Trabalho Prático de Interação e Concorrência

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Enunciado

Each group of students has a number assigned, N.

Now, you have to use a quantum algorithm to find s



$s = N \mod 8$

in an unsorted list. Implement the correct algorithm in a Jupyter Notebook file. Each work should contain (and will be evaluated on) the following steps:

- 1. Division of the algorithm into sections; Utilisation of the state vector simulator to explain each step (special attention to the oracle);
- 2. Application of noise simulator to predict the best optimisation;
- 3. Execution in an IBM Q backend.
- 4. Mitigation of Error with Ignis.

Implementação do Algoritmo de Groover para encontrar s



```
In [1]:

1  # Relevant QISKit modules
2  from qiskit import Aer, IBMQ
3  from qiskit import QuantumCircuit, ClassicalRegister, QuantumRegister
4  from qiskit import execute, transpile
5  from qiskit.tools.visualization import plot_histogram, visualize_transition, plot_state
7  # Useful additional packages
9  import matplotlib.pyplot as plt
10  %matplotlib inline
```

```
In [2]:
```

```
backend_vector = Aer.get_backend("statevector_simulator")
backend_unitary = Aer.get_backend('unitary_simulator')
backend = Aer.get_backend("qasm_simulator")
```

- Queremos encontrar s = N mod 8 numa lista desordenada, onde N é igual ao número do nosso grupo.
- · Vamos identificar primeiro qual o número que queremos encontrar.

In [3]: ▶

```
1 N = 15
2 s = N % 8
3 print('Number that we are looking for:', s)
```

Number that we are looking for: 7

· Depois passsamos o número para binário.

```
In [4]:

1   sb = bin(s)[2:]
2   print('Number in binary form:',sb)
```

Number in binary form: 111

Precisamos então de 3 qubits.



```
In [5]: ▶
```

```
1 x = len(sb)
2 print('Number of qubits:', x)
```

Number of qubits: 3

1 Inicializamos o sistema com a mesma amplitude em todos os estados de input.

$$\sum_{x_i} |x_i\rangle$$

- **2** Aplica \sqrt{N} vezes as seguintes operações unitárias:
- a) Operador Quantum Oracle U_w . Este operador é responsável por identificar as soluções para o problema e indicar o que estamos à procura.

$$-\alpha_m|x_m\rangle + \beta \sum_{x_i \neq x_m} |x_i\rangle$$

Com esta implementação, a fase do estado marcado ($f(x_m)=1$) roda π radianos, enquanto os outros estados mantêm o sistema inalterado.

Como o oráculo apenas precisa de mudar o estado do que estamos à procura, então basta implementar uma porta CCZ, que no qiskit é representada pela composição de portas de Hadamard e da porta CCX. Também não precisamos de usar nenhuma porta X, pois como queremos encontrar $|7\rangle = |111\rangle$ não necessitamos de usar essa porta.

In [6]: ▶

```
def phase_oracle(circuit, qr_x):
    circuit.h(qr_x[2])
    circuit.ccx(qr_x[0], qr_x[1], qr_x[2])
    circuit.h(qr_x[2])
```

Então uma representação do oráculo será:

Aplicação da porta de Hadamard

$$(I \otimes I \otimes H)|000\rangle = I|0\rangle \otimes I|0\rangle \otimes H|0\rangle = \begin{bmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Aplicação da porta CCX

$$CCX(|0\rangle, |0\rangle, \frac{|0\rangle + |1\rangle}{\sqrt{2}}) = \begin{bmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

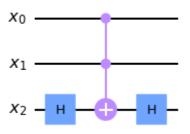
Aplicação da porta de Hadamard de novo

$$(I \otimes I \otimes H)|0\rangle|0\rangle(\frac{|0\rangle + |1\rangle}{\sqrt{2}}) = \begin{bmatrix} 1\\0\\0\\0\\0\\0\\0\\0\\0 \end{bmatrix}$$

In [7]:

```
1  qr_x = QuantumRegister(x, 'x')
2  qc = QuantumCircuit(qr_x)
3  phase_oracle(qc, qr_x)
4  
5  qc.draw(output='mpl')
```

Out[7]:



Utilização do State Vector para simular os passos.



```
In [8]: ▶
```

```
1 result = execute(qc, backend_vector).result()
2 qstate = result.get_statevector(qc)
3 print(qstate)
```

```
[1.00000000e+00-6.123234e-17j 0.0000000e+00+0.000000e+00j 0.0000000e+00+0.000000e+00j 0.0000000e+00+0.000000e+00j 4.26642159e-17+6.123234e-17j 0.0000000e+00+0.000000e+00j 0.0000000e+00+0.000000e+00j 0.0000000e+00+0.000000e+00j]
```

b) Aplicar a tranformação de difusão U_D . Chega-se à implementação deste operador através de $U_D=WRW$, onde W é a matriz de transformação Walsh-Hadamard, e R é a matriz de rotação.

$$(2A + \alpha_m)|x_m\rangle + (2A - \beta)\sum_{x_i \neq x_m}|x_i\rangle$$

Este passo do algoritmo não só altera o input desejado mas também aumenta a sua amplitude.



```
In [9]:

def diffuser(circuit, qr_x):
    circuit.h(qr_x)
    circuit.x(qr_x)
    phase_oracle(circuit, qr_x)
    circuit.x(qr_x)
    circuit.x(qr_x)
    circuit.h(qr_x)
```

Estes passos (a) e (b) têm de ser repetidos \sqrt{N} vezes para chegar ao valor mais aproximado.

```
In [10]:

1   import math as m
2   times= round(m.sqrt(2**x))
    print(times)
```

3

 Vamos agora criar um Registo Clássico para guardar a informação após a medição dos qubits e, depois, um Circuito Quântico (circuito de Grover) com um registo quântico qr_x e também com o registo clássico cr. O circuito é inicializado com a mesma amplitude em todos os estados de input.

```
In [11]:

1     cr = ClassicalRegister(x,'cr')
2     qc_Grover = QuantumCircuit(qr_x,cr)
3     qc_Grover.draw(output='mpl')
```

Out[11]:

x₀ —

 x_1 —

 x_2 —

cr ≟

Utilizando o State Vector obtemos a matriz

$$|000\rangle = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

In [12]:

```
result = execute(qc_Grover, backend_vector).result()
qstate = result.get_statevector(qc_Grover)
print(qstate)
```

• Aplicar uma gate de Hadamard a cada qubit, ou seja, aplicar $H^{\otimes n}$.

$$H|000\rangle = H(|0\rangle \otimes |0\rangle \otimes |0\rangle) = H|0\rangle \otimes H|0\rangle \otimes H|0\rangle = \begin{bmatrix} \frac{1}{2\sqrt{2}} \\ \frac{1}{2\sqrt{2}} \end{bmatrix}$$

```
In [13]:

1     qc_Grover.h(qr_x)
2     qc_Grover.barrier()
3     qc_Grover.draw(output='mpl')
```

Out[13]:



```
In [14]:

1    result = execute(qc_Grover, backend_vector).result()
2    qstate = result.get_statevector(qc_Grover)
    print(qstate)
```

```
[0.35355339+0.j 0.35355339+0.j 0.35355339+0.j 0.35355339+0.j 0.35355339+0.j 0.35355339+0.j 0.35355339+0.j]
```

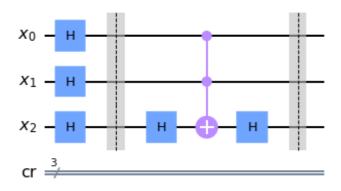
- Como só precisamos de encontrar um elemento, a variável t só é executada uma vez.
- Dentro do ciclo for é executado o oráculo.

```
In [15]: ▶
```

```
for t in range(1):
    # a)
    phase_oracle(qc_Grover, qr_x)
    qc_Grover.barrier()

qc_Grover.draw(output='mpl')
```

Out[15]:



```
In [16]:
```

```
1 result = execute(qc_Grover, backend_vector).result()
2 qstate = result.get_statevector(qc_Grover)
3 print(qstate)
```

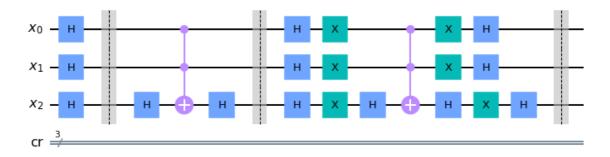
· Agora executamos o difusor.

In [17]: ▶

```
for t in range(1):
    # b)
    diffuser(qc_Grover,qr_x)
    qc_Grover.barrier()

qc_Grover.draw(output='mpl')
```

Out[17]:



```
In [18]:
```

```
result = execute(qc_Grover, backend_vector).result()
qstate = result.get_statevector(qc_Grover)
print(qstate)
```

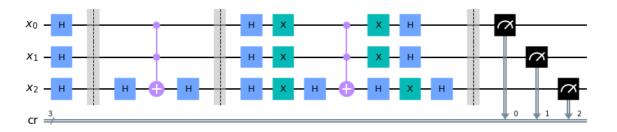
```
[-0.1767767 +2.03637921e-35j -0.1767767 +2.16489014e-17j -0.1767767 +2.16489014e-17j -0.1767767 -2.66556279e-32j -0.1767767 +1.35579187e-17j -0.1767767 -8.09098269e-18j -0.1767767 -8.09098269e-18j -0.88388348+1.32517455e-16j]
```

- · Por fim, medimos o circuito.
- Desenho do circuito completo.

```
In [19]: ▶
```

```
1 qc_Grover.measure(qr_x,cr)
2 qc_Grover.draw(output='mpl')
```

Out[19]:



```
In [20]:

1    result = execute(qc_Grover, backend_vector).result()
2    qstate = result.get_statevector(qc_Grover)
3    print(qstate)
```

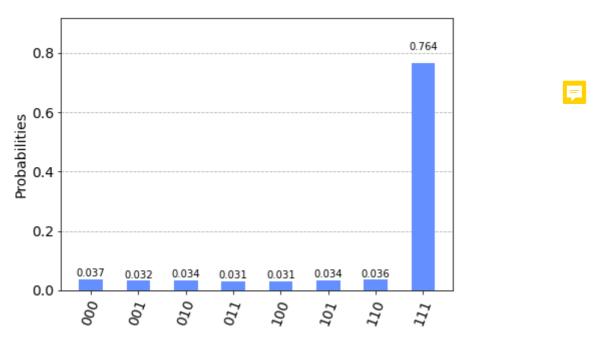
```
[-0.+0.00000000e+00j -0.+0.00000000e+00j -0.+0.00000000e+00j 0.-0.00000000e+00j -0.+0.00000000e+00j 0.+0.00000000e+00j -1.+1.49926386e-16j]
```

Desenha o histograma com as probabilidades das medições.

```
In [21]:

1    shots=1024
2    result = execute(qc_Grover, backend, shots=shots).result()
3    counts_Grover = result.get_counts(qc_Grover)
4    plot_histogram(counts_Grover)
```

Out[21]:



• Profundidade do circuito, caminho mais longo entre o input e o output.

```
In [22]:

1 qc_Grover.depth()
```

Out[22]:

12

Noise Simulator

· Load da Conta IBMQ.

```
In [23]:

1  provider = IBMQ.load_account()
2  provider.backends()
```

```
Out[23]:
```

```
[<IBMQSimulator('ibmq gasm simulator') from IBMQ(hub='ibm-q', group='open',</pre>
project='main')>,
 <IBMQBackend('ibmqx2') from IBMQ(hub='ibm-q', group='open', project='main')</pre>
 <IBMQBackend('ibmq_16_melbourne') from IBMQ(hub='ibm-q', group='open', proj</pre>
ect='main')>,
 <IBMQBackend('ibmq armonk') from IBMQ(hub='ibm-q', group='open', project='m</pre>
ain')>,
 <IBMQBackend('ibmq_athens') from IBMQ(hub='ibm-q', group='open', project='m
 <IBMQBackend('ibmq_santiago') from IBMQ(hub='ibm-q', group='open', project</pre>
='main')>,
 <IBMQBackend('ibmq_lima') from IBMQ(hub='ibm-q', group='open', project='mai</pre>
 <IBMQBackend('ibmq_belem') from IBMQ(hub='ibm-q', group='open', project='ma</pre>
in')>,
 <IBMQBackend('ibmq_quito') from IBMQ(hub='ibm-q', group='open', project='ma</pre>
in')>,
 <IBMQSimulator('simulator_statevector') from IBMQ(hub='ibm-q', group='ope</pre>
n', project='main')>,
 <IBMQSimulator('simulator_mps') from IBMQ(hub='ibm-q', group='open', projec</pre>
t='main')>,
 <IBMQSimulator('simulator_extended_stabilizer') from IBMQ(hub='ibm-q', grou</pre>
p='open', project='main')>,
 <IBMQSimulator('simulator stabilizer') from IBMQ(hub='ibm-q', group='open',</pre>
project='main')>,
 <IBMQBackend('ibmq_manila') from IBMQ(hub='ibm-q', group='open', project='m
ain')>]
```

• Visualização dos Computadores Quânticos.

```
In [24]:

1  import qiskit.tools.jupyter
2  3  %qiskit_backend_overview
```

VBox(children=(HTML(value="<h2 style ='color:#ffffff; background-color:#0000
00;padding-top: 1%; padding-bottom...</pre>

Ver informações em específico sobre qual o computador quântico menos ocupado no momento.

```
In [25]:
    backends_list =provider.backends( simulator=False, open_pulse=False)
 1
 2
 3
    from qiskit.providers.ibmq import least_busy
    backend_device = least_busy(backends_list)
 5
 6
    print("Running on current least busy device: ", backend_device)
 7
    backend device
Running on current least busy device: ibmqx2
VBox(children=(HTML(value="<h1 style='color:#ffffff;background-color:#00000
0; padding-top: 1%; padding-bottom: 1...
Out[25]:
<IBMQBackend('ibmqx2') from IBMQ(hub='ibm-q', group='open', project='main')>
In [26]:
                                                                                           H
    coupling_map = backend_device.configuration().coupling_map
In [27]:
                                                                                           H
   from giskit.providers.aer.noise import NoiseModel
 • Construção do modelo Noise a partir de propriedades backend.
In [28]:
                                                                                           H
    noise_model = NoiseModel.from_backend(backend_device)
    print(noise_model)
NoiseModel:
  Basis gates: ['cx', 'id', 'reset', 'rz', 'sx', 'x']
  Instructions with noise: ['cx', 'reset', 'measure', 'x', 'sx', 'id']
  Qubits with noise: [0, 1, 2, 3, 4]
  Specific qubit errors: [('id', [0]), ('id', [1]), ('id', [2]), ('id',
[3]), ('id', [4]), ('sx', [0]), ('sx', [1]), ('sx', [2]), ('sx', [3]), ('s
x', [4]), ('x', [0]), ('x', [1]), ('x', [2]), ('x', [3]), ('x', [4]), ('cx',
[4, 2]), ('cx', [2, 4]), ('cx', [3, 4]), ('cx', [4, 3]), ('cx', [3, 2]), ('c
x', [2, 3]), ('cx', [1, 2]), ('cx', [2, 1]), ('cx', [0, 2]), ('cx', [2, 0]),
('cx', [0, 1]), ('cx', [1, 0]), ('reset', [0]), ('reset', [1]), ('reset',
[2]), ('reset', [3]), ('reset', [4]), ('measure', [0]), ('measure', [1]),
('measure', [2]), ('measure', [3]), ('measure', [4])]
```

Obter os gates base do modelo noise.

In [29]: ▶

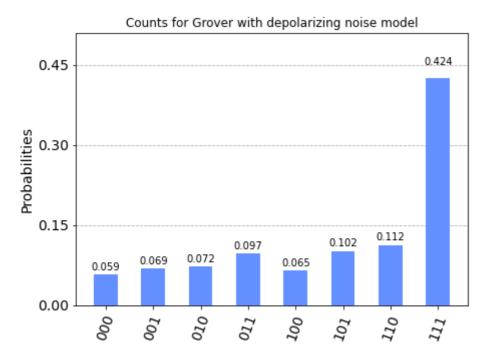
```
basis_gates = noise_model.basis_gates
print(basis_gates)
```

```
['cx', 'id', 'reset', 'rz', 'sx', 'x']
```

• Executa simulação do modelo noise e obtém os counts.

```
In [30]: ▶
```

Out[30]:



· Imprime o count de Grover.

```
In [31]:

1 print(counts_Grover)
```

```
{'111': 782, '001': 33, '110': 37, '000': 38, '011': 32, '100': 32, '010': 35, '101': 35}
```

Imprime o count do modelo noise.

```
In [32]:
                                                                                                  H
   print(counts_noise)
{'111': 434, '011': 99, '101': 104, '000': 60, '110': 115, '001': 71, '010':
74, '100': 67}
In [33]:
                                                                                                  M
  1
    def resume(counts_raw):
 2
         s0=s1=0
  3
         k=counts_raw.keys()
 4
         lk=list(k)
  5
         for c in lk:
             if c[0]=='0':
  6
 7
                  s0 = s0 + counts_raw.get(c)
 8
             else:
 9
                  s1 = s1 + counts_raw.get(c)
         return({'0':s0, '1':s1})
10
In [34]:
                                                                                                  H
   cn = resume(counts_noise)
    c = resume(counts_Grover)

    Desenha o histograma.

In [35]:
   plot_histogram([c,cn], legend= ['simulation','simulation with noise'], color=['#061727
Out[35]:
   1.00
                                                                  simulation
                                          0.865
                                                                  simulation with noise
                                                    0.703
   0.75
Probabilities
   0.50
                       0.297
   0.25
             0.135
```

IBM Q Provider

0.00

Devolve a lista dos computadores quânticos.

0

```
In [36]:

1    from qiskit.tools.monitor import backend_overview, backend_monitor
2    backend_overview()
```

ibmq_manila		ibmq_quito		ibmq_belem	
Num. Qubits: Pending Jobs: Least busy: Operational: Avg. T1: Avg. T2:	23 False True 148.5	Num. Qubits: Pending Jobs: Least busy: Operational: Avg. T1: Avg. T2:	19 False True 80.3	Num. Qubits: Pending Jobs: Least busy: Operational: Avg. T1: Avg. T2:	True True
ibmq_lima		ibmq_santiago		ibmq_athens	
Num. Qubits: Pending Jobs: Least busy:	7	Num. Qubits: Pending Jobs: Least busy:	24	Num. Qubits: Pending Jobs: Least busy:	
Operational: Avg. T1: Avg. T2:	62.4	Operational: Avg. T1: Avg. T2:	120.9	Operational: Avg. T1: Avg. T2:	True 90.2 104.
ibmq_armonk		ibmq_16_melbo		ibmqx2	
Num. Qubits: Pending Jobs: Least busy:	2	Num. Qubits: Pending Jobs: Least busy:	15 19	Num. Qubits: Pending Jobs: Least busy:	1
e Operational: Avg. T1: Avg. T2:	True 169.7 261.0	Operational: Avg. T1: Avg. T2:	54.6	Operational: Avg. T1: Avg. T2:	True 58.6 35.8

• Vamos ver qual o computador quântico menos ocupado.

```
In [37]:

1 print("Running on current least busy device: ", backend_device)
```

Running on current least busy device: ibmqx2

```
In [38]:
                                                                                          H
   backend_monitor(backend_device)
ibmqx2
=====
Configuration
-----
    n_qubits: 5
    operational: True
    status_msg: active
    pending jobs: 1
    backend_version: 2.3.6
    basis_gates: ['id', 'rz', 'sx', 'x', 'cx', 'reset']
    local: False
    simulator: False
    conditional: False
   meas_kernels: ['hw_boxcar']
    qubit_lo_range: [[4.78233846827291e+18, 5.78233846827291e+18], [4.747
504372507464e+18, 5.747504372507464e+18], [4.533385431152394e+18, 5.53338
5431152394e+18], [4.791961703900664e+18, 5.791961703900664e+18], [4.57844
0770845786e+18, 5.578440770845786e+18]]
    pulse num channels: 9
In [39]:
                                                                                          M
 1
   # Informação backend
   backend device
VBox(children=(HTML(value="<h1 style='color:#ffffff;background-color:#00000
0; padding-top: 1%; padding-bottom: 1...
Out[39]:
<IBMQBackend('ibmqx2') from IBMQ(hub='ibm-q', group='open', project='main')>
In [40]:
    %qiskit_job_watcher
Accordion(children=(VBox(layout=Layout(max_width='710px', min_width='710p
x')),), layout=Layout(max_height='500...
<IPython.core.display.Javascript object>
```

• Imprime o ID que será utilizado para executar o circuito definido no computador quântico escolhido.

```
In [41]: ▶
```

```
job_Grover_r = execute(qc_Grover, backend_device, shots=shots)

jobID_Grover_r = job_Grover_r.job_id()

print('JOB ID: {}'.format(jobID_Grover_r))
```

JOB ID: 60bd374d5f4eaa0098dafef9

```
In [43]:

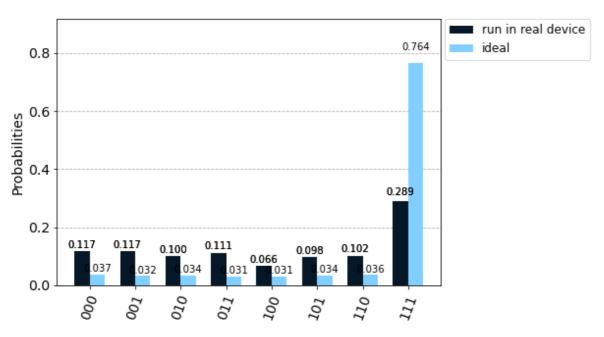
1    job_get=backend_device.retrieve_job("60bd374d5f4eaa0098dafef9")
2    result_Grover_r = job_get.result()
4    counts_Grover_run = result_Grover_r.get_counts(qc_Grover)
```

· Desenha o histograma.

```
In [44]:

1 plot_histogram([counts_Grover_run, counts_Grover], legend=[ 'run in real device', 'idea
```

Out[44]:



· Desenha o circuito.

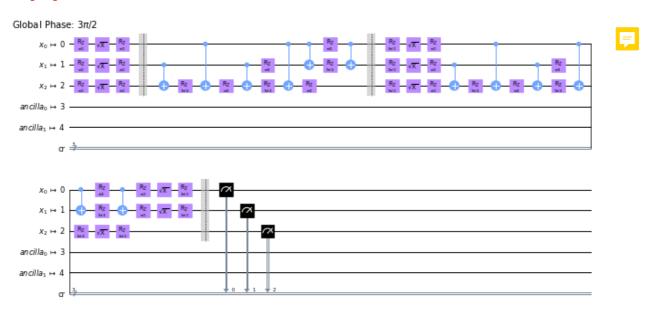
In [45]: ▶

```
from qiskit.compiler import transpile

qc_t_real = transpile(qc_Grover, backend=backend_device)

qc_t_real.draw(output='mpl', scale=0.5)
```

Out[45]:

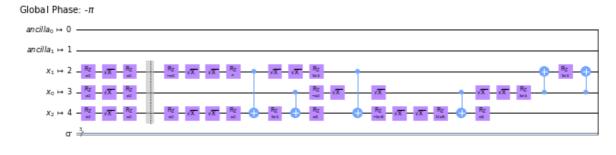


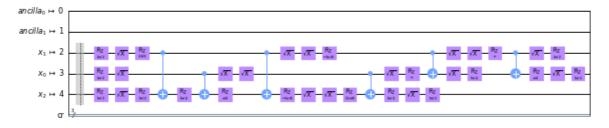
• Otimiza o circuito.

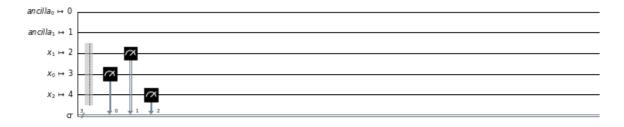
In [46]: ▶

```
qc_optimized = transpile(qc_Grover, backend=backend_device, optimization_level=3)
qc_optimized.draw(output='mpl', scale=0.5)
```

Out[46]:







• Profundidade do circuito de Grover.

In [47]: ▶

1 qc_Grover.depth()

Out[47]:

12

• Profundidade real do circuito executado anteriormente.

In [48]: ▶

```
1 qc_t_real.depth()
```

Out[48]:

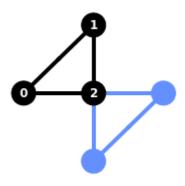
30

• Desenha o layout do circuito.

In [49]: ▶

```
from qiskit.visualization import plot_circuit_layout
plot_circuit_layout(qc_t_real, backend_device)
```

Out[49]:



• Profundidade do circuito otimizado.

In [50]: ▶

```
1 qc_optimized.depth()
```

Out[50]:

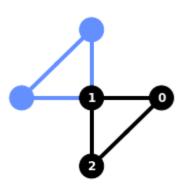
47

· Desenho do circuito otimizado.

```
In [51]:

1 plot_circuit_layout(qc_optimized, backend_device)
```

Out[51]:



• Executa o circuito otimizado no computador quântico.

```
job_exp = execute(qc_optimized, backend_device, shots = shots)

# job_id allows you to retrive old jobs
jobID = job_exp.job_id()

print('JOB ID: {}'.format(jobID))

job_exp.result().get_counts(qc_optimized)
```

JOB ID: 60bd379b1eb0243bf1cefbcb

Out[52]:

In [52]:

```
{'000': 103,
'001': 70,
'010': 109,
'011': 96,
'100': 83,
'101': 113,
'110': 89,
'111': 361}
```

M

```
In [53]: ▶
```

```
#with optimization 2
job_get_o=backend_device.retrieve_job("60bd379b1eb0243bf1cefbcb")

result_real_o = job_get_o.result(timeout=3600, wait=5)

counts_opt = result_real_o.get_counts(qc_optimized)
```

```
In [54]: ▶
```

```
1 %qiskit_disable_job_watcher
```

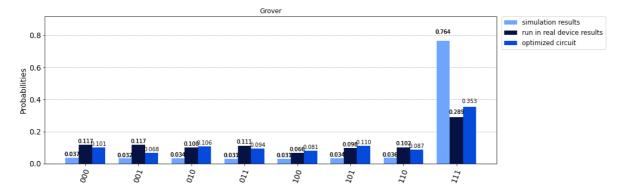
· Desenha o histograma

```
In [55]: ▶
```

```
title = 'Grover'
legend = [ 'simulation results','run in real device results', 'optimized circuit']
color = ['#6ea6ff','#051243','#054ada']

plot_histogram([counts_Grover, counts_Grover_run, counts_opt], legend = legend, title=
```

Out[55]:



IGNIS

Importa as funções de medida e calibração.

• Gera os circuitos de calibração.

```
In [57]:
                                                                                             H
    qr = QuantumRegister(x)
    meas_calibs, state_labels = complete_meas_cal(qubit_list=[0,1,2], qr=qr, circlabel='mca
 · Lista de estados.
In [58]:
                                                                                             H
   state labels
Out[58]:
['000', '001', '010', '011', '100', '101', '110', '111']

    Descobre o ID.

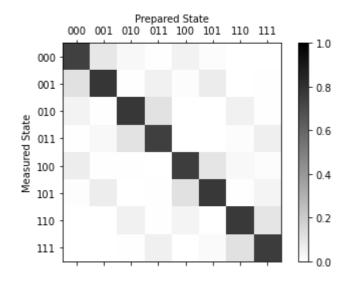
In [59]:
                                                                                             H
    %qiskit_job_watcher
Accordion(children=(VBox(layout=Layout(max_width='710px', min_width='710p
x')),), layout=Layout(max_height='500...
<IPython.core.display.Javascript object>
                                                                                             M
In [60]:
 1
    job_ignis = execute(meas_calibs, backend=backend_device, shots=shots)
 3
    jobID_run_ignis = job_ignis.job_id()
 4
    print('JOB ID: {}'.format(jobID_run_ignis))
JOB ID: 60bd3807917aa0525e9b7fe6
 · Obtém os Resultados.
In [61]:
                                                                                             H
    job_get=backend_device.retrieve_job("60bd3807917aa0525e9b7fe6")
 2
    cal_results = job_get.result()
 3
In [62]:
                                                                                             H
    %qiskit_disable_job_watcher
```

Faz um mapa da matriz de calibração.

In [63]: ▶

```
meas_fitter = CompleteMeasFitter(cal_results, state_labels, circlabel='mcal')

# Plot the calibration matrix
meas_fitter.plot_calibration()
```



```
In [64]:

1 print("Average Measurement Fidelity: %f" % meas_fitter.readout_fidelity())
```

Average Measurement Fidelity: 0.767456

• Obtém o objeto de filtro.

```
In [65]:

1   meas_filter = meas_fitter.filter
2   
3   # Results with mitigation
4   mitigated_results = meas_filter.apply(result_Grover_r)
5   mitigated_counts = mitigated_results.get_counts()
```

· Desenha o histograma.

In [66]: ▶

plot_histogram([counts_Grover_run, mitigated_counts, counts_Grover], legend=['raw', 'mi

Out[66]:

