

5) a) (S (WNP (WDT What)
 (NN courses))
 (VP (BE are)
 (VP (VBN offered)
 (PP (IN in)
 (NN fall))))))

~~(S (WNP who)
 (VP (VBN offered)
 (NP (~~

(S (WNP who)
 (VP (VBZ teaches)
 (NP (NN CSCE)
 (NN 1100))))

CFG induced from parse tree

Parse tree \Rightarrow

S \rightarrow WNP VP
 WNP \rightarrow WDT NN
 WDT \rightarrow what
 NN \rightarrow courses

VP \rightarrow BE VP
 BE \rightarrow are
 VP \rightarrow VBN PP
 VBN \rightarrow offered

PP \rightarrow IN NN

IN \rightarrow in

NN \rightarrow Fall

Second \Rightarrow
tree

VP \rightarrow VBZ NP

WNP \rightarrow who

VBZ \rightarrow teaches

(not
including
ones in first)

NP \rightarrow NN NN

NN \rightarrow CSCI

NN \rightarrow 1100

CFA with probabilities

S \rightarrow WNP VP / 1

PP \rightarrow IN NN / 1

WNP \rightarrow WDT NN / 0.5

IN \rightarrow in / 1

WNP \rightarrow who / 0.5

VBZ \rightarrow teaches / 1

WDT \rightarrow what / 1

NP \rightarrow NN NN / 1

NN \rightarrow courses / 0.25

NN \rightarrow Fall / 0.25

NN \rightarrow CSCI / 0.25

NN \rightarrow 1100 / 0.25

VP \rightarrow BE VP / 0.33

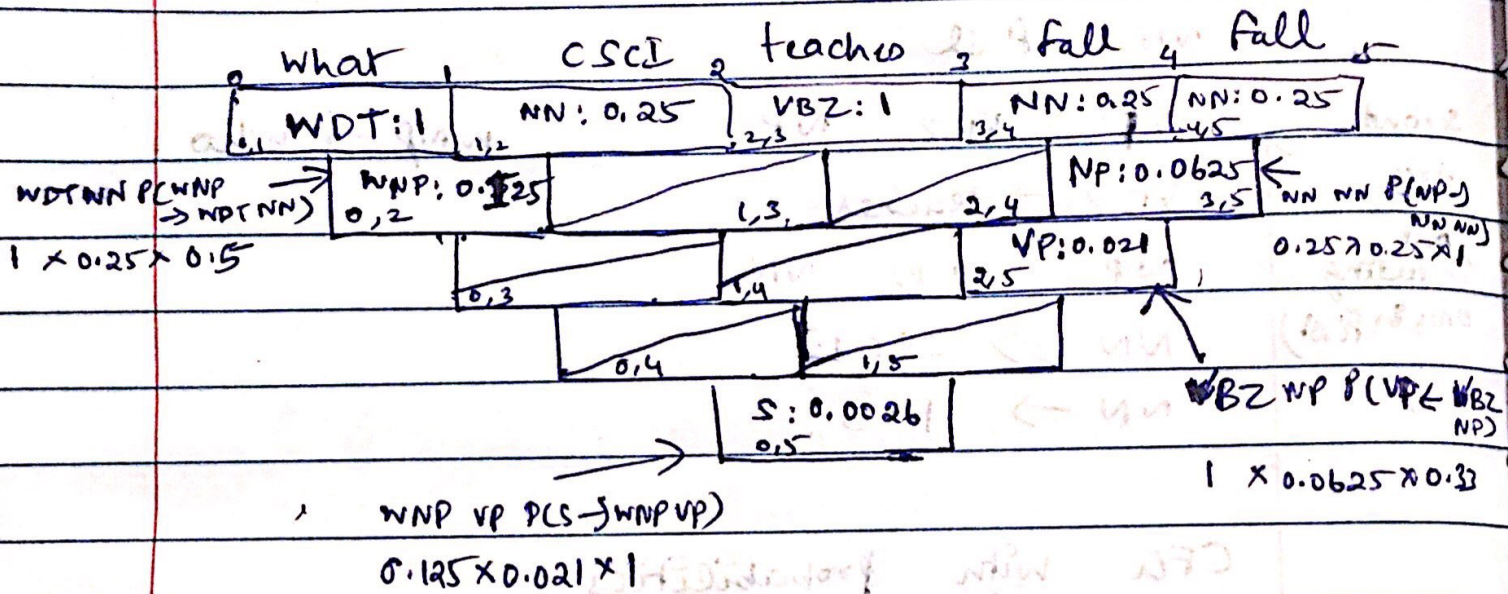
VP \rightarrow VBN PP / 0.33

VP \rightarrow VBZ NP / 0.33

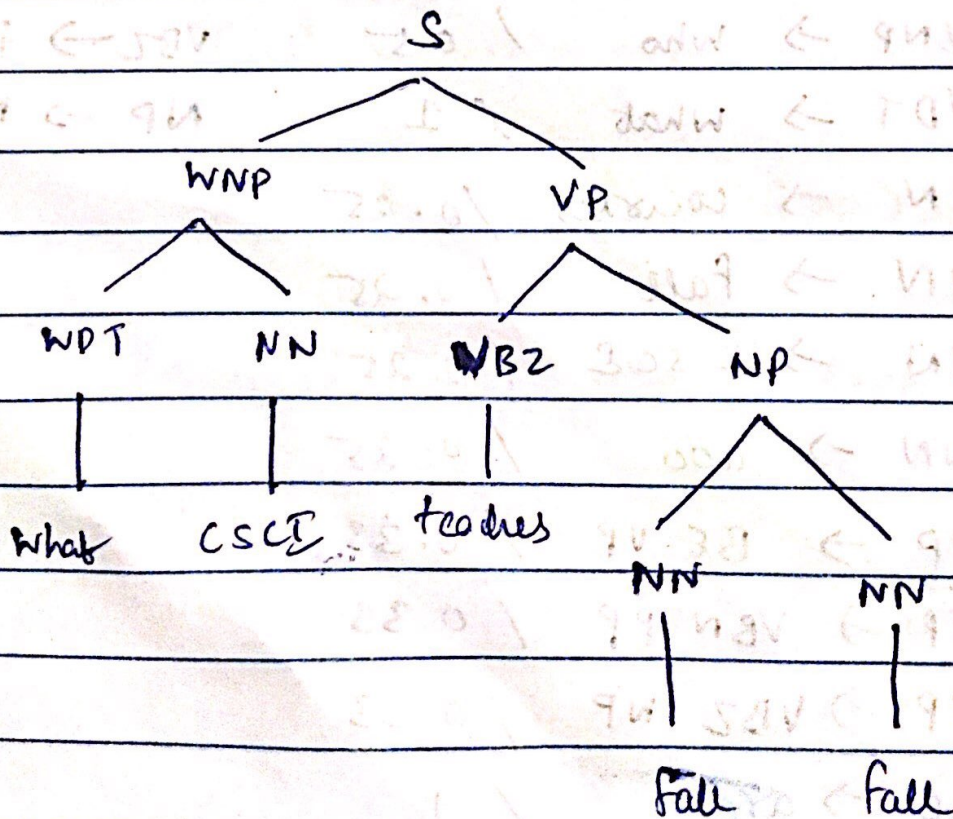
BE \rightarrow are / 1

VBN \rightarrow offered / 1

5)b) CYK Parsing without probabilities.



5)c) Final parse tree.



$$\begin{aligned}
 P(\text{free}) &= P(S \rightarrow WNP \text{ VP}) \\
 &\quad P(WNP \rightarrow WDT \text{ NN}) P(WDT \rightarrow \text{who}) \\
 &\quad P(NN \rightarrow \text{CSCD}) P(VP \rightarrow \text{VBZ} \text{ NP}) \\
 &\quad P(\text{VBZ} \rightarrow \text{teaches}) P(NP \rightarrow \text{NN NN}) \\
 &\quad P(\text{NN} \rightarrow \text{fall}) P(\text{NN} \rightarrow \text{fall}) \\
 &= 1 \times 0.5 \times 1 \times 0.25 \times 0.33 \times 1 \times 1 \\
 &\quad \times 0.25 \times 0.25 \\
 &= \underline{0.0026}
 \end{aligned}$$