

GATE-2023 CRASH COURSE

GENERAL APTITUDE

CUBES

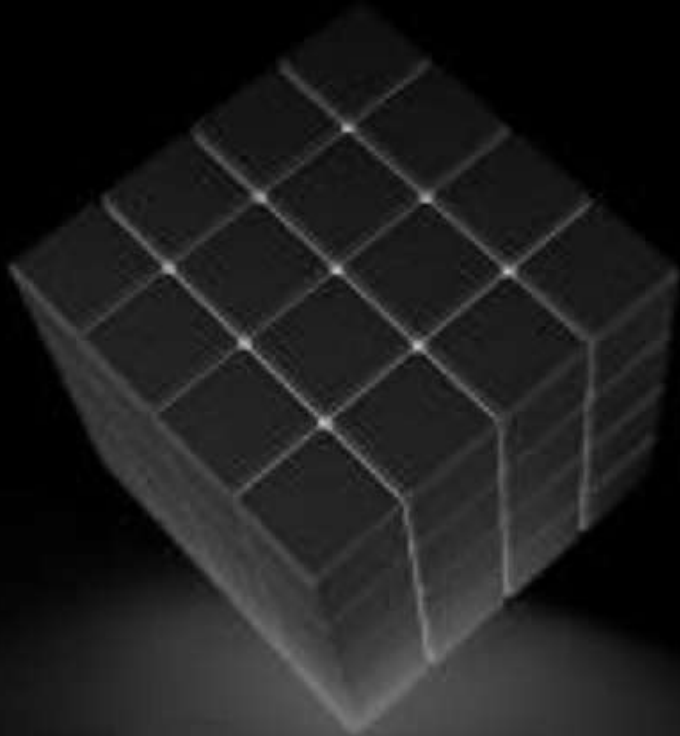
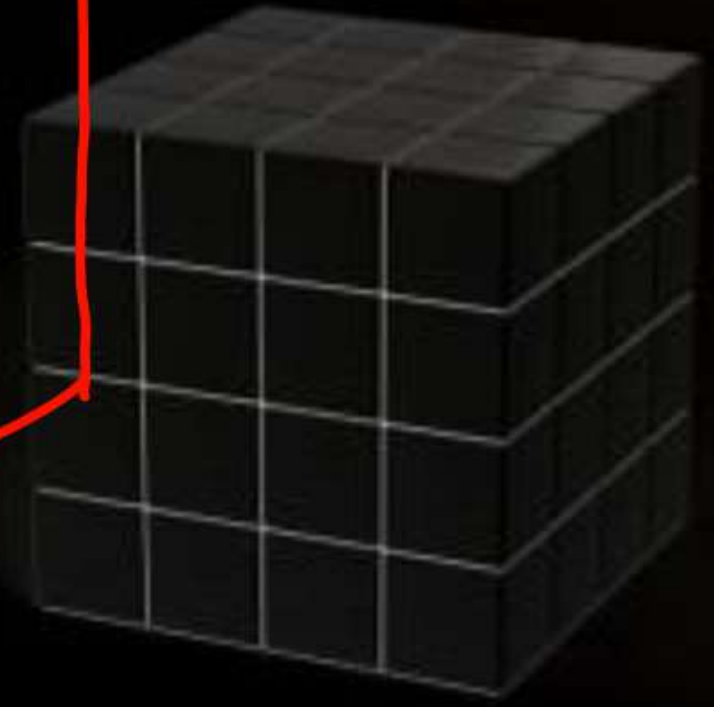
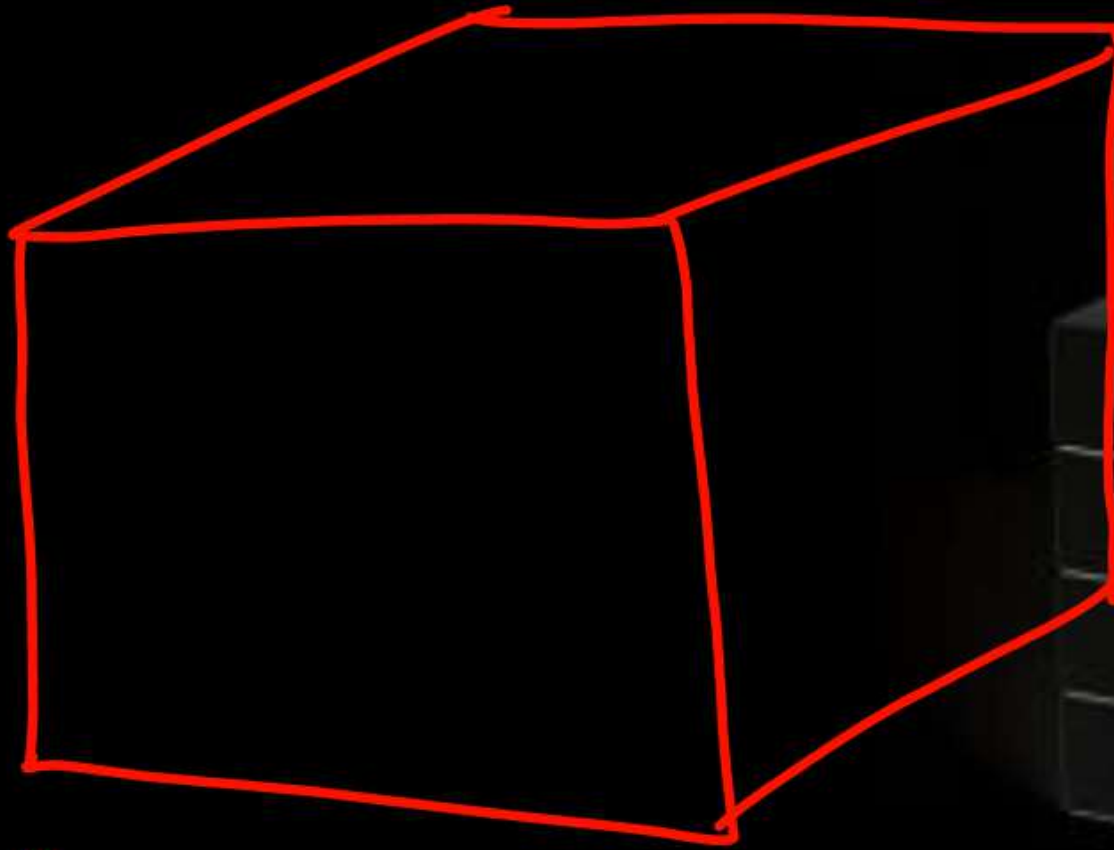
faces



Lecture no-09

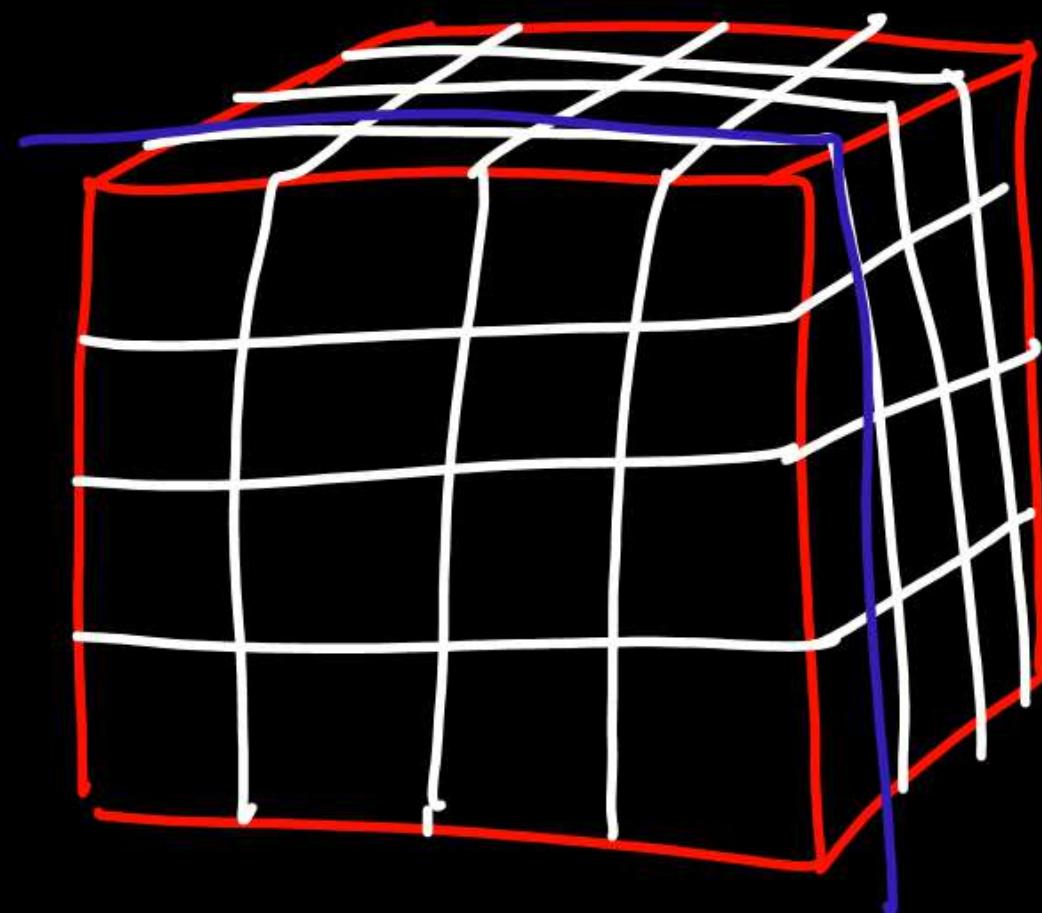
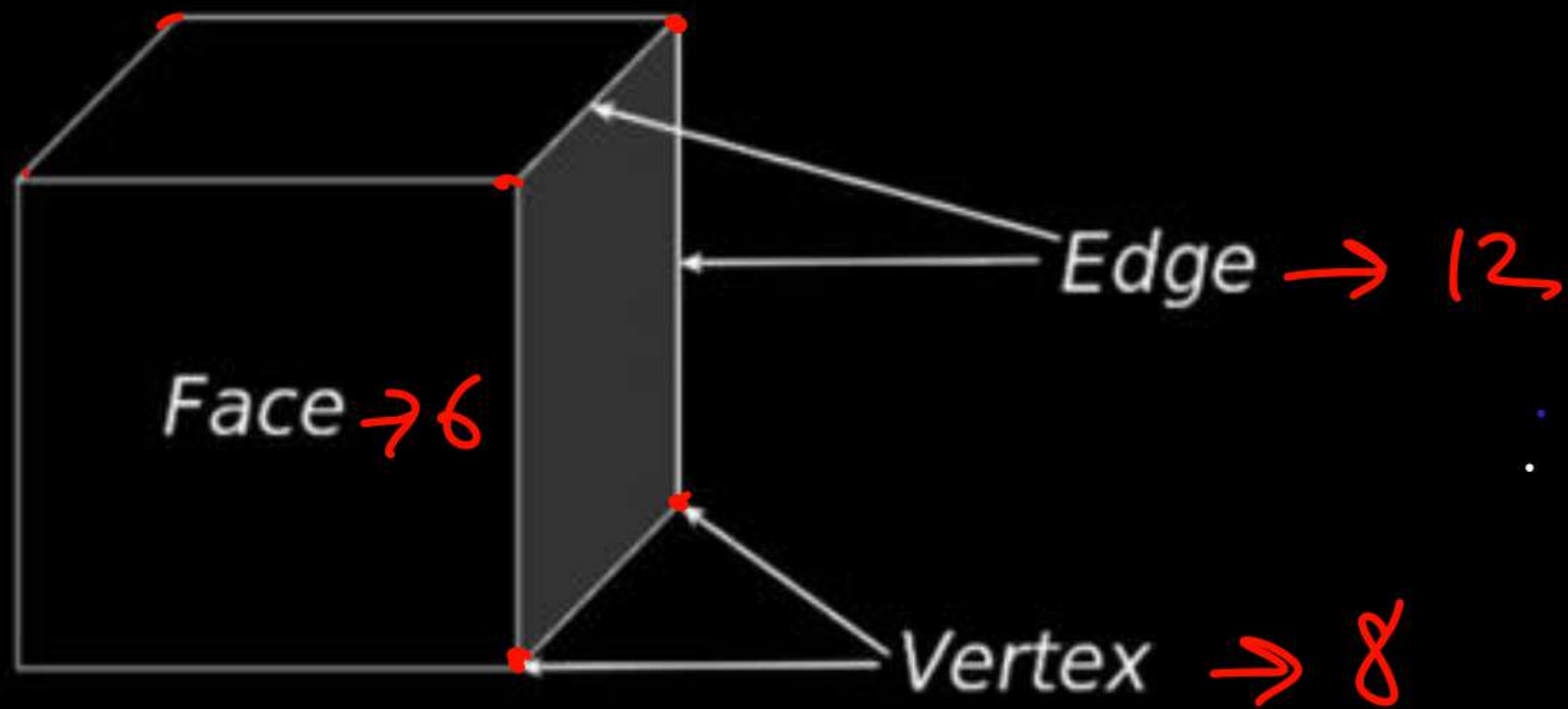
AMULYA RATAN SIR

CUBES

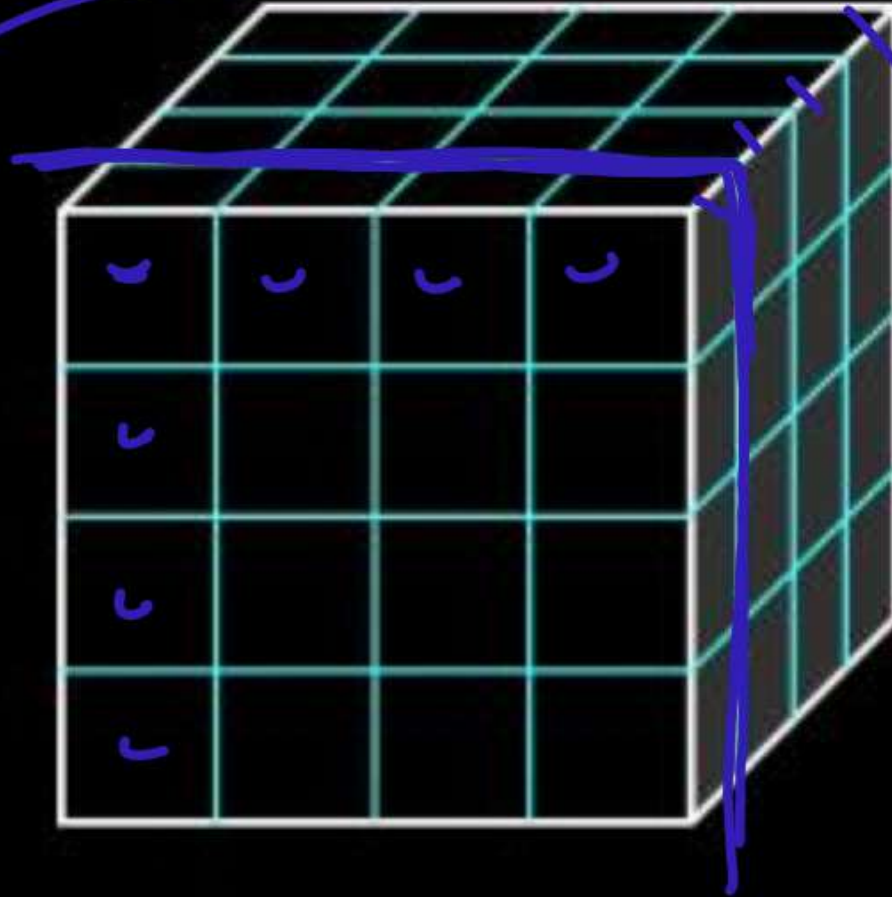


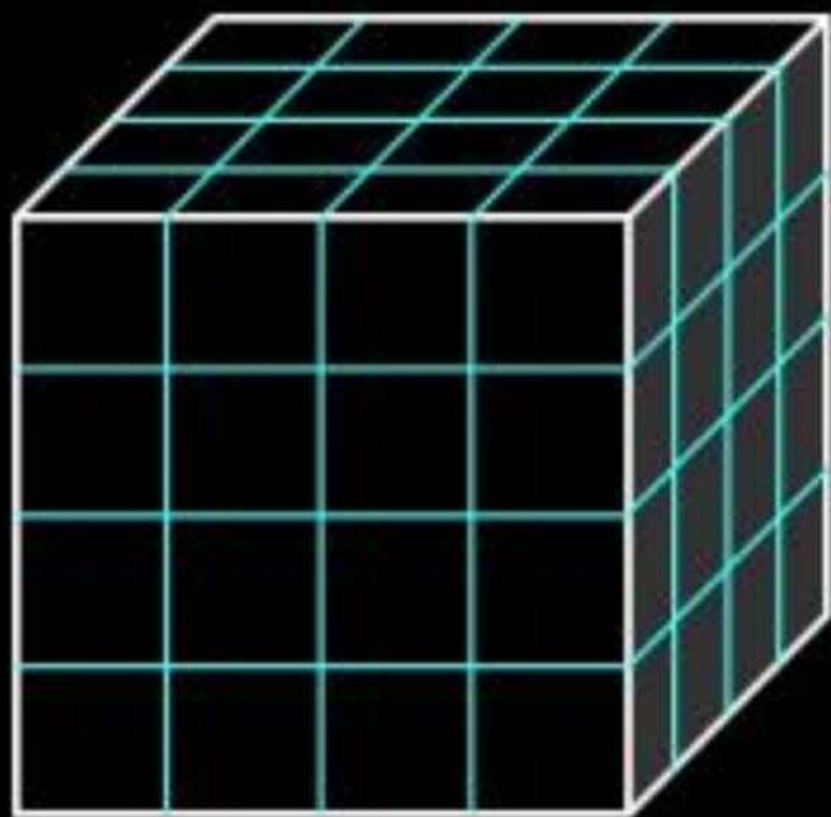
Vertex - 8

faces $\rightarrow 6$
Edges $\rightarrow 12$



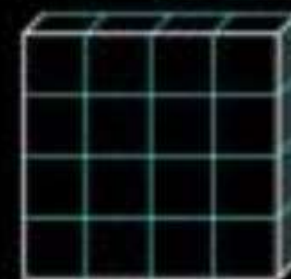
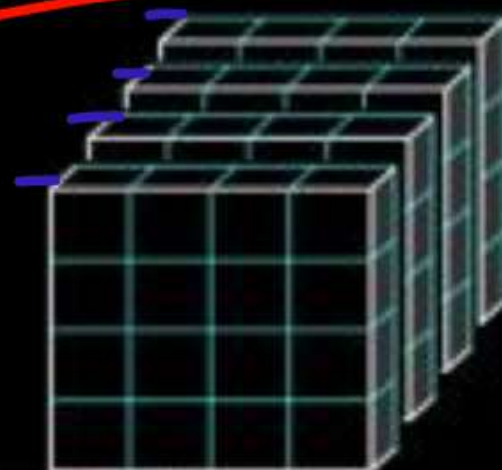
$$16 \times 4 = \underline{\underline{64}}$$





'x' cut

'8' cuts



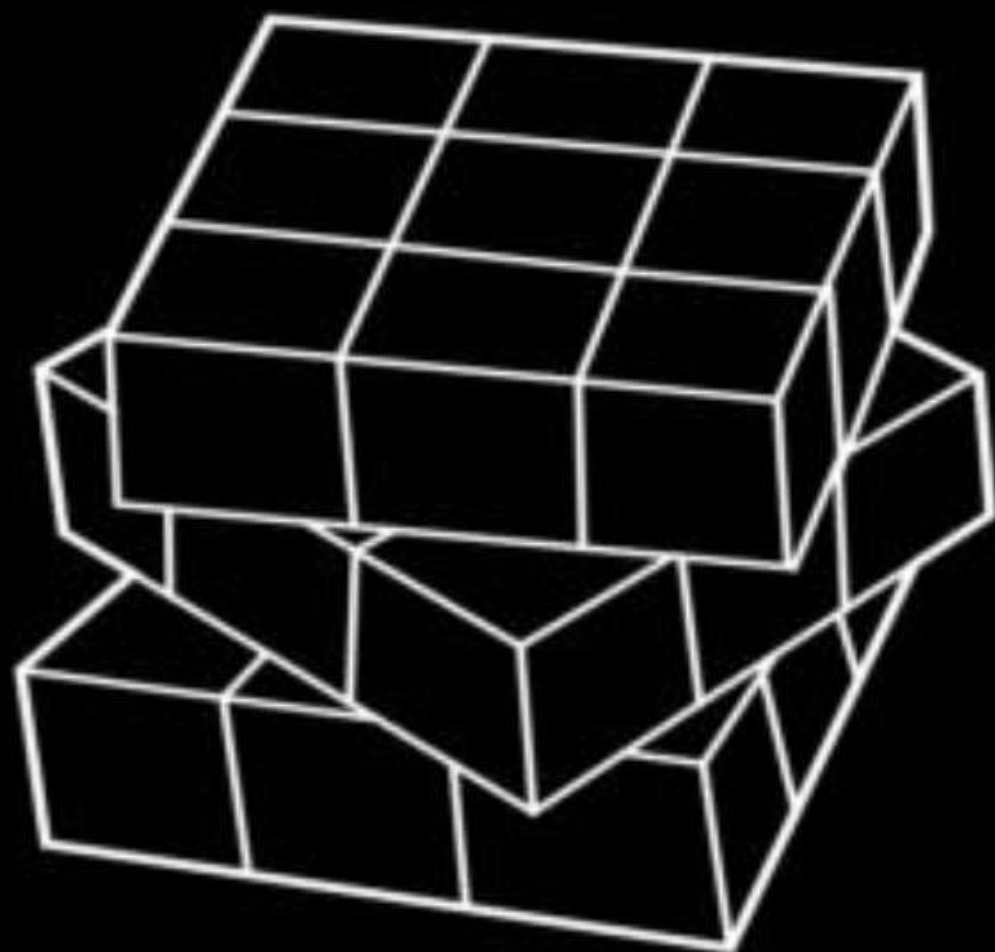
No. of cubes

$$= (x+1)^3$$

$$= 4^3 = \underline{\underline{64}}$$

7

9 cuts



Q.

A Cube was painted on one of the opposite pair faces as black & remaining four faces as green. five cuts were given on each edges to form smaller Cubes of equal size.

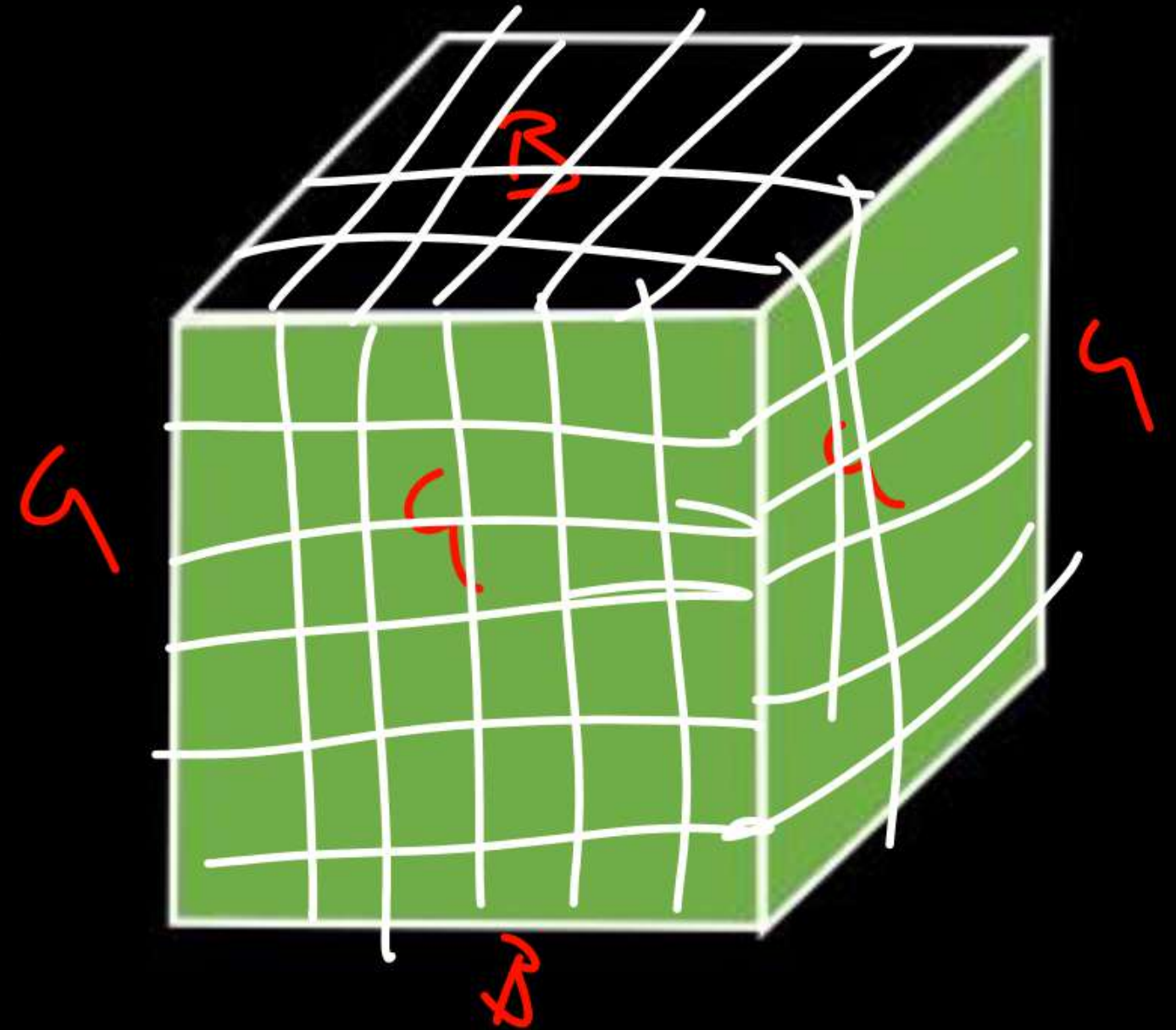


- 1 • How many cubes will be formed?
- 2 • How many cubes will have no face painted at all?
- 3 • How many cubes will have only one face painted?
- 4 • How many cubes will have only two face painted, but with same colour?
- 5 • How many cubes will have only two face painted, but different colour?
- 6 • How many cubes will have atleast two face painted?
- 7 • How many cubes will have three face painted?

Sol.

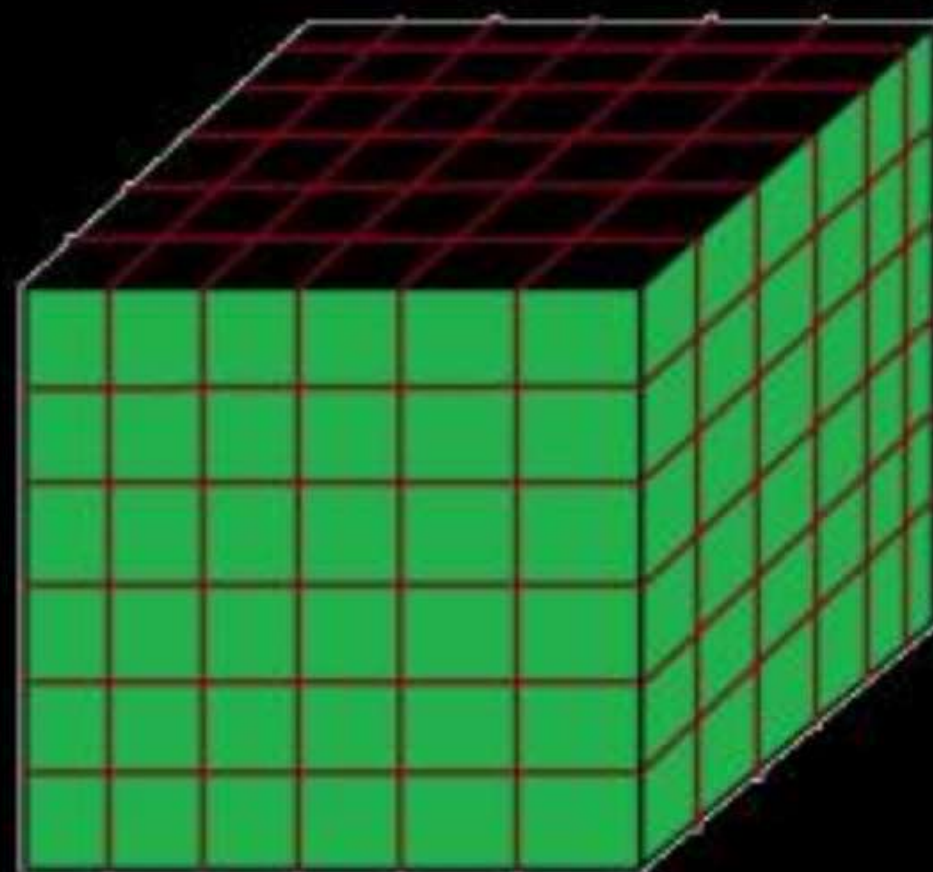


A Cube was painted on one of the opposite pair faces as black & remaining four faces as green. five cuts were given on each edges to form smaller Cubes of equal size.



Sol.

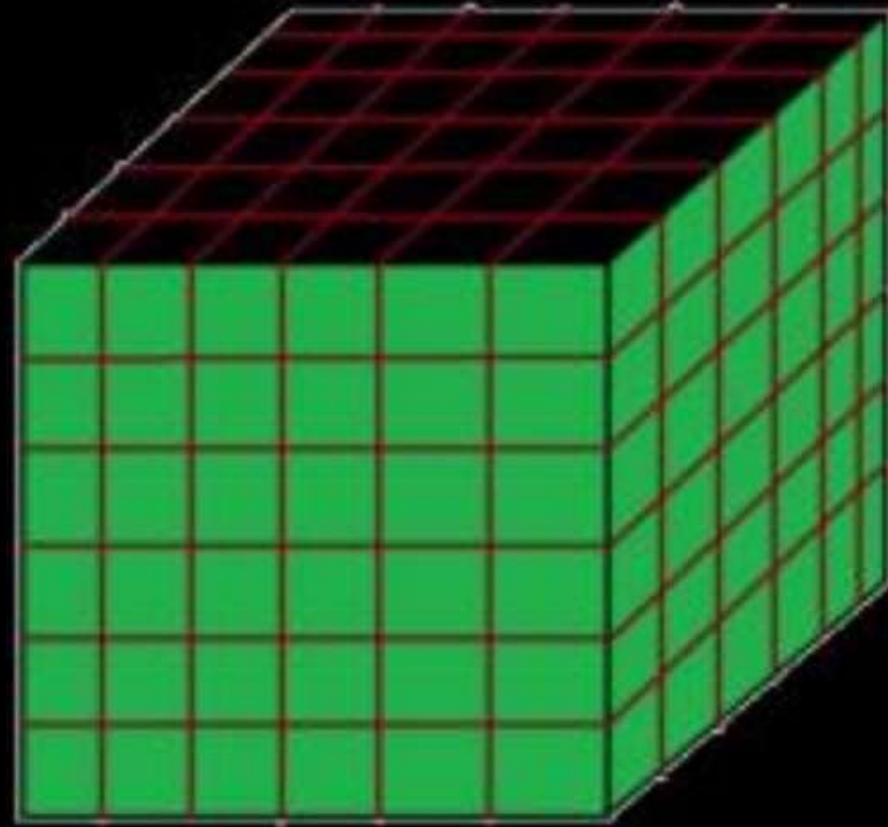
A Cube was painted on one of the opposite pair faces as black & remaining four faces as green. five cuts were given on each edges to form smaller Cubes of equal size.



CUBES

How many cubes will be formed?

216



CUBES

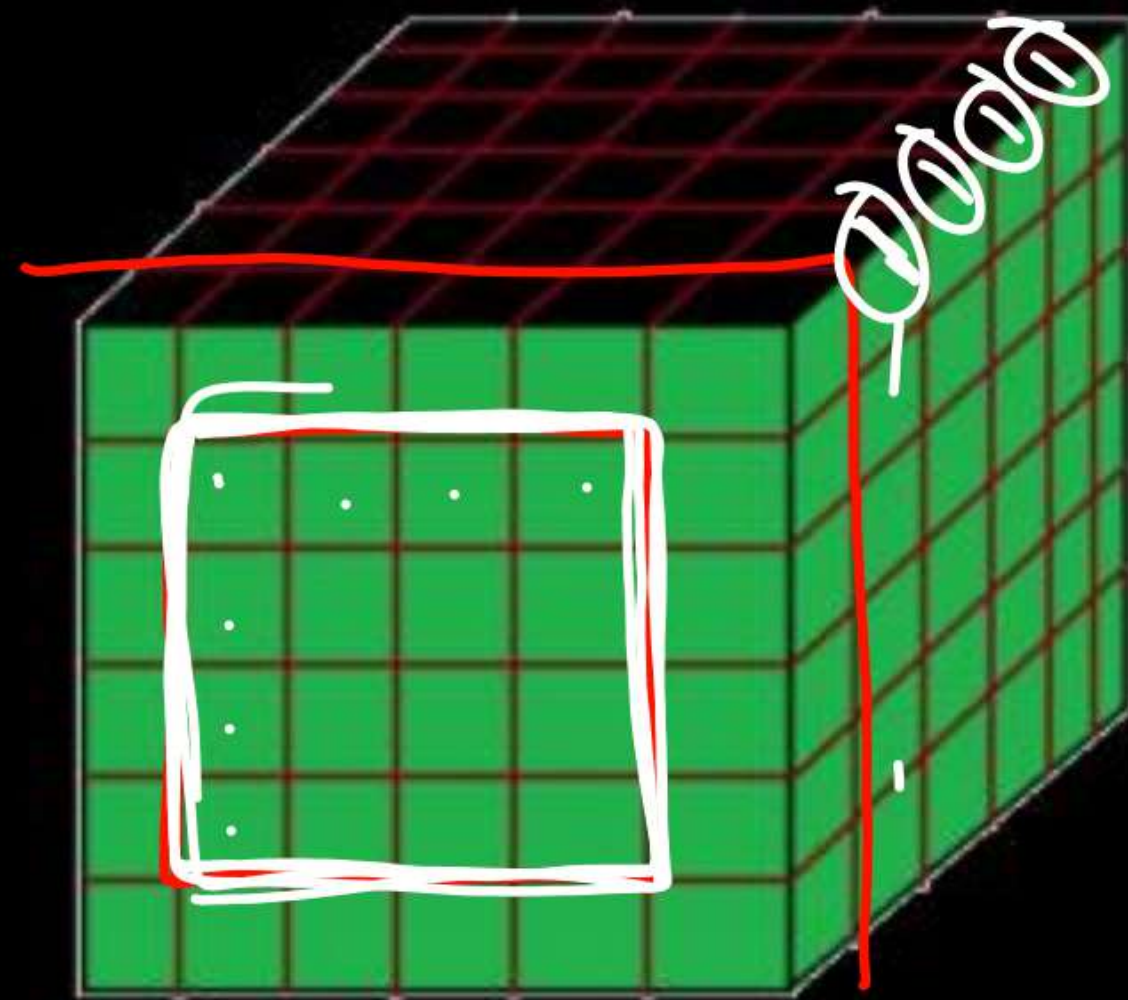
5

How many cubes will have no face painted at all?

'x' cut

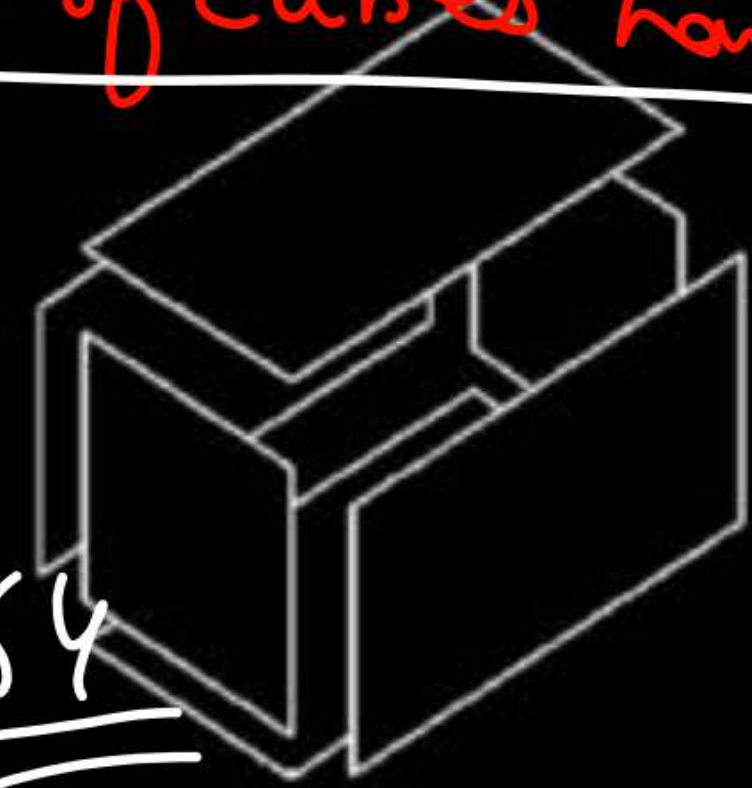
No. of cubes = $(x+1)^3$

$(5+1)^3 = \underline{\underline{216}}$



No. of cubes having x face

64



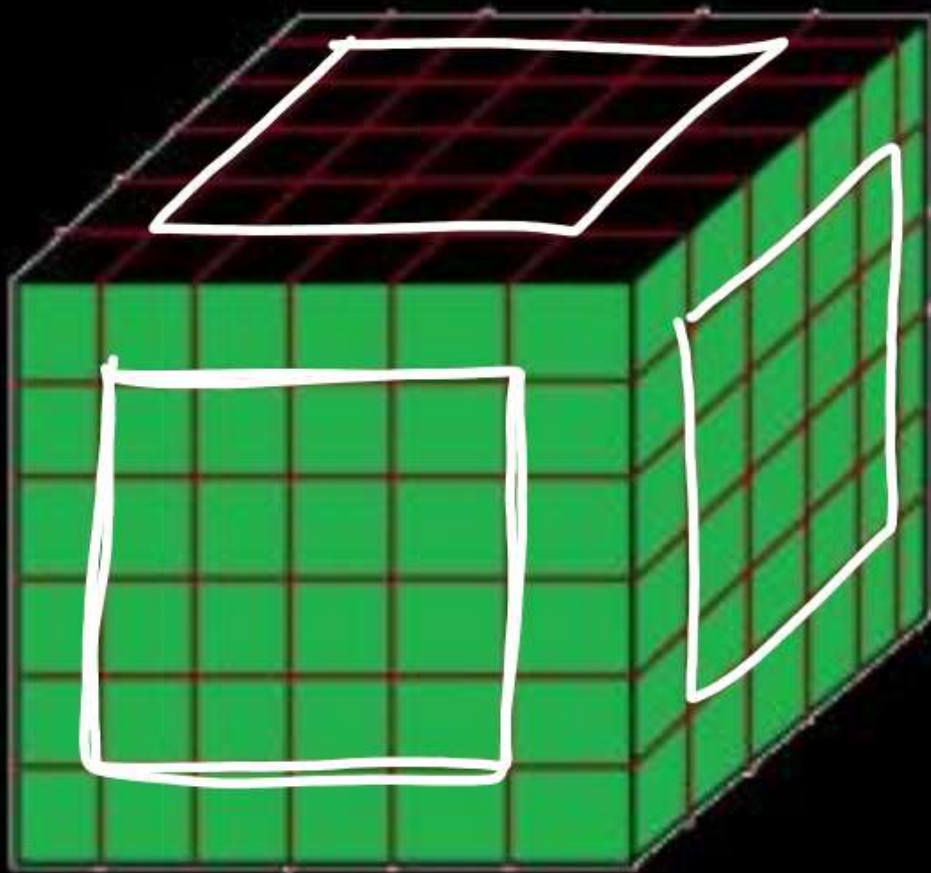
$4^3 = \underline{\underline{64}}$

Painted
 $= (x-1)^3$

CUBES



How many cubes will have only one face painted?



$$16 \times 6 = \underline{\underline{96}}$$

CUBES

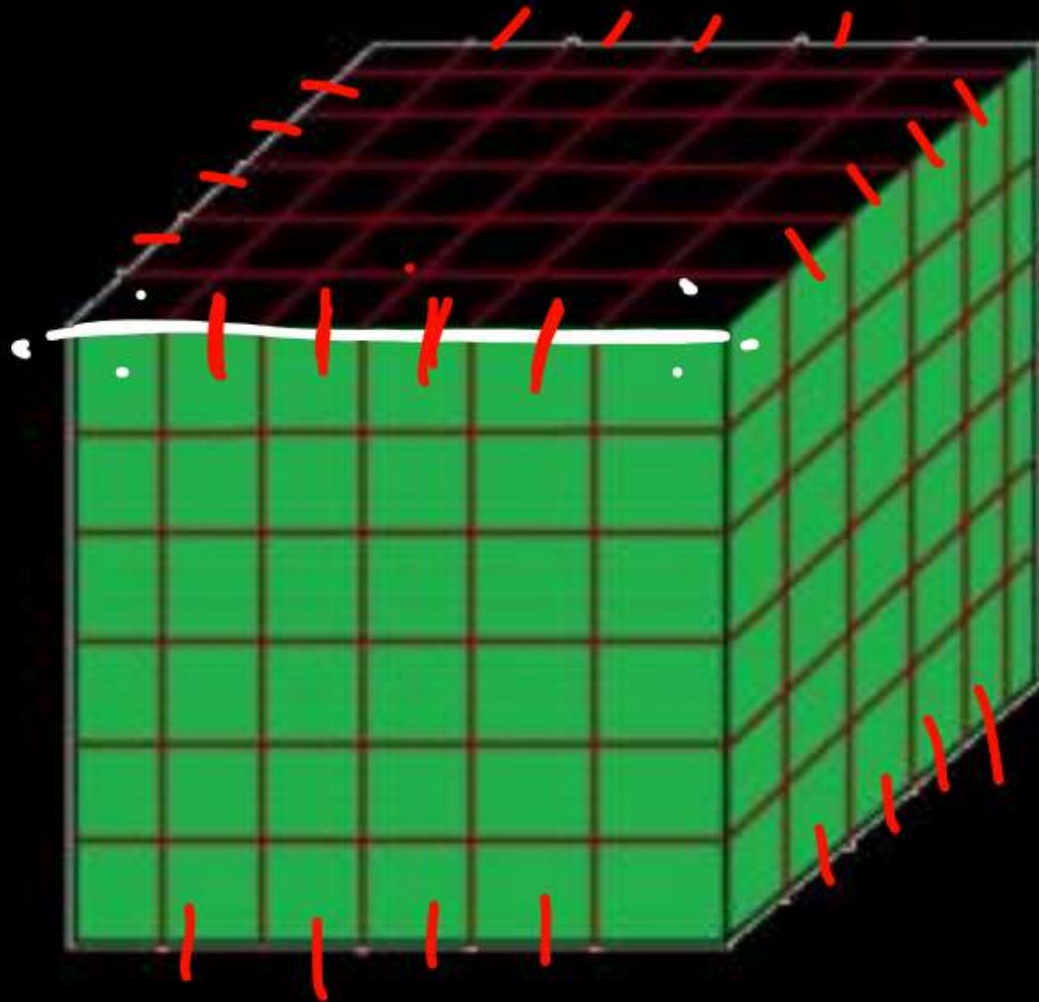


$$12 \times 4 = \underline{\underline{48}}$$

How many cubes will have only two face painted, but with same colour?

~~different~~

~~32~~

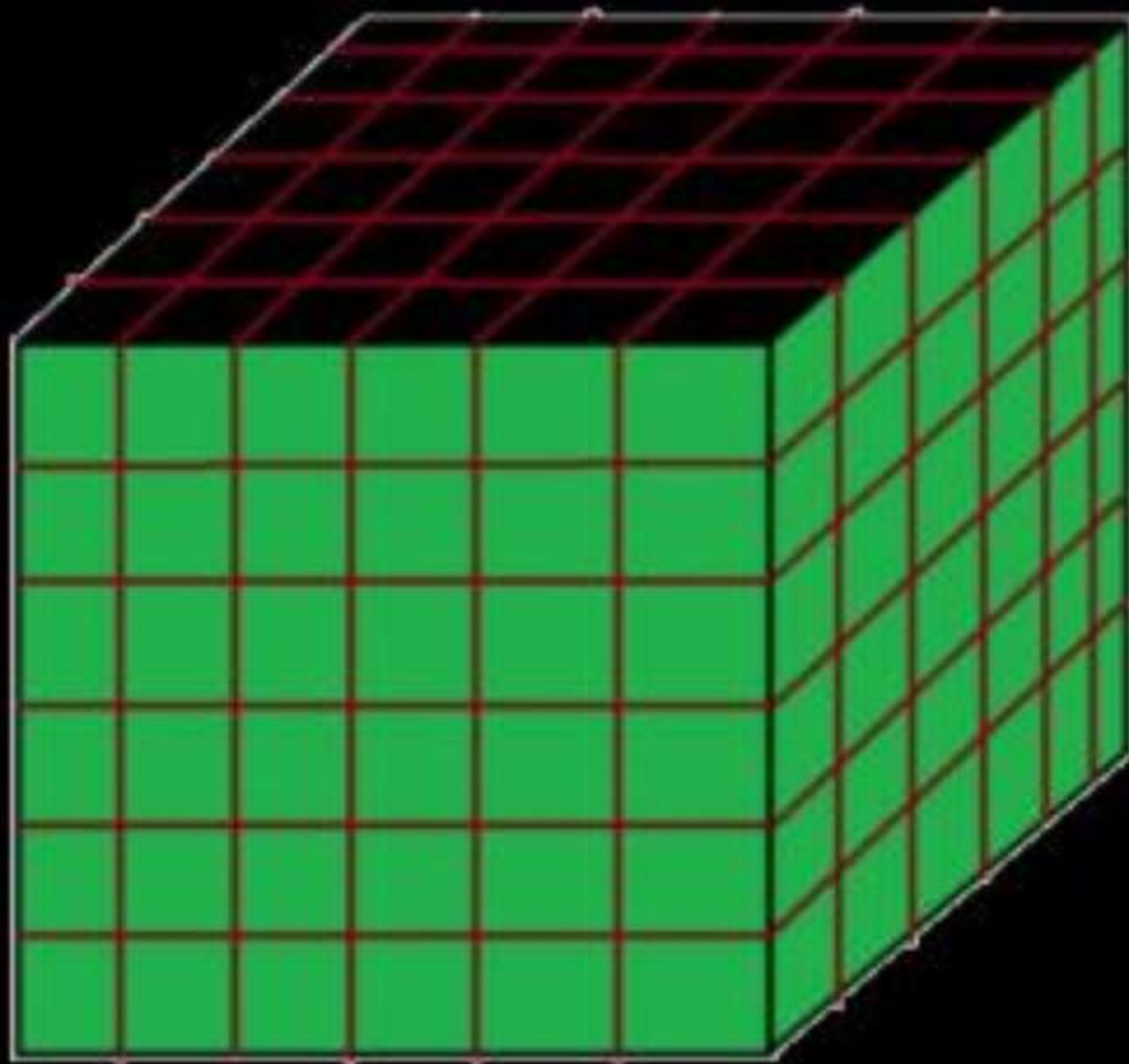


$$4 \times 4$$

$$= \underline{\underline{16}}$$

CUBES

How many cubes will have at least two face painted?



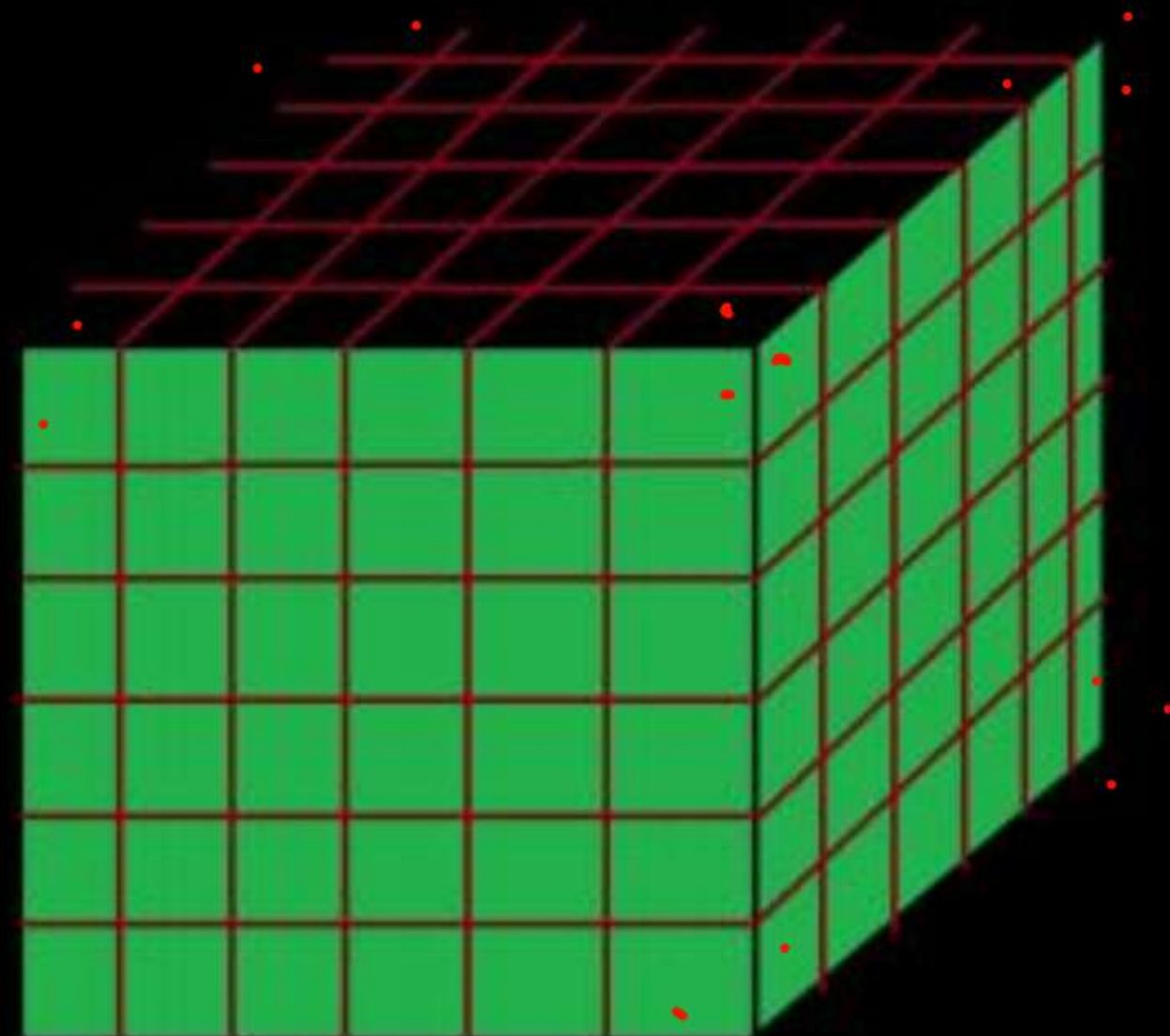
$$\begin{array}{r} 48 \\ + 8 \\ \hline 56 \\ \hline \hline \end{array}$$

CUBES



How many cubes will have three face painted?

8



CUBES



- Ans 1 :
- Ans 2 :
- Ans 3 :
- Ans 4 :
- Ans 5 :
- Ans 6 :
- Ans 7 :

216

64

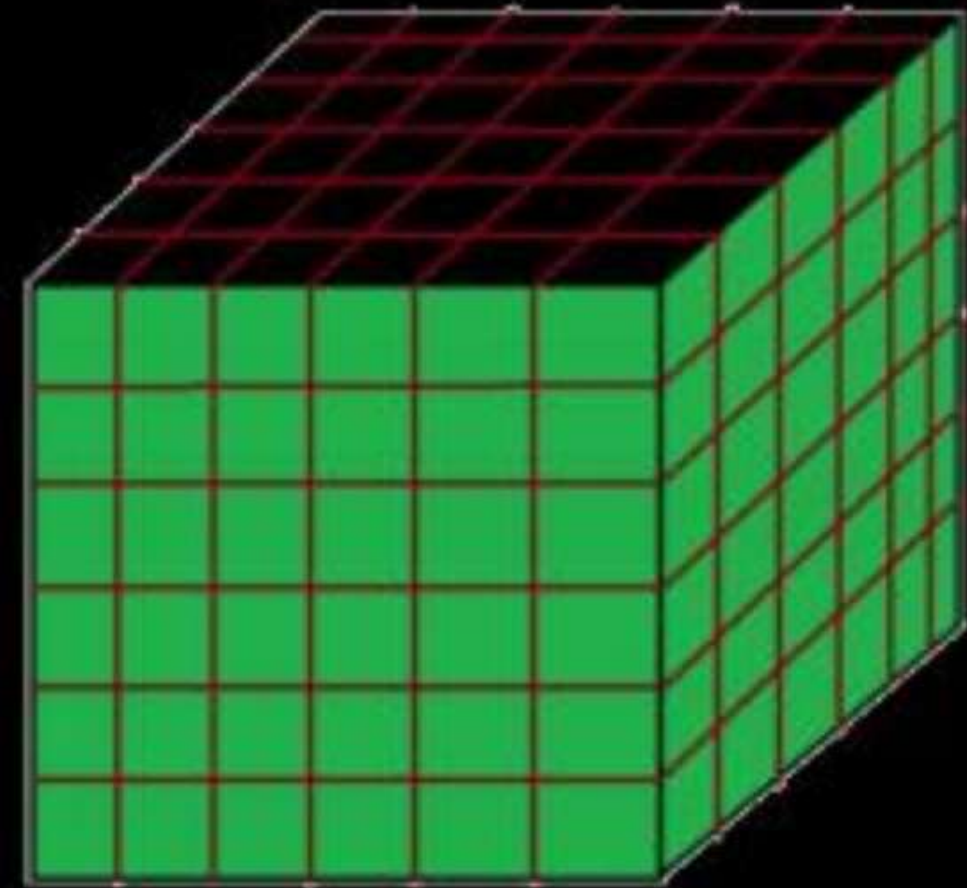
96

16

32

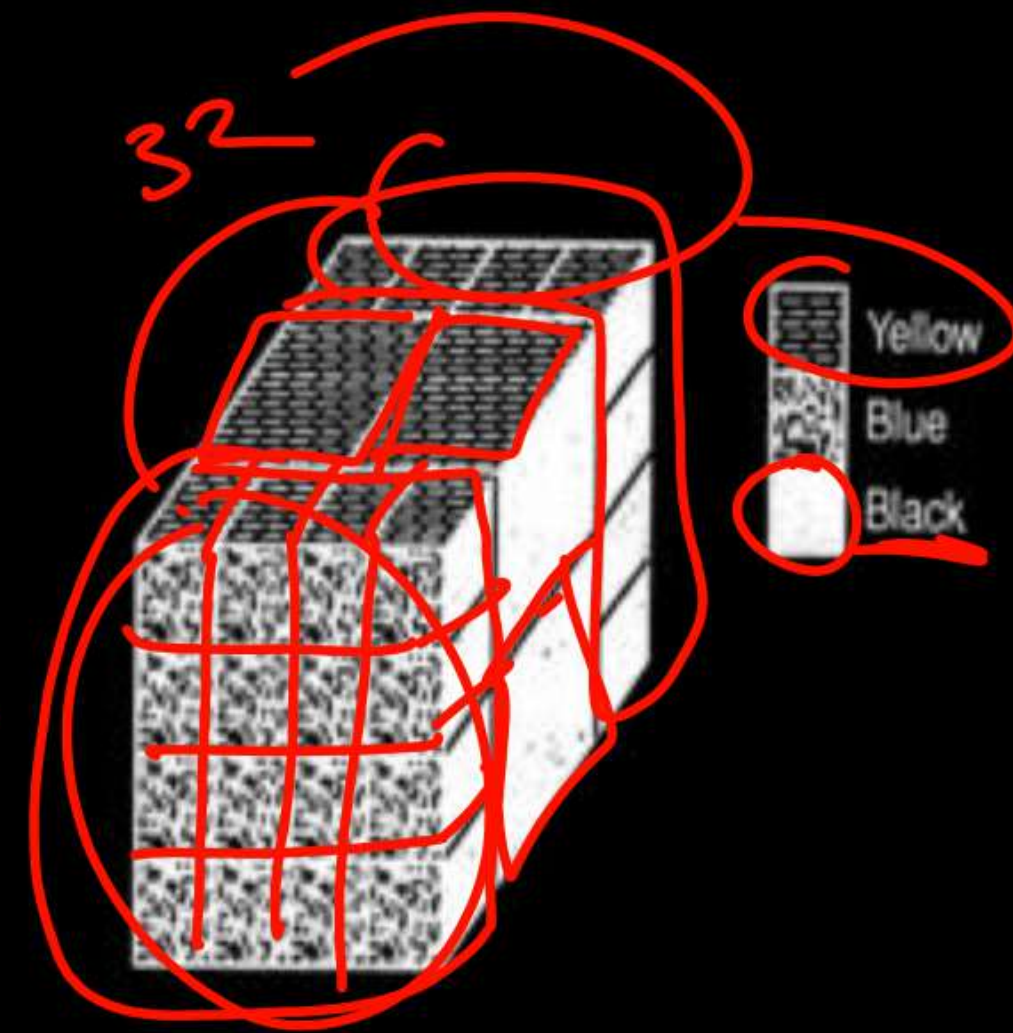
56

8



Brainstorming

A solid cube has been painted yellow, blue and black on pairs of opposite face. The cube is cut into 36 smaller cubes such that 32 cubes are of the same size while 4 others are of bigger size. Also no face of any of the bigger cubes is painted blue.



Q.

How many cubes have at least one face painted blue.

A

0

B

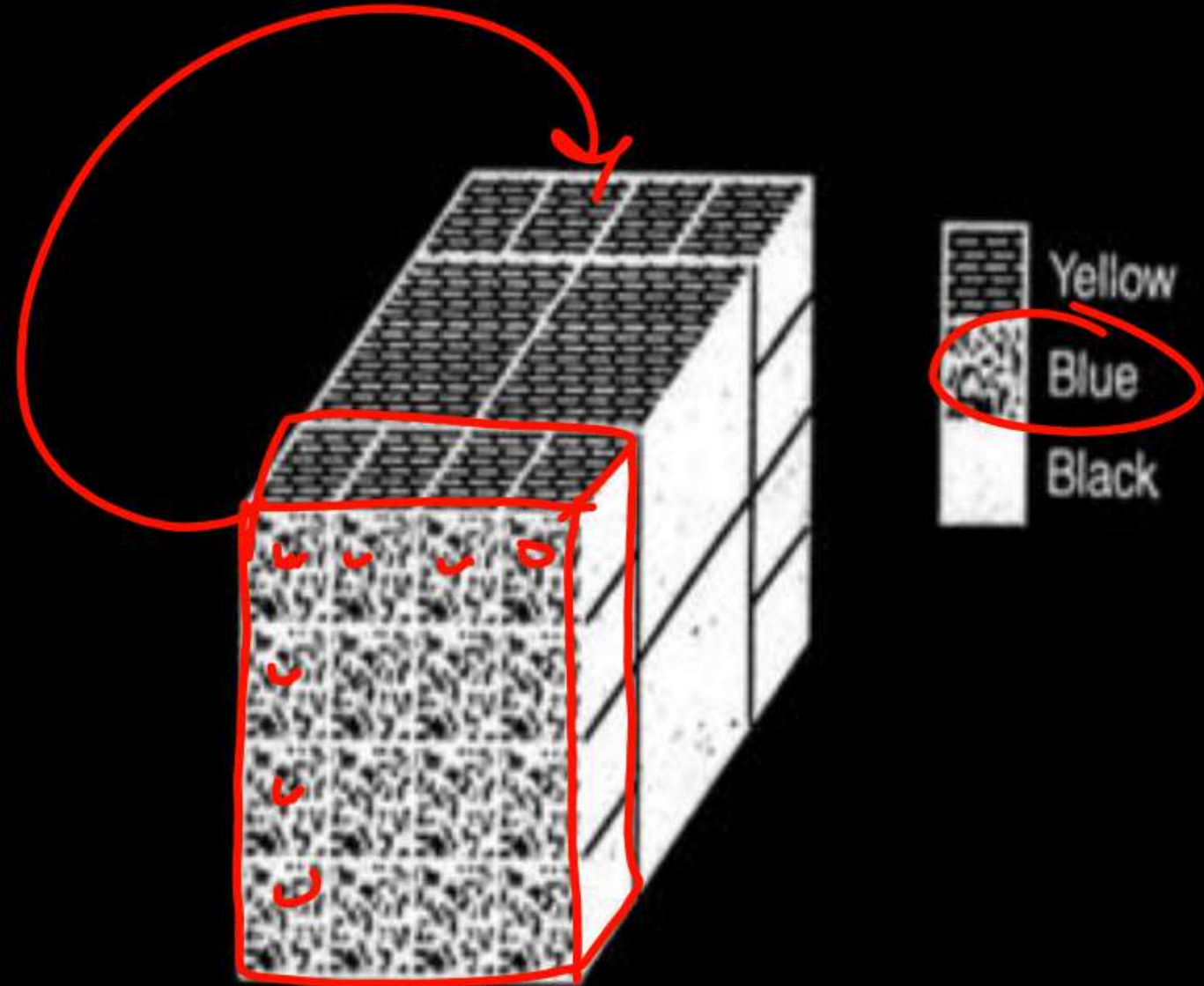
8

C

16

D

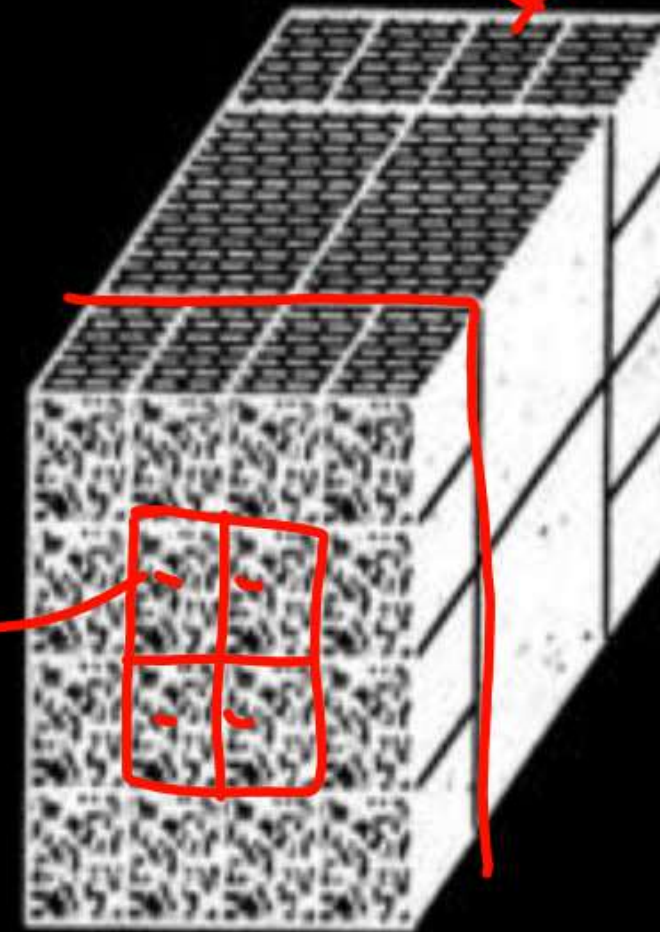
32



Q.

How many cubes have only one face painted.

- A 12
- B 8
- C 4
- D 0



Q.

How many cubes have two or more faces painted.

$$36 - 8 = \underline{\underline{28}}$$

A 36

B 34

C 28

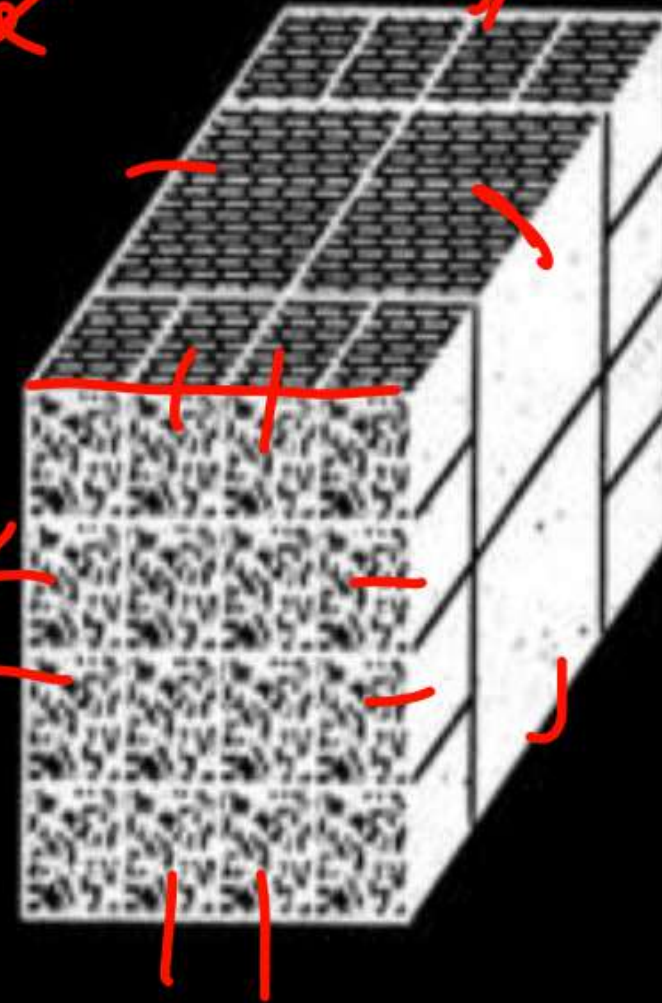
D 24

8 → Three faces

Small = 16

Big = 4

20



Yellow
Blue
Black

Q.

How many cubes only three faces painted?

A

8

B

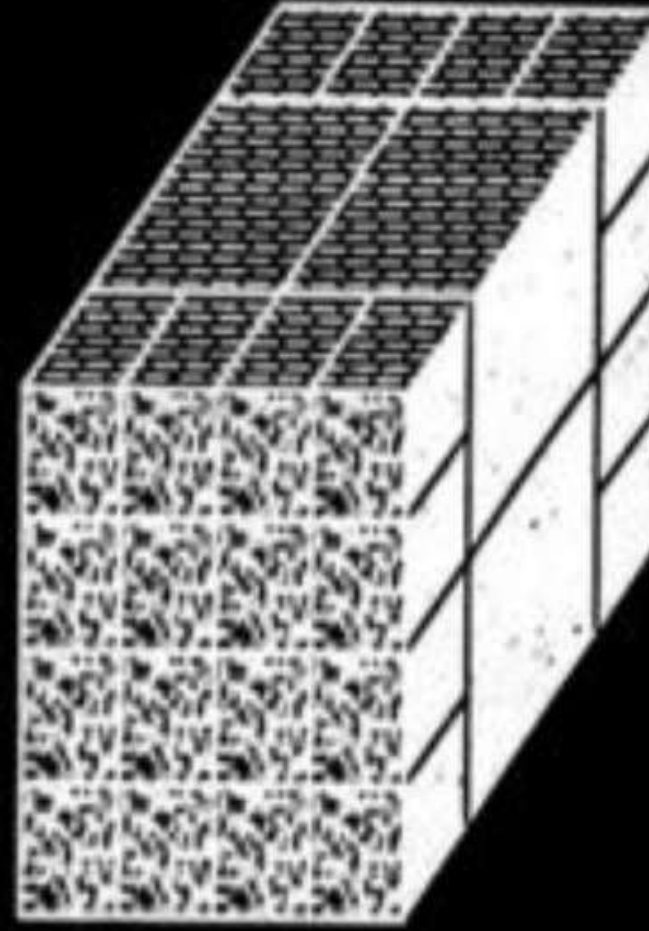
4

C

2

D

0



Yellow

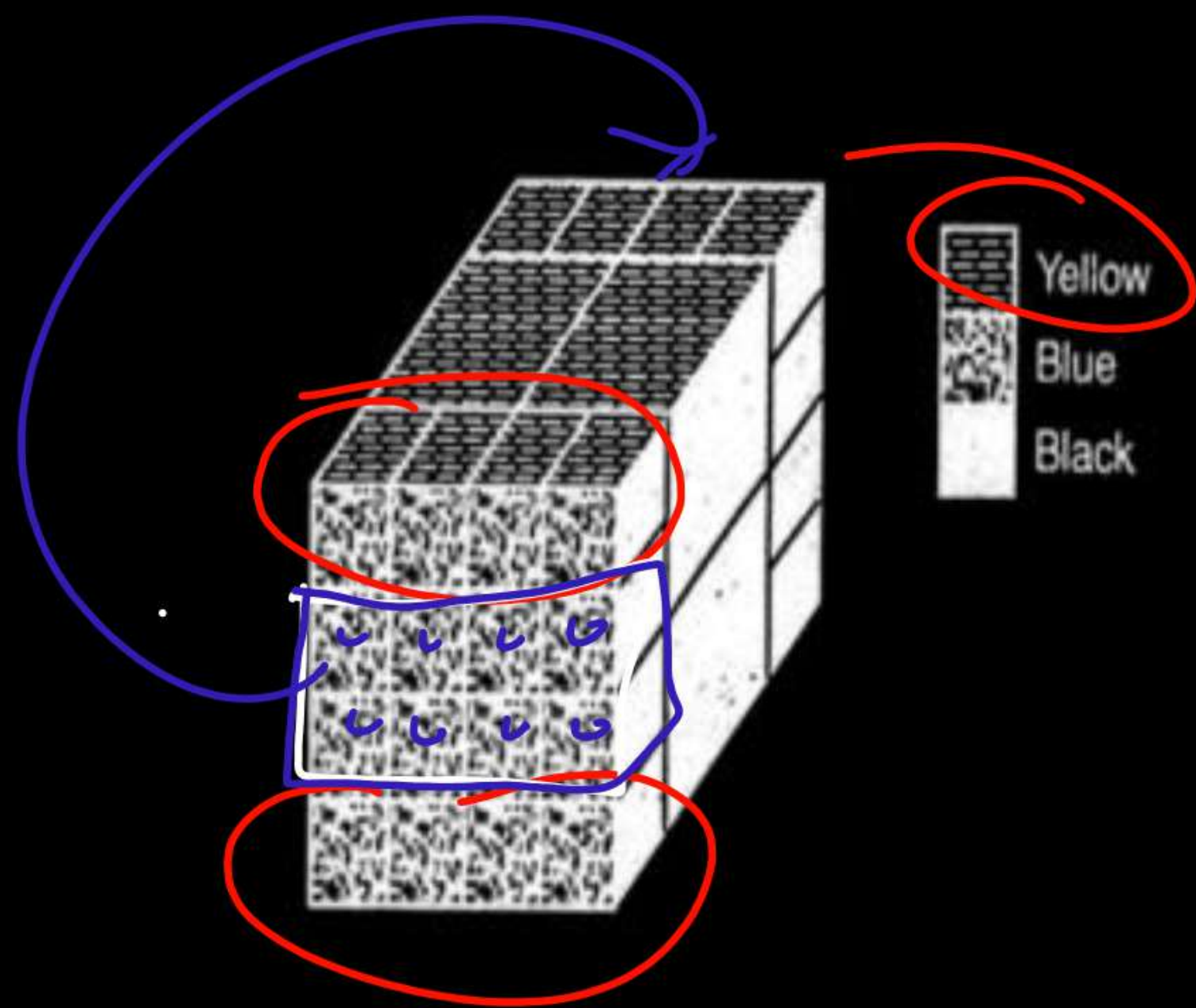
Blue

Black

Q.

How many cubes do not have any of their faces painted yellow?

- A 0
- B 8
- C 16
- D 20



Q.

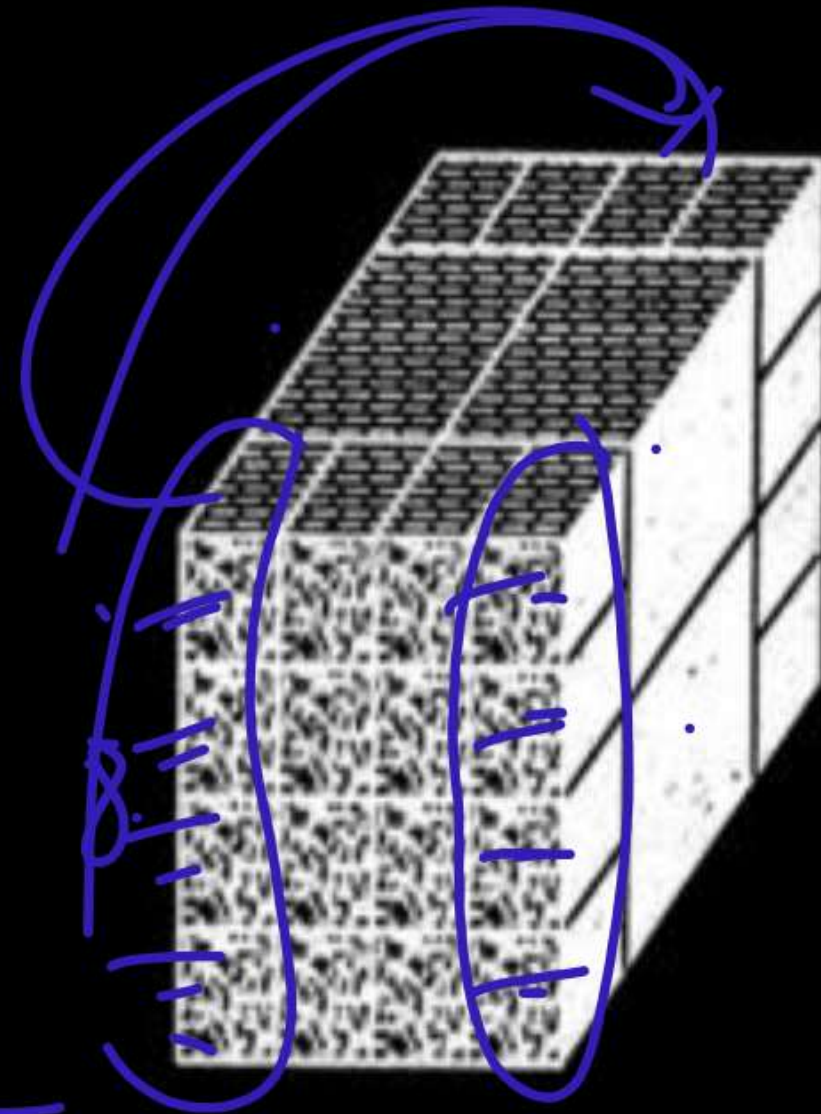
How many cubes have at least one of their faces painted black?

- A 0
- B 8
- C 16
- D 20**

Big = 4

Small = 16

20



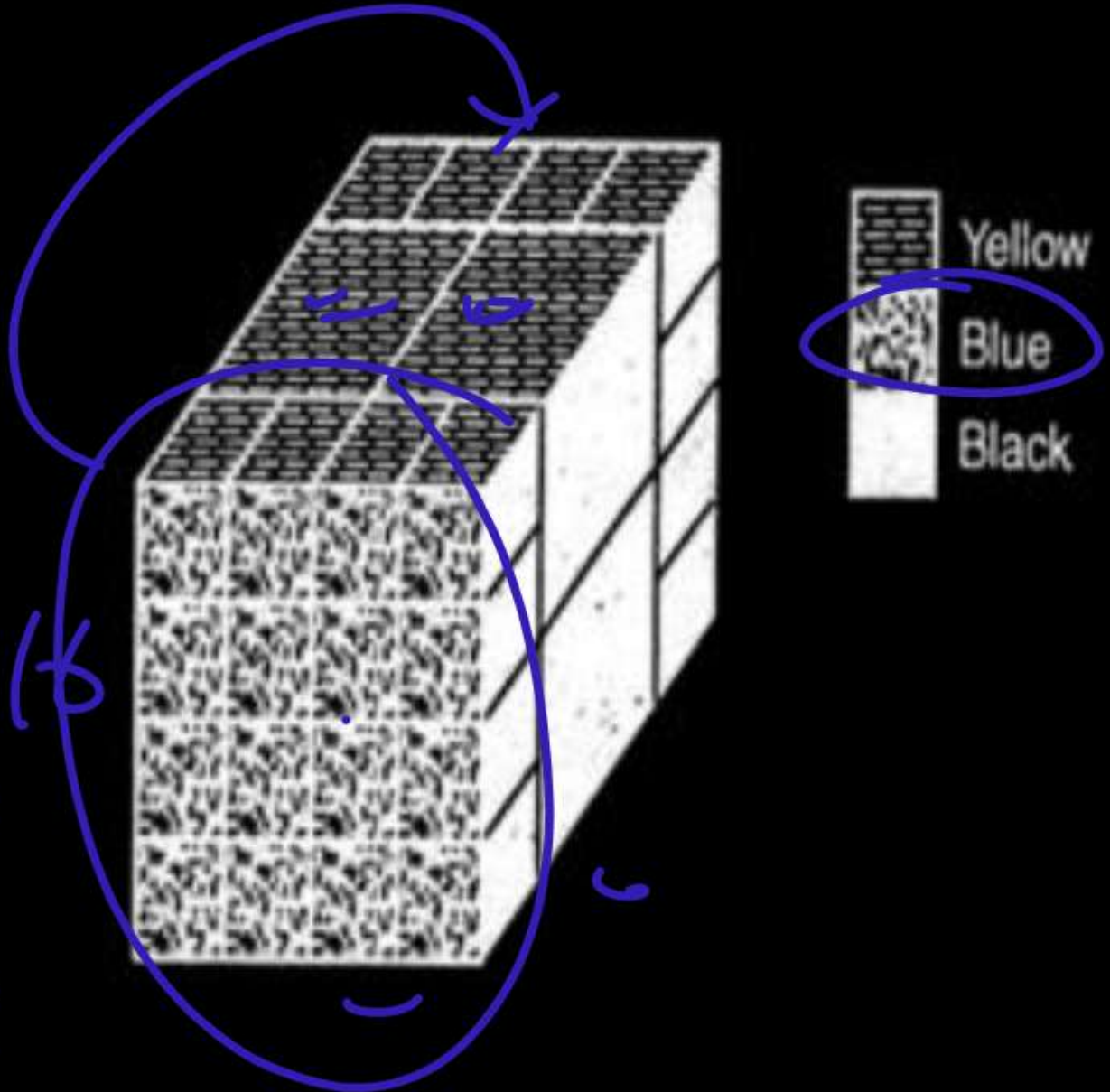
Yellow
Blue
Black

Q.

How many cubes have at least one of their faces painted yellow or blue?

- A 36
- B 32
- C 16
- D 0

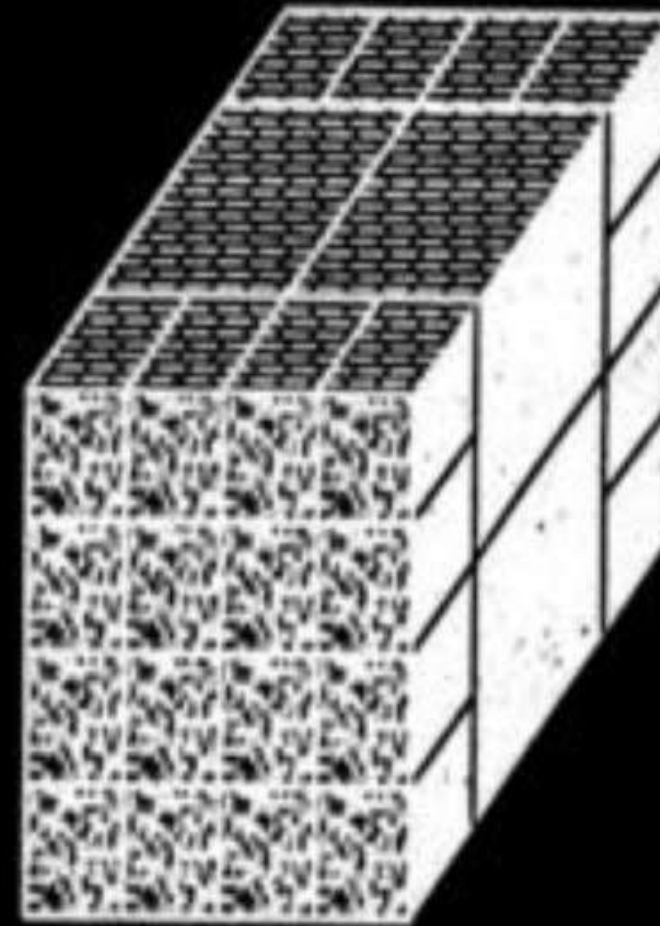
$$\begin{aligned} \text{Small} &= 32 \\ \text{Big} &= 4 \times 16 \\ \hline &= 36 \end{aligned}$$



Q.

How many cubes have no face painted?

- A** 0 ✓
- B** 8
- C** 12
- D** 16



Q.

How many cubes have two faces painted yellow and black respectively?

- A 0
- B 8
- C 12**
- D 16

Big = 4

Small = 8

12

