# CCS and equivalences

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#### To do

Solve the exercises and produce a PDF with your answers.

### How to submit via email

Please send it by email (pro@isep.ipp.pt) with the name "pcf2223-N.pdf", where "N" is your student number. The subject of the email should be "pcf2223 N TPC-1".

### Valorization questions

Questions marked with  $[\underline{\textbf{Hard}}]$  are valorization questions. These have very small marks when compared with the other questions and are meant to be more difficult.

### **Deadline**

7 April 2023 @ 23:59 (Friday)

# **CCS** analysis

**Exercise 1.** For each of the CCS processes below, **draw** its transition system.

- **1.1.** A = a.b.0
- **1.2.** B = A + a.0
- **1.3.**  $C = (B||c.d.A) \setminus \{d\}$

**Exercise 2.** Recall A and B processes from Ex. 1.

- **2.1.** Prove that  $A \lesssim B$  or explain why not.
- **2.2.** Prove that  $B \lesssim A$  or explain why not.
- **2.3. Prove** that  $A \sim B$  or **explain** why not.

**Exercise 3.** [Hard] Prove that, for all CCS processes P and Q:

$$P+Q \sim Q+P$$

## **CCS** modelling

**Exercise 4.** Consider the 5 components below.

- T: A temperature sensor that periodically sends a temperature value;
- H: A humidity sensor that periodically sends a humidity value;
- C: A clock that sends a timestamp with the current time;
- **O**: An orchestrator that receives a <u>temperature</u> value, followed by a <u>humidity</u> value and by a <u>timestamp</u>, and in the end sends this <u>data</u> package;
- **D**: A display that receives <u>data</u> from the orchestrator and displays the content.

Consider each <u>underlined</u> word above to be an action of our CSS processes.

- **4.1. Specify** each of these 5 components in CCS and **draw** their transition system.
- **4.2. Specify** a new component **S** of this system, which composes the 5 components above in parallel, imposing synchronisation of all actions except display.
- **4.3. Propose** a variation of a similar system **S2** in CCS with no orchestrator. In this variation:
  - 1. the humidity sensor informs the temperature sensor, then
  - 2. the temperature sensor informs the timestamp, then
  - 3. the timestamp sends the whole data to the display; and finally
  - 4. the display prompts the humidity sensor to restart the process.
- **4.4.** [Hard] Experiment with the tool mCRL2 (https://mcrl2.org). Use it to validate your **S** and **S2** definitions above.