Show

$$2x + 1 \in \mathbb{Z}_4[x] \quad \text{has a multiplicative}$$

inverse in $\mathbb{Z}_4[x]$

$$(2x + 1)(2x + 1) = 4x^2 + 4x + 1 = 1$$