

Trabalho Prático

Grupo 7

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Descrição

Neste trabalho prático é pretendido descobrir um n tal que $n \equiv N \bmod 8$ sendo N o número de grupo atribuído, usando um algoritmo quântico. O algoritmo quântico que vai ser usado é o algoritmo *Grover*. Os possíveis casos vão ser 000,001,010,011,100,101,110,111. Como no nosso caso $N \equiv 7$, depois de converter para binário vamos ter que o resultado pretendido vai ser 111.

Algoritmo de Grover

Para a construção do algoritmo de Grover vamos ter as seguintes etapas:

- Inicialização
- Oráculo
- Amplificação

Inicialização

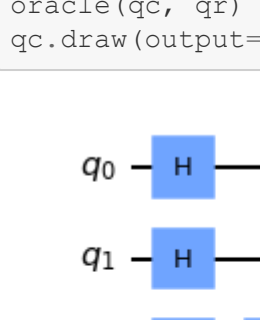
Vamos inicializar os estados do sistema com a mesma amplitude.

$$\sum_i |x_i\rangle$$

Esta inicialização é feita através da sobreposição dos *qubits* aplicando um gate de Hadamard a cada um.

```
In [1]: from qiskit import QuantumCircuit, ClassicalRegister, QuantumRegister, transpile, execute, Aer, IBMQ
import matplotlib.pyplot as plt
from qiskit.visualization import plot_circuit_layout, plot_histogram
from qiskit.providers.ibmq import least_busy

In [2]: n=3
qr = ClassicalRegister(n, 'c')
qc = QuantumCircuit(qr, cr)
qc.h(qr)
qc.draw('mpl')
```



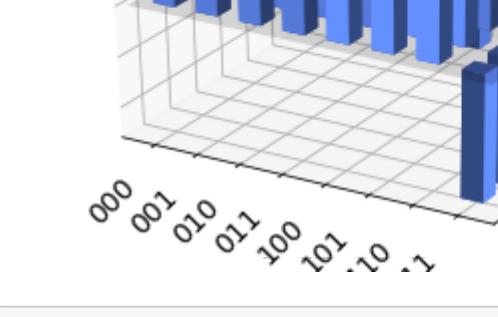
Oráculo

Vamos criar o oráculo que vai ser responsável por mudar a fase para o nosso número em binário pretendido.

Como no nosso caso o número pretendido é o 111 não vamos precisar aplicar nenhum gate-X e simplesmente vamos aplicar o um gate-CX que pode ser construído em *qiskit* através da sequência *gate-H*, *gate-CX* e *gate-H*.

```
In [3]: def oracle(circuit,q):
circuit.h(q[0])
circuit.ccx(q[0],q[1],q[2])
circuit.h(q[2])

oracle(qc,qr)
qc.draw(output='mpl')
```



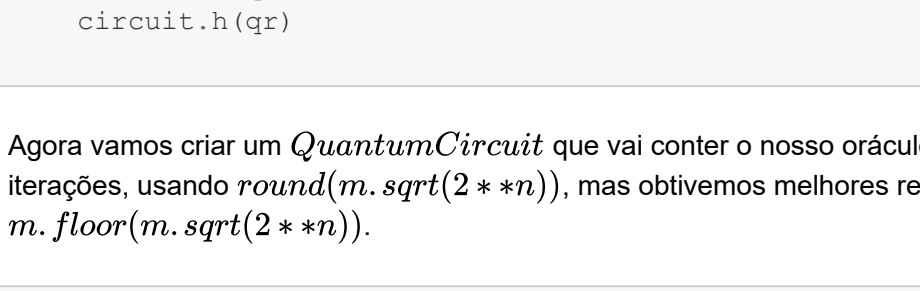
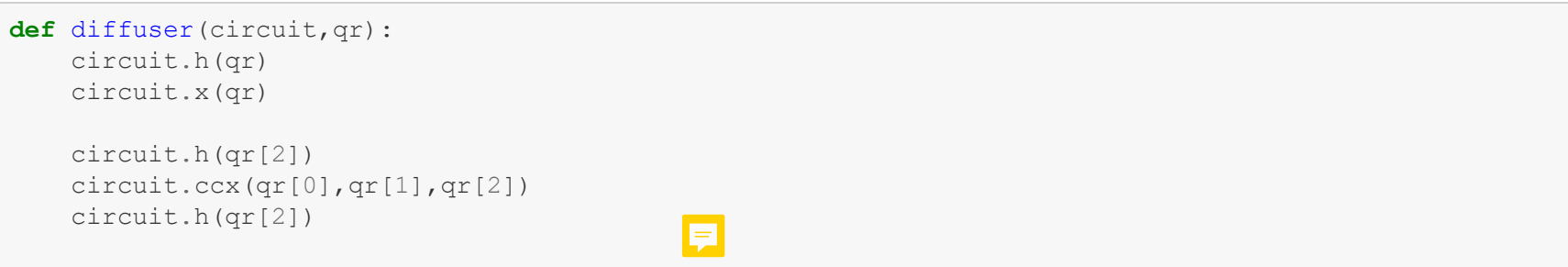
Através do statevector a seguir representado podemos verificar que o oráculo está a mudar de fase nos qubits pretendidos.

```
In [4]: backend = Aer.get_backend('statevector_simulator')
In [5]: result = execute(qc, backend.state).result()
qstate = result.get_statevector(qc)
```

Como o último elemento da matriz é 0 e este está negativo, e esse elemento representa o 111 temos que o oráculo está correto.

```
In [6]: qstate
Out [6]: array([ 0.35355339+0.00000000e+00j, 0.35355339+0.00000000e+00j,
0.35355339+0.00000000e+00j, 0.35355339+0.32978028e+17j,
0.35355339+0.00000000e+00j, 0.35355339+0.00000000e+00j,
0.35355339+0.00000000e+00j, -0.35355339+4.32978028e-17j])
```

Apresentamos em seguida o statevector em forma de gráficos para melhor visualização.



Amplificação

Nesta fase vamos criar um *diffuser* que nos vai permitir aumentar a amplitude dos qubits de forma a que aumente a probabilidade de obtermos o resultado que pretendemos. Para isso é necessário inverter e aumentar a amplitude da componente pretendida em torno da média das amplitudes e simultaneamente reduzir das restantes componentes.

```
In [9]: def diffuser(circuit,qr):
circuit.h(qr[0])
circuit.ccx(qr[0],qr[1],qr[2])
circuit.h(qr[2])
circuit.x(qr[0])
circuit.h(qr[0])
```

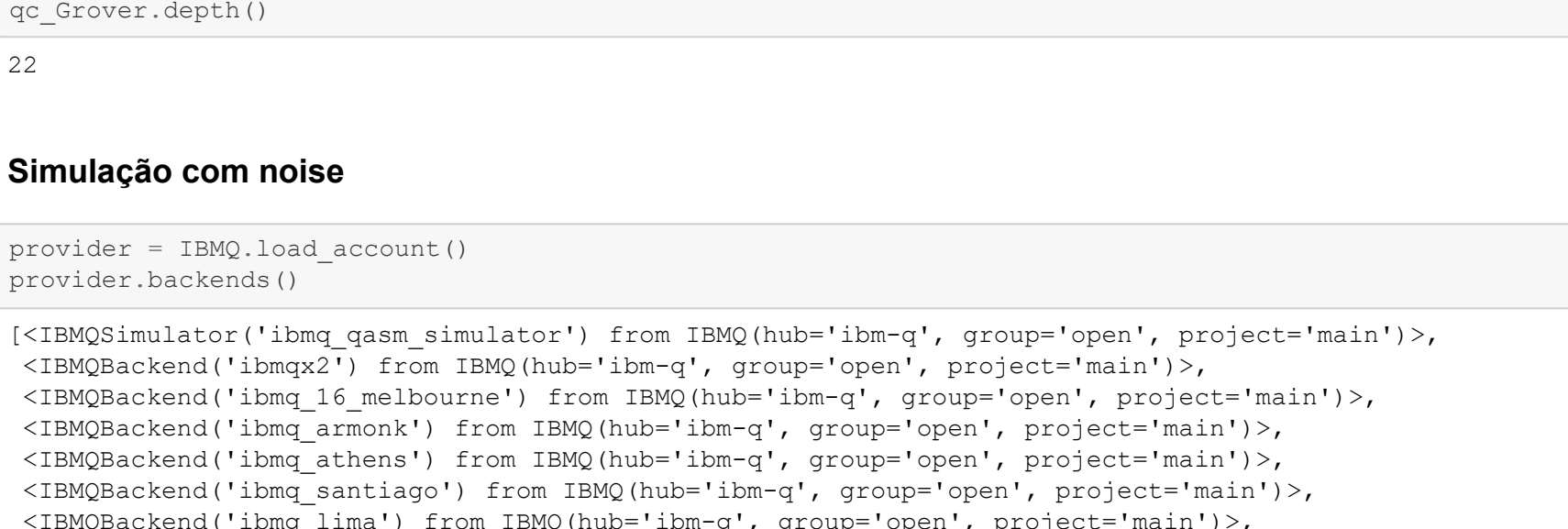
Agora vamos usar um *QuantumCircuit* que vai conter o nosso oráculo e *diffuser* aproximadamente $\sqrt{2^n}$. O espectroscópio seria fazer 3 iterações, usando *round(m.sqrt(2^n))*, nos obtemos melhores resultados fazendo duas iterações, por isso usamos *m.floor(m.sqrt(2^n))*.

```
In [10]: import math as m
times = m.floor(m.sqrt(2**n))
print(times)

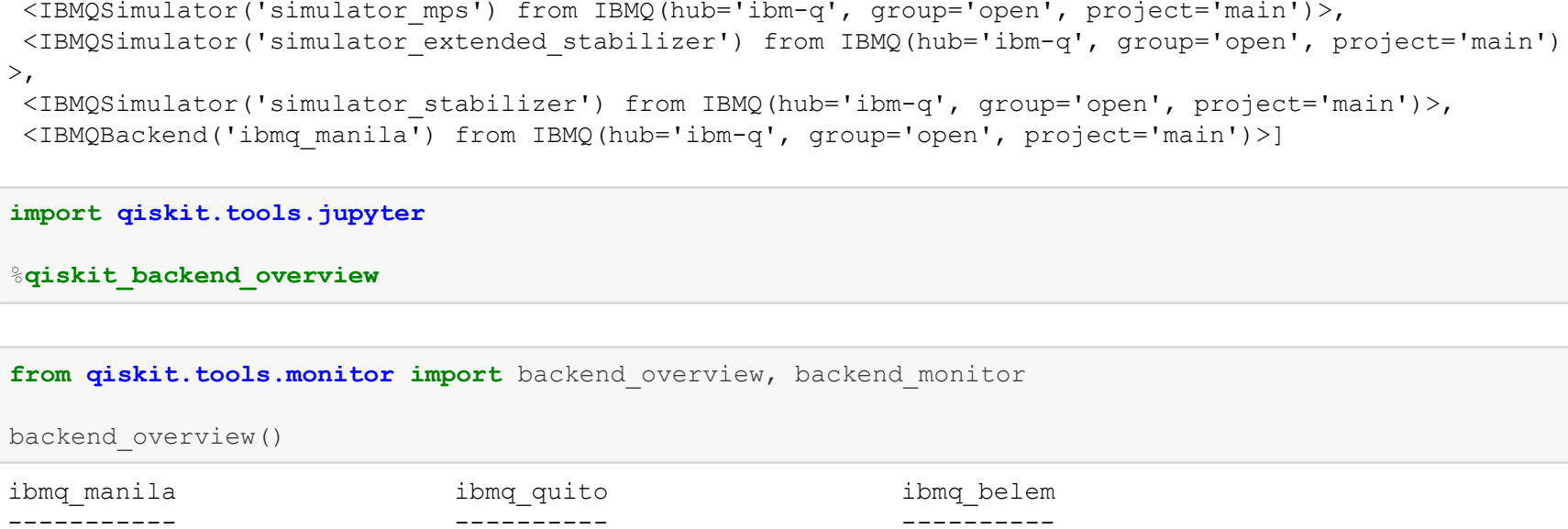
2
```

Fazemos no fim a medição que consiste na projeção do estado quântico de cada um dos qubits para um bit clássico. Ao ser medido, cada qubit colapsa para um dos estados possíveis, não sendo mais possível obter o estado quântico inicial.

```
In [11]: qc_Grover= QuantumCircuit(qr,cr)
qc_Grover.h(qr)
for t in range(times):
    oracle(qc_Grover,qr)
    diffuser(qc_Grover,qr)
qc_Grover.measure(qr,cr)
qc_Grover.draw(output='mpl')
```

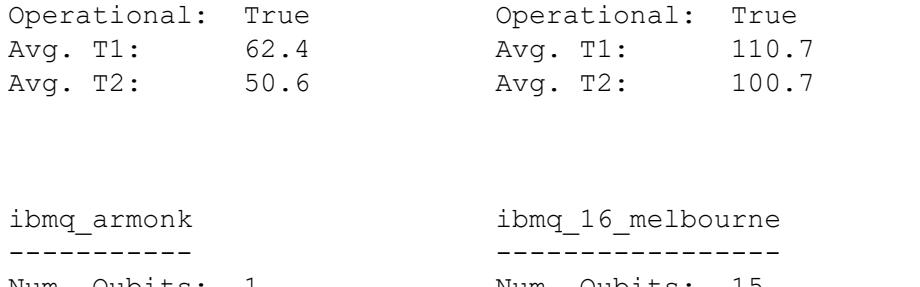


Temos então que o estado que queremos é o que tem a maior probabilidade.



Simulação

```
In [13]: backend = Aer.get_backend('qasm_simulator')
In [14]: shots=1024
result = execute(qc_Grover, backend, shots=shots).result()
counts_sim = result.get_counts(qc_Grover)
plot_histogram(counts_sim)
```



```
In [15]: qc_Grover.depth()
Out [15]: 22
```

Simulação com noise

```
In [16]: provider = IBMQ.load_account()
provider.backends()
```

Out [16]:

```
<IBMQSimulator('ibmq_qasm_simulator') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq2') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_16_melbourne') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_armonk') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_athens') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_santiago') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_lima') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_belem') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmqquito') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQSimulator('simulator_statevector') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQSimulator('simulator_mps') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQSimulator('simulator_extended_stabilizer') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQSimulator('simulator_stabilizer') from IBMQ(hub='ibm-q', group='open', project='main')>,
<IBMQBackend('ibmq_manila') from IBMQ(hub='ibm-q', group='open', project='main')>
```

```
In [17]: import qiskit.tools.jupyter
qiskit_backend_overview
```

```
In [18]: from qiskit.tools.monitor import backend_overview, backend_monitor
backend_overview()
```

ibmq_manila	ibmqquito	ibmq_belem
Num. Qubits: 5	Num. Qubits: 5	Num. Qubits: 5
Pending Jobs: 13	Pending Jobs: 14	Pending Jobs: 9
Least busy: False	Least busy: False	Least busy: False
Operational: True	Operational: True	Operational: True
Avg. T1: 163.8	Avg. T1: 80.3	Avg. T1: 75.9
Avg. T2: 68.2	Avg. T2: 71.2	Avg. T2: 75.6

ibmq_lima	ibmq_santiago	ibmq_athens
Num. Qubits: 5	Num. Qubits: 5	Num. Qubits: 5
Pending Jobs: 3	Pending Jobs: 18	Pending Jobs: 1
Least busy: False	Least busy: True	Least busy: False
Operational: True	Operational: True	Operational: True
Avg. T1: 62.4	Avg. T1: 110.7	Avg. T1: 96.0
Avg. T2: 50.6	Avg. T2: 100.7	Avg. T2: 104.1

ibmq_armonk	ibmq_16_melbourne	ibmq2
Num. Qubits: 1	Num. Qubits: 15	Num. Qubits: 5
Pending Jobs: 1	Pending Jobs: False	Pending Jobs: 5
Least busy: False	Least busy: False	Least busy: False
Operational: True	Operational: True	Operational: True
Avg. T1: 169.7	Avg. T1: 54.6	Avg. T1: 56.6
Avg. T2: 261.0	Avg. T2: 53.1	Avg. T2: 35.8

Escolhemos o computador com menos erro.

```
In [19]: backend_device = provider.get_backend('ibmq_santiago')
print("Running on: ", backend_device)

Running on: ibmq_santiago
```

```
In [20]: backend_device
```

Out [20]: <IBMQBackend('ibmq_santiago') from IBMQ(hub='ibm-q', group='open', project='main')>

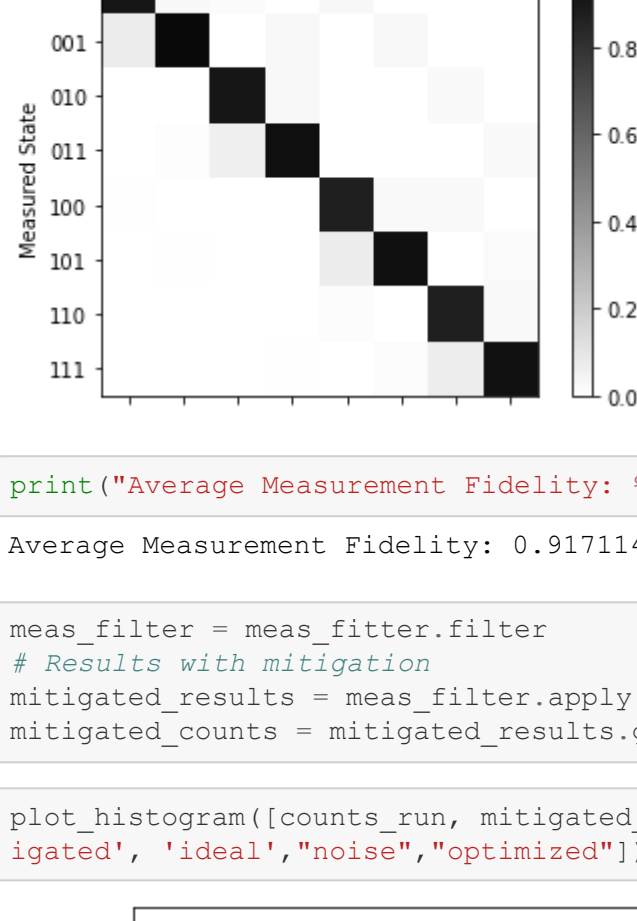
```
In [21]: backend_monitor(backend_device)

ibmq_santiago
=====
Configuration
-----
n_qubits: 5
operational: True
status_msg: active
pending jobs: 0
backend version: 1.3.22
basis_gates: ['id', 'rz', 'sx', 'x', 'cx', 'reset']
local: False
simulator: False
online date: 2020-06-03 04:00:00+00:00
qubit_id_range: [4, 33, 42, 90, 64, 32, 0, 18, 5, 3, 2, 1, 0]
11887708e+18], [4.3205355364195937e+18, 5.320535536419594e+18], [4.2423110151676165e+18, 5.2423110151676165e+18], [4.316329983561523e+18, 5.316329983561523e+18])
n_channels: 8
meas_kernels: ['hw_gmrfk']
backend name: ibmq_santiago
dtm: 0.2222222222222222
meas_levels: [0, 1, 2, 3]
input_allowed: ['job']
meas_map: [0, 1, 2, 3, 4]
rep_delay_range: [0.001, 0.002, 0.003, 0.004, 0.005, 0.006, 0.007, 0.008, 0.009, 0.01, 0.011, 0.012, 0.013, 0.014, 0.015, 0.016, 0.017, 0.018, 0.019, 0.02, 0.021, 0.022, 0.023, 0.024, 0.025, 0.026, 0.027, 0.028, 0.029, 0.03, 0.031, 0.032, 0.033, 0.034, 0.035, 0.036, 0.037, 0.038, 0.039, 0.04, 0.041, 0.042, 0.043, 0.044, 0.045, 0.046, 0.047, 0.048, 0.049, 0.05, 0.051, 0.052, 0.053, 0.054, 0.055, 0.056, 0.057, 0.058, 0.059, 0.06, 0.061, 0.062, 0.063, 0.064, 0.065, 0.066, 0.067, 0.068, 0.069, 0.07, 0.071, 0.072, 0.073, 0.074, 0.075, 0.076, 0.077, 0.078, 0.079, 0.08, 0.081, 0.082, 0.083, 0.084, 0.085, 0.086, 0.087, 0.088, 0.089, 0.09, 0.091, 0.092, 0.093, 0.094, 0.095, 0.096, 0.097, 0.098, 0.099, 0.1, 0.101, 0.102, 0.103, 0.104, 0.105, 0.106, 0.107, 0.108, 0.109, 0.11, 0.111, 0.112, 0.113, 0.114, 0.115, 0.116, 0.117, 0.118, 0.119, 0.12, 0.121, 0.122, 0.123, 0.124, 0.125, 0.126, 0.127, 0.128, 0.129, 0.13, 0.131, 0.132, 0.133, 0.134, 0.135, 0.136, 0.137, 0.138, 0.139, 0.14, 0.141, 0.142, 0.143, 0.144, 0.145, 0.146, 0.147, 0.148, 0.149, 0.15, 0.151, 0.152, 0.153, 0.154, 0.155, 0.156, 0.157, 0.158, 0.159, 0.16, 0.161, 0.162, 0.163, 0.164, 0.165, 0.166, 0.167, 0.168, 0.169, 0.17, 0.171, 0.172, 0.173, 0.174, 0.175, 0.176, 0.177, 0.178, 0.179, 0.18, 0.181, 0.182, 0.183, 0.184, 0.185, 0.186, 0.187, 0.188, 0.189, 0.19, 0.191, 0.192, 0.193, 0.194, 0.195, 0.196, 0.197, 0.198, 0.199, 0.2, 0.201, 0.202, 0.203, 0.204, 0.205, 0.206, 0.207, 0.208, 0.209, 0.21, 0.211, 0.212, 0.213, 0.214, 0.215, 0.216, 0.217, 0.218, 0.219, 0.22, 0.221, 0.222, 0.223, 0.224, 0.225, 0.226, 0.227, 0.228, 0.229, 0.23, 0.231, 0.232, 0.233, 0.234, 0.235, 0.236, 0.237, 0.238, 0.239, 0.24, 0.241, 0.242, 0.243, 0.244, 0.245, 0.246, 0.247, 0.248, 0.249, 0.25, 0.251, 0.252, 0.253, 0.254, 0.255, 0.256, 0.257, 0.258, 0.259, 0.26, 0.261, 0.262, 0.263, 0.264, 0.265, 0.266, 0.267, 0.268, 0.269, 0.27, 0.271, 0.272, 0.273, 0.274, 0.275, 0.276, 0.277, 0.278, 0.279, 0.28, 0.281, 0.282, 0.283, 0.284, 0.285, 0.286, 0.287, 0.288, 0.289, 0.29, 0.291, 0.292, 0.293, 0.294, 0.295, 0.296, 0.297, 0.298, 0.299, 0.3, 0.301, 0.302, 0.303, 0.304, 0.305, 0.306, 0.307, 0.308, 0.309, 0.31, 0.311, 0.312, 0.313, 0.314, 0.315, 0.316, 0.317, 0.318, 0.319, 0.32, 0.321, 0.322, 0.323, 0.324, 0.325, 0.326, 0.327, 0.328, 0.329, 0.33, 0.331, 0.332, 0.333, 0.334, 0.335, 0.336, 0.337, 0.338, 0.339, 0.34, 0.341, 0.342, 0.343, 0.344, 0.345, 0.346, 0.347, 0.348, 0.349, 0.35, 0.351, 0.352, 0.353, 0.354, 0.355, 0.356, 0.357, 0.358, 0.359, 0.36, 0.361, 0.362, 0.363, 0.364, 0.365, 0.366, 0.367, 0.368, 0.369, 0.37, 0.371, 0.372, 0.373, 0.374, 0.375, 0.376, 0.377, 0.378, 0.379, 0.38, 0.381, 0.382, 0.383, 0.384, 0.385, 0.386, 0.387, 0.388, 0.389, 0.39, 0.391, 0.392, 0.393, 0.394, 0.395, 0.396, 0.397, 0.398, 0.399, 0.4, 0.401, 0.402, 0.403, 0.404, 0.405, 0.406, 0.407, 0.408, 0.409, 0.41, 0.411, 0.412, 0.413, 0.414, 0.415, 0.416, 0.417, 0.418, 0.419, 0.42, 0.421, 0.422, 0.423, 0.424, 0.425, 0.426, 0.427, 0.428, 0.429, 0.43, 0.431, 0.432, 0.433, 0.434, 0.435, 0.436, 0.437, 0.438, 0.439, 0.44, 0.441, 0.442, 0.443, 0.444, 0.445, 0.446, 0.447, 0.448, 0.449, 0.45, 0.451, 0.452, 0.453, 0.454, 0.455, 0.456, 0.457, 0.458, 0.459, 0.46, 0.461, 0.462, 0.463, 0.464, 0.465, 0.466, 0.467, 0.468, 0.469, 0.47, 0.471, 0.472, 0.473, 0.474, 0.475, 0.476, 0.477, 0.478, 0.479, 0.48, 0.481, 0.482, 0.483, 0.484, 0.485, 0.486, 0.487, 0.488, 0.489, 0.49, 0.491, 0.492, 0.493, 0.494, 0.495, 0.496, 0.497, 0.498, 0.499, 0.5, 0.501, 0.502, 0.503, 0.504, 0.505, 0.506, 0.507, 0.508, 0.509, 0.51, 0.511, 0.512, 0.513, 0.514, 0.515, 0.516, 0.517, 0.518, 0.519, 0.52, 0.521, 0.522, 0.523, 0.524, 0.525, 0.526, 0.527, 0.528, 0.529, 0.53, 0.531, 0.532, 0.533, 0.534, 0.535, 0.536, 0.537, 0.538, 0.539, 0.54, 0.541, 0.542, 0.543, 0.544, 0.545, 0.546, 0.547, 0.548, 0.549, 0.55, 0.551, 0.552, 0.553, 0.554, 0.555, 0.556, 0.557, 0.558, 0.559, 0.56, 0.561, 0.562, 0.563, 0.564, 0.565, 0.566, 0.567, 0.568, 0.569, 0.57, 0.571, 0.572, 0.573, 0.574, 0.575, 0.576, 0.577, 0.578, 0.579, 0.58, 0.581, 0.582, 0.583, 0.584, 0.585, 0.586, 0.587, 0.588, 0.589, 0.59, 0.591, 0.592, 0.593, 0.594, 0.595, 0.596, 0.597, 0.598, 0.599, 0.6, 0.601, 0.602, 0.603, 0.604, 0.605, 0.606, 0.607, 0.608, 0.609, 0.61, 0.611, 0.612, 0.613, 0.614, 0.615, 0.616, 0.617, 0.618, 0.619, 0.62, 0.621, 0.622, 0.623, 0.624, 0.625, 0.626, 0.627, 0.628, 0.629, 0.63, 0.631, 0.632, 0.633, 0.634, 0.635, 0.636, 0.637, 0.638, 0.639, 0.64, 0.641, 0.642, 0.643, 0.644, 0.645, 0.646, 0.647, 0.648, 0.649, 0.65, 0.651, 0.652, 0.653, 0.654, 0.655, 0.656, 0.657, 0.658, 0.659, 0.66, 0.661, 0.662, 0.663, 0.664, 0.665, 0.666, 0.667, 0.668, 0.669, 0.67, 0.671, 0.672, 0.673, 0.674, 0.675, 0.676, 0.677, 0.678, 0.679, 0.68, 0.681, 0.682, 0.683, 0.684, 0.685, 0.686, 0.687, 0.688, 0.689, 0.69, 0.691, 0.692, 0.693, 0.694, 0.695, 0.696, 0.697, 0.698, 0.699, 0.7, 0.701, 0.702, 0.703, 0.704, 0.705, 0.706, 0.707, 0.708, 0.709, 0.71, 0.711, 0.712, 0.713, 0.714, 0.715, 0.716, 0.717, 0.718, 0.719, 0.72, 0.721, 0.722, 0.723, 0.724, 0.725, 0.726, 0.727, 0.728, 0.729, 0.73, 0.731, 0.732, 0.733, 0.734, 0.735, 0.736, 0.737, 0.738, 0.739, 0.74, 0.741, 0.742, 0.743, 0.744, 0.745, 0.746, 0.747, 0.748, 0.749, 0.75, 0.751, 0.752, 0.753, 0.754, 0.755, 0.756, 0.757, 0.758, 0.759, 0.76, 0.761, 0.762, 0.763, 0.764, 0.765, 0.766, 0.767, 0.768, 0.769, 0.77, 0.771, 0.772, 0.773, 0.774, 0.775, 0.776, 0.777, 0.778, 0.779, 0.78, 0.781, 0.782, 0.783, 0.784, 0.785, 0.786, 0.787, 0.788, 0.789, 0.79, 0.791, 0.792, 0.793, 0.794, 0.795, 0.796, 0.797, 0.798, 0.799, 0.8, 0.801, 0.802, 0.803, 0.804, 0.805, 0.806, 0.807, 0.808, 0.809, 0.81, 0.811, 0.812, 0.813, 0.814, 0.815, 0.816, 0.817, 0.818, 0.819, 0.82, 0.821, 0.822, 0.823, 0.824, 0.825, 0.826, 0.827, 0.828, 0.829, 0.83, 0.831, 0.832, 0.833, 0.834, 0.835, 0.836, 0.837, 0.838, 0.839, 0.84, 0.841, 0.842, 0.843, 0.844, 0.845, 0.846, 0.847, 0.848, 0.849, 0.85, 0.851, 0.852, 0.853, 0.854, 0.855, 0.856, 0.857, 0.858, 0.859, 0.86, 0.861, 0.862, 0.863, 0.864, 0.865, 0.866, 0.867, 0.868, 0.869, 0.87, 0.871, 0.872, 0.873, 0.874, 0.875, 0.876, 0.877, 0.878, 0.879, 0.88, 0.881, 0.882, 0.883, 0.884, 0.885, 0.886, 0.887, 0.888, 0.889, 0.89, 0.891, 0.892, 0.893, 0.894, 0.895, 0.896, 0.897, 0.898, 0.899, 0.9, 0.901, 0.902, 0.903, 0.904, 0.905, 0.906, 0.907, 0.908, 0.909, 0.91, 0.911, 0.912, 0.913, 0.914, 0.915, 0.916, 0.917, 0.918, 0.919, 0.92, 0.921, 0.922, 0.923, 0.924, 0.925, 0.926, 0.927, 0.928, 0.929, 0.93, 0.931, 0.932, 0.933, 0.934, 0.935, 0.936, 0.937, 0.938, 0.939, 0.94, 0.941, 0.942, 0.943, 0.944, 0.945, 0.946, 0.947, 0.948, 0.949, 0.95, 0.951, 0.952, 0.953, 0.954, 0.955, 0.956, 0.957, 0.958, 0.959, 0.96, 0.961, 0.962, 0.963, 0.964, 0.965, 0.966, 0.967, 0.968, 0.969, 0.97, 0.971, 0.972, 0.973, 0.974, 0.975, 0.976, 0.977, 0.978, 0.979, 0.98, 0.981, 0.982, 0.983, 0.984, 0.985, 0.986, 0.987, 0.988, 0.989, 0.99, 0.991, 0.992, 0.993, 0.994, 0.995, 0.996, 0.997, 0.998, 0.999, 1.0]
```

```
Q0 / 4.8343 GHz / 135.71038 us / 10
```



```
[46]: meas_filter = CompleteMeasFilter(cal_results, state_labels, circLabel='mcal')
      meas_filter.plot_calibration()
```



```
In [47]: print("Average Measurement Fidelity: %f" % meas_filter.readout_fidelity())
Average Measurement Fidelity: 0.917114
```

```
In [48]: meas_filter = meas_filter.filter
# Results with mitigation
mitigated_results = meas_filter.apply(result_r)
mitigated_counts = mitigated_results.get_counts()
```

```
In [49]: plot_histogram([counts_run, mitigated_counts, counts_sin, counts_noise, counts_opt], legend=['raw', 'mitigated', 'ideal', 'noise', 'optimized'])
```



```
In [ ]:
```