



Computer Graphics



by Ruen-Rone Lee ICL/ITRI

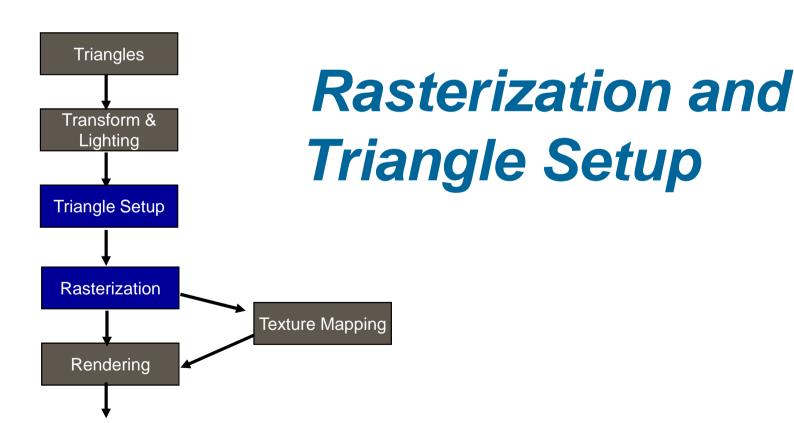


Wrap up from last Class

- Introduction to Computer Graphics
- Graphics Applications
- Graphics Display System
- Concept of Graphics Rendering Pipeline



Part I: Conventional 3D Graphics Pipeline



Primitives
Rasterization
Triangle Setup









Point
Line
Circle
Polygon
Triangles

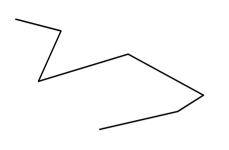


Primitives

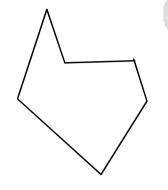
Primitives

Primitive types



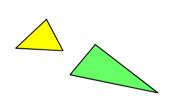


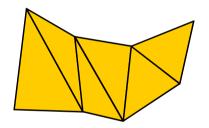
LINE_STRIP

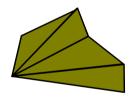


LINE_LOOP







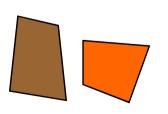


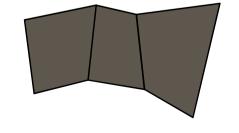
POLYGON

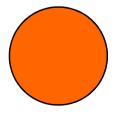
TRIANGLES

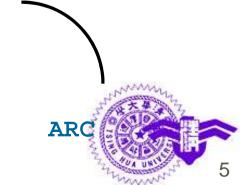
TRIANGLE_STRIP

TRIANGLE_FAN









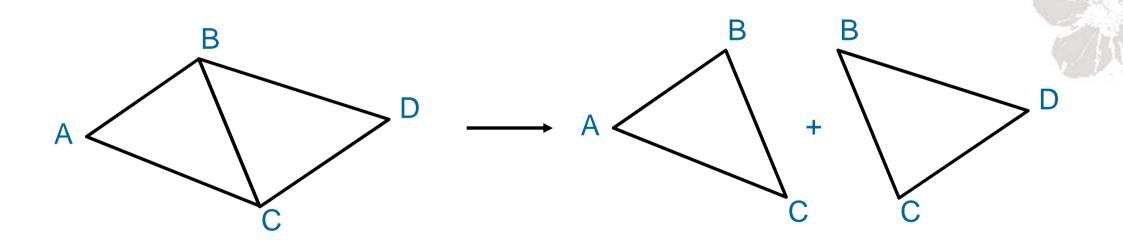
QUADS

QUAD_STRIP

CIRCLE

Triangles

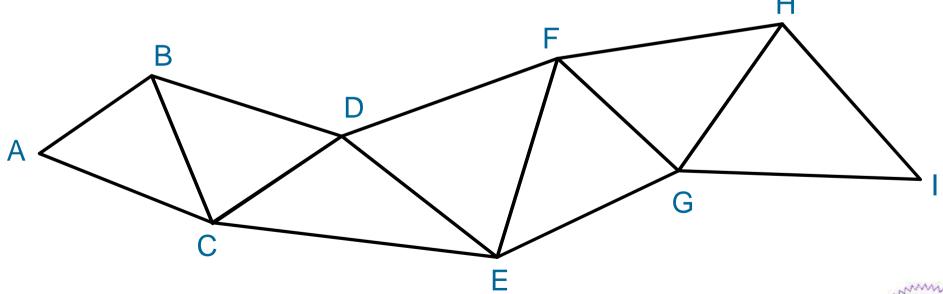
- Triangle List
 - A list of individually defined triangles





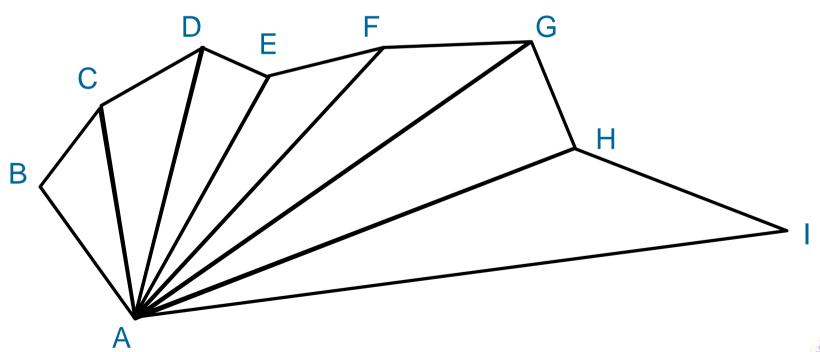
Triangles

- ◆ Triangle Strip
 - A new triangle is defined with one new vertex and two shared vertices from triangle defined immediate prior to it



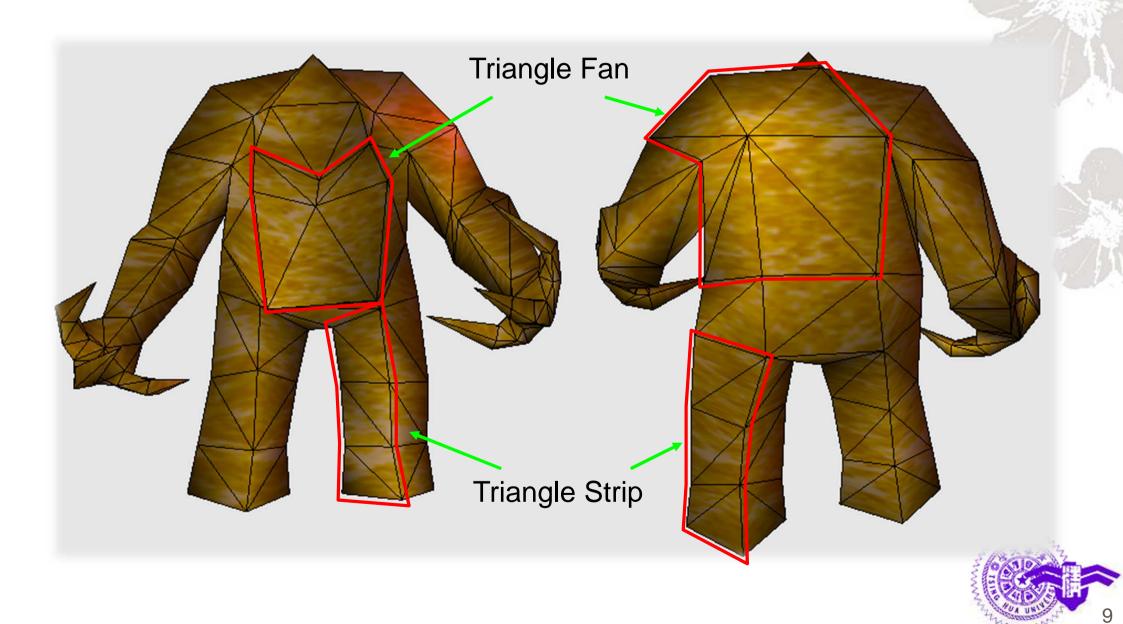
Triangles

- Triangle Fan
 - Similar to triangle strip but with one common shared vertex for each triangle





Application of Triangle Primitives

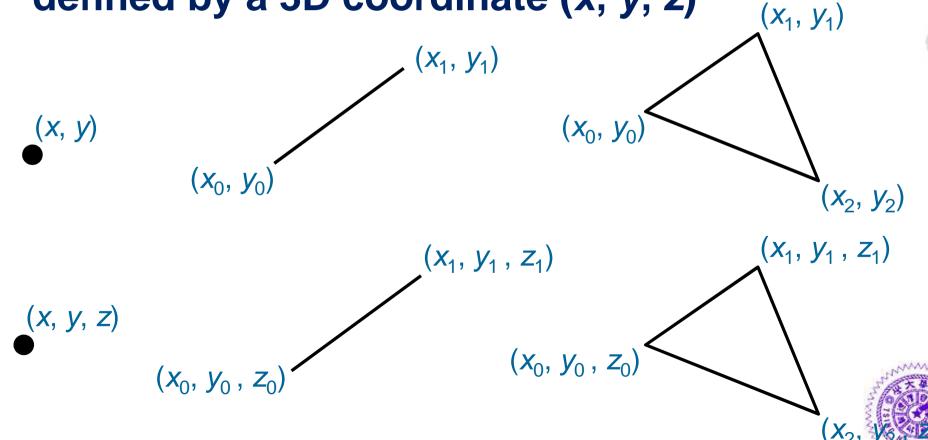


2D vs. 3D Primitives

Points / Lines / Triangles (Polygons)

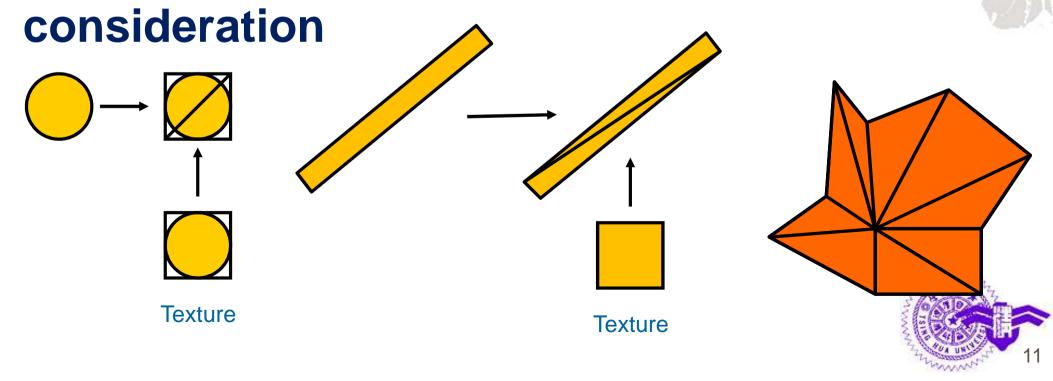
Similar to 2D primitives except each vertex is

defined by a 3D coordinate (x, y, z)



Implementation Consideration

- Points are sometimes implemented as sprite with size and texture defined.
- Points, lines or polygons can be converted into triangles for implementation









Modeling using Primitives

Model Editing

Model Data



Basic 3D Modeling

Modeling using Primitives

 Using geometric primitives as the basic building components

Getting started with Google SketchUp

Google





Modeling using Primitives

Using primitives and the associated

operations

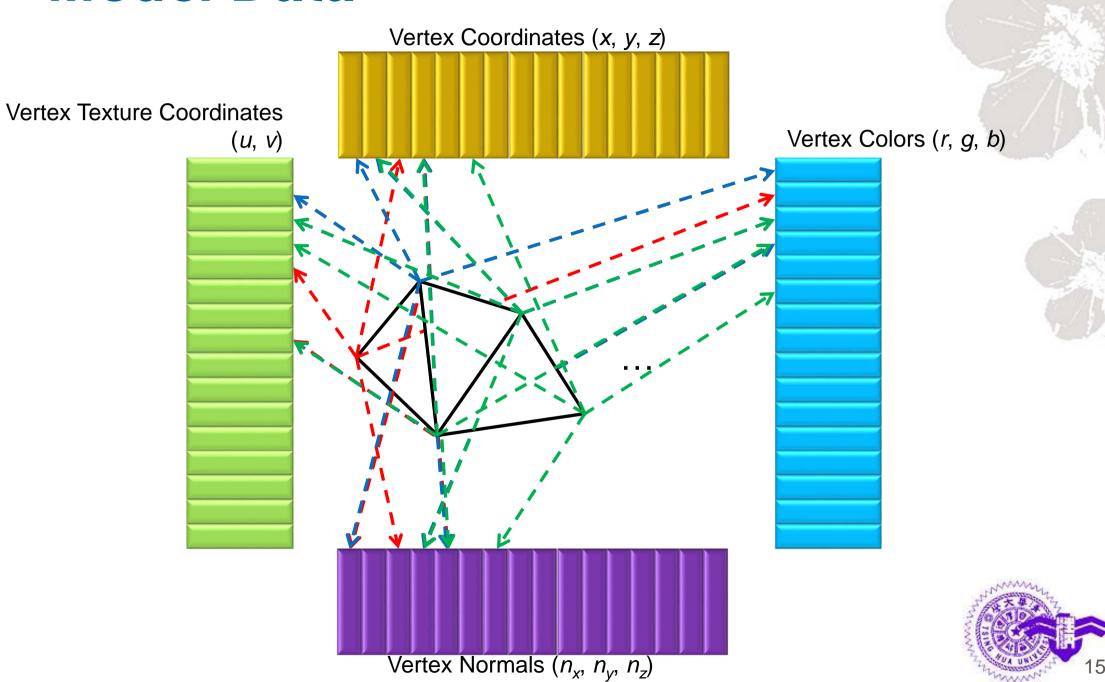








Model Data



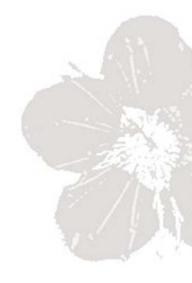
Example 3D Model Data Format

- Wavefront 3D Graphics model description file with extension .obj
- Refer to
 http://en.wikipedia.org/wiki/Wavefront_.obj_file
 for detail file format
- Example
 - Model with colors (boxC.obj)
 - Model with normals (boxN.obj, boxN.mtl)
 - Model with textures (boxT.obj, boxT.mtl, tex1.tga, tex2.jpg)











Scan Converting Lines
Scan Converting Circles
Scan Converting Polygons



- Principles
 - The sequence of pixels should lie as close as possible to the ideal line
 - The scan converted line should be as straight as possible





Implicit Form

$$f(x,y) = ax + by + c = 0$$

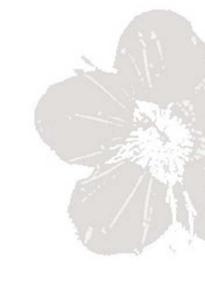
Explicit Form

$$y = f(x) = mx + B$$

Parametric Form

$$x = x(t) = a_0 t + b_0$$

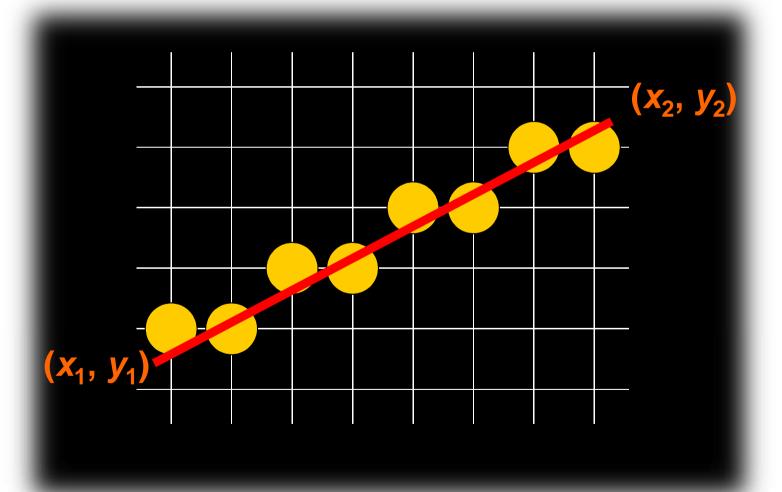
$$y = y(t) = a_1 t + b_1$$







• Example: Draw from (x_1, y_1) to (x_2, y_2)

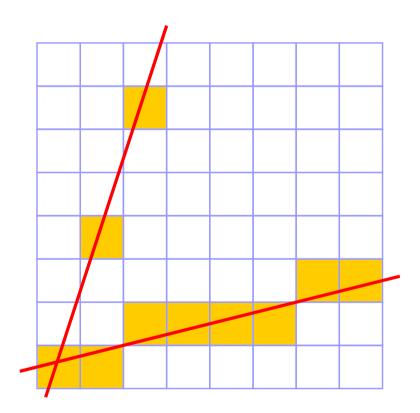




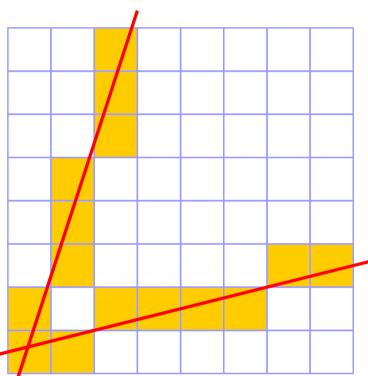




Quality Issues



Gaps exist in slope > 1

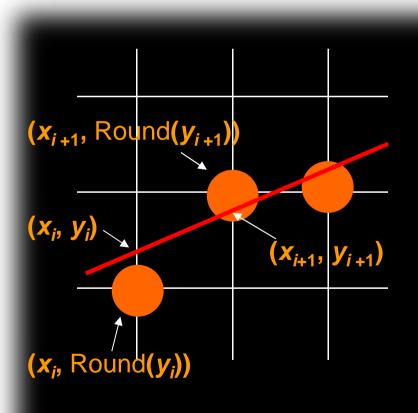








 Incremental Algorithm (DDA: Digital Differential Analyzer)



```
y = mx + B, where m = \Delta y/\Delta x, and 0 \le m \le 1

y_i = mx_i + B

draw pixel at (x_i, \text{Round}(y_i))
```

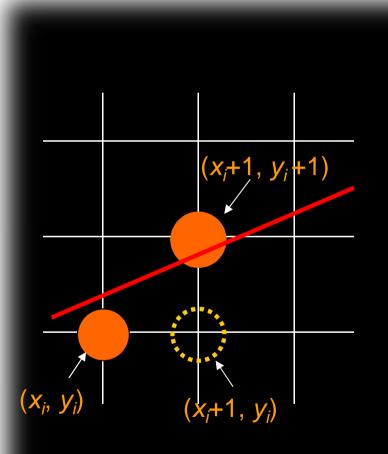
$$x_{i+1} = x_i + 1$$

$$y_{i+1} = mx_{i+1} + B$$

$$= m(x_i + 1) + B$$

$$= y_i + m$$
draw pixel at $(x_{i+1}, \text{Round}(y_{i+1}))$

Bresenham Algorithm



$$y = mx + B$$
, where $m = \Delta y/\Delta x$, and $0 \le m \le 1$

Current pixel : (x_i, y_i)

Next pixel:
$$(x_i+1, y_i)$$
 or (x_i+1, y_i+1)

$$d_1 = y - y_i = m(x_i + 1) + B - y_i$$

$$d_2 = y_i + 1 - y = y_i + 1 - m(x_i + 1) - B$$

$$d_1 - d_2 = 2m(x_i + 1) - 2y_i + 2B - 1$$

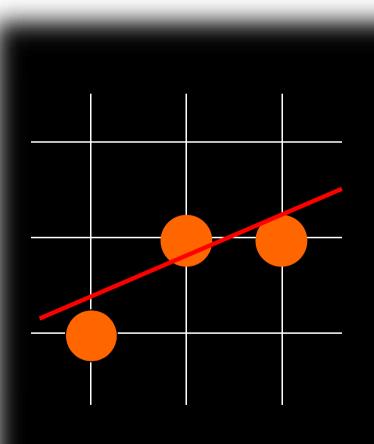
Let
$$P_i = \Delta x (d_1 - d_2) = 2\Delta y \cdot x_i - 2\Delta x \cdot y_i + C$$

where $C = 2\Delta y + \Delta x (2B - 1)$

If
$$P_i < 0$$
 then choose (x_i+1, y_i) otherwise, choose (x_i+1, y_i+1)



◆ Incremental Computation of P_i



$$P_{i+1} = 2\Delta y \cdot x_{i+1} - 2\Delta x \cdot y_{i+1} + C$$

= $2\Delta y \cdot (x_i+1) - 2\Delta x \cdot y_{i+1} + C$
= $P_i + 2\Delta y - 2\Delta x (y_{i+1} - y_i)$

Incremental update:

When
$$P_i < 0$$
, $P_{i+1} = P_i + 2\Delta y$

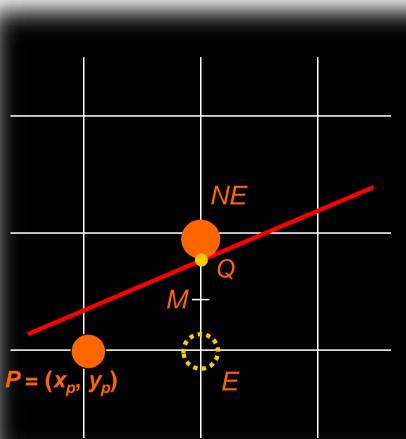
When
$$P_i \ge 0$$
, $P_{i+1} = P_i + 2\Delta y - 2\Delta x$

Initial Value:

$$P_1 = 2\Delta y - \Delta x$$



Mid-Point Algorithm



$$y = mx + B$$
, where $m = \Delta y/\Delta x$, and $0 \le m \le 1$

$$F(x, y) = \Delta y \cdot x - \Delta x \cdot y + B \cdot \Delta x = 0$$

let $a = \Delta y$, $b = -\Delta x$, and $c = B \cdot \Delta x$

Current pixel: (x_p, y_p)

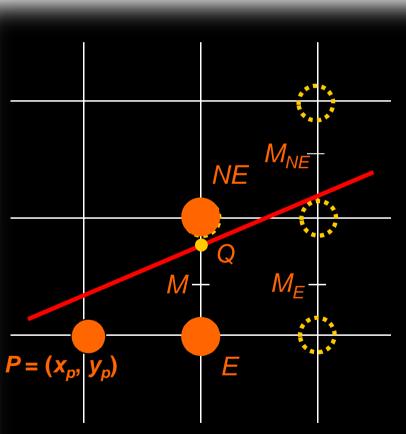
Let
$$d = F(M) = F(x_p + 1, y_p + \frac{1}{2})$$

If d > 0, then choose pixel NE

If $d \le 0$, then choose pixel E



Mid-Point Algorithm



$$d_{old} = F(x_p+1, y_p+1/2) = a(x_p+1) + b(y_p+1/2) + c$$

If E is chosen, then

$$d_E = F(x_p+2, y_p+1/2)$$
= $a(x_p+2) + b(y_p+1/2) + c$
= $d_{old} + a$

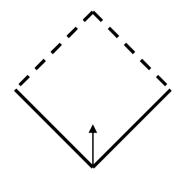
If NE is chosen, then

$$d_{NE} = F(x_p+2, y_p+\frac{3}{2})$$

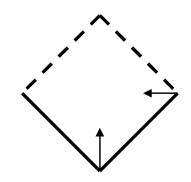
$$= a(x_p+2) + b(y_p+\frac{3}{2}) + c$$

$$= d_{old} + a + b$$

- Diamond Test Area
 - x-major lines (-1 \leq slope \leq 1)



y-major lines (slope < -1 or slope > 1)



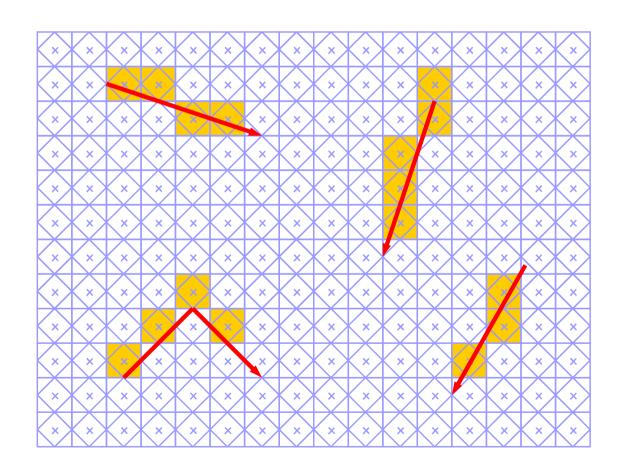


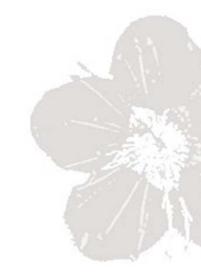






Diamond Check









Issues on Scan Converting Lines

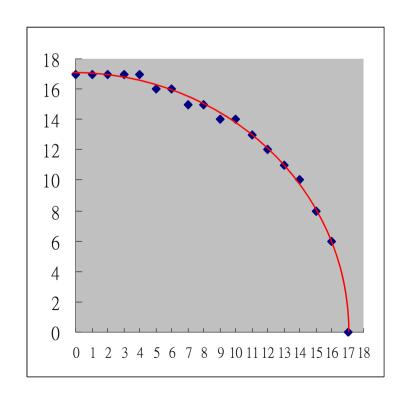
- Precision
 - Fixed-point (e.g. s.7.16)
 - Floating-point (e.g. s.[8].23)
- Endpoint Order
 - Left to right or right to left
- Aliasing
 - Coverage of a line

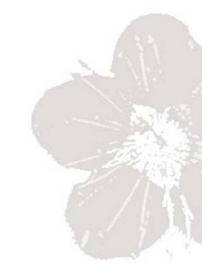


Method I

$$x^{2} + y^{2} = R^{2}$$

 $y = \pm \operatorname{sqrt}(R^{2} - x^{2}), x = 0, 1, ..., R$



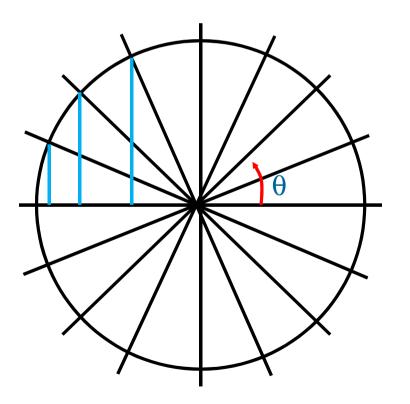


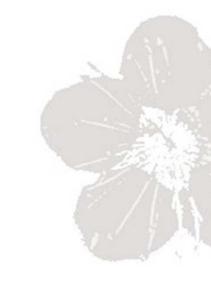




Method II

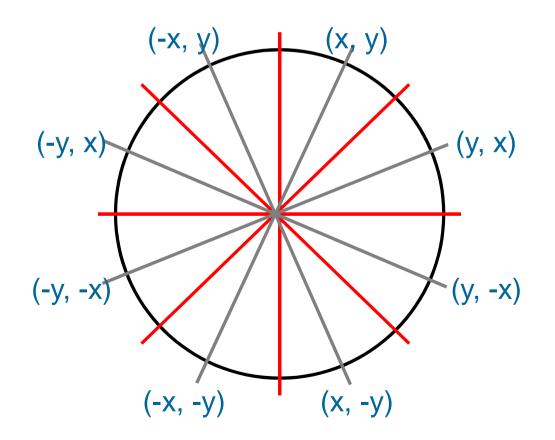
$$(x, y) = (r \cos \theta, r \sin \theta), \theta = 0^{\circ}, \dots, 360^{\circ}$$

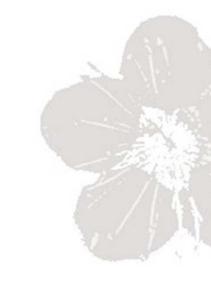






Method IIIEight-Way Symmetry

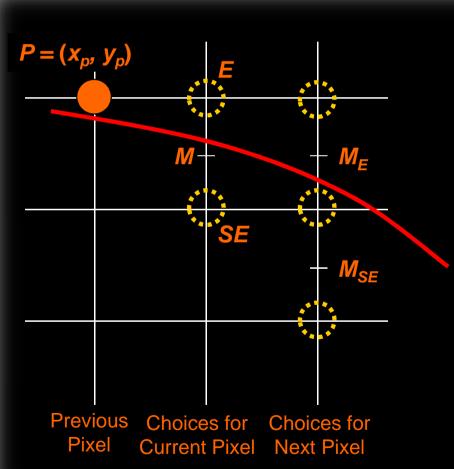








Midpoint Circle Algorithm



Let
$$F(x, y) = x^2 + y^2 - R^2$$

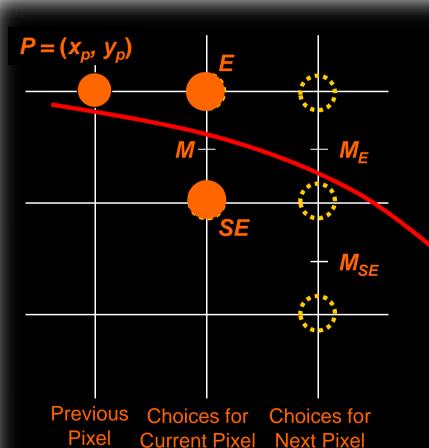
Current Pixel: (x_p, y_p)

Let
$$d = F(M) = F(x_p+1, y_p-1/2)$$

If $d \ge 0$, then choose pixel SE

If d < 0, then choose pixel E

Midpoint Circle Algorithm



$$d_{old} = F(x_p+1, y_p-1/2) = (x_p+1)^2 + (y_p-1/2)^2 - R^2$$

If E is chosen, then

$$d_E = F(x_p+2, y_p-1/2)$$

$$= (x_p+2)^2 + (y_p-1/2)^2 - R^2$$

$$= d_{old} + (2x_p+3)$$

If SE is chosen, then

$$d_{SE} = F(x_p+2, y_p-3/2)$$

$$= (x_p+2)^2 + (y_p-3/2)^2 - R^2$$

$$= d_{old} + (2x_p - 2y_p + 5)$$

Rectangle Fill

- Determine which pixels to fill
 - Taking successive scan lines that intersect the rectangle
 - Filling in spans of adjacent pixels that lie inside the rectangle from left to right





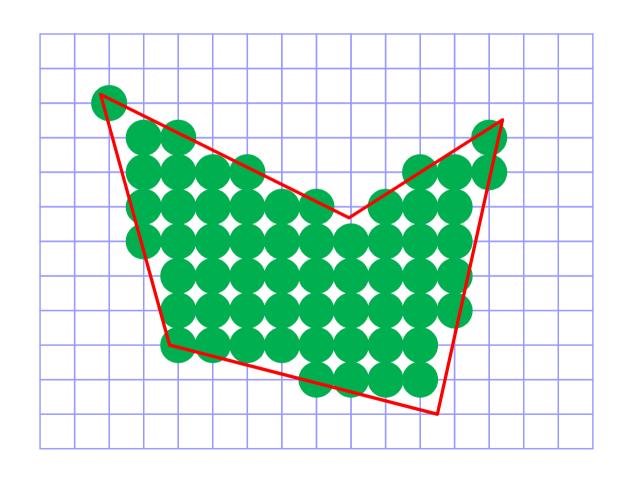
Polygon Fill

- Find the intersections of the scan line with all edges of the polygon
- Sort the intersections by increasing the x coordinate
- Fill in all pixels between pairs of intersections that lie inside the polygon (using odd-parity rule)





◆ Example



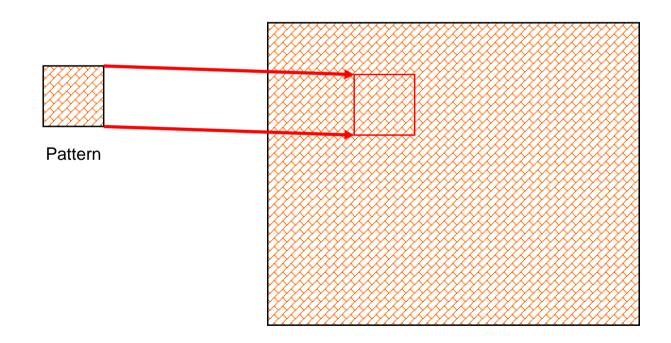






Pattern Fill

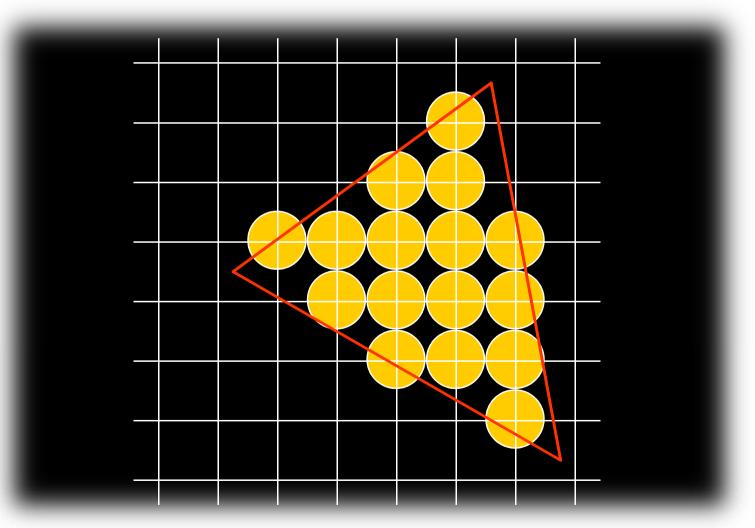
 A pattern map is retrieved and mapped onto the destination primitive

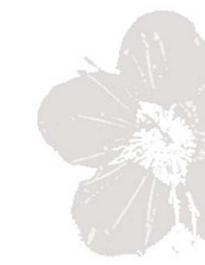






Generate Interior Pixels of a Triangle









Triangle Rasterization



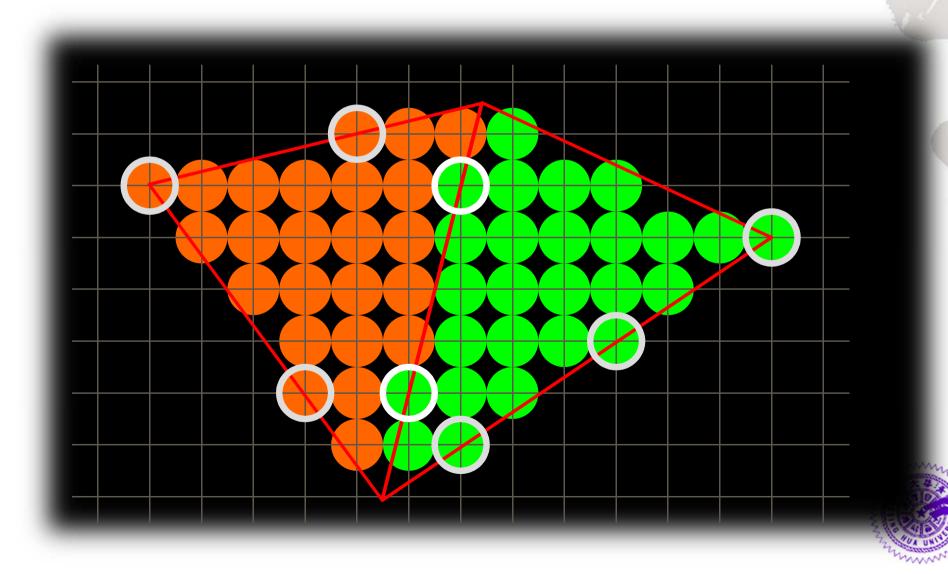


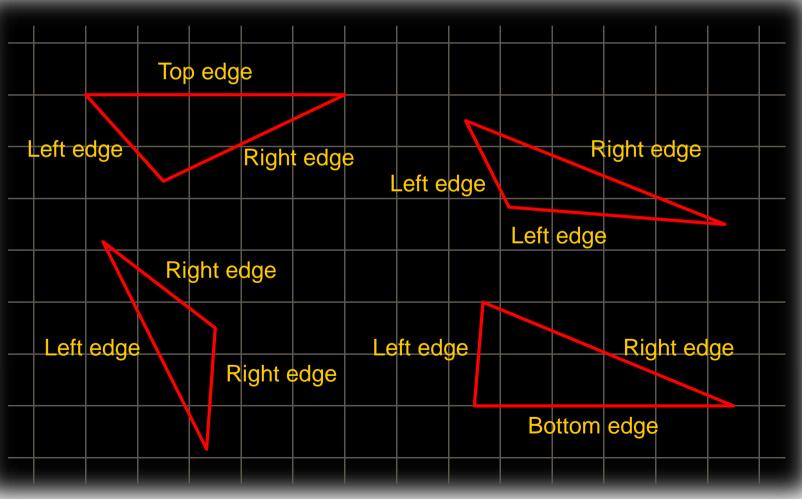
Triangle Rasterization
Triangle Rasterization Rule



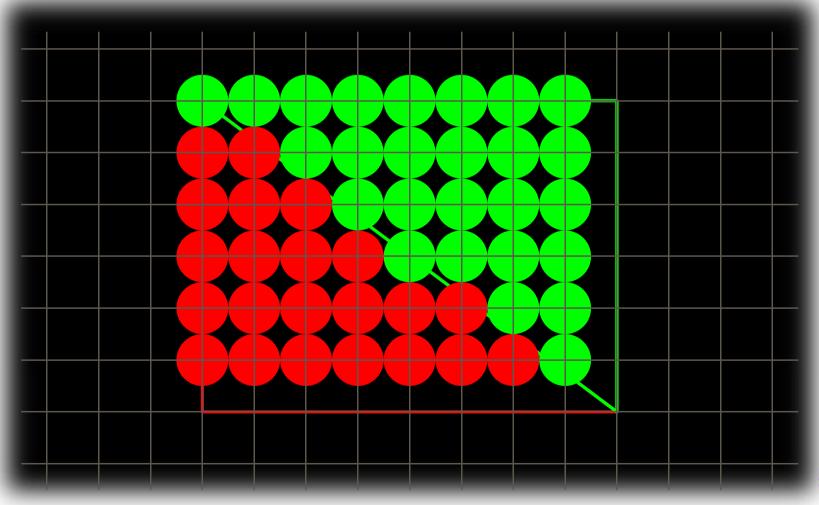
Triangle Rasterization

Scan Line Conversion

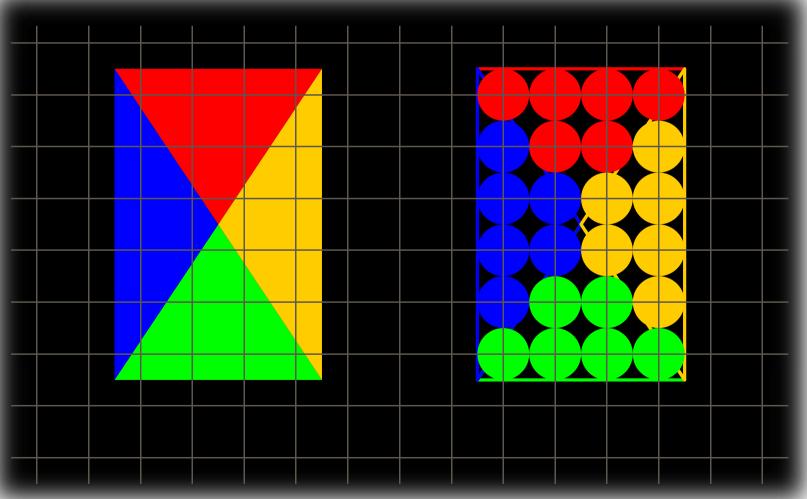




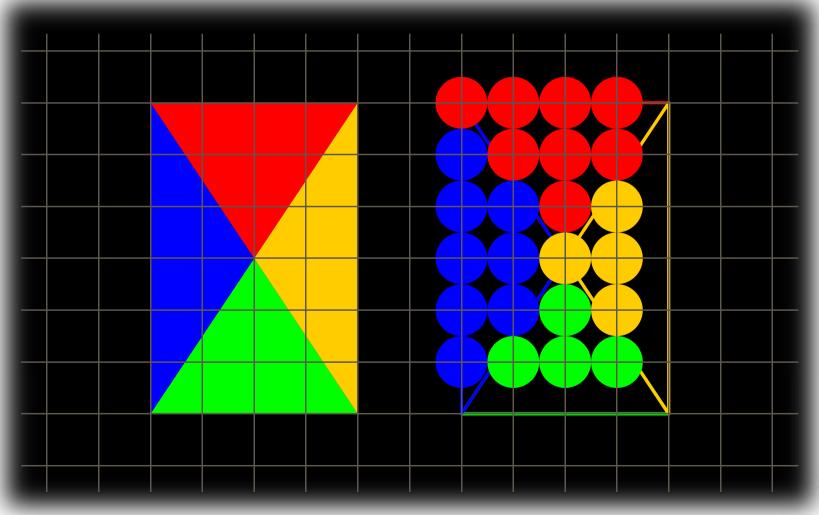














- Sorting is required to scan covert from top to bottom
- For each scan line, scan convert from left to right
- Mid-point check for not over shooting and switch to right slope



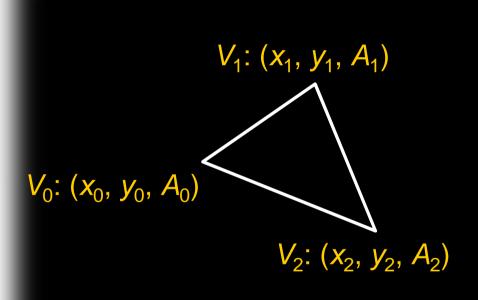
Attribute Derivation inside a Triangle

Color
Depth
Texture Coordinates



Attribute Derivation

Plane Equation



$$f(x, y, A) = ax + by + cA + d = 0$$

$$(a, b, c) = \overrightarrow{V_0 V_1} \times \overrightarrow{V_0 V_2}$$
 d is a constant

$$A = f(x, y)$$

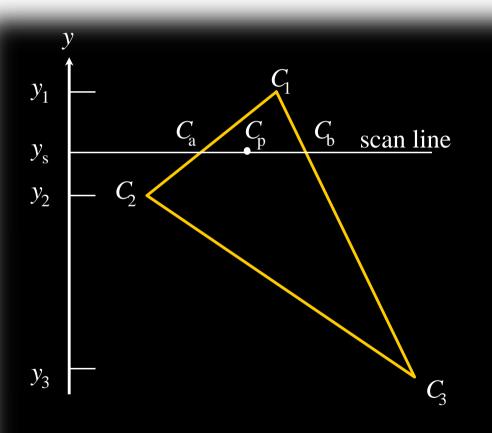
= $-(a/c)x - (b/c)y - (d/c)$

$$A_i = f(x_i, y_i)$$



Attribute Derivation

Interpolation



$$C_a = C_1 - (C_1 - C_2) \frac{y_1 - y_s}{y_1 - y_2}$$

$$C_b = C_1 - (C_1 - C_3) \frac{y_1 - y_s}{y_1 - y_3}$$

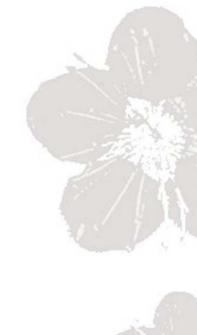
$$C_p = C_a - (C_a - C_b) \frac{x_a - x_p}{x_a - x_b}$$



(255, 0, 0)Attribute Derivation Color Interpolation (0, 0, 0)(0, 0, 0)Red (0, 0, 0)(255, 0, 0)Green (0, 0, 0)(0, 255, 0) (0, 0, 0)(0, 0, 255)(0, 255, 0)Blue (0, 0, 255) (0, 0, 0)



- Advantage of Interpolation
 - Can apply the concept of DDA to reduce computation cost

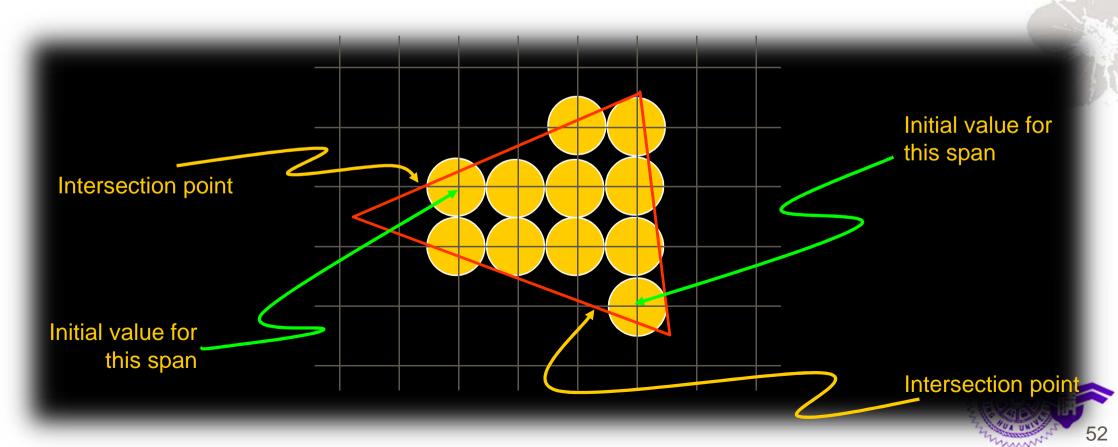






Attribute Derivation

- Disadvantage of Interpolation using DDA
 - Need to derive the initial value for each span
 - Precision error will accumulate



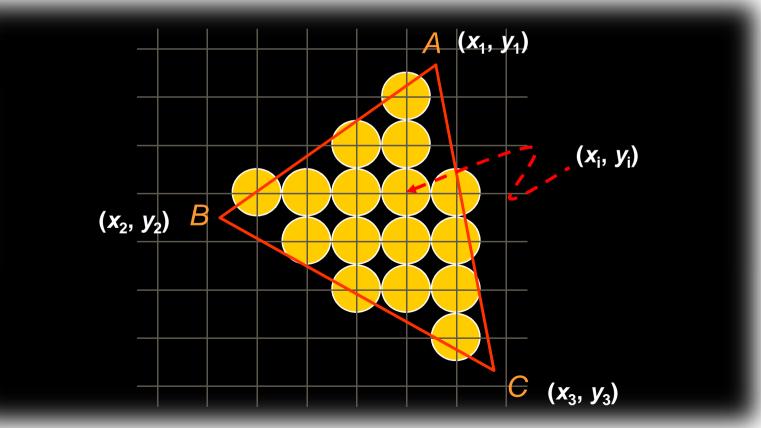
Setup for Coordinate Rasterization



Screen Coordinates

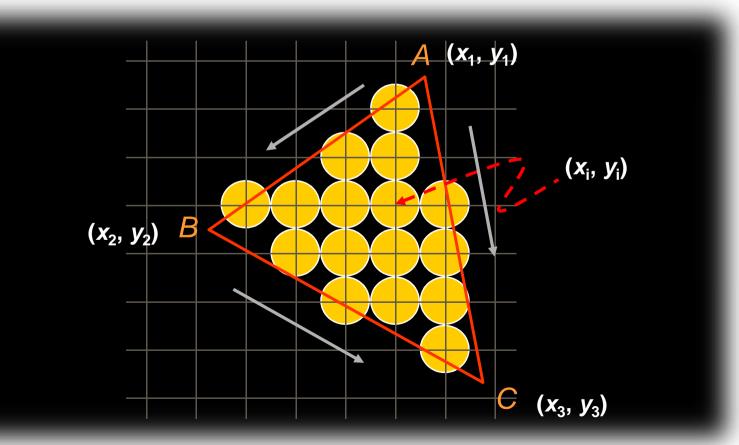


- Initial setup for triangle rasterization
 - Use to generate digitized (x, y) coordinates inside a triangle





- Initial setup for triangle rasterization
 - Calculate gradients, $\Delta x/\Delta y$ for lines AB, BC, and AC





- Initial setup for triangle rasterization
 - Calculate gradients, $\Delta x / \Delta y$ for lines AB, BC, and AC

Line AB:
$$\Delta x / \Delta y = \frac{x_2 - x_1}{y_2 - y_1}$$

Line BC: $\Delta x / \Delta y = \frac{x_3 - x_2}{y_3 - y_2}$

Line AC: $\Delta x / \Delta y = \frac{x_3 - x_1}{y_3 - y_1}$

(x_1, y_2)

(x_2, y_2)

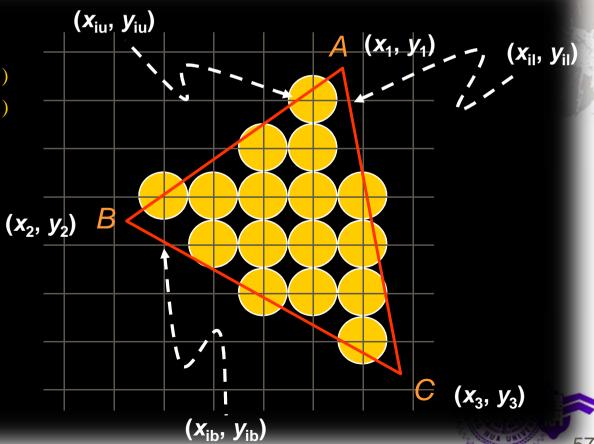
(x_3, y_3)

- Initial setup for triangle rasterization
 - Y intersections for the line segments

$$x_{iu} = x_1 + \frac{x_2 - x_1}{y_2 - y_1} (y_{iu} - y_1), y_{iu} = \begin{cases} y_1 & \text{if } y_1 = \text{int}(y_1) \\ \text{int}(y_1) + 1 & \text{if } y_1 \neq \text{int}(y_1) \end{cases}$$

$$x_{ib} = x_2 + \frac{x_3 - x_2}{y_3 - y_2} (y_{ib} - y_2), y_{ib} = \begin{cases} y_2 & \text{if } y_2 = \text{int}(y_2) \\ \text{int}(y_2) + 1 & \text{if } y_2 \neq \text{int}(y_2) \end{cases}$$

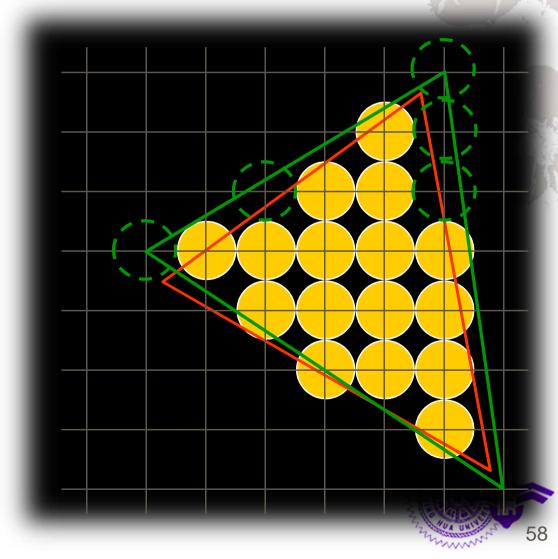
$$x_{il} = x_1 + \frac{x_3 - x_1}{y_3 - y_1} (y_{il} - y_1), y_{il} = \begin{cases} y_1 & \text{if } y_1 = \text{int}(y_1) \\ \text{int}(y_1) + 1 & \text{if } y_1 \neq \text{int}(y_1) \end{cases}$$



Adjustment to the vertex position might

cause

- Distortion
- Draw different pixels than the pixels without vertex adjustment







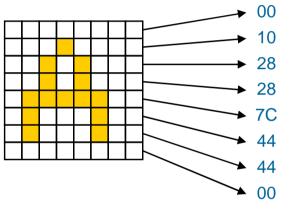


Text Display
Block Copy
Raster Operations



2D Text

 Use rectangle fill with character bitmap pattern



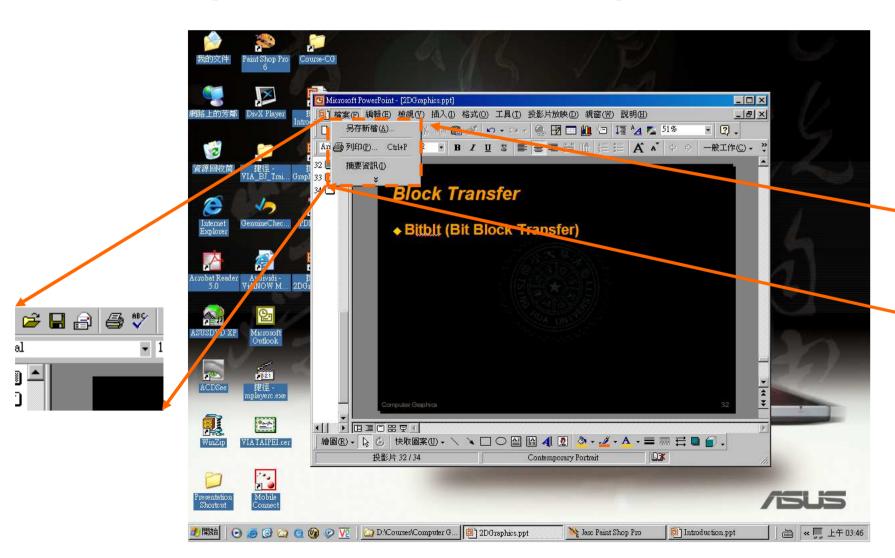
ABCDEFGHIJKLMN OPQRSTUVWXYZ abcdefghijklmnopqr stuvwxyz

- Attributes
 - Font (Time Roman, Courier, Arial)
 - Appearance (Normal, Bold, Italic, Underline)
 - Size (points)
 - Constant/Proportional Spacing



Block Transfer

Bitblt (Bit Block Transfer)



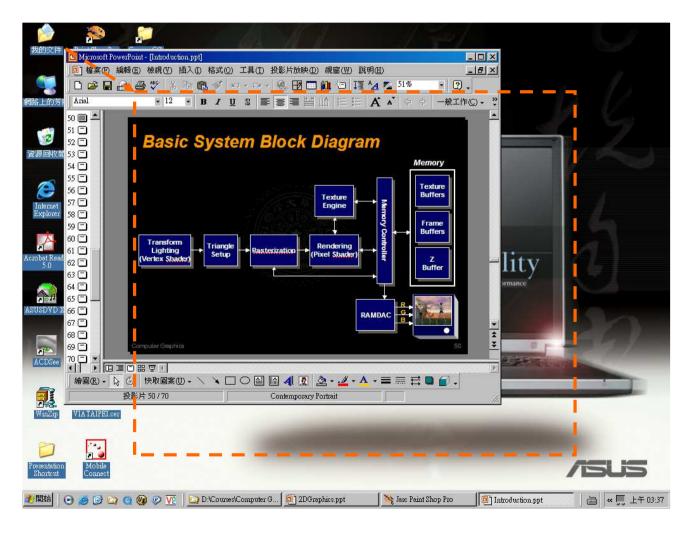








Bitblt (Bit Block Transfer)







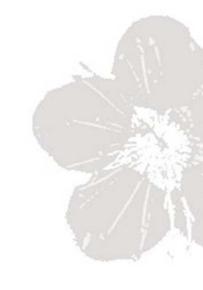


◆ ROP3 (Source, Pattern, Destination)













◆ ROP3 (Source, Pattern, Destination)

Brush "P"	1	1	1	1	0	0	0	0			
Source "S"	1	1	0	0	1	1	0	0	Code in Hex	Name	Boolean Equation (C style)
Background "D"	1	0	1	0	1	0	1	0			
Result	0	0	0	0	0	0	0	0	00	BLACKNESS	0
	0	0	0	1	0	0	0	1	11	NOTSRCERASE	~(D S)
	0	0	1	1	0	0	1	1	33	NOTSRCCOPY	~S
	0	1	0	0	0	1	0	0	44	SRCERASE	S&~D
	0	1	0	1	0	1	0	1	55	DSTINVERT	~D
	0	1	0	1	1	0	1	0	5 A	PATINVERT	D^P
	0	1	1	0	0	1	1	0	66	SRCINVERT	D^S
	1	0	0	0	1	0	0	0	88	SRCAND	D&S
	1	0	1	1	1	0	1	1	BB	MERGEPAINT	D ~S
	1	1	0	0	0	0	0	0	C0	MERGECOPY	P&S
	1	1	0	0	1	1	0	0	CC	SRCCOPY	>S
	1	1	1	0	1	1	1	0	EE	SRCPAINT	D S
	1	1	1	1	0	0	0	0	F0	PATCOPY	P
	1	1	1	1	1	0	1	1	FB	PATPAINT	D P ~S
	1	1	1	1	1	1	1	1	FF	WHITENESS	1





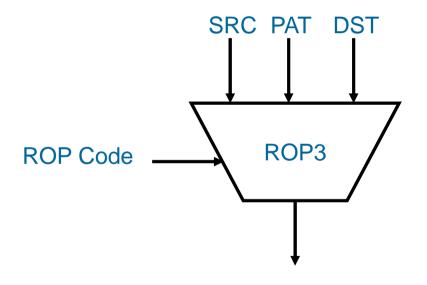


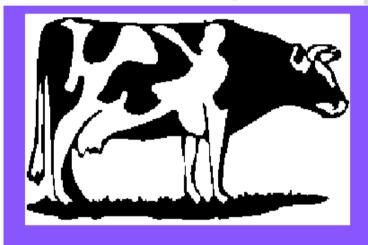
Raster Operations

◆ ROP3 (Source, Pattern, Destination)



SRC & DST







Q&A





