

# 2021-August

## Session-01-09-2021-shift-2-16-20

EE24BTECH11038 - MALAKALA BALA SUBRAHMANYA ARAVIND

- 16) Let  $p_1, p_2, p_3, \dots, p_{15}$  be points on circle. The number of distinct triangles formed by points  $p_i, p_j, p_k$  such that  $i+j+k \neq 15$ , is :
- 12
  - 419
  - 443
  - 455
- 17) The range of the function,
- $$f(x) = \log_{\sqrt{5}} \left( 3 + \cos \left( \frac{3\pi}{4} + x \right) + \cos \left( \frac{\pi}{4} + x \right) + \cos \left( \frac{\pi}{4} - x \right) - \cos \left( \frac{3\pi}{4} - x \right) \right)$$
- is:
- $(0, \sqrt{5})$
  - $[-2, 2]$
  - $\left[ \frac{1}{\sqrt{5}}, \sqrt{5} \right]$
  - $[0, 2]$
- 18) Let  $a_1, a_2, a_3, \dots, a_{21}$  be an A.P such that  $\sum_{n=1}^{20} \frac{1}{a_n a_{n+1}} = \frac{4}{9}$ . If the sum of this A.P is 189, then  $a_6 a_{16}$  is equal to :
- 57
  - 72
  - 48
  - 36
- 19) The function  $f(x)$ , that satisfies the condition  $f(x) = x + \int_0^{\frac{\pi}{2}} \sin x \cdot \cos y f(y) dy$ , is :
- $x + \frac{2}{3}(\pi - 2) \sin x$
  - $x + (\pi + 2) \sin x$
  - $x + \frac{\pi}{2} \sin x$
  - $x + (\pi - 2) \sin x$
- 20) Let  $\theta$  be the acute angle between the tangents to the ellipse  $\frac{x^2}{9} + \frac{y^2}{1} = 1$  and the circle  $x^2 + y^2 = 3$  at their point of intersection in the first quadrant then  $\tan \theta$  is equal to:

- a)  $\frac{5}{2\sqrt{3}}$
- b)  $\frac{2}{\sqrt{3}}$
- c)  $\frac{4}{\sqrt{3}}$
- d) 2