

# GATE-2023 CRASH COURSE



GENERAL APTITUDE

# NUMBERS



Lecture No.15

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# NUMBER (VARIOUS CALCULATIONS)



$$\frac{0}{9} = 0 \quad \checkmark$$

$$\frac{15}{3} = 5 \quad \checkmark$$

$$\frac{8}{0} = \text{undefined}$$

$$9 \overline{)000} \quad 3 \overline{)15} \quad 5 \quad \checkmark$$

$$\frac{16}{2} = 8 \quad \checkmark$$

$$2 \overline{)16} \quad 8 \quad \checkmark$$

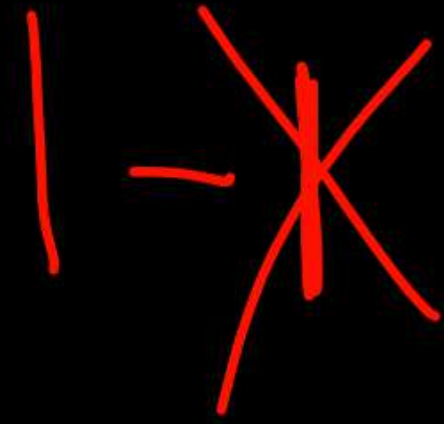
$$0 \overline{)8}$$





# Basic

- Natural Number ✓ 1, 2, 3, 4, ...  $\infty$
- Whole Number ✓ 0, 1, 2, 3, ...  $\infty$
- Even Number
- ODD Number
- Integers
- Prime Numbers Number
- Composite Numbers {Non-Prime}
- Rational & Irrational





factor

~~1~~ ~~1~~  
1-1

Multiples

6  $\rightarrow$  1, 2, 3, 6

6  $\rightarrow$  6, 12, 18, 24, 30, 36, 42, 48, 54, 60, 66  
72, 78, 84, 90, 96, 102, 108, ...  $\infty$



Rational

$$42.\overline{4} = \frac{382}{9}$$

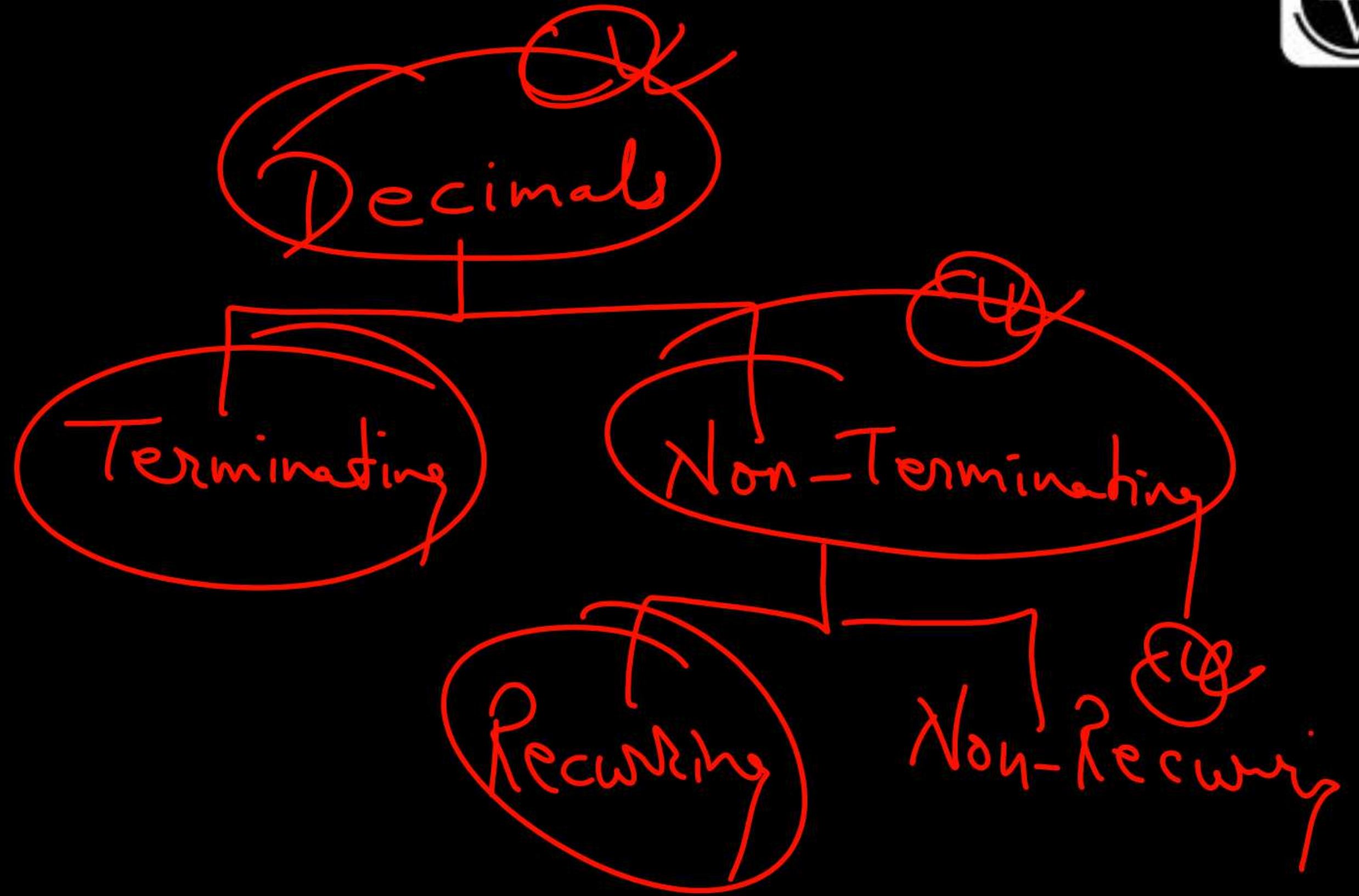
$$3 = \frac{3}{1}$$

$$-8 = \frac{-8}{1}$$

$$3.8 = \frac{38}{10}$$

$$0 = \frac{0}{1}$$







Irrational

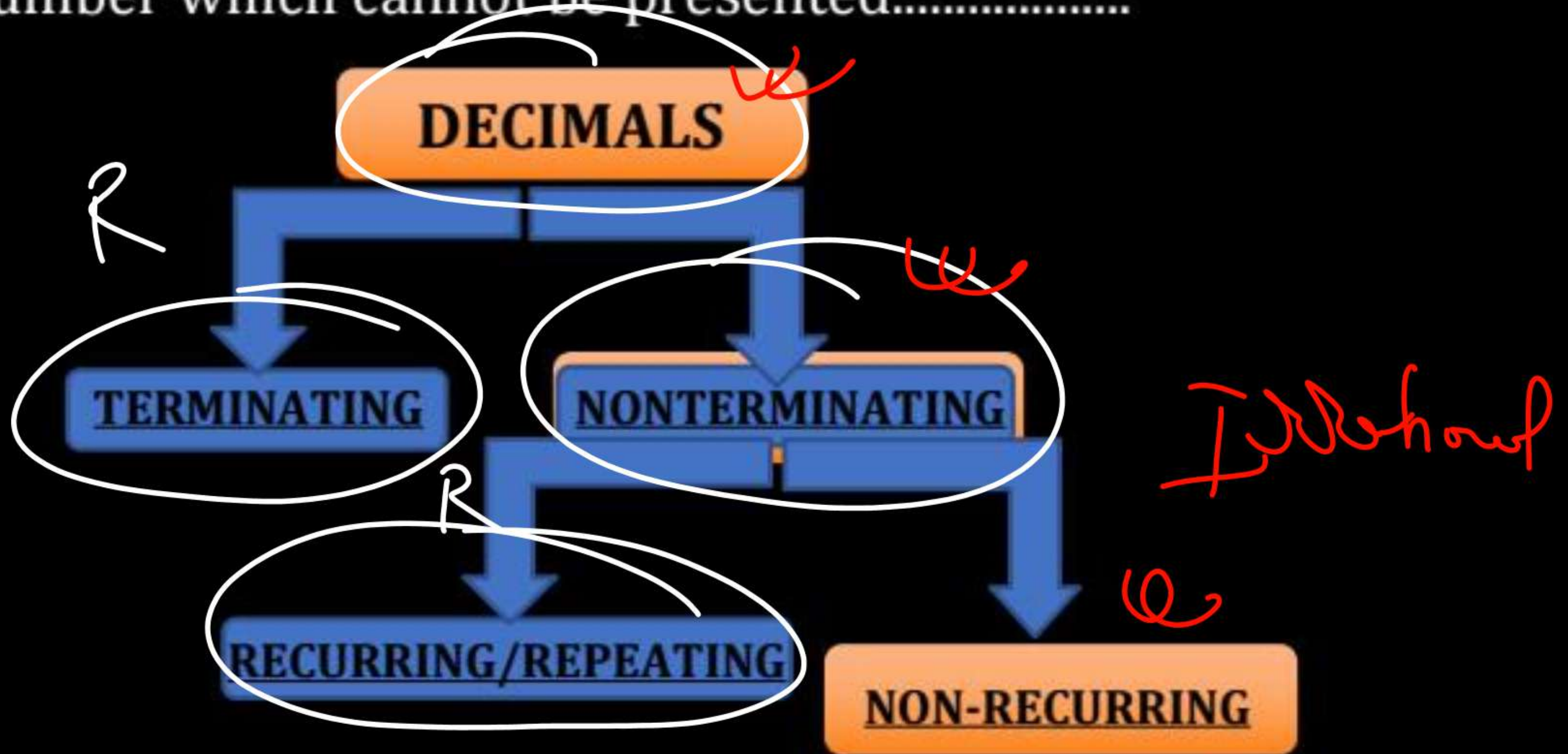
$\sqrt{2}$

1.41421356259797349

28 - - - - -

# IRRATIONAL

- A number which cannot be presented.....







$\pi$  Irrational



Rational

$$\frac{22}{7} \text{ OR } 3.14$$

$$7 \overline{) 22} (3.1428571$$

$$\begin{array}{r} 60 \\ 56 \\ \hline 40 \\ 35 \\ \hline 50 \\ 49 \\ \hline 10 \end{array}$$

$$\begin{array}{r} 10 \\ 7 \\ \hline 30 \\ 28 \\ \hline 20 \\ 14 \end{array}$$

# IRRATIONAL $\sqrt{2}$



$$= 1.414213562373095\dots$$

Square root, Cube root

{Cannot be found perfectly}

$\pi$

*Rational*

$$\frac{22}{7} = 3.\underline{142857}\underline{142857}\dots$$

*For*

$$\underline{\Pi = 3.14159265358979\dots \text{ {approx.}}}$$



# Brainstorming: 1

$$\underbrace{1 - 2}_{-1} + \underbrace{3 - 4}_{-1} + 5 \dots \dots \dots \underline{2022} = ?$$

$-1$

$-1011$



# Brainstorming: 2



$$\underline{1! + 2! + 3! + \dots + 2022!} = \underline{\underline{\text{Ans}}}$$

120 ✓  
x 6  
720  
x 7  
5040

$$\begin{aligned} 1! &= 1 \\ 2! &= 2 \\ 3! &= 6 \\ 4! &= 24 \end{aligned}$$

3) Ans  
R = ?  
5! = 120

11 3 11  
1 1  
2 2  
3 0  
4) (can it be done)

# Brainstorming: 3



How many zeroes would be at the end in the answer of  $100!$ ?

$$25 = 5 \times 5$$

$$25 \times 2$$

$$25 \times 3$$

$$25 \times 4$$

$$1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \dots 100$$

$$1-10 \rightarrow 2$$

$$11-20 \rightarrow 2$$

$$21-30 \rightarrow 3$$

$$31-40 \rightarrow 2$$

$$41-50 \rightarrow 3$$

$$51-60 \rightarrow 2$$

$$61-70 \rightarrow 2$$

$$71-80 \rightarrow 3$$

$$81-90 \rightarrow 2$$

$$91-100 \rightarrow 3$$

24

$$\frac{100}{5} = 20$$

$$\frac{20}{5} = 4$$

$$\frac{4}{1} = 0$$

$$\hline 24$$





## Brainstorming: 4

50! can be denoted maximum 7?

10!

$$\frac{50}{7} = 7$$

$$50! \Rightarrow 7^8$$

$$\frac{7}{7} = 1$$

$$\frac{1}{7} = \frac{0}{8}$$



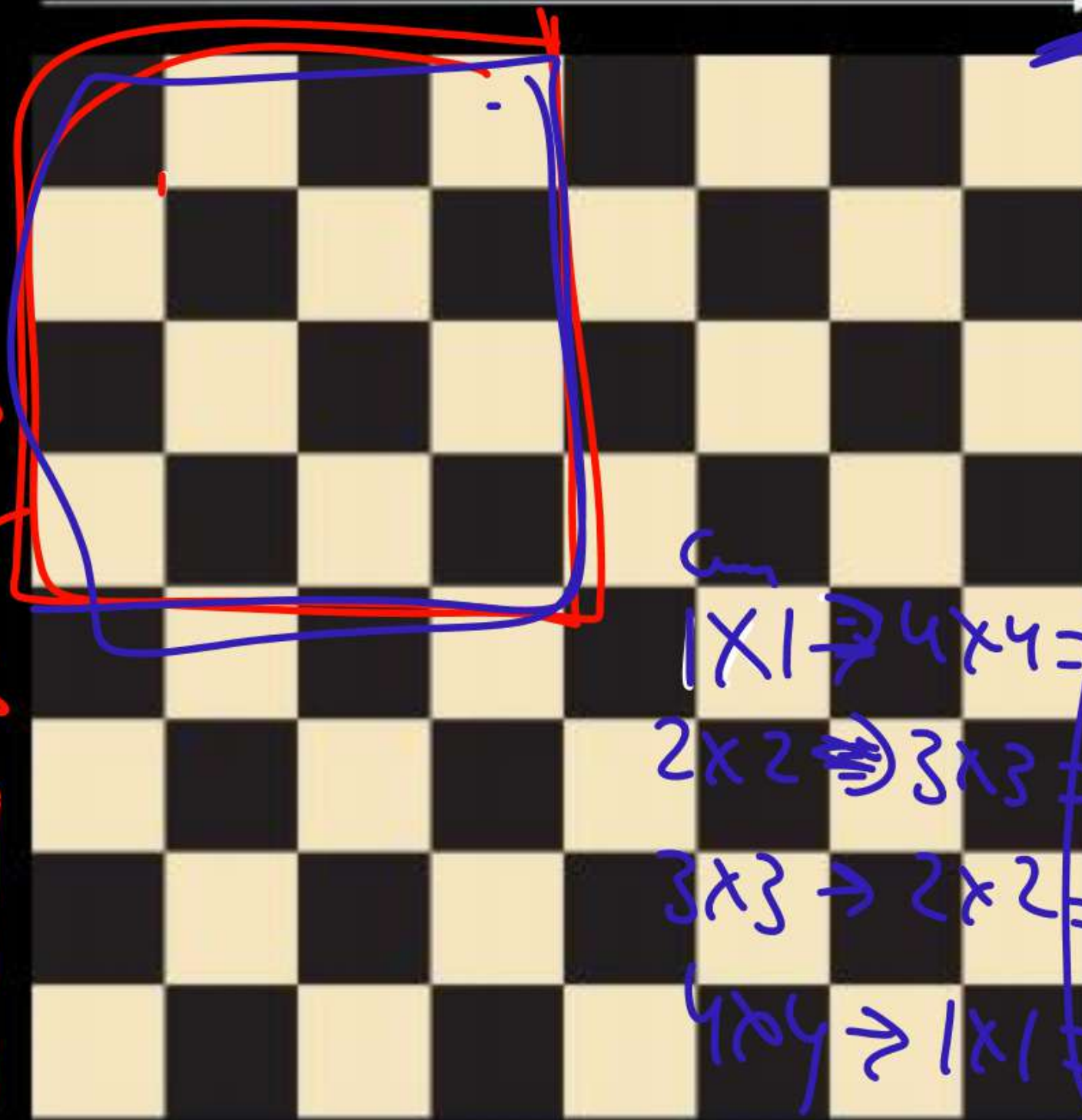
## Brainstorming: 5

How many squares are there in a chessboard ?

How many squares are there in a chessboard ?



Size	No
$1 \times 1$	$8 \times 8 = 64$
$2 \times 2$	$7 \times 7 = 49$
$3 \times 3$	$6 \times 6 = 36$
$4 \times 4$	$5 \times 5 = 25$
$5 \times 5$	$4 \times 4 = 16$
$6 \times 6$	$3 \times 3 = 9$
$7 \times 7$	$2 \times 2 = 4$
$8 \times 8$	$1 \times 1 = 1$



30  
... 8 CMS

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Can  
 $1 \times 1 \Rightarrow 4 \times 4 = 16$   
 $2 \times 2 \Rightarrow 3 \times 3 = 9$   
 $3 \times 3 \Rightarrow 2 \times 2 = 4$   
 $4 \times 4 \Rightarrow 1 \times 1 = 1$

~~8~~



