

Assignment9

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Q.The probability that a K-digit number does not contain the digits 0,5 or 9 is?:

- a) $.3^k$ b) $.6^k$ c) $.7^k$ d) $.9^k$

Solution:Let $Z_i \in (0,1,2,3,4,5,6,7,8,9)$ represents the i^{th} position of k digit number

$$Pr(Z_i \notin 0, 5, 9) = \frac{7}{10}$$

If a K-digit number does not contain 0,5,9 it can be written as

$$Pr(Z_1 \notin 0, 5, 9, Z_2 \notin 0, 5, 9, Z_3 \notin 0, 5, 9, \dots, Z_k \notin 0, 5, 9)$$

Since getting digit in different places of a number is a independent event it can be written as

$$\begin{aligned} &= Pr(Z_1 \notin 0, 5, 9, Z_2 \notin 0, 5, 9, Z_3 \notin 0, 5, 9, \dots, Z_k \notin 0, 5, 9) \\ &= Pr(Z_1 \notin 0, 5, 9) \times Pr(Z_2 \notin 0, 5, 9) \times Pr(Z_3 \notin 0, 5, 9) \times \dots \times Pr(Z_k \notin 0, 5, 9) \end{aligned}$$

$$\begin{aligned} &= \prod_{i=1}^k .7 \\ &= .7^k \end{aligned}$$

So, Answer is option C

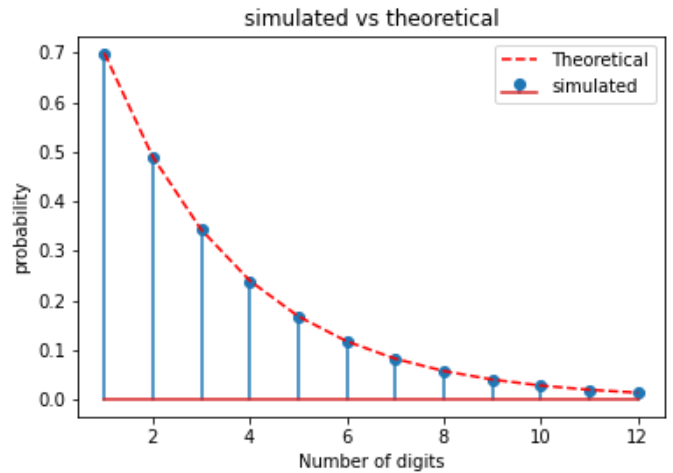


Figure 1: theoretical vs simulated