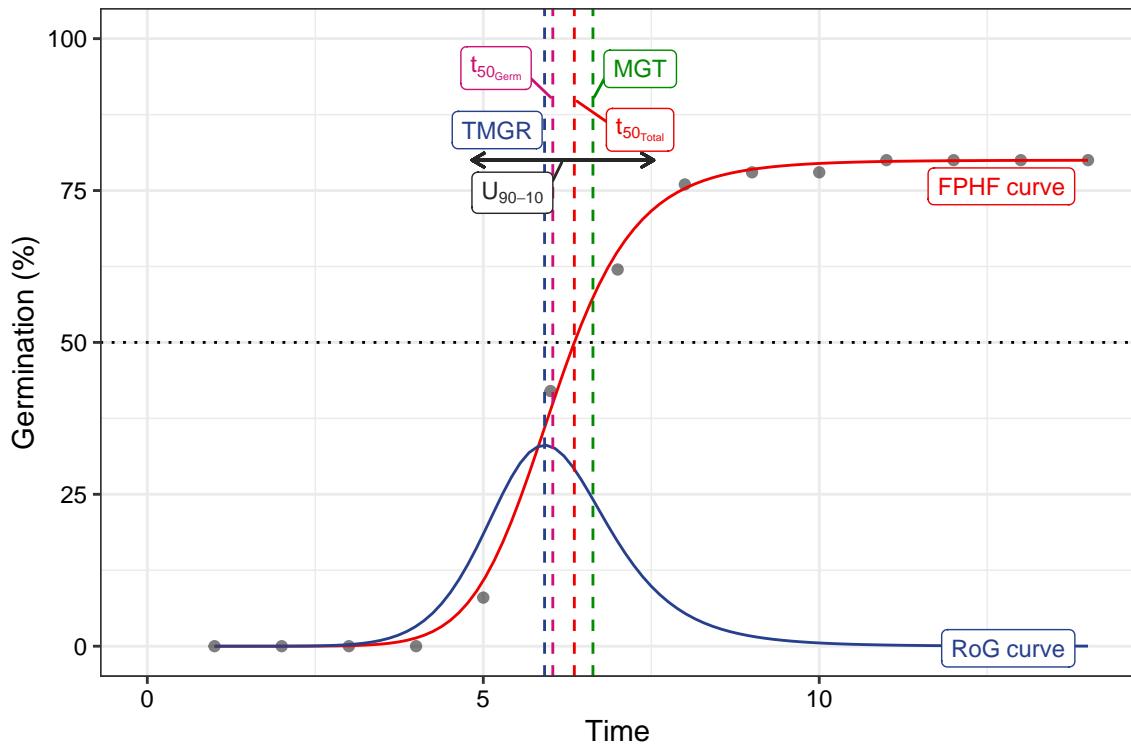
Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have 14 rows
 i Please consider using `annotate()` or provide this layer with data containing a single row.

Warning in geom_segment(aes(x = UfmMax, xend = UfmMin, y = ypos2, yend = ypos2), : All aesthetics have 14 rows
 i Please consider using `annotate()` or provide this layer with data containing a single row.



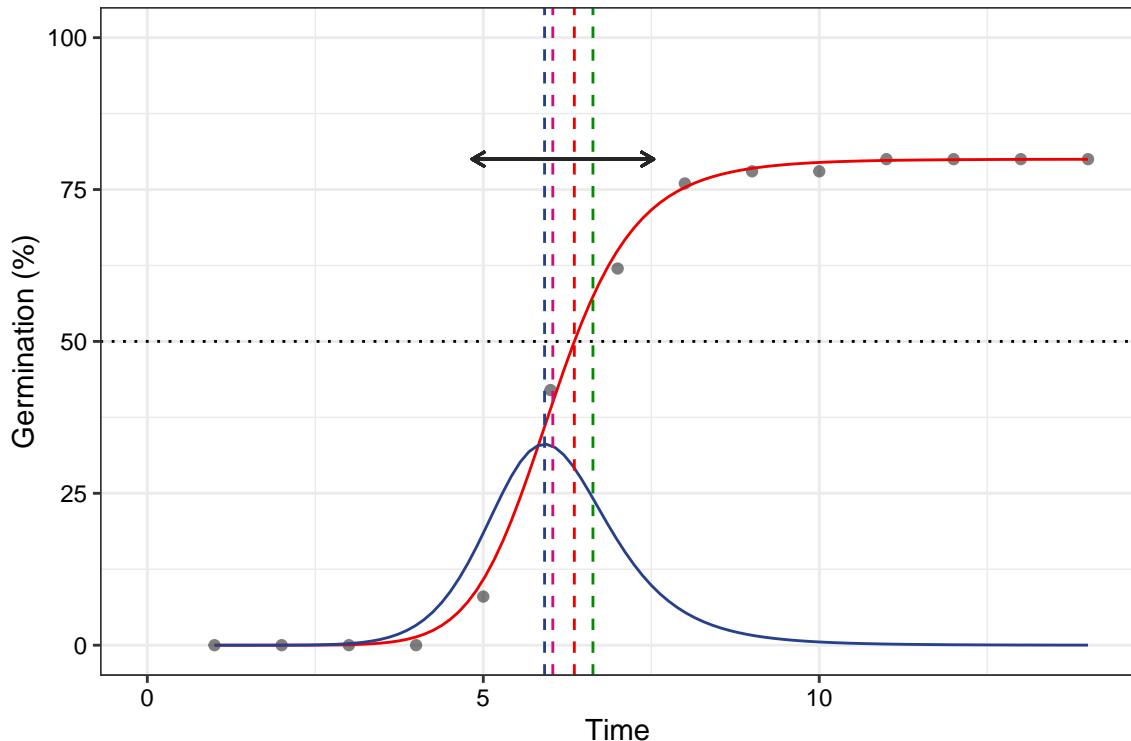
```
plot(fit2)
```

Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have 14 rows
 i Please consider using `annotate()` or provide this layer with data containing a single row.
 All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.



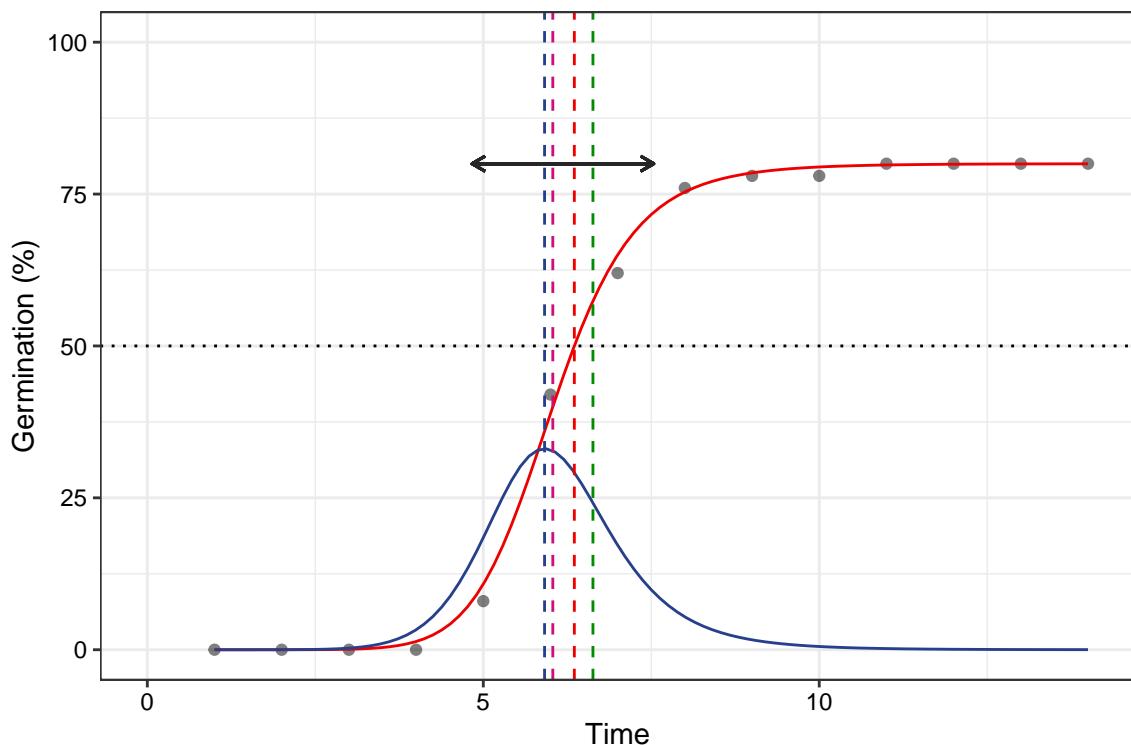
```
# No labels
plot(fit1, plotlabels = FALSE)
```

Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.
 All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.

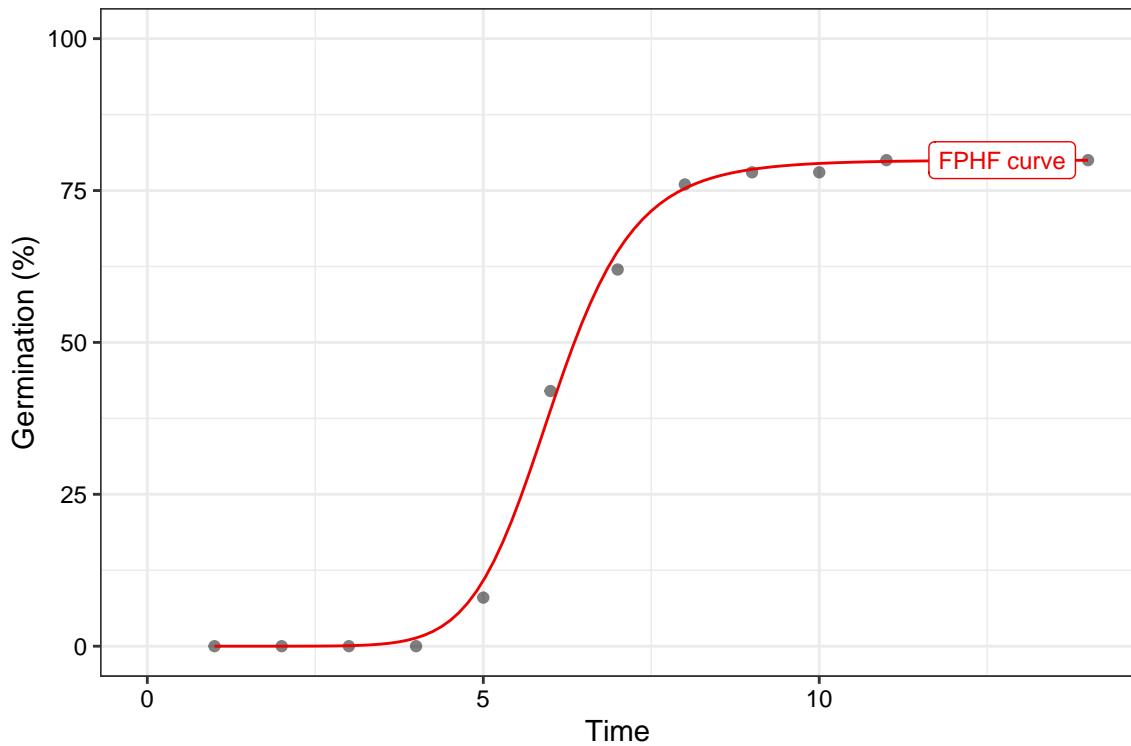


```
plot(fit2, plotlabels = FALSE)
```

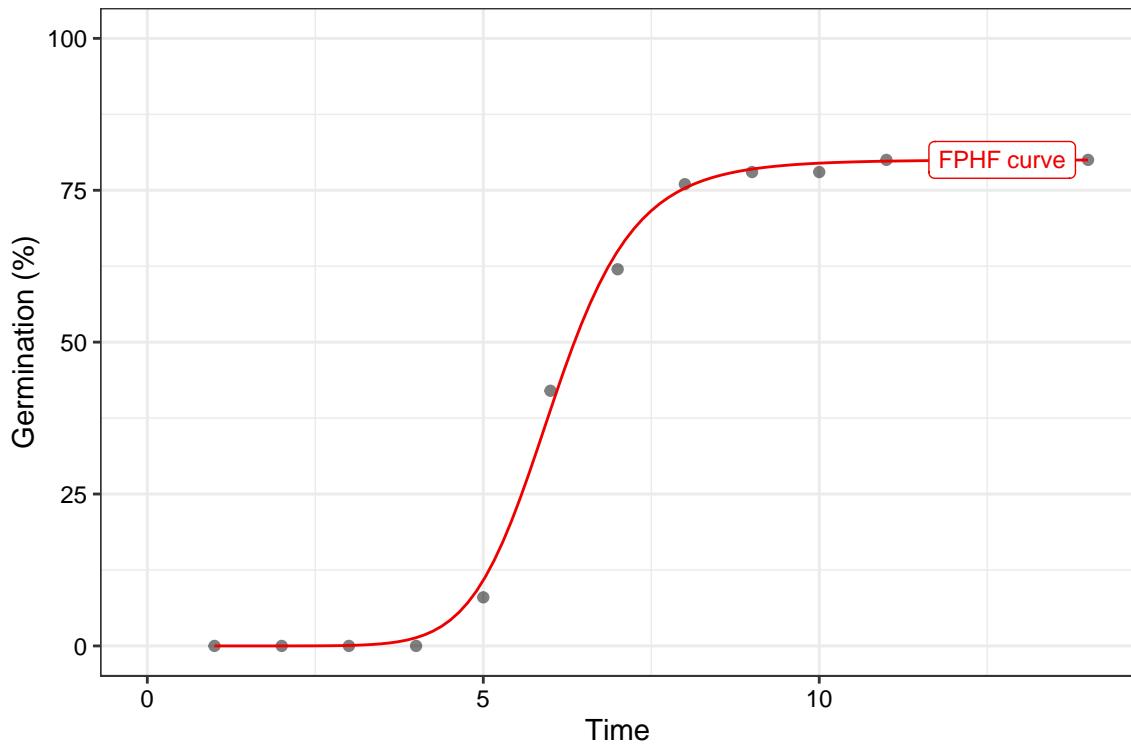
Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have length 1, but the data has 14 rows.
i Please consider using `annotate()` or provide this layer with data containing a single row.
All aesthetics have length 1, but the data has 14 rows.
i Please consider using `annotate()` or provide this layer with data containing a single row.



```
# Only the FPHF curve
plot(fit1, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
      tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```



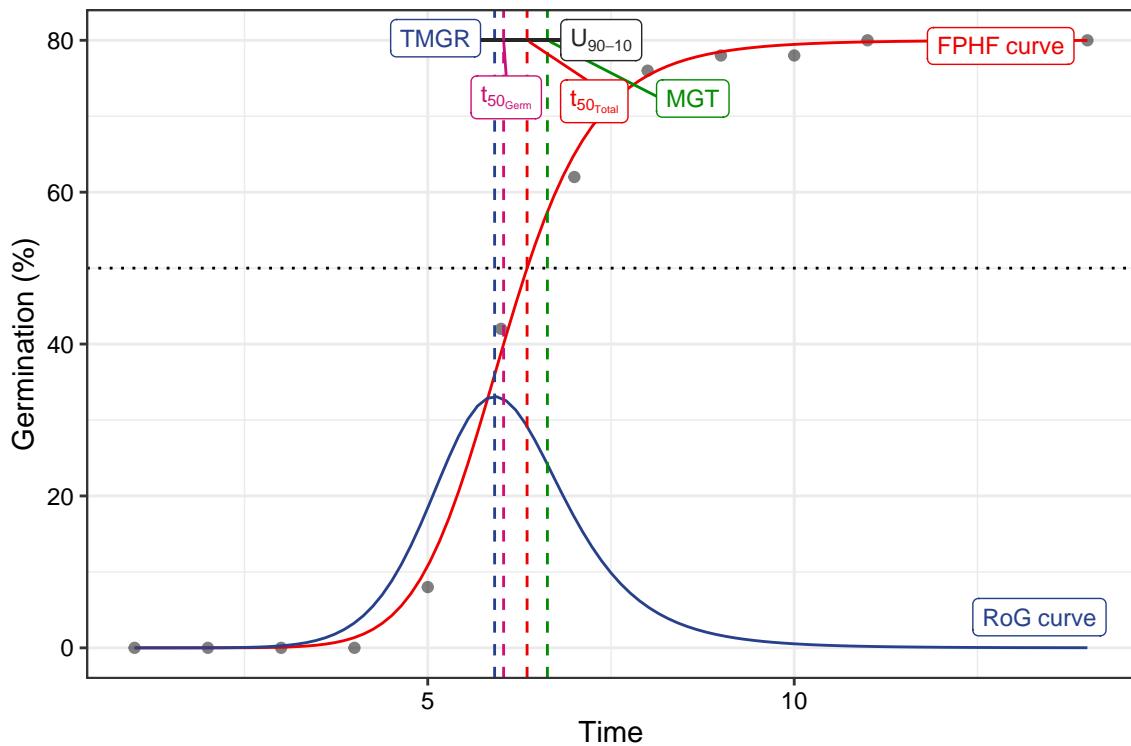
```
plot(fit2, rog = FALSE, t50.total = FALSE, t50. germ = FALSE,  
tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```



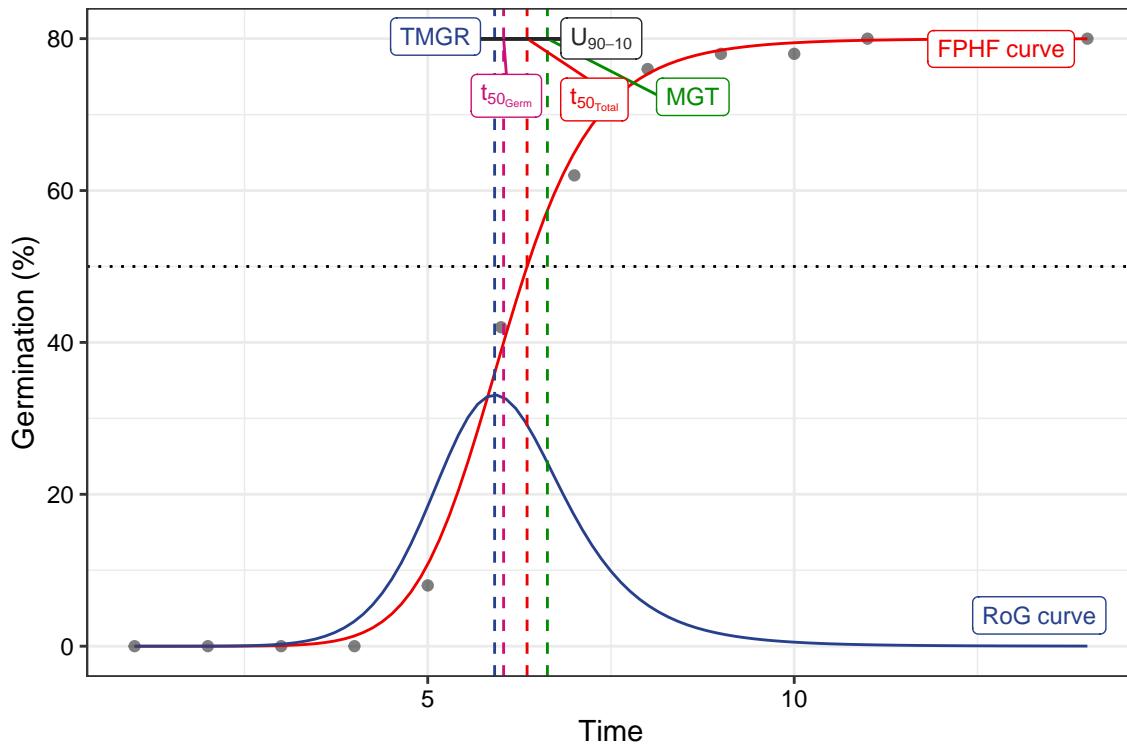
```
# Without y axis limits adjustment  
plot(fit1, limits = FALSE)
```

Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have

i Please consider using `annotate()` or provide this layer with data containing a single row.
 All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.



Warning in geom_segment(aes(x = UfmMin, xend = UfmMax, y = ypos2, yend = ypos2), : All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.
 All aesthetics have length 1, but the data has 14 rows.
 i Please consider using `annotate()` or provide this layer with data containing a single row.



Wrapper functions

Wrapper functions `germination.indices()` and `FourPHFFit.bulk()` are available in the package for computing results for multiple samples in batch from a data frame of germination counts recorded at specific time intervals.

germination.indices() This wrapper function can be used to compute several germination indices simultaneously for multiple samples in batch.

```
data(gcdata)

counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
                           "Day06", "Day07", "Day08", "Day09", "Day10",
                           "Day11", "Day12", "Day13", "Day14")
germination.indices(gcdata, total.seeds.col = "Total Seeds",
                    counts.intervals.cols = counts.per.intervals,
                    intervals = 1:14, partial = TRUE, max.int = 5)
```

	Genotype	Rep	Day01	Day02	Day03	Day04	Day05	Day06	Day07	Day08	Day09	Day10	Day11	Day12	Day13	Day14	Total
1	G1	1	0	0	0	0	0	4	17	10	7	1	0	1	0	0	0
2	G2	1	0	0	0	0	1	3	15	13	6	2	1	0	1	0	0
3	G3	1	0	0	0	0	2	3	18	9	8	2	1	1	1	0	0
4	G4	1	0	0	0	0	0	4	19	12	6	2	1	1	1	0	0
5	G5	1	0	0	0	0	0	5	20	12	8	1	0	0	1	1	0
6	G1	2	0	0	0	0	0	3	21	11	7	1	1	1	1	0	0
7	G2	2	0	0	0	0	0	4	18	11	7	1	0	1	0	0	0
8	G3	2	0	0	0	0	1	3	14	12	6	2	1	0	1	0	0
9	G4	2	0	0	0	0	1	3	19	10	8	1	1	1	0	0	0
10	G5	2	0	0	0	0	0	4	18	13	6	2	1	0	1	0	0
11	G1	3	0	0	0	0	0	5	21	11	8	1	0	0	1	1	0

12	G2	3	0	0	0	0	3	20	10	7	1	1	1	1	0	0	
13	G3	3	0	0	0	0	4	19	12	8	1	1	0	1	1	0	
14	G4	3	0	0	0	0	3	21	11	6	1	0	1	1	0	0	
15	G5	3	0	0	0	0	4	17	10	8	1	1	1	0	0	0	
	GermPercent	PeakGermPercent	FirstGermTime	LastGermTime	PeakGermTime	TimeSpreadGerm	t50_Coolbear	t50_L									
1	80.00000	34.00000		5	11	6	6	5.970588	5.9								
2	82.35294	29.41176		4	12	6	8	6.192308	6.								
3	93.75000	37.50000		4	12	6	8	6.333333	5.9								
4	90.19608	37.25490		5	12	6	7	6.041667	6.								
5	96.00000	40.00000		5	13	6	8	5.975000	5.9								
6	93.87755	42.85714		5	12	6	7	5.976190	5.								
7	87.50000	37.50000		5	11	6	6	5.972222	5.								
8	85.10638	29.78723		4	12	6	8	6.208333	6.								
9	86.53846	36.53846		4	12	6	8	6.310345	5.								
10	90.00000	36.00000		5	12	6	7	6.076923	6.								
11	94.11765	41.17647		5	13	6	8	5.928571	5.								
12	86.27451	39.21569		5	12	6	7	5.975000	5.								
13	95.91837	38.77551		5	13	6	8	6.083333	6.								
14	91.66667	43.75000		5	12	6	7	5.928571	5.								
15	87.50000	35.41667		5	11	6	6	6.050000	6.								
	MeanGermTime	VarGermTime	SEGermTime	CVGermTime	MeanGermRate	VarGermRate	SEGermRate	CVG	GermRa								
1	6.700000	1.446154	0.1901416	0.1794868	0.1492537	0.0007176543	0.004235724	14.92537									
2	6.857143	2.027875	0.2197333	0.2076717	0.1458333	0.0009172090	0.004673148	14.58333									
3	6.866667	2.572727	0.2391061	0.2335882	0.1456311	0.0011572039	0.005071059	14.56311									
4	6.891304	2.187923	0.2180907	0.2146419	0.1451104	0.0009701218	0.004592342	14.51104									
5	6.812500	2.368351	0.2221275	0.2259002	0.1467890	0.0010995627	0.004786184	14.67890									
6	6.869565	2.071498	0.2122088	0.2095140	0.1455696	0.0009301809	0.004496813	14.55696									
7	6.690476	1.389663	0.1818989	0.1761967	0.1494662	0.0006935558	0.004063648	14.94662									
8	6.875000	2.112179	0.2297923	0.2113940	0.1454545	0.0009454531	0.004861721	14.54545									
9	6.866667	2.300000	0.2260777	0.2208604	0.1456311	0.0010345321	0.004794747	14.56311									
10	6.822222	1.831313	0.2017321	0.1983606	0.1465798	0.0008453940	0.004334343	14.65798									
11	6.791667	2.381206	0.2227295	0.2272072	0.1472393	0.0011191581	0.004828643	14.72393									
12	6.886364	2.149577	0.2210295	0.2129053	0.1452145	0.0009558577	0.004660905	14.52145									
13	6.936170	2.539315	0.2324392	0.2297410	0.1441718	0.0010970785	0.004831366	14.41718									
14	6.772727	1.900634	0.2078370	0.2035568	0.1476510	0.0009033254	0.004531018	14.76510									
15	6.809524	1.670151	0.1994129	0.1897847	0.1468531	0.0007767634	0.004300508	14.68531									
	GermRateRecip_Farooq	GermSpeed_Count	GermSpeed_Percent	GermSpeedAccumulated_Count	GermSpeedAccumulate												
1	0.1683168	6.138925	12.27785		34.61567												
2	0.1625000	6.362698	12.47588		35.54058												
3	0.1674419	6.882179	14.33787		38.29725												
4	0.1606218	6.927417	13.58317		38.68453												
5	0.1680672	7.318987	14.63797		41.00786												
6	0.1680000	6.931782	14.14649		38.77620												
7	0.1682243	6.448449	13.43427		36.38546												
8	0.1621622	6.053175	12.87909		33.77079												
9	0.1674009	6.830592	13.13575		38.11511												
10	0.1656051	6.812698	13.62540		38.19527												
11	0.1693548	7.342796	14.39764		41.17452												
12	0.1680672	6.622258	12.98482		37.00640												
13	0.1655172	7.052320	14.39249		39.29399												
14	0.1693548	6.706782	13.97246		37.69490												
15	0.1597633	6.363925	13.25818		35.69697												
	GermSpeedCorrected_Normal	GermSpeedCorrected_Accumulated	WeightGermPercent	MeanGermPercent	MeanGermN												
1	0.1534731		0.8653917	47.42857	5.714286	2.8											

2	0.1514928	0.8462043	47.89916	5.882353	3.00		
3	0.1529373	0.8510501	54.46429	6.696429	3.21		
4	0.1505960	0.8409680	52.24090	6.442577	3.21		
5	0.1524789	0.8543303	56.14286	6.857143	3.41		
6	0.1506909	0.8429608	54.51895	6.705539	3.21		
7	0.1535345	0.8663205	51.93452	6.250000	3.00		
8	0.1513294	0.8442698	49.39210	6.079027	2.81		
9	0.1517909	0.8470024	50.27473	6.181319	3.21		
10	0.1513933	0.8487837	52.57143	6.428571	3.21		
11	0.1529749	0.8578026	55.18207	6.722689	3.41		
12	0.1505059	0.8410547	50.00000	6.162465	3.14		
13	0.1500494	0.8360424	55.24781	6.851312	3.31		
14	0.1524269	0.8567022	53.86905	6.547619	3.14		
15	0.1515220	0.8499278	51.19048	6.250000	3.00		
	TimsonsIndex	TimsonsIndex_Labouriau	TimsonsIndex_KhanUngar	GermRateGeorge	GermIndex		
1	8.000000	1.00	0.5714286	4	5.840000		
2	9.803922	1.25	0.7002801	5	5.882353		
3	14.583333	1.40	1.0416667	7	6.687500		
4	7.843137	1.00	0.5602241	4	6.411765		
5	10.000000	1.00	0.7142857	5	6.900000		
6	6.122449	1.00	0.4373178	3	6.693878		
7	8.333333	1.00	0.5952381	4	6.395833		
8	10.638298	1.25	0.7598784	5	6.063830		
9	9.615385	1.25	0.6868132	5	6.173077		
10	8.000000	1.00	0.5714286	4	6.460000		
11	9.803922	1.00	0.7002801	5	6.784314		
12	5.882353	1.00	0.4201681	3	6.137255		
13	8.163265	1.00	0.5830904	4	6.775510		
14	6.250000	1.00	0.4464286	3	6.625000		
15	8.333333	1.00	0.5952381	4	6.291667		
	EmergenceRateIndex_SG	EmergenceRateIndex_SG_mod	EmergenceRateIndex_Bilbro	Wanjura	EmergenceRateIndex_L		
1	292	7.300000		5.970149	8.00		
2	300	7.142857		6.125000	8.00		
3	321	7.133333		6.553398	8.00		
4	327	7.108696		6.675079	8.00		
5	345	7.187500		7.045872	8.00		
6	328	7.130435		6.696203	8.00		
7	307	7.309524		6.277580	8.00		
8	285	7.125000		5.818182	8.00		
9	321	7.133333		6.553398	8.00		
10	323	7.177778		6.596091	8.00		
11	346	7.208333		7.067485	8.00		
12	313	7.113636		6.389439	8.00		
13	332	7.063830		6.776074	8.00		
14	318	7.227273		6.496644	8.00		
15	302	7.190476		6.167832	8.00		
	PeakValue	GermValue_Czabator	GermValue_DP	GermValue_Czabator_mod	GermValue_DP_mod	CUGerm	GermSync
1	9.500000	54.28571	57.93890	54.28571	39.56076	0.7092199	0.26
2	9.313725	54.78662	52.58713	54.78662	40.99260	0.5051546	0.23
3	10.416667	69.75446	68.62289	69.75446	53.42809	0.3975265	0.22
4	10.049020	64.74158	70.43331	64.74158	48.86825	0.4672113	0.25
5	11.250000	77.14286	80.16914	77.14286	56.23935	0.4312184	0.26
6	10.714286	71.84506	76.51983	71.84506	53.06435	0.4934701	0.27
7	10.416667	65.10417	69.41325	65.10417	47.37690	0.7371500	0.27

8	9.574468	58.20345	56.00669	58.20345	43.67948	0.4855842	0.22
9	9.855769	60.92165	58.13477	60.92165	45.30801	0.4446640	0.24
10	10.250000	65.89286	70.91875	65.89286	49.10820	0.5584666	0.25
11	11.029412	74.14731	77.39782	74.14731	54.27520	0.4288905	0.26
12	9.803922	60.41632	64.44988	60.41632	44.71582	0.4760266	0.27
13	10.969388	75.15470	78.16335	75.15470	54.94192	0.4023679	0.25
14	10.677083	69.90947	74.40140	69.90947	51.41913	0.5383760	0.29
15	10.156250	63.47656	67.62031	63.47656	46.48043	0.6133519	0.24
GermUncertainty							
1	2.062987						
2	2.321514						
3	2.462012						
4	2.279215						
5	2.146051						
6	2.160545						
7	2.040796						
8	2.357249						
9	2.321080						
10	2.187983						
11	2.128670						
12	2.185245						
13	2.241181						
14	2.037680						
15	2.185028						

FourPHFFit.bulk() This wrapper function can be used to fit the four-parameter hill function for multiple samples in batch.

```
data(gadata)

counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
                           "Day06", "Day07", "Day08", "Day09", "Day10",
                           "Day11", "Day12", "Day13", "Day14")

FourPHFFit.bulk(gadata, total.seeds.col = "Total Seeds",
                 counts.intervals.cols = counts.per.intervals,
                 intervals = 1:14, partial = TRUE,
                 fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
                 tmax = 20, tries = 3, umax = 90, umin = 10)
```

	Genotype	Rep	Day01	Day02	Day03	Day04	Day05	Day06	Day07	Day08	Day09	Day10	Day11	Day12	Day13	Day14	Total
1	G1	1	0	0	0	0	4	17	10	7	1	0	1	0	0	0	0
2	G2	1	0	0	0	1	3	15	13	6	2	1	0	1	0	0	0
3	G3	1	0	0	0	2	3	18	9	8	2	1	1	1	0	0	0
4	G4	1	0	0	0	0	4	19	12	6	2	1	1	1	0	0	0
5	G5	1	0	0	0	0	5	20	12	8	1	0	0	1	1	0	0
6	G1	2	0	0	0	0	3	21	11	7	1	1	1	1	0	0	0
7	G2	2	0	0	0	0	4	18	11	7	1	0	1	0	0	0	0
8	G3	2	0	0	0	1	3	14	12	6	2	1	0	1	0	0	0
9	G4	2	0	0	0	1	3	19	10	8	1	1	1	1	0	0	0
10	G5	2	0	0	0	0	4	18	13	6	2	1	0	1	0	0	0
11	G1	3	0	0	0	0	5	21	11	8	1	0	0	1	1	0	0
12	G2	3	0	0	0	0	3	20	10	7	1	1	1	1	0	0	0
13	G3	3	0	0	0	0	4	19	12	8	1	1	0	1	1	0	0
14	G4	3	0	0	0	0	3	21	11	6	1	0	1	1	0	0	0

	G5	3	0	0	0	0	4	17	10	8	1	1	1	0	0	0	0
	b	c	y0	lag	Dlag50	t50.total	t10.total	t60.total	t50.Germinated	t10.Germinated	t60.Germinated						
1	9.881937	6.034954	0	0	6.034954	6.355121	4.956264	6.744598	6.034954					4.831807			
2	9.227666	6.175193	0	0	6.175193	6.473490	4.983236	6.872603	6.175193					4.866755			
3	7.793051	6.138110	0	0	6.138110	6.244191	4.673022	6.608438	6.138110					4.630062			
4	8.925655	6.125173	0	0	6.125173	6.276794	4.850875	6.614968	6.125173					4.788597			
5	9.419181	6.049642	0	0	6.049642	6.103433	4.814125	6.386789	6.049642					4.790946			
6	9.450149	6.097415	0	0	6.097415	6.182279	4.868632	6.477599	6.097415					4.832471			
7	10.172459	6.029851	0	0	6.029851	6.202812	4.930422	6.510495	6.029851					4.858476			
8	8.940696	6.189774	0	0	6.189774	6.439510	4.940057	6.823299	6.189774					4.841105			
9	8.617391	6.125122	0	0	6.125122	6.352172	4.836658	6.733276	6.125122					4.746573			
10	9.608844	6.109504	0	0	6.109504	6.253043	4.920629	6.566506	6.109504					4.860681			
11	9.400212	6.018760	0	0	6.018760	6.099435	4.798627	6.391291	6.018760					4.764246			
12	9.162526	6.108452	0	0	6.108452	6.326184	4.893596	6.684526	6.108452					4.806013			
13	8.995210	6.149012	0	0	6.149012	6.207501	4.841308	6.509954	6.149012					4.816393			
14	10.391845	6.015910	0	0	6.015910	6.122389	4.915140	6.397491	6.015910					4.869398			
15	9.136744	6.121579	0	0	6.121579	6.317392	4.892502	6.667247	6.121579					4.813083			
	Uniformity_90	Uniformity_10	Uniformity		TMGR	AUC	MGT	Skewness		msg	sigma						
1	7.537690	4.831807	2.705882	5.912194	1108.976	6.632252	1.098973	#1. success	1.615220	7.1							
2	7.835407	4.866755	2.968652	6.031282	1128.559	6.784407	1.098655	#1. success	1.115372	2.3							
3	8.137342	4.630062	3.507280	5.938180	1283.693	6.772742	1.103392	#1. success	2.432704	9.9							
4	7.834810	4.788597	3.046213	5.972686	1239.887	6.739666	1.100323	#1. success	2.396582	5.6							
5	7.639028	4.790946	2.848083	5.914289	1328.328	6.654981	1.100062	#1. success	2.399662	1.0							
6	7.693469	4.832471	2.860997	5.961879	1294.463	6.702473	1.099232	#1. success	3.034962	1.5							
7	7.483643	4.858476	2.625166	5.914057	1213.908	6.622417	1.098272	#1. success	1.663019	1.4							
8	7.914163	4.841105	3.073058	6.036192	1164.346	6.804000	1.099232	#1. success	1.120704	4.3							
9	7.904041	4.746573	3.157468	5.961631	1188.793	6.745241	1.101242	#1. success	2.429960	7.9							
10	7.679177	4.860681	2.818496	5.978115	1240.227	6.711900	1.098600	#1. success	1.686656	8.1							
11	7.603611	4.764246	2.839365	5.883557	1305.200	6.624248	1.100600	#1. success	2.628113	1.9							
12	7.763854	4.806013	2.957841	5.964080	1188.021	6.718639	1.099892	#1. success	2.878146	1.1							
13	7.850345	4.816393	3.033952	5.998270	1316.407	6.762274	1.099733	#1. success	2.604588	2.9							
14	7.432372	4.869398	2.562974	5.905180	1273.385	6.604967	1.097916	#1. success	2.764756	9.8							
15	7.785806	4.813083	2.972723	5.976087	1203.664	6.732266	1.099760	#1. success	1.954008	8.7							
	logLik	AIC	BIC		deviance	df.residual	nobs										
1	-25.49868	56.99736	58.91453	31.30723		12	14										
2	-20.31471	46.62943	48.54660	14.92865		12	14										
3	-31.23213	68.46426	70.38143	71.01658		12	14										
4	-31.02269	68.04538	69.96256	68.92324		12	14										
5	-31.04067	68.08135	69.99852	69.10052		12	14										
6	-34.32887	74.65774	76.57491	110.53195		12	14										
7	-25.90697	57.81395	59.73112	33.18760		12	14										
8	-20.38149	46.76298	48.68015	15.07174		12	14										
9	-31.21633	68.43266	70.34984	70.85647		12	14										
10	-26.10456	58.20911	60.12629	34.13771		12	14										
11	-32.31381	70.62762	72.54479	82.88372		12	14										
12	-33.58613	73.17227	75.08944	99.40469		12	14										
13	-32.18793	70.37586	72.29303	81.40654		12	14										
14	-33.02342	72.04684	73.96401	91.72652		12	14										
15	-28.16444	62.32888	64.24606	45.81777		12	14										

Multiple fitted curves generated in batch can also be plotted.

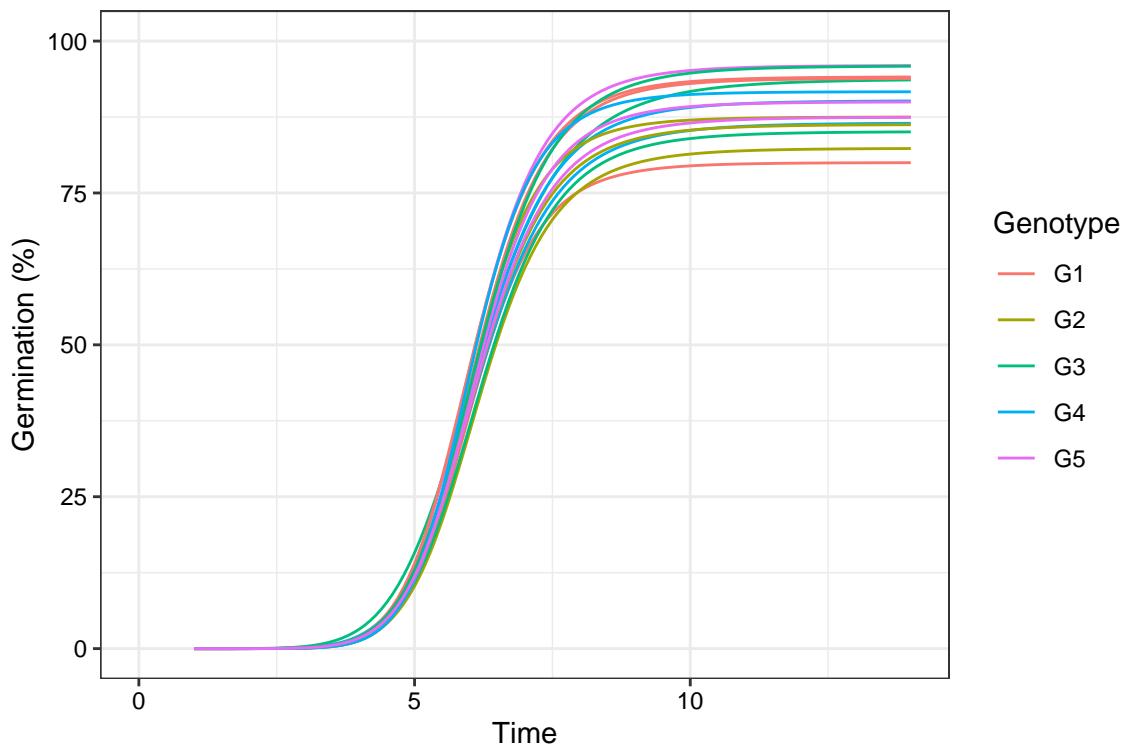
```
data(gcdata)
```

```
counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",
```

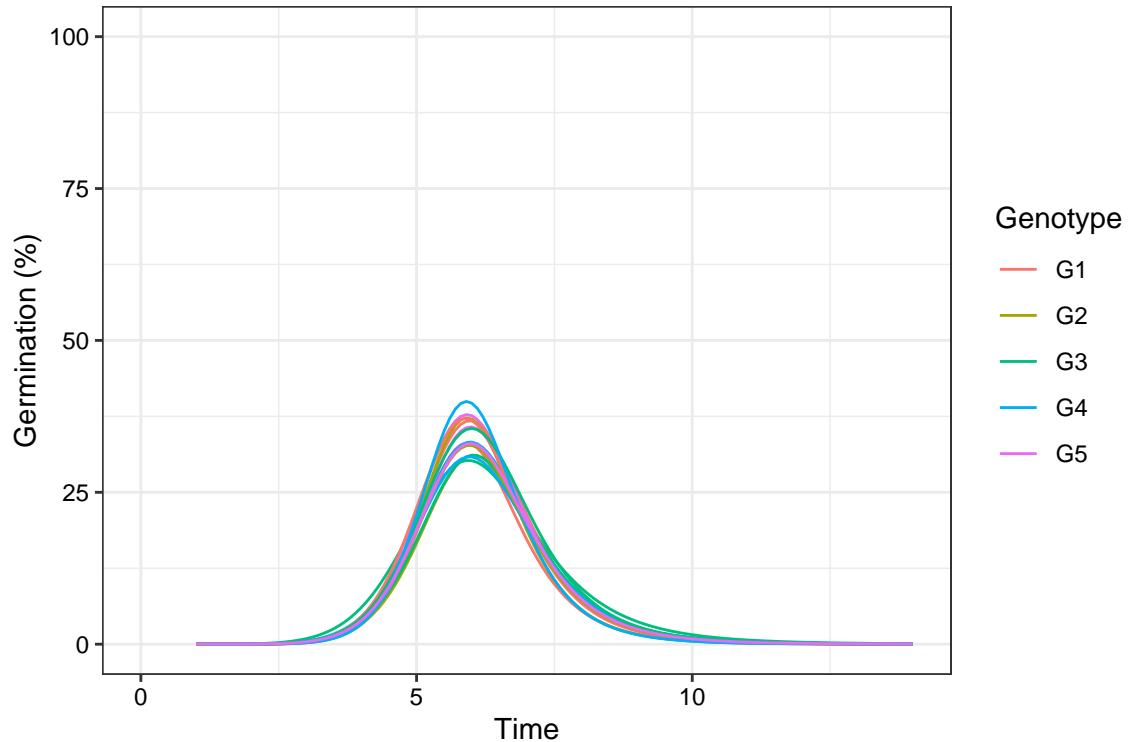
```
"Day06", "Day07", "Day08", "Day09", "Day10",
"Day11", "Day12", "Day13", "Day14")

fits <- FourPHFFit.bulk(gcdata, total.seeds.col = "Total Seeds",
counts.intervals.cols = counts.per.intervals,
intervals = 1:14, partial = TRUE,
fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
tmax = 20, tries = 3, umax = 90, umin = 10)

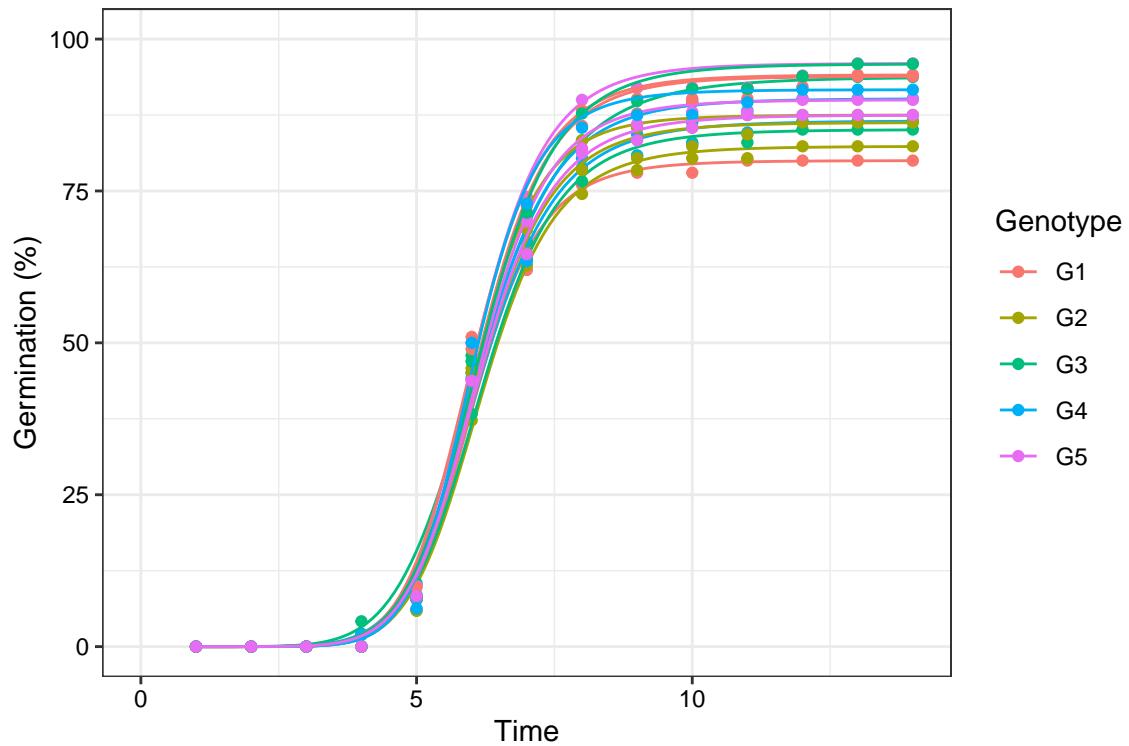
# Plot FPHF curves
plot(fits, group.col = "Genotype")
```



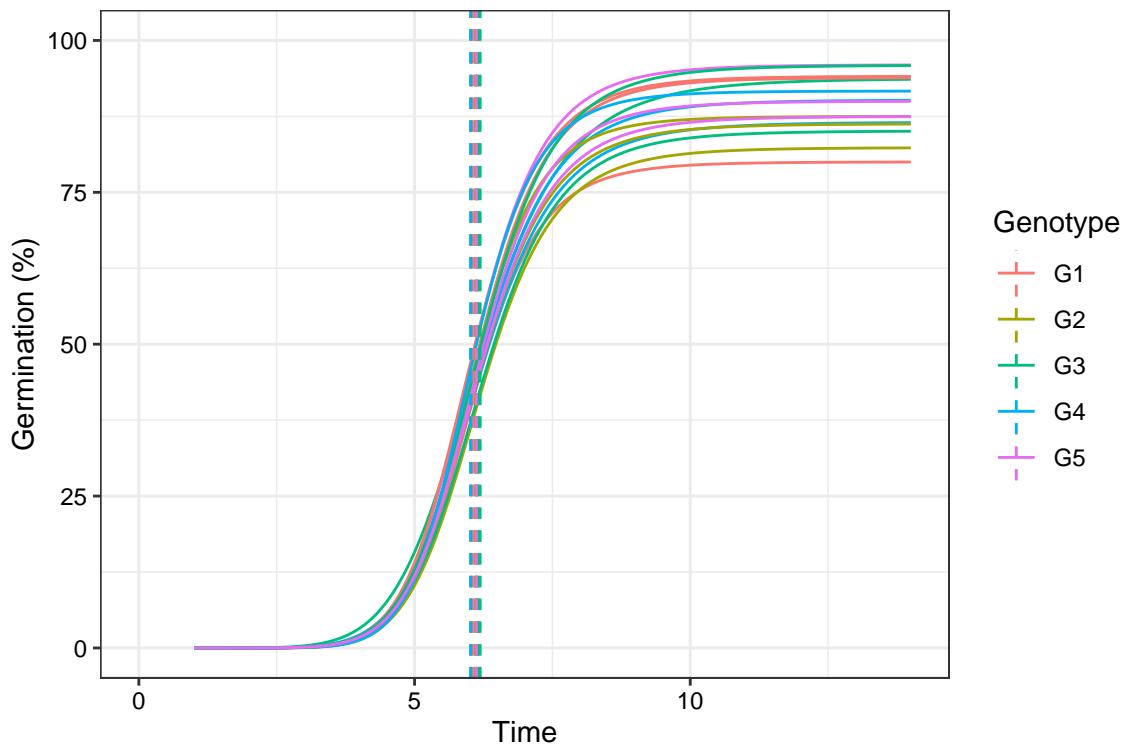
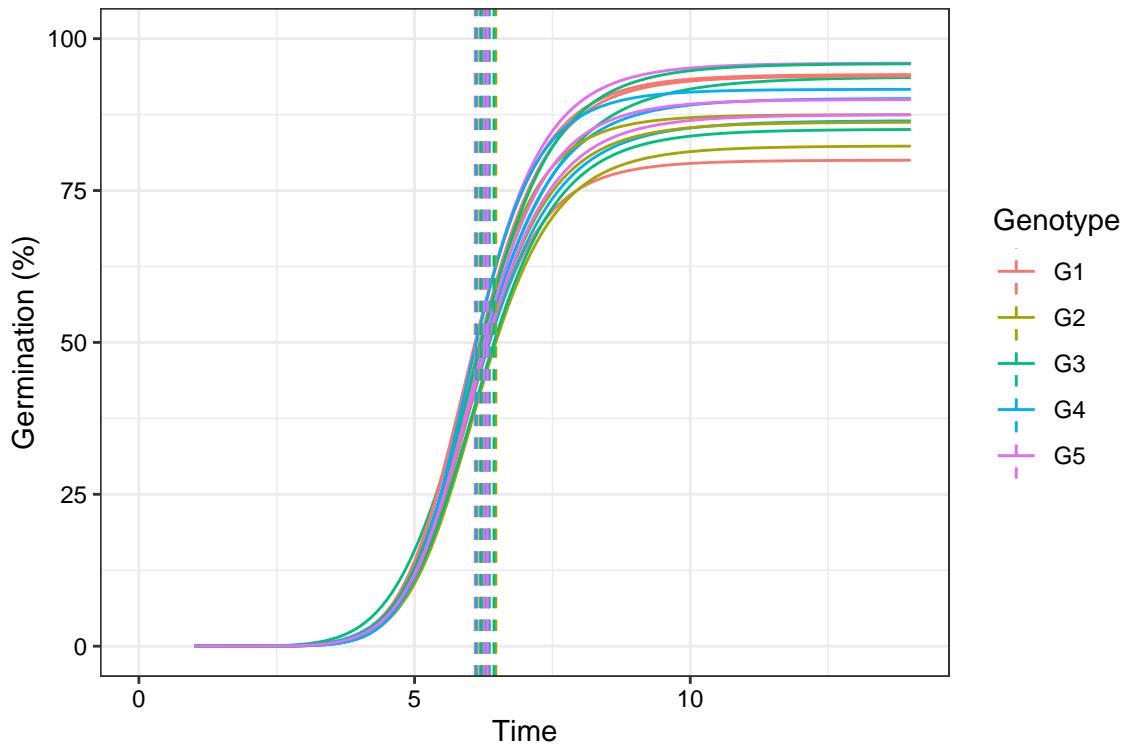
```
# Plot ROG curves
plot(fits, rog = TRUE, group.col = "Genotype")
```

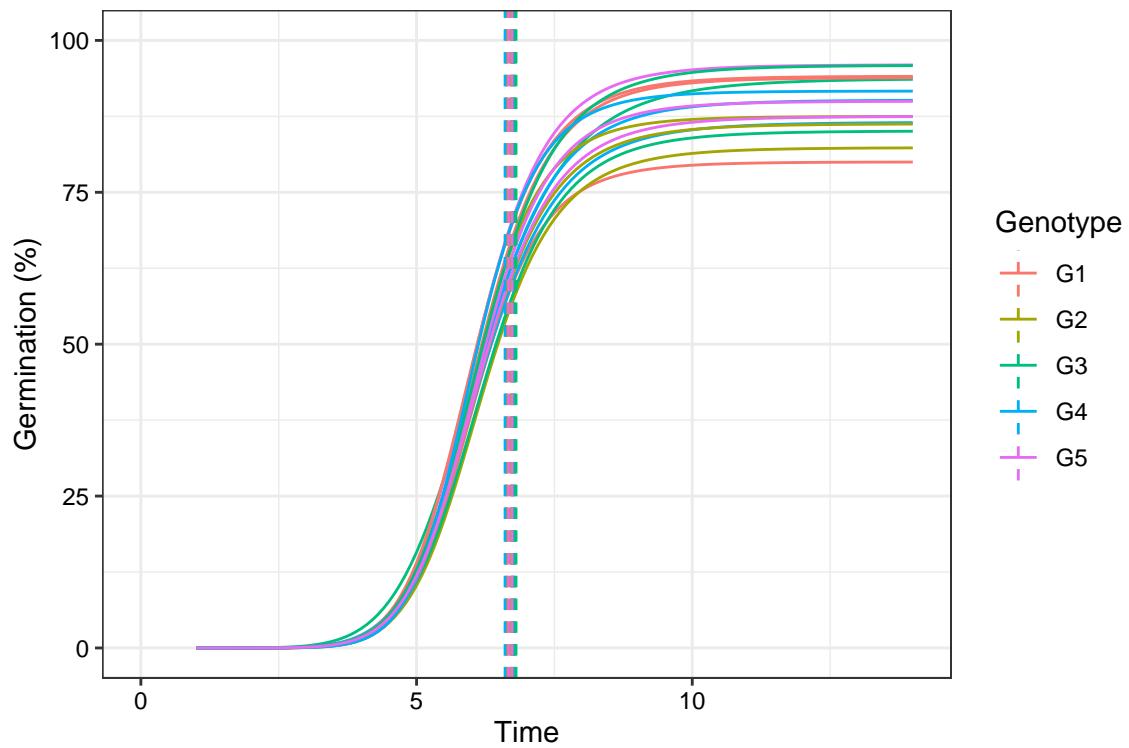
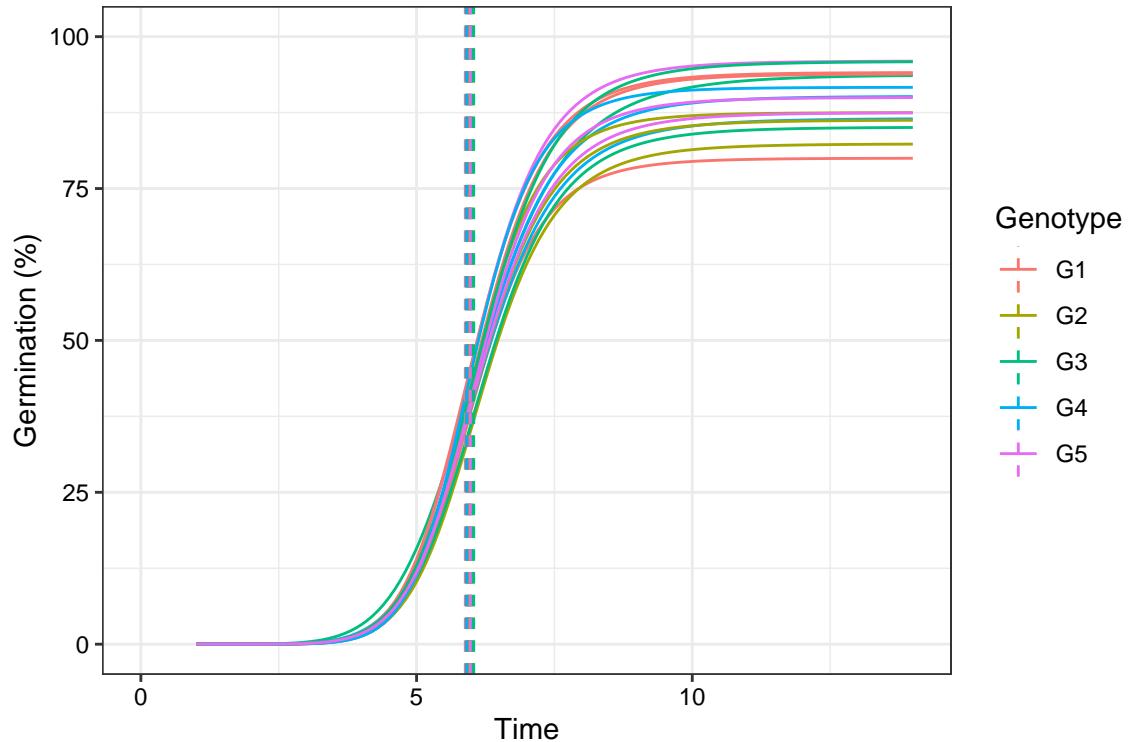


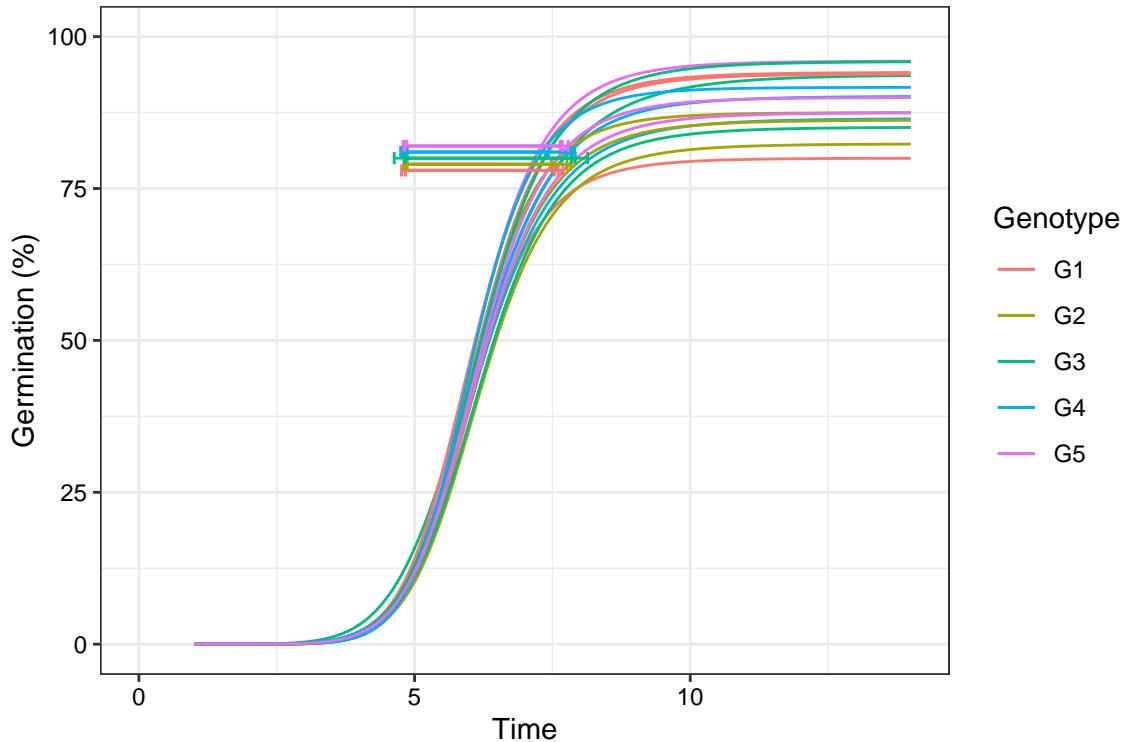
```
# Plot FPHF curves with points
plot(fits, group.col = "Genotype", show.points = TRUE)
```



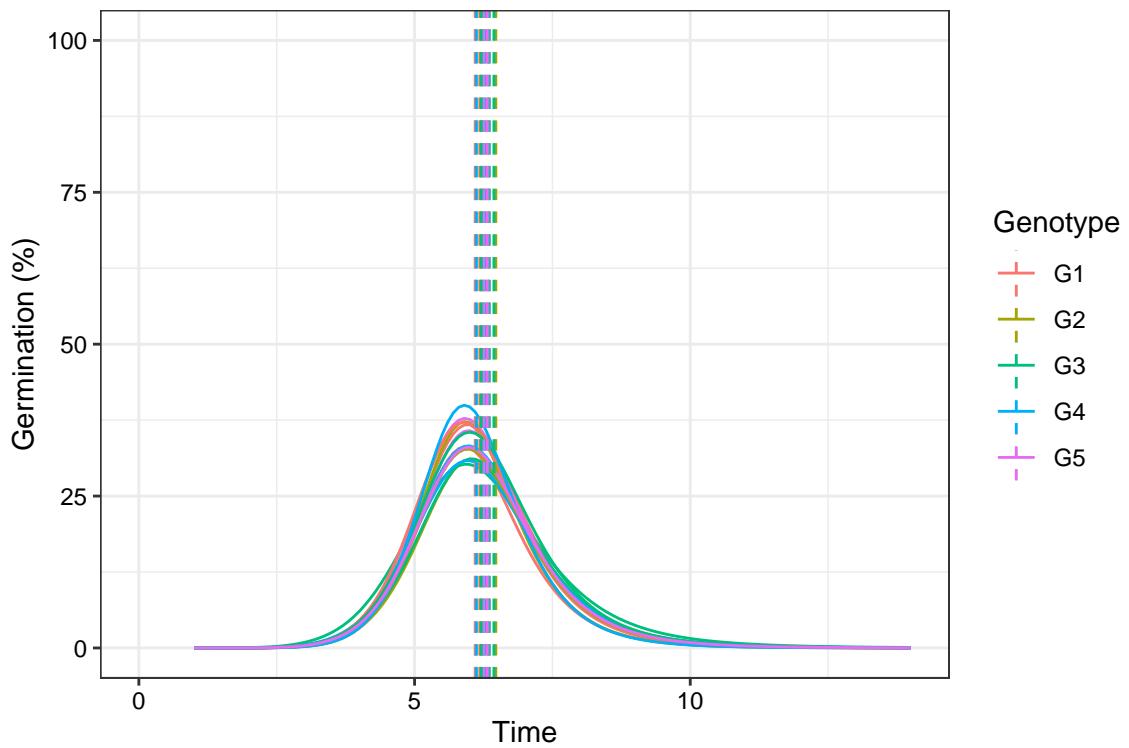
```
# Plot FPHF curves with annotations
plot(fits, group.col = "Genotype", annotate = "t50.total")
```



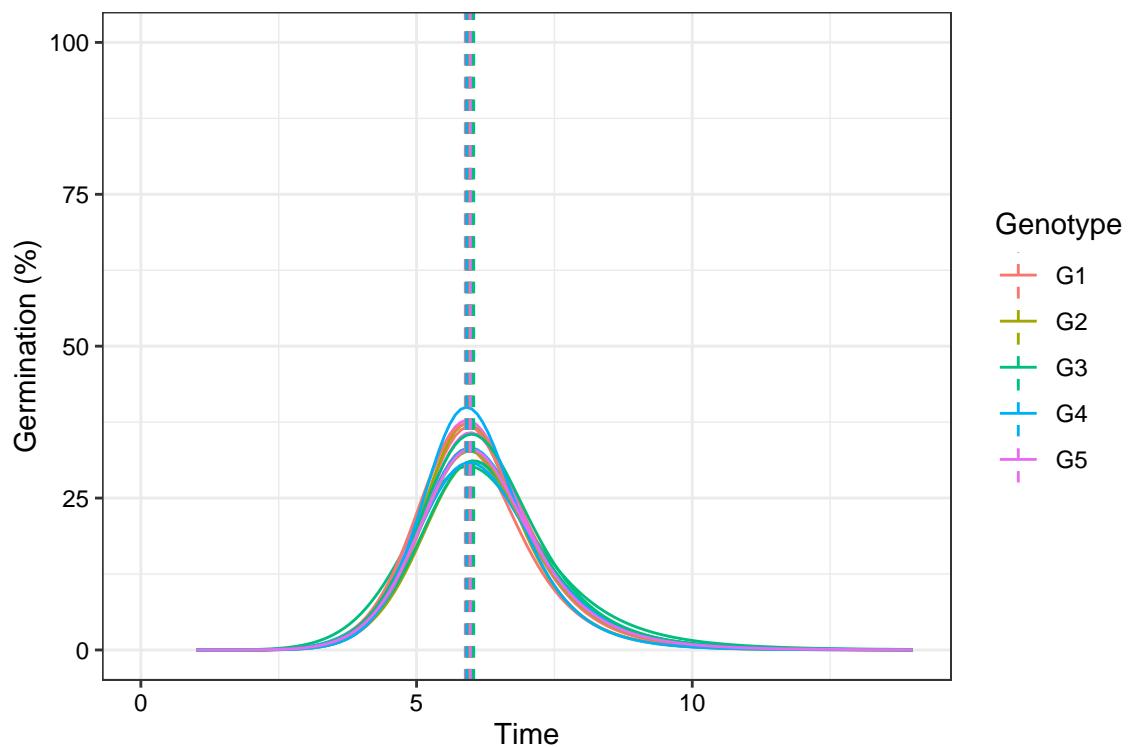
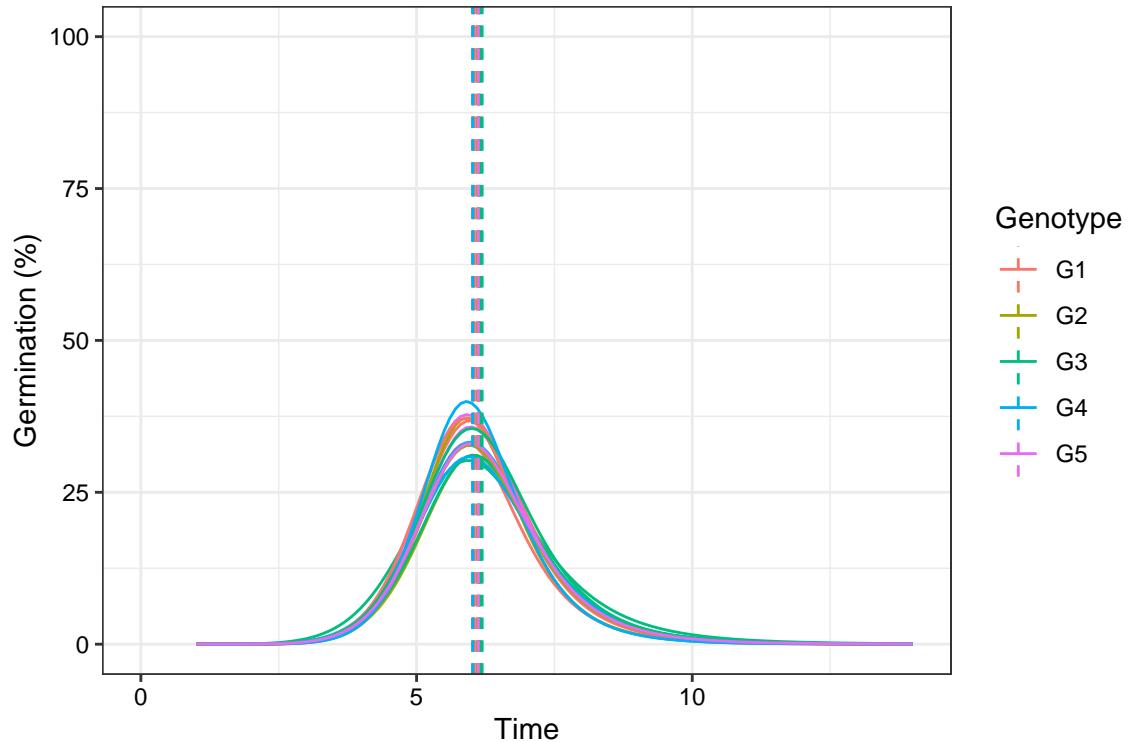


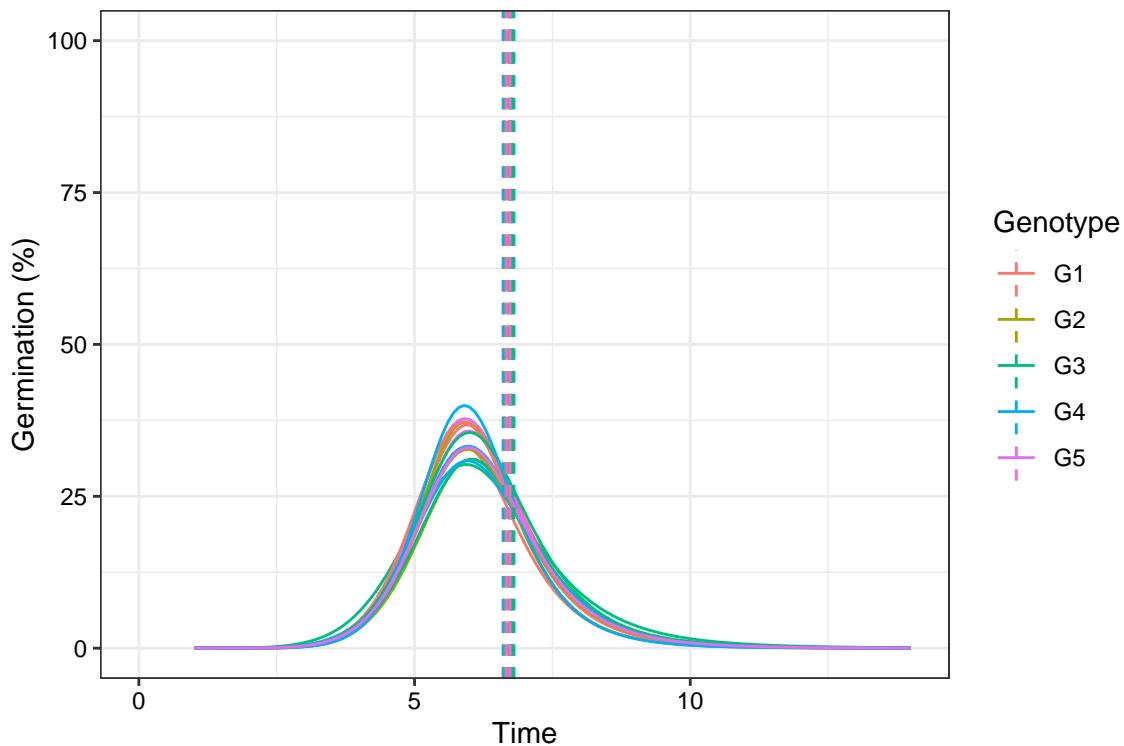


```
# Plot ROG curves with annotations
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.total")
```

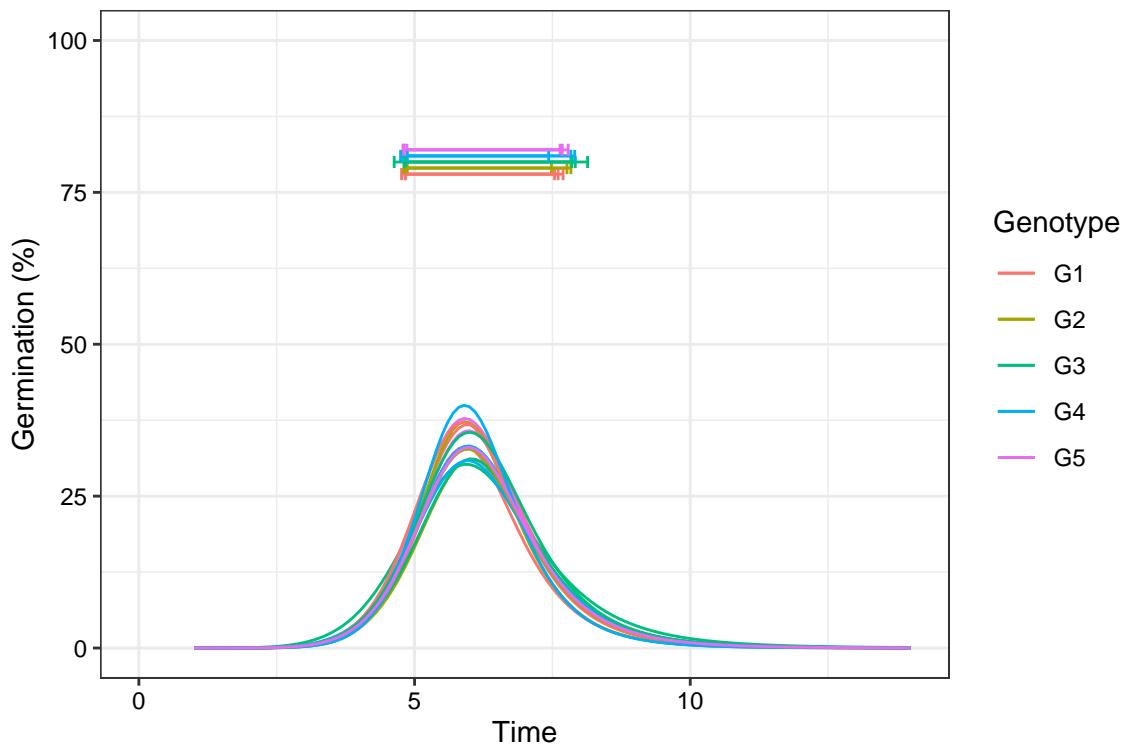


```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.germ")
```





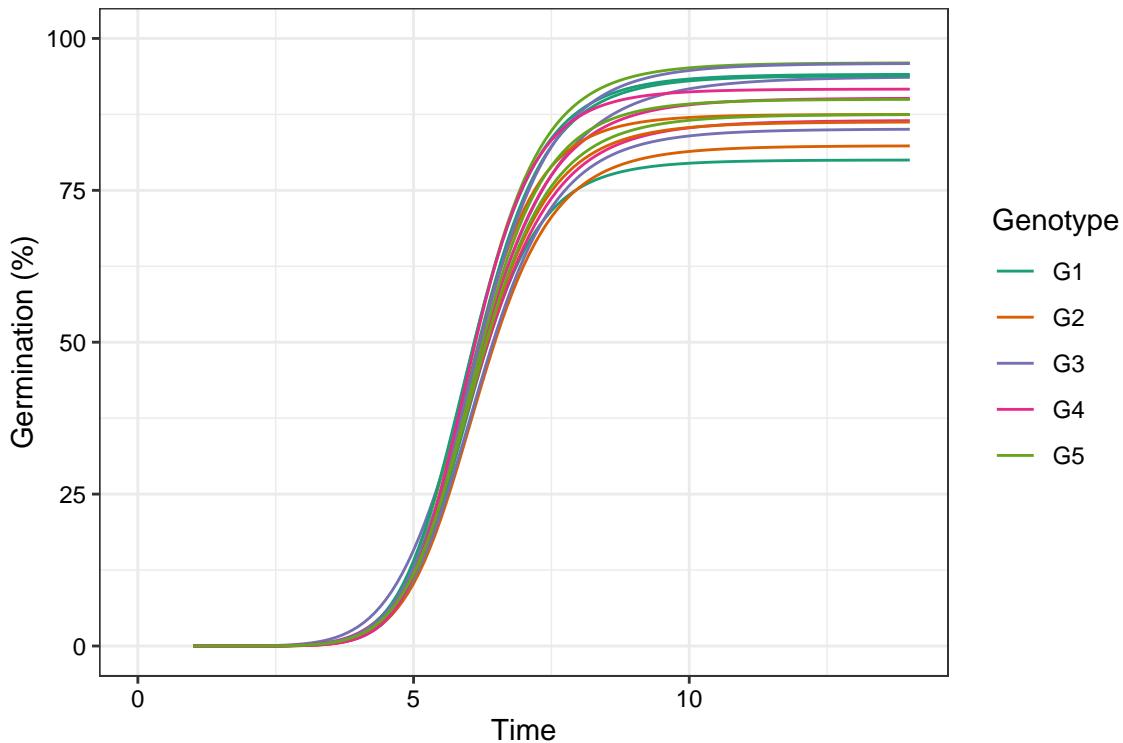
```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "uniformity")
```



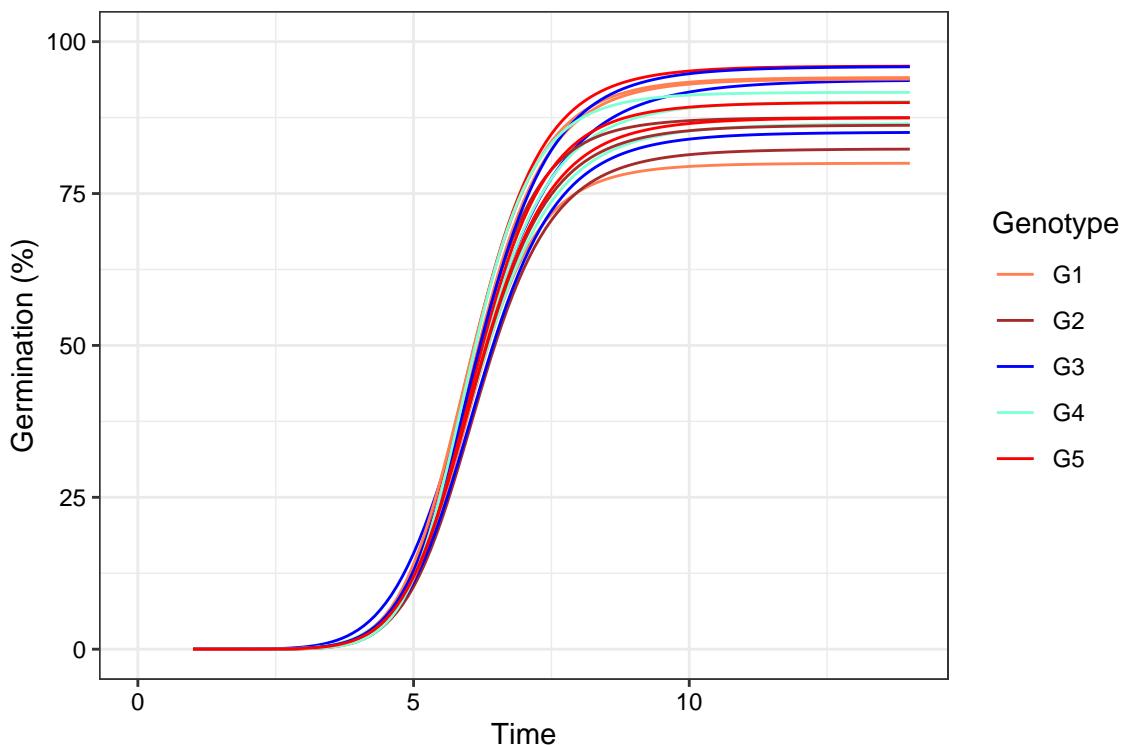
```
# Change colour of curves using ggplot2 options
library(ggplot2)
curvesplot <- plot(fits, group.col = "Genotype")

# 'Dark2' palette from RColorBrewer
```

```
curvesplot + scale_colour_brewer(palette = "Dark2")
```



```
# Manual colours
curvesplot +
  scale_colour_manual(values = c("Coral", "Brown", "Blue",
                                 "Aquamarine", "Red"))
```



Citing germinationmetrics

To cite the R package 'germinationmetrics' in publications use:

Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and Kalyani Srinivasan (2025). germinationmetrics: Seed Germination Indices and Curve Fitting. R package version 0.1.9, <https://github.com/aravind-j/germinationmetrics> <https://cran.r-project.org/package=germinationmetrics>

A BibTeX entry for LaTeX users is

```
@Manual{,
  title = {germinationmetrics: Seed Germination Indices and Curve Fitting},
  author = {J. Aravind and S. {Vimala Devi} and J. Radhamani and Sherry Rachel Jacob and {Kalyani Srinivasan}},
  note = {R package version 0.1.9 https://aravind-j.github.io/germinationmetrics/ https://CRAN.R-project.org/package=germinationmetrics},
  year = {2025},
}
```

This free and open-source software implements academic research by the authors and co-workers. If you use it, please support the project by citing the package.

Session Info

```
sessionInfo()
```

```
R Under development (unstable) (2025-12-09 r89129 ucrt)
Platform: x86_64-w64-mingw32/x64
Running under: Windows 11 x64 (build 26200)

Matrix products: default
  LAPACK version 3.12.1

locale:
[1] LC_COLLATE=English_India.utf8  LC_CTYPE=English_India.utf8    LC_MONETARY=English_India.utf8
[4] LC_NUMERIC=C                 LC_TIME=English_India.utf8

time zone: Asia/Calcutta
tzcode source: internal

attached base packages:
[1] stats      graphics   grDevices  utils      datasets   methods    base

other attached packages:
[1] germinationmetrics_0.1.9 ggplot2_4.0.1           readxl_1.4.5          RCurl_1.98-1.17
[5] testthat_3.3.1

loaded via a namespace (and not attached):
 [1] gtable_0.3.6       xfun_0.54        devtools_2.4.6      remotes_2.5.0      ggrepel_0.9.6      rJa_
 [7] lattice_0.22-7     mathjaxr_2.0-0    vctrs_0.6.5        tools_4.6.0        Rdpack_2.6.4      bitc_
[13] generics_0.1.4     stats4_4.6.0      curl_7.0.0         parallel_4.6.0    tibble_3.3.0      pkgd_
[19] gslnls_1.4.2       Matrix_1.7-4     data.table_1.17.8  RColorBrewer_1.1-3  S7_0.2.1       des_
[25] lifecycle_1.0.4    compiler_4.6.0    farver_2.1.2       stringr_1.6.0      brio_1.1.5       tiny_
[31] htmltools_0.5.9    usethis_3.2.1     yaml_2.3.12       pillar_1.11.1     tidyverse_1.3.1    ellip_
[37] rsconnect_1.7.0    cachem_1.1.0     sessioninfo_1.2.3  tidyselect_1.2.1   digest_0.6.39     strin_
[43] reshape2_1.4.5     pandoc_0.6.6     dplyr_1.1.4       purrr_1.2.0       labeling_0.4.3    rpr_
```

```
[49] fastmap_1.2.0      grid_4.6.0        cli_3.6.5       magrittr_2.0.4    XML_3.99-0.20
[55] pkgbuild_1.4.8     broom_1.0.11      withr_3.0.2     scales_1.4.0     backports_1.5.0
[61] roxygen2_7.3.3     rmarkdown_2.30    cellranger_1.1.0 memoise_2.0.1    evaluate_1.0.5
[67] rbibutils_2.4      rlang_1.1.6       Rcpp_1.1.0.8.1  glue_1.8.0       xml2_1.5.1
[73] rstudioapi_0.17.1   R6_2.6.1         plyr_1.8.9       fs_1.6.6
```

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