# The germinationmetrics Package: A Brief Introduction

Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and Kalyani Srinivasan

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ICAR-National Bureau of Plant Genetic Resources, New Delhi.

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#### Overview

The package germinationmetrics is a collection of functions which implements various methods for describing the time-course of germination in terms of single-value germination indices as well as fitted curves.

The goal of this vignette is to introduce the users to these functions and get started in describing sequentially recorded germination count data. This document assumes a basic knowledge of R programming language.



## Installation

The package can be installed using the following functions:

```
# Install from CRAN
install.packages('germinationmetrics', dependencies=TRUE)

# Install development version from Github
devtools::install_github("aravind-j/germinationmetrics")
```

Then the package can be loaded using the function

library(germinationmetrics)

## Version History

The current version of the package is 0.1.7. The previous versions are as follows.

Table 1. Version history of germinationmetrics R package.

Version	Date
0.1.0	2018-04-17
0.1.1	2018-07-26
0.1.1.1	2018-10-16
0.1.2	2018-10-31
0.1.3	2019-01-19
0.1.4	2020-06-16
0.1.5	2021-02-17
0.1.6	2022-06-15

To know detailed history of changes use news(package='germinationmetrics').

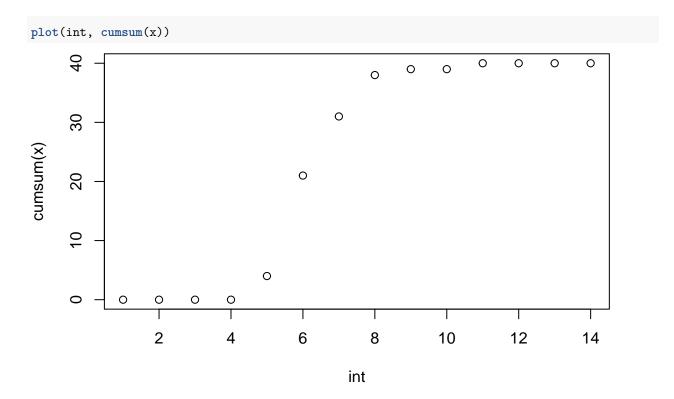
## Germination count data

Typically in a germination test, the germination count data of a fixed number of seeds is recorded at regular intervals for a definite period of time or until all the seeds have germinated. These germination count data can be either partial or cumulative (Table 2).

**Table 2**: A typical germination count data.

intervals	counts	cumulative.counts
1	0	0
2	0	0
3	0	0
4	0	0
5	4	4
6	17	21
7	10	31
8	7	38
9	1	39
10	0	39
11	1	40
12	0	40
13	0	40
14	0	40

The time-course of germination can be plotted as follows.



## Single-value germination indices

The details about the single-value germination indices implemented in **germinationmetrics** are described in Table 3.

 ${\bf Table~3:}~{\bf Single-value~germination~indices~implemented~in~germinationmetrics.}$ 

Germination index	Function	Details	Unit	Measures	Reference
Germination percentage or Final germination percentage or Germinability (GP)	GermPercent	It is computed as follows. $GP=\frac{N_g}{N_t}\times 100$ Where, $N_g$ is the number of germinated seeds and $N_t$ is the total number of seeds.	Percentage (%)	Germination capacity	ISTA (2015)
Peak germination percentage $(PGP)$	PeakGermPercent	It is computed as follows. $PGP = \frac{N_{max}}{N_t} \times 100$ Where, $N_{max}$ is the maximum number of seeds germinated per interval.	Percentage (%)	Germination capacity	Vallance (1950); Roh et al. (2004)
Time for the first germination or Germination time lag $(t_0)$	FirstGermTime	It is the time for first germination to occur (e.g. First day of germination). $t_0 = \min \left\{ T_i : N_i \neq 0 \right\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval and $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval)	time	Germination time	Edwards (1932); Czabator (1962); Goloff and Bazzaz (1975); Labouriau (1983a); Ranal (1999); Quintanilla et al. (2000)
Time for the last germination $(t_g)$	LastGermTime	It is the time for last germination to occur (e.g. Last day of germination) $t_g = \max \{T_i : N_i \neq 0\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval and $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval)	time	Germination time	Edwards (1932)
Time spread of germination or Germination distribution	TimeSpreadGerm	It is the difference between time for last germination $(t_g)$ and time for first germination $(t_0)$ .  Time spread of germination = $t_g - t_0$	time	Germination time	Al-Mudaris (1998); Schrader and Graves (2000); Kader (2005)
Peak period of germination or Modal time of germination $(t_{peak})$	PeakGermTime	It is the time in which highest frequency of germinated seeds are observed and need not be unique. $t_{peak} = \{T_i: N_i = N_{max}\}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval) and $N_{max}$ is the maximum number of seeds germinated per interval.	time	Germination time	Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Median germination time $(t_{50})$ (Coolbear)	t50	It is the time to reach 50% of final/maximum germination. With argument method specified as "coolbear", it is computed as follows.	time	Germination time	Coolbear et al. (1984)
		$t_{50} = T_i + \frac{(\frac{N+1}{2} - N_i)(T_j - T_i)}{N_j - N_i}$ Where, $t_{50}$ is the median germination time, $N$ is the final number of germinated seeds, and $N_i$ and $N_j$ are the total number of seeds germinated in adjacent counts at time $T_i$ and $T_j$ respectively, when $N_i < \frac{N+1}{2} < N_j$ .			
Median germination time $(t_{50})$ (Farooq)	t50	With argument method specified as "farooq", it is computed as follows. $t_{50} = T_i + \frac{(\frac{N}{2} - N_i)(T_j - T_i)}{N_j - N_i}$ Where, $t_{50}$ is the median germination time, $N$ is the final number of germinated seeds, and $N_i$ and $N_j$ are the total number of seeds germinated in adjacent counts at time $T_i$ and	time	Germination time	Farooq et al. (2005)
Mean germination time or Mean length of incubation time $(\overline{T})$ or Germination resistance $(GR)$ or Sprouting index $(SI)$ or Emergence index $(EI)$	MeanGermTime	$T_j$ respectively, when $N_i < \frac{N}{2} < N_j$ . It is the average length of time required for maximum germination of a seed lot and is estimated according to the following formula. $\overline{T} = \frac{\sum_{i=1}^k N_i T_i}{\sum_{i=1}^k N_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals. It is the inverse of mean germination rate $(\overline{V})$ . $\overline{T} = \frac{1}{\overline{V}}$	time	Germination time	Edmond and Drapala (1958); Czabator (1962); Smith and Millet (1964); Gordon (1969); Gordon (1971); Mock and Eberhart (1972); Ellis and Roberts (1980) Labouriau (1983a); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Variance of germination time $(s_T^2)$	VarGermTime	It is computed according to the following formula. $s_T^2 = \frac{\sum_{i=1}^k N_i (T_i - \overline{T})^2}{\sum_{i=1}^k N_i - 1}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals.	time <sup>-1</sup>	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Standard error of germination time $(s_{\overline{T}})$	SEGermTime	It signifies the accuracy of the calculation of the mean germination time. It is estimated according to the following formula: $s_{\overline{T}} = \sqrt{\frac{s_T^2}{\sum_{i=1}^k N_i}}$ Where, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval) and $k$ is the total number of time intervals.	time	Germination time	Labouriau (1983a); Ranal and Santana (2006)
Mean germination rate $(\overline{V})$	MeanGermRate	It is computed according to the following formula: $\overline{V} = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals. It is the inverse of mean germination time $(\overline{T})$ .	${ m time^{-1}}$	Germination rate	Labouriau and Valadares (1976); Labouriau (1983b); Ranal and Santana (2006)

 $\overline{V} = \frac{1}{\overline{T}}$ 

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Germination index	Function	Details	Unit	Measures	Reference
Coefficient of velocity of germination $(CVG)$ or Coefficient of rate of germination $(CRG)$ or Kotowski's coefficient of velocity	CVG	It is estimated according to the following formula. $CVG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i} \times 100$ $CVG = \overline{V} \times 100$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals.	$\%  ext{ time}^{-1}$	Germination rate	Kotowski (1926), Nichols and Heydecker (1968); Bewley and Black (1994); Labouriau (1983b); Scott et al. (1984)
Variance of germination rate $(s_V^2)$	VarGermRate	It is calculated according to the following formula. $s_V^2=\overline{V}^4\times s_T^2$ Where, $s_T^2$ is the variance of germination time.	${\rm time^{-2}}$	Germination rate	Labouriau (1983b); Ranal and Santana (2006)
Standard error of germination rate $(s_{\overline{V}})$	SEGermRate	It is estimated according to the following formula. $s_{\overline{V}} = \sqrt{\frac{s_V^2}{\sum_{i=1}^k N_i}}$ Where, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals.	${ m time}^{-1}$	Germination rate	Labouriau (1983b); Ranal and Santana (2006)
Germination rate as the reciprocal of the median time $(v_{50})$	GermRateRecip	It is the reciprocal of the median germination time $(t_{50}).$ $v_{50} = \frac{1}{t_{50}}$	${ m time}^{-1}$	Germination rate	Went (1957); Labouriau (1983b); Ranal and Santana (2006)
Speed of germination or Germination rate Index or index of velocity of germination or Emergence rate index (Allan, Vogel and Peterson; Erbach; Hsu and Nelson) or Germination index (AOSA)	GermSpeed	It is the rate of germination in terms of the total number of seeds that germinate in a time interval. It is estimated as follows. $S = \sum_{i=1}^k \frac{N_i}{T_i}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $k$ is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of germination.	% time <sup>-1</sup> or count time <sup>-1</sup>	Mixed	Throneberry and Smith (1955); Maguire (1962); Allan et al. (1962); Kendrick and Frankland (1969); Bouton et al. (1976); Erbach (1982); AOSA (1983); Khandakar and Bradbeer (1983); Hsu and Nelson (1986); Bradbeer (1988); Wardle et al. (1991)

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Germination index	Function	Details	Unit	Measures	Reference
Timson's index $[\sum 10 \text{ (Ten summation)}, \sum 5 \text{ or } \sum 20] \text{ or Germination energy index } (GEI)$	TimsonsIndex	It is the progressive total of cumulative germination percentage recorded at specific intervals for a set period of time and is estimated in terms of cumulative germination percentage $(G_i)$ as follows. $\Sigma k = \sum_{i=1}^k G_i$ Where, $G_i$ is the cumulative germination percentage in time interval $i$ , and $k$ is the total number of time intervals. It also estimated in terms of partial germination percentage as follows. $\Sigma k = \sum_{i=1}^k g_i(k-j)$ Where, $g_i$ is the germination (not cumulative, but partial germination) in time interval $i$ ( $i$ varying from 0 to $k$ ), $k$ is the total number of time intervals, and $j=i-1$ .	Percentage (%)	Mixed	Grose and Zimmer (1958); Timson (1965); (lyonRapid-MethodDetermining1966?); Chaudhary and Ghildyal (1970); Negm and Smith (1978); Brown and Mayer (1988); Baskin and Baskin (1998); Goodchild and Walker (1971)
Modified Timson's index $(\Sigma k_{mod})$ (Labouriau)	TimsonsIndex	It is estimated as Timson's index $\Sigma k$ divided by the sum of partial germination percentages. $\Sigma k_{mod} = \frac{\Sigma k}{\sum_{i=1}^k g_i}$	no unit	Mixed	Ranal and Santana (2006)
Modified Timson's index $(\Sigma k_{mod})$ (Khan and Unger)	TimsonsIndex	It is estimated as Timson's index $(\Sigma k)$ divided by the total time period of germination $(T_k)$ . $\Sigma k_{mod} = \frac{\Sigma k}{T_k}$	$\% { m \ time^{-1}}$	Mixed	Khan and Ungar (1984)
George's index $(GR)$	GermRateGeorge	It is estimated as follows. $GR = \sum_{i=1}^k N_i K_i$ Where $N_i$ is the number of seeds germinated by $i$ th interval and $K_i$ is the number of intervals(eg. days) until the end of the test, and and $k$ is the total number of time intervals.	count time	Mixed	George (1961); Tucker and Wright (1965); Nichols and Heydecker (1968);Chopra and Chaudhary (1980)

Germination index	Function	Details	Unit	Measures	Reference
Germination Index $(GI)$ (Melville)	GermIndex	It is estimated as follows. $GI = \sum_{i=1}^k \frac{ (T_k - T_i)  N_i }{N_t}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval (day for the example), $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $N_t$ is the total number of seeds used in the test, and $k$ is the total number of time intervals.	time	Mixed	Melville et al. (1980)
Germination Index $(GI_{mod})$ (Melville; Santana and Ranal)	GermIndex	It is estimated as follows. $GI_{mod} = \sum_{i=1}^k \frac{ (T_k - T_i)  N_i }{N_g}$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval (day for the example), $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $N_g$ is the total number of germinated seeds at the end of the test, and $k$ is the total number of time intervals.	time	Mixed	Melville et al. (1980); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index $(ERI)$ or Germination Rate Index (Shmueli and Goldberg)	EmergenceRateIndex	It is estimated as follows. $ERI = \sum_{i=i_0}^{k-1} N_i(k-i)$ Where, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $i_0$ is the time interval when emergence/germination started, and $k$ is the total number of time intervals.	count	Mixed	Shmueli and Goldberg (1971)
Modified Emergence Rate Index $(ERI_{mod})$ or Modified Germination Rate Index (Shmueli and Goldberg; Santana and Ranal)	EmergenceRateIndex	It is estimated by dividing Emergence rate index $(ERI)$ by total number of emerged seedlings (or germinated seeds). $ERI_{mod} = \frac{\sum_{i=i_0}^{k-1} N_i(k-i)}{N_g} = \frac{ERI}{N_g}$ Where, $N_g$ is the total number of germinated seeds at the end of the test, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), $i_0$ is the time interval when emergence/germination started, and $k$ is the total number of time intervals.	no unit	Mixed	Shmueli and Goldberg (1971); Santana and Ranal (2004); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Emergence Rate Index (ERI) or Germination Rate Index (Bilbro & Wanjura)	EmergenceRateIndex	It is the estimated as follows. $ERI = \frac{\sum_{i=1}^k N_i}{\overline{T}} = \frac{N_g}{\overline{T}}$ Where, $N_g$ is the total number of germinated seeds at the end of the test, $N_i$ is the number of seeds germinated in the $i$ th time interval (not the accumulated number, but the number corresponding to the $i$ th interval), and $\overline{T}$ is the mean germination time or mean emergence time.	count time <sup>-1</sup>	Mixed	Bilbro and Wanjura (1982)
Emergence Rate Index $(ERI)$ or Germination Rate Index (Fakorede)	EmergenceRateIndex	It is estimated as follows. $ERI=\frac{\overline{T}}{FGP/100}$ Where, $\overline{T}$ is the Mean germination time and $FGP$ is the final germination time.	time count <sup>-1</sup>	Mixed	Fakorede and Ayoola (1980); Fakorede and Ojo (1981); Fakorede and Agbana (1983)
Peak value $(PV)$ (Czabator) or Emergence Energy $(EE)$	PeakValue	It is the accumulated number of seeds germinated at the point on the germination curve at which the rate of germination starts to decrease. It is computed as the maximum quotient obtained by dividing successive cumulative germination values by the relevant incubation time. $PV = \max\left(\frac{G_1}{T_1}, \frac{G_2}{T_2}, \cdots \frac{G_k}{T_k}\right)$ Where, $T_i$ is the time from the start of the experiment to the $i$ th interval, $G_i$ is the cumulative germination percentage in the $i$ th time interval, and $k$ is the total number of time intervals.	$\% \ \mathrm{time^{-1}}$	Mixed	Czabator (1962); Bonner (1967)
Germination value $(GV)$ (Czabator)	GermValue	It is computed as follows. $GV = PV \times MDG$ Where, $PV$ is the peak value and $MDG$ is the mean daily germination percentage from the onset of germination. It can also be computed for other time intervals of successive germination counts, by replacing $MDG$ with the mean germination percentage per unit time $(\overline{GP})$ . $GV$ value can be modified $(GV_{mod})$ , to consider the entire duration from the beginning of the test instead of just from the	$\%^2$ time <sup>-2</sup>	Mixed	Czabator (1962); Brown and Mayer (1988)

onset of germination.

 $\overline{E} = -\sum_{i=1}^{k} f_i \log_2 f_i$ 

Where,  $f_i$  is the relative frequency of germination  $(f_i = \frac{N_i}{\sum_{i=1}^k N_i})$ ,  $N_i$  is the number of seeds germinated on the

ith time interval, and k is the total number of time intervals.

 $GV = \frac{\sum DGS}{N} \times GP \times c$ 

Where, DGS is the daily germination speed computed by dividing cumulative germination percentage by the number of days since the since the onset of germination, N is the frequency or number of DGS calculated during the test, GP is the

Unit

 $\%^2$  time<sup>-1</sup>

Measures

Mixed

Reference

(1983b)

Djavanshir and Pourbeik (1976);

Brown and Mayer (1988)

Germination index

Germination value

Uncertainty of the

germination process (U) or

informational entropy (H)

(GV) (Diavanshir

and Pourbiek)

Function

GermValue

Details

It is computed as follows.

Germination index	Function	Details	Unit	Measures	Reference
Synchrony of germination $(Z \text{ index})$	GermSynchrony	It is computed as follows. $Z = \frac{\sum_{i=1}^k C_{N_i,2}}{C_{\Sigma N_i,2}}$ Where, $C_{N_i,2}$ is the partial combination of the two germinated seeds from among $N_i$ , the number of seeds germinated on the $i$ th time interval (estimated as $C_{N_i,2} = \frac{N_i(N_i-1)}{2}$ ), and $C_{\Sigma N_i,2}$ is the partial combination of the two germinated seeds from among the total number of seeds germinated at the final count, assuming that all seeds that germinated did so simultaneously.	no unit	Germination synchrony	Primack (1985); Ranal and Santana (2006)

#### Examples

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z \leftarrow c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)</pre>
# From partial germination counts
GermPercent(germ.counts = x, total.seeds = 50)
GermPercent()
[1] 80
PeakGermPercent(germ.counts = x, intervals = int, total.seeds = 50)
[1] 34
# For multiple peak germination times
PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50)
Warning in PeakGermPercent(germ.counts = z, intervals = int, total.seeds = 50): Multiple peak germinati
[1] 22
# From cumulative germination counts
GermPercent(germ.counts = y, total.seeds = 50, partial = FALSE)
[1] 80
PeakGermPercent(germ.counts = y, intervals = int, total.seeds = 50,
                partial = FALSE)
[1] 34
# For multiple peak germination times
PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50,
                partial = FALSE)
Warning in PeakGermPercent(germ.counts = cumsum(z), intervals = int, total.seeds = 50, : Multiple peak
exist.
[1] 22
# From number of germinated seeds
GermPercent(germinated.seeds = 40, total.seeds = 50)
[1] 80
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z \leftarrow c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)</pre>
# From partial germination counts
```

```
FirstGermTime(germ.counts = x, intervals = int)
FirstGermTime(), LastGermTime(), PeakGermTime(), TimeSpreadGerm()
[1] 5
LastGermTime(germ.counts = x, intervals = int)
[1] 11
TimeSpreadGerm(germ.counts = x, intervals = int)
[1] 6
PeakGermTime(germ.counts = x, intervals = int)
[1] 6
# For multiple peak germination times
PeakGermTime(germ.counts = z, intervals = int)
Warning in PeakGermTime(germ.counts = z, intervals = int): Multiple peak germination times exist.
[1] 5 6
# From cumulative germination counts
FirstGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 5
LastGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 11
TimeSpreadGerm(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
PeakGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
# For multiple peak germination time
PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE)
Warning in PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE): Multiple peak germing
exist.
[1] 5 6
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
t50(germ.counts = x, intervals = int, method = "coolbear")
```

t50()

```
[1] 5.970588
t50(germ.counts = x, intervals = int, method = "farooq")
[1] 5.941176
# From cumulative germination counts
t50(germ.counts = y, intervals = int, partial = FALSE, method = "coolbear")
[1] 5.970588
t50(germ.counts = y, intervals = int, partial = FALSE, method = "farooq")
[1] 5.941176
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermTime(germ.counts = x, intervals = int)
MeanGermTime(), VarGermTime(), SEGermTime(), CVGermTime()
[1] 6.7
VarGermTime(germ.counts = x, intervals = int)
[1] 1.446154
SEGermTime(germ.counts = x, intervals = int)
[1] 0.1901416
CVGermTime(germ.counts = x, intervals = int)
[1] 0.1794868
# From cumulative germination counts
MeanGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.7
VarGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 19.04012
SEGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.2394781
CVGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.6512685
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
```

```
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermRate(germ.counts = x, intervals = int)
MeanGermRate(), CVG(), VarGermRate(), SEGermRate(), GermRateRecip()
[1] 0.1492537
CVG(germ.counts = x, intervals = int)
[1] 14.92537
VarGermRate(germ.counts = x, intervals = int)
[1] 0.0007176543
SEGermRate(germ.counts = x, intervals = int)
[1] 0.004235724
GermRateRecip(germ.counts = x, intervals = int, method = "coolbear")
[1] 0.1674877
GermRateRecip(germ.counts = x, intervals = int, method = "farooq")
[1] 0.1683168
# From cumulative germination counts
MeanGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.1492537
CVG(germ.counts = y, intervals = int, partial = FALSE)
[1] 14.92537
VarGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.009448666
SEGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.005334776
GermRateRecip(germ.counts = y, intervals = int,
              method = "coolbear", partial = FALSE)
[1] 0.1674877
GermRateRecip(germ.counts = y, intervals = int,
              method = "farooq", partial = FALSE)
[1] 0.1683168
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
```

```
# From partial germination counts
GermSpeed(germ.counts = x, intervals = int)
GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)
[1] 34.61567
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "accumulated")
[1] 0.8653917
# From partial germination counts (with percentages instead of counts)
GermSpeed(germ.counts = x, intervals = int,
         percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                     percent = TRUE, total.seeds = 50)
[1] 69.23134
# From cumulative germination counts
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.138925
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
[1] 34.61567
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "normal")
[1] 0.1534731
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "accumulated")
[1] 0.8653917
# From cumulative germination counts (with percentages instead of counts)
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
         percent = TRUE, total.seeds = 50)
```

[1] 12.27785

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
        percent = TRUE, total.seeds = 50)
[1] 69.23134
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
#-----
WeightGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
WeightGermPercent()
[1] 47.42857
# From cumulative germination counts
WeightGermPercent(germ.counts = y, total.seeds = 50, intervals = int,
                 partial = FALSE)
[1] 47.42857
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermPercent(germ.counts = x, total.seeds = 50, intervals = int)
MeanGermPercent(), MeanGermNumber()
[1] 5.714286
MeanGermNumber(germ.counts = x, intervals = int)
[1] 2.857143
# From cumulative germination counts
MeanGermPercent(germ.counts = y, total.seeds = 50, intervals = int, partial = FALSE)
[1] 5.714286
MeanGermNumber(germ.counts = y, intervals = int, partial = FALSE)
[1] 2.857143
# From number of germinated seeds
MeanGermPercent(germinated.seeds = 40, total.seeds = 50, intervals = int)
```

[1] 5.714286

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
# Wihout max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50)
TimsonsIndex(), GermRateGeorge()
[1] 664
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             modification = "none")
[1] 664
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
           modification = "labouriau")
[1] 8.3
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             modification = "khanungar")
[1] 47.42857
GermRateGeorge(germ.counts = x, intervals = int)
[1] 332
# With max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50, max = 10)
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "none")
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "labouriau")
[1] 4.410256
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "khanungar")
[1] 24.57143
GermRateGeorge(germ.counts = x, intervals = int, max = 10)
[1] 172
GermRateGeorge(germ.counts = x, intervals = int, max = 14)
```

[1] 332

```
# From cumulative germination counts
# Wihout max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50)
[1] 664
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "none")
[1] 664
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "labouriau")
[1] 8.3
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             modification = "khanungar")
[1] 47.42857
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,)
[1] 332
# With max specified
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50, max = 10)
[1] 344
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "none")
[1] 344
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
             total.seeds = 50,
             max = 10, modification = "labouriau")
[1] 4.410256
TimsonsIndex(germ.counts = y, intervals = int, partial = FALSE,
            total.seeds = 50,
             max = 10, modification = "khanungar")
[1] 24.57143
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 10
[1] 172
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,
               max = 14
```

[1] 332

#### GermIndex()

[1] 5.84

[1] 5.84

[1] 7.3

[1] 5.84

[1] 5.84

[1] 7.3

```
x <- c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y <- c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)

# From partial germination counts
#------
EmergenceRateIndex(germ.counts = x, intervals = int)</pre>
```

#### EmergenceRateIndex()

[1] 292

```
[1] 292
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "sgsantanaranal")
[1] 7.3
EmergenceRateIndex(germ.counts = x, intervals = int,
                   method = "bilbrowanjura")
[1] 5.970149
EmergenceRateIndex(germ.counts = x, intervals = int,
                   total.seeds = 50, method = "fakorede")
[1] 8.375
# From cumulative germination counts
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,)
[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "shmueligoldberg")
[1] 292
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "sgsantanaranal")
[1] 7.3
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   method = "bilbrowanjura")
[1] 5.970149
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,
                   total.seeds = 50, method = "fakorede")
[1] 8.375
x \leftarrow c(0, 0, 34, 40, 21, 10, 4, 5, 3, 5, 8, 7, 7, 6, 6, 4, 0, 2, 0, 2)
y \leftarrow c(0, 0, 34, 74, 95, 105, 109, 114, 117, 122, 130, 137, 144, 150,
      156, 160, 160, 162, 162, 164)
int <- 1:length(x)</pre>
total.seeds = 200
# From partial germination counts
PeakValue(germ.counts = x, intervals = int, total.seeds = 200)
PeakValue(), GermValue()
[1] 9.5
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
```

method = "czabator")

# \$`Germination Value` [1] 38.95

## [[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	7 58.5	6.500000
10	5	10	122	2 61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	1 72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	2 81.0	4.500000
19	0	19	162	2 81.0	4.263158
20	2	20	164	82.0	4.100000
Ge	rmValue(germ	.counts = 2	x, intervals = int, tot	cal.seeds = 200,	

## \$`Germination Value`

method = "dp", k = 10)

[1] 53.36595

## [[2]]

		in+on] a	Cumulative mamm counts	Cumulative mamm nameant	DCC	CDCCbN	GV
	•		•	Cumulative.germ.percent		SumDGSbyN	
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250
7	4	7	109	54.5	7.785714	8.190476	44.638095
8	5	8	114	57.0	7.125000	8.012897	45.673512
9	3	9	117	58.5	6.500000	7.796769	45.611097
10	5	10	122	61.0	6.100000	7.584673	46.266503
11	8	11	130	65.0	5.909091	7.398497	48.090230
12	7	12	137	68.5	5.708333	7.229481	49.521942
13	7	13	144	72.0	5.538462	7.075752	50.945411
14	6	14	150	75.0	5.357143	6.932534	51.994006
15	6	15	156	78.0	5.200000	6.799262	53.034246
16	4	16	160	80.0	5.000000	6.670744	53.365948
17	0	17	160	80.0	4.705882	6.539753	52.318022
18	2	18	162	81.0	4.500000	6.412268	51.939373
19	0	19	162	81.0	4.263158	6.285850	50.915385
20	2	20	164	82.0	4.100000	6.164414	50.548194

## \$testend

[1] 16

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "czabator", from.onset = FALSE)
```

## \$`Germination Value`

[1] 38.95

[[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

## \$`Germination Value`

[1] 46.6952

[[2]]

L L Z	7 T						
	germ.counts	${\tt intervals}$	Cumulative.germ.counts	Cumulative.germ.percent	DGS	${\tt SumDGSbyN}$	GV
1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111
4	40	4	74	37.0	9.250000	3.729167	13.797917
5	21	5	95	47.5	9.500000	4.883333	23.195833
6	10	6	105	52.5	8.750000	5.527778	29.020833
7	4	7	109	54.5	7.785714	5.850340	31.884354
8	5	8	114	57.0	7.125000	6.009673	34.255134
9	3	9	117	58.5	6.500000	6.064153	35.475298
10	5	10	122	61.0	6.100000	6.067738	37.013202
11	8	11	130	65.0	5.909091	6.053316	39.346552
12	7	12	137	68.5	5.708333	6.024567	41.268285
13	7	13	144	72.0	5.538462	5.987174	43.107655
14	6	14	150	75.0	5.357143	5.942172	44.566291
15	6	15	156	78.0	5.200000	5.892694	45.963013
16	4	16	160	80.0	5.000000	5.836901	46.695205
17	0	17	160	80.0	4.705882	5.770370	46.162961

18	2	18	162	81.0 4.500000	5.699794 46.168331
19	0	19	162	81.0 4.263158	5.624182 45.555871
20	2	20	164	82.0 4.100000	5.547972 45.493374

#### \$testend

[1] 16

## [1] 9.5

#### \$`Germination Value`

[1] 38.95

#### [[2]]

	2				
	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

#### \$`Germination Value`

[1] 53.36595

## [[2]]

	-11						
	germ.counts	${\tt intervals}$	Cumulative.germ.counts	Cumulative.germ.percent	DGS	${\tt SumDGSbyN}$	GV
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250
7	4	7	109	54.5	7.785714	8.190476	44.638095
8	5	8	114	57.0	7.125000	8.012897	45.673512
9	3	9	117	58.5	6.500000	7.796769	45.611097

10	5	10	122	61.0 6.100000	7.584673 46.266503
11	8	11	130	65.0 5.909091	7.398497 48.090230
12	7	12	137	68.5 5.708333	7.229481 49.521942
13	7	13	144	72.0 5.538462	7.075752 50.945411
14	6	14	150	75.0 5.357143	6.932534 51.994006
15	6	15	156	78.0 5.200000	6.799262 53.034246
16	4	16	160	80.0 5.000000	6.670744 53.365948
17	0	17	160	80.0 4.705882	6.539753 52.318022
18	2	18	162	81.0 4.500000	6.412268 51.939373
19	0	19	162	81.0 4.263158	6.285850 50.915385
20	2	20	164	82.0 4.100000	6.164414 50.548194

#### \$testend

[1] 16

## \$`Germination Value`

[1] 38.95

## [[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
1	0	1	0		0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

## \$`Germination Value`

[1] 46.6952

#### [[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	${\tt SumDGSbyN}$	GV
1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111

4	40	4	74	37.0 9.250000	3.729167 13.797917
5	21	5	95	47.5 9.500000	4.883333 23.195833
6	10	6	105	52.5 8.750000	5.527778 29.020833
7	4	7	109	54.5 7.785714	5.850340 31.884354
8	5	8	114	57.0 7.125000	6.009673 34.255134
9	3	9	117	58.5 6.500000	6.064153 35.475298
10	5	10	122	61.0 6.100000	6.067738 37.013202
11	8	11	130	65.0 5.909091	6.053316 39.346552
12	7	12	137	68.5 5.708333	6.024567 41.268285
13	7	13	144	72.0 5.538462	5.987174 43.107655
14	6	14	150	75.0 5.357143	5.942172 44.566291
15	6	15	156	78.0 5.200000	5.892694 45.963013
16	4	16	160	80.0 5.000000	5.836901 46.695205
17	0	17	160	80.0 4.705882	5.770370 46.162961
18	2	18	162	81.0 4.500000	5.699794 46.168331
19	0	19	162	81.0 4.263158	5.624182 45.555871
20	2	20	164	82.0 4.100000	5.547972 45.493374

#### \$testend

[1] 16

#### CUGerm()

[1] 0.7092199

```
# From cumulative germination counts
#-----
CUGerm(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 0.05267935

#### GermSynchrony(), GermUncertainty()

[1] 0.2666667

```
GermUncertainty(germ.counts = x, intervals = int)
```

[1] 2.062987

```
# From cumulative germination counts
#------
GermSynchrony(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 0.2666667

GermUncertainty(germ.counts = y, intervals = int, partial = FALSE)

[1] 2.062987

## Non-linear regression analysis

Several mathematical functions have been used to fit the cumulative germination count data and describe the germination process by non-linear regression analysis. They include functions such as Richard's, Weibull, logistic, log-logistic, gaussian, four-parameter hill function etc. Currently germinationmetrics implements the four-parameter hill function to fit the count data and computed various associated metrics.

## Four-parameter hill function

The four-parameter hill function defined as follows (El-Kassaby et al., 2008).

$$f(x) = y = y_0 + \frac{ax^b}{x^b + c^b}$$

Where, y is the cumulative germination percentage at time x,  $y_0$  is the intercept on the y axis, a is the asymptote, b is a mathematical parameter controlling the shape and steepness of the germination curve and c is the "half-maximal activation level".

this function can also be be reparameterized by substituting b with  $e^{\beta}$  to constraint b to positive values only.

$$y = y_0 + \frac{ax^{e^{\beta}}}{c^{e^{\beta}} + x^{e^{\beta}}}$$

Where,  $b = e^{\beta}$  and  $\beta = \log_e(b)$ .

The details of various parameters that are computed from this function are given in Table 4.

Table 4 Germination parameters estimated from the four-parameter hill function.

Germination parameters	Details	Unit	Measures
y intercept $(y_0)$	The intercept on the y axis.		
Asymptote $(a)$	It is the maximum cumulative germination percentage, which is equivalent to germination capacity.	%	Germination capacity
Shape and steepness $(b)$	Mathematical parameter controlling the shape and steepness of the germination curve. The larger the $b$ , the steeper the rise toward the asymptote $a$ , and the shorter the time between germination onset and maximum germination.		Germination rate
Half-maximal activation level $(c)$	Time required for $50\%$ of viable seeds to germinate.	time	Germination time

Germination parameters	Details	Unit	Measures
lag	It is the time at germination onset and is computed by solving four-parameter hill function after setting y to 0 as follows.	time	Germination time
	$lag = b\sqrt{\frac{-y_0c^b}{a+y_0}}$		
$D_{lag-50}$	The duration between the time at germination onset $(lag)$ and that at 50% germination $(c)$ .	time	Germination time
$t_{50_{total}}$	Time required for $50\%$ of total seeds to germinate.	time	Germination time
$t_{50_{germinated}}$	Time required for 50% of viable/germinated seeds to germinate	time	Germination time
$t_{x_{total}}$	Time required for $x\%$ of total seeds to germinate.	time	Germination time
$t_{x_{germinated}}$	Time required for $x\%$ of viable/germinated seeds to germinate	time	Germination time
Uniformity $(U_{t_{max}-t_{min}})$	It is the time interval between the percentages of viable seeds specified in the arguments umin and umin to germinate.	time	Germination time
Time at maximum germination rate $(TMGR)$	The partial derivative of the four-parameter hill function gives the instantaneous rate of germination $(s)$ as follows.	time	Germination time
	$s = \frac{\partial y}{\partial x} = \frac{abc^b x^{b-1}}{(c^b + x^b)^2}$		
	From this function for instantaneous rate of germination, $TMGR$ can be estimated as follows.		
	$TMGR = b\sqrt{\frac{c^b(b-1)}{b+1}}$		
	It represents the point in time when the instantaneous rate of germination starts to decline.		
Area under the curve $(AUC)$	It is obtained by integration of the fitted curve between time 0 and time specified in the argument tmax.		Mixed
MGT	Calculated by integration of the fitted curve and proper normalisation.	time	Germination time
Skewness	It is computed as follows.		
	MGT		
	$\overline{t_{50_{germinated}}}$		
	yerminatea		

## Examples

#### FourPHFfit()

Warning in FourPHFfit(germ.counts = x, intervals = int, total.seeds = 50, : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

#### \$data

φαάσα				
	gp	csgp	intervals	
1	0	0	1	
2	0	0	2	
3	0	0	3	
4	0	0	4	
5	8	8	5	
6	34	42	6	
7	20	62	7	
8	14	76	8	
9	2	78	9	
10	0	78	10	
11	2	80	11	
12	0	80	12	
13	0	80	13	
14	0	80	14	

#### \$Parameters

```
term estimate std.error statistic p.value
      NA
                 NA
  a
2
                           NA
                                 NA
  b
          NA
                  NA
3
   С
          NA
                  NA
                           NA
                                 NA
          NA
                  NA
                           NA
                                 NA
  у0
```

#### \$Fit

```
sigma isConv finTol logLik AIC BIC deviance df.residual nobs 1 NA NA NA NA NA NA NA NA
```

\$a

[1] NA

\$b

[1] NA

\$c

[1] NA

\$y0

[1] NA

```
$lag
[1] NA
$Dlag50
[1] NA
$t50.total
[1] NA
$txp.total
10 60
NA NA
$t50.Germinated
[1] NA
$txp.Germinated
10 60
NA NA
$Uniformity
       90
                   10 uniformity
       NA
                              NA
                   NA
$TMGR
[1] NA
$AUC
[1] NA
$MGT
[1] NA
$Skewness
[1] NA
[1] "#1. failed to evaluate 'fn' at starting values: could not find function \"FourPHF_fixa_fixy0\" "
$isConv
[1] NA
<simpleError in gsl_nls.formula(csgp ~ FourPHF_fixa_fixy0(x = intervals, a = max(csgp), bta, c), da</pre>
attr(,"class")
[1] "FourPHFfit" "list"
# From cumulative germination counts
FourPHFfit(germ.counts = y, intervals = int, total.seeds = 50, tmax = 20,
partial = FALSE)
```

#### \$data

	gp	csgp	${\tt intervals}$
1	0	0	1
2	0	0	2
3	0	0	3
4	0	0	4
5	8	8	5
6	34	42	6
7	20	62	7
8	14	76	8
9	2	78	9
10	0	78	10
11	2	80	11
12	0	80	12
13	0	80	13
14	0	80	14

#### \$Parameters

term estimate std.error statistic p.value NANANANANANANA 2 b 3 С NANANANA у0 NANANANA

#### \$Fit

sigma is<br/>Conv fin Tol log<br/>Lik AIC BIC deviance df.<br/>residual nobs 1 NA NA NA NA NA NA NA NA

\$a

[1] NA

\$b

[1] NA

\$с

[1] NA

\$y0

[1] NA

\$lag

[1] NA

\$Dlag50

[1] NA

\$t50.total

[1] NA

\$txp.total

10 60

NA NA

\$t50.Germinated

```
[1] NA
$txp.Germinated
10 60
NA NA
$Uniformity
       90
                  10 uniformity
       NA
                  NA
                             NA
$TMGR
[1] NA
$AUC
[1] NA
$MGT
[1] NA
$Skewness
[1] NA
$msg
[1] "#1. failed to evaluate 'fn' at starting values: could not find function \"FourPHF_fixa_fixy0\" "
$isConv
[1] NA
$model
<simpleError in gsl_nls.formula(csgp ~ FourPHF_fixa_fixy0(x = intervals, a = max(csgp), bta, c), da</pre>
attr(,"class")
[1] "FourPHFfit" "list"
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
total.seeds = 50
# From partial germination counts
#-----
fit1 <- FourPHFfit(germ.counts = x, intervals = int,</pre>
                 total.seeds = 50, tmax = 20)
Warning in FourPHFfit(germ.counts = x, intervals = int, total.seeds = 50, : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
# From cumulative germination counts
fit2 <- FourPHFfit(germ.counts = y, intervals = int,</pre>
```

Warning in FourPHFfit(germ.counts = y, intervals = int, total.seeds = 50, : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

total.seeds = 50, tmax = 20, partial = FALSE)

# # Default plots plot(fit1)

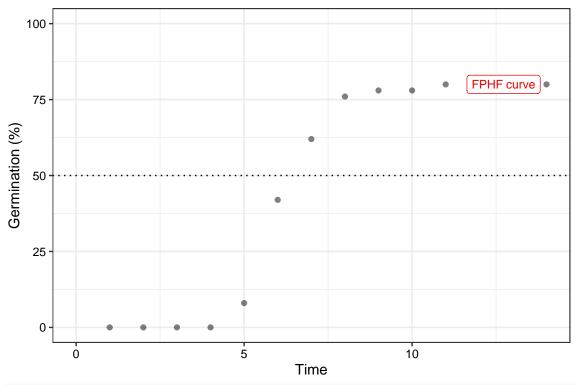
Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

Warning: Removed 14 rows containing missing values (`geom\_segment()`).
Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`). Removed 1 rows containing missing values (`geom\_vline()`).



## plot(fit2)

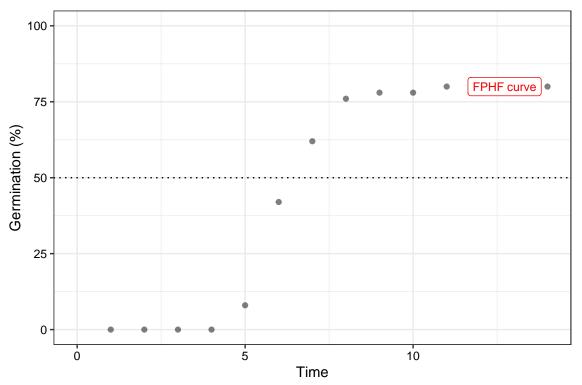
Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

Warning: Removed 14 rows containing missing values (`geom\_segment()`). Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).



```
# No labels
plot(fit1, plotlabels = FALSE)
```

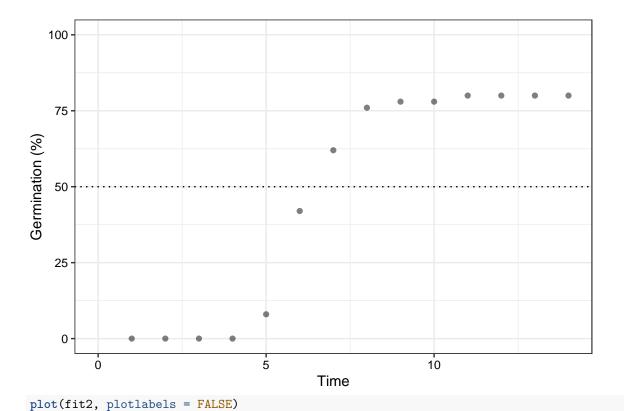
Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

Warning: Removed 14 rows containing missing values (`geom\_segment()`). Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`). Removed 1 rows containing missing values (`geom\_vline()`).

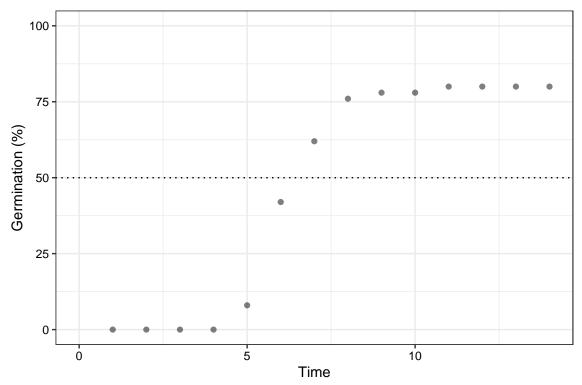


Warning: Removed 101 rows containing missing values (`geom\_function()`).

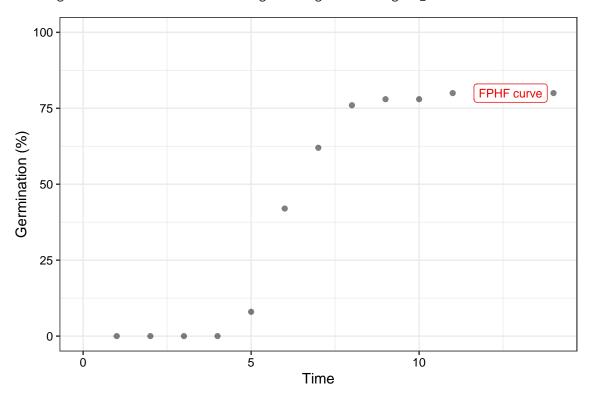
Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

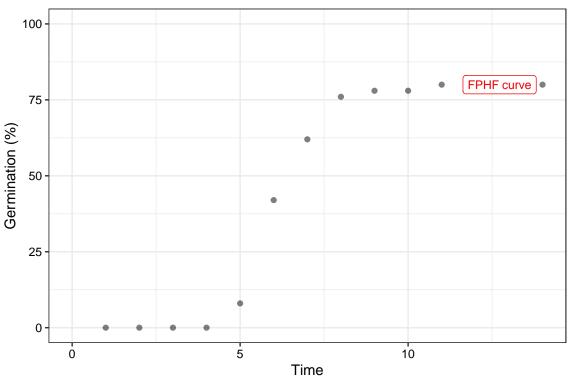
Warning: Removed 14 rows containing missing values (`geom\_segment()`). Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).



```
# Only the FPHF curve
plot(fit1, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
     tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```





```
# Without y axis limits adjustment
plot(fit1, limits = FALSE)
```

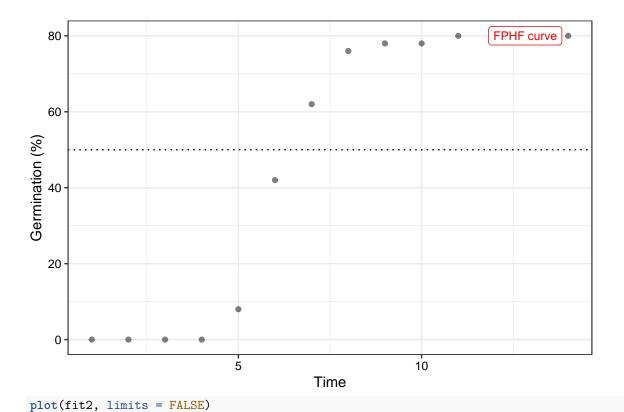
Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

Warning: Removed 14 rows containing missing values (`geom\_segment()`).
Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

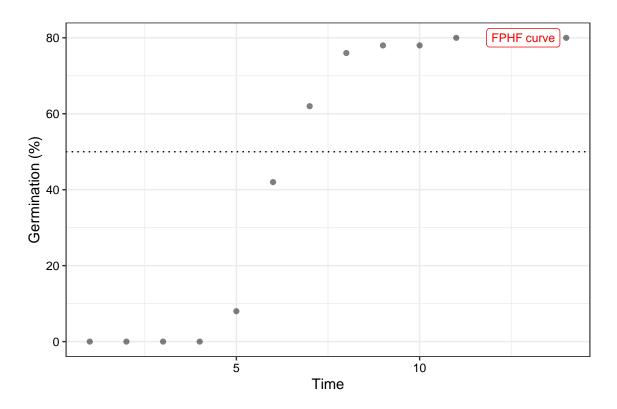


Warning: Removed 101 rows containing missing values (`geom\_function()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`).
Removed 1 rows containing missing values (`geom\_vline()`).

Warning: Removed 14 rows containing missing values (`geom\_segment()`). Removed 14 rows containing missing values (`geom\_segment()`).

Warning: Removed 1 rows containing missing values (`geom\_vline()`). Removed 1 rows containing missing values (`geom\_vline()`).



# Wrapper functions

Wrapper functions germination.indices() and FourPHFfit.bulk() are available in the package for computing results for multiple samples in batch from a data frame of germination counts recorded at specific time intervals.

**germination.indices()** This wrapper function can be used to compute several germination indices simultaneously for multiple samples in batch.

Genotype Rep Day01 Day02 Day03 Day04 Day05 Day06 Day07 Day08 Day09 Day10 Day11 Day12 Day13 Day14 Tot G1 G2 GЗ G4 G5 G1 G2 G3 G4 G5 G1 

```
12
         G2
                                                                  7
               3
                     0
                            0
                                  0
                                        0
                                               3
                                                    20
                                                           10
                                                                         1
                                                                               1
                                                                                      1
                                                                                                   0
                                                                                                         0
                                                                                            1
13
         G3
               3
                     0
                            0
                                  0
                                        0
                                               4
                                                    19
                                                           12
                                                                  8
                                                                         1
                                                                               1
                                                                                      0
                                                                                            1
                                                                                                   1
                                                                                                         0
14
                                                                                                         0
         G4
              3
                     0
                            0
                                  0
                                        0
                                               3
                                                    21
                                                           11
                                                                  6
                                                                         1
                                                                               0
                                                                                      1
                                                                                            1
                                                                                                   0
15
         G5
               3
                            0
                                  0
                                               4
                                                                  8
                                                                                            0
                                                                                                   0
                                                                                                         0
                     0
                                        0
                                                    17
                                                           10
                                                                         1
                                                                               1
                                                                                      1
   GermPercent PeakGermPercent FirstGermTime LastGermTime PeakGermTime TimeSpreadGerm t50 Coolbear t50
      80.00000
                       34.00000
                                                                          6
                                                                                          6
                                                                                                5.970588
                                                                                                            5.
1
                                              5
                                                           11
2
      82.35294
                       29.41176
                                              4
                                                           12
                                                                          6
                                                                                          8
                                                                                                6.192308
                                                                                                            6.
3
      93.75000
                       37.50000
                                              4
                                                           12
                                                                          6
                                                                                          8
                                                                                                            5.
                                                                                                6.000000
4
      90.19608
                       37.25490
                                              5
                                                           12
                                                                          6
                                                                                          7
                                                                                                6.041667
                                                                                                            6.
5
      96.00000
                                              5
                                                           13
                                                                          6
                                                                                          8
                                                                                                            5.
                       40.00000
                                                                                                5.975000
6
      93.87755
                       42.85714
                                              5
                                                           12
                                                                          6
                                                                                          7
                                                                                                5.976190
                                                                                                            5.
7
                                              5
                                                                          6
      87.50000
                       37.50000
                                                           11
                                                                                          6
                                                                                                5.972222
                                                                                                            5.
8
      85.10638
                       29.78723
                                              4
                                                           12
                                                                          6
                                                                                          8
                                                                                                6.208333
                                                                                                            6.
9
      86.53846
                       36.53846
                                              4
                                                           12
                                                                          6
                                                                                          8
                                                                                                6.000000
                                                                                                            5.
10
      90.00000
                       36.00000
                                              5
                                                           12
                                                                          6
                                                                                          7
                                                                                                6.076923
                                                                                                            6.
11
      94.11765
                       41.17647
                                              5
                                                           13
                                                                          6
                                                                                          8
                                                                                                5.928571
                                                                                                            5.
12
                                              5
                                                           12
                                                                          6
                                                                                          7
                                                                                                5.975000
                                                                                                            5.
      86.27451
                       39.21569
                                              5
                                                                          6
13
      95.91837
                       38.77551
                                                           13
                                                                                          8
                                                                                                6.083333
                                                                                                            6.
14
      91.66667
                       43.75000
                                              5
                                                           12
                                                                          6
                                                                                          7
                                                                                                5.928571
                                                                                                            5.
                                              5
15
      87.50000
                       35.41667
                                                           11
                                                                          6
                                                                                          6
                                                                                                6.050000
                                                                                                            6.
   MeanGermTime VarGermTime SEGermTime CVGermTime MeanGermRate
                                                                   VarGermRate
                                                                                  SEGermRate
                                                                                                    CVG GermRa
1
       6.700000
                    1.446154
                               0.1901416
                                          0.1794868
                                                         0.1492537 0.0007176543 0.004235724 14.92537
2
                    2.027875
                               0.2197333
                                          0.2076717
                                                         0.1458333 0.0009172090 0.004673148 14.58333
       6.857143
3
       6.866667
                    2.572727
                               0.2391061
                                          0.2335882
                                                         0.1456311 0.0011572039 0.005071059 14.56311
4
                               0.2180907
                                                         0.1451104 0.0009701218 0.004592342 14.51104
       6.891304
                    2.187923
                                          0.2146419
5
       6.812500
                    2.368351
                               0.2221275
                                          0.2259002
                                                         0.1467890 0.0010995627 0.004786184 14.67890
6
       6.869565
                    2.071498
                               0.2122088
                                          0.2095140
                                                         0.1455696 0.0009301809 0.004496813 14.55696
7
                    1.389663
                               0.1818989
                                          0.1761967
                                                         0.1494662 0.0006935558 0.004063648 14.94662
       6.690476
8
                                                        0.1454545 0.0009454531 0.004861721 14.54545
       6.875000
                    2.112179
                               0.2297923
                                          0.2113940
9
                                          0.2208604
                                                         0.1456311 0.0010345321 0.004794747 14.56311
       6.866667
                    2.300000
                               0.2260777
10
       6.822222
                    1.831313
                               0.2017321
                                          0.1983606
                                                        0.1465798 0.0008453940 0.004334343 14.65798
11
       6.791667
                    2.381206
                               0.2227295
                                          0.2272072
                                                         0.1472393 0.0011191581 0.004828643 14.72393
12
                                                         0.1452145 0.0009558577 0.004660905 14.52145
       6.886364
                    2.149577
                               0.2210295
                                          0.2129053
13
                    2.539315
                               0.2324392
                                          0.2297410
                                                         0.1441718 0.0010970785 0.004831366 14.41718
       6.936170
                                                         0.1476510 0.0009033254 0.004531018 14.76510
14
       6.772727
                    1.900634
                               0.2078370
                                          0.2035568
15
       6.809524
                    1.670151
                               0.1994129
                                          0.1897847
                                                         0.1468531 0.0007767634 0.004300508 14.68531
   GermRateRecip Faroog GermSpeed Count GermSpeed Percent GermSpeedAccumulated Count GermSpeedAccumulat
1
               0.1683168
                                 6.138925
                                                    12.27785
                                                                                 34.61567
2
               0.1625000
                                 6.362698
                                                    12.47588
                                                                                 35.54058
3
               0.1674419
                                 6.882179
                                                    14.33787
                                                                                 38.29725
4
                                                                                 38.68453
               0.1666667
                                 6.927417
                                                    13.58317
5
               0.1680672
                                 7.318987
                                                    14.63797
                                                                                 41.00786
6
               0.1680000
                                 6.931782
                                                    14.14649
                                                                                 38.77620
7
               0.1682243
                                 6.448449
                                                    13.43427
                                                                                 36.38546
8
                                                                                 33.77079
               0.1621622
                                 6.053175
                                                    12.87909
9
               0.1674009
                                 6.830592
                                                                                 38.11511
                                                    13.13575
10
               0.1656051
                                 6.812698
                                                    13.62540
                                                                                 38.19527
11
                                 7.342796
               0.1693548
                                                    14.39764
                                                                                 41.17452
12
               0.1680672
                                 6.622258
                                                    12.98482
                                                                                 37.00640
13
               0.1655172
                                 7.052320
                                                    14.39249
                                                                                 39.29399
                                 6.706782
14
               0.1693548
                                                    13.97246
                                                                                 37.69490
15
                                 6.363925
                                                    13.25818
                                                                                 35.69697
               0.1666667
   GermSpeedCorrected_Normal GermSpeedCorrected_Accumulated WeightGermPercent MeanGermPercent MeanGermN
```

0.8653917

47.42857

5.714286

0.1534731

1

2	0.1514928		0.8462043		47.89916		5.882353	3.00
3	0.1529373		0.8510501		54.46429	)	6.696429	3.2
4	0.1505960		0.8409680		52.24090	)	6.442577	3.2
5	0.1524789		0.8543303		56.14286	5	6.857143	3.4
6	0.1506909		0.8429608		54.51895	·	6.705539	3.2
7	0.1535345		0.8663205		51.93452	2	6.250000	3.00
8	0.1513294		0.8442698		49.39210	)	6.079027	2.8
9	0.1517909		0.8470024		50.27473	3	6.181319	3.2
10	0.1513933		0.8487837		52.57143	3	6.428571	3.2
11	0.1529749		0.8578026		55.18207	•	6.722689	3.4
12	0.1505059		0.8410547		50.00000	)	6.162465	3.14
13	0.1500494		0.8360424		55.24781	-	6.851312	3.3
14	0.1524269		0.8567022		53.86905	5	6.547619	3.14
15	0.1515220		0.8499278		51.19048		6.250000	3.00
	TimsonsIndex_La		_		ateGeorge			
1	8.000000	1.00	0.571428		4	5.84000		300000
2	9.803922	1.25	0.700280		5	5.88235		142857
3	14.583333	1.40	1.04166		7	6.68750		133333
4	7.843137	1.00	0.56022		4	6.41176		108696
5	10.000000	1.00	0.71428		5	6.90000		187500
6	6.122449	1.00	0.43731		3	6.69387		130435
7	8.333333	1.00	0.595238		4	6.39583		309524
8	10.638298	1.25	0.759878		5	6.06383		125000
9	9.615385	1.25	0.686813		5	6.17307		133333
10	8.000000	1.00	0.571428		4	6.46000		177778
11	9.803922	1.00	0.700280		5	6.78431		208333
12 13	5.882353 8.163265	1.00 1.00	0.420168		3 4	6.13725 6.77551		113636
14	6.250000	1.00	0.583090 0.446428		3	6.62500		063830 227273
15	8.333333	1.00	0.595238		4	6.29166		190476
10	EmergenceRateIndex_SG Emerge							
1	292		300000	Juguerinae		970149	mer geneem	.aucinacx_i
2	300		142857			125000		
3	321		133333			553398		•
4	327		108696			675079		•
5	345		187500			045872		•
6	328	7.1	130435		6.	696203		
7	307	7.3	309524		6.	277580		•
8	285	7.1	125000		5.	818182		
9	321	7.1	133333		6.	553398		•
10	323	7.1	177778		6.	596091		•
11	346	7.2	208333		7.	067485		•
12	313	7.1	113636		6.	389439		•
13	332	7.0	063830		6.	776074		•
14	318		227273			496644		•
15	302		190476			167832		•
	PeakValue GermValue_Czabator							GermSyncl
1	9.500000 54.28571			54.28571			0.7092199	
2	9.313725 54.78662			54.78662			0.5051546	
	10.416667 69.75446			69.75446			0.3975265	
	10.049020 64.74158			54.74158			0.4672113	
	11.250000 77.14286			77.14286			0.4312184	
	10.714286 71.84506			71.84506			0.4934701	
7	10.416667 65.10417	69.41325	•	35.10417	4	1.3/690	0.7371500	0.27

```
9.574468
                       58.20345
                                     56.00669
                                                             58.20345
                                                                              43.67948 0.4855842
                                                                                                      0.22
9
    9.855769
                       60.92165
                                     58.13477
                                                             60.92165
                                                                              45.30801 0.4446640
                                                                                                      0.24
10 10.250000
                       65.89286
                                     70.91875
                                                             65.89286
                                                                              49.10820 0.5584666
                                                                                                      0.25
11 11.029412
                       74.14731
                                     77.39782
                                                             74.14731
                                                                              54.27520 0.4288905
                                                                                                      0.26
12 9.803922
                       60.41632
                                     64.44988
                                                             60.41632
                                                                              44.71582 0.4760266
                                                                                                      0.27
13 10.969388
                       75.15470
                                     78.16335
                                                                              54.94192 0.4023679
                                                                                                      0.25
                                                             75.15470
14 10.677083
                       69.90947
                                     74.40140
                                                             69.90947
                                                                              51.41913 0.5383760
                                                                                                      0.29
15 10.156250
                                     67.62031
                                                                              46.48043 0.6133519
                                                                                                      0.24
                       63.47656
                                                             63.47656
   GermUncertainty
```

1 2.062987 2 2.321514 3 2.462012 4 2.279215 5 2.146051 6 2.160545 7 2.040796 8 2.357249 9 2.321080 10 2.187983 11 2.128670 12 2.185245 13 2.241181 14 2.037680 15 2.185028

FourPHFfit.bulk() This wrapper function can be used to fit the four-parameter hill function for multiple samples in batch.

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

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Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

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Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

	Genoty	pe Re	ep Da	ay01	Day02	Day03	Day04	Day05	Day06	Day07	Day08	Day09	Day10	Day11	Day12	Day13	Day14	Tota
1	(	G1	1	0	0	0	0	4	17	10	7	1	0	1	0	0	0	
2	(	G2	1	0	0	0	1	3	15	13	6	2	1	0	1	0	0	
3	(	G3	1	0	0	0	2	3	18	9	8	2	1	1	1	0	0	
4	(	G4	1	0	0	0	0	4	19	12	6	2	1	1	1	0	0	
5	(	G5	1	0	0	0	0	5	20	12	8	1	0	0	1	1	0	
6	(	G1	2	0	0	0	0	3	21	11	7	1	1	1	1	0	0	
7	(	G2	2	0	0	0	0	4	18	11	7	1	0	1	0	0	0	
8	(	G3	2	0	0	0	1	3	14	12	6	2	1	0	1	0	0	
9	(	G4	2	0	0	0	1	3	19	10	8	1	1	1	1	0	0	
10	(	G5	2	0	0	0	0	4	18	13	6	2	1	0	1	0	0	
11	(	G1	3	0	0	0	0	5	21	11	8	1	0	0	1	1	0	
12	(	G2	3	0	0	0	0	3	20	10	7	1	1	1	1	0	0	
13	(	G3	3	0	0	0	0	4	19	12	8	1	1	0	1	1	0	
14	(	G4	3	0	0	0	0	3	21	11	6	1	0	1	1	0	0	
15	(	G5	3	0	0	0	0	4	17	10	8	1	1	1	0	0	0	
	b	С	у0	lag	Dlag5	0 t50.	.total	txp.to	otal_10	) txp.1	total_6	0 t50	.Germi	nated 1	txp.Ge	rminate	ed_10 1	txp.
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```

Multiple fitted curves generated in batch can also be plotted.

```
data(gcdata)
counts.per.intervals <- c("Day01", "Day02", "Day03", "Day04", "Day05",</pre>
                          "Day06", "Day07", "Day08", "Day09", "Day10",
                          "Day11", "Day12", "Day13", "Day14")
fits <- FourPHFfit.bulk(gcdata, total.seeds.col = "Total Seeds",</pre>
                    counts.intervals.cols = counts.per.intervals,
                    intervals = 1:14, partial = TRUE,
                    fix.y0 = TRUE, fix.a = TRUE, xp = c(10, 60),
                    tmax = 20, tries = 3, umax = 90, umin = 10)
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF_fixa_fixy0"
Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error
```

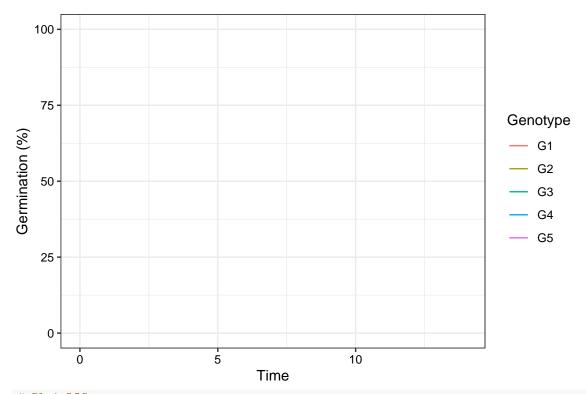
#1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

Warning in FourPHFfit(germ.counts = unlist(mget(counts.intervals.cols)), : Convergence Error #1. failed to evaluate 'fn' at starting values: could not find function "FourPHF\_fixa\_fixy0"

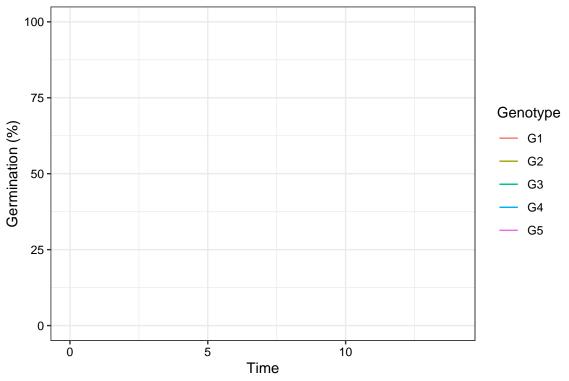
```
# Plot FPHF curves
plot(fits, group.col = "Genotype")
```

Warning: Removed 1965 rows containing missing values (`geom\_line()`).

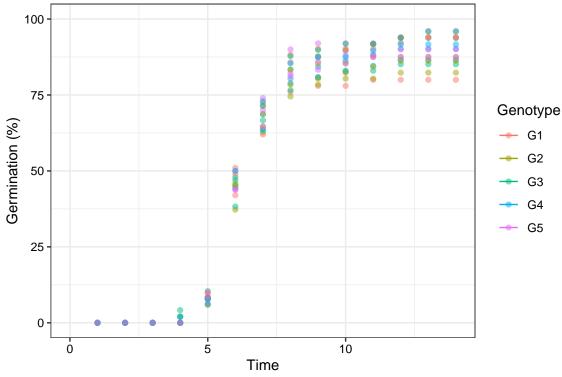


```
# Plot ROG curves
plot(fits, rog = TRUE, group.col = "Genotype")
```

Warning: Removed 1965 rows containing missing values (`geom\_line()`).

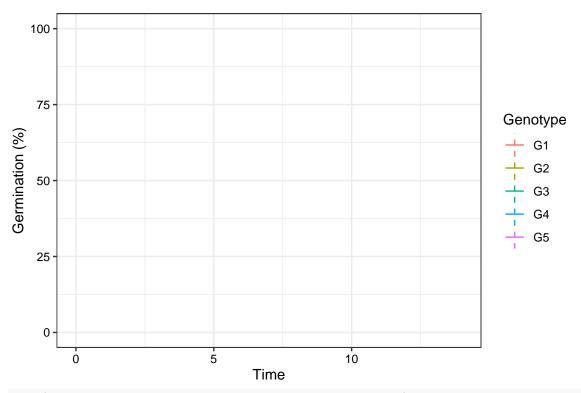


```
# Plot FPHF curves with points
plot(fits, group.col = "Genotype", show.points = TRUE)
```



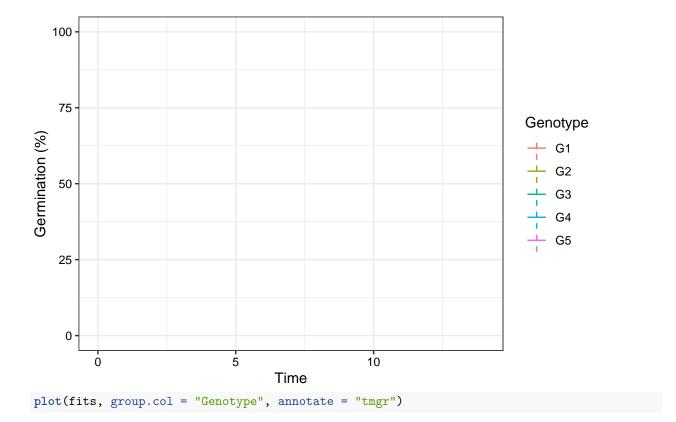
```
# Plot FPHF curves with annotations
plot(fits, group.col = "Genotype", annotate = "t50.total")
```

Warning: Removed 15 rows containing missing values (`geom\_vline()`).

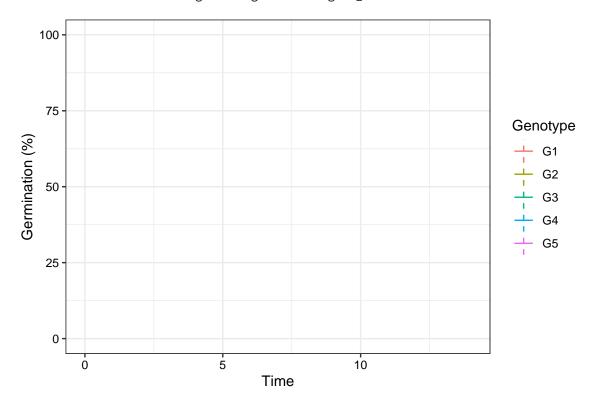


plot(fits, group.col = "Genotype", annotate = "t50.germ")

Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).

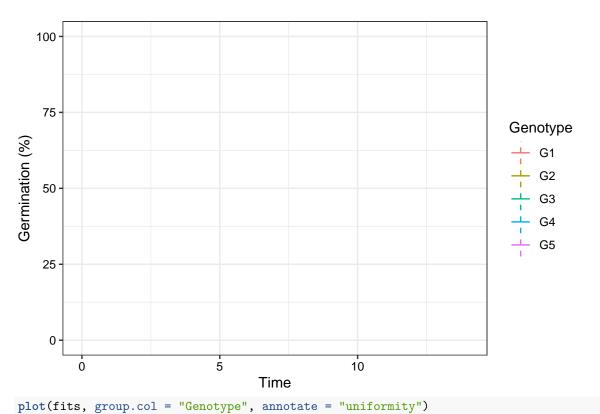


Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).



```
plot(fits, group.col = "Genotype", annotate = "mgt")
```

Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).

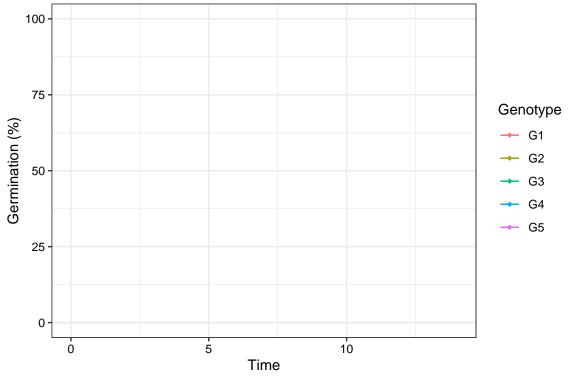


provided, group.com according, among among a

Warning: Removed 1965 rows containing missing values (`geom\_line()`).

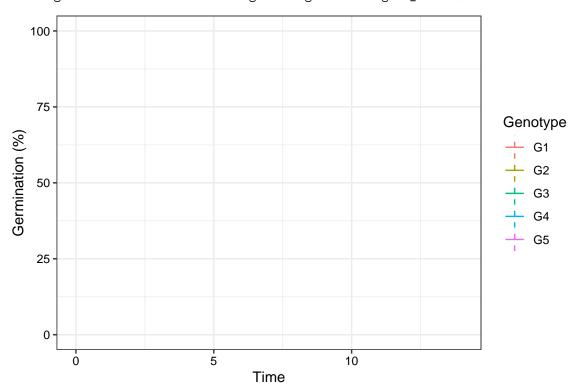
Warning: Removed 15 rows containing missing values (`geom\_point()`). Removed 15 rows containing missing values (`geom\_point()`).

Warning: Removed 15 rows containing missing values (`geom\_segment()`).



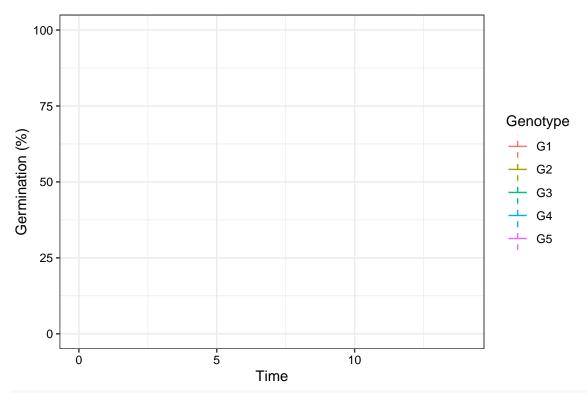
```
# Plot ROG curves with annotations
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.total")
```

Warning: Removed 15 rows containing missing values (`geom\_vline()`).



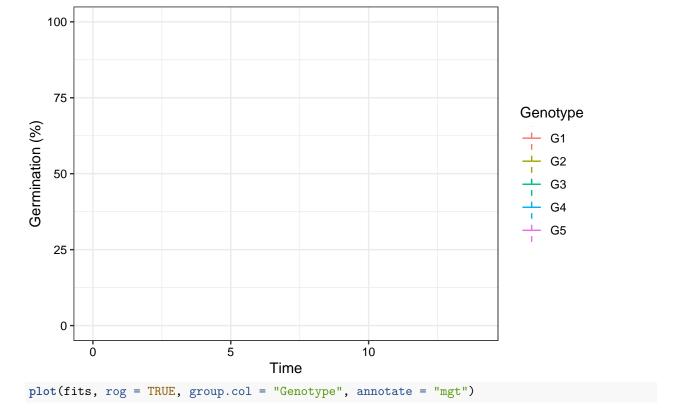
```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "t50.germ")
```

Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).

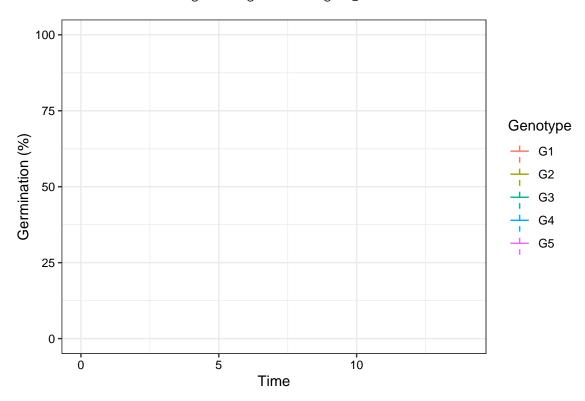


plot(fits, rog = TRUE, group.col = "Genotype", annotate = "tmgr")

Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).



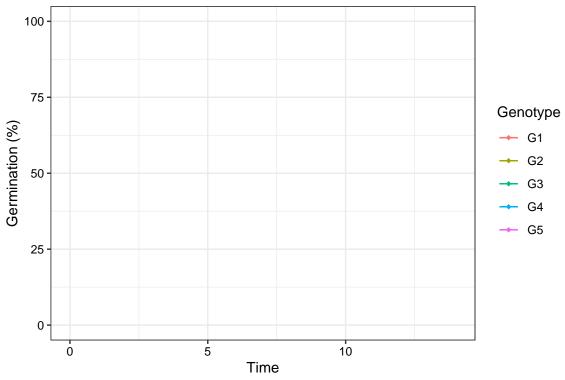
Warning: Removed 1965 rows containing missing values (`geom\_line()`). Removed 15 rows containing missing values (`geom\_vline()`).



```
plot(fits, rog = TRUE, group.col = "Genotype", annotate = "uniformity")
```

Warning: Removed 15 rows containing missing values (`geom\_point()`). Removed 15 rows containing missing values (`geom\_point()`).

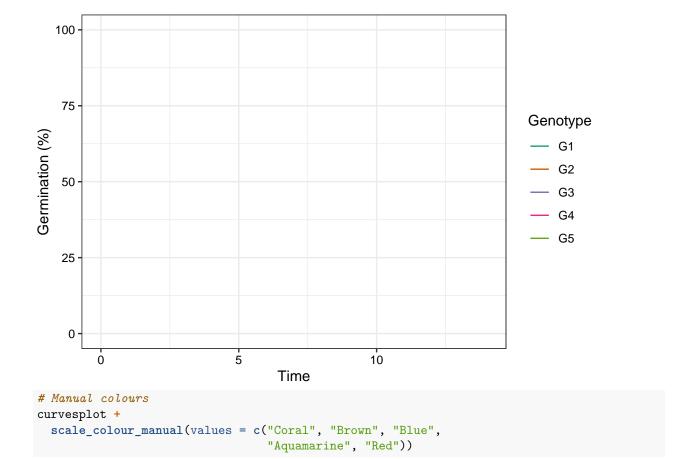
Warning: Removed 15 rows containing missing values (`geom\_segment()`).

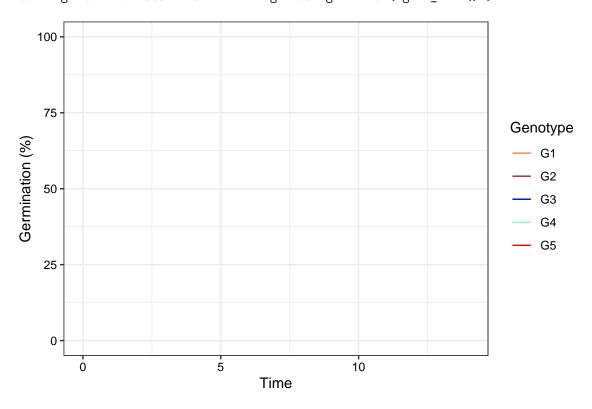


```
# Change colour of curves using ggplot2 options
library(ggplot2)
curvesplot <- plot(fits, group.col = "Genotype")

# 'Dark2' palette from RColorBrewer
curvesplot + scale_colour_brewer(palette = "Dark2")</pre>
```

Warning: Removed 1965 rows containing missing values (`geom\_line()`).





# Citing germinationmetrics

```
To cite the R package 'germinationmetrics' in publications use:
```

Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and Kalyani Srinivasan (). germinationmetrics: Seed Germination Indices and Curve Fitting. R package version 0.1.7.9000, https://github.com/aravind-j/germinationmetricshttps://cran.r-project.org/package=germinationmetrics.

A BibTeX entry for LaTeX users is

```
@Manual{,
    title = {germinationmetrics: Seed Germination Indices and Curve Fitting},
    author = {J. Aravind and S. {Vimala Devi} and J. Radhamani and Sherry Rachel Jacob and {Kalyani Srinote = {R package version 0.1.7.9000 https://aravind-j.github.io/germinationmetrics/ https://CRAN.R
```

This free and open-source software implements academic research by the authors and co-workers. If you u it, please support the project by citing the package.

#### Session Info

}

```
sessionInfo()
```

R Under development (unstable) (2023-08-09 r84924 ucrt)

Platform: x86\_64-w64-mingw32/x64

Running under: Windows 11 x64 (build 22621)

Matrix products: default

## locale:

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[4] LC\_NUMERIC=C LC\_TIME=English\_India.utf8

time zone: Asia/Calcutta tzcode source: internal

attached base packages:

[1] stats graphics grDevices utils datasets methods base

other attached packages:

[1] germinationmetrics\_0.1.7.9000 ggplot2\_3.4.2 testthat\_3.1.10

loaded via a namespace (and not attached):

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[1]	utf8_1.2.3	generics_0.1.3	tidyr_1.3.0	bitops_1.0-7	stringi_1.7.12
[7]	digest_0.6.33	magrittr_2.0.3	RColorBrewer_1.1-3	evaluate_0.21	grid_4.4.0
[13]	fastmap_1.1.1	plyr_1.8.8	Matrix_1.6-0	ggrepel_0.9.3	backports_1.4.1
[19]	tinytex_0.46	httr_1.4.6	pander_0.6.5	purrr_1.0.1	fansi_1.0.4
[25]	XML_3.99-0.14	Rdpack_2.4	cli_3.6.1	rlang_1.1.1	rbibutils_2.2.14
[31]	withr_2.5.0	yam1_2.3.7	tools_4.4.0	parallel_4.4.0	reshape2_1.4.4
[37]	colorspace_2.1-0	mathjaxr_1.6-0	curl_5.0.1	broom_1.0.5	vctrs_0.6.3
[43]	lifecycle_1.0.3	gslnls_1.1.2	stringr_1.5.0	pkgconfig_2.0.3	rJava_1.0-6
[49]	gtable_0.3.3	data.table_1.14.8	glue_1.6.2	Rcpp_1.0.11	highr_0.10
[55]	tibble_3.2.1	tidyselect_1.2.0	rstudioapi_0.15.0	knitr_1.43	farver_2.1.1

lat pkg bri sca mun dpl R6\_ pil xfu [61] labeling\_0.4.2 rmarkdown\_2.23 compiler\_4.4.0 RCurl\_1.98-1.12

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