# The germinationmetrics Package: A Brief Introduction

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## Overview

The package **germinationmetrics** is a collection of functions which implements various methods for describing the time-course of germination in terms of single-value germination indices as well as fitted curves.

The goal of this vignette is to introduce the users to these functions and get started in describing sequentially recorded germination count data. This document assumes a basic knowledge of R programming language.



## Installation

The package can be installed using the following functions:

```
# Install from CRAN
install.packages('germinationmetrics', dependencies=TRUE)

# Install development version from Github
devtools::install_github("aravind-j/germinationmetrics")
```

Then the package can be loaded using the function

library(germinationmetrics)

-----

Welcome to germinationmetrics version 0.1.6.9000

- # To know how to use this package type:
   browseVignettes(package = 'germinationmetrics')
   for the package vignette.
- # To know whats new in this version type: news(package='germinationmetrics') for the NEWS file.
- # To cite the methods in the package type: citation(package='germinationmetrics')
- # To suppress this message use: suppressPackageStartupMessages(library(germinationmetrics))

## Version History

The current version of the package is 0.1.6. The previous versions are as follows.

Table 1. Version history of germinationmetrics R package.

Version	Date
0.1.0	2018-04-17
0.1.1	2018-07-26
0.1.1.1	2018-10-16
0.1.2	2018-10-31
0.1.3	2019-01-19
0.1.4	2020-06-16
0.1.5	2021-02-17

To know detailed history of changes use news(package='germinationmetrics').

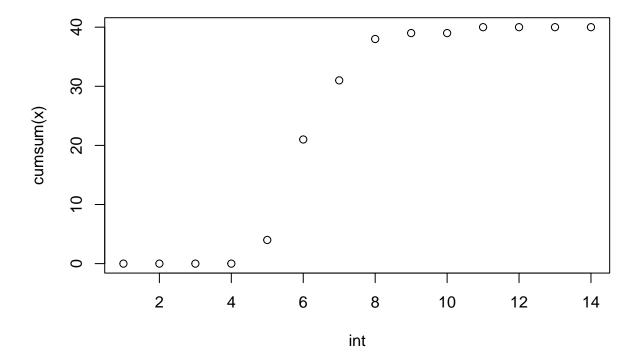
## Germination count data

Typically in a germination test, the germination count data of a fixed number of seeds is recorded at regular intervals for a definite period of time or until all the seeds have germinated. These germination count data can be either partial or cumulative (Table 2).

Table 2 : A typical germination count data.

intervals	counts	cumulative.counts
1	0	0
2	0	0
3	0	0
4	0	0
5	4	4
6	17	21
7	10	31
8	7	38
9	1	39
10	0	39
11	1	40
12	0	40
13	0	40
14	0	40

The time-course of germination can be plotted as follows.



## Single-value germination indices

The details about the single-value germination indices implemented in **germinationmetrics** are described in Table 3.

 ${\bf Table~3:}~{\bf Single-value~germination~indices~implemented~in~germinationmetrics.}$ 

Germination index	Function	Details	Unit	Measures	Reference
Germination percentage or Final germination percentage or Germinability (GP)	GermPercent	It is computed as follows. $GP = \frac{N_g}{N_t} \times 100$ Where, $N_g$ is the number of germinated seeds and $N_t$ is the total number of seeds.	Percentage (%)	Germination capacity	ISTA (2015)
Peak germination percentage $(PGP)$	PeakGermPercent	It is computed as follows. $PGP = \frac{N_{max}}{N_t} \times 100$ Where, $N_{max}$ is the maximum number of seeds germinated per interval.	Percentage (%)	Germination capacity	Vallance (1950); Roh et al. (2004)
Time for the first germination or Germination time lag $(t_0)$	FirstGermTime	It is the time for first germination to occur (e.g. First day of germination). $t_0 = \min \left\{ T_i : N_i \neq 0 \right\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval and $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval)	time	Germination time	Edwards (1932); Czabator (1962); Goloff and Bazzaz (1975); Labouriau (1983a); Ranal (1999); Quintanilla et al. (2000)
Time for the last germination $(t_g)$	LastGermTime	It is the time for last germination to occur (e.g. Last day of germination) $t_g = \max \{T_i : N_i \neq 0\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval and $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval)	time	Germination time	Edwards (1932)
Time spread of germination or Germination distribution	TimeSpreadGerm	It is the difference between time for last germination $(t_g)$ and time for first germination $(t_0)$ .  Time spread of germination = $t_g - t_0$	time	Germination time	Al-Mudaris (1998); Schrader and Graves (2000); Kader (2005)
Peak period of germination or Modal time of germination $(t_{peak})$	PeakGermTime	It is the time in which highest frequency of germinated seeds are observed and need not be unique. $t_{peak} = \{T_i: N_i = N_{max}\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval) and $N_{max}$ is the maximum number of seeds germinated per interval.	time	Germination time	Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Median germination time $(t_{50})$ (Coolbear)	t50	It is the time to reach 50% of final/maximum germination. With argument method specified as "coolbear", it is computed as follows.	time	Germination time	Coolbear et al. (1984)
		$t_{50} = T_i + \frac{(\frac{N+1}{2} - N_i)(T_j - T_i)}{N_j - N_i}$ Where, $t_{50}$ is the median germination time, $N$ is the final number of germinated seeds, and $N_i$ and $N_j$ are the total number of seeds germinated in adjacent counts at time $T_i$ and			
		T <sub>j</sub> respectively, when $N_i < \frac{N+1}{2} < N_j$ .			
Median germination time $(t_{50})$ (Farooq)	t50	With argument method specified as "farooq", it is computed as follows. $t_{50}=T_i+\frac{(\frac{N}{2}-N_i)(T_j-T_i)}{N_j-N_i}$	time	Germination time	Farooq et al. (2005)
		Where, $t_{50}$ is the median germination time, $N$ is the final number of germinated seeds, and $N_i$ and $N_j$ are the total number of seeds germinated in adjacent counts at time $T_i$ and $T_j$ respectively, when $N_i < \frac{N}{2} < N_j$ .			
Mean germination time or Mean length of incubation time $(\overline{T})$ or Germination resistance $(GR)$ or Sprouting index $(SI)$ or Emergence index $(EI)$	MeanGermTime	It is the average length of time required for maximum germination of a seed lot and is estimated according to the following formula. $\overline{T} = \frac{\sum_{i=1}^k N_i T_i}{\sum_{i=1}^k N_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals. It is the inverse of mean germination rate $(\overline{V})$ .	time	Germination time	Edmond and Drapala (1958); Czabator (1962); Smith and Millet (1964); Gordon (1969); Gordon (1971); Mock and Eberhart (1972); Ellis and Roberts (1980) Labouriau (1983a); Ranal and Santana (2006)
		$\overline{T}=rac{1}{\overline{V}}$			

Germination index	Function	Details	Unit	Measures	Reference
Variance of germination time $(s_T^2)$	VarGermTime	It is computed according to the following formula. $s_T^2 = \frac{\sum_{i=1}^k N_i (T_i - \overline{T})^2}{\sum_{i=1}^k N_i - 1}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals.	time <sup>-1</sup>	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Standard error of germination time $(s_{\overline{T}})$	SEGermTime	It signifies the accuracy of the calculation of the mean germination time. It is estimated according to the following formula: $s_{\overline{T}} = \sqrt{\frac{s_T^2}{\sum_{i=1}^k N_i}}$ Where, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval) and $k$ is the total number of time intervals.	time	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Mean germination rate $(\overline{V})$	MeanGermRate	It is computed according to the following formula: $\overline{V} = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals. It is the inverse of mean germination time $(\overline{T})$ . $\overline{V} = \frac{1}{\overline{T}}$	${ m time^{-1}}$	Germination rate	Labouriau and Valadares (1976); Labouriau (1983b); Ranal and Santana (2006)

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Germination index	Function	Details	Unit	Measures	Reference
Speed of accumulated germination	GermSpeedAccumulate	It is the rate of germination in terms of the accumulated/cumulative total number of seeds that germinate in a time interval.  It is estimated as follows.	% time <sup>-1</sup> or count time <sup>-1</sup>	Mixed	Bradbeer (1988); Wardle et al. (1991); Haugland and Brandsaeter (1996); Santana and Ranal (2004)
		$S_{accumulated} = \sum_{i=1}^k \frac{\sum_{j=1}^i N_j}{T_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $\sum_{j=1}^i N_j$ is the cumuative/accumulated number of seeds germinated in the $i$ th interval, and $k$ is the total number of time intervals. Instead of germination counts, germination percentages may			
Corrected	CC	also be used for computation of speed of germination.	time <sup>-1</sup>	Mixed	Frotto and Dumoido (1079)
germination rate index	GermSpeedCorrected	It is computed as follows. $S_{corrected} = \frac{S}{FGP} \label{eq:Scorrected}$	time	Mixed	Evetts and Burnside (1972)
		Where, $S$ is the germination speed computed with germination percentage instead of counts and $FGP$ is the final germination percentage or germinability.			
Weighted germination percentage $(WGP)$	WeightGermPercent	It is estimated as follows. $WGP = \frac{\sum_{i=1}^k (k-i+1)N_i}{k\times N}\times 100$	Percentage (%)	Mixed	Reddy et al. (1985); Reddy (1978)
		Where, $N_i$ is the number of seeds that germinated in the time interval $i$ (not cumulative, but partial count), $N$ is the total number of seeds tested, and $k$ is the total number of time intervals.			
Mean germination percentage per unit time $(\overline{GP})$	MeanGermPercent	It is estimated as follows. $\overline{GP} = \frac{GP}{T_{\rm c}} \label{eq:GP}$	$\% \ {\rm time^{-1}}$	Mixed	Czabator (1962)
, ,		Where, $GP$ is the final germination percentage, $T_k$ is the time at the $k$ th time interval, and $k$ is the total number of time intervals required for final germination.			
Number of seeds germinated per unit time $\overline{N}$	MeanGermNumber	It is estimated as follows. $\overline{N} = \frac{N_g}{T_k}$	count time <sup>-1</sup>	Mixed	Khamassi et al. (2013)
		Where, $N_g$ is the number of germinated seeds at the end of the germination test, $T_k$ is the time at the $k$ th time interval, and $k$ is the total number of time intervals required for final germination.			

Germination index	Function	Details	Unit	Measures	Reference
Timson's index $[\sum 10 \text{ (Ten summation)}, \sum 5 \text{ or } \sum 20] \text{ or Germination energy index } (GEI)$	TimsonsIndex	It is the progressive total of cumulative germination percentage recorded at specific intervals for a set period of time and is estimated in terms of cumulative germination percentage $(G_i)$ as follows. $\Sigma k = \sum_{i=1}^k G_i$ Where, $G_i$ is the cumulative germination percentage in time interval $i$ , and $k$ is the total number of time intervals. It also estimated in terms of partial germination percentage as follows. $\Sigma k = \sum_{i=1}^k g_i(k-j)$ Where, $g_i$ is the germination (not cumulative, but partial germination) in time interval $i$ ( $i$ varying from 0 to $k$ ), $k$ is the total number of time intervals, and $j=i-1$ .	Percentage (%)	Mixed	Grose and Zimmer (1958); Timson (1965); Lyon and Coffelt (1966); Chaudhary and Ghildyal (1970); Negm and Smith (1978); Brown and Mayer (1988); Baskin and Baskin (1998); Goodchild and Walker (1971)
Modified Timson's index $(\Sigma k_{mod})$ (Labouriau)	TimsonsIndex	It is estimated as Timson's index $\Sigma k$ divided by the sum of partial germination percentages. $\Sigma k_{mod} = \frac{\Sigma k}{\sum_{i=1}^k g_i}$	no unit	Mixed	Ranal and Santana (2006)
Modified Timson's index $(\Sigma k_{mod})$ (Khan and Unger)	TimsonsIndex	It is estimated as Timson's index $(\Sigma k)$ divided by the total time period of germination $(T_k)$ . $\Sigma k_{mod} = \frac{\Sigma k}{T_k}$	$\%  ext{ time}^{-1}$	Mixed	Khan and Ungar (1984)
George's index $(GR)$	GermRateGeorge	It is estimated as follows. $GR = \sum_{i=1}^k N_i K_i$ Where $N_i$ is the number of seeds germinated by $i$ th interval and $K_i$ is the number of intervals(eg. days) until the end of the test, and and $k$ is the total number of time intervals.	count	Mixed	George (1961); Tucker and Wright (1965); Nichols and Heydecker (1968)

Germination index	Function	Details	Unit	Measures	Reference
Germination Index $(GI)$ (Melville)	GermIndex	It is estimated as follows. $GI = \sum_{i=1}^k \frac{ (T_k - T_i) \ N_i }{N_t}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval (day for the example), $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $N_t$ is the total number of seeds used in the test, and $k$ is the total number of time intervals.	time	Mixed	Melville et al. (1980)
Germination Index $(GI_{mod})$ (Melville; Santana and Ranal)	GermIndex	It is estimated as follows. $GI_{mod} = \sum_{i=1}^k \frac{ (T_k - T_i)  N_i }{N_g}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval (day for the example), $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $N_g$ is the total number of germinated seeds at the end of the test, and $k$ is the total number of time intervals.	time	Mixed	Melville et al. (1980); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index $(ERI)$ or Germination Rate Index (Shmueli and Goldberg)	EmergenceRateIndex	It is estimated as follows. $ERI = \sum_{i=i_0}^{k-1} N_i(k-i)$ Where, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $i_0$ is the time interval when emergence/germination started, and $k$ is the total number of time intervals.	count	Mixed	Shmueli and Goldberg (1971)
Modified Emergence Rate Index $(ERI_{mod})$ or Modified Germination Rate Index (Shmueli and Goldberg; Santana and Ranal)	EmergenceRateIndex	It is estimated by dividing Emergence rate index $(ERI)$ by total number of emerged seedlings (or germinated seeds). $ERI_{mod} = \frac{\sum_{i=i_0}^{k-1} N_i(k-i)}{N_g} = \frac{ERI}{N_g}$ Where, $N_g$ is the total number of germinated seeds at the end of the test, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $i_0$ is the time interval when emergence/germination started, and $k$ is the total number of time intervals.	no unit	Mixed	Shmueli and Goldberg (1971); Santana and Ranal (2004); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Germination value $(GV)$ (Diavanshir and Pourbiek)	GermValue	It is computed as follows. $GV = \frac{\sum DGS}{N} \times GP \times c$ Where, $DGS$ is the daily germination speed computed by dividing cumulative germination percentage by the number of days since the since the onset of germination, $N$ is the frequency or number of DGS calculated during the test, $GP$ is the germination percentage expressed over 100, and $c$ is a constant. The value of $c$ is decided on the basis of average daily speed of germination $(\frac{\sum DGS}{N})$ . If it is less than 10, then $c$ value of 10 can be used and if it is more than 10, then value of 7 or 8 can be used for $c$ . $GV$ value can be modified $(GV_{mod})$ , to consider the entire duration from the beginning of the test instead of just from the onset of germination.	$\%^2~{ m time^{-1}}$	Mixed	Djavanshir and Pourbeik (1976); Brown and Mayer (1988)
Coefficient of uniformity of germination $(CUG)$	CUGerm	It is computed as follows. $CUG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k (\overline{T} - T_i)^2 N_i}$ Where, $\overline{T}$ is the the mean germination time, $T_i$ is the time from the start of the experiment to the $i$ th interval (day for the example), $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals.	${ m time^{-2}}$	Germination unifromity	Heydecker (1972); Bewley and Black (1994)
Coefficient of variation of the germination time $(CV_T)$	CVGermTime	It is estimated as follows. $CV_T=\sqrt{\frac{s_T^2}{\overline{T}}}$ Where, $s_T^2$ is the variance of germination time and $\overline{T}$ is the mean germination time.	no unit	Germination unifromity	Gomes (1960); Ranal and Santana (2006)
Synchronization index $(\overline{E})$ or Uncertainty of the germination process $(U)$ or informational entropy $(H)$	GermUncertainty	It is estimated as follows. $\overline{E} = -\sum_{i=1}^k f_i \log_2 f_i$ Where, $f_i$ is the relative frequency of germination $(f_i = \frac{N_i}{\sum_{i=1}^k N_i}),  N_i \text{ is the number of seeds germinated on the}$ $i$ th time interval, and $k$ is the total number of time intervals.	bit	Germination synchrony	Shannon (1948); Labouriau and Valadares (1976); Labouriau (1983b)

Germination index	Function	Details	Unit	Measures	Reference
Synchrony of germination $(Z \text{ index})$	GermSynchrony	It is computed as follows. $Z = \frac{\sum_{i=1}^k C_{N_i,2}}{C_{\Sigma N_i,2}}$ Where, $C_{N_i,2}$ is the partial combination of the two germinated seeds from among $N_i$ , the number of seeds germinated on the $i$ th time interval (estimated as $C_{N_i,2} = \frac{N_i(N_i-1)}{2}$ ), and $C_{\Sigma N_i,2}$ is the partial combination of the two germinated seeds from among the total number of seeds germinated at the final count, assuming that all seeds that germinated did so simultaneously.	no unit	Germination synchrony	Primack (1985); Ranal and Santana (2006)

### Examples

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z \leftarrow c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)</pre>
# From partial germination counts
GermPercent(germ.counts = x, total.seeds = 50)
GermPercent()
[1] 80
PeakGermPercent(germ.counts = x, intervals = int, total.seeds = 50)
[1] 34
# For multiple peak germination times
PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50)
Warning in PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50): Multiple peak germinati
[1] 22
# From cumulative germination counts
GermPercent(germ.counts = y, total.seeds = 50, partial = FALSE)
[1] 80
PeakGermPercent(germ.counts = y, intervals = int, total.seeds = 50,
                partial = FALSE)
[1] 34
# For multiple peak germination times
PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50,
                partial = FALSE)
Warning in PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50, : Multiple peak
exist.
[1] 22
# From number of germinated seeds
GermPercent(germinated.seeds = 40, total.seeds = 50)
[1] 80
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z \leftarrow c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)</pre>
```

# From partial germination counts

t50()

```
FirstGermTime(germ.counts = x, intervals = int)
FirstGermTime(), LastGermTime(), PeakGermTime(), TimeSpreadGerm()
[1] 5
LastGermTime(germ.counts = x, intervals = int)
[1] 11
TimeSpreadGerm(germ.counts = x, intervals = int)
[1] 6
PeakGermTime(germ.counts = x, intervals = int)
[1] 6
# For multiple peak germination times
PeakGermTime(germ.counts = z, intervals = int)
Warning in PeakGermTime(germ.counts = z, intervals = int): Multiple peak germination times exist.
[1] 5 6
# From cumulative germination counts
FirstGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 5
LastGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 11
TimeSpreadGerm(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
PeakGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
# For multiple peak germination time
PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE)
Warning in PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE): Multiple peak germing
exist.
[1] 5 6
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
t50(germ.counts = x, intervals = int, method = "coolbear")
```

```
[1] 5.970588
t50(germ.counts = x, intervals = int, method = "farooq")
[1] 5.941176
# From cumulative germination counts
t50(germ.counts = y, intervals = int, partial = FALSE, method = "coolbear")
[1] 5.970588
t50(germ.counts = y, intervals = int, partial = FALSE, method = "farooq")
[1] 5.941176
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermTime(germ.counts = x, intervals = int)
MeanGermTime(), VarGermTime(), SEGermTime(), CVGermTime()
[1] 6.7
VarGermTime(germ.counts = x, intervals = int)
[1] 1.446154
SEGermTime(germ.counts = x, intervals = int)
[1] 0.1901416
CVGermTime(germ.counts = x, intervals = int)
[1] 0.1794868
# From cumulative germination counts
MeanGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.7
VarGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 19.04012
SEGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.2394781
CVGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.6512685
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
```

```
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermRate(germ.counts = x, intervals = int)
MeanGermRate(), CVG(), VarGermRate(), SEGermRate(), GermRateRecip()
[1] 0.1492537
CVG(germ.counts = x, intervals = int)
[1] 14.92537
VarGermRate(germ.counts = x, intervals = int)
[1] 0.0007176543
SEGermRate(germ.counts = x, intervals = int)
[1] 0.004235724
GermRateRecip(germ.counts = x, intervals = int, method = "coolbear")
[1] 0.1674877
GermRateRecip(germ.counts = x, intervals = int, method = "farooq")
[1] 0.1683168
# From cumulative germination counts
MeanGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.1492537
CVG(germ.counts = y, intervals = int, partial = FALSE)
[1] 14.92537
VarGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.009448666
SEGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.005334776
GermRateRecip(germ.counts = y, intervals = int,
              method = "coolbear", partial = FALSE)
[1] 0.1674877
GermRateRecip(germ.counts = y, intervals = int,
              method = "farooq", partial = FALSE)
[1] 0.1683168
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
```

```
# From partial germination counts
GermSpeed(germ.counts = x, intervals = int)
GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)
[1] 34.61567
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                  method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "accumulated")
[1] 0.8653917
# From partial germination counts (with percentages instead of counts)
GermSpeed(germ.counts = x, intervals = int,
         percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                     percent = TRUE, total.seeds = 50)
[1] 69.23134
# From cumulative germination counts
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.138925
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
[1] 34.61567
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "accumulated")
[1] 0.8653917
# From cumulative germination counts (with percentages instead of counts)
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
         percent = TRUE, total.seeds = 50)
```

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
                     percent = TRUE, total.seeds = 50)
[1] 69.23134
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
GermSpeed(germ.counts = x, intervals = int)
GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)
[1] 34.61567
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "accumulated")
[1] 0.8653917
# From partial germination counts (with percentages instead of counts)
GermSpeed(germ.counts = x, intervals = int,
         percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                     percent = TRUE, total.seeds = 50)
[1] 69.23134
# From cumulative germination counts
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.138925
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
[1] 34.61567
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "accumulated")
```

```
[1] 0.8653917
# From cumulative germination counts (with percentages instead of counts)
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
         percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
              percent = TRUE, total.seeds = 50)
[1] 69.23134
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
#-----
WeightGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
WeightGermPercent()
[1] 47.42857
# From cumulative germination counts
WeightGermPercent(germ.counts = y, total.seeds = 50, intervals = int,
              partial = FALSE)
[1] 47.42857
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
MeanGermPercent(), MeanGermNumber()
[1] 5.714286
MeanGermNumber(germ.counts = x, intervals = int)
[1] 2.857143
# From cumulative germination counts
MeanGermPercent(germ.counts = y, total.seeds = 50, intervals = int, partial = FALSE)
[1] 5.714286
MeanGermNumber(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 2.857143

```
# From number of germinated seeds
MeanGermPercent(germinated.seeds = 40, total.seeds = 50, intervals = int)
[1] 5.714286
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
# Wihout max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50)
TimsonsIndex(), GermRateGeorge()
[1] 664
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "none")
[1] 664
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             modification = "labouriau")
[1] 8.3
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             modification = "khanungar")
[1] 47.42857
GermRateGeorge(germ.counts = x, intervals = int)
[1] 332
# With max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50, max = 10)
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "none")
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "labouriau")
[1] 4.410256
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "khanungar")
[1] 24.57143
GermRateGeorge(germ.counts = x, intervals = int, max = 10)
```

```
[1] 172
GermRateGeorge(germ.counts = x, intervals = int, max = 14)
[1] 332
# From cumulative germination counts
#-----
# Wihout max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
  total.seeds = 50)
[1] 664
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
            modification = "none")
Γ17 664
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
            modification = "labouriau")
[1] 8.3
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
            modification = "khanungar")
[1] 47.42857
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,)
[1] 332
# With max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50, max = 10)
[1] 344
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
            max = 10, modification = "none")
[1] 344
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50.
            max = 10, modification = "labouriau")
[1] 4.410256
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
            max = 10, modification = "khanungar")
[1] 24.57143
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
             max = 10
```

```
[1] 172
```

[1] 332

### GermIndex()

[1] 5.84

[1] 5.84

[1] 7.3

[1] 5.84

[1] 5.84

[1] 7.3

#### EmergenceRateIndex()

```
[1] 292
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "shmueligoldberg")
[1] 292
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "sgsantanaranal")
[1] 7.3
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "bilbrowanjura")
[1] 5.970149
EmergenceRateIndex(germ.counts = x, intervals = int,
                 total.seeds = 50, method = "fakorede")
[1] 8.375
# From cumulative germination counts
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,)
[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "shmueligoldberg")
[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "sgsantanaranal")
[1] 7.3
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "bilbrowanjura")
[1] 5.970149
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   total.seeds = 50, method = "fakorede")
[1] 8.375
x \leftarrow c(0, 0, 34, 40, 21, 10, 4, 5, 3, 5, 8, 7, 7, 6, 6, 4, 0, 2, 0, 2)
y \leftarrow c(0, 0, 34, 74, 95, 105, 109, 114, 117, 122, 130, 137, 144, 150,
     156, 160, 160, 162, 162, 164)
int <- 1:length(x)</pre>
total.seeds = 200
# From partial germination counts
```

PeakValue(), GermValue()

PeakValue(germ.counts = x, intervals = int, total.seeds = 200)

## [1] 9.5

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "czabator")
```

## \$`Germination Value`

[1] 38.95

## [[2]]

	germ.counts	${\tt intervals}$	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

GermValue(germ.counts = x, intervals = int, total.seeds = 200,
 method = "dp", k = 10)

## \$`Germination Value`

[1] 53.36595

### [[2]]

LL∠	7]]						
	germ.counts	${\tt intervals}$	${\tt Cumulative.germ.counts}$	${\tt Cumulative.germ.percent}$	DGS	${\tt SumDGSbyN}$	GV
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250
7	4	7	109	54.5	7.785714	8.190476	44.638095
8	5	8	114	57.0	7.125000	8.012897	45.673512
9	3	9	117	58.5	6.500000	7.796769	45.611097
10	5	10	122	61.0	6.100000	7.584673	46.266503
11	8	11	130	65.0	5.909091	7.398497	48.090230
12	7	12	137	68.5	5.708333	7.229481	49.521942
13	7	13	144	72.0	5.538462	7.075752	50.945411
14	6	14	150	75.0	5.357143	6.932534	51.994006
15	6	15	156	78.0	5.200000	6.799262	53.034246
16	4	16	160	80.0	5.000000	6.670744	53.365948
17	0	17	160	80.0	4.705882	6.539753	52.318022
18	2	18	162	81.0	4.500000	6.412268	51.939373
19	0	19	162	81.0	4.263158	6.285850	50.915385
20	2	20	164	82.0	4.100000	6.164414	50.548194

[1] 16

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "czabator", from.onset = FALSE)
```

#### \$`Germination Value`

[1] 38.95

## [[2]]

	germ.counts	intervals	${\tt Cumulative.germ.counts}$	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

GermValue(germ.counts = x, intervals = int, total.seeds = 200,
 method = "dp", k = 10, from.onset = FALSE)

## \$`Germination Value`

[1] 46.6952

## [[2]]

	-,,						
	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	SumDGSbyN	GV
1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111
4	40	4	74	37.0	9.250000	3.729167	13.797917
5	21	5	95	47.5	9.500000	4.883333	23.195833
6	10	6	105	52.5	8.750000	5.527778	29.020833
7	4	7	109	54.5	7.785714	5.850340	31.884354
8	5	8	114	57.0	7.125000	6.009673	34.255134
9	3	9	117	58.5	6.500000	6.064153	35.475298
10	5	10	122	61.0	6.100000	6.067738	37.013202
11	8	11	130	65.0	5.909091	6.053316	39.346552
12	7	12	137	68.5	5.708333	6.024567	41.268285
13	7	13	144	72.0	5.538462	5.987174	43.107655
14	6	14	150	75.0	5.357143	5.942172	44.566291

15	6	15	156	78.0 5.200000	5.892694 45.963013
16	4	16	160	80.0 5.000000	5.836901 46.695205
17	0	17	160	80.0 4.705882	5.770370 46.162961
18	2	18	162	81.0 4.500000	5.699794 46.168331
19	0	19	162	81.0 4.263158	5.624182 45.555871
20	2	20	164	82.0 4.100000	5.547972 45.493374

[1] 16

## [1] 9.5

## \$`Germination Value`

[1] 38.95

#### [[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

## \$`Germination Value`

[1] 53.36595

#### [[2]]

	germ.counts	${\tt intervals}$	Cumulative.germ.counts	Cumulative.germ.percent	DGS	${\tt SumDGSbyN}$	GV
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250

7	4	7	109	54.5 7.785714	8.190476 44.638095
8	5	8	114	57.0 7.125000	8.012897 45.673512
9	3	9	117	58.5 6.500000	7.796769 45.611097
10	5	10	122	61.0 6.100000	7.584673 46.266503
11	8	11	130	65.0 5.909091	7.398497 48.090230
12	7	12	137	68.5 5.708333	7.229481 49.521942
13	7	13	144	72.0 5.538462	7.075752 50.945411
14	6	14	150	75.0 5.357143	6.932534 51.994006
15	6	15	156	78.0 5.200000	6.799262 53.034246
16	4	16	160	80.0 5.000000	6.670744 53.365948
17	0	17	160	80.0 4.705882	6.539753 52.318022
18	2	18	162	81.0 4.500000	6.412268 51.939373
19	0	19	162	81.0 4.263158	6.285850 50.915385
20	2	20	164	82.0 4.100000	6.164414 50.548194

[1] 16

## \$`Germination Value`

[1] 38.95

#### [[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

## \$`Germination Value`

[1] 46.6952

## [[2]]

germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent

DGS SumDGSbyN

0	1	0	0.0 0.000000	0.000000 0.000000
0	2	0	0.0 0.000000	0.000000 0.000000
34	3	34	17.0 5.666667	1.888889 3.211111
40	4	74	37.0 9.250000	3.729167 13.797917
21	5	95	47.5 9.500000	4.883333 23.195833
10	6	105	52.5 8.750000	5.527778 29.020833
4	7	109	54.5 7.785714	5.850340 31.884354
5	8	114	57.0 7.125000	6.009673 34.255134
3	9	117	58.5 6.500000	6.064153 35.475298
5	10	122	61.0 6.100000	6.067738 37.013202
8	11	130	65.0 5.909091	6.053316 39.346552
7	12	137	68.5 5.708333	6.024567 41.268285
7	13	144	72.0 5.538462	5.987174 43.107655
6	14	150	75.0 5.357143	5.942172 44.566291
6	15	156	78.0 5.200000	5.892694 45.963013
4	16	160	80.0 5.000000	5.836901 46.695205
0	17	160	80.0 4.705882	5.770370 46.162961
2	18	162	81.0 4.500000	5.699794 46.168331
0	19	162	81.0 4.263158	5.624182 45.555871
2	20	164	82.0 4.100000	5.547972 45.493374
	0 34 40 21 10 4 5 3 5 8 7 7 6 6 6 4 0 2	0 2 34 3 40 4 21 5 10 6 4 7 5 8 3 9 5 10 8 11 7 12 7 13 6 14 6 15 4 16 0 17 2 18 0 19	0       2       0         34       3       34         40       4       74         21       5       95         10       6       105         4       7       109         5       8       114         3       9       117         5       10       122         8       11       130         7       12       137         7       13       144         6       14       150         6       15       156         4       16       160         0       17       160         2       18       162         0       19       162	0       2       0       0.0 0.000000         34       3       34       17.0 5.666667         40       4       74       37.0 9.250000         21       5       95       47.5 9.500000         10       6       105       52.5 8.750000         4       7       109       54.5 7.785714         5       8       114       57.0 7.125000         3       9       117       58.5 6.500000         5       10       122       61.0 6.100000         8       11       130       65.0 5.909091         7       12       137       68.5 5.708333         7       13       144       72.0 5.538462         6       14       150       75.0 5.357143         6       15       156       78.0 5.200000         4       16       160       80.0 5.000000         0       17       160       80.0 4.705882         2       18       162       81.0 4.263158

[1] 16

#### CUGerm()

[1] 0.7092199

```
# From cumulative germination counts
#-----
CUGerm(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 0.05267935

## GermSynchrony(), GermUncertainty()

[1] 0.2666667

[1] 2.062987

## Non-linear regression analysis

Several mathematical functions have been used to fit the cumulative germination count data and describe the germination process by non-linear regression analysis. They include functions such as Richard's, Weibull, logistic, log-logistic, gaussian, four-parameter hill function etc. Currently germinationmetrics implements the four-parameter hill function to fit the count data and computed various associated metrics.

## Four-parameter hill function

The four-parameter hill function defined as follows (El-Kassaby et al., 2008).

GermUncertainty(germ.counts = y, intervals = int, partial = FALSE)

$$f(x) = y = y_0 + \frac{ax^b}{x^b + c^b}$$

Where, y is the cumulative germination percentage at time x,  $y_0$  is the intercept on the y axis, a is the asymptote, b is a mathematical parameter controlling the shape and steepness of the germination curve and c is the "half-maximal activation level".

The details of various parameters that are computed from this function are given in Table 4.

**Table 4** Germination parameters estimated from the four-parameter hill function.

Germination parameters	Details	Unit	Measures
y intercept $(y_0)$	The intercept on the y axis.		
Asymptote $(a)$	It is the maximum cumulative germination percentage, which is equivalent to germination capacity.	%	Germination capacity
Shape and steepness $(b)$	Mathematical parameter controlling the shape and steepness of the germination curve. The larger the $b$ , the steeper the rise toward the asymptote $a$ , and the shorter the time between germination onset and maximum germination.		Germination rate
Half-maximal activation level $(c)$	Time required for $50\%$ of viable seeds to germinate.	time	Germination time

Germination parameters	Details	Unit	Measures
lag	It is the time at germination onset and is computed by solving four-parameter hill function after setting y to 0 as follows.	time	Germination time
	$lag = b\sqrt{\frac{-y_0c^b}{a+y_0}}$		
$D_{lag-50}$	The duration between the time at germination onset $(lag)$ and that at 50% germination $(c)$ .	time	Germination time
$t_{50_{total}}$	Time required for $50\%$ of total seeds to germinate.	time	Germination time
$t_{50_{germinated}}$	Time required for 50% of viable/germinated seeds to germinate	time	Germination time
$t_{x_{total}}$	Time required for $x\%$ of total seeds to germinate.	time	Germination time
$t_{x_{germinated}}$	Time required for $x\%$ of viable/germinated seeds to germinate	time	Germination time
Uniformity $(U_{t_{max}-t_{min}})$	It is the time interval between the percentages of viable seeds specified in the arguments umin and umin to germinate.	time	Germination time
Time at maximum germination rate $(TMGR)$	The partial derivative of the four-parameter hill function gives the instantaneous rate of germination $(s)$ as follows.	time	Germination time
	$s = \frac{\partial y}{\partial x} = \frac{abc^b x^{b-1}}{(c^b + x^b)^2}$		
	From this function for instantaneous rate of germination, $TMGR$ can be estimated as follows.		
	$TMGR = b\sqrt{\frac{c^b(b-1)}{b+1}}$		
	It represents the point in time when the instantaneous rate of germination starts to decline.		
Area under the curve $(AUC)$	It is obtained by integration of the fitted curve between time 0 and time specified in the argument tmax.		Mixed
MGT	Calculated by integration of the fitted curve and proper normalisation.	time	Germination time
Skewness	It is computed as follows.		
	$\frac{MGT}{t_{50_{germinated}}}$		

## Examples

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
total.seeds = 50
# From partial germination counts
#-----
FourPHFfit(germ.counts = x, intervals = int, total.seeds = 50, tmax = 20)
FourPHFfit()
$data
  gp csgp intervals
  0 0 1
2
 0
     0
               2
              3
3
  0
      0
4 0
     0
5 8 8
6 34 42
              6
7 20
      62
              7
8 14 76
              8
9 2 78
              9
10 0 78
              10
11 2 80
              11
12 0 80
              12
13 0 80
              13
14 0 80
              14
$Parameters
term estimate std.error statistic p.value
1 a 80.000000 1.24158595 64.43372 1.973240e-14
 b 9.881947 0.70779379 13.96162 6.952322e-08
3 c 6.034954 0.04952654 121.85294 3.399385e-17
4 y0 0.000000 0.91607007 0.00000 1.000000e+00
$Fit
                   finTol logLik AIC BIC deviance df.residual nobs
    sigma isConv
1 1.769385 TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723 10 14
$a
[1] 80
$b
[1] 9.881947
[1] 6.034954
$y0
[1] 0
$lag
[1] 0
```

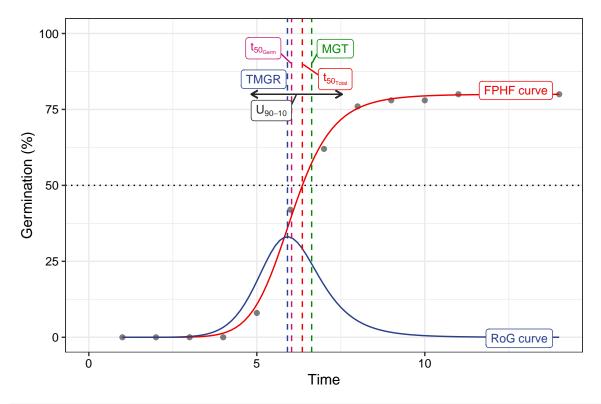
8

```
$Dlag50
[1] 6.034954
$t50.total
[1] 6.355122
$txp.total
     10
             60
4.956266 6.744598
$t50.Germinated
[1] 6.034954
$txp.Germinated
     10
             60
4.831809 6.287724
$Uniformity
    90
               10 uniformity
 7.537688 4.831809 2.705880
$TMGR
[1] 5.912195
$AUC
[1] 1108.975
$MGT
[1] 6.632252
$Skewness
[1] 1.098973
[1] "#1. Relative error in the sum of squares is at most `ftol'."
$isConv
[1] TRUE
attr(,"class")
[1] "FourPHFfit" "list"
# From cumulative germination counts
#-----
FourPHFfit(germ.counts = y, intervals = int, total.seeds = 50, tmax = 20,
partial = FALSE)
$data
  gp csgp intervals
       0
                 1
1
  0
2
  0
       0
      0
3
  0
                3
  0
      0
```

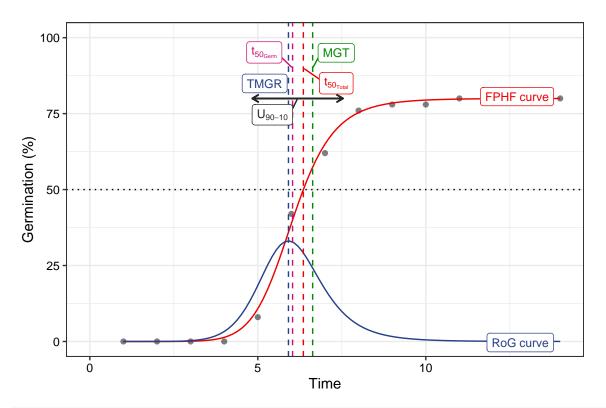
```
6 34
       42
7
  20
       62
                 7
8
  14
       76
                 8
9
   2
       78
                 9
10 0
       78
                10
11 2 80
                11
12 0
       80
                12
13 0
       80
                13
14 0
       80
                 14
$Parameters
 term estimate std.error statistic
                                       p.value
1 a 80.000000 1.2415867 64.43368 1.973252e-14
  b 9.881927 0.7077918 13.96163 6.952270e-08
  c 6.034953 0.0495266 121.85275 3.399437e-17
   y0 0.000000 0.9160705 0.00000 1.000000e+00
$Fit
                                logLik
    sigma isConv
                      finTol
                                           AIC
                                                   BIC deviance df.residual nobs
1 1.769385 TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723
$a
[1] 80
$b
[1] 9.881927
$c
[1] 6.034953
$y0
[1] 0
$lag
[1] 0
$Dlag50
[1] 6.034953
$t50.total
[1] 6.355121
$txp.total
     10
              60
4.956263 6.744599
$t50.Germinated
[1] 6.034953
$txp.Germinated
     10
              60
4.831806 6.287723
```

\$Uniformity

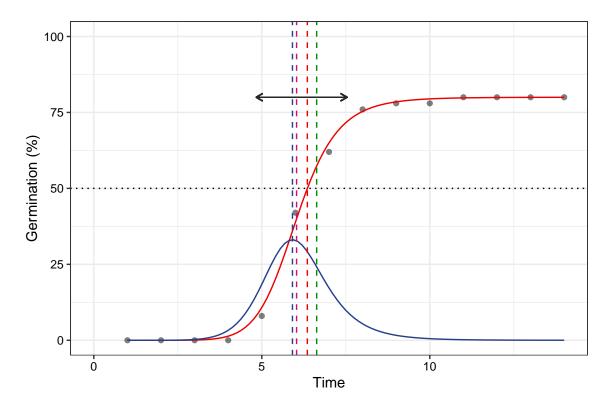
```
10 uniformity
 7.537691 4.831806 2.705885
$TMGR
[1] 5.912194
$AUC
[1] 1108.976
$MGT
[1] 6.632252
$Skewness
[1] 1.098973
$msg
[1] "#1. Relative error in the sum of squares is at most `ftol'."
$isConv
[1] TRUE
attr(,"class")
[1] "FourPHFfit" "list"
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
total.seeds = 50
# From partial germination counts
#-----
fit1 <- FourPHFfit(germ.counts = x, intervals = int,</pre>
                 total.seeds = 50, tmax = 20)
# From cumulative germination counts
fit2 <- FourPHFfit(germ.counts = y, intervals = int,</pre>
                 total.seeds = 50, tmax = 20, partial = FALSE)
# Default plots
plot(fit1)
```



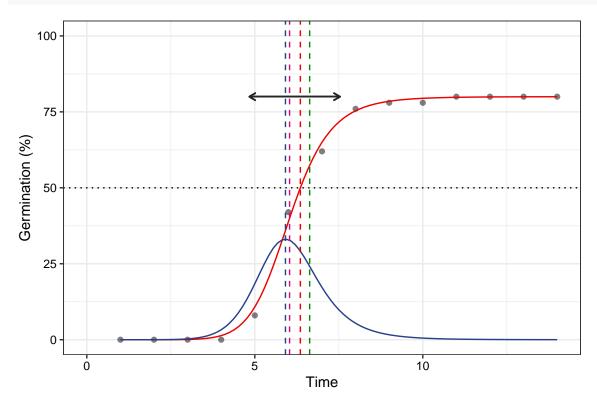
## plot(fit2)



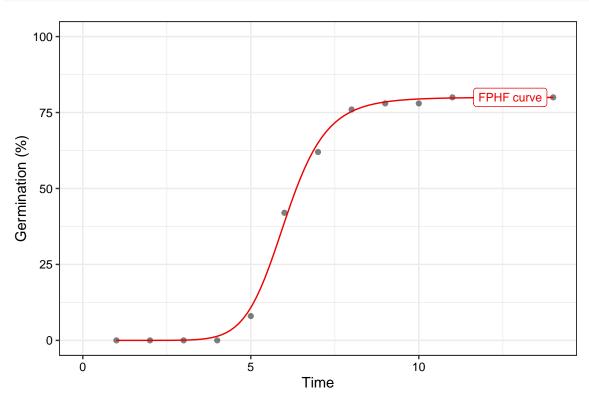
```
# No labels
plot(fit1, plotlabels = FALSE)
```

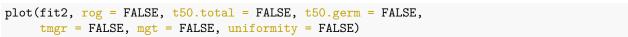


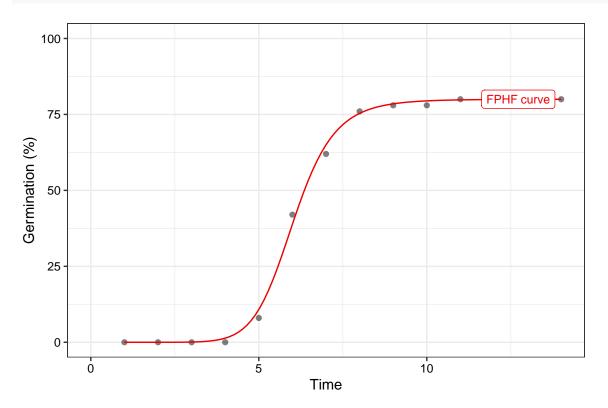




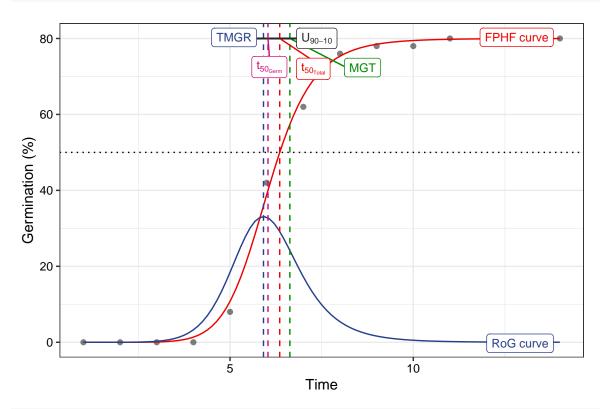
```
# Only the FPHF curve
plot(fit1, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
    tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```



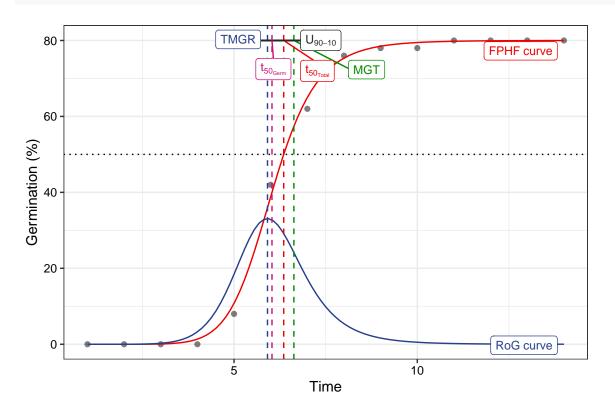




# # Without y axis limits adjustment plot(fit1, limits = FALSE)



### plot(fit2, limits = FALSE)



## Wrapper functions

6.857143

6.866667

6.891304

Wrapper functions germination.indices() and FourPHFfit.bulk() are available in the package for computing results for multiple samples in batch from a data frame of germination counts recorded at specific time intervals.

**germination.indices()** This wrapper function can be used to compute several germination indices simultaneously for multiple samples in batch.

```
data(gcdata)
counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04",</pre>
                                                                      "Day05",
                             "Day06", "Day07", "Day08", "Day09",
                                                                      "Day10",
                             "Day11", "Day12", "Day13", "Day14")
germination.indices(gcdata, total.seeds.col = "Total Seeds",
                      counts.intervals.cols = counts.per.intervals,
                      intervals = 1:14, partial = TRUE, max.int = 5)
   Genotype Rep Day01 Day02 Day03 Day04 Day05 Day06 Day07 Day08 Day09 Day10 Day11 Day12 Day13 Day14 Tot
                                    0
                                                        17
                                                              10
                                                                             1
                                                                                                               0
1
          G1
                                                                      7
                                                                                                               0
2
          G2
                1
                      0
                             0
                                    0
                                           1
                                                  3
                                                        15
                                                              13
                                                                      6
                                                                             2
                                                                                    1
                                                                                           0
                                                                                                  1
                                                                                                        0
3
                      0
                                                  3
                                                                             2
                                                                                                        0
                                                                                                               0
          G3
                1
                             0
                                    0
                                           2
                                                        18
                                                               9
                                                                      8
                                                                                    1
                                                                                           1
                                                                                                  1
4
          G4
                1
                      0
                             0
                                    0
                                           0
                                                  4
                                                       19
                                                              12
                                                                      6
                                                                             2
                                                                                                  1
                                                                                                        0
                                                                                                               0
                                                                                    1
                                                                                           1
5
          G5
               1
                      0
                             0
                                    0
                                           0
                                                  5
                                                       20
                                                              12
                                                                      8
                                                                             1
                                                                                    0
                                                                                           0
                                                                                                  1
                                                                                                        1
                                                                                                               0
                                                                      7
6
                2
                             0
                                    0
                                                  3
                                                                                                        0
          G1
                      0
                                           0
                                                       21
                                                              11
                                                                             1
                                                                                    1
                                                                                           1
                                                                                                  1
                                                                                                               0
                2
                                                                      7
7
          G2
                      0
                             0
                                    0
                                           0
                                                  4
                                                        18
                                                              11
                                                                             1
                                                                                    0
                                                                                           1
                                                                                                  0
                                                                                                        0
                                                                                                               0
8
          G3
                2
                      0
                             0
                                    0
                                                  3
                                                                      6
                                                                             2
                                                                                                        0
                                                                                                               0
                                           1
                                                        14
                                                              12
                                                                                    1
                                                                                           0
                                                                                                  1
9
          G4
                2
                      0
                             0
                                    0
                                           1
                                                  3
                                                        19
                                                              10
                                                                      8
                                                                             1
                                                                                    1
                                                                                           1
                                                                                                  1
                                                                                                        0
                                                                                                               0
                2
                                                                             2
10
          G5
                      0
                             0
                                    0
                                           0
                                                  4
                                                        18
                                                              13
                                                                      6
                                                                                    1
                                                                                           0
                                                                                                  1
                                                                                                        0
                                                                                                               0
11
          G1
               3
                      0
                             0
                                    0
                                                  5
                                                       21
                                                                      8
                                                                                           0
                                                                                                               0
                                           0
                                                              11
                                                                             1
                                                                                    0
                                                                                                  1
                                                                                                        1
                                                                      7
12
          G2
               3
                      0
                             0
                                    0
                                           0
                                                  3
                                                       20
                                                              10
                                                                             1
                                                                                    1
                                                                                           1
                                                                                                  1
                                                                                                        0
                                                                                                               0
13
          G3
                3
                      0
                             0
                                    0
                                           0
                                                  4
                                                       19
                                                              12
                                                                      8
                                                                                           0
                                                                                                               0
                                                                             1
                                                                                    1
                                                                                                  1
                                                                                                        1
14
          G4
                3
                      0
                             0
                                    0
                                           0
                                                  3
                                                       21
                                                              11
                                                                      6
                                                                             1
                                                                                    0
                                                                                           1
                                                                                                  1
                                                                                                        0
                                                                                                               0
15
          G5
                3
                      0
                             0
                                    0
                                           0
                                                  4
                                                        17
                                                              10
                                                                      8
                                                                             1
                                                                                    1
                                                                                           1
                                                                                                  0
                                                                                                        0
                                                                                                               0
   GermPercent PeakGermPercent FirstGermTime LastGermTime PeakGermTime TimeSpreadGerm t50 Coolbear t50
      80.00000
                         34.00000
                                                5
                                                                              6
                                                                                               6
                                                                                                                   5.
1
                                                              11
                                                                                                      5.970588
2
      82.35294
                         29.41176
                                                 4
                                                              12
                                                                              6
                                                                                               8
                                                                                                      6.192308
                                                                                                                   6.
                                                 4
                                                              12
                                                                              6
                                                                                               8
                                                                                                                   5.
3
      93.75000
                         37.50000
                                                                                                      6.000000
                                                 5
                                                                              6
                                                                                               7
4
      90.19608
                         37.25490
                                                              12
                                                                                                      6.041667
                                                                                                                   6.
5
                                                 5
                                                              13
                                                                              6
                                                                                                      5.975000
      96.00000
                         40.00000
                                                                                               8
                                                                                                                   5.
6
      93.87755
                         42.85714
                                                 5
                                                              12
                                                                              6
                                                                                               7
                                                                                                      5.976190
                                                                                                                   5.
7
      87.50000
                         37.50000
                                                 5
                                                              11
                                                                              6
                                                                                               6
                                                                                                      5.972222
8
      85.10638
                         29.78723
                                                 4
                                                              12
                                                                              6
                                                                                               8
                                                                                                      6.208333
                                                                                                                   6.
9
                                                 4
                                                              12
                                                                              6
      86.53846
                         36.53846
                                                                                               8
                                                                                                      6.000000
                                                                                                                   5.
                         36.00000
10
      90.00000
                                                 5
                                                              12
                                                                              6
                                                                                               7
                                                                                                      6.076923
                                                                                                                   6.
                                                 5
                                                                              6
11
      94.11765
                         41.17647
                                                              13
                                                                                               8
                                                                                                      5.928571
                                                                                                                   5.
12
                                                 5
                                                              12
                                                                              6
                                                                                               7
      86.27451
                         39.21569
                                                                                                      5.975000
                                                                                                                   5.
13
      95.91837
                         38.77551
                                                 5
                                                              13
                                                                              6
                                                                                               8
                                                                                                      6.083333
                                                                                                                   6.
                                                 5
                                                                                               7
14
      91.66667
                         43.75000
                                                              12
                                                                              6
                                                                                                      5.928571
                                                                                                                   5.
15
      87.50000
                         35.41667
                                                 5
                                                                                               6
                                                                                                      6.050000
                                                              11
                                                                                                                   6.
   MeanGermTime VarGermTime SEGermTime CVGermTime MeanGermRate VarGermRate SEGermRate
                                                                                                          CVG GermRa
1
        6.700000
                     1.446154
                                0.1901416
                                             0.1794868
                                                            0.1492537 0.0007176543 0.004235724 14.92537
```

0.2076717

0.2335882

0.2146419

0.1458333 0.0009172090 0.004673148 14.58333

0.1456311 0.0011572039 0.005071059 14.56311

0.1451104 0.0009701218 0.004592342 14.51104

2.027875 0.2197333

2.187923 0.2180907

2.572727

0.2391061

```
5
                                          0.2259002
                                                        0.1467890 0.0010995627 0.004786184 14.67890
       6.812500
                    2.368351
                              0.2221275
6
       6.869565
                    2.071498
                              0.2122088
                                          0.2095140
                                                        0.1455696 0.0009301809 0.004496813 14.55696
7
       6.690476
                                                        0.1494662 0.0006935558 0.004063648 14.94662
                    1.389663
                              0.1818989
                                          0.1761967
8
                    2.112179
                              0.2297923
                                                        0.1454545 0.0009454531 0.004861721 14.54545
       6.875000
                                          0.2113940
9
       6.866667
                    2.300000
                              0.2260777
                                          0.2208604
                                                        0.1456311 0.0010345321 0.004794747 14.56311
10
                    1.831313
                              0.2017321
                                          0.1983606
                                                        0.1465798 0.0008453940 0.004334343 14.65798
       6.822222
11
                    2.381206
                              0.2227295
                                          0.2272072
                                                        0.1472393 0.0011191581 0.004828643 14.72393
       6.791667
12
                              0.2210295
                                          0.2129053
                                                        0.1452145 0.0009558577 0.004660905 14.52145
       6.886364
                    2.149577
13
       6.936170
                    2.539315
                              0.2324392
                                          0.2297410
                                                        0.1441718 0.0010970785 0.004831366 14.41718
14
                    1.900634
                                          0.2035568
                                                        0.1476510 0.0009033254 0.004531018 14.76510
       6.772727
                              0.2078370
15
       6.809524
                    1.670151
                              0.1994129
                                          0.1897847
                                                        0.1468531 0.0007767634 0.004300508 14.68531
   GermRateRecip_Farooq GermSpeed_Count GermSpeed_Percent GermSpeedAccumulated_Count GermSpeedAccumulat
              0.1683168
                                 6.138925
                                                    12.27785
                                                                                34.61567
1
2
                                                                                35.54058
              0.1625000
                                6.362698
                                                    12.47588
3
              0.1674419
                                6.882179
                                                    14.33787
                                                                                38.29725
4
              0.1666667
                                6.927417
                                                    13.58317
                                                                                38.68453
5
              0.1680672
                                7.318987
                                                    14.63797
                                                                                41.00786
6
              0.1680000
                                 6.931782
                                                    14.14649
                                                                                38.77620
7
                                                    13.43427
                                                                                36.38546
              0.1682243
                                6.448449
8
              0.1621622
                                6.053175
                                                    12.87909
                                                                                33.77079
9
              0.1674009
                                6.830592
                                                    13.13575
                                                                                38.11511
10
              0.1656051
                                6.812698
                                                    13.62540
                                                                                38.19527
                                7.342796
                                                    14.39764
                                                                                41.17452
11
              0.1693548
12
              0.1680672
                                6.622258
                                                    12.98482
                                                                                37.00640
13
              0.1655172
                                7.052320
                                                    14.39249
                                                                                39.29399
14
              0.1693548
                                 6.706782
                                                    13.97246
                                                                                37.69490
15
              0.1666667
                                 6.363925
                                                    13.25818
                                                                                35.69697
   GermSpeedCorrected_Normal GermSpeedCorrected_Accumulated WeightGermPercent MeanGermPercent MeanGermN
                                                                                                          2.8
                    0.1534731
                                                    0.8653917
                                                                         47.42857
                                                                                          5.714286
1
2
                                                                         47.89916
                                                                                                          3.0
                    0.1514928
                                                    0.8462043
                                                                                          5.882353
3
                    0.1529373
                                                    0.8510501
                                                                         54.46429
                                                                                          6.696429
                                                                                                          3.2
                                                    0.8409680
4
                    0.1505960
                                                                         52.24090
                                                                                          6.442577
                                                                                                          3.2
5
                                                                                                          3.4
                    0.1524789
                                                    0.8543303
                                                                         56.14286
                                                                                          6.857143
6
                                                                                          6.705539
                                                                                                          3.2
                    0.1506909
                                                    0.8429608
                                                                         54.51895
7
                    0.1535345
                                                     0.8663205
                                                                         51.93452
                                                                                          6.250000
                                                                                                          3.0
8
                    0.1513294
                                                                                          6.079027
                                                                                                          2.8
                                                    0.8442698
                                                                         49.39210
9
                    0.1517909
                                                    0.8470024
                                                                         50.27473
                                                                                          6.181319
                                                                                                          3.2
10
                    0.1513933
                                                    0.8487837
                                                                         52.57143
                                                                                          6.428571
                                                                                                          3.2
11
                    0.1529749
                                                    0.8578026
                                                                         55.18207
                                                                                          6.722689
                                                                                                          3.4
12
                                                                         50.00000
                                                                                                          3.1
                    0.1505059
                                                    0.8410547
                                                                                          6.162465
13
                    0.1500494
                                                                         55.24781
                                                                                          6.851312
                                                                                                          3.3
                                                    0.8360424
14
                    0.1524269
                                                    0.8567022
                                                                         53.86905
                                                                                          6.547619
                                                                                                          3.1
15
                                                                                                          3.0
                    0.1515220
                                                    0.8499278
                                                                         51.19048
                                                                                          6.250000
   TimsonsIndex TimsonsIndex_Labouriau TimsonsIndex_KhanUngar GermRateGeorge GermIndex GermIndex_mod
       8.000000
                                    1.00
                                                       0.5714286
                                                                                  5.840000
1
                                                                                                 7.300000
2
                                    1.25
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       9.803922
                                                       0.7002801
                                                                                  5.882353
                                                                                                 7.142857
3
                                    1.40
                                                                               7
      14.583333
                                                       1.0416667
                                                                                  6.687500
                                                                                                 7.133333
4
                                    1.00
                                                                               4
       7.843137
                                                       0.5602241
                                                                                  6.411765
                                                                                                 7.108696
5
      10.000000
                                    1.00
                                                       0.7142857
                                                                               5
                                                                                  6.900000
                                                                                                 7.187500
6
                                                                               3
       6.122449
                                    1.00
                                                       0.4373178
                                                                                  6.693878
                                                                                                 7.130435
7
                                    1.00
                                                                               4
                                                                                  6.395833
                                                                                                 7.309524
       8.333333
                                                       0.5952381
8
                                                                               5
                                                                                  6.063830
      10.638298
                                    1.25
                                                       0.7598784
                                                                                                 7.125000
9
       9.615385
                                    1.25
                                                       0.6868132
                                                                               5
                                                                                  6.173077
                                                                                                 7.133333
10
       8.000000
                                    1.00
                                                       0.5714286
                                                                                  6.460000
                                                                                                 7.177778
```

```
1.00
11
       9.803922
                                                      0.7002801
                                                                              5 6.784314
                                                                                                7.208333
12
       5.882353
                                   1.00
                                                      0.4201681
                                                                              3 6.137255
                                                                                                7.113636
                                   1.00
13
       8.163265
                                                      0.5830904
                                                                              4 6.775510
                                                                                                7.063830
                                   1.00
14
       6.250000
                                                      0.4464286
                                                                              3 6.625000
                                                                                                7.227273
15
       8.333333
                                   1.00
                                                      0.5952381
                                                                              4 6.291667
                                                                                                7.190476
   EmergenceRateIndex SG EmergenceRateIndex SG mod EmergenceRateIndex BilbroWanjura EmergenceRateIndex
                      292
                                            7.300000
                                                                              5.970149
1
2
                      300
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3
                      321
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                                                                              6.553398
4
                      327
                                           7.108696
                                                                              6.675079
5
                      345
                                           7.187500
                                                                              7.045872
6
                      328
                                           7.130435
                                                                              6.696203
7
                      307
                                           7.309524
                                                                              6.277580
8
                      285
                                           7.125000
                                                                              5.818182
9
                      321
                                                                              6.553398
                                           7.133333
10
                      323
                                           7.177778
                                                                              6.596091
11
                      346
                                           7.208333
                                                                              7.067485
12
                      313
                                           7.113636
                                                                              6.389439
13
                      332
                                           7.063830
                                                                              6.776074
14
                      318
                                           7.227273
                                                                              6.496644
15
                      302
                                           7.190476
                                                                              6.167832
   PeakValue GermValue_Czabator GermValue_DP GermValue_Czabator_mod GermValue_DP_mod
                                                                                            CUGerm GermSync
    9.500000
                        54.28571
                                     57.93890
                                                             54.28571
                                                                                                       0.26
                                                                               39.56076 0.7092199
1
2
    9.313725
                        54.78662
                                     52.58713
                                                             54.78662
                                                                               40.99260 0.5051546
                                                                                                       0.23
                                                                                                       0.22
                                                                               53.42809 0.3975265
3 10.416667
                        69.75446
                                     68.62289
                                                             69.75446
4
  10.049020
                        64.74158
                                     70.43331
                                                             64.74158
                                                                               48.86825 0.4672113
                                                                                                       0.25
5
  11.250000
                        77.14286
                                     80.16914
                                                             77.14286
                                                                               56.23935 0.4312184
                                                                                                       0.26
  10.714286
                                                                               53.06435 0.4934701
                                                                                                       0.27
6
                        71.84506
                                     76.51983
                                                             71.84506
                                                                                                       0.27
7
  10.416667
                        65.10417
                                     69.41325
                                                             65.10417
                                                                               47.37690 0.7371500
                                                                                                       0.22
8
    9.574468
                        58.20345
                                     56.00669
                                                             58.20345
                                                                               43.67948 0.4855842
9
    9.855769
                        60.92165
                                     58.13477
                                                             60.92165
                                                                               45.30801 0.4446640
                                                                                                       0.24
10 10.250000
                        65.89286
                                     70.91875
                                                             65.89286
                                                                               49.10820 0.5584666
                                                                                                       0.25
                                                                                                       0.26
11 11.029412
                        74.14731
                                     77.39782
                                                             74.14731
                                                                               54.27520 0.4288905
12 9.803922
                                     64.44988
                                                                               44.71582 0.4760266
                                                                                                       0.27
                        60.41632
                                                             60.41632
                                                                                                       0.25
13 10.969388
                        75.15470
                                     78.16335
                                                             75.15470
                                                                               54.94192 0.4023679
14 10.677083
                        69.90947
                                     74.40140
                                                             69.90947
                                                                               51.41913 0.5383760
                                                                                                       0.29
15 10.156250
                        63.47656
                                     67.62031
                                                             63.47656
                                                                               46.48043 0.6133519
                                                                                                       0.24
   GermUncertainty
1
          2.062987
2
          2.321514
3
          2.462012
4
          2.279215
5
          2.146051
6
          2.160545
7
          2.040796
8
          2.357249
9
          2.321080
10
          2.187983
11
          2.128670
12
          2.185245
13
          2.241181
```

14

15

2.037680

2.185028

data(gcdata)

FourPHFfit.bulk() This wrapper function can be used to fit the four-parameter hill function for multiple samples in batch.

```
counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",</pre>
                            "Day06", "Day07", "Day08", "Day09", "Day10",
                            "Day11", "Day12", "Day13", "Day14")
FourPHFfit.bulk(gcdata, total.seeds.col = "Total Seeds",
                     counts.intervals.cols = counts.per.intervals,
                     intervals = 1:14, partial = TRUE,
                     fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
                     tmax = 20, tries = 3, umax = 90, umin = 10)
   Genotype Rep Day01 Day02 Day03 Day04 Day05 Day06 Day07 Day08 Day09 Day10 Day11 Day12 Day13 Day14 Tot
                     0
                            0
                                                                   7
                                                                                                         0
1
         G1
               1
                                  0
                                         0
                                               4
                                                     17
                                                           10
                                                                         1
                                                                               0
                                                                                      1
2
         G2
               1
                     0
                            0
                                  0
                                               3
                                                     15
                                                           13
                                                                   6
                                                                         2
                                                                                      0
                                                                                            1
                                                                                                   0
                                                                                                         0
                                         1
                                                                                1
                                                            9
                                                                         2
                                                                                                   0
                                                                                                         0
3
         G3
                     0
                            0
                                  0
                                         2
                                               3
                                                     18
                                                                   8
               1
                                                                               1
                                                                                      1
                                                                                            1
4
         G4
                            0
                                  0
                                                     19
                                                                   6
                                                                         2
                                                                                                   0
               1
                     0
                                         0
                                               4
                                                           12
                                                                               1
                                                                                      1
                                                                                            1
5
         G5
                     0
                            0
                                  0
                                         0
                                               5
                                                    20
                                                           12
                                                                   8
                                                                               0
                                                                                      0
                                                                                                   1
                                                                                                         0
               1
                                                                         1
                                                                                            1
               2
                                                                                                   0
6
         G1
                     0
                            0
                                  0
                                         0
                                               3
                                                    21
                                                           11
                                                                   7
                                                                         1
                                                                               1
                                                                                      1
                                                                                            1
                                                                                                         0
7
         G2
               2
                     0
                            0
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                                         0
                                               4
                                                    18
                                                                   7
                                                                                            0
                                                                                                   0
                                                                                                         0
                                                           11
                                                                         1
                                                                               0
                                                                                      1
8
         G3
               2
                     0
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                                  0
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                                                    14
                                                           12
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                                                                         2
                                                                                      0
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9
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         G4
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                                                           10
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         G5
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                                                     18
                                                           13
                                                                   6
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         G1
               3
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                                               5
11
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                                         0
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         G2
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                                                                                1
               3
13
         G3
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                                                     19
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14
         G4
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                     0
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                                  0
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                                                                   6
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                                                           11
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         G5
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                       y0 lag
                                 Dlag50 t50.total t50.Germinated
                                                                        TMGR
                                                                                   AUC
           b
                                                                                            MGT Skewness
                     С
    9.881947 6.034954
                             0 6.034954
                                         6.355122
                                                          6.034954 5.912195 1108.975 6.632252 1.098973
1
                        0
2
    9.227667 6.175193
                        0
                             0 6.175193
                                         6.473490
                                                          6.175193 6.031282 1128.559 6.784407 1.098655
3
    7.793055 6.138110
                             0 6.138110
                                         6.244190
                                                          6.138110 5.938179 1283.693 6.772742 1.103392
4
    8.925668 6.125172
                             0 6.125172
                                         6.276793
                                                          6.125172 5.972686 1239.887 6.739665 1.100323
                        0
5
    9.419194 6.049641
                        0
                             0 6.049641
                                         6.103433
                                                          6.049641 5.914289 1328.328 6.654980 1.100062
                                                          6.097412 5.961877 1294.463 6.702470 1.099232
6
    9.450187 6.097412
                       0
                             0 6.097412
                                         6.182276
                                                          6.029851 5.914057 1213.908 6.622417 1.098272
7
   10.172466 6.029851
                             0 6.029851
                                         6.202812
    8.940702 6.189774
                             0 6.189774
                                         6.439510
                                                          6.189774 6.036193 1164.346 6.804000 1.099232
8
                        0
9
    8.617395 6.125121
                        0
                             0 6.125121
                                         6.352172
                                                          6.125121 5.961631 1188.793 6.745241 1.101242
    9.608849 6.109503
                             0 6.109503
                                         6.253042
                                                          6.109503 5.978115 1240.227 6.711899 1.098600
    9.400248 6.018759
                        0
                             0 6.018759
                                         6.099434
                                                          6.018759 5.883558 1305.200 6.624247 1.100600
11
                                                          6.108449 5.964079 1188.021 6.718636 1.099892
12
    9.162558 6.108449
                        0
                             0 6.108449
                                          6.326181
    8.995233 6.149011
                        0
                             0 6.149011
                                                          6.149011 5.998270 1316.407 6.762272 1.099733
13
                                          6.207500
                                                          6.015907 5.905179 1273.386 6.604963 1.097916
14 10.391898 6.015907
                             0 6.015907
                                          6.122385
    9.136762 6.121580
                             0 6.121580
                                                          6.121580 5.976088 1203.664 6.732267 1.099760
                        0
                                         6.317392
                                                                msg isConv txp.total_10 txp.total_60 Unifor
                                                                       TRUE
                                                                                 4.956266
                                                                                               6.744598
   #1. Relative error in the sum of squares is at most `ftol'.
1
   #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                 4.983236
                                                                                               6.872603
   #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                 4.673022
                                                                                               6.608437
   #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                4.850876
                                                                                              6.614967
   #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                4.814126
                                                                                               6.386788
   #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                 4.868635
                                                                                               6.477594
  #1. Relative error in the sum of squares is at most `ftol'.
                                                                       TRUE
                                                                                 4.930423
                                                                                               6.510495
```

3.157466

2.818494

2.839354

2.562960

2.972718

2.957830

4.816395 3.033943

9

10

11

12

13

14

15

4.746574

4.860681

4.764249

4.806015

4.869401

4.813086

7

7

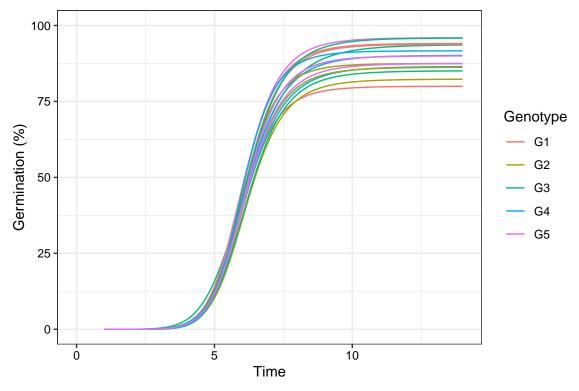
7

7

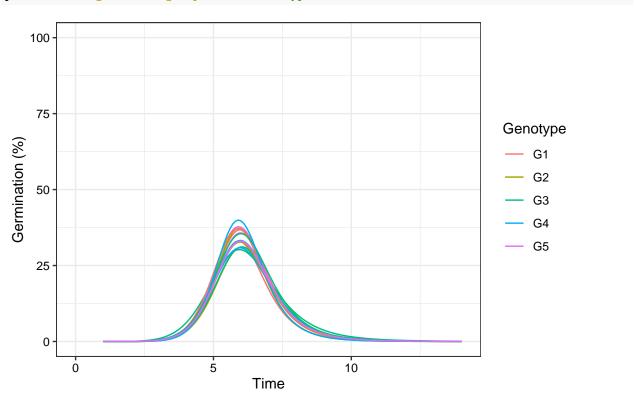
7

```
8 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                           4.940058
                                                                                        6.823299
9 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                          4.836659
                                                                                       6.733275
10 #1. Relative error in the sum of squares is at most `ftol'.
                                                                          4.920629
                                                                                       6.566505
                                                                 TRUE
11 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                          4.798630
                                                                                       6.391288
12 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                          4.893597
                                                                                       6.684521
13 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                                       6.509952
                                                                          4.841310
14 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                          4.915143
                                                                                       6.397486
15 #1. Relative error in the sum of squares is at most `ftol'.
                                                                 TRUE
                                                                          4.892505
                                                                                       6.667247
   Uniformity_10 Uniformity
        4.831809
                  2.705880
1
2
        4.866755
                  2.968652
3
                  3.507277
       4.630062
4
       4.788598
                  3.046208
5
       4.790947
                  2.848078
6
       4.832474
                  2.860984
7
       4.858477
                  2.625165
8
                  3.073056
       4.841106
```

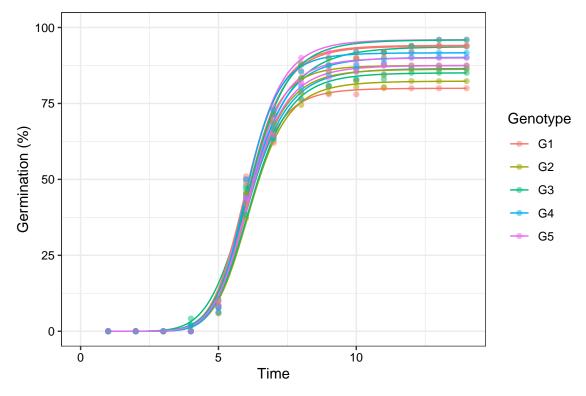
Multiple fitted curves generated in batch can also be plotted.



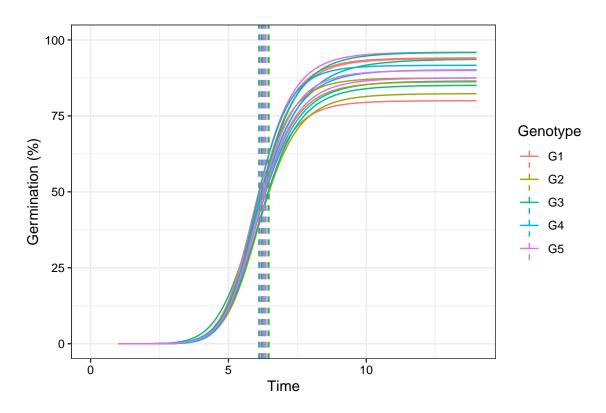


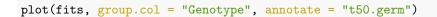


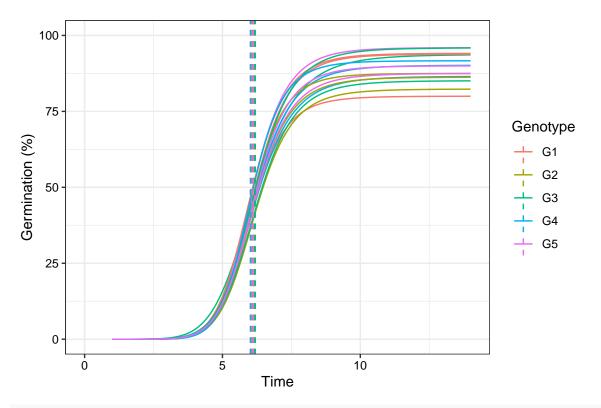
```
# Plot FPHF curves with points
plot(fits, group.col = "Genotype", show.points = TRUE)
```



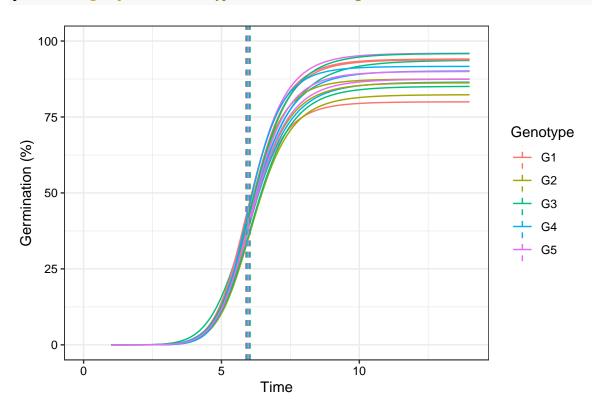
# Plot FPHF curves with annotations
plot(fits, group.col = "Genotype", annotate = "t50.total")



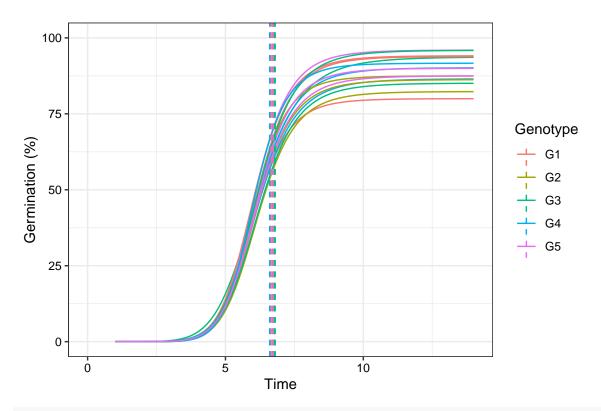




## plot(fits, group.col = "Genotype", annotate = "tmgr")

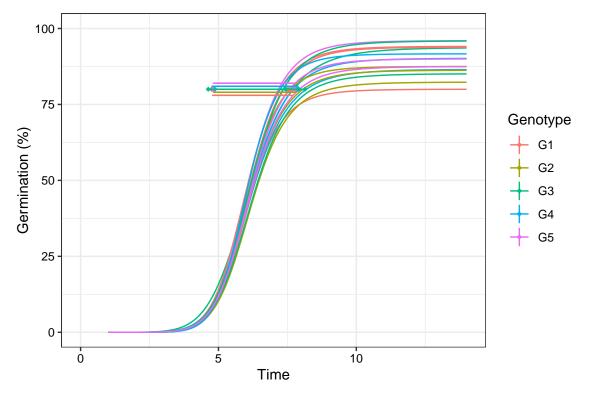


plot(fits, group.col = "Genotype", annotate = "mgt")

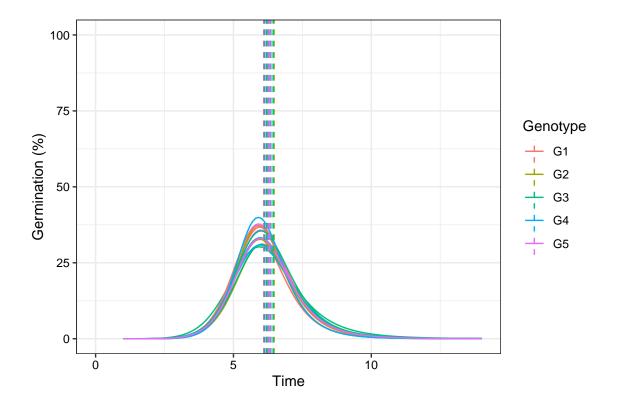


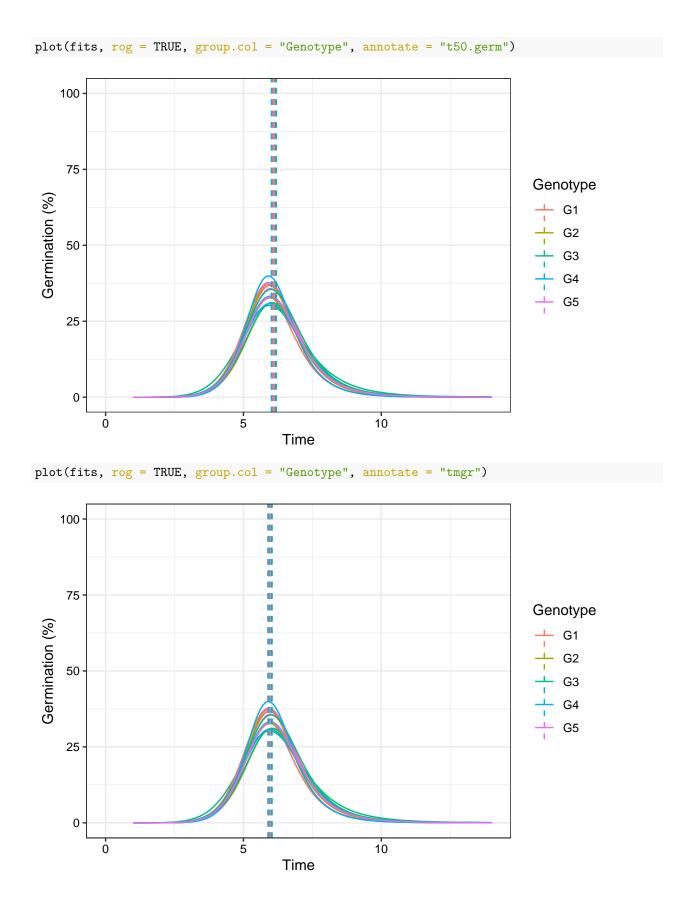
plot(fits, group.col = "Genotype", annotate = "uniformity")

Warning: position\_dodge requires non-overlapping x intervals position\_dodge requires non-overlapping x intervals





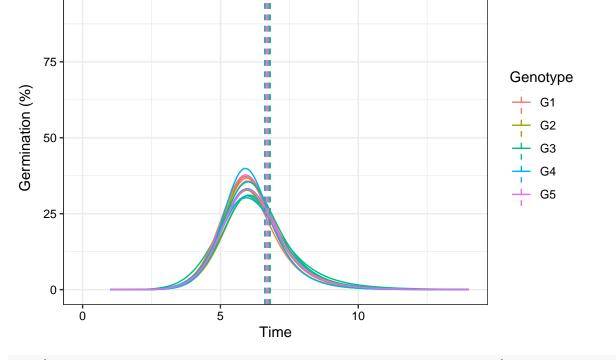




100 -

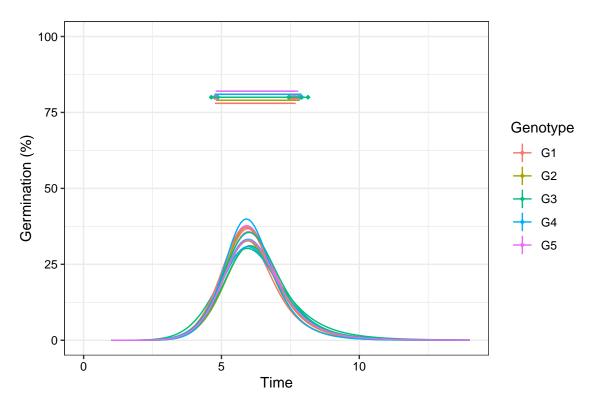
```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "mgt")
```

10



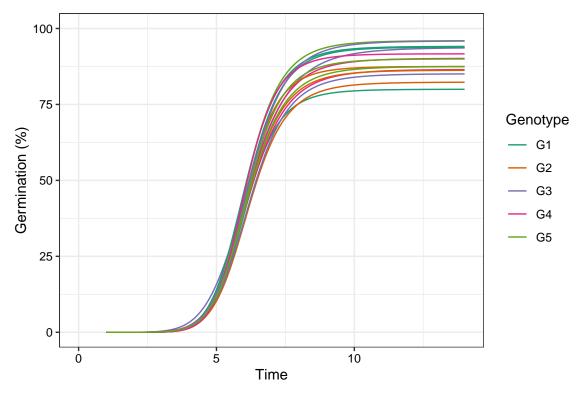
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "uniformity")

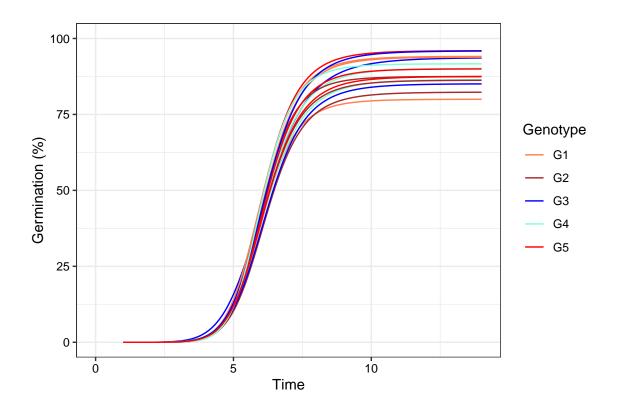
Warning: position\_dodge requires non-overlapping x intervals position\_dodge requires non-overlapping x intervals



```
# Change colour of curves using ggplot2 options
library(ggplot2)
curvesplot <- plot(fits, group.col = "Genotype")

# 'Dark2' palette from RColorBrewer
curvesplot + scale_colour_brewer(palette = "Dark2")</pre>
```





To cite the R package 'germinationmetrics' in publications use:

#### Citing germinationmetrics

```
Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and Kalyani Srinivasan (2022). germinationmetrics: Seed Germination Indices and Curve Fitting. R package version 0.1.6.9000, https://github.com/aravind-j/germinationmetricshttps://cran.r-project.org/package=germinationmetrics.

A BibTeX entry for LaTeX users is
```

```
@Manual{,
   title = {germinationmetrics: Seed Germination Indices and Curve Fitting},
   author = {J. Aravind and S. {Vimala Devi} and J. Radhamani and Sherry Rachel Jacob and {Kalyani Sringer = {2022},
   note = {R package version 0.1.6.9000},
   note = {https://github.com/aravind-j/germinationmetrics},
   note = {https://cran.r-project.org/package=germinationmetrics},
}
```

This free and open-source software implements academic research by the authors and co-workers. If you u it, please support the project by citing the package.

#### Session Info

```
sessionInfo()
R Under development (unstable) (2022-06-05 r82452 ucrt)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19044)
Matrix products: default
locale:
[1] LC_COLLATE=English_India.utf8 LC_CTYPE=English_India.utf8
                                                                  LC_MONETARY=English_India.utf8
[4] LC_NUMERIC=C
                                   LC_TIME=English_India.utf8
attached base packages:
[1] stats
             graphics grDevices utils
                                            datasets methods
                                                                base
other attached packages:
[1] germinationmetrics_0.1.6.9000 ggplot2_3.3.6
loaded via a namespace (and not attached):
 [1] tidyselect_1.1.2
                        farver_2.1.0
                                           dplyr_1.0.9
                                                               bitops_1.0-7
                                                                                  RCurl_1.98-1.6
                        xopen_1.0.0
                                           mathjaxr_1.6-0
                                                               XML_3.99-0.9
                                                                                  rex_1.2.1
```

fas [7] lazyeval\_0.2.2 dig [13] lifecycle\_1.0.1  ${\tt ellipsis\_0.3.2}$ processx\_3.5.3 magrittr\_2.0.3 compiler\_4.3.0 rla [19] tools\_4.3.0 utf8\_1.2.2 yaml\_2.3.5 data.table\_1.14.2 knitr\_1.39 lab [25] prettyunits\_1.1.1 pkgbuild\_1.3.1 curl\_4.3.2 xmlparsedata\_1.0.5 RColorBrewer\_1.1-3 ply [31] xml2\_1.3.3 pkgload\_1.2.4 covr\_3.5.1 withr\_2.5.0 purrr\_0.3.4 des [37] hunspell\_3.0.1 grid\_4.3.0 goodpractice\_1.0.2 fansi\_1.0.3 colorspace\_2.0-3 who [43] scales\_1.2.0 cli\_3.3.0 rmarkdown\_2.14 crayon\_1.5.1 generics\_0.1.2 rem [49] rstudioapi\_0.13 reshape2\_1.4.4 httr\_1.4.3 sessioninfo\_1.2.2 DBI\_1.1.2 cac [55] pander\_0.6.5 stringr\_1.4.0 assertthat\_0.2.1 vctrs\_0.4.1 devtools\_2.4.3 jso [61] minpack.lm\_1.2-2 callr\_3.7.0 rcmdcheck\_1.4.0 ggrepel\_0.9.1 testthat\_3.1.4 сус

[67] tidyr_1.2.0	glue_1.6.2	pkgdown_2.0.3	ps_1.7.0	stringi_1.7.6	gtal
[73] munsell_0.5.0	tibble_3.1.7	pillar_1.7.0	clisymbols_1.2.0	htmltools_0.5.2	bri
[79] praise_1.0.0	R6_2.5.1	lintr_2.0.1	Rdpack_2.3	rprojroot_2.0.3	eval
[85] highr_0.9	backports_1.4.1	rbibutils_2.2.8	memoise_2.0.1	broom_0.8.0	Rcp
[91] xfun_0.31	fs_1.5.2	usethis_2.1.6	pkgconfig_2.0.3		

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