



# Practice Questions

## Multiplexer

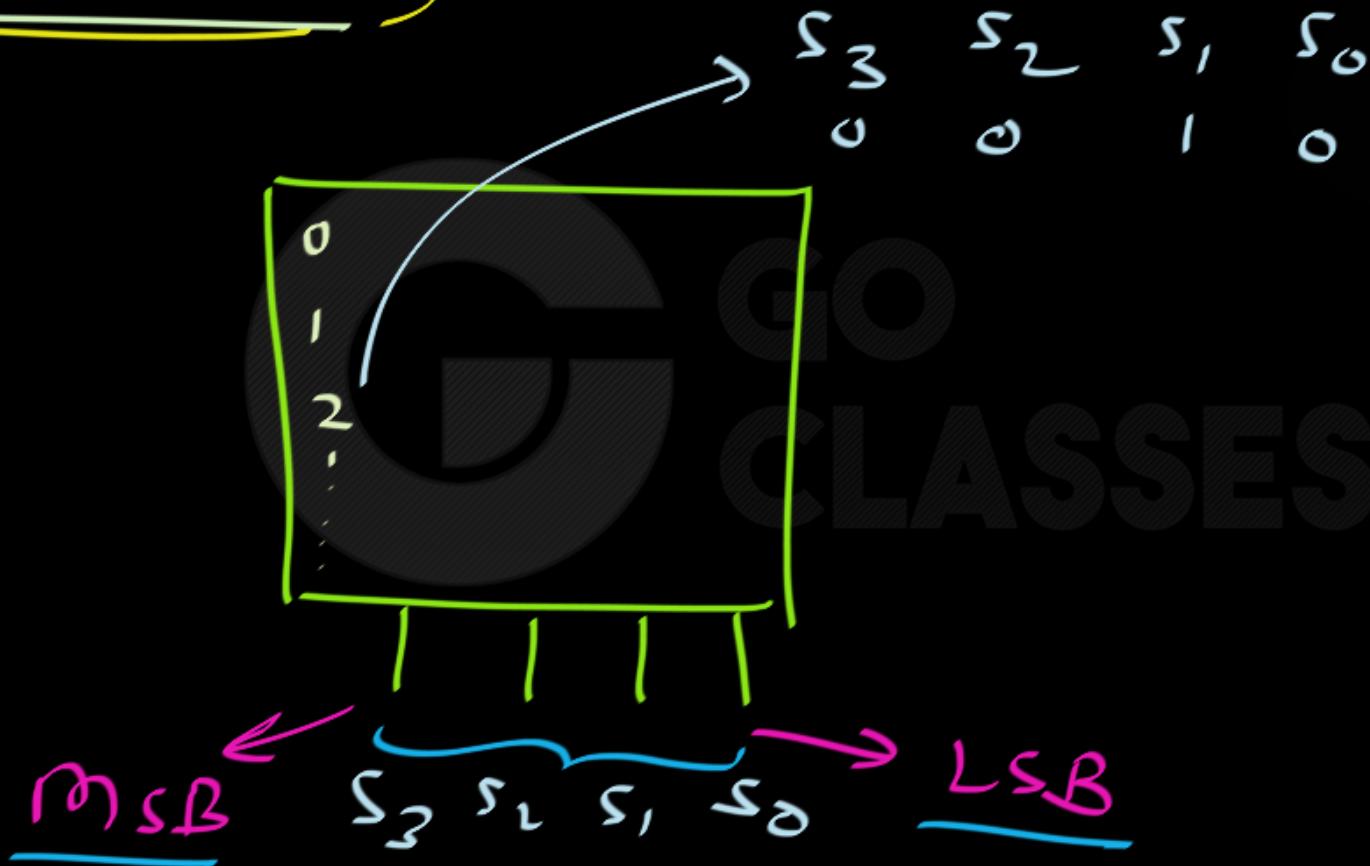


# Next Topic:

Realization(Implementation)  
Of Functions using Mux



By Default:

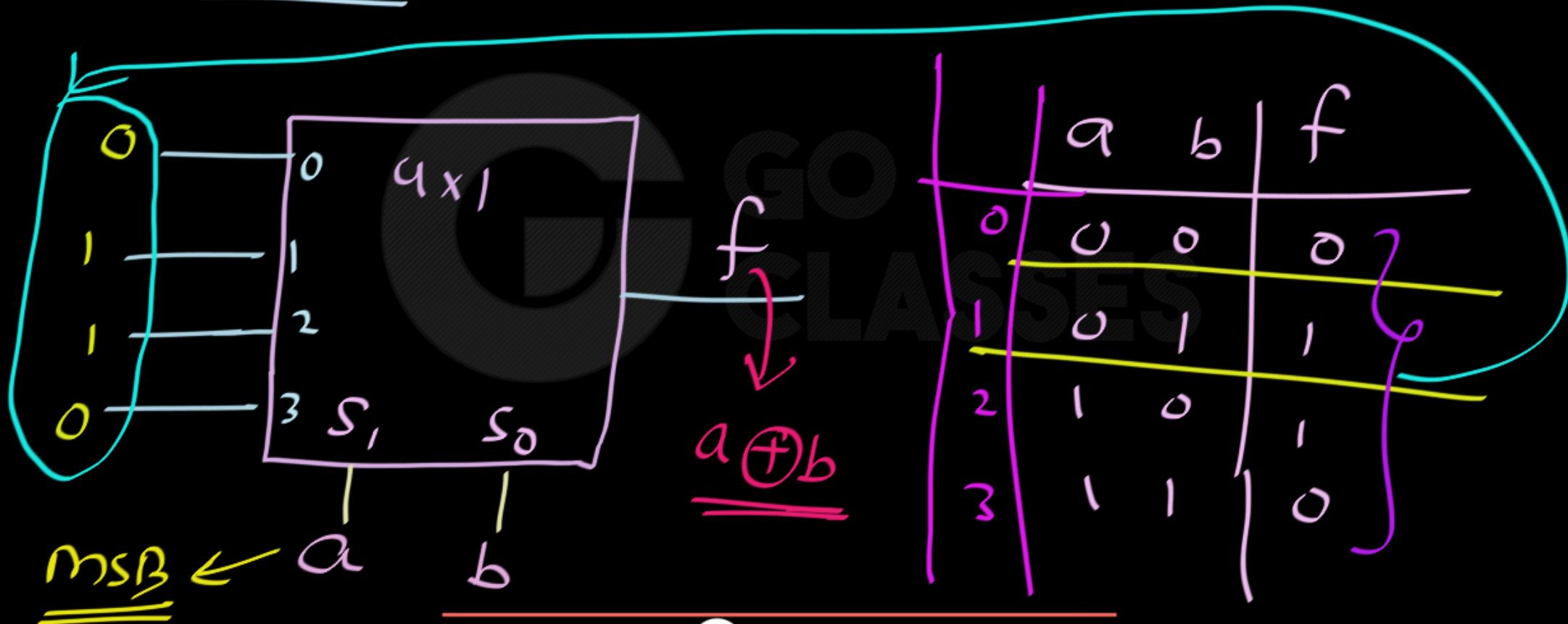




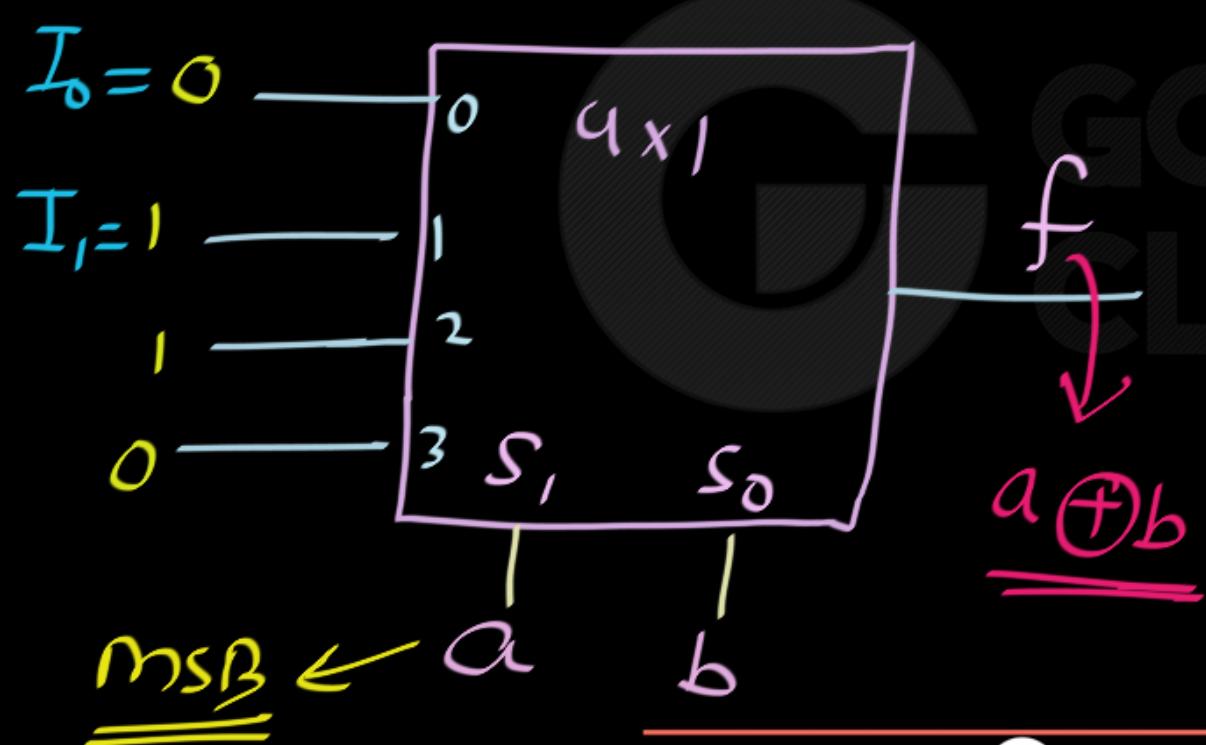
Q:  $f(a,b) = a \oplus b$  using 4x1 mux .



$\oplus$ :  $f(a,b)$  =  $a \oplus b$  using  $4 \times 1$  mux.



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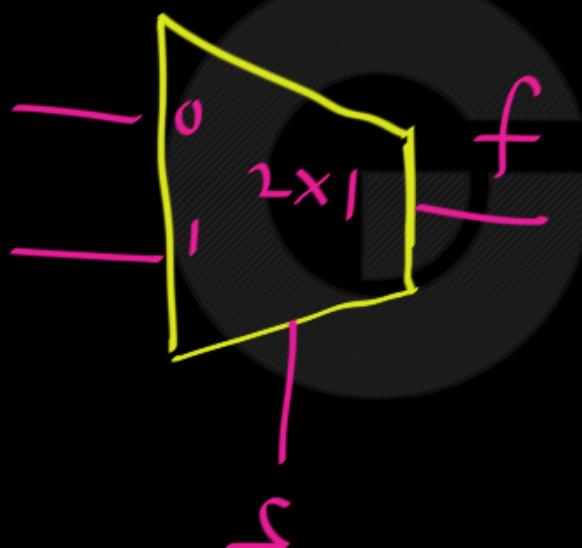


$$\begin{aligned}
 f(a,b) &= (\overline{a} \overline{b}) + \\
 &\quad \overline{a} b + \\
 &\quad a \overline{b} + \\
 &\quad = \overline{a} b + a \overline{b} \\
 &= a \oplus b
 \end{aligned}$$

Below the equations, there is a green circle containing the expression  $ab_0$  with an arrow pointing down to it.

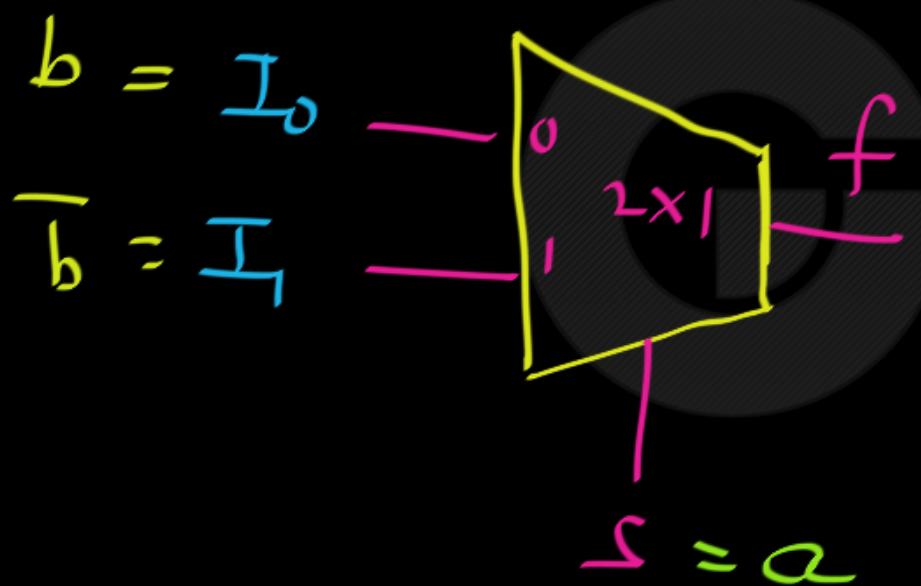


$\oplus$ :  $f(a,b) = a \oplus b$  using  $2 \times 1$  mux.



GO  
CLASSES

Q:  $f(a,b) = a \oplus b$  using  $2 \times 1$  mux.

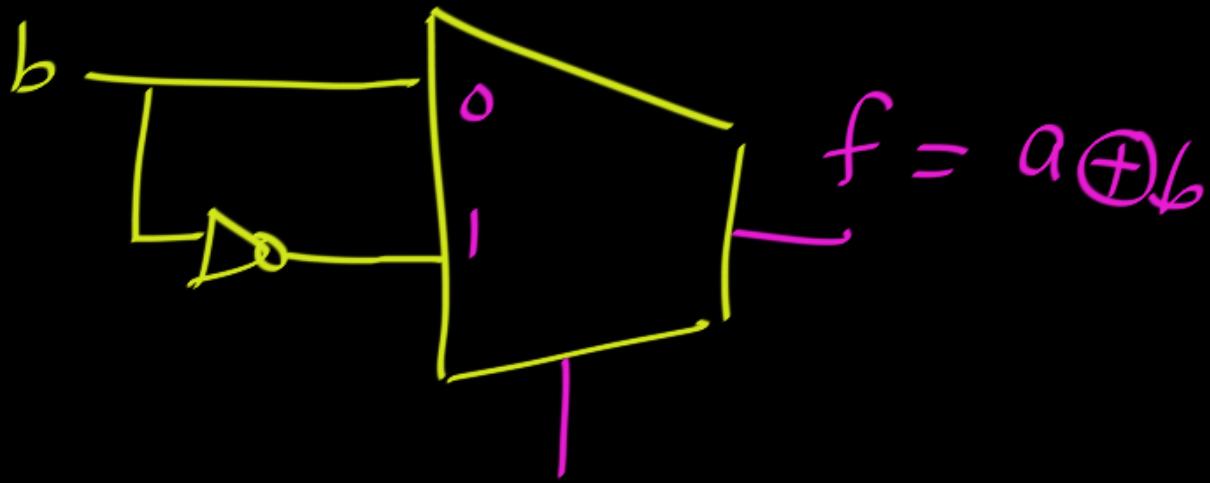


Csol:  $f = \overline{a} \overline{b} + \overline{a} b$

$$f = \overline{a} I_0 + \overline{a} I_1$$

$\swarrow$        $\searrow$

$b$        $\overline{b}$

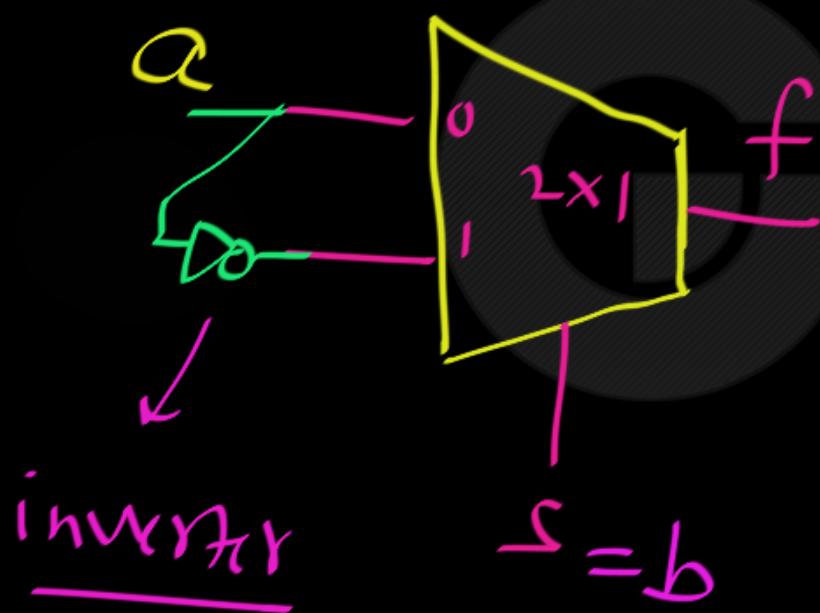


$$f = a \oplus b$$

$$s = a$$

(2 - 1 mux) + 1 inverter.

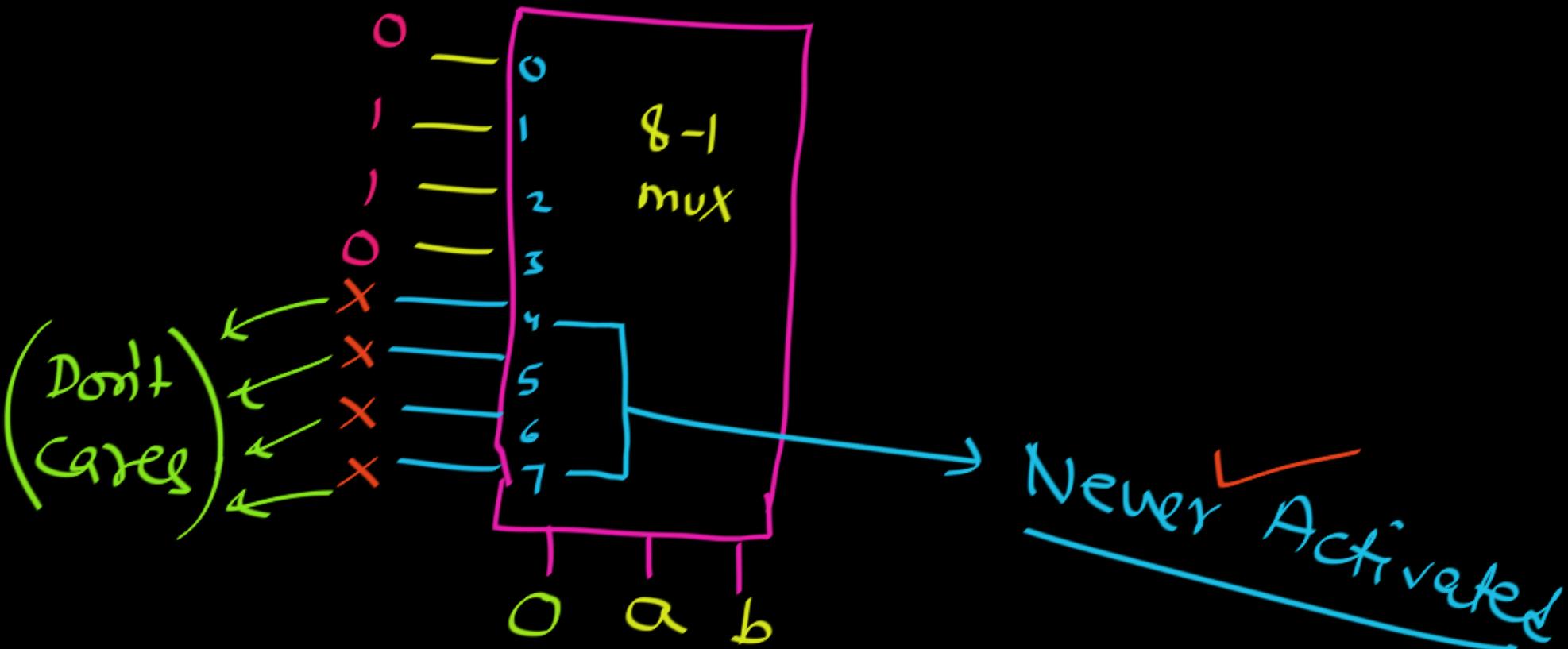
$\oplus$ :  $f(a,b) = a \oplus b$  using  $2 \times 1$  mux.



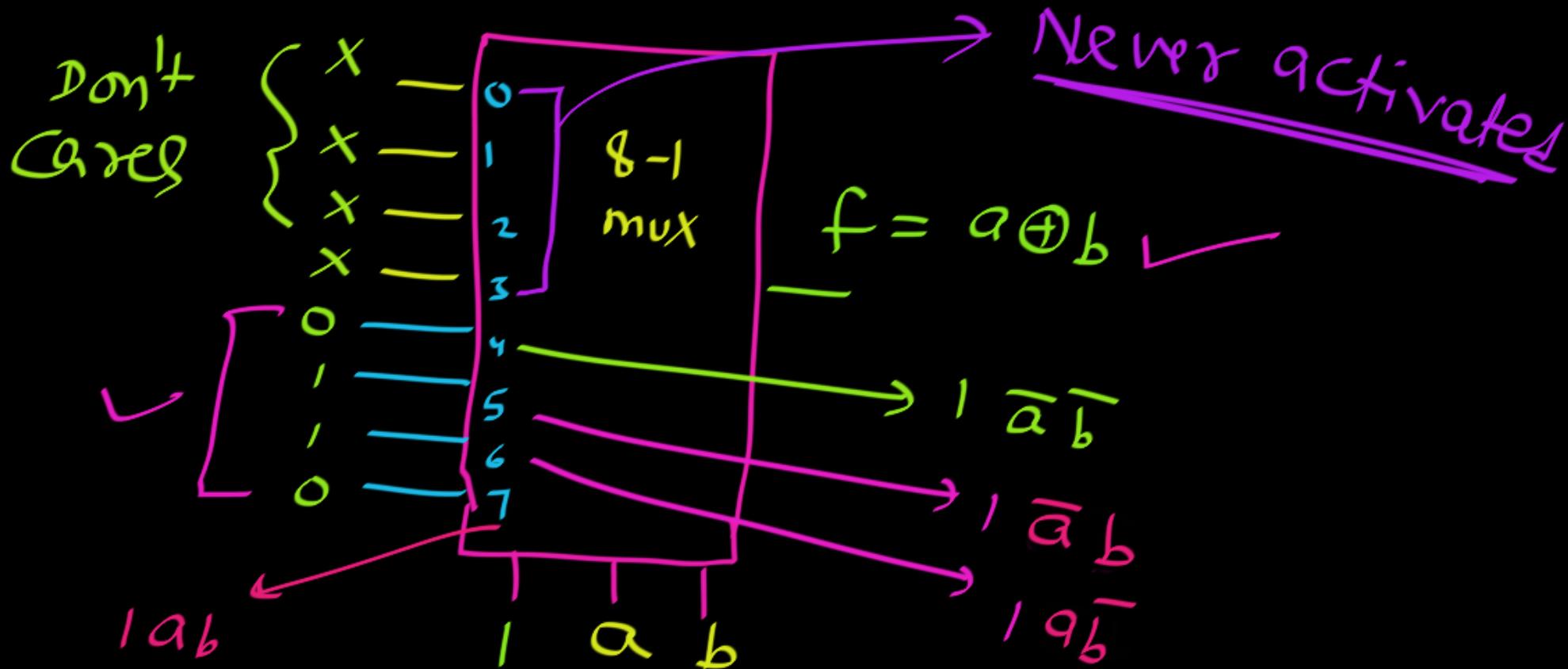
$$\begin{aligned}
 f &= \bar{S}a + S\bar{b} \\
 &= a \oplus b \\
 &\quad \underbrace{(2-1 \text{ mux}) + 1 \text{ inverter}}_{}
 \end{aligned}$$

$\Phi$ :  $f(a, b) = a \oplus b$  using 8x1 mux.

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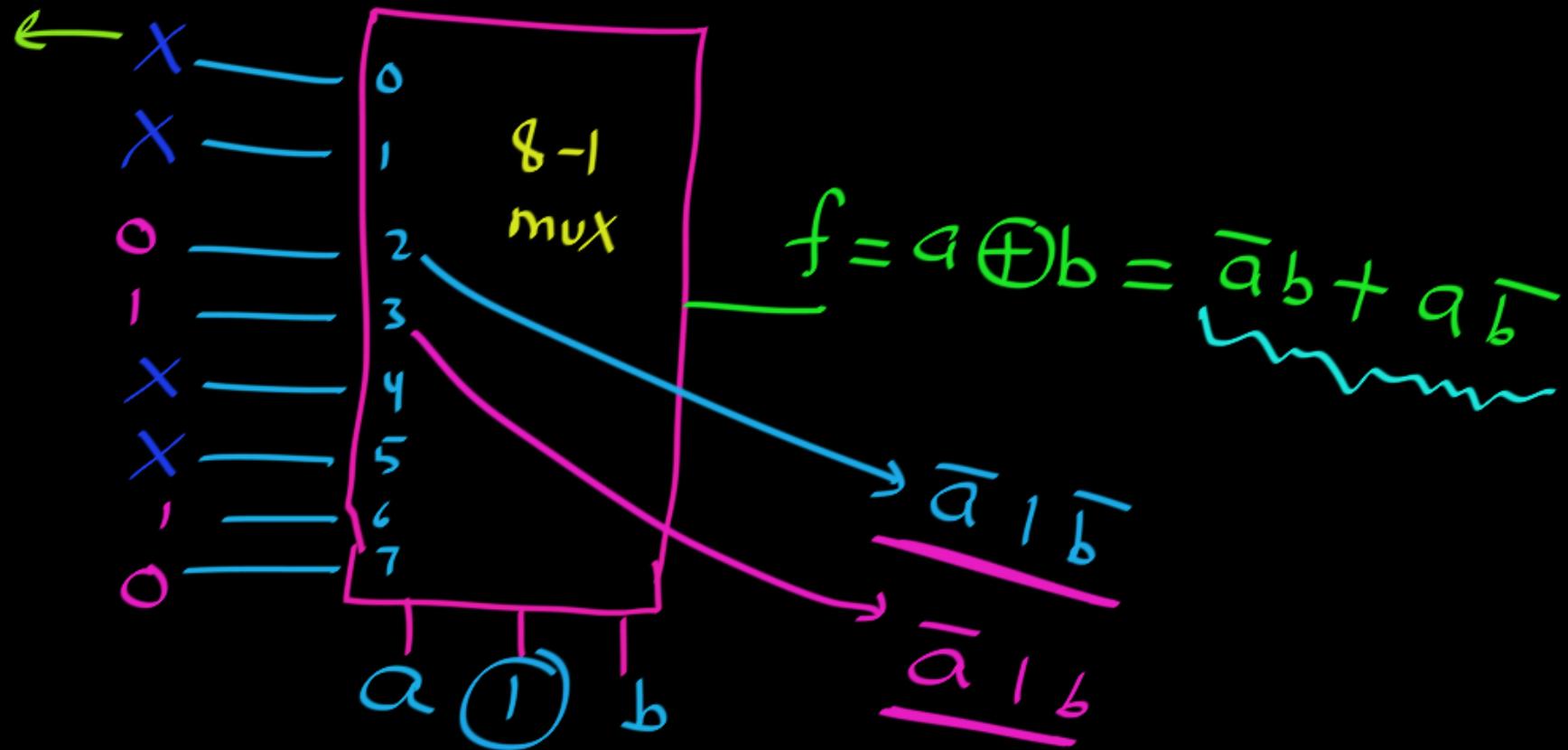


$\Phi: f(a, b) = a \oplus b$  using 8x1 mux.



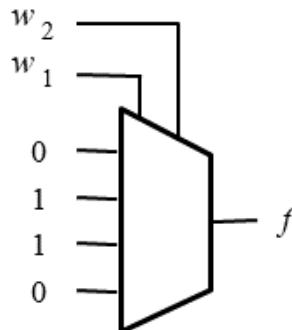
$\Phi$ :  $f(a, b) = a \oplus b$  using 8X1 mux.

Don't Care



# Implementation of a logic function with a 4x1 multiplexer

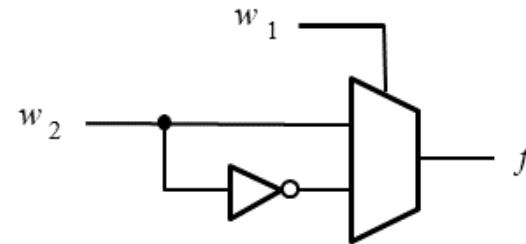
$w_1$	$w_2$	$f$
0	0	0
0	1	1
1	0	1
1	1	0



# Implementation of the same logic function with a 2x1 multiplexer

$w_1$	$w_2$	$f$
0	0	0
0	1	1
1	0	1
1	1	0

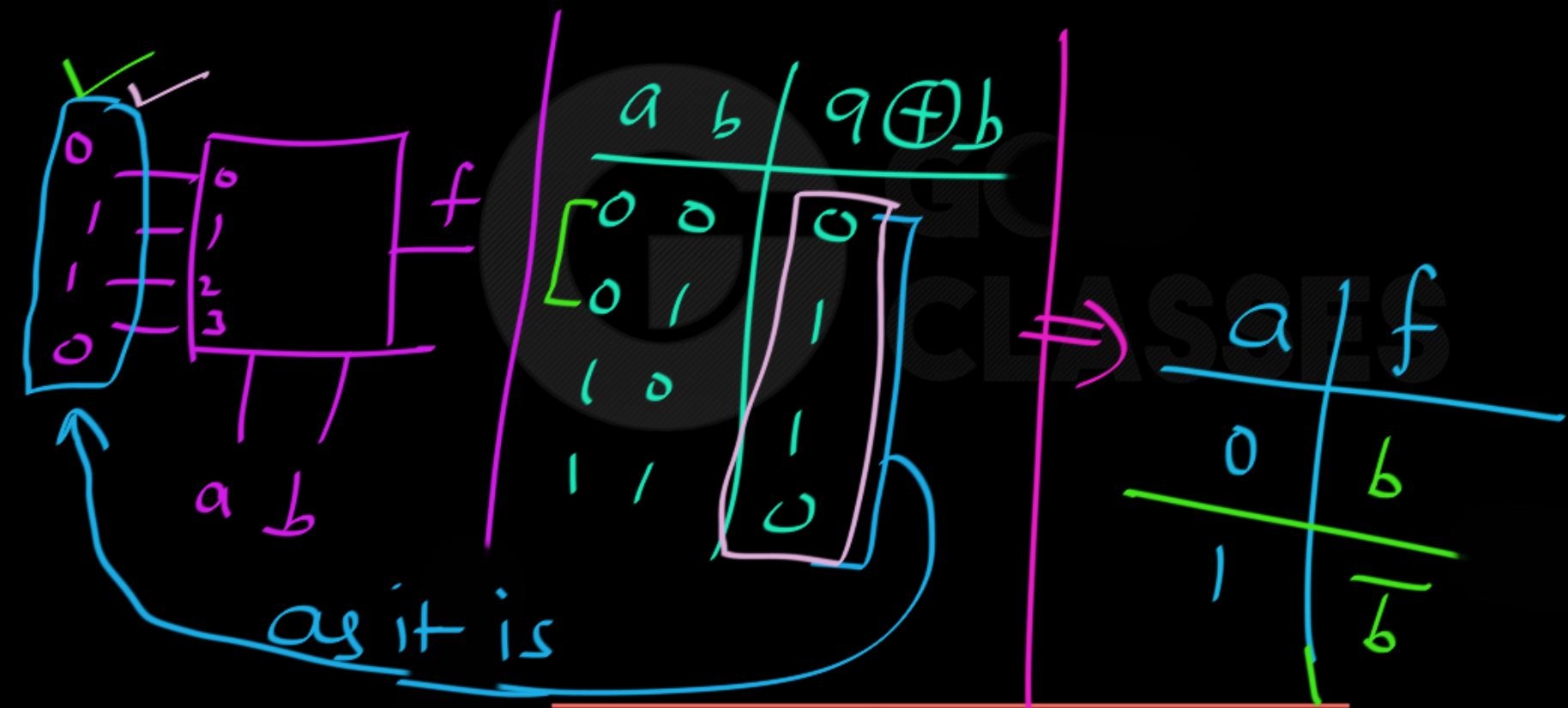
(b) Modified truth table



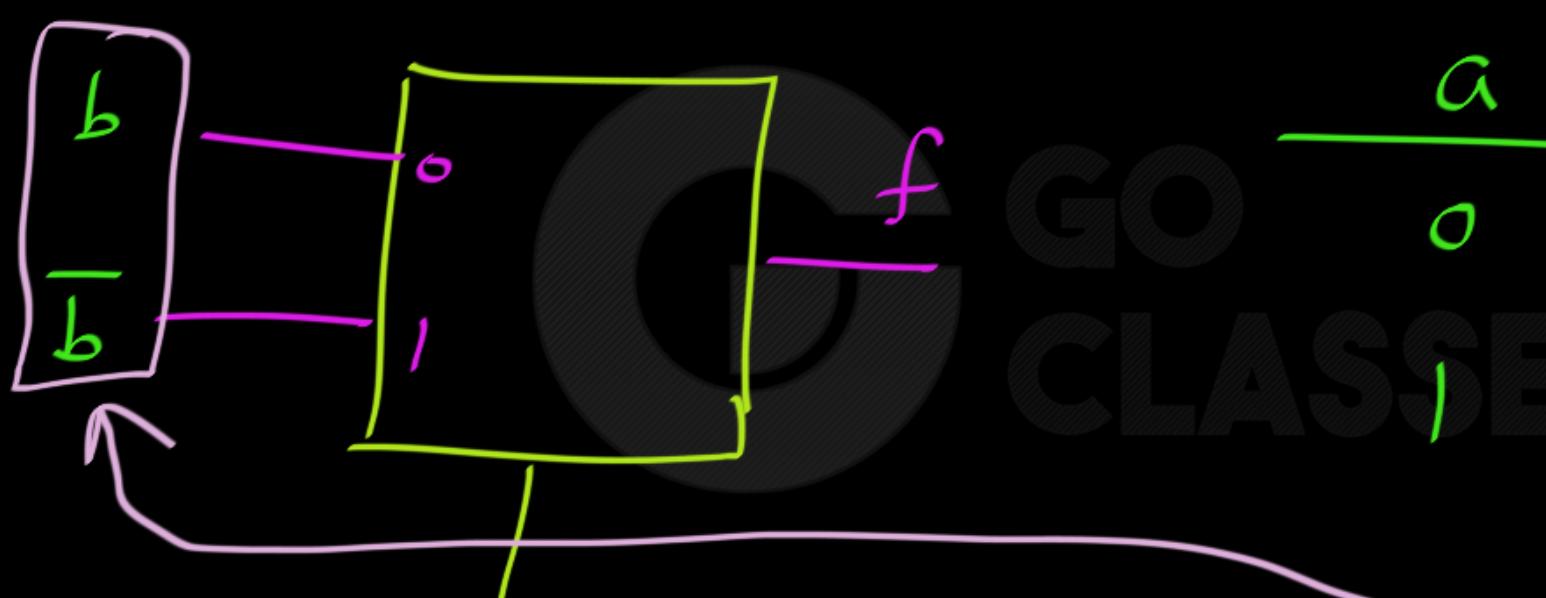
(c) Circuit

$$f(a, b) = a \oplus b \Rightarrow \text{Best mux: } 4 \times 1 \rightarrow$$

2 select lines



$$f(a,b) = \underline{a \oplus b} \Rightarrow \underline{\text{using } 2X1}$$

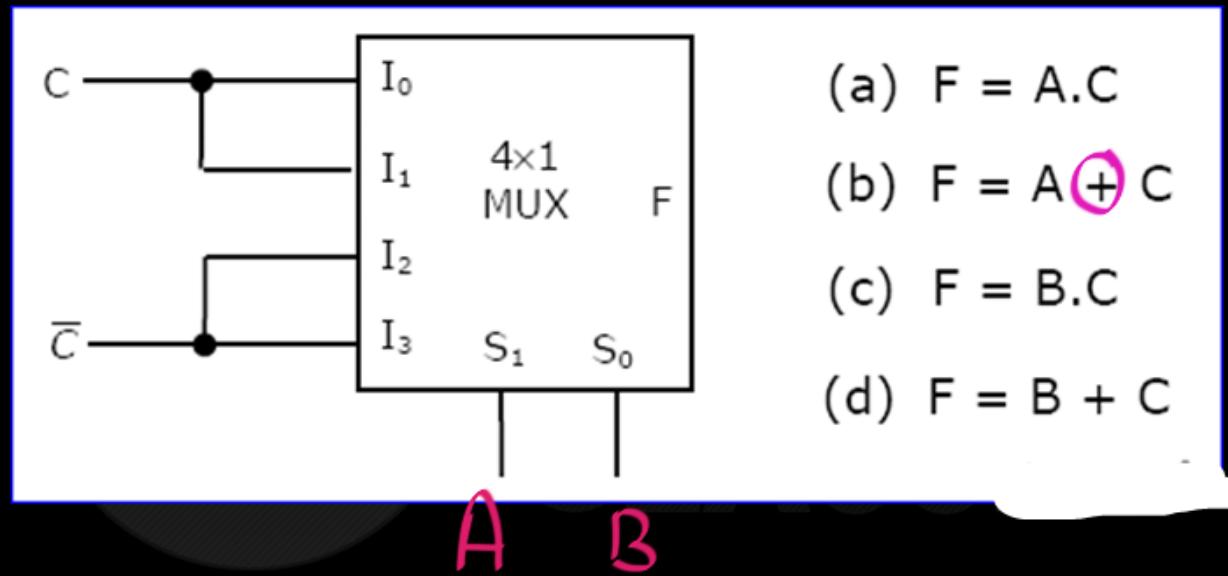


$a$	$f(a,b)$
0	$b$
1	$\bar{b}$

$s = a$   $\Rightarrow$  Control input



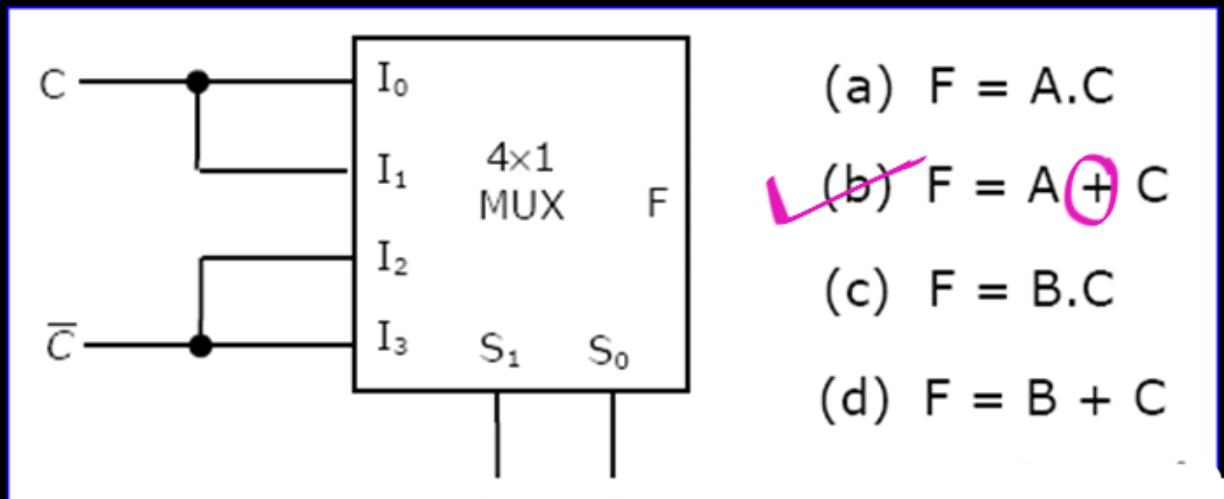
$\varphi$ :



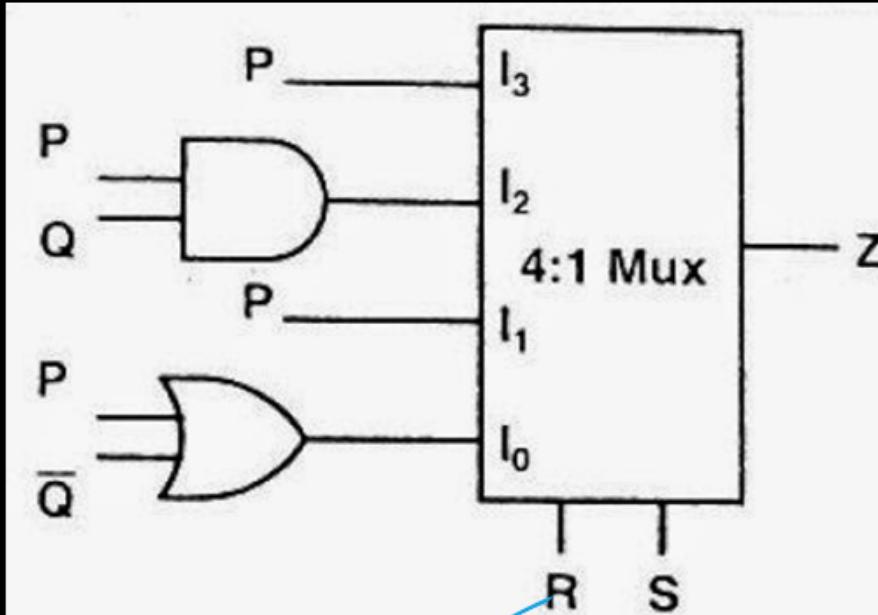
- (a)  $F = A.C$
- (b)  $F = A + C$
- (c)  $F = B.C$
- (d)  $F = B + C$



$\varphi$ :



$$\begin{aligned} F &= [\overline{A} \overline{B} C + \overline{A} B C] + [A \overline{B} \overline{C} + A B \overline{C}] \\ &= \overline{A} C + A \overline{C} \end{aligned}$$

 $\varphi :$ 

find z?

(a)  $PQ + P\bar{Q}S + \bar{Q}\bar{R}\bar{S}$

(b)  $P\bar{Q} + PQR + \bar{P}\bar{Q}\bar{S}$

(c)  $P\bar{Q}\bar{R} + \bar{P}QR + PQRS + \bar{Q}\bar{R}\bar{S}$

(d)  $PQR\bar{R} + PQR\bar{S} + \bar{P}\bar{Q}\bar{R}S + \bar{Q}\bar{R}\bar{S}$

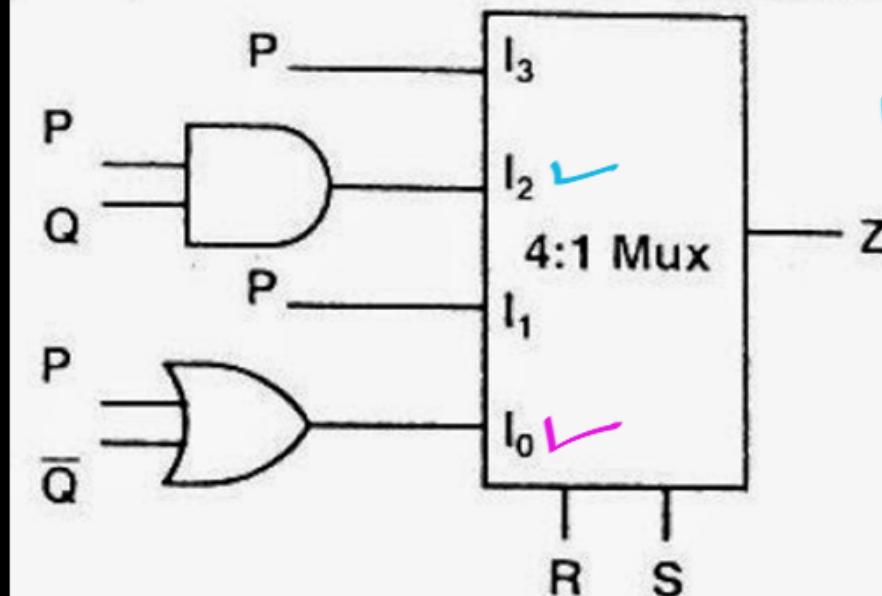
MSB

$\varphi :$ 

$R=0$

$S=1$

$Z=P$

*What is Z?*

(a)  $PQ + P\bar{Q}S + \bar{Q}\bar{R}\bar{S}$

(b)  $P\bar{Q} + PQR + \bar{P}\bar{Q}\bar{S}$

(c)  $P\bar{Q}\bar{R} + \bar{P}QR + PQRS + \bar{Q}\bar{R}\bar{S}$

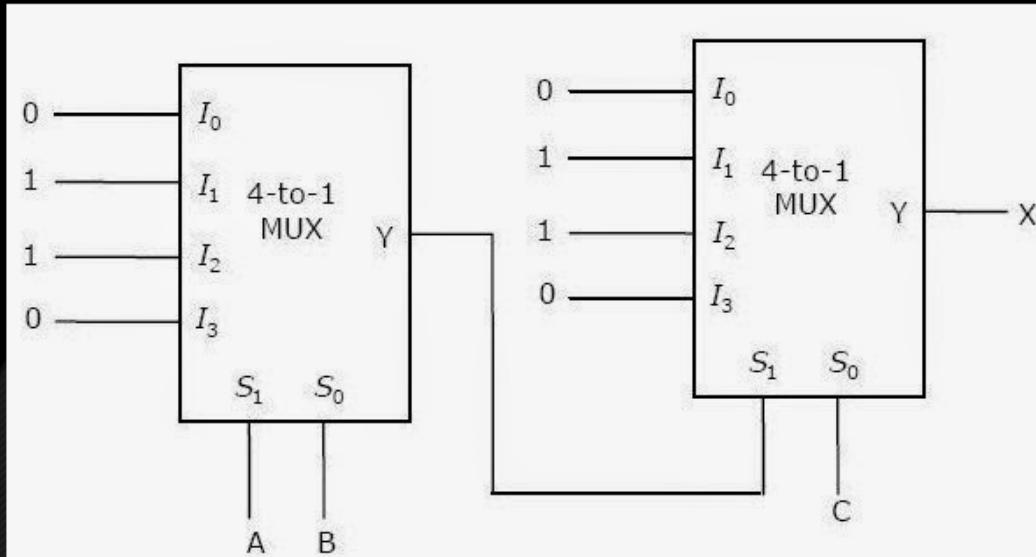
(d)  $PQR + PQR\bar{S} + P\bar{Q}\bar{R}S + \bar{Q}\bar{R}\bar{S}$

$R=0, S=0$   
 $Z=P+\bar{Q}$

$R=S=1$   
 $Z=P$

Option b X  
|| c X  
|| d X

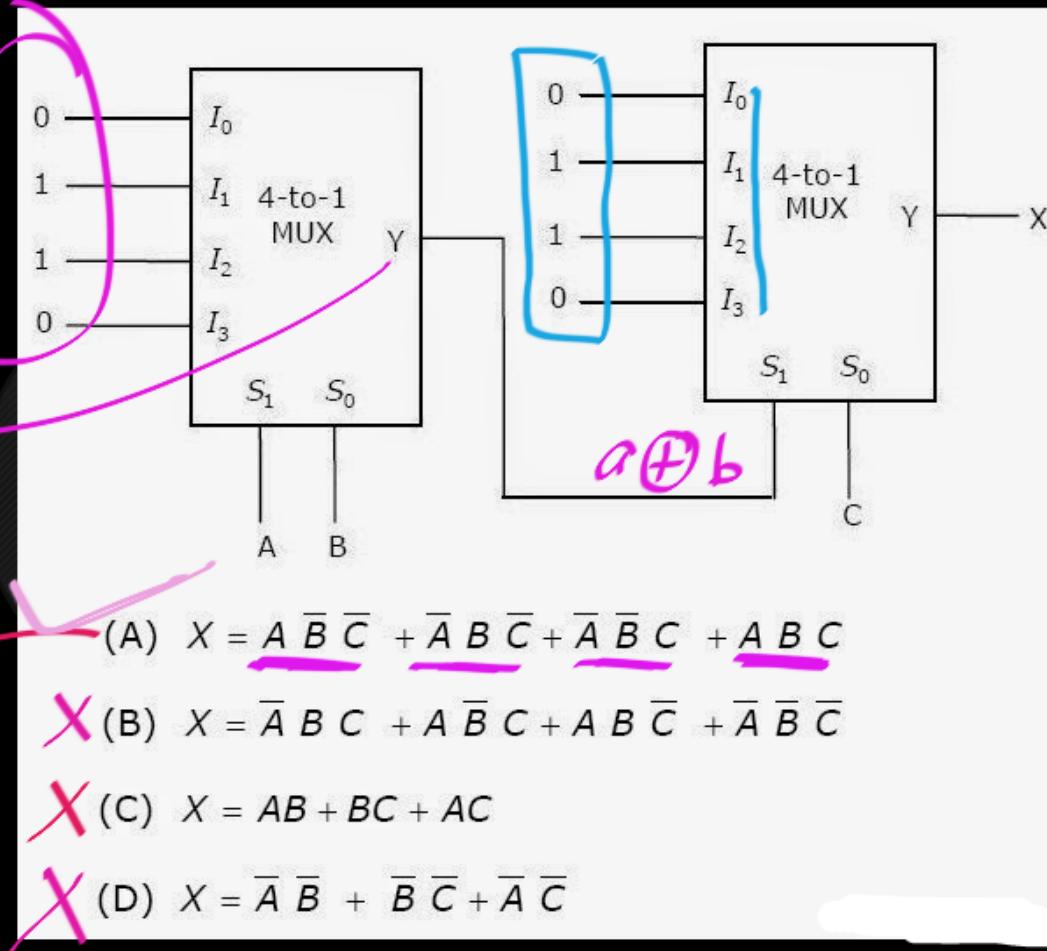
$R=1, S=0$   
 $Z=PQ$



- (A)  $X = A \bar{B} \bar{C} + \bar{A} B \bar{C} + \bar{A} \bar{B} C + A B C$
- (B)  $X = \bar{A} B C + A \bar{B} C + A B \bar{C} + \bar{A} \bar{B} \bar{C}$
- (C)  $X = AB + BC + AC$
- (D)  $X = \bar{A} \bar{B} + \bar{B} \bar{C} + \bar{A} \bar{C}$

$$\underline{Y = A \oplus B}$$

$$\checkmark \underline{A \oplus B \oplus C}$$



$$x = (a \oplus b) \oplus c$$

$$x = s_1 \oplus s_0$$

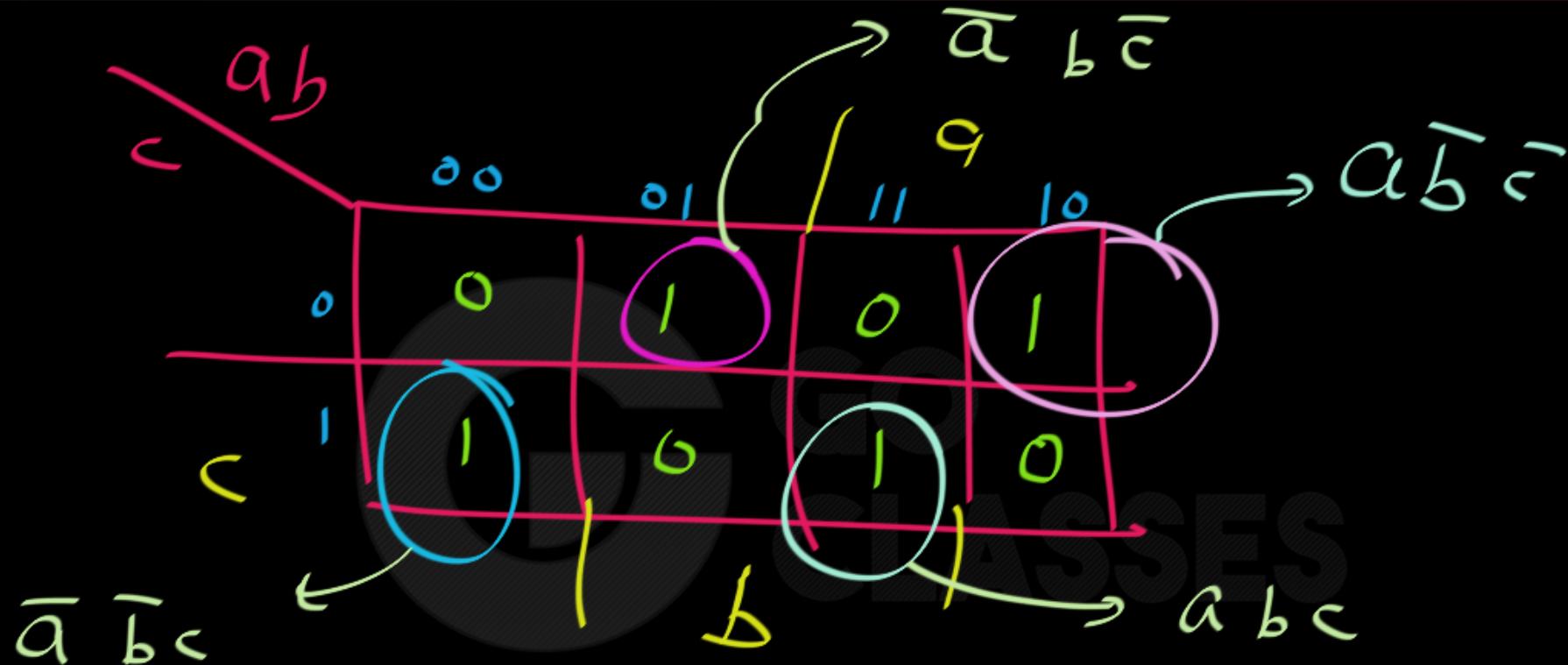
$$= (a \oplus b) \oplus c$$

$$= a \oplus b \oplus c$$

Exor

= " odd function"

means: Exor = 1 iff odd number of  
inputs are 1.



$$f = a \oplus b \oplus c$$

odd function

$$a \oplus b \oplus c = a\bar{b}\bar{c} + \bar{a}bc + \bar{a}\bar{b}c + \bar{a}b\bar{c}$$

$$f = \underbrace{a \oplus b \oplus c}_{\text{odd function}}$$

$$f = \underbrace{abc}_{\text{all 1}} + \overbrace{\bar{a}\bar{b}c}^{\text{OR}} + \overbrace{a\bar{b}\bar{c}}^{\text{Exactly one}} + \overbrace{\bar{a}b\bar{c}}$$

$$f = a \oplus b \oplus c \oplus d$$

Odd fun

$f = 1$  iff  
odd number  
of inputs are 1.

$f =$  Exactly one is 1

OR      Exactly three are 1

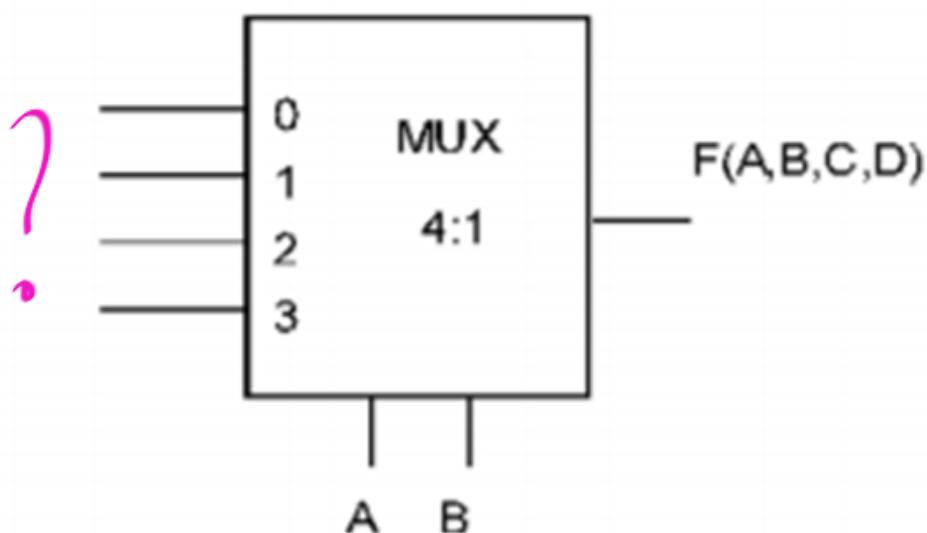
$$\overline{a} \overline{b} \overline{c} \overline{d} + \overline{a} \overline{b} c \overline{d} + \\ \overline{a} b \overline{c} \overline{d} + a \overline{b} \overline{c} \overline{d}$$

$$+ \quad \begin{array}{l} \overline{a} b c \overline{d} + a \overline{b} c \overline{d} \\ + a b \overline{c} \overline{d} + a b c \overline{d} \end{array}$$



(a) A logic function is given as  $F(A,B,C,D) = AD + BC + \overline{A+B+C}$

Show how to implement this function by a 4:1 MUX with (A, B) as control inputs (clearly label every input)



$$f(a, b, c, d) = \frac{ad}{\cancel{bc}} + \frac{bc}{\cancel{ad}} + \frac{\bar{a}\bar{b}\bar{c}}{\cancel{d}}$$

$$1 - - 1 \quad - 11 - \quad 000 -$$

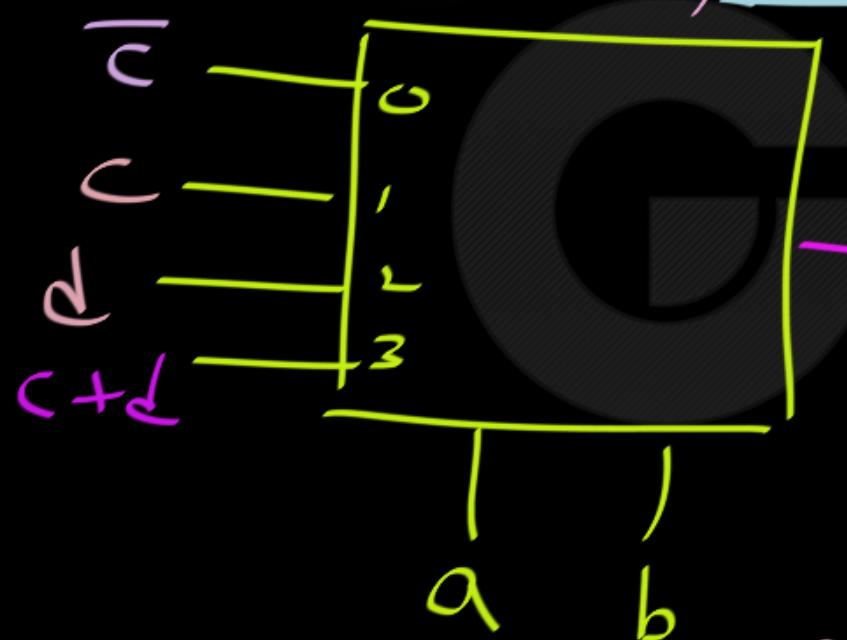
$$\left\{ \begin{array}{l} 9 \\ 11 \\ 13 \\ 15 \end{array} \right\}$$

$$\left\{ \begin{array}{l} 6 \\ 7 \\ 14 \\ 15 \end{array} \right\}$$

$$\left\{ \begin{array}{l} 0000 = h_0 \\ 0001 = h_1 \end{array} \right.$$

$$f = ad + bc + \underline{ab\bar{c}\bar{d}}$$

$$f = \sum(0, 1, 6, 7, 9, 11, 13, 14, 15)$$



method 1:

find CSOP of f.

with  $\bar{a}\bar{b} \Rightarrow m_0, 1$

$\bar{a}\bar{b}(\bar{c}\bar{d} + \bar{c}d)$

with  $\bar{a}b \Rightarrow m_6, 7$

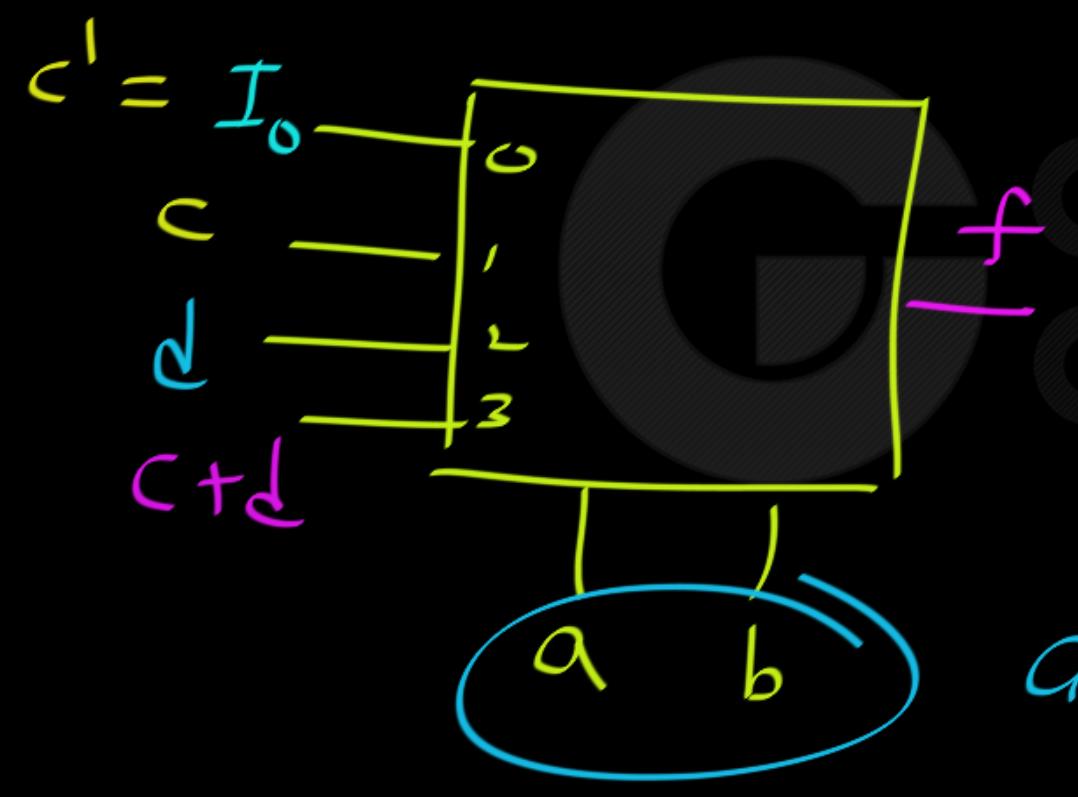
$\bar{a}b(c\bar{d} + cd)$

with  $\underline{ab} \Rightarrow m \underline{13, 14, 15} \rightarrow 1101$

$ab(\bar{c}\downarrow + \frac{\bar{c}\bar{d} + cd}{\bar{c}\downarrow + c}) \rightarrow 1110$

$= (\bar{c} + d)$

$$f = \underbrace{ad + bc}_{c'} + \underbrace{ab'c'}_{d'} \quad \underline{\text{method 2}}$$



$I_0$  means  $f$  when  $a=0$

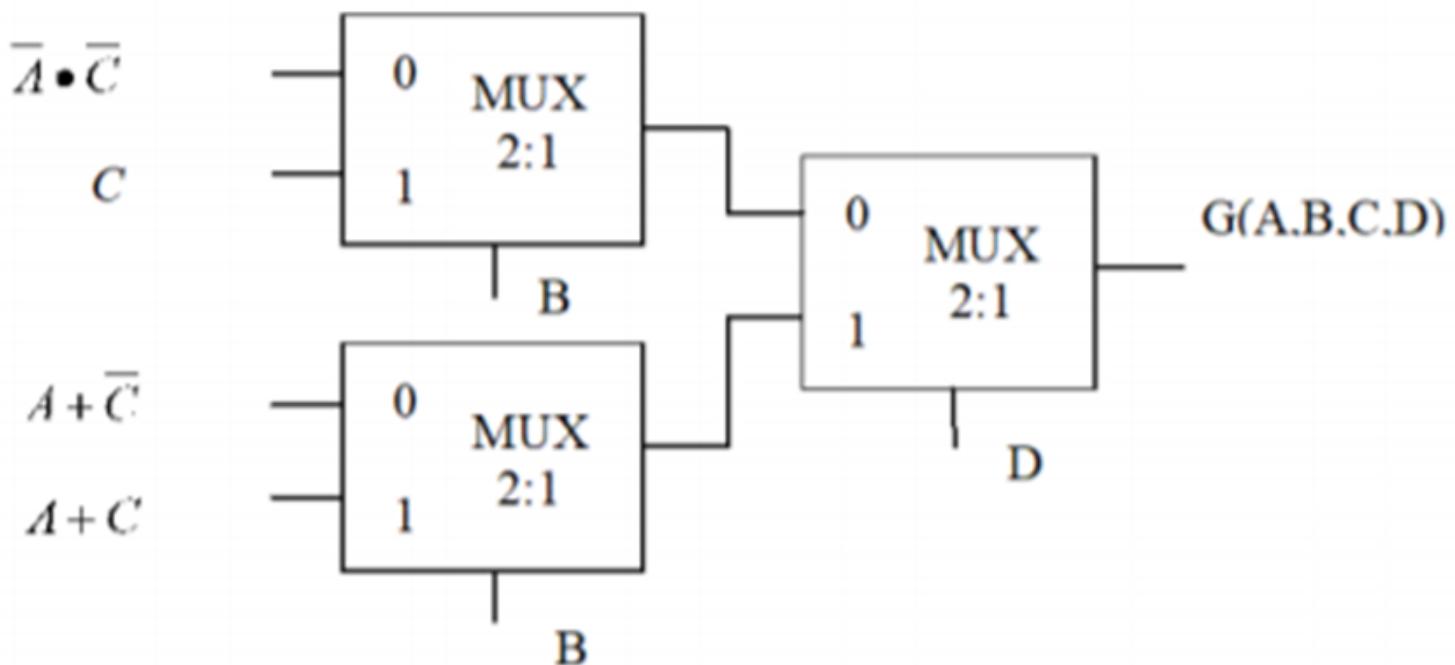
When  $a=0, b=0 \Rightarrow f = c'$

~~$a=0, b=1 \Rightarrow f = c'$~~

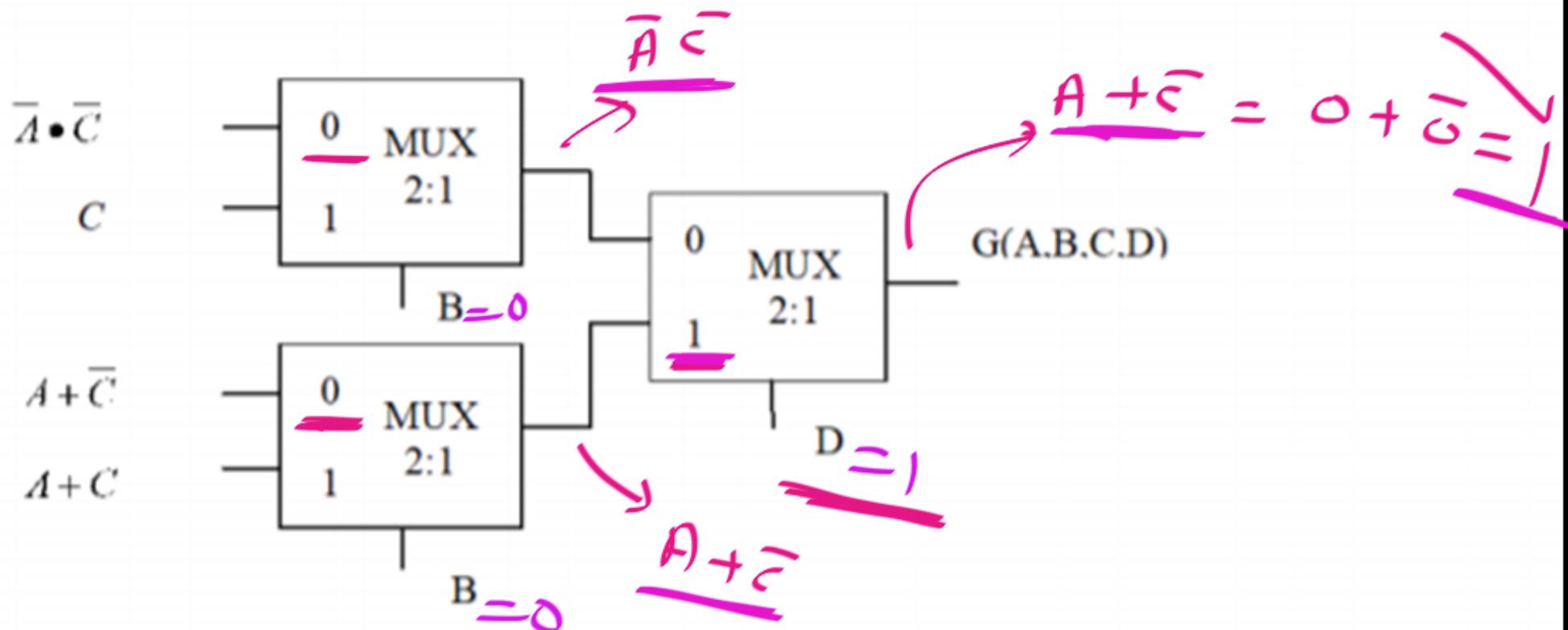
~~$a=1, b=0 \Rightarrow f = c'$~~

$a=1, b=1 \Rightarrow f = d'$

(b) Determine the output function  $G(A,B,C,D)$  when  $ABCD = 0001$  for the schematic given below:



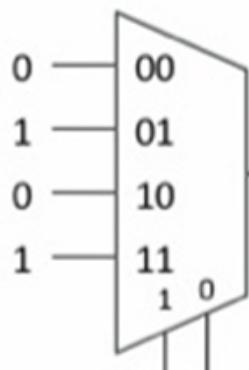
(b) Determine the output function  $G(A,B,C,D)$  when  $\underline{ABCD} = 0001$  for the schematic given below:



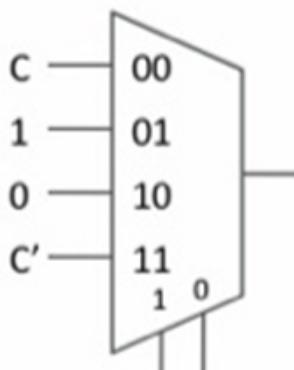
## Question #7

- Implement the given logic function using an 4-to-1 multiplexer.

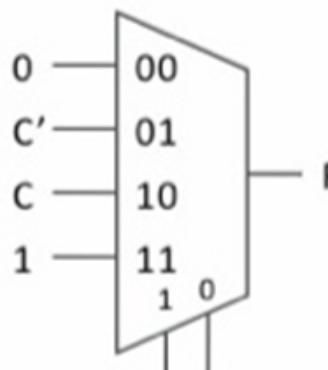
$$F(A, B, C) = B.C' + A'.C$$



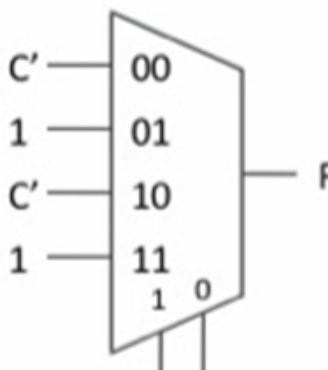
(a)



(b)



(c)



(d)

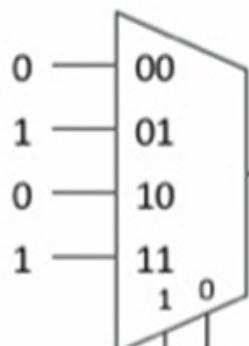
- (e) None of the above.

## Question #7

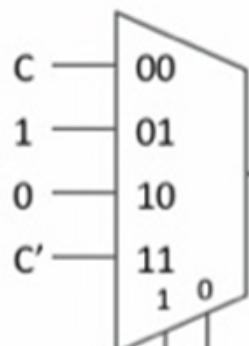
- Implement the given logic function

$$F(A, B, C) = B.C' + A'.C$$

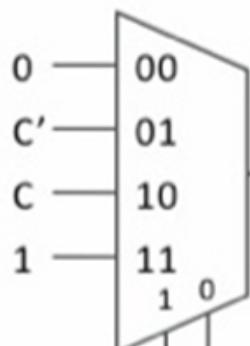
A	B	$f(a, b, c)$	
0	0	C	
0	1		1
1	0		0
1	1	C	



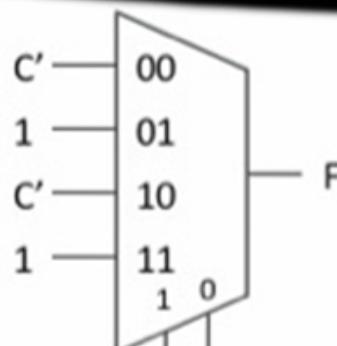
(a)



(b)



(c)

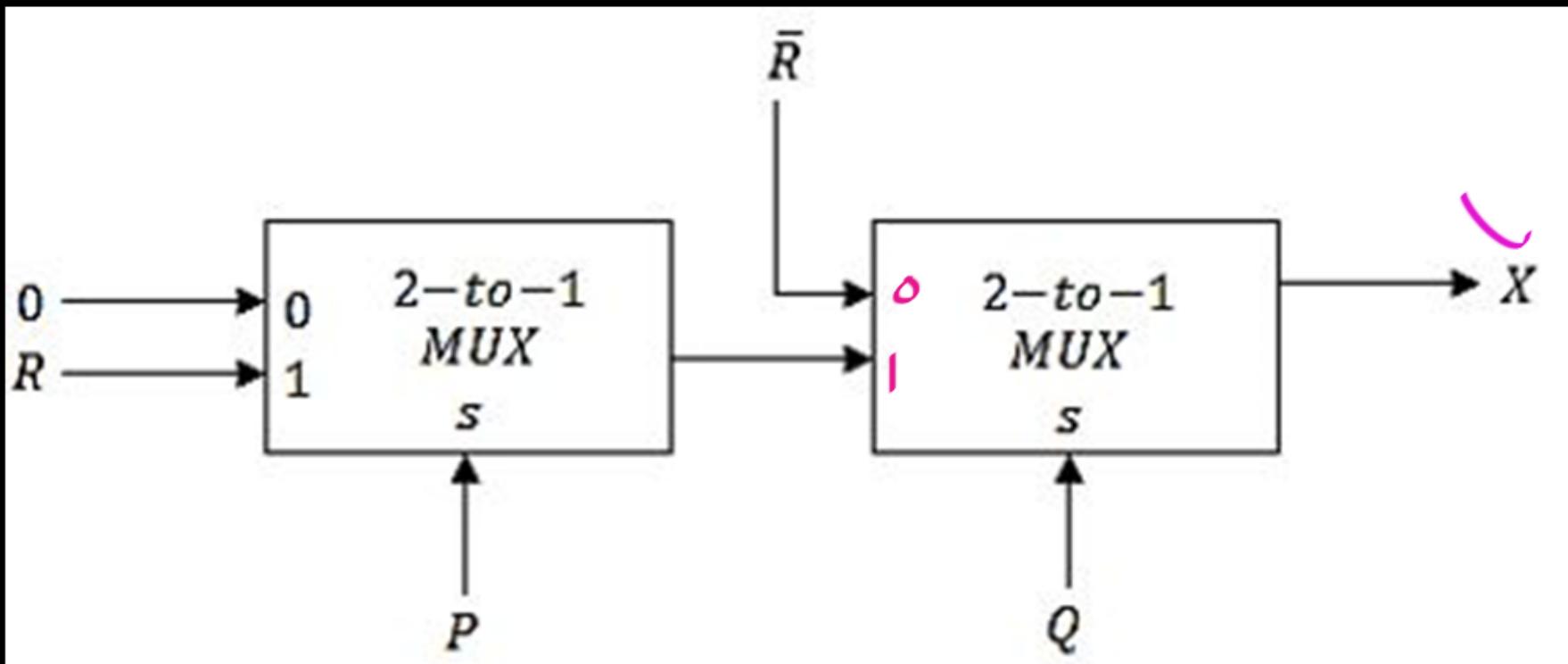


(d)

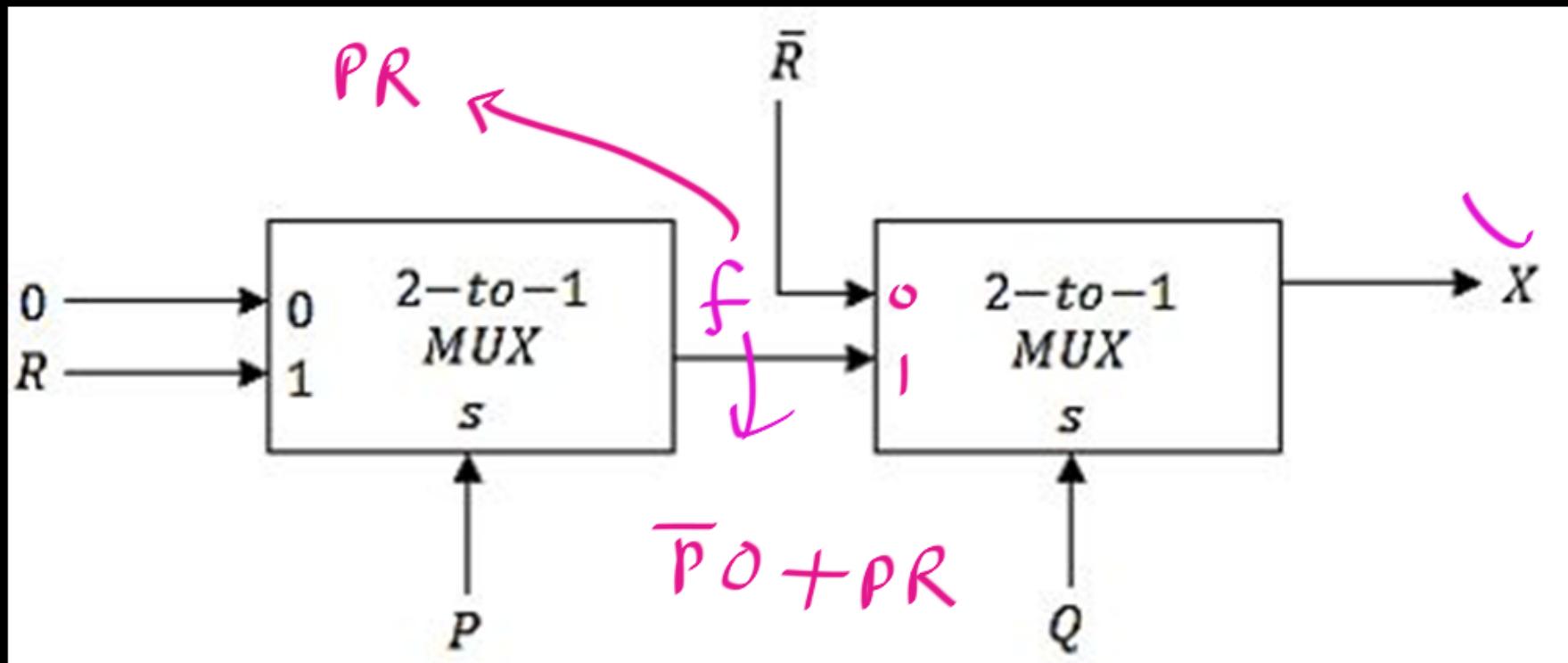
(e) None of the above.



Q:



Q:



$$X = \overline{Q}(\bar{R}) + Q(PR) = \underline{\bar{Q}\bar{R}} + \underline{PQR}$$