# The SRE's Crystal Ball

Predicting Performance with Queues and USL



Aravindh Sampathkumar Booking.com October 09, 2025

#### About Me

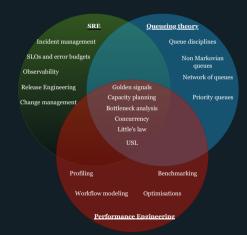
#### **Aravindh Sampathkumar**

Site Reliability Engineer @ Booking.com

#### Background

- High Performance Computing (HPC)
- Storage Systems
- Performance Engineering

## The big picture



### The big picture

- Let's have some fun.
- Aimed at inspiring you, my peer practitioners to apply these concepts in ways I haven't thought of.
- A system/service is a chain of bottlenecks removing one reveals the next.

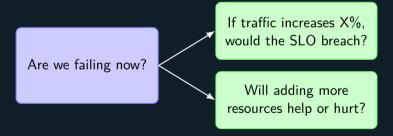
#### **Credits**

- Dr. Neil J. Gunther authored Universal Scalability Law and taught GCAP workshop.
- Stefan Moeding maintains the R package that I use in Demo.

#### Why bother?

#### Most SLOs are reactive alarms

- Availability SLO Miss: "We're down."
- Latency SLO Miss: "We're slow."



Move from firefights to preventing *some* issues entirely — think in **queues** and **scalability models**.

### Agenda

- Thinking in queues
- Golden signals through the lens of queueing theory
- Predicting scalability with Universal Scalability Law(USL)
- See it in action

## The Birth of Queueing Theory



Figure: A. K. Erlang (1878-1929) Source: Wikipedia

- In the early 1900s, Danish mathematician **Agner Krarup Erlang** had to figure out how many telephone circuits were needed to handle a given number of calls without excessive waiting or dropped connections.
- His work created queueing theory the mathematical study of waiting lines (or queues).

## Thinking in queues

- Queues are everywhere Loadbalancers, connection pooling, Jira boards...
- Queueing systems are non-linear It is not intuitive. Double the instance count and you can serve double the load right?
- Queues occur even if there is enough average capacity Grocery store
  - High variance in arrvivals
  - High variance in service times

## Thinking in queues

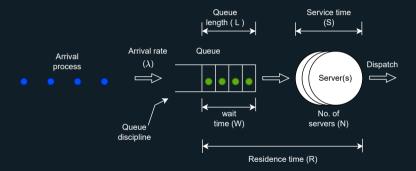


Figure: A simple queue.

## Thinking in queues - Terminology

Queue length (L)	Number of requests in the system or queue $(L_q)$
Arrival Rate $(\lambda)$	The rate at which requests enter the system (e.g., requests/sec). aka "demand" or "load".
Service Time (S)	The time required for a single server to process one request.
Waiting Time ( <i>W</i> )	The time a request spends waiting in the queue before its service begins.
Response Time aka Latency $(R)$	The total time a request is in the system. The sum of waiting and service time $(R=W+S)$ .
Utilization $( ho)$	The fraction of time a server is busy.
Number of servers (N)	The number of servers in the system(node/cpu/thread/instance).
Throughput $(X)$	Completion rate of requests. In a stable system, $(X = \lambda)$ .

## Golden signals 60 through queueing theory

- Latency = Service time + Waiting time
  - Utilisation drives waiting time
  - Coefficient of variation is a leading indicator
- Traffic as Arrival rate( $\lambda$ ): The demand driver
- Errors as symptoms of overload
- Saturation as high Utilisation( $\rho$ ): The harbinger of Doom

#### Little's Law and Related Formulae

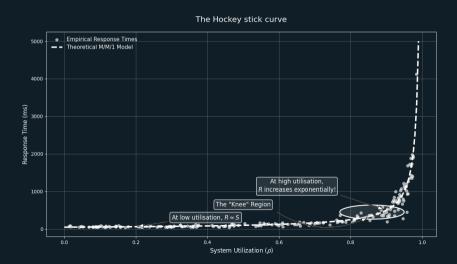
$$L = \lambda R$$

$$\rho = \lambda S$$

or

$$ho = rac{\lambda S}{N}$$

#### Utilisation curve and the "Knee"



#### A little intuition

Which design performs better?









An API endpoint ('/api/v1/resource') is timing out. Latency has spiked!

♣ An API endpoint ('/api/v1/resource') is timing out. Latency has spiked!

What do we know?

- Arrival Rate ( $\lambda$ ): 180 requests/second.
- Avg. Service Time (S): 50 milliseconds per request.
- Number of Servers (N): 4 API server pods.

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- Arrival Rate ( $\lambda$ ): 180 requests/second.
- Avg. Service Time (S): 50 milliseconds per request.
- Number of Servers (N): 4 API server pods.

- "Should we scale up to 8 pods? "
- "Would it be enough?"

$$\rho = \frac{\lambda S}{N} = \frac{\text{Arrival Rate} \times \text{Service Time}}{\text{Number of Servers}}$$
 
$$\rho = \frac{180 \text{ req/s} \times 0.05 \text{ s/req}}{4 \text{ pods}} = \frac{9}{4} = \textbf{2.25}$$

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- Utilisation ( $\rho > 1.0$  or 100%)  $\Rightarrow$  the system is unstable. In other words, the queue is growing infinitely.
- Increase N to 8 pods?  $\Rightarrow \rho$  will compute to 1.125 (still > 1.0).
- Let's increase N to at least 10 pods (ho=0.9) to also accommodate variance.

## USL

I promised a crystal ball. Lets do some predictions.

#### USL

#### Scalability

A mathematical function of being able to perform more work (RPS, TPS etc) while work per server<sup>1</sup> remains constant and the number of servers increases.\*

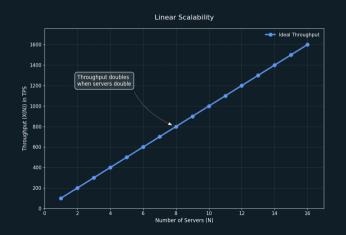
#### Universal Scalability Law(USL)

A formal definition of scalability.

<sup>(</sup>node/instance, cpu/thread etc)
Improvised from a definition by Dr. Neil J Gunther

#### USL - Linear Scalability

The ideal condition. We all want that right?

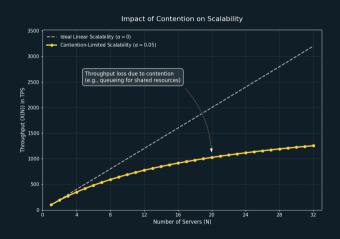


$$X(N) = \frac{\gamma N}{1}$$

#### Where:

- X(N) is the throughput with N servers.
- lacksquare  $\gamma$  is the ideal throughput of a single server.
- *N* is the number of servers.

### USL - Scalability villain no.1 - Contention

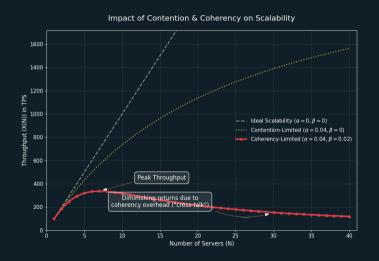


$$extstyle extstyle X( extstyle extstyle N) = rac{\gamma extstyle N}{1 + lpha ( extstyle N - 1)}$$

#### Where:

- lacksquare  $\alpha$  represents contention.
- contention is non-parallelisable serialised work.

## USL - Scalability villain no.2 - Coherency (a.k.a. Crosstalk)



#### USL

$$X(N) = \frac{\gamma N}{1 + \alpha(N-1) + \beta N(N-1)}$$

#### Where:

- lacksquare  $\gamma$  represents ideal single server throughput.
- lacksquare  $\alpha$  represents contention.
- lacksquare  $\beta$  represents coherency penalty.

#### USL - What do we do with it?

#### Model system/scalability (obviously).

- 1. Apply observed system/service behaviour metrics.
- 2. Estimate  $\alpha$ ,  $\beta$ , and  $\gamma$  using non-linear least squares regression.
- 3. Interpret the results to know scalability limits and improve bottlenecks.

USL

Demo

#### USL - Limits

- Noisy data real-world data is quite noisy(network jitter, OS scheduler, GC pauses etc.).
- Distributed systems harder to model aggregate functions(/order depends on 10 microservices).
- Asynchronous and event driven architecture pattern is hard to model.
- Coherency factor( $\beta$ ) assumes 1-1 coordination.
- Systems dont always behave the same way at scale. E.g switch to a different algorithm or co-ordinate in batches etc.
- Noisy neighbours multi-tenancy.
- Rate limits and throttling at dependencies.

## Common pitfalls - USL

Keep these in mind while working with USL.

- Garbage In Garbage Out be diligent about noise. Noise will have non linear effects.
- Over-extrapolation Dont forecast too far(new constraints emerge at scale). 2x is the rule of thumb.
- Max throughput if often NOT the goal max throughput @desired latency is.

### Key takeaways

- Start thinking in queues. Enrich your monitoring capture service times and waiting times in histograms, queue lengths.
- Use Little's law for napkin math of fundamental relationship between Utilisation, Throughput/arrival rate, and response time.
- Use USL as a diagnostic compass to identify coarse contention and coherance penalties - rethink design choices to achieve practical goals.
- Keep queing theory wisdom in mind while designing services:
  - Favour pooled resources single queue and a shared pool of workers.
  - Attack variability Use caching strategies, optimisations for slower code paths etc to reduce service time variability.
  - Heavy-tailed service times? consider priority queues or size based routing.

## References and further reading

- Dr. Neil J Gunther's page on Scalability and USL.
- Baron Schwartz's The essential Guide to QueueingTheory.
- Neil J. Gunther and Stefan Moeding's USL R package
- Eben Freeman's LISA 17 talk on Queueing theory in practice
- Kavya Joshi's talk on Applied Performance Theory.

#### Thank You!

#### Questions?

#### Get in Touch

■ 
: aravindh at fastmail.com

■ in : linkedin.com/in/aravindhsampath

■ **(?)**: github.com/aravindhsampath

■ Bluesky : aravindh.net

#### Slides Available At

aravindh.net/srecon2025.pdf