



Homework 1



Question 1

If we have seven (7) bits to represent integers, what is largest unsigned number and what is largest 2s complement signed number we can represent (in decimal **and** binary)?

Largest unsigned:

Most positive signed:





Solution:

Largest unsigned:

1111 111 (127)

Most positive signed:

0111 111 (63)





Question 2

Complete the following table. Use the fewest number of bits on each case.

Decimal	2's complement
-256	
-154	
-107	
135	



Solution:

Complete the following table. Use the fewest number of bits on each case.

Decimal	2's complement
-256	100000000
-154	101100110
-107	10010101
135	010000111



Question 3

- Convert the decimal number -67 to 8-bit, signed 2's complement binary. **Hint: $67 = 0100\ 0011$**
- Convert the 16-bit signed 2's complement binary number 1001 0001 1111 1010 to decimal **Hint: We can apply method 1 or method 2 to get answer**
- Give the 8 bit 2's complement representation of the integer -23.
- Give the 32 bit 2's complement representation of the integer -23.



Solution

- Convert the decimal number -67 to 8-bit, signed 2's complement binary.

$$-67 = 1011\ 1100 + 1 = 1011\ 1101$$

- Convert the 16-bit signed 2's complement binary number 1001 0001 1111 1010 to decimal

We can apply method 1 or method 2 to get answer

- Give the 8 bit 2's complement representation of the integer -23.

11101001

- Give the 32 bit 2's complement representation of the integer -23.

11111111111111111111111111111111 11101001





Question 4

GATE CSE 2003

Assuming all numbers are in 2^s complement representation, which of the following numbers is divisible by 1111011?

- A. 11100111
- B. 11100100
- C. 11010111
- D. 11011011





Solution

GATE CSE 2003

Assuming all numbers are in $2's$ complement representation, which of the following numbers is divisible by 1111011 ?
=-5

- A. 11100111 =-25
- B. 11100100 =-28
- C. 11010111 =-41
- D. 11011011 =-37

A is correct





Question 5

GATE CSE 2016 Set 1

The 16-bit 2's complement representation of an integer is
1111 1111 1111 0101; its decimal representation is _____





Solution

GATE CSE 2016 Set 1

The 16-bit 2's complement representation of an integer is
1111 1111 1111 0101; its decimal representation is _____

We can apply method1 or method 2 to get answer

Using Method2-
MSb is 1 => number is negative

Take 2's complement of given binary.
=1000 0000 0000 1011
=11 (in decimal)

Note:- we can also ignore leading one's except first one before solving using any method

Hence answer is -11





Question 6

Suppose you are given the following 4-bit binary number: **0101**.

You're not told whether or not the number is signed or unsigned. Is this information important in knowing what the value of the number is, in decimal? That is, do you need to know if it's signed or unsigned to say what the decimal value is? Why or why not?





Solution

Suppose you are given the following 4-bit binary number: **0101**.

You're not told whether or not the number is signed or unsigned. Is this information important in knowing what the value of the number is, in decimal? That is, do you need to know if it's signed or unsigned to say what the decimal value is? Why or why not?

Since MSb is 0 hence it does not matter if we treat this number as signed or unsigned. We will get same decimal





Question 7

In 5 bits, what is the most negative value and the most positive value representable in signed form, using two's complement? Express your answers in both binary and decimal.

Same question as above, but representable in unsigned form?





Solution

In 5 bits, what is the most negative value and the most positive value representable in signed form, using two's complement? Express your answers in both binary and decimal.

Most negative: 10000, -16

Most positive: 01111, 15

Same question as above, but representable in unsigned form?

You cannot represent negative numbers with unsigned binaries.

Most positive: 11111, 31





Question 8

Convert these unsigned binary numbers into decimal.

- a. 1010
- b. 10101010
- c. 11000001

Convert these signed binary numbers into decimal.

- a. 1010
- b. 00110100
- c. 11000001





Solution

Convert these unsigned binary numbers into decimal.

- a. 1010 **10**
- b. 10101010 **170**
- c. 11000001 **193**

Convert these signed binary numbers into decimal.

- a. 1010 **-6**
- b. 00110100 **52**
- c. 11000001 **-63**





Bonus Question GATE CSE 2022

Let R1 and R2 be two 4-bit registers that store numbers in 2's complement form. For the operation $R1 + R2$, which one of the following values of R1 and R2 gives an arithmetic overflow?

- A. $R1 = 1011$ and $R2 = 1110$
- B. $R1 = 1100$ and $R2 = 1010$
- C. $R1 = 0011$ and $R2 = 0100$
- D. $R1 = 1001$ and $R2 = 1111$

<https://gateoverflow.in/371928/Gate-cse-2022-question-8>





2's complement range for 4 bits = $[-8, 7]$

Option **A**

$R1 = 1011 = -5$ and $R2 = 1110 = -2$. $R1 + R2 = -7$ No overflow

Option **B**

$R1 = 1100 = -4$ and $R2 = 1010 = -6$. $R1 + R2 = -10$ **Overflow**

Option **C**

$R1 = 0011 = 3$ and $R2 = 0100 = 4$. $R1 + R2 = 7$ No overflow

Option **D**

$R1 = 1001 = -7$ and $R2 = 1111 = -1$. $R1 + R2 = -8$ No overflow

