The germinationmetrics Package: A Brief Introduction

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Overview

The package germinationmetrics is a collection of functions which implements various methods for describing the time-course of germination in terms of single-value germination indices as well as fitted curves.

The goal of this vignette is to introduce the users to these functions and get started in describing sequentially recorded germination count data. This document assumes a basic knowledge of R programming language.



Installation

The package can be installed using the following functions:

```
# Install from CRAN
install.packages('germinationmetrics', dependencies=TRUE)

# Install development version from Github
devtools::install_github("aravind-j/germinationmetrics")
```

Then the package can be loaded using the function

library(germinationmetrics)

Version History

The current version of the package is 0.1.4. The previous versions are as follows.

Table 1. Version history of germinationmetrics R package.

Version	Date
0.1.0	2018-04-17
0.1.1	2018-07-26
0.1.1.1	2018-10-16
0.1.2	2018-10-31

To know detailed history of changes use news(package='germinationmetrics').

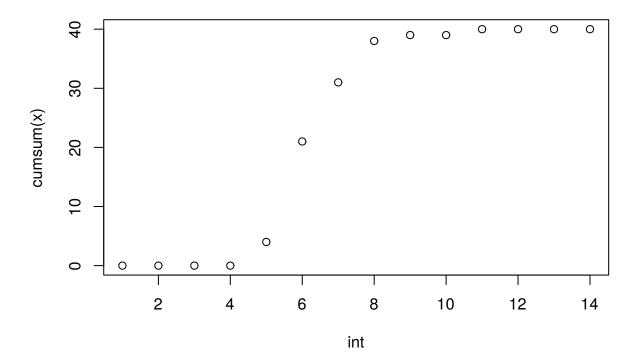
Germination count data

Typically in a germination test, the germination count data of a fixed number of seeds is recorded at regular intervals for a definite period of time or until all the seeds have germinated. These germination count data can be either partial or cumulative (Table 2).

Table 2 : A typical germination count data.

intervals	counts	cumulative.counts
1	0	0
2	0	0
3	0	0
4	0	0
5	4	4
6	17	21
7	10	31
8	7	38
9	1	39
10	0	39
11	1	40
12	0	40
13	0	40
14	0	40

The time-course of germination can be plotted as follows.



Single-value germination indices

The details about the single-value germination indices implemented in $\mathsf{germinationmetrics}$ are described in Table 3.

 ${\bf Table~3:}~{\bf Single-value~germination~indices~implemented~in~germinationmetrics.}$

Germination index	Function	Details	Unit	Measures	Reference
Germination percentage or Final germination percentage or Germinability (GP)	GermPercent	It is computed as follows. $GP = \frac{N_g}{N_t} \times 100$ Where, N_g is the number of germinated seeds and N_t is the total number of seeds.	Percentage (%)	Germinatior capacity	ISTA (2015)
Time for the first germination or Germination time lag (t_0)	FirstGermTime	It is the time for first germination to occur (e.g. First day of germination)	time	Germinatior time	Edwards (1932); Czabator (1962); Goloff and Bazzaz (1975); Labouriau (1983a); Ranal (1999); Quintanilla et al. (2000)
Time for the last germination (t_g)	LastGermTime	It is the time for last germination to occur (e.g. Last day of germination)	time	Germinatior time	Edwards (1932)
Time spread of germination or Germination distribution	TimeSpreadGerm	It is the difference between time for last germination (t_g) and time for first germination (t_0) . Time spread of germination = $t_g - t_0$	time	Germination time	Al-Mudaris (1998); Schrader and Graves (2000); Kader (2005)
Peak period of germination or Modal time of germination	PeakGermTime	It is the time in which highest frequency of germinated seeds are observed and need not be unique.	time	Germination time	Ranal and Santana (2006)
Median germination time (t_{50}) (Coolbear)	t50	It is the time to reach 50% of final/maximum germination. With argument method specified as "coolbear", it is computed as follows. $t_{50} = T_i + \frac{(\frac{N+1}{2} - N_i)(T_j - T_i)}{N_j - N_i}$ Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N+1}{2} < N_j$.	time	Germination time	Coolbear et al. (1984)

Germination index	Function	Details	Unit	Measures	Reference
Median germination time (t_{50}) (Farooq)	t50	With argument method specified as "farooq", it is computed as follows. $t_{50} = T_i + \frac{(\frac{N}{2} - N_i)(T_j - T_i)}{N_j - N_i}$ Where, t_{50} is the median germination time, N is the final number of germinated seeds, and N_i and N_j are the total number of seeds germinated in adjacent counts at time T_i and T_j respectively, when $N_i < \frac{N}{2} < N_j$.	time	Germinatior time	Farooq et al. (2005)
Mean germination time or Mean length of incubation time (\overline{T}) or Germination resistance (GR) or Sprouting index (SI) or Emergence index (EI)	MeanGermTime	It is the average length of time required for maximum germination of a seed lot and is estimated according to the following formula. $\overline{T} = \frac{\sum_{i=1}^k N_i T_i}{\sum_{i=1}^k N_i}$ Where, T_i is the time from the start of the experiment to the i th interval, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals. It is the inverse of mean germination rate (\overline{V}) . $\overline{T} = \frac{1}{\overline{V}}$	time	Germinatior time	Edmond and Drapala (1958); Czabator (1962); Smith and Millet (1964); Gordon (1969); Gordon (1971); Mock and Eberhart (1972); Ellis and Roberts (1980) Labouriau (1983a); Ranal and Santana (2006)
Variance of germination time (s_T^2)	VarGermTime	It is computed according to the following formula. $s_T^2 = \frac{\sum_{i=1}^k N_i (T_i - \overline{T})^2}{\sum_{i=1}^k N_i - 1}$ Where, T_i is the time from the start of the experiment to the i th interval, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but	time	Germinatior time	Labouriau (1983a); Ranal and Santana (2006)

Where, T_i is the time from the start of the experiment to the ith interval, N_i is the number of seeds germinated in the ith time interval (not the accumulated number, but the number corresponding to the ith interval), and k is the total number of time intervals.

Germination index	Function	Details	Unit	Measures	Reference
Standard error of germination time $(s_{\overline{T}})$	SEGermTime	It signifies the accuracy of the calculation of the mean germination time. It is estimated according to the following formula: $s_{\overline{T}} = \sqrt{\frac{s_T^2}{\sum_{i=1}^k N_i}}$ Where, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval) and k is the total number of time intervals.	time	Germinatior time	Labouriau (1983a); Ranal and Santana (2006)
Mean germination rate (\overline{V})	MeanGermRate	It is computed according to the following formula: $\overline{V} = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i}$ Where, T_i is the time from the start of the experiment to the i th interval, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals. It is the inverse of mean germination time (\overline{T}) . $\overline{V} = \frac{1}{\overline{T}}$	time ⁻¹	Germination rate	Labouriau and Valadares (1976); Labouriau (1983b); Ranal and Santana (2006)
Coefficient of velocity of germination (CVG) or Coefficient of rate of germination (CRG) or Kotowski's coefficient of velocity	CVG	It is estimated according to the following formula. $CVG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k N_i T_i} \times 100$ $CVG = \overline{V} \times 100$ Where, T_i is the time from the start of the experiment to the i th interval, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals.	% day ⁻¹	Germination rate	Kotowski (1926), Nichols and Heydecker (1968); Bewley and Black (1994); Labouriau (1983b); Scott et al. (1984)
Variance of germination rate (s_V^2)	VarGermRate	It is calculated according to the following formula. $s_V^2=\overline{V}^4\times s_T^2$ Where, s_T^2 is the variance of germination time.	time ⁻²	Germinatior rate	Labouriau (1983b); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Standard error of germination rate $(s_{\overline{V}})$	SEGermRate	It is estimated according to the following formula. $s_{\overline{V}} = \sqrt{\frac{s_V^2}{\sum_{i=1}^k N_i}}$ Where, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals.	time ⁻¹	Germination rate	Labouriau (1983b); Ranal and Santana (2006)
Germination rate as the reciprocal of the median time (v_{50})	GermRateRecip	It is the reciprocal of the median germination time $(t_{50}).$ $v_{50} = \frac{1}{t_{50}}$	${ m time}^{-1}$	Germination rate	Went (1957); Labouriau (1983b); Ranal and Santana (2006)
Speed of germination or Germination rate Index or index of velocity of germination or Emergence rate index (Allan, Vogel and Peterson; Erbach; Hsu and Nelson) or Germination index (AOSA)	GermSpeed	It is the rate of germination in terms of the total number of seeds that germinate in a time interval. It is estimated as follows. $S = \sum_{i=1}^k \frac{N_i}{T_i}$ Where, T_i is the time from the start of the experiment to the i th interval, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of germination.	% time ⁻¹	Mixed	Throneberry and Smith (1955); Maguire (1962); Allan et al. (1962); Kendrick and Frankland (1969); Bouton et al. (1976); Erbach (1982); AOSA (1983); Khandakar and Bradbeer (1983); Hsu and Nelson (1986); Bradbeer (1988); Wardle et al. (1991)

Germination index	Function	Details	Unit	Measures	Reference
Speed of accumulated germination	GermSpeedAccumula	It is the rate of germination in terms of the accumulated/cumulative total number of seeds that germinate in a time interval. It is estimated as follows.	% time ⁻¹	Mixed	Bradbeer (1988); Wardle et al. (1991); Haugland and Brandsaeter (1996); Santana and Ranal (2004)
		$S_{accumulated} = \sum_{i=1}^k \frac{\sum_{j=1}^i N_j}{T_i}$ Where, T_i is the time from the start of the experiment to the i th interval, $\sum_{j=1}^i N_j$ is the cumuative/accumulated number of seeds germinated in the i th interval, and k is the total number of time intervals. Instead of germination counts, germination percentages may also be used for computation of speed of			
Corrected germination rate index	GermSpeedCorrecte	germination. It is computed as follows. $S_{corrected} = \frac{S}{FGP}$ Where, FGP is the final germination percentage or germinability.	${ m time^{-1}}$	Mixed	Evetts and Burnside (1972)
Weighted germination percentage (WGP)	WeightGermPercent	It is estimated as follows. $WGP = \frac{\sum_{i=1}^k (k-i+1)N_i}{k\times N}\times 100$ Where, N_i is the number of seeds that germinated in the time interval i (not cumulative, but partial count), N is the total number of seeds tested, and k is the total number of time intervals.		Mixed	Reddy et al. (1985); Reddy (1978)
Mean germination percentage per unit time (\overline{GP})	MeanGermPercent	It is estimated as follows. $\overline{GP} = \frac{GP}{T_k}$ Where, GP is the final germination percentage, T_k is the time at the k th time interval, and k is the total number of time intervals required for final germination.		Mixed	Czabator (1962)
Number of seeds germinated per unit time \overline{N}	MeanGermNumber	It is estimated as follows. $\overline{N} = \frac{N_g}{T_k}$ Where, N_g is the number of germinated seeds at the end of the germination test, T_k is the time at the k th time interval, and k is the total number of time intervals required for final germination.		Mixed	Khamassi et al. (2013)

Germination index	Function	Details	Unit	Measures	Reference
Timson's index $[\sum 10 \text{ (Ten summation)}, \sum 5 \text{ or } \sum 20]$ or Germination energy index (GEI)	TimsonsIndex	It is the progressive total of cumulative germination percentage recorded at specific intervals for a set period of time and is estimated in terms of cumulative germination percentage (G_i) as follows. $\Sigma k = \sum_{i=1}^k G_i$ Where, G_i is the cumulative germination percentage in time interval i , and k is the total number of time intervals. It also estimated in terms of partial germination percentage as follows. $\Sigma k = \sum_{i=1}^k g_i(k-j)$ Where, g_i is the germination (not cumulative, but partial germination) in time interval i (i varying from 0 to k), k is the total number of time intervals, and $j = i-1$.		Mixed	Grose and Zimmer (1958); Timson (1965); Lyon and Coffelt (1966); Chaudhary and Ghildyal (1970); Negm and Smith (1978); Brown and Mayer (1988); Baskin and Baskin (1998); Goodchild and Walker (1971)
Modified Timson's index (Σk_{mod}) (Labouriau)	TimsonsIndex	It is estimated as Timson's index Σk divided by the sum of partial germination percentages. $\Sigma k_{mod} = \frac{\Sigma k}{\sum_{i=1}^k g_i}$		Mixed	Ranal and Santana (2006)
Modified Timson's index (Σk_{mod}) (Khan and Unger)	TimsonsIndex	It is estimated as Timson's index (Σk) divided by the total time period of germination (T_k) . $\Sigma k_{mod} = \frac{\Sigma k}{T_k}$		Mixed	Khan and Ungar (1984)
George's index (GR)	GermRateGeorge	It is estimated as follows. $GR = \sum_{i=1}^k N_i K_i$ Where N_i is the number of seeds germinated by i th interval and K_i is the number of intervals(eg. days) until the end of the test, and and k is the total number of time intervals.		Mixed	George (1961); Tucker and Wright (1965); Nichols and Heydecker (1968)

Germination index	Function	Details	Unit	Measures	Reference
Germination Index (GI) (Melville)	GermIndex	It is estimated as follows. $GI = \sum_{i=1}^k \frac{ (T_k - T_i) N_i }{N_t}$ Where, T_i is the time from the start of the experiment to the i th interval (day for the example), N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), N_t is the total number of seeds used in the test, and k is the total number of time intervals.		Mixed	Melville et al. (1980)
Germination Index (GI_{mod}) (Melville; Santana and Ranal)	GermIndex	It is estimated as follows. $GI_{mod} = \sum_{i=1}^k \frac{ (T_k - T_i) N_i }{N_g}$ Where, T_i is the time from the start of the experiment to the i th interval (day for the example), N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), N_g is the total number of germinated seeds at the end of the test, and k is the total number of time intervals.		Mixed	Melville et al. (1980); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index (ERI) or Germination Rate Index (Shmueli and Goldberg)	EmergenceRateInde	It is estimated as follows. $ERI = \sum_{i=i_0}^{k-1} N_i(k-i)$ Where, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.		Mixed	Shmueli and Goldberg (1971)

Germination index	Function	Details	Unit	Measures	Reference
Modified Emergence Rate Index (ERI _{mod}) or Modified Germination Rate Index (Shmueli and Goldberg; Santana and Ranal)	EmergenceRateInde	It is estimated by dividing Emergence rate index (ERI) by total number of emerged seedlings (or germinated seeds). $ERI_{mod} = \frac{\sum_{i=i_0}^{k-1} N_i(k-i)}{N_g} = \frac{ERI}{N_g}$ Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), i_0 is the time interval when emergence/germination started, and k is the total number of time intervals.		Mixed	Shmueli and Goldberg (1971); Santana and Ranal (2004); Ranal and Santana (2006)
Emergence Rate Index (ERI) or Germination Rate Index (Bilbro & Wanjura)	EmergenceRateInde	It is the estimated as follows. $ERI = \frac{\sum_{i=1}^k N_i}{\overline{T}} = \frac{N_g}{\overline{T}}$ Where, N_g is the total number of germinated seeds at the end of the test, N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and \overline{T} is the mean germination time or mean emergence time.		Mixed	Bilbro and Wanjura (1982)
Emergence Rate Index (ERI) or Germination Rate Index $(Fakorede)$	EmergenceRateInde	It is estimated as follows. $ERI=\frac{\overline{T}}{FGP/100}$ Where, \overline{T} is the Mean germination time and FGP is the final germination time.		Mixed	Fakorede and Ayoola (1980); Fakorede and Ojo (1981); Fakorede and Agbana (1983)
Peak value (PV) (Czabator) or Emergence Energy (EE)	PeakValue	It is the accumulated number of seeds germinated at the point on the germination curve at which the rate of germination starts to decrease. It is computed as the maximum quotient obtained by dividing successive cumulative germination values by the relevant incubation time. $PV = \max\left(\frac{G_1}{T_1}, \frac{G_2}{T_2}, \cdots \frac{G_k}{T_k}\right)$ Where, T_i is the time from the start of the experiment to the i th interval, G_i is the cumulative germination percentage in the i th time interval, and k is the total number of time intervals.	% time ⁻¹	Mixed	Czabator (1962); Bonner (1967)

Germination index	Function	Details	Unit	Measures	Reference
Germination value (GV) (Czabator)	GermValue	It is computed as follows. $GV = PV \times MDG$ Where, PV is the peak value and MDG is the mean daily germination percentage from the onset of germination. It can also be computed for other time intervals of successive germination counts, by replacing MDG with the mean germination percentage per unit time (\overline{GP}) . GV value can be modified (GV_{mod}) , to consider the entire duration from the beginning of the test instead of just from the onset of germination.		Mixed	Czabator (1962); Brown and Mayer (1988)
Germination value (GV) (Diavanshir and Pourbiek)	GermValue	It is computed as follows. $GV = \frac{\sum DGS}{N} \times GP \times c$ Where, DGS is the daily germination speed computed by dividing cumulative germination percentage by the number of days since the since the onset of germination, N is the frequency or number of DGS calculated during the test, GP is the germination percentage expressed over 100, and c is a constant. The value of c is decided on the basis of average daily speed of germination $(\sum \frac{DGS}{N})$. If it is less than 10, then c value of 10 can be used and if it is more than 10, then value of 7 or 8 can be used for c . GV value can be modified (GV_{mod}) , to consider the entire duration from the beginning of the test instead of just from the onset of germination.		Mixed	Djavanshir and Pourbeik (1976); Brown and Mayer (1988)
Coefficient of uniformity of germination (CUG)	CUGerm	It is computed as follows. $CUG = \frac{\sum_{i=1}^k N_i}{\sum_{i=1}^k (\overline{T} - T_i)^2 N_i}$ Where, \overline{T} is the the mean germination time, T_i is the time from the start of the experiment to the i th interval (day for the example), N_i is the number of seeds germinated in the i th time interval (not the accumulated number, but the number corresponding to the i th interval), and k is the total number of time intervals.		Germinatior unifromity	Heydecker (1972); Bewley and Black (1994)
Coefficient of variation of the germination time (CV_T)	CVGermTime	It is estimated as follows. $CV_T=\sqrt{\frac{s_T^2}{\overline{T}}}$ Where, s_T^2 is the variance of germination time and \overline{T} is the mean germination time.		Germinatior unifromity	Gomes (1960); Ranal and Santana (2006)

Germination index	Function	Details	Unit	Measures	Reference
Synchronization index (\overline{E}) or Uncertainty of the germination process (U) or informational entropy (H)	GermUncertainty	It is estimated as follows. $\overline{E} = -\sum_{i=1}^k f_i \log_2 f_i$ Where, f_i is the relative frequency of germination $(f_i = \frac{N_i}{\sum_{i=1}^k N_i}), \ N_i \text{ is the number of seeds germinated}$ on the i th time interval, and k is the total number of time intervals.	bit	Germination synchrony	Shannon (1948); Labouriau and Valadares (1976); Labouriau (1983b)
Synchrony of germination (Z index)	GermSynchrony	It is computed as follows. $Z = \frac{\sum_{i=1}^k C_{N_i,2}}{C_{\Sigma N_i,2}}$ Where, $C_{N_i,2}$ is the partial combination of the two germinated seeds from among N_i , the number of seeds germinated on the i th time interval (estimated as $C_{N_i,2} = \frac{N_i(N_i-1)}{2}$), and $C_{\Sigma N_i,2}$ is the partial combination of the two germinated seeds from among the total number of seeds germinated at the final count, assuming that all seeds that germinated did so simultaneously.		Germinatior synchrony	Primack (1985); Ranal and Santana (2006)

Examples

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
# From partial germination counts
GermPercent(germ.counts = x, total.seeds = 50)
GermPercent()
[1] 80
# From cumulative germination counts
GermPercent(germ.counts = y, total.seeds = 50, partial = FALSE)
[1] 80
# From number of germinated seeds
GermPercent(germinated.seeds = 40, total.seeds = 50)
[1] 80
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
z \leftarrow c(0, 0, 0, 0, 11, 11, 9, 7, 1, 0, 1, 0, 0, 0)
int <- 1:length(x)</pre>
# From partial germination counts
FirstGermTime(germ.counts = x, intervals = int)
FirstGermTime(), LastGermTime(), PeakGermTime(), TimeSpreadGerm()
[1] 5
LastGermTime(germ.counts = x, intervals = int)
[1] 11
TimeSpreadGerm(germ.counts = x, intervals = int)
```

[1] 6

```
PeakGermTime(germ.counts = x, intervals = int)
[1] 6
# For multiple peak germination times
PeakGermTime(germ.counts = z, intervals = int)
Warning in PeakGermTime(germ.counts = z, intervals = int): Multiple peak germination times exist.
[1] 5 6
# From cumulative germination counts
FirstGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 5
LastGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 11
TimeSpreadGerm(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
PeakGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 6
# For multiple peak germination time
PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE)
Warning in PeakGermTime(germ.counts = cumsum(z), intervals = int, partial = FALSE): Multiple peak germing
[1] 5 6
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
                                _____
t50(germ.counts = x, intervals = int, method = "coolbear")
t50()
[1] 5.970588
```

```
t50(germ.counts = x, intervals = int, method = "farooq")
[1] 5.941176
# From cumulative germination counts
t50(germ.counts = y, intervals = int, partial = FALSE, method = "coolbear")
[1] 5.970588
t50(germ.counts = y, intervals = int, partial = FALSE, method = "farooq")
[1] 5.941176
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermTime(germ.counts = x, intervals = int)
MeanGermTime(), VarGermTime(), SEGermTime(), CVGermTime()
[1] 6.7
VarGermTime(germ.counts = x, intervals = int)
[1] 1.446154
SEGermTime(germ.counts = x, intervals = int)
[1] 0.1901416
CVGermTime(germ.counts = x, intervals = int)
[1] 0.1794868
# From cumulative germination counts
MeanGermTime(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 6.7

```
VarGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 19.04012
SEGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.2394781
CVGermTime(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.6512685
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
MeanGermRate(germ.counts = x, intervals = int)
MeanGermRate(), CVG(), VarGermRate(), SEGermRate(), GermRateRecip()
[1] 0.1492537
CVG(germ.counts = x, intervals = int)
[1] 14.92537
VarGermRate(germ.counts = x, intervals = int)
[1] 0.0007176543
SEGermRate(germ.counts = x, intervals = int)
[1] 0.004235724
GermRateRecip(germ.counts = x, intervals = int, method = "coolbear")
[1] 0.1674877
GermRateRecip(germ.counts = x, intervals = int, method = "farooq")
[1] 0.1683168
```

```
# From cumulative germination counts
MeanGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.1492537
CVG(germ.counts = y, intervals = int, partial = FALSE)
[1] 14.92537
VarGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.009448666
SEGermRate(germ.counts = y, intervals = int, partial = FALSE)
[1] 0.005334776
GermRateRecip(germ.counts = y, intervals = int,
              method = "coolbear", partial = FALSE)
[1] 0.1674877
GermRateRecip(germ.counts = y, intervals = int,
              method = "farooq", partial = FALSE)
[1] 0.1683168
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
GermSpeed(germ.counts = x, intervals = int)
GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)
```

[1] 34.61567

```
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                   method = "normal")
[1] 0.07673656
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                method = "accumulated")
[1] 0.4326958
# From partial germination counts (with percentages instead of counts)
GermSpeed(germ.counts = x, intervals = int,
         percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                     percent = TRUE, total.seeds = 50)
[1] 69.23134
# From cumulative germination counts
GermSpeed(germ.counts = y, intervals = int, partial = FALSE)
[1] 6.138925
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
[1] 34.61567
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "normal")
[1] 0.07673656
GermSpeedCorrected(germ.counts = y, intervals = int,
                   partial = FALSE, total.seeds = 50, method = "accumulated")
[1] 0.4326958
# From cumulative germination counts (with percentages instead of counts)
GermSpeed(germ.counts = y, intervals = int, partial = FALSE,
         percent = TRUE, total.seeds = 50)
```

[1] 12.27785

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE,
                    percent = TRUE, total.seeds = 50)
[1] 69.23134
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
# From partial germination counts
#-----
GermSpeed(germ.counts = x, intervals = int)
GermSpeed(), GermSpeedAccumulated(), GermSpeedCorrected()
[1] 6.138925
GermSpeedAccumulated(germ.counts = x, intervals = int)
[1] 34.61567
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
               method = "normal")
[1] 0.07673656
GermSpeedCorrected(germ.counts = x, intervals = int, total.seeds = 50,
                method = "accumulated")
[1] 0.4326958
# From partial germination counts (with percentages instead of counts)
GermSpeed(germ.counts = x, intervals = int,
 percent = TRUE, total.seeds = 50)
[1] 12.27785
GermSpeedAccumulated(germ.counts = x, intervals = int,
                    percent = TRUE, total.seeds = 50)
[1] 69.23134
# From cumulative germination counts
```

[1] 6.138925

GermSpeed(germ.counts = y, intervals = int, partial = FALSE)

```
GermSpeedAccumulated(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 34.61567

[1] 0.07673656

[1] 0.4326958

[1] 12.27785

[1] 69.23134

WeightGermPercent()

[1] 47.42857

[1] 47.42857

MeanGermPercent(), MeanGermNumber()

[1] 5.714286

```
MeanGermNumber(germ.counts = x, intervals = int)
```

[1] 2.857143

```
# From cumulative germination counts
#-----
MeanGermPercent(germ.counts = y, total.seeds = 50, intervals = int, partial = FALSE)
```

[1] 5.714286

```
MeanGermNumber(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 2.857143

```
# From number of germinated seeds
#-----
MeanGermPercent(germinated.seeds = 40, total.seeds = 50, intervals = int)
```

[1] 5.714286

TimsonsIndex(), GermRateGeorge()

[1] 664

```
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "none")
[1] 664
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            modification = "labouriau")
[1] 8.3
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             modification = "khanungar")
[1] 47.42857
GermRateGeorge(germ.counts = x, intervals = int)
[1] 332
# With max specified
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50, max = 10)
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            max = 10, modification = "none")
[1] 344
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
             max = 10, modification = "labouriau")
[1] 4.410256
TimsonsIndex(germ.counts = x, intervals = int, total.seeds = 50,
            max = 10, modification = "khanungar")
[1] 24.57143
GermRateGeorge(germ.counts = x, intervals = int, max = 10)
[1] 172
GermRateGeorge(germ.counts = x, intervals = int, max = 14)
[1] 332
```

[1] 664

[1] 664

[1] 8.3

[1] 47.42857

```
GermRateGeorge(germ.counts = y, intervals = int, partial = FALSE,)
```

[1] 332

[1] 344

[1] 344

[1] 4.410256

[1] 24.57143

[1] 172

[1] 332

GermIndex()

[1] 5.84

[1] 5.84

[1] 7.3

[1] 5.84

[1] 5.84

[1] 7.3

EmergenceRateIndex()

[1] 292

[1] 292

[1] 7.3

[1] 5.970149

[1] 8.375

```
# From cumulative germination counts
#-----
EmergenceRateIndex(germ.counts = y, intervals = int, partial = FALSE,)
```

[1] 292

[1] 292

[1] 7.3

[1] 5.970149

[1] 8.375

PeakValue(), GermValue()

[1] 9.5

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "czabator")
```

\$'Germination Value'
[1] 38.95

[[2]] germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent DGS 17.0 5.666667 37.0 9.250000 47.5 9.500000 52.5 8.750000 54.5 7.785714 57.0 7.125000 58.5 6.500000 61.0 6.100000 65.0 5.909091 68.5 5.708333 72.0 5.538462 75.0 5.357143 78.0 5.200000 80.0 5.000000 80.0 4.705882 81.0 4.500000 81.0 4.263158 82.0 4.100000

```
method = "dp", k = 10)
```

GermValue(germ.counts = x, intervals = int, total.seeds = 200,

\$'Germination Value'

[1] 53.36595

[[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	SumDGSbyN	GV
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250
7	4	7	109	54.5	7.785714	8.190476	44.638095
8	5	8	114	57.0	7.125000	8.012897	45.673512
9	3	9	117	58.5	6.500000	7.796769	45.611097
10	5	10	122	61.0	6.100000	7.584673	46.266503
11	8	11	130	65.0	5.909091	7.398497	48.090230
12	7	12	137	68.5	5.708333	7.229481	49.521942
13	7	13	144	72.0	5.538462	7.075752	50.945411
14	6	14	150	75.0	5.357143	6.932534	51.994006
15	6	15	156	78.0	5.200000	6.799262	53.034246
16	4	16	160	80.0	5.000000	6.670744	53.365948
17	0	17	160	80.0	4.705882	6.539753	52.318022
18	2	18	162	81.0	4.500000	6.412268	51.939373
19	0	19	162	81.0	4.263158	6.285850	50.915385
20	2	20	164	82.0	4.100000	6.164414	50.548194

\$testend

[1] 16

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "czabator", from.onset = FALSE)
```

\$'Germination Value' [1] 38.95

[[2]]

	germ.counts	${\tt intervals}$	${\tt Cumulative.germ.counts}$	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.000000
2	0	2	0	0.0	0.000000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

```
GermValue(germ.counts = x, intervals = int, total.seeds = 200,
    method = "dp", k = 10, from.onset = FALSE)
```

\$'Germination Value'

[1] 46.6952

[[2]]

LL	2]]						
	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS	SumDGSbyN	GV
1	0	1	0	0.0	0.000000	0.000000	0.000000
2	0	2	0	0.0	0.000000	0.000000	0.000000
3	34	3	34	17.0	5.666667	1.888889	3.211111
4	40	4	74	37.0	9.250000	3.729167	13.797917
5	21	5	95	47.5	9.500000	4.883333	23.195833
6	10	6	105	52.5	8.750000	5.527778	29.020833
7	4	7	109	54.5	7.785714	5.850340	31.884354
8	5	8	114	57.0	7.125000	6.009673	34.255134
9	3	9	117	58.5	6.500000	6.064153	35.475298
10	5	10	122	61.0	6.100000	6.067738	37.013202
11	8	11	130	65.0	5.909091	6.053316	39.346552
12	7	12	137	68.5	5.708333	6.024567	41.268285
13	7	13	144	72.0	5.538462	5.987174	43.107655
14	6	14	150	75.0	5.357143	5.942172	44.566291
15	6	15	156	78.0	5.200000	5.892694	45.963013
16	4	16	160	80.0	5.000000	5.836901	46.695205
17	0	17	160	80.0	4.705882	5.770370	46.162961
18	2	18	162	81.0	4.500000	5.699794	46.168331
19	0	19	162	81.0	4.263158	5.624182	45.555871
20	2	20	164	82.0	4.100000	5.547972	45.493374

\$testend

[1] 16

[1] 9.5

\$'Germination Value'

[1] 38.95

[[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

\$'Germination Value'

[1] 53.36595

[[2]]

	-11						
	germ.counts	${\tt intervals}$	Cumulative.germ.counts	Cumulative.germ.percent	DGS	${\tt SumDGSbyN}$	GV
3	34	3	34	17.0	5.666667	5.666667	9.633333
4	40	4	74	37.0	9.250000	7.458333	27.595833
5	21	5	95	47.5	9.500000	8.138889	38.659722
6	10	6	105	52.5	8.750000	8.291667	43.531250
7	4	7	109	54.5	7.785714	8.190476	44.638095
8	5	8	114	57.0	7.125000	8.012897	45.673512

9	3	9	117	58.5 6.500000	7.796769 45.611097
10	5	10	122	61.0 6.100000	7.584673 46.266503
11	8	11	130	65.0 5.909091	7.398497 48.090230
12	7	12	137	68.5 5.708333	7.229481 49.521942
13	7	13	144	72.0 5.538462	7.075752 50.945411
14	6	14	150	75.0 5.357143	6.932534 51.994006
15	6	15	156	78.0 5.200000	6.799262 53.034246
16	4	16	160	80.0 5.000000	6.670744 53.365948
17	0	17	160	80.0 4.705882	6.539753 52.318022
18	2	18	162	81.0 4.500000	6.412268 51.939373
19	0	19	162	81.0 4.263158	6.285850 50.915385
20	2	20	164	82.0 4.100000	6.164414 50.548194

\$testend

[1] 16

\$'Germination Value'

[1] 38.95

[[2]]

	germ.counts	intervals	Cumulative.germ.counts	Cumulative.germ.percent	DGS
1	0	1	0	0.0	0.00000
2	0	2	0	0.0	0.00000
3	34	3	34	17.0	5.666667
4	40	4	74	37.0	9.250000
5	21	5	95	47.5	9.500000
6	10	6	105	52.5	8.750000
7	4	7	109	54.5	7.785714
8	5	8	114	57.0	7.125000
9	3	9	117	58.5	6.500000
10	5	10	122	61.0	6.100000
11	8	11	130	65.0	5.909091
12	7	12	137	68.5	5.708333
13	7	13	144	72.0	5.538462
14	6	14	150	75.0	5.357143
15	6	15	156	78.0	5.200000
16	4	16	160	80.0	5.000000
17	0	17	160	80.0	4.705882
18	2	18	162	81.0	4.500000
19	0	19	162	81.0	4.263158
20	2	20	164	82.0	4.100000

\$'Germination Value'

[1] 46.6952

[[2]]

germ.counts intervals Cumulative.germ.counts Cumulative.germ.percent

DGS SumDGSbyN

1	0	1	0	0.0 0.000000	0.000000 0.000000
2	0	2	0	0.0 0.000000	0.000000 0.000000
3	34	3	34	17.0 5.666667	1.888889 3.211111
4	40	4	74	37.0 9.250000	3.729167 13.797917
5	21	5	95	47.5 9.500000	4.883333 23.195833
6	10	6	105	52.5 8.750000	5.527778 29.020833
7	4	7	109	54.5 7.785714	5.850340 31.884354
8	5	8	114	57.0 7.125000	6.009673 34.255134
9	3	9	117	58.5 6.500000	6.064153 35.475298
10	5	10	122	61.0 6.100000	6.067738 37.013202
11	8	11	130	65.0 5.909091	6.053316 39.346552
12	7	12	137	68.5 5.708333	6.024567 41.268285
13	7	13	144	72.0 5.538462	5.987174 43.107655
14	6	14	150	75.0 5.357143	5.942172 44.566291
15	6	15	156	78.0 5.200000	5.892694 45.963013
16	4	16	160	80.0 5.000000	5.836901 46.695205
17	0	17	160	80.0 4.705882	5.770370 46.162961
18	2	18	162	81.0 4.500000	5.699794 46.168331
19	0	19	162	81.0 4.263158	5.624182 45.555871
20	2	20	164	82.0 4.100000	5.547972 45.493374

\$testend

[1] 16

CUGerm()

[1] 0.7092199

```
# From cumulative germination counts
#-----
CUGerm(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 0.05267935

GermSynchrony(), GermUncertainty()

[1] 0.2666667

GermUncertainty(germ.counts = x, intervals = int)

[1] 2.062987

```
# From cumulative germination counts
#-----
GermSynchrony(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 0.2666667

```
GermUncertainty(germ.counts = y, intervals = int, partial = FALSE)
```

[1] 2.062987

Non-linear regression analysis

Several mathematical functions have been used to fit the cumulative germination count data and describe the germination process by non-linear regression analysis. They include functions such as Richard's, Weibull, logistic, log-logistic, gaussian, four-parameter hill function etc. Currently germinationmetrics implements the four-parameter hill function to fit the count data and computed various associated metrics.

Four-parameter hill function

The four-parameter hill function defined as follows (El-Kassaby et al., 2008).

$$f(x) = y = y_0 + \frac{ax^b}{x^b + c^b}$$

Where, y is the cumulative germination percentage at time x, y_0 is the intercept on the y axis, a is the asymptote, b is a mathematical parameter controlling the shape and steepness of the germination curve and c is the "half-maximal activation level".

The details of various parameters that are computed from this function are given in Table 4.

Table 4 Germination parameters estimated from the four-parameter hill function.

Germination parameters	Details	Unit	Measures
y intercept (y_0)	The intercept on the y axis.		
Asymptote (a)	It is the maximum cumulative germination percentage, which is equivalent to germination capacity.	%	Germination capacity
Shape and steepness (b)	Mathematical parameter controlling the shape and steepness of the germination curve. The larger the b , the steeper the rise toward the asymptote a , and the shorter the time between germination onset and maximum germination.		Germination rate

Germination parameters	Details	Unit	Measures
Half-maximal activation level (c)	Time required for 50% of viable seeds to germinate.	time	Germination time
lag	It is the time at germination onset and is computed by solving four-parameter hill function after setting y to 0 as follows. $lag = b\sqrt{\frac{-y_0c^b}{a+y_0}}$	time	Germination time
D_{lag-50}	The duration between the time at germination onset (lag) and that at 50% germination (c) .	time	Germination time
$t_{50_{total}}$	Time required for 50% of total seeds to germinate.	time	Germination time
$t_{50_{germinated}}$	Time required for 50% of viable/germinated seeds to germinate	time	Germination time
$t_{x_{total}}$	Time required for $x\%$ of total seeds to germinate.	time	Germination time
$t_{x_{germinated}}$	Time required for $x\%$ of viable/germinated seeds to germinate	time	Germination time
Uniformity $(U_{t_{max}-t_{min}})$	It is the time interval between the percentages of viable seeds specified in the arguments umin and umin to germinate.	time	Germination time
Time at maximum germination rate $(TMGR)$	The partial derivative of the four-parameter hill function gives the instantaneous rate of germination (s) as follows. $s = \frac{\partial y}{\partial x} = \frac{abc^bx^{b-1}}{(c^b+x^b)^2}$ From this function for instantaneous rate of germination, $TMGR$ can be estimated as follows. $TMGR = b\sqrt{\frac{c^b(b-1)}{b+1}}$ It represents the point in time when the instantaneous rate of germination starts to decline.	time	Germination time
Area under the curve (AUC)	It is obtained by integration of the fitted curve between time 0 and time specified in the argument tmax.		Mixed
MGT	Calculated by integration of the fitted curve and proper normalisation.	time	Germination time
Skewness	It is computed as follows.		
	$\frac{MGT}{t_{50_{germinated}}}$		

Examples

```
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
total.seeds = 50
# From partial germination counts
FourPHFfit(germ.counts = x, intervals = int, total.seeds = 50, tmax = 20)
FourPHFfit()
$data
  gp csgp intervals
      0
  0
2
  0
       0
3
  0
       0
                 3
4
  0
      0
5 8
      8
                5
6 34
      42
                 6
7 20
      62
                7
8 14
       76
                8
9
  2
       78
                9
       78
                10
10 0
11 2
       80
                11
12 0
       80
                12
13 0
       80
                13
14 0
       80
                14
$Parameters
 term estimate std.error statistic
                                    p.value
   a 80.000000 1.24158597 64.43372 1.973240e-14
   b 9.881947 0.70779381 13.96162 6.952324e-08
  c 6.034954 0.04952654 121.85294 3.399384e-17
   y0 0.000000 0.91607007 0.00000 1.000000e+00
$Fit
    sigma isConv
                      finTol
                                logLik
                                           AIC
                                                    BIC deviance df.residual
1 1.769385 TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723
$a
[1] 80
$b
[1] 9.881947
$с
[1] 6.034954
$y0
```

```
[1] 0
$lag
[1] 0
$Dlag50
[1] 6.034954
$t50.total
[1] 6.355122
$txp.total
               60
     10
4.956266 6.744598
$t50.Germinated
[1] 6.034954
$txp.Germinated
     10
4.831809 6.287724
$Uniformity
        90
                   10 uniformity
  7.537688 4.831809 2.705880
$TMGR
[1] 5.912195
$AUC
[1] 1108.975
$MGT
[1] 6.632252
$Skewness
[1] 1.098973
$msg
[1] "#1. Relative error in the sum of squares is at most 'ftol'."
$isConv
[1] TRUE
attr(,"class")
[1] "FourPHFfit"
# From cumulative germination counts
FourPHFfit(germ.counts = y, intervals = int, total.seeds = 50, tmax = 20,
partial = FALSE)
```

\$data

gp csgp intervals

```
0
        0
                  1
2
   0
        0
                  2
3
   0
        0
                  3
4
   0
        0
                  4
5
   8
                 5
        8
6 34
       42
                 6
7 20
       62
                 7
       76
8 14
                 8
9
   2
       78
                 9
10 0
       78
                 10
11
  2
       80
                 11
12 0
       80
                 12
13 0
       80
                 13
14 0
       80
                 14
```

\$Parameters

```
term estimate std.error statistic p.value
1 a 80.000000 1.2415867 64.43368 1.973252e-14
2 b 9.881927 0.7077918 13.96163 6.952270e-08
3 c 6.034953 0.0495266 121.85275 3.399437e-17
4 y0 0.000000 0.9160705 0.00000 1.000000e+00
```

\$Fit

sigma isConv finTol logLik AIC BIC deviance df.residual 1 1.769385 TRUE 1.490116e-08 -25.49868 60.99736 64.19265 31.30723 10

\$a

[1] 80

\$ъ

[1] 9.881927

\$с

[1] 6.034953

\$y0

[1] 0

\$lag

[1] 0

\$Dlag50

[1] 6.034953

\$t50.total

[1] 6.355121

\$txp.total

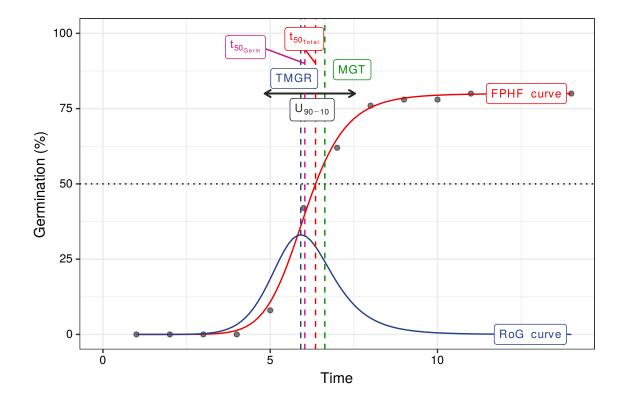
10 60

4.956263 6.744599

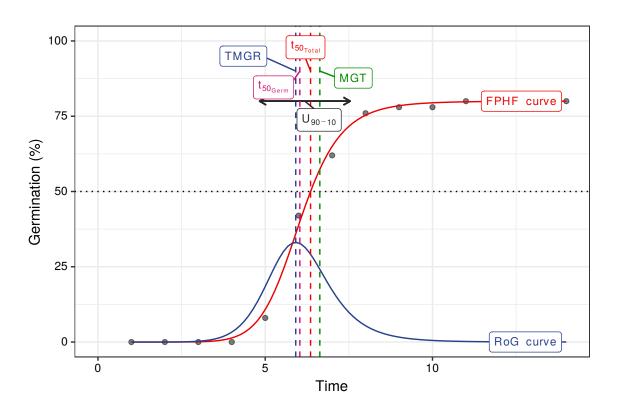
\$t50.Germinated

[1] 6.034953

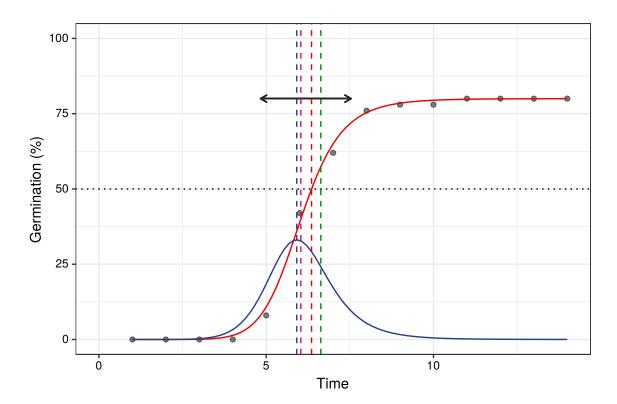
```
$txp.Germinated
     10
         60
4.831806 6.287723
$Uniformity
   90
              10 uniformity
 7.537691 4.831806 2.705885
$TMGR
[1] 5.912194
$AUC
[1] 1108.976
$MGT
[1] 6.632252
$Skewness
[1] 1.098973
$msg
[1] "#1. Relative error in the sum of squares is at most 'ftol'. "
$isConv
[1] TRUE
attr(,"class")
[1] "FourPHFfit"
## No test:
x \leftarrow c(0, 0, 0, 0, 4, 17, 10, 7, 1, 0, 1, 0, 0, 0)
y \leftarrow c(0, 0, 0, 0, 4, 21, 31, 38, 39, 39, 40, 40, 40, 40)
int <- 1:length(x)</pre>
total.seeds = 50
# From partial germination counts
fit1 <- FourPHFfit(germ.counts = x, intervals = int,</pre>
                 total.seeds = 50, tmax = 20)
# From cumulative germination counts
#-----
fit2 <- FourPHFfit(germ.counts = y, intervals = int,</pre>
                 total.seeds = 50, tmax = 20, partial = FALSE)
# Default plots
plot(fit1)
```



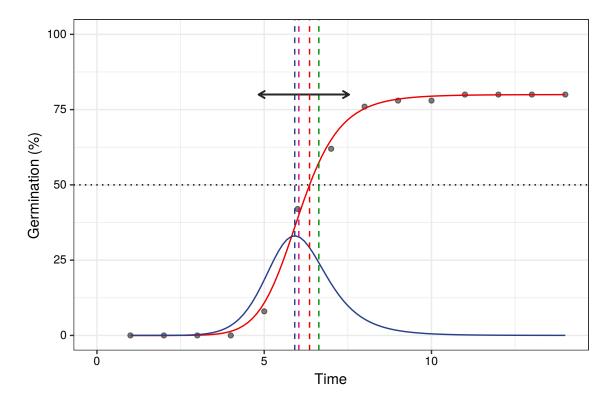
plot(fit2)



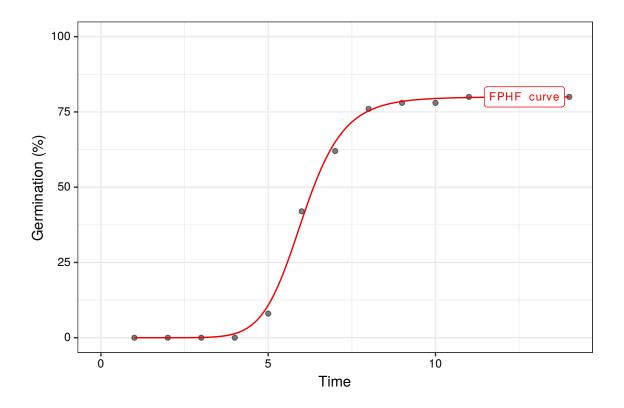
No labels plot(fit1, plotlabels = FALSE)



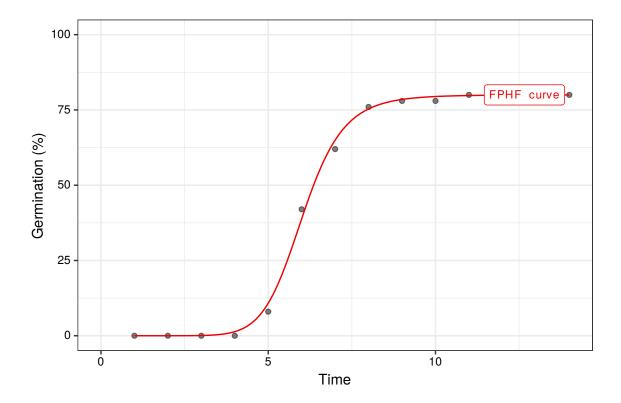
plot(fit2, plotlabels = FALSE)



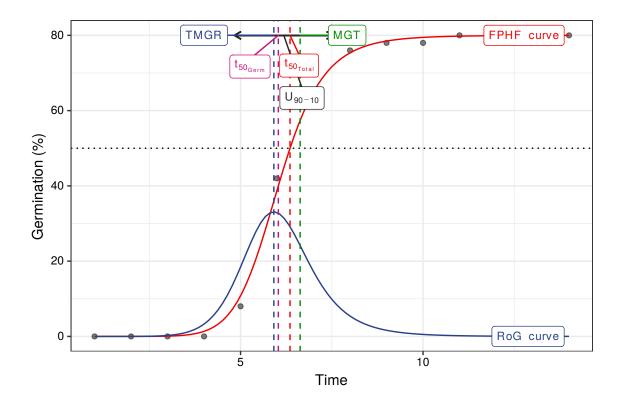
```
# Only the FPHF curve
plot(fit1, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
    tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```



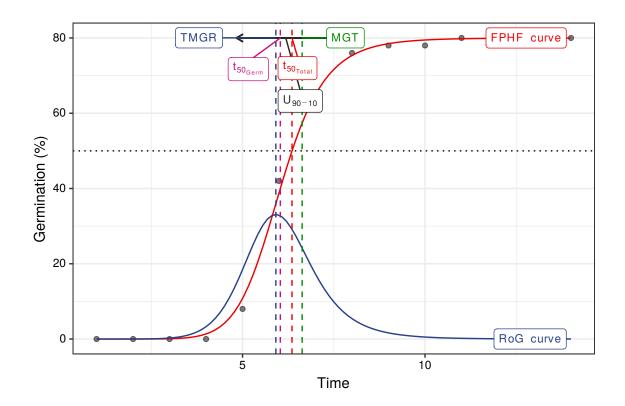
```
plot(fit2, rog = FALSE, t50.total = FALSE, t50.germ = FALSE,
    tmgr = FALSE, mgt = FALSE, uniformity = FALSE)
```



Without y axis limits adjustment
plot(fit1, limits = FALSE)



plot(fit2, limits = FALSE)



```
## End(No test)
```

Wrapper functions

Wrapper functions germination.indices() and FourPHFfit.bulk() are available in the package for computing results for multiple samples in batch from a data frame of germination counts recorded at specific time intervals.

germination.indices() This wrapper function can be used to compute several germination indices simultaneously for multiple samples in batch.

	Genotype	Rep	Day01	Day02	Day03	Day04	Day05	Day06	Day07	Day08	Day09	Day10	Day11	Day12	Day13	Day14	Tot
1	G1	1	0	0	0	0	4	17	10	7	1	0	1	0	0	0	
2	G2	1	0	0	0	1	3	15	13	6	2	1	0	1	0	0	
3	G3	1	0	0	0	2	3	18	9	8	2	1	1	1	0	0	
4	G4	1	0	0	0	0	4	19	12	6	2	1	1	1	0	0	
5	G5	1	0	0	0	0	5	20	12	8	1	0	0	1	1	0	
6	G1	2	0	0	0	0	3	21	11	7	1	1	1	1	0	0	
7	G2	2	0	0	0	0	4	18	11	7	1	0	1	0	0	0	
8	G3	2	0	0	0	1	3	14	12	6	2	1	0	1	0	0	
9	G4	2	0	0	0	1	3	19	10	8	1	1	1	1	0	0	
10	G5	2	0	0	0	0	4	18	13	6	2	1	0	1	0	0	
11	G1	3	0	0	0	0	5	21	11	8	1	0	0	1	1	0	
12	G2	3	0	0	0	0	3	20	10	7	1	1	1	1	0	0	
13	G3	3	0	0	0	0	4	19	12	8	1	1	0	1	1	0	
14	G4	3	0	0	0	0	3	21	11	6	1	0	1	1	0	0	
15	G5	3	0	0	0	0	4	17	10	8	1	1	1	0	0	0	

15	GD 3	0 0	0 0	4 17 10) 0	1 1 .	1 0 '	0
	${\tt LastGermTime}$	${\tt PeakGermTime}$	TimeSpreadGerm	t50_Coolbear	t50_Farooq	${\tt MeanGermTime}$	${\tt VarGermTime}$	${\tt SEGermTime}$
1	11	6	6	5.970588	5.941176	6.700000	1.446154	0.1901416
2	12	6	8	6.192308	6.153846	6.857143	2.027875	0.2197333
3	12	6	8	6.000000	5.972222	6.866667	2.572727	0.2391061
4	12	6	7	6.041667	6.000000	6.891304	2.187923	0.2180907
5	13	6	8	5.975000	5.950000	6.812500	2.368351	0.2221275
6	12	6	7	5.976190	5.952381	6.869565	2.071498	0.2122088
7	11	6	6	5.972222	5.944444	6.690476	1.389663	0.1818989
8	12	6	8	6.208333	6.166667	6.875000	2.112179	0.2297923
9	12	6	8	6.000000	5.973684	6.866667	2.300000	0.2260777
10	12	6	7	6.076923	6.038462	6.822222	1.831313	0.2017321
11	13	6	8	5.928571	5.904762	6.791667	2.381206	0.2227295
12	12	6	7	5.975000	5.950000	6.886364	2.149577	0.2210295
13	13	6	8	6.083333	6.041667	6.936170	2.539315	0.2324392

4.0	10	•	7	F 000F74	F 004760	c 770707	1 000	CO 1 A	0070270
14	12 11	6	7 6	5.928571	5.904762	6.772727	1.900		.2078370
15		6 Campatal		6.050000	6.000000	6.809524	1.670		.1994129
1	SEGermRate CVG 0.004235724 14.92537	Germate	Recip_Coolbear 0.1674877	Germnatene	0.1683168	6.1389		_	.27785
_						6.3626			
2	0.004673148 14.58333		0.1614907		0.1625000				.47588
3	0.005071059 14.56311		0.1666667		0.1674419	6.8821			.33787
4	0.004592342 14.51104		0.1655172		0.1666667	6.9274			.58317
5	0.004786184 14.67890		0.1673640		0.1680672	7.3189			.63797
6	0.004496813 14.55696		0.1673307		0.1680000	6.9317			.14649
7	0.004063648 14.94662		0.1674419		0.1682243	6.4484			.43427
8	0.004861721 14.54545		0.1610738		0.1621622	6.0531			.87909
9	0.004794747 14.56311		0.1666667		0.1674009	6.8305			.13575
	0.004334343 14.65798		0.1645570		0.1656051	6.8126			.62540
	0.004828643 14.72393		0.1686747		0.1693548	7.3427	96	14	.39764
12	0.004660905 14.52145		0.1673640		0.1680672	6.6222	58	12	.98482
13	0.004831366 14.41718		0.1643836		0.1655172	7.0523	20	14	.39249
14	0.004531018 14.76510		0.1686747		0.1693548	6.7067	82	13	.97246
15	0.004300508 14.68531		0.1652893		0.1666667	6.3639	25	13	.25818
	GermSpeedAccumulated	_Percent (GermSpeedCorre	cted_Normal	GermSpeed(Corrected_Accu	mulated '	Weight	GermPerc
1	•	69.23134		0.07673656		0.	4326958		47.428
2		69.68741		0.07726134		0.	4315642		47.89
3	•	79.78594		0.07340991		0.	4085040		54.46
4		75.85202		0.07680397		0.	4288937		52.24
5	:	82.01571		0.07623944		0.	4271652		56.14
6		79.13509		0.07383855		0.	4130508		54.51
7		75.80304		0.07369656			4158338		51.93
8		71.85275		0.07112480			3968068		49.39
9		73.29829		0.07893128			4404413		50.27
10		76.39054		0.07569665			4243919		52.57
11		80.73436		0.07801721			4374793		55.18
12		72.56158		0.07675799			4289379		50.000
13		80.19182		0.07352419			4096608		55.24
14		78.53103		0.07316490			4112171		53.86
15		74.36868		0.07310430			4079653		51.19
13	TimsonsIndex Timsons		ouriou Timaona		ngar CarmPr			rm Tndo	-
1	8.000000	Index_Lab	1.00	0.571	-	_	111dex Ge. 40000		x_mod Em
2	9.803922		1.25	0.700			82353		42857
_									
3	14.583333		1.40	1.041			87500 11765		33333
4	7.843137		1.00 1.00	0.560			11765		08696
5	10.000000			0.714			00000		87500
6	6.122449		1.00	0.437			93878		30435
7	8.333333		1.00	0.595			95833		09524
8	10.638298		1.25	0.759			63830		25000
9	9.615385		1.25	0.686			73077		33333
10	8.000000		1.00	0.571			60000		77778
11	9.803922		1.00	0.700			84314		08333
12	5.882353		1.00	0.420			37255		13636
13	8.163265		1.00	0.583			75510		63830
14	6.250000		1.00	0.446			25000		27273
15	8.333333		1.00	0.595			91667		90476
	<pre>EmergenceRateIndex_Me</pre>		_	teIndex_Bil	_	EmergenceRate			
1		7.3000			5.970149			375000	
2		7.1428			6.125000			326531	9.3137
2		7 1333	33		6 553308		7	301111	10 /1166

6.553398

7.324444 10.4166

7.133333

3

```
4
                           7.108696
                                                             6.675079
                                                                                           7.640359 10.0490
5
                           7.187500
                                                             7.045872
                                                                                           7.096354 11.2500
                                                                                           7.317580 10.7142
6
                           7.130435
                                                             6.696203
7
                                                                                           7.646259 10.4166
                           7.309524
                                                             6.277580
8
                           7.125000
                                                             5.818182
                                                                                           8.078125 9.5744
9
                           7.133333
                                                             6.553398
                                                                                           7.934815 9.8557
10
                           7.177778
                                                             6.596091
                                                                                           7.580247 10.2500
11
                           7.208333
                                                             7.067485
                                                                                           7.216146 11.0294
12
                           7.113636
                                                             6.389439
                                                                                           7.981921 9.8039
13
                           7.063830
                                                             6.776074
                                                                                           7.231326 10.9693
14
                           7.227273
                                                             6.496644
                                                                                           7.388430 10.6770
15
                           7.190476
                                                             6.167832
                                                                                           7.782313 10.1562
   GermValue_Czabator_mod GermValue_DP_mod
                                                CUGerm GermSynchrony GermUncertainty
1
                 54.28571
                                   39.56076 0.7092199
                                                           0.2666667
                                                                             2.062987
2
                                   40.99260 0.5051546
                 54.78662
                                                           0.2346109
                                                                             2.321514
3
                 69.75446
                                   53.42809 0.3975265
                                                           0.2242424
                                                                             2.462012
4
                 64.74158
                                   48.86825 0.4672113
                                                           0.2502415
                                                                             2.279215
5
                 77.14286
                                   56.23935 0.4312184
                                                           0.2606383
                                                                             2.146051
6
                 71.84506
                                   53.06435 0.4934701
                                                           0.2792271
                                                                             2.160545
7
                 65.10417
                                   47.37690 0.7371500
                                                           0.2729384
                                                                             2.040796
8
                 58.20345
                                   43.67948 0.4855842
                                                           0.2256410
                                                                             2.357249
9
                 60.92165
                                   45.30801 0.4446640
                                                           0.2494949
                                                                             2.321080
                                   49.10820 0.5584666
10
                 65.89286
                                                           0.255556
                                                                             2.187983
                                   54.27520 0.4288905
11
                 74.14731
                                                           0.2686170
                                                                             2.128670
12
                 60.41632
                                   44.71582 0.4760266
                                                           0.2737844
                                                                             2.185245
13
                 75.15470
                                   54.94192 0.4023679
                                                           0.2506938
                                                                             2.241181
14
                 69.90947
                                   51.41913 0.5383760
                                                           0.2991543
                                                                             2.037680
15
                 63.47656
                                   46.48043 0.6133519
                                                           0.2497096
                                                                             2.185028
## End(No test)
```

FourPHFfit.bulk() This wrapper function can be used to fit the four-parameter hill function for multiple samples in batch.

```
Genotype Rep Day01 Day02 Day03 Day04 Day05 Day06 Day07 Day08 Day09 Day10 Day11 Day12 Day13 Day14 To
                                                                                                     0
1:
          G1
                1
                       0
                              0
                                     0
                                            0
                                                   4
                                                         17
                                                                10
                                                                        7
                                                                               1
                                                                                       0
                                                                                              1
                                                                                                            0
                                                                                                                   0
2:
          G2
                1
                       0
                              0
                                     0
                                            1
                                                   3
                                                         15
                                                                13
                                                                         6
                                                                               2
                                                                                       1
                                                                                              0
                                                                                                     1
                                                                                                            0
                                                                                                                   0
                                            2
                                                   3
                                                                                                            0
                                                                                                                   0
3:
          G3
                1
                       0
                              0
                                     0
                                                         18
                                                                 9
                                                                        8
                                                                               2
                                                                                       1
                                                                                              1
                                                                                                     1
          G4
                       0
                              0
                                     0
                                            0
                                                   4
                                                         19
                                                                12
                                                                         6
                                                                               2
                                                                                       1
                                                                                              1
                                                                                                     1
                                                                                                            0
                                                                                                                   0
4:
                1
                                            0
                                                   5
                                                         20
                                                                                                                   0
5:
          G5
                       0
                              0
                                     0
                                                                12
                                                                        8
                                                                                       0
                                                                                              0
                                                                                                     1
                                                                                                            1
                1
                                                                               1
```

```
6:
          G1
               2
                            0
                                         0
                                               3
                                                    21
                                                                                                        0
                                                           11
                                                                               1
7:
          G2
               2
                                         0
                                               4
                                                    18
                                                                  7
                                                                               0
                                                                                     1
                                                                                           0
                      0
                            0
                                  0
                                                           11
                                                                        1
                                                                                                  0
                                                                                                        0
8:
          G3
               2
                                               3
                                                           12
                                                           10
9:
          G4
               2
                            0
                                  0
                                               3
                                                    19
                                                                  8
                                                                                                  0
                                                                                                        0
                      0
                                         1
                                                                        1
                                                                               1
                                                                                     1
10:
          G5
               2
                      0
                            0
                                  0
                                         0
                                               4
                                                    18
                                                           13
                                                                  6
                                                                        2
                                                                               1
                                                                                                  0
                                                                                                        0
               3
                                  0
                                         0
                                               5
                                                                               0
11:
          G1
                      0
                            0
                                                    21
                                                           11
                                                                  8
                                                                        1
                                                                                     0
                                                                                                  1
                                                                                                        0
               3
                                         0
                                               3
12:
          G2
                      0
                            0
                                  0
                                                    20
                                                           10
                                                                  7
                                                                        1
                                                                               1
                                                                                                        0
13:
          G3
               3
                      0
                            0
                                  0
                                         0
                                               4
                                                    19
                                                           12
                                                                  8
                                                                        1
                                                                               1
                                                                                     0
                                                                                           1
                                                                                                  1
                                                                                                        0
14:
          G4
               3
                      0
                            0
                                  0
                                         0
                                               3
                                                    21
                                                           11
                                                                  6
                                                                        1
                                                                               0
                                                                                     1
                                                                                           1
                                                                                                  0
                                                                                                        0
               3
                      0
                                  0
                                         0
                                                                                                  0
                                                                                                        0
15:
          G5
                            0
                                                    17
                                                           10
                                                                  8
                                                                        1
                                                                               1
    y0 lag
             Dlag50 t50.total t50.Germinated
                                                   TMGR
                                                              AUC
                                                                       MGT Skewness
 1:
         0 6.034954
                      6.355122
                                     6.034954 5.912195 1108.975 6.632252 1.098973
 2:
    0
         0 6.175193
                      6.473490
                                     6.175193 6.031282 1128.559 6.784407 1.098655
                                     6.138110 5.938179 1283.693 6.772742 1.103392
 3:
    0
         0 6.138110
                      6.244190
         0 6.125172
                      6.276793
                                     6.125172 5.972686 1239.887 6.739665 1.100323
 4:
    0
 5:
     0
         0 6.049641
                      6.103433
                                     6.049641 5.914289 1328.328 6.654980 1.100062
         0 6.097412
                                     6.097412 5.961877 1294.463 6.702470 1.099232
 6:
    0
                      6.182276
7:
         0 6.029851
                      6.202812
                                     6.029851 5.914057 1213.908 6.622417 1.098272
         0 6.189774
                      6.439510
                                     6.189774 6.036193 1164.346 6.804000 1.099232
8:
    0
                                     6.125121 5.961631 1188.793 6.745241 1.101242
9:
    0
         0 6.125121
                      6.352172
10:
    Ω
         0 6.109503
                      6.253042
                                     6.109503 5.978115 1240.227 6.711899 1.098600
11:
         0 6.018759
                      6.099434
                                     6.018759 5.883558 1305.200 6.624247 1.100600
12:
         0 6.108449
                                     6.108449 5.964079 1188.021 6.718636 1.099892
    0
                      6.326181
         0 6.149011
                      6.207500
                                     6.149011 5.998270 1316.407 6.762272 1.099733
13:
                                     6.015907 5.905179 1273.386 6.604963 1.097916
14: 0
         0 6.015907
                      6.122385
15: 0
         0 6.121580
                     6.317392
                                     6.121580 5.976088 1203.664 6.732267 1.099760
                                                                msg isConv txp.total_10 txp.total_60 Unifor
1: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.956266
                                                                                             6.744598
2: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.983236
                                                                                             6.872603
3: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.673022
                                                                                             6.608437
4: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.850876
                                                                                             6.614967
5: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.814126
                                                                                             6.386788
6: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.868635
                                                                                             6.477594
                                                                      TRUE
7: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                                4.930423
                                                                                             6.510495
8: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.940058
                                                                                             6.823299
                                                                      TRUE
9: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                                4.836659
                                                                                             6.733275
10: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.920629
                                                                                             6.566505
11: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                             6.391288
                                                                                4.798630
12: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.893597
                                                                                             6.684521
13: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.841310
                                                                                             6.509952
14: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.915143
                                                                                             6.397486
15: #1. Relative error in the sum of squares is at most 'ftol'.
                                                                      TRUE
                                                                                4.892505
                                                                                             6.667247
```

End(No test)

Citing germinationmetrics

To cite the R package 'germinationmetrics' in publications use:

Aravind, J., Vimala Devi, S., Radhamani, J., Jacob, S. R., and Kalyani Srinivasan (2020). germination Germination Indices and Curve Fitting. R package version 0.1.4,

https://github.com/aravind-j/germinationmetricshttps://cran.r-project.org/package=germinationmetrics.

```
A BibTeX entry for LaTeX users is

@Manual{,
   title = {germinationmetrics: Seed Germination Indices and Curve Fitting},
   author = {J. Aravind and S. {Vimala Devi} and J. Radhamani and Sherry Rachel Jacob and {Kalyani Sri:
    year = {2020},
   note = {R package version 0.1.4},
   note = {https://github.com/aravind-j/germinationmetrics},
   note = {https://cran.r-project.org/package=germinationmetrics},
```

This free and open-source software implements academic research by the authors and co-workers. If you use the project by citing the package.

Session Info

}

```
sessionInfo()
R version 4.0.1 (2020-06-06)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 18.04.4 LTS
Matrix products: default
       /usr/lib/x86_64-linux-gnu/atlas/libblas.so.3.10.3
LAPACK: /usr/lib/x86_64-linux-gnu/atlas/liblapack.so.3.10.3
locale:
 [1] LC_CTYPE=en_US.UTF-8
                                LC_NUMERIC=C
                                                           LC_TIME=en_IN.UTF-8
                                                                                       LC_COLLATE=en_US.
 [6] LC_MESSAGES=en_US.UTF-8
                                LC_PAPER=en_IN.UTF-8
                                                           LC_NAME=C
                                                                                       LC_ADDRESS=C
[11] LC_MEASUREMENT=en_IN.UTF-8 LC_IDENTIFICATION=C
attached base packages:
[1] stats
              graphics grDevices utils
                                            datasets methods
other attached packages:
[1] germinationmetrics_0.1.4
1
```

loaded via a namespace	<pre>(and not attached):</pre>				
[1] whoami_1.3.0	$nlme_3.1-147$	bitops_1.0-6	fs_1.4.1	xopen_1.0.0	use
[8] covr_3.5.0	httr_1.4.1	rprojroot_1.3-2	hunspell_3.0	tools_4.0.1	bacl
[15] lazyeval_0.2.2	colorspace_1.4-1	withr_2.2.0	tidyselect_1.1.0	<pre>prettyunits_1.1.1</pre>	pro
[22] compiler_4.0.1	cli_2.0.2	xml2_1.3.2	desc_1.2.0	labeling_0.3	sca:
[29] goodpractice_1.0.2	pkgdown_1.5.1	stringr_1.4.0	digest_0.6.25	rmarkdown_2.2	lin [.]
[36] htmltools_0.4.0	bibtex_0.4.2.2	sessioninfo_1.1.1	highr_0.8	rlang_0.4.6	rstı
[43] farver_2.0.3	jsonlite_1.6.1	dplyr_1.0.0	RCurl_1.98-1.2	magrittr_1.5	Rcpj
[50] fansi_0.4.1	lifecycle_0.2.0	stringi_1.4.6	yaml_2.2.1	mathjaxr_0.8-3	gbRo
[57] pkgbuild_1.0.8	plyr_1.8.6	grid_4.0.1	ggrepel_0.8.2	crayon_1.3.4	lat
[64] knitr_1.28	ps_1.3.3	pillar_1.4.4	clisymbols_1.2.0	pkgload_1.1.0	XML
[71] packrat_0.5.0	praise_1.0.0	evaluate_0.14	rex_1.2.0	data.table_1.12.8	reme
[78] Rdpack_0.11-1	testthat_2.3.2	gtable_0.3.0	purrr_0.3.4	rcmdcheck_1.3.3	tid
[85] ggplot2_3.3.1	xfun_0.14	broom_0.5.6	roxygen2_7.1.0	cyclocomp_1.1.0	minj

[92] memoise_1.1.0 ellipsis_0.3.1 xmlparsedata_1.0.3

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