

Q3

a)

$$T(n) = 5n^2 + 3n + 10$$

if we take $c=18$, then

$$T(n) \leq 18n^2$$

for all $n \geq 1$

Thus $T(n)$ is $O(n^2)$

b)

$$T(n) = 7n^2 + 22m^2 + 4nm + 10m + 200$$

$$O(T(n)) = O(n^2) + O(m^2) + O(nm) + O(m)$$

According to additive property of big-Oh the result is the maximum term.

As $n \geq m$

$$n^2 \geq m^2 \text{ and } n^2 \geq n \cdot m \text{ and } n \geq m$$

Thus in both cases $n > m$ or $n = m$, $O(n^2)$ will be the max term
thus

$$O(T(n)) = O(n^2)$$

c)

First algorithm:

$$T(n) = n/3 + n/2 + 2\sqrt{n} + 3n$$

$$O(T(n)) = O(3n) = O(n)$$

Second Algorithm:

$$\begin{aligned} T(n) &= n/2 * n + 10 * (n/2) + 100000 \\ &= 0.5n^2 + 5n + 100000 \end{aligned}$$

$$O(T(n)) = O(n^2)$$

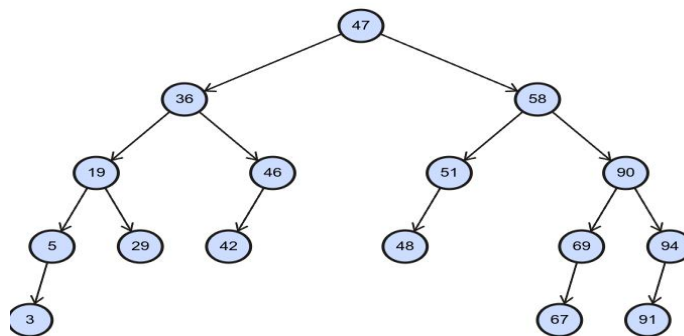
Q4

Hash Table after all insertion:

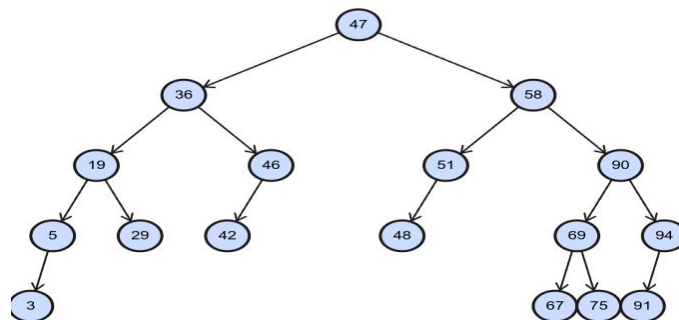
0	1	2	3	4	5	6	7	8	9	10	11	12
12	31	26		5	44	92	40	45	57	80	42	38

Q5

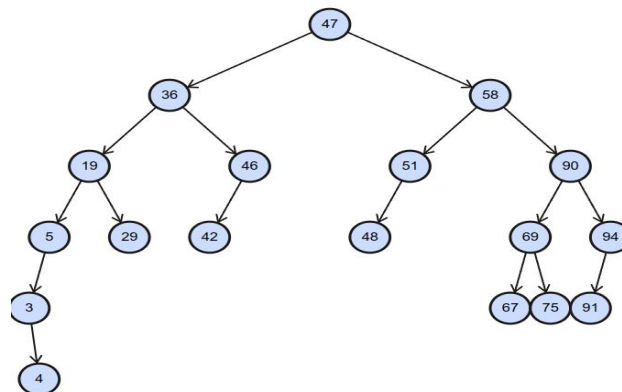
Insert 48



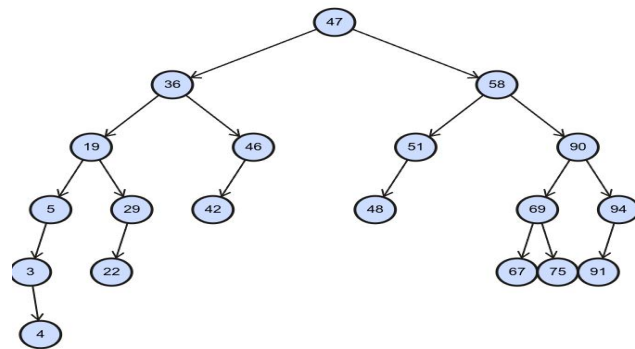
Insert 75



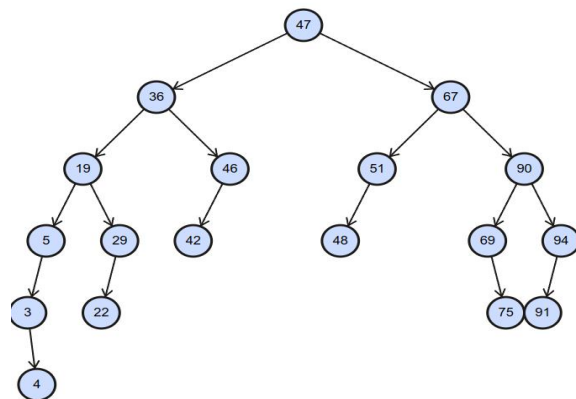
Insert 4



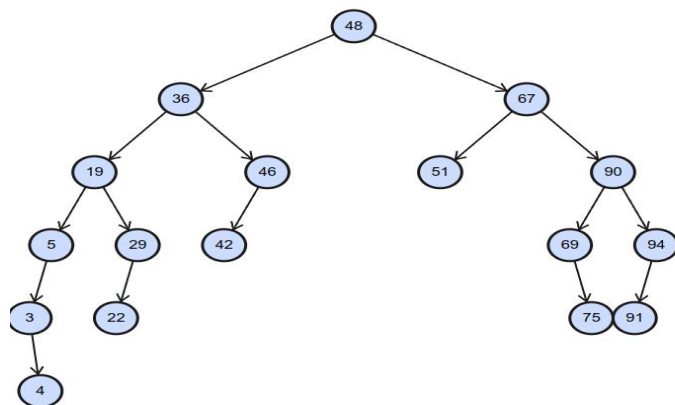
Insert 22



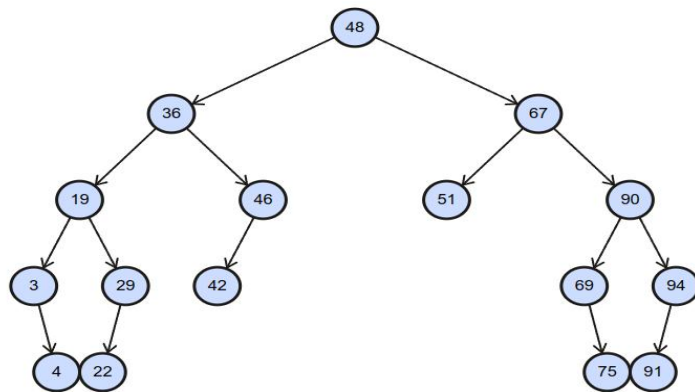
Delete 58



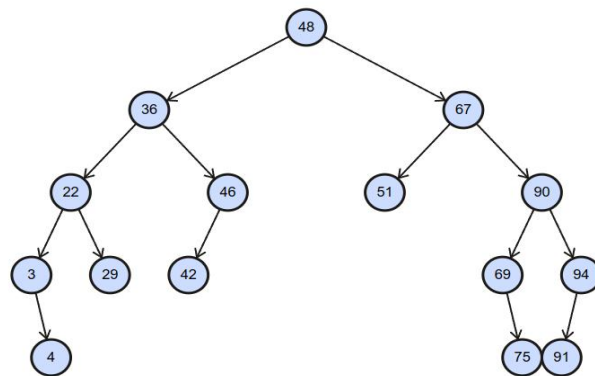
Delete 47



Delete 5



Delete 19



Q6

Inorder: 3 6 7 16 33 40 36 44 49 69 68 70 75 91 94 98
pre-order: 49 7 6 3 33 16 40 36 44 94 70 68 69 91 75 98
post-order: 3 6 16 36 44 40 33 7 69 68 75 91 70 98 94 49

Q7

Bubble Sort:

iteration 1: 7 9 3 8 5 10
iteration 2: 7 3 8 5 9 10
iteration 3: 3 7 5 8 9 10
iteration 4: 3 5 7 8 9 10

iteration 5: 3 5 7 8 9 10

Selection Sort:

iteration 1: 3 7 9 10 8 5

iteration 2: 3 5 9 10 8 7

iteration 3: 3 5 7 10 8 9

iteration 4: 3 5 7 8 10 9

iteration 5: 3 5 7 8 9 10

Insertion Sort:

iteration 1: 7 10 9 3 8 5

iteration 2: 7 9 10 3 8 5

iteration 3: 3 7 9 10 8 5

iteration 4: 3 7 8 9 10 5

iteration 5: 3 5 7 8 9 10

Q8

iteration 1: 1

iteration 2: 4 1

iteration 3: 5 1 4

iteration 4: 5 3 4 1

iteration 5: 5 3 4 1 2

iteration 6: 8 3 5 1 2 4

iteration 7: 9 3 8 1 2 4 5

iteration 8: 9 6 8 3 2 4 5 1

iteration 9: 9 7 8 6 2 4 5 1 3

iteration 10: 10 9 8 6 7 3 5 1 3 2

Q9

Insert 10

heap: 10

Insert 12

heap: 12 10

Insert 13

heap: 13 10 12

Insert 7

heap: 13 10 12 7

Insert 16

heap: 16 13 12 7 10

Insert 19

heap: 19 13 16 7 10 12

Insert 9

heap: 19 13 16 7 10 12 9

Insert 14:

heap: 19 14 16 13 10 12 9 7

Delete 19

heap: 16 14 12 13 10 7 9

Delete 16

heap: 14 13 12 9 10 7