

Question-1-1.10-27

EE24BTECH11038 - MALAKALA BALA SUBRAHMANYA ARAVIND

Question:

Write the direction ratios of the vector $\vec{a} = \hat{i} + \hat{j} - \hat{k}$ and hence calculate its direction cosines

Solution:

Variable	Description	Formula
a	A vector	$A = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}$

TABLE 0

$$\vec{a} = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \quad (0.1)$$

(0.2)

The direction ratios are 1,1,-1

Let the direction cosines be $\cos\alpha$, $\cos\beta$, $\cos\gamma$

$$\|a\| = \sqrt{(a^T a)} \quad (0.3)$$

$$\|a\| = \sqrt{3} \quad (0.4)$$

$$\begin{pmatrix} \cos\alpha \\ \cos\beta \\ \cos\gamma \end{pmatrix} = \frac{\vec{a}}{\|a\|} \quad (0.5)$$

$$\begin{pmatrix} \cos\alpha \\ \cos\beta \\ \cos\gamma \end{pmatrix} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix} \quad (0.6)$$

The direction cosines are $\cos\alpha = \frac{1}{\sqrt{3}}$, $\cos\beta = \frac{1}{\sqrt{3}}$, $\cos\gamma = \frac{-1}{\sqrt{3}}$