

Question-7-7.2-26

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Question:

The centre of circle is $(2a, a - 7)$. Find the values of a if the circle passes through the point $A(11, -9)$ and has diameter $10\sqrt{2}$ units

Solution:

Description	Given value
point C	$(2a, a - 7)$
Diameter	$10\sqrt{2}$
point A	$(11, -9)$

TABLE 0: variables used

The radius of circle is $\frac{\text{diameter}}{2}$

$$\Rightarrow \text{radius} = 5\sqrt{2} \quad (0.1)$$

$$\|\mathbf{A} - \mathbf{C}\| = 5\sqrt{2} \quad (0.2)$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} 11 - 2a \\ -2 - a \end{pmatrix} \quad (0.3)$$

$$(11 - 2a)^2 + (2 + a)^2 = 50 \quad (0.4)$$

$$a^2 - 8a + 15 = 0 \quad (0.5)$$

$$(a - 3)(a - 5) = 0 \quad (0.6)$$

$$\therefore a = 3 \text{ or } a = 5 \quad (0.7)$$

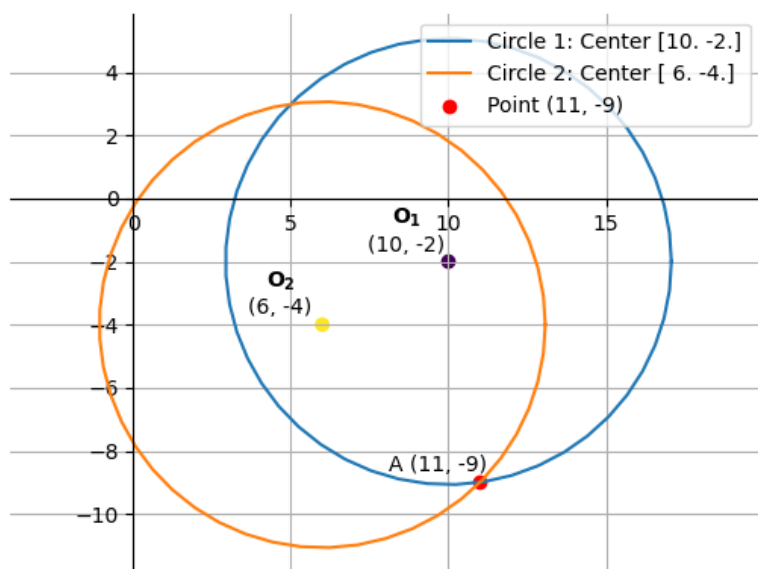


Fig. 0.1