

Matrix or 2D array or Grid

	c0	c1	c2	c3	c4
r0	0,0	0,1	0,2	0,3	0,4
r1	1,0	1,1	1,2	1,3	1,4
r2	2,0	2,1	2,2	2,3	2,4
r3	3,0	3,1	3,2	3,3	3,4
r4	4,0	4,1	4,2	4,3	4,4
r5	5,0	5,1	5,2	5,3	5,4

$m \times n$
 6×5

~~Derived
datatype~~

int [][] mat
= new int [6][5];

```
-for(int row=0; row<6; row++){  
    for(int col=0; col<5; col++){  
        mat [row][col] = scn.nextInt();  
        System.out.print(mat [row][col] + " ");  
    }  
    System.out.println();  
}
```

```

int rows = 6, cols = 5;
int[][] mat = new int[rows][cols];

// Input
for(int row = 0; row < rows; row++){
    for(int col = 0; col < cols; col++){
        mat[row][col] = row * 10 + col;
    }
}

// Output
for(int row = 0; row < rows; row++){
    for(int col = 0; col < cols; col++){
        System.out.print(mat[row][col] + " ");
    }
    System.out.println();
}

```

not preferred
 # no of cells = N (eg $\underline{\underline{30}}$)

Time $\Rightarrow O(N)$

Space (Create matrix)
 $\Rightarrow O(N)$

\star no of rows = m , no of cols = n

Time $\Rightarrow O(m \times n)$

Input Space $\Rightarrow O(m \times n)$

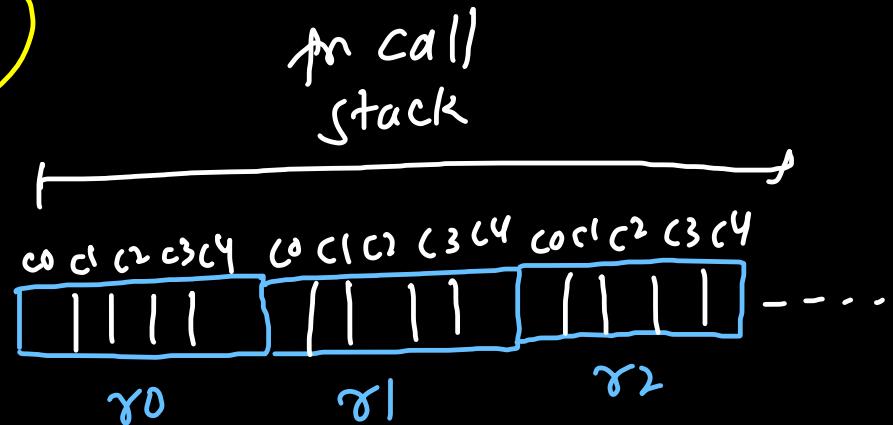
quadratic

memory mapping

C++ (2d arrays → row major form)

	c0	c1	c2	c3	c4
r0	0,0	0,1	0,2	0,3	0,4
r1	1,0	1,1	1,2	1,3	1,4
r2	2,0	2,1	2,2	2,3	2,4
r3	3,0	3,1	3,2	3,3	3,4
r4	4,0	4,1	4,2	4,3	4,4
r5	5,0	5,1	5,2	5,3	5,4

1d array



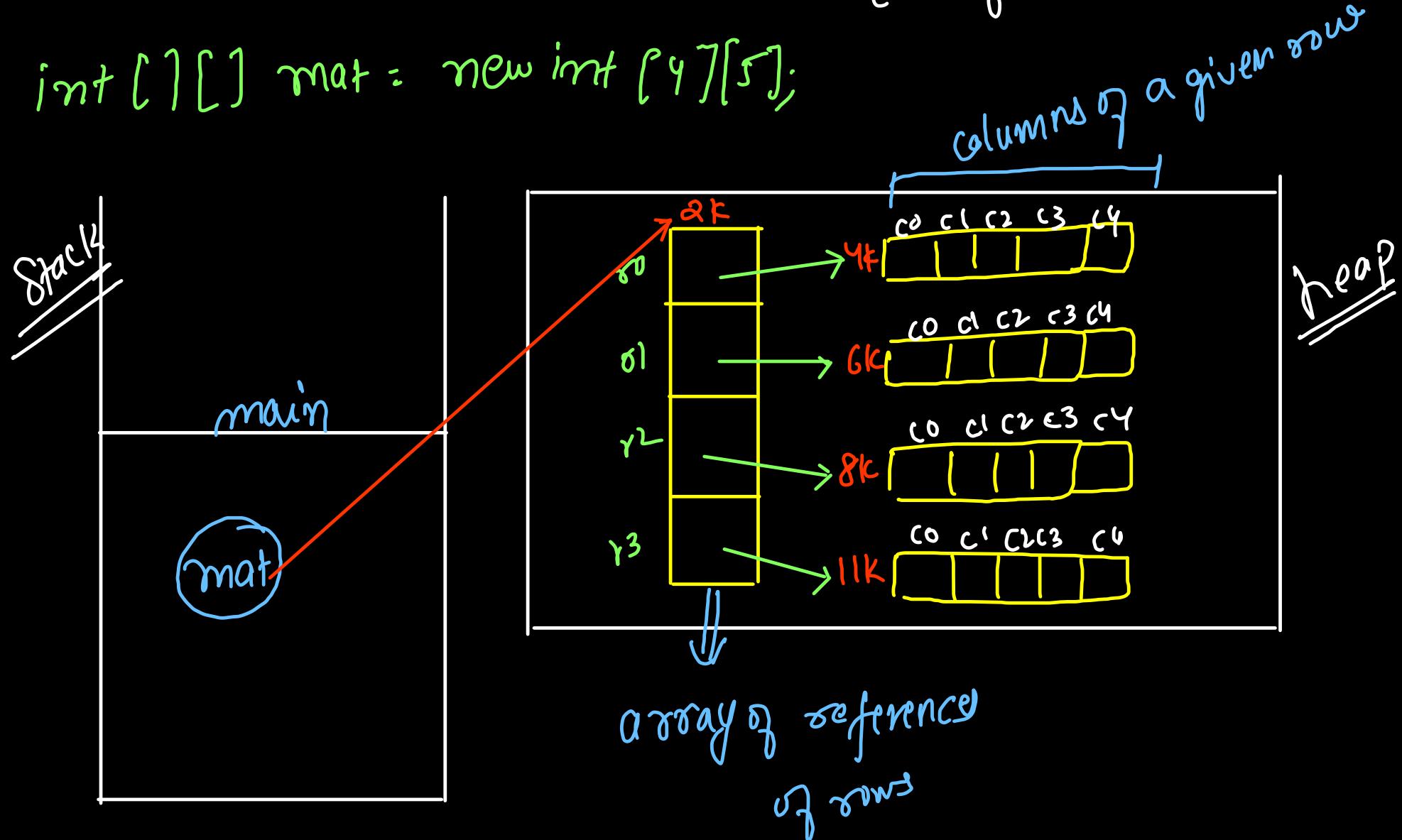
advantage: contiguous
(random access)

disadvantage: availability
of contiguous space

Java (jagged arrays)

no of rows = mat.length
no of columns = mat[0].length

```
int[][] mat = new int[4][5];
```



```
Scanner scn = new Scanner(System.in);

int rows = scn.nextInt();
int cols = scn.nextInt();
int[][] mat = new int[rows][cols];

// Input
for(int row = 0; row < mat.length; row++){
    for(int col = 0; col < mat[0].length; col++){
        mat[row][col] = scn.nextInt();
    }
}

// Output
for(int row = 0; row < mat.length; row++){
    for(int col = 0; col < mat[0].length; col++){
        System.out.print(mat[row][col] + " ");
    }
    System.out.println();
}
```

Finished in 127 ms

0 1 2 3
10 11 12 13
20 21 22 23

stdin ▾

3 4
00 01 02 03
10 11 12 13
20 21 22 23

```
int[][] mat = new int[4][];  
  
for(int row = 0; row < mat.length; row++){  
    mat[row] = new int[row + 1];  
    for(int col = 0; col < mat[row].length; col++){  
        mat[row][col] = row * 10 + col;  
        System.out.print(mat[row][col] + " ");  
    }  
    System.out.println();  
}
```

Finished in 138 ms

0

10 11

20 21 22

30 31 32 33

Each row can have different no of columns

```

String[] words = new String[5];

for(int idx = 0; idx < words.length; idx++){
    words[idx] = scn.next();
    System.out.print(words[idx] + " ");
}

System.out.println();

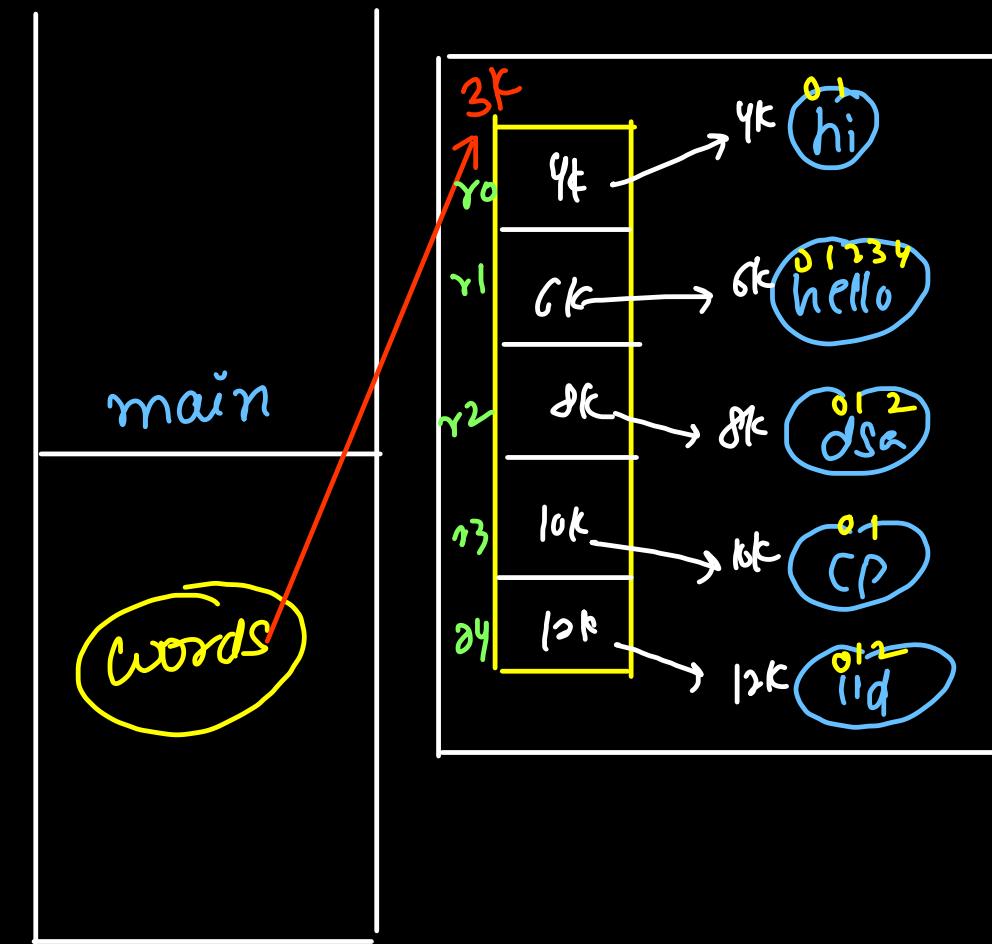
for(int row = 0; row < words.length; row++){
    for(int col = 0; col < words[row].length(); col++){
        System.out.print(words[row].charAt(col) + " ");
    }
    System.out.println();
}

```

↑ string fix
charackr

h	i			
h	e	l	l	o
d	s	a		
c	p			
l	l	d		

→ List< List< ?>>
 → methods → return
 → shallow vs deep



	c0	c1	c2	c3	c4
r0	0,0	0,1	0,2	0,3	0,4
r1	1,0	1,1	1,2	1,3	1,4
r2	2,0	2,1	2,2	2,3	2,4
r3	3,0	3,1	3,2	3,3	3,4
r4	4,0	4,1	4,2	4,3	4,4
r5	5,0	5,1	5,2	5,3	5,4

```
// Output: Row by Row Traversal
for(int row = 0; row < mat.length; row++){
    for(int col = 0; col < mat[0].length; col++){
        System.out.print(mat[row][col] + " ");
    }
    System.out.println();
}
System.out.println();

// Output: Col by Col Traversal
for(int col = 0; col < mat[0].length; col++){
    for(int row = 0; row < mat.length; row++){
        System.out.print(mat[row][col] + " ");
    }
    System.out.println();
}
```

$O(n)$ $\rightarrow O(m)$

$O(1)$

$O(m \times n)$ quadratic

$O(n)$ $\rightarrow O(m)$

$O(1)$

$O(n \times m)$ quadratic

how level
row by row \Rightarrow better \Rightarrow locality of reference

c_0	c_1	c_2	c_3
γ_0	10 \rightarrow 20 \rightarrow 30 \rightarrow 40 		
γ_1	50 \leftarrow 60 \leftarrow 70 \leftarrow 80 		
γ_2	27 \rightarrow 29 \rightarrow 47 \rightarrow 48 		
γ_3	32 \leftarrow 33 \leftarrow 39 \leftarrow 50 		

GFG "Snake Traversal"

row by row \Rightarrow outer loop

col by col \Rightarrow inner loop

→ odd rows = right to left
(last col to first col)

→ even rows \Rightarrow left to right
(first col to last col)

```

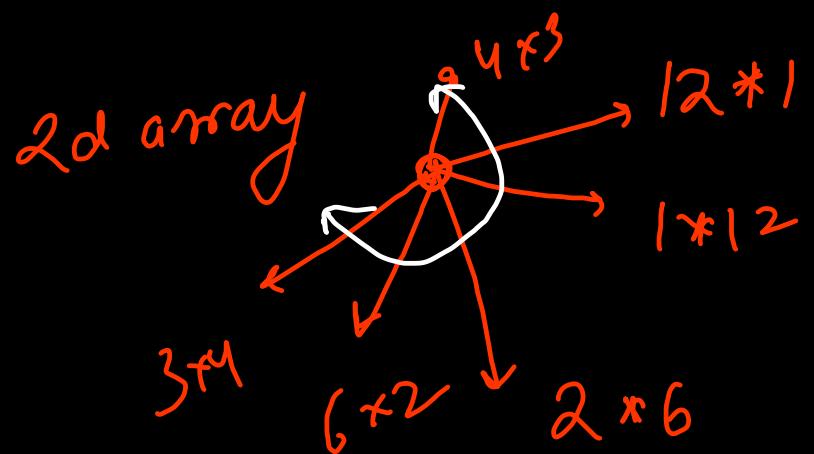
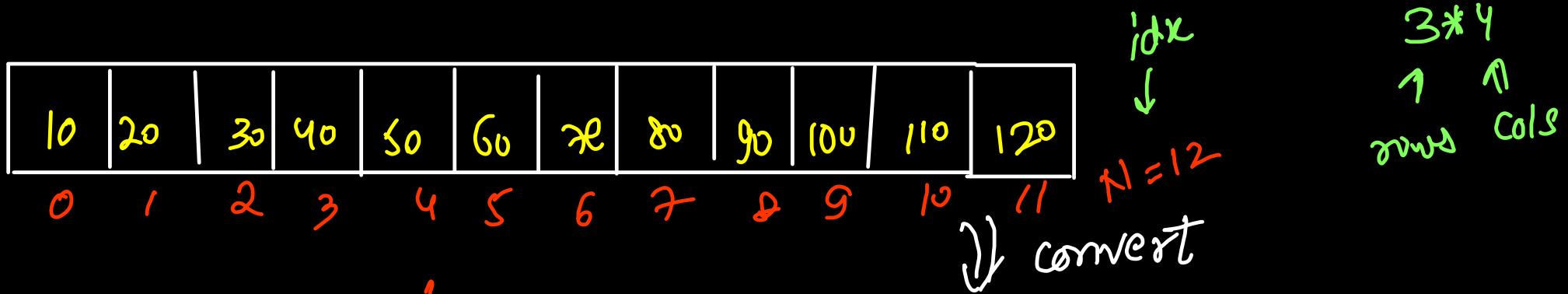
 $\rightarrow \text{outputspace: } O(n^2)$   $\rightarrow \text{inputspace: } O(n^2)$ 
static ArrayList<Integer> snakePattern(int[][] mat)
{
    ArrayList<Integer> res = new ArrayList<>();
    // top to down row by row
    for(int row = 0; row < mat.length; row++){
        if(row % 2 == 0){
            // even row -> left to right
            for(int col = 0; col < mat[0].length; col++){
                res.add(mat[row][col]);
            }
        } else {
            // odd row -> right to left
            for(int col = mat[0].length - 1; col >= 0; col--){
                res.add(mat[row][col]);
            }
        }
    }
    return res;
}

```

~~Time~~ # rows = cols = n
 $O(\text{rows} * \text{cols})$
 quadratic

~~Space~~ $O(1)$ constant
 ('inplace')
 extra space

Convert 1D to 2D array



3x4

	c0	c1	c2	c3
r0	10	20	30	40
r1	50	60	70	80
r2	90	100	110	120

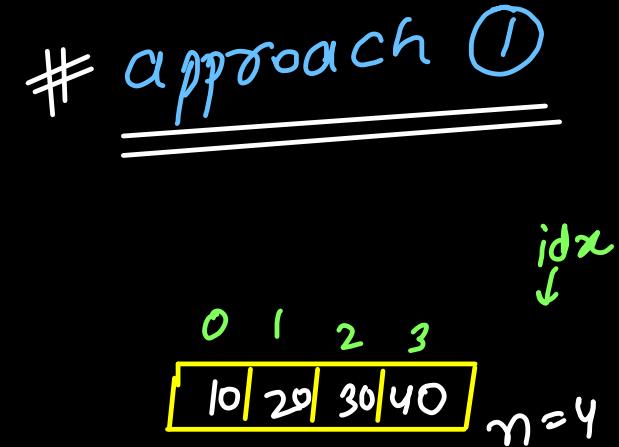
```

 $\rightarrow \text{output}$   $\rightarrow \text{input}$ 
public int[][] construct2DArray(int[] original, int m, int n) {
    // conversion not possible
    if(m * n != original.length){
        return new int[0][0]; //empty array
    }
    int[][] mat = new int[m][n];
    int idx = 0;
    for(int row = 0; row < m; row++){
        for(int col = 0; col < n; col++){
            mat[row][col] = original[idx++];
        }
    }
    return mat;
}

```

$\hookrightarrow N \text{ elements}$

$m \times n = 1 \times 1 \neq 4$
 $m \times n = 2 \times 3 \neq 4$



① Store
② $idx++$

	c_0	c_1
r_0	10	20
r_1	30	40

$m \times n$
 2×2

Time = $\frac{O(N)}{\text{array length}} = O(\underline{m \times n})$
 $\underline{\text{matrix cells}}$

Space = $O(1)$ constant/inplace

2nd approach

10	20	30	40	50	60	70	80	90	100	110	120
0	1	2	3	4	5	6	7	8	9	10	11

rows, cols
3 * 4

	c0	c1	c2	c3
70	10	20	30	40
81	50	60	70	80
82	90	100	110	120

$$0 \rightarrow (0, 0)$$

$$1 \rightarrow (0, 1)$$

$$2 \rightarrow (0, 2)$$

$$3 \rightarrow (0, 3)$$

$$4 \rightarrow (1, 0)$$

$$5 \rightarrow (1, 1)$$

$$6 \rightarrow (1, 2)$$

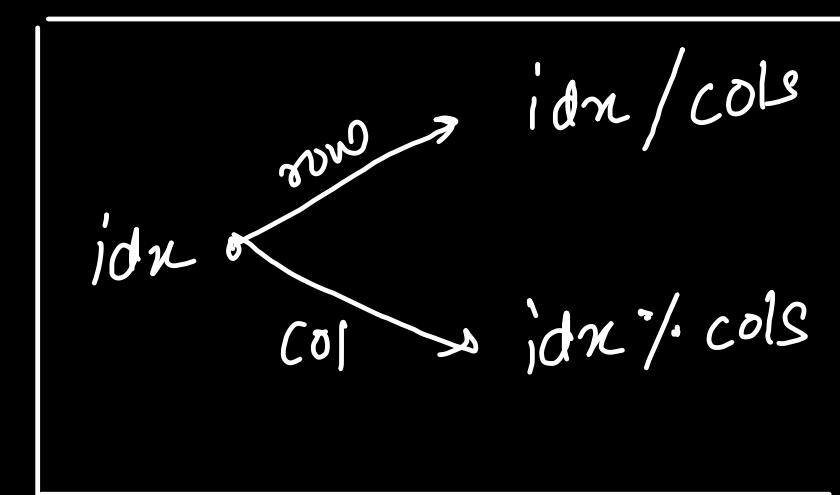
$$7 \rightarrow (1, 3)$$

$$8 \rightarrow (2, 0)$$

$$9 \rightarrow (2, 1)$$

$$10 \rightarrow (2, 2)$$

$$11 \rightarrow (2, 3)$$



```

public int[][] construct2DArray(int[] original, int m, int n) {
    // conversion not possible
    if(m * n != original.length){
        return new int[0][0];
    }

    int[][] mat = new int[m][n];

    for(int idx = 0; idx < original.length; idx++){
        int row = idx / n;
        int col = idx % n; * formula to convert 1D to 2D
        mat[row][col] = original[idx];
    }

    return mat;
}

```

HC 2022

$$\text{Row} = \text{idx} / \text{cols}$$

$$\text{Col} = \text{idx} \% \text{cols}$$

Time $\Rightarrow O(m \times n) = O(N)$ linear

Space $\Rightarrow O(1)$ inplace

$\cancel{*}$

$m = \text{no of rows}$
 $n = \text{no of columns}$
 $N = \text{1D array length} = M \times n$

Conversion from 2D matrix to 1D array

	c_0	c_1	c_2	c_3
r_0	10	20	30	40
r_1	50	60	70	80
r_2	90	100	110	120

3×4

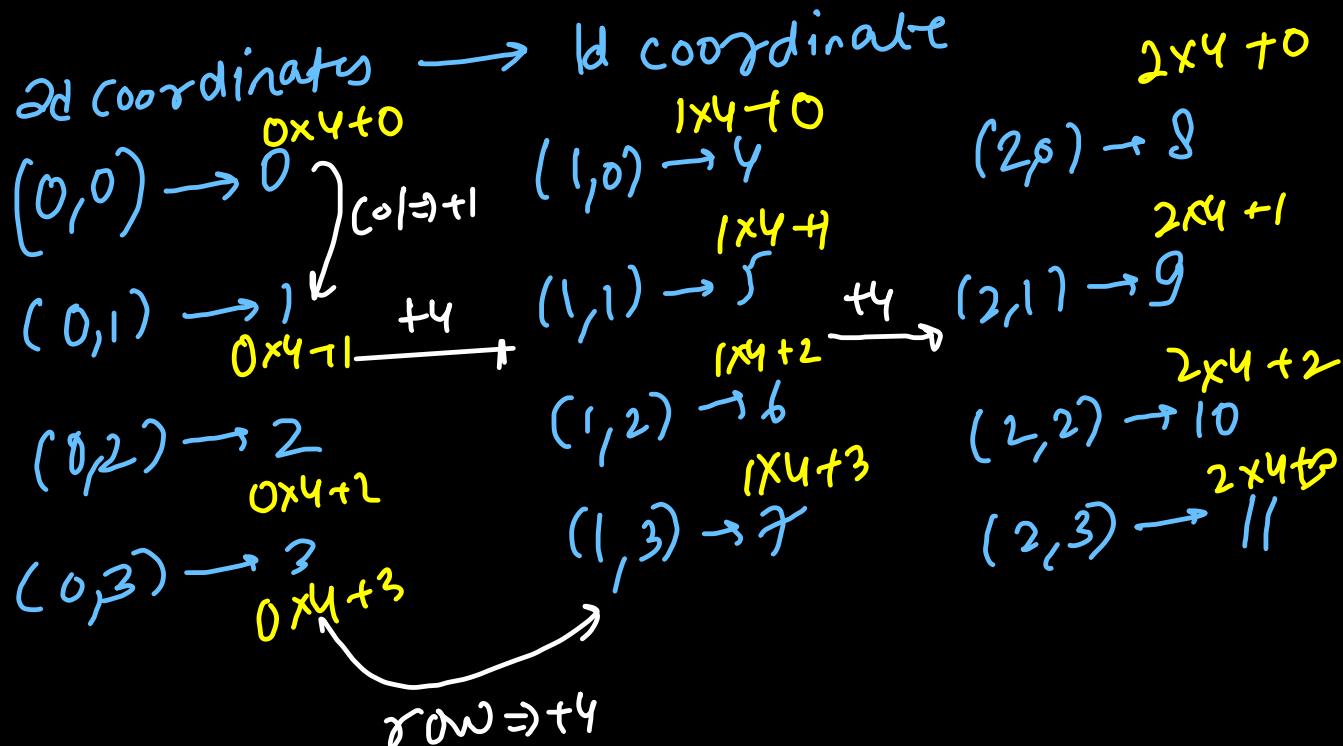
$m \times n$



$$\text{idn} = (r * \text{cols} + c)$$



10	20	30	40	50	60	70	80	90	100	110	120
0	1	2	3	4	5	6	7	8	9	10	11



Identical matrices

10	20
30	40

2×2

\neq

10	20	30	40
----	----	----	----

1×4

①

$\text{rows}_1 \neq \text{rows}_2$
 $\text{cols}_1 \neq \text{cols}_2$

} non-identical

10	20
30	40
50	60

3×2

\neq

10	20
30	40
50	600

3×2

②

any one value is
different
 \Rightarrow non-identical

```

int areMatricesIdentical(int N, int[][] g1, int[][] g2) {
    if(g1.length != g2.length) {
        return 0; // rows are not same
    }
    if(g1[0].length != g2[0].length){
        return 0; // cols are not same
    }

    // values comparison
    for(int row = 0; row < g1.length; row++){
        for(int col = 0; col < g1[0].length; col++){
            if(g1[row][col] != g2[row][col]) {
                return 0;
            }
        }
    }

    return 1;
}

```

m x n

Time

↳ $O(m \times n)$
 $= O(n^2)$
 quadratic

Space

↳ $O(1)$ constant
 in place

	c_0	c_1	c_2	c_3
r_0	10	20	30	40
r_1	50	60	70	80
r_2	90	100	110	120

3×4

Add 2 matrices

	c_0	c_1	c_2	c_3
r_0	100	200	300	400
r_1	500	600	700	800
r_2	900	1000	1100	1200

3×4

$$m_{0(i,j)} = m_1(i,j) + m_2(i,j)$$

$$m_1[i][j] += m_2[i][j]$$

	c_0	c_1	c_2	c_3
r_0	110	220	330	440
r_1	550	660	770	880
r_2	990	1100	1210	1320

3×4

```
public void Addition(int[][] m1, int[][] m2){  
    for(int row = 0; row < m1.length; row++){  
        for(int col = 0; col < m1[0].length; col++){  
            m1[row][col] = m1[row][col] + m2[row][col];  
        }  
    }  
}
```

Time = $O(n^2)$

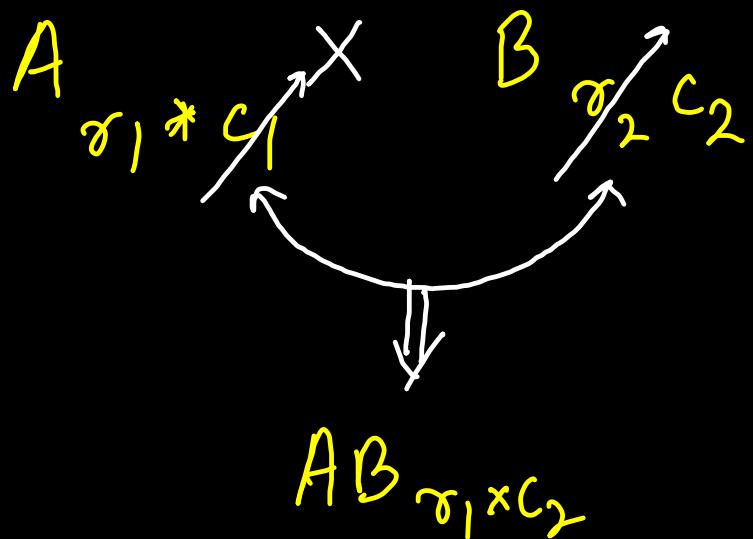
Space = $O(1)$
inplace

Subtraction \Rightarrow replace + with -
multiplication \Rightarrow this logic will fail

Matrix Multiplication

$$A \times B \neq B \times A$$

commutative \times



$$\text{constraints} \Rightarrow c_1 = \sigma_2$$

matrix
multiplicatⁿ

possible

only if constraint
is true

$A_{2 \times 3}$

10	20	30
40	50	60

$\gamma_1 \times c_1$

$c_0 \quad c_1 \quad c_2$

k

$\gamma_1 \times c_1 \times k = 2 \times 3$

$k = \gamma_0$

$\gamma_2 = \gamma_1$

$k = \gamma^2$

100	110	120	130
200	210	220	230
300	310	320	330

$\gamma_1 \times c_2$

$c_0 \quad c_1 \quad c_2 \quad c_3$

3×4

$C_{2 \times 4}$

γ_0

γ_1

10×100 20×200 30×300	10×110 20×210 30×310	10×120 20×220 30×320	10×130 20×230 30×330
A_{γ_1} $*B_{C_0}$	A_{γ_1} $*B_{C_1}$	A_{γ_1} $*B_{C_2}$	A_{γ_1} $*B_{C_3}$

2×4

$\gamma_1 \times c_2$

3 nested loops

$$C[\gamma_1][c_2] = A[\gamma_1][0] * B[0][c_2]$$

$$+ A[\gamma_1][1] * B[1][c_2]$$

$$+ A[\gamma_1][2] * B[2][c_2]$$

```

public static void multiply(int A[][], int B[][], int C[][], int N)
{
    int r1 = A.length, c1 = A[0].length; input ↑ Output
    int r2 = B.length, c2 = B[0].length;

    if(c1 != r2) return; // matrix multiplication not possible

    // resultant dimensions: (r1, c2)

    for(int row = 0; row < r1; row++){
        for(int col = 0; col < c2; col++){
            for(int k = 0; k < c1; k++){
                C[row][col] += A[row][k] * B[k][col];
            }
        }
    }
}

```

$$\gamma_1 = c_1 = \gamma_2 = c_2 = N$$

Time $\Rightarrow O(N^3)$
cubic

Space $\Rightarrow O(1)$
in place

LC 867) Rectangular matrix Transpose

```
public int[][] transpose(int[][] mat) {  
    int m = mat.length, n = mat[0].length;  
    int[][] res = new int[n][m];  
    Output  
    for(int row = 0; row < res.length; row++){  
        for(int col = 0; col < res[0].length; col++){  
            res[row][col] = mat[col][row];  
        }  
    }  
    return res;  
}
```

	c ⁰	c ¹	c ²
r ⁰	10	20	30
r ¹	40	50	60
2*3			

Time = $O(n^2)$ quadratic
Space = $O(1)$ no extra space

	c ⁰	c ¹
r ⁰	10	40
r ¹	20	50
r ²	30	60
3*2		

(GFG)

Transpose Matrix → rows interchange with cols
↳ Square matrix, new matrix not allowed.

$r0$	$c0$	$c1$	$c2$	$c3$
$r0$	00	01	02	03
$r1$	10	11	12	13
$r2$	20	21	22	23
$r3$	30	31	32	33

$r_{0w} \rightarrow c_{0l}$

$c_{0l} \rightarrow r_{0w}$

$\text{mat}[r][c] \leftrightarrow \text{mat}[c][r]$

swap

γ^0	c^0	c^1	c^2	c^3
γ^0	00 ✓	10 ✓	20 ✓	30 ✓
γ^1	01 ✗	11 ✓	21 ✓	31 ✓
γ^2	02 ✗	12 ✗	22 ✓	32 ✓
γ^3	03 ✗	13 ✗	23 ✗	33 ✓

$m(r, c) \leftrightarrow m(c, r)$

```

for(int r=0; r < N; r++) {
    for(int c=r; c < N; c++) {
        swap(mat, r, c);
    }
}

```

Output \Rightarrow Input dimensions

```
//Function to find transpose of a matrix.  
static void transpose(int mat[][], int n)  
{  
    // run loop only in upper right triangle  
    for(int row = 0; row < n; row++){  
        for(int col = row; col < n; col++){  
            // Swapping values at (row, col) with (col, row)  
            int temp = mat[row][col];  
            mat[row][col] = mat[col][row];  
            mat[col][row] = temp;  
        }  
    }  
}
```

Lc 867 Code

If I had created a new resultant matrix, then due to void return type, it will be considered $O(n^2)$ extra space

Time $\Rightarrow O(n^2)$ quadratic

Space $\Rightarrow O(1)$ ^{inplace}
(w/o new matrix)

Rotate Image
square matrix

90° clockwise



	c ₀	c ₁	c ₂	c ₃
r ₀	00	01	02	03
r ₁	10	11	12	13
r ₂	20	21	22	23
r ₃	30	31	32	33

in place
hint?
2 traversals

	c ₀	c ₁	c ₂	c ₃
r ₀	00	01	02	03
r ₁	11	12	13	10
r ₂	22	23	20	21
r ₃	32	33	30	31

	c ⁰	c ¹	c ²	c ³
r ⁰	00	01	02	03
r ¹	10	11	12	13
r ²	20	21	22	23
r ³	30	31	32	33

transpose

rows → columns

columns → rows

(i, j)
swap

r⁰ r¹ r² r³

00	10	20	30
01	11	21	31
02	12	22	32
03	13	23	33

rotate 90° clockwise

↓ flip
c⁰ c¹ c² c³ ↓
r⁰ r¹ r² r³

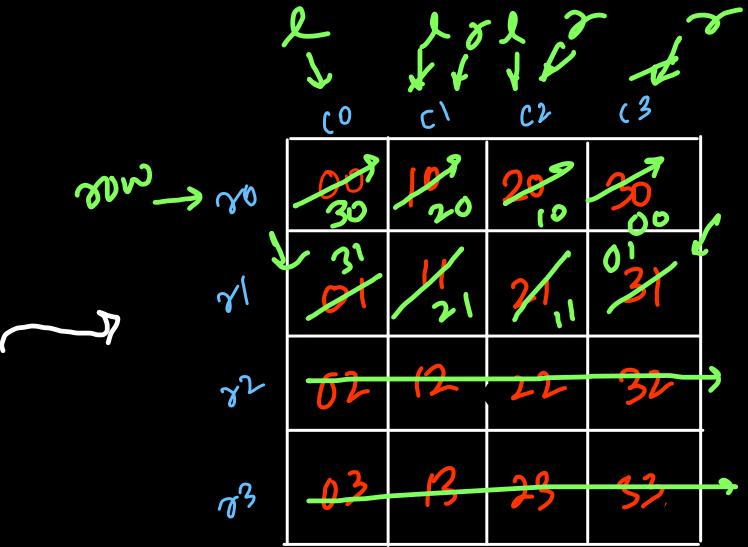
	c ⁰	c ¹	c ²	c ³
r ⁰	20	30	10	00
r ¹	31	21	11	01
r ²	22	12	12	02
r ³	13	23	13	03

reverse each row

two pointers

iterate on each row
& apply 2 pointer

c_0	c_1	c_2	c_3	
r_0	00	01	02	03
r_1	10	11	12	13
r_2	20	21	22	23
r_3	30	31	32	33



c_0	c_1	c_2	c_3	
r_0	00	00	00	00
r_1	10	10	10	10
r_2	20	20	20	20
r_3	30	30	30	30

```
// swap (r1, c1) with (r2, c2) values
public static void swap(int[][] mat, int r1, int c1, int r2, int c2){
    int temp = mat[r1][c1];
    mat[r1][c1] = mat[r2][c2];
    mat[r2][c2] = temp;
}
```

```
// rows -> columns, columns -> rows
public void transpose(int[][] mat, int n) {
    // run loop only in upper right triangle
    for(int row = 0; row < n; row++){
        for(int col = row; col < n; col++){
            // Swapping values at (row, col) with (col, row)
            swap(mat, row, col, col, row);
        }
    }
}
```

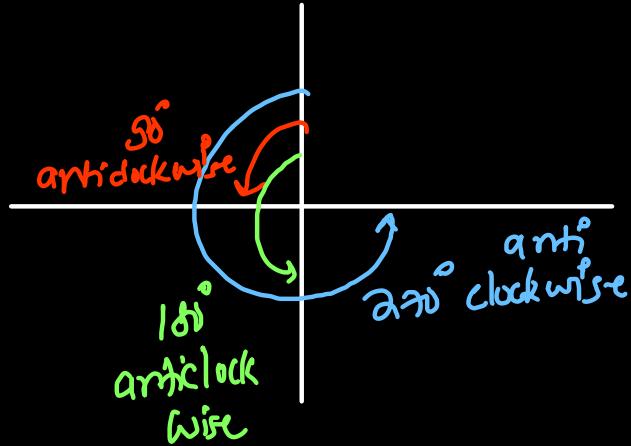
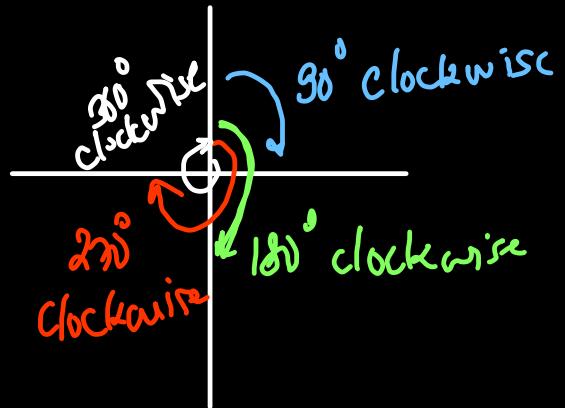
$O(n^2)$ time

```
// reverse each row by using two pointer technique
public void reverseRows(int[][] mat, int n){
    for(int row = 0; row < n; row++){
        int left = 0, right = n - 1;
        while(left < right){
            // swapping values at (row, left) with (row, right)
            swap(mat, row, left, row, right);
            left++; right--;
        }
    }
}

public void rotate(int[][] mat) {
    int n = mat.length;
    transpose(mat, n);
    reverseRows(mat, n);
}
```

$O(n^2)$ time

Time $\Rightarrow O(n^2)$
Space $\Rightarrow O(1)$
inplace



$$90^\circ \text{ anticlockwise} = 270^\circ \text{ clockwise}$$

$$270^\circ \text{ anticlockwise} = 90^\circ \text{ clockwise}$$

$$180^\circ \text{ anticlockwise} = 180^\circ \text{ clockwise}$$

hw

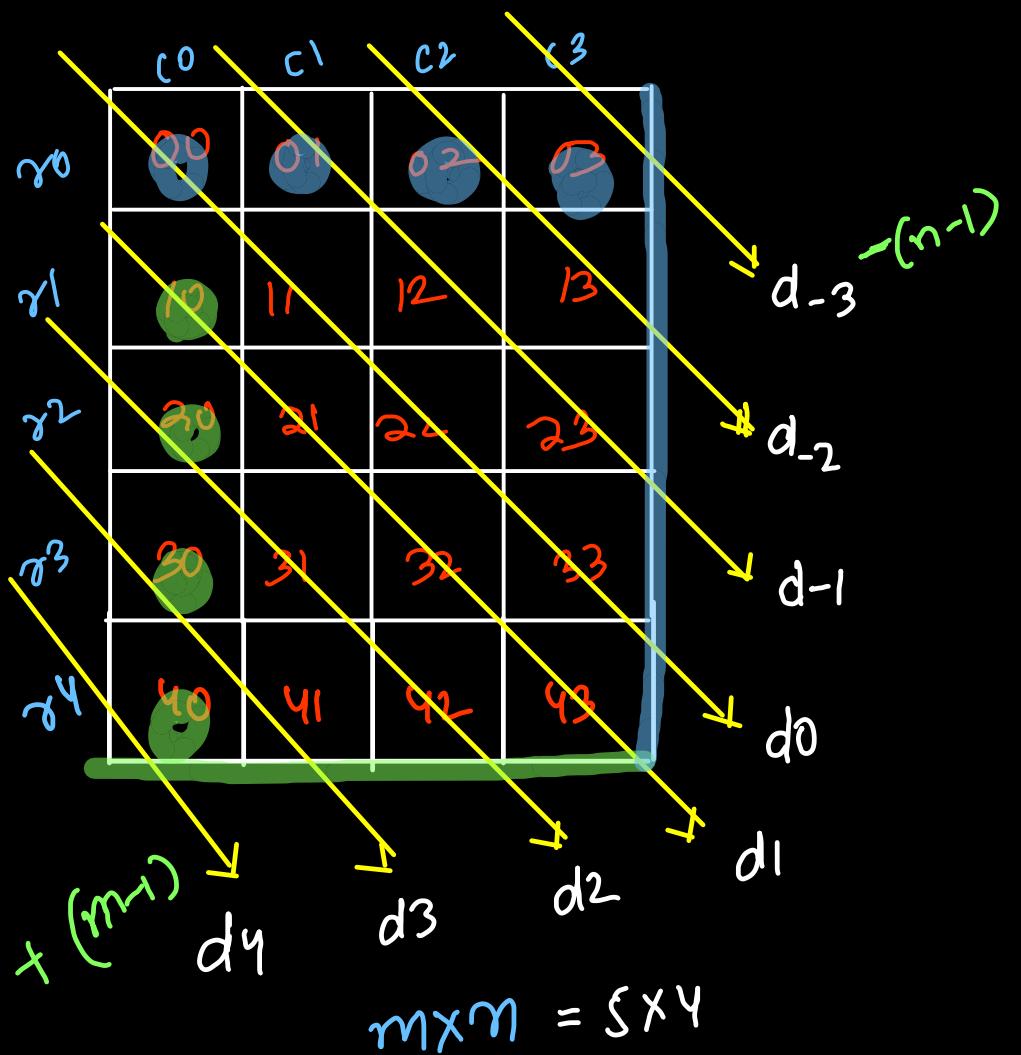
c ₀	c ₁	c ₂	c ₃
r ₀	00 03	01 02	02 00
r ₁	10 13	11 12	12 11
r ₂	20 23	21 22	22 21
r ₃	30 33	31 32	32 33

- ① reverse rows
- ② reverse cols

↓
180°

c ₀	c ₁	c ₂	c ₃	
r ₀	33	32	31	30
r ₁	23	22	21	20
r ₂	13	12	11	10
r ₃	03	02	01	00

Diagonal Traversal



① top left to bottom right
 \star (row - col) same for all indices of a given diagonal

- * Outer loop \rightarrow diagonal
- * inner loop \rightarrow row, col

Traversal

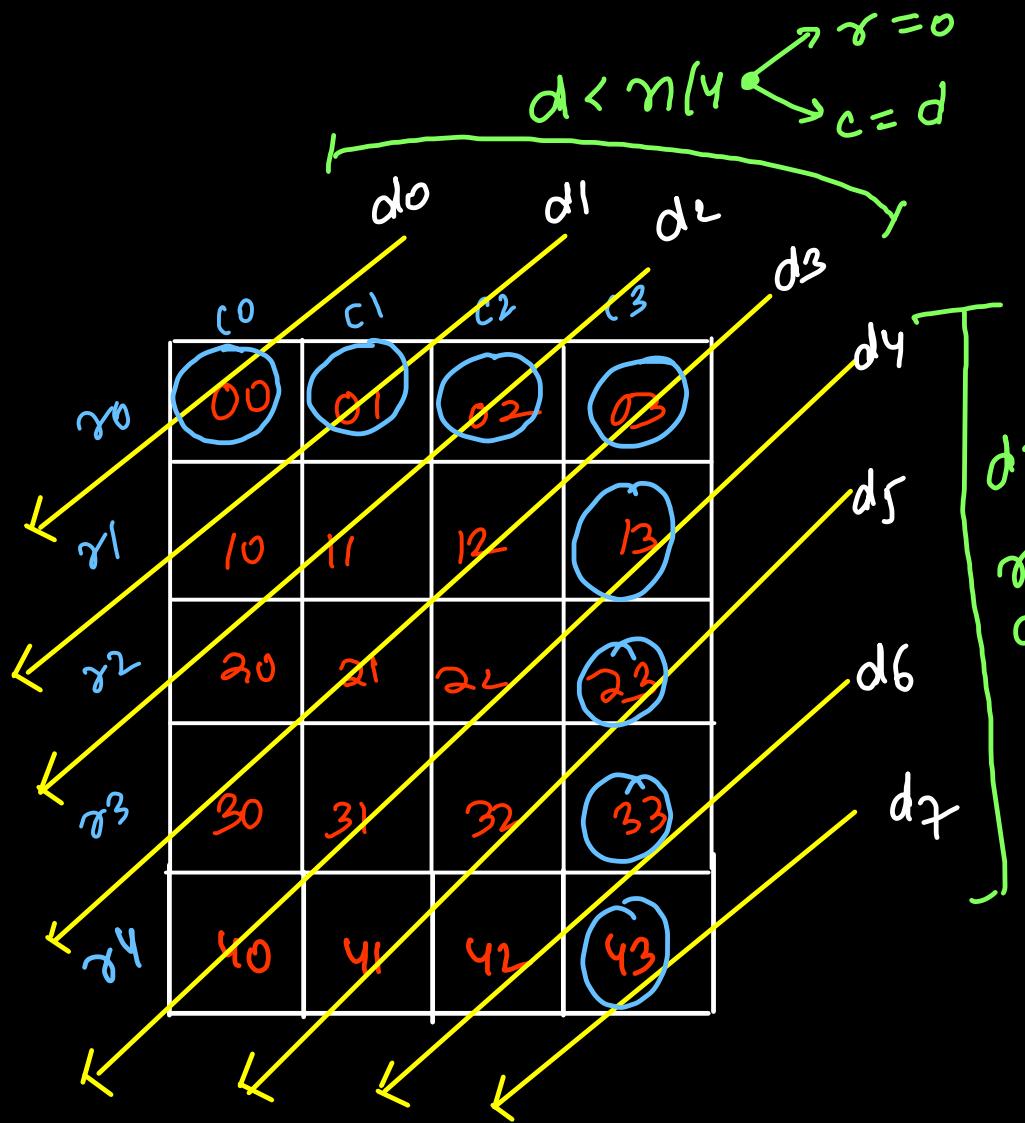
```
int m = mat.length, n = mat[0].length;
for(int d = 1 - n; d <= m - 1; d++){
    int row = (d <= 0) ? 0 : d;
    int col = (d <= 0) ? -d : 0;

    while(row < m && col < n){
        System.out.print(mat[row][col] + " ");
        row++; col++;
    }
}

return false;
```

Time $\Rightarrow O(n^2)$

Space $\Rightarrow O(1)$



$m \times n$

$S \times 4$

② top right to bottom left

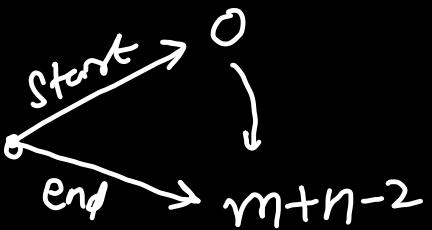
$\cancel{(row + col)}$ values for a given
diagonal is same

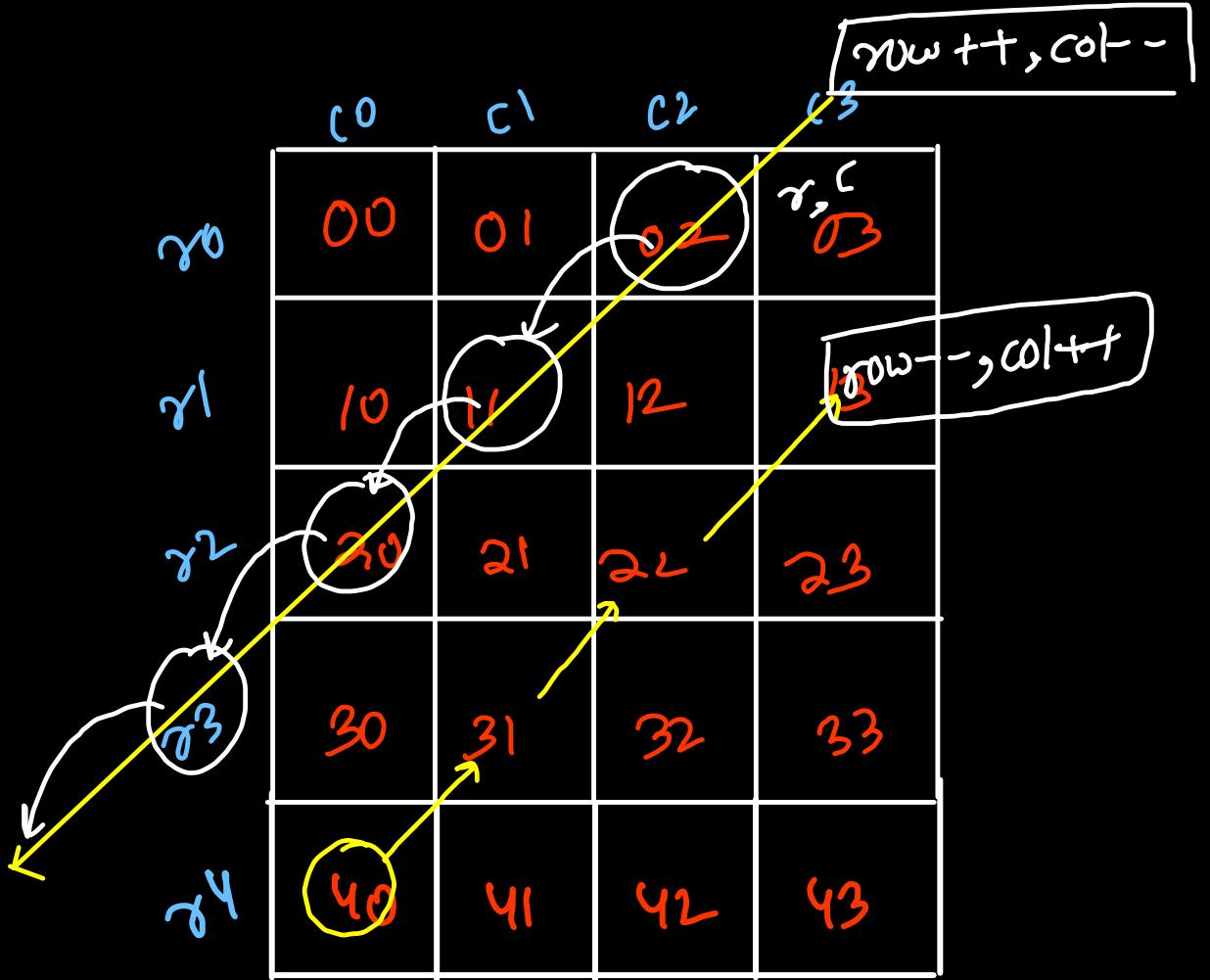
$$row = d - n + 1$$

$$col = n - 1$$

outer loop \rightarrow diagonal

inner loop \rightarrow row, col





top right to bottom left

out of matrix

$\text{col} == -1$, left wall

$\text{row} == m$, bottom wall

$\text{row} > 0$, $\text{col} < n$

bottom left to top right

$\text{row} == -1$, top wall

$\text{col} == n$, right wall

$\text{row} > 0$, $\text{col} < n$

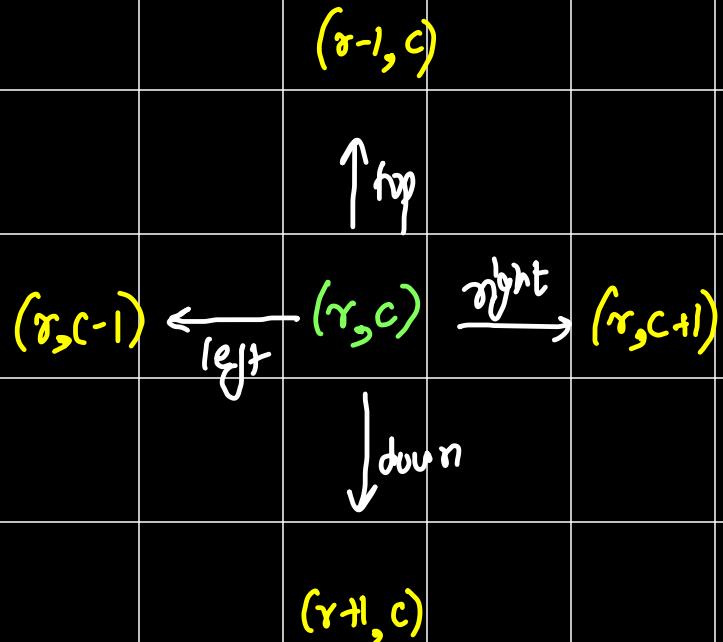
Top Right to Bottom Left

```
int m = mat.length, n = mat[0].length;  
  
for(int d = 0; d <= m + n - 2; d++){  
    int row = (d < n) ? 0 : d - n + 1;  
    int col = (d < n) ? d : n - 1;  
  
    while(row < m && col >= 0){  
        System.out.print(mat[row][col] + " ");  
        row++; col--;  
    }  
}
```

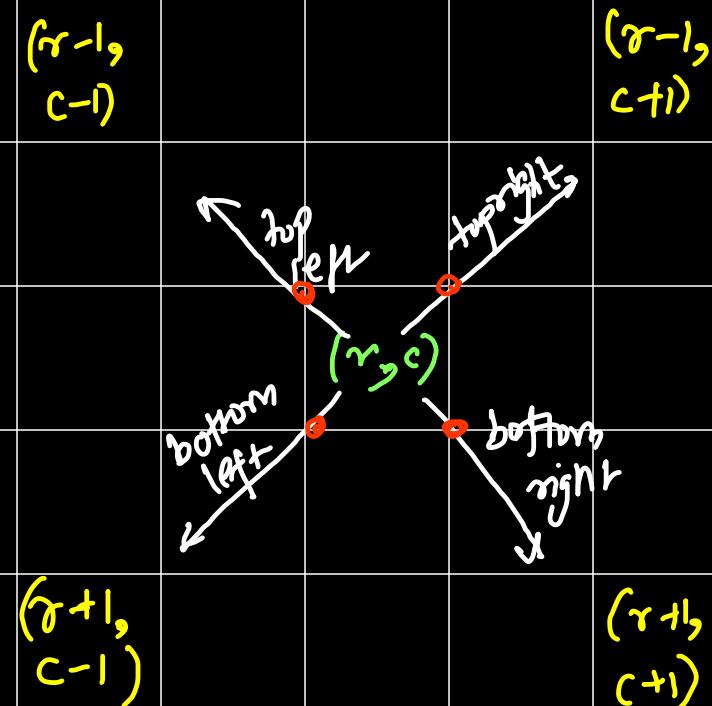
Time $\Rightarrow O(m * n)$
rows ↑
cols ↑
quadratic

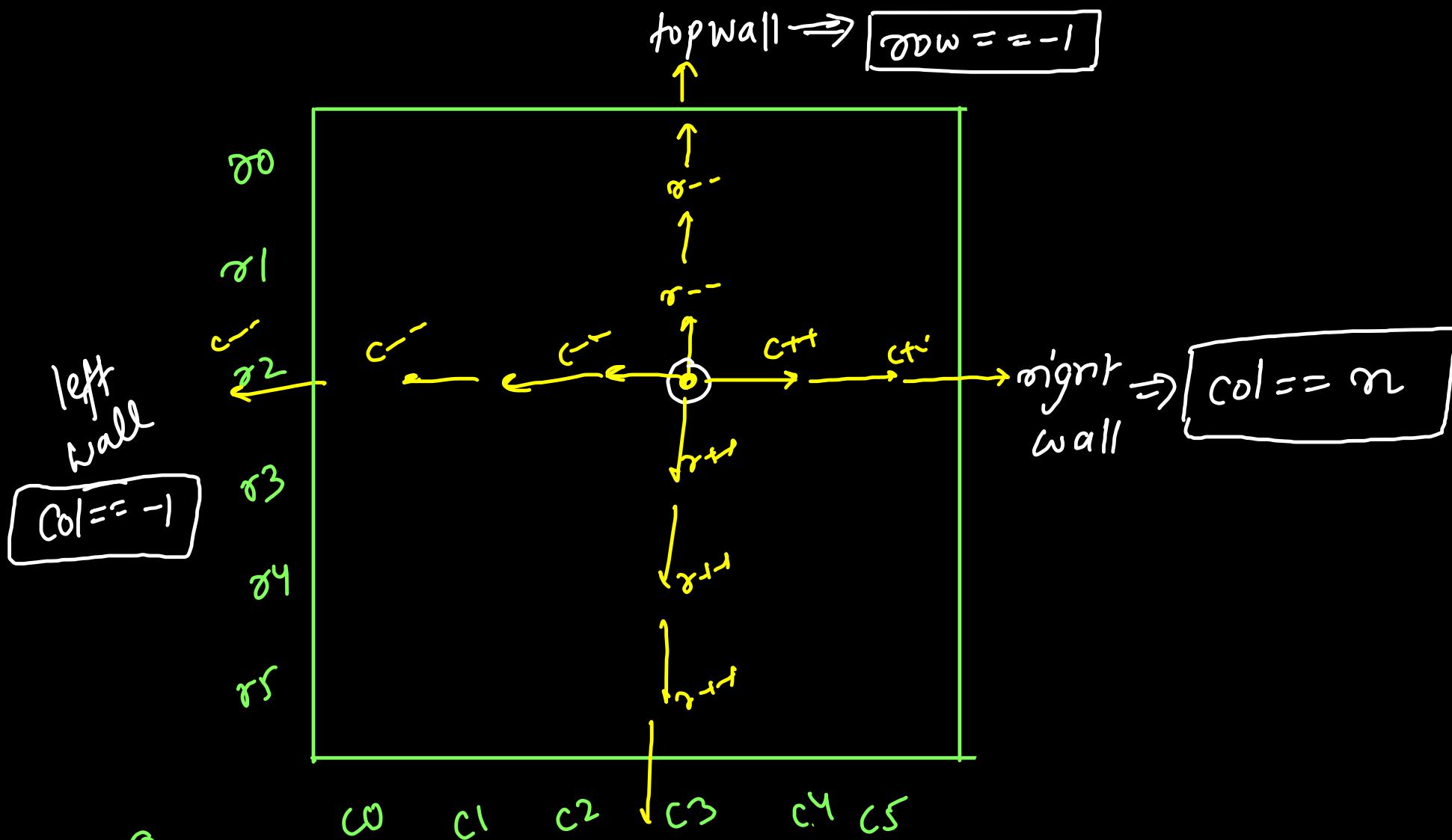
Space $\Rightarrow O(1)$
inplace

boundary neighbours



corner adjacent

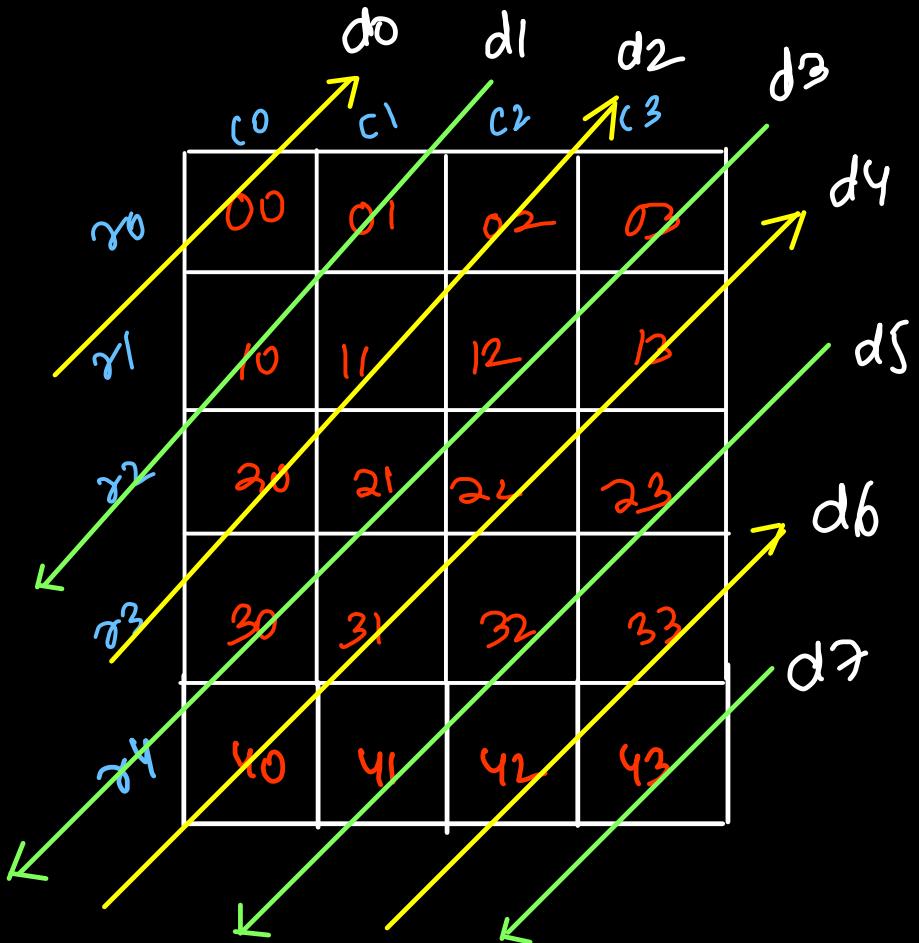




m_{out}

$$\Rightarrow \partial v_w == m$$

LC 498) ZigZag Traversal



d

odd : top right to bottom left

even: bottom left to top right

```

public int[] findDiagonalOrder(int[][][] mat) {
    int m = mat.length, n = mat[0].length;
    int[] res = new int[m * n];
    int idx = 0;

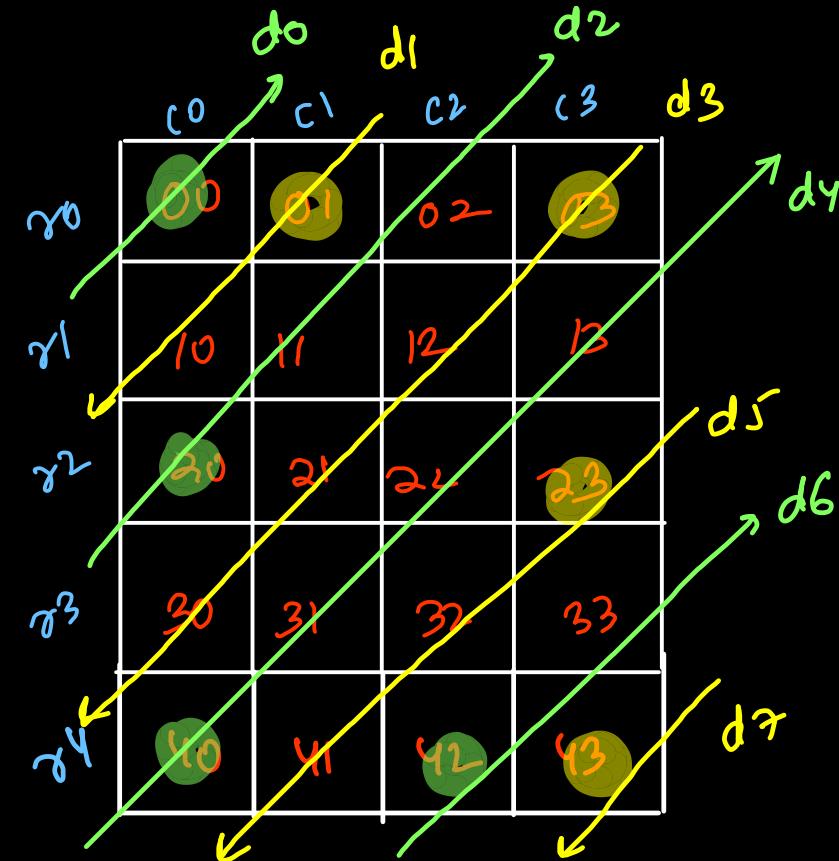
    for(int d = 0; d <= m + n - 2; d++){
        if(d % 2 == 1){
            // top right to bottom left
            int row = (d < n) ? 0 : d - n + 1;
            int col = (d < n) ? d : n - 1;

            while(row < m && col >= 0){
                res[idx++] = mat[row][col];
                row++; col--;
            }
        } else {
            // bottom left to top right
            int row = (d < m) ? d : m - 1;
            int col = (d < m) ? 0 : d - m + 1;

            while(row >= 0 && col < n){
                res[idx++] = mat[row][col];
                row--; col++;
            }
        }
    }

    return res;
}

```

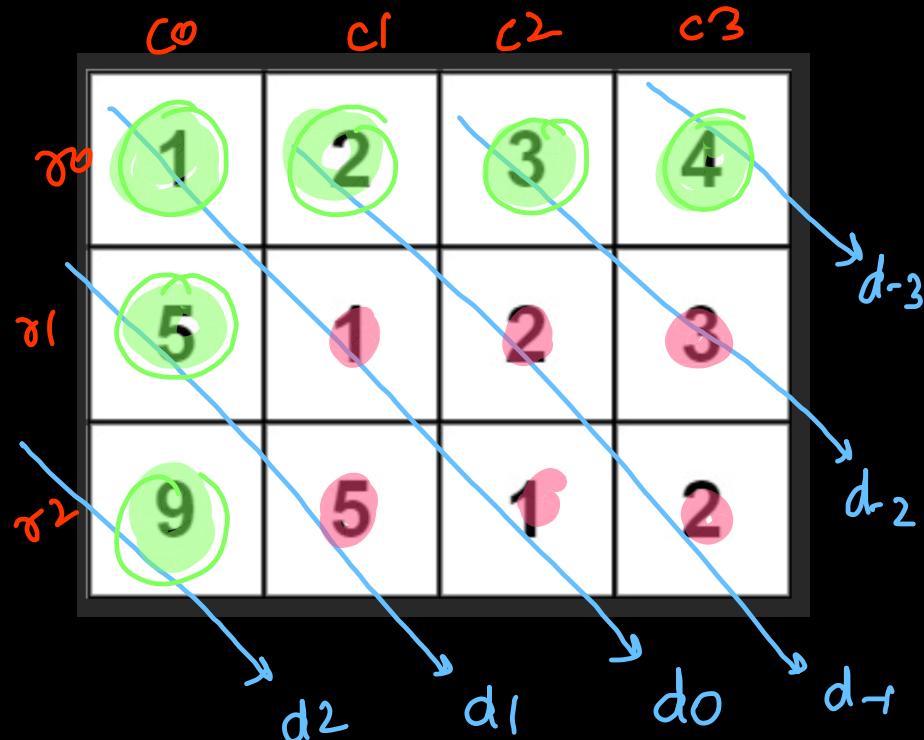


Time $\Rightarrow O(m \times n)$
quadratic

Space $\Rightarrow O(1)$
inplace

LC 766) Toeplitz Matrix

```
public boolean isToeplitzMatrix(int[][] mat) {  
    int m = mat.length, n = mat[0].length;  
    for(int d = 1 - n; d <= m - 1; d++){  
        int row = (d <= 0) ? 0 : d;  
        int col = (d <= 0) ? -d : 0;  
        int val = mat[row][col];  
  
        while(row < m && col < n){  
            if(mat[row][col] != val) return false;  
            row++; col++;  
        }  
    }  
  
    return true;  
}
```



1380. Lucky Numbers in a Matrix

Hint



Easy



1.5K

75



Companies

Given an $m \times n$ matrix of **distinct** numbers, return all **lucky numbers** in the matrix in **any order**.

A **lucky number** is an element of the matrix such that it is the minimum element in its row and maximum in its column.

3	7	8
9	11	13
15	16	17

1 saddle point

1	5	8
2	1	7
4	3	1

no saddle point

There can be no more than 1 saddle point given that all rows are unique!

- brute force → check every cell is lucky $\Rightarrow O(mn)$
- for all cells $\Rightarrow m \times n \times (m+n)$
 $\Rightarrow N^3$ cubic

	c_0	c_1	c_2
r_0	3 ✓ cx	7	8
r_1	12	11 ✓ cx	13
r_2	15 ✓ cv	16	17

$$r_0 \left\{ \begin{array}{l} \min Col = 0 \\ \max Row = \emptyset \checkmark 2 \end{array} \right.$$

$$r_1 \left\{ \begin{array}{l} \min Col = \emptyset 1 \\ \max Row = \emptyset \checkmark 2 \end{array} \right.$$

$$r_2 \left\{ \begin{array}{l} \min Col = 0 \\ \max Row = \emptyset / 12 \end{array} \right.$$

```

public List<Integer> luckyNumbers (int[][] mat) {
    for(int row = 0; row < mat.length; row++){
        int min = 0; // column index
        for(int col = 0; col < mat[0].length; col++){
            if(mat[row][col] < mat[row][min]){
                min = col;
            }
        }
        min value's col in the current row
    }

    int max = 0;
    for(int r = 0; r < mat.length; r++){
        if(mat[r][min] > max){
            max = mat[r][min];
        }
    }
    max value in min col

    if(min == max) {
        List<Integer> res = new ArrayList<>();
        res.add(max);
        return res;
    }
    no saddle pt (lucky no)
}

return new ArrayList<>();
}

```

Time \rightarrow quadratic $O(n^2)$

Space \rightarrow $O(1)$

	c0	c1	c2
r0	8	7	3
r1	12	11	13
r2	15	16	17

$$\min(\text{Col}) = \cancel{0} \cancel{1} \cancel{2}$$

$$\max = \cancel{\emptyset} \cancel{0} \cancel{1} \cancel{2}$$

$$\min(\text{Col}) = \cancel{0} \cancel{1} \cancel{2}$$

$$\min(\text{Col}) = \cancel{0} \cancel{1}$$

$$\max = \cancel{0} \cancel{1} \cancel{2} \cancel{3} \cancel{4} \cancel{5} \cancel{6}$$

{ Google Interview } # Set Matrix Zeroes LC 73

boolean
true(1)
false(0)

int
0
nonzero (-2³¹ to 2³¹-1)

	c0	c1	c2	c3
r0	1	1	1	1
r1	1	1	0	1
r2	0	1	1	1
r3	1	1	1	1
r4	1	1	1	0



	c0	c1	c2	c3
r0	0	1	0	0
r1	0	0	0	0
r2	0	0	0	0
r3	0	1	0	0
r4	0	0	0	0

Approach 1) extra matrix
brute force

	c ⁰	c ¹	c ²	c ³
r ⁰	0	1	0	0
r ¹	0	0	0	0
r ²	0	1	0	0
r ³	0	1	0	0
r ⁴	0	0	0	0

updates
(original)

	c ⁰	c ¹	c ²	c ³
r ⁰	1	1	1	1
r ¹	1	1	0	1
r ²	0	1	1	1
r ³	1	1	1	1
r ⁴	1	1	1	0

queried
(copy)

```

public int[][] deepCopy(int[][] mat){
    int m = mat.length, n = mat[0].length;
    int[][] copy = new int[m][n];
    for(int row = 0; row < m; row++){
        for(int col = 0; col < n; col++){
            copy[row][col] = mat[row][col];
        }
    }
    return copy;
}

public void setRowZero(int[][] mat, int row){
    for(int col = 0; col < mat[0].length; col++){
        mat[row][col] = 0;
    }
}

public void setColZero(int[][] mat, int col){
    for(int row = 0; row < mat.length; row++){
        mat[row][col] = 0;
    }
}

```

~~extraspace~~

```

public void setZeroes(int[][] mat) {
    int[][] copy = deepCopy(mat);

    for(int row = 0; row < copy.length; row++){
        for(int col = 0; col < copy[0].length; col++){
            if(copy[row][col] == 0){
                m+n { setRowZero(mat, row);
                        setColZero(mat, col);
                }
            }
        }
    }
}

```

Time $\Rightarrow O(m \times n \times (m+n))$
 $= \text{Cubic}$

Space $\Rightarrow O(m \times n)$ quadratic
~~inplace~~

2nd approach

(lazy)

- ① queries \Rightarrow zeros
(store)
- then
- ② updates (set zeros)

$m=5$

$\gamma_0 \gamma_1 \gamma_2 \gamma_3 \gamma_4$	c^0	c^1	c^2	c^3
f	0 →	1	1 → 0	1 →
t	0 →	1 → 0	0 (blue circle)	1 →
$f \rightarrow t$	0 (red circle)	1 → 0	1 → 0	1 → 0
f	0 →	1	1 → 0	1 → 0
$f \rightarrow t$	0 →	1	1 → 0	0 (blue circle)

Col $\begin{bmatrix} t \cancel{f} & f & f \rightarrow t & \cancel{f \rightarrow t} \end{bmatrix}$ $n=4$

queries $\Rightarrow O(m \times n)$

+
updates $\Rightarrow O(m \times n)$

Time = $O(m \times n)$ quadratic

Space = $O(m+n)$ linear
(extra space) ~~in place~~

* ~~2nd~~

```

public void setZeroes(int[][] mat) {
    boolean[] rows = new boolean[mat.length];
    boolean[] cols = new boolean[mat[0].length]; } extra space

    // Queries -> Store Zeroes
    for(int row = 0; row < mat.length; row++){
        for(int col = 0; col < mat[0].length; col++){
            if(mat[row][col] == 0){
                rows[row] = cols[col] = true;
            }
        }
    }

    // Updates -> Set Zeros
    for(int row = 0; row < mat.length; row++){
        for(int col = 0; col < mat[0].length; col++){
            if(rows[row] == true || cols[col] == true){
                mat[row][col] = 0;
            }
        }
    }
}

```

1st → 2nd → 3rd

$O(N^3)$ ⇒ $O(N^2)$ ⇒ $O(N^2)$
 time time time

$O(N^2)$ ⇒ $O(N)$ ⇒ $O(1)$
 Space Space Space
 (in place)

③rd approach (most optimised) Time $\Rightarrow O(n^2)$
 Space $\Rightarrow O(1)$
 inplace

	c ⁰	c ¹	c ²	c ³
r ⁰	0 ¹	1	X ⁰	X ⁰
r ¹	0 ¹	X ⁰	0 ¹	1 ⁰
r ²	0 ¹	X ⁰	X ⁰	1 ⁰
r ³	0 ¹	1	X ⁰	X ⁰
r ⁴	0 ¹	X ⁰	0 ¹	0 ¹

boolean firstRow = false;

boolean firstCol = false;
 true

① queen's \rightarrow store zeros

② update \rightarrow set zeros

time
↓
 $O(mn)$
quadratic

space
↓
 $O(1)$
constant
(inplace)

```
public void setZeroes(int[][] mat) {
    boolean r0Zero = false, c0Zero = false;

    // Queries -> Store Zeros
    for(int row = 0; row < mat.length; row++){
        for(int col = 0; col < mat[0].length; col++){
            if(mat[row][col] == 0){
                mat[0][col] = mat[row][0] = 0;
                if(row == 0) r0Zero = true;
                if(col == 0) c0Zero = true;
            }
        }
    }
}
```

	c ⁰	c ¹	c ²	c ³
r ⁰	0	1	20	30
r ¹	0	10	0	0
r ²	0	10	0	0
r ³	0	1	20	30
r ⁴	0	0	0	0

$r0 = \text{false}$.
 $c0 = \cancel{\text{false}};$ true

$O(mn)$

```
// Updates -> Set Zeros
for(int row = 1; row < mat.length; row++){
    for(int col = 1; col < mat[0].length; col++){
        if(mat[row][0] == 0 || mat[0][col] == 0){
            mat[row][col] = 0;
        }
    }
}
```

$O(mn)$

```
// first Row (r0)
if(r0Zero == true){
    for(int col = 0; col < mat[0].length; col++){
        mat[0][col] = 0;
    }
}
```

$O(mn)$

```
// first Col (c0)
if(c0Zero == true){
    for(int row = 0; row < mat.length; row++){
        mat[row][0] = 0;
    }
}
```

corner case

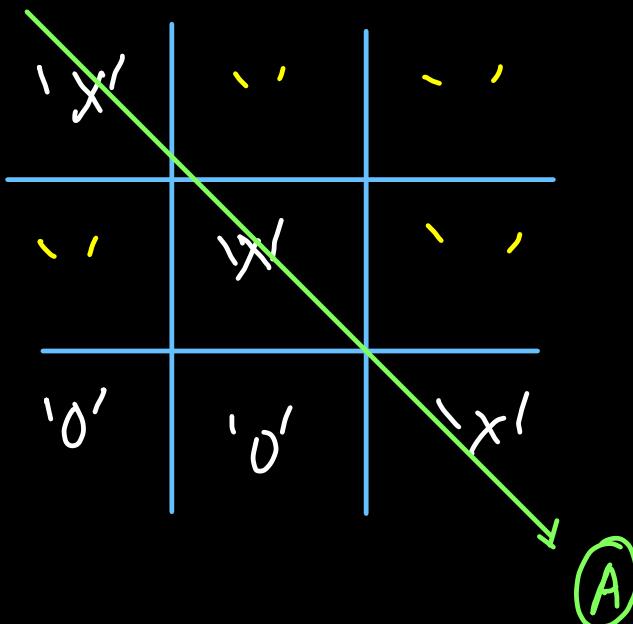
LC 1235)

Tic Tac Toe Game

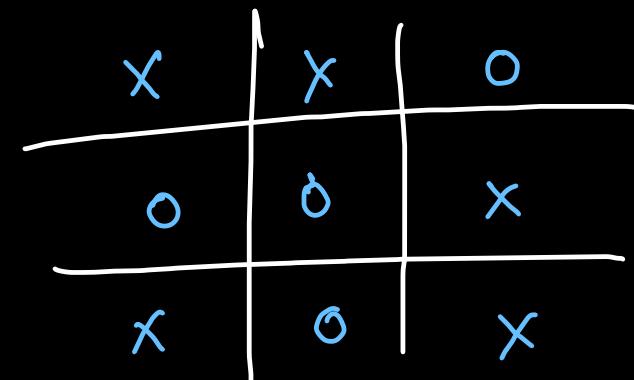
eg:

```
moves = [[0,0], [2,0], [1,1], [2,1], [2,2]]
```

move = 'x' 'o' 'x' 'o' 'x'



```
moves = [[0,0], [1,1], [2,0], [1,0], [1,2], [2,1], [0,1], [0,2], [2,2]]  
"Pending"      x' 'o' x o x 0 x } 0 o x } "Draw"
```



```
public boolean isWinner(char[][] board, int row, int col, char ch){  
    // entire row  
    if(board[row][0] == ch && board[row][1] == ch && board[row][2] == ch)  
        return true;  
  
    // entire column  
    if(board[0][col] == ch && board[1][col] == ch && board[2][col] == ch)  
        return true;  
  
    // left diagonals  
    if(board[0][0] == ch && board[1][1] == ch && board[2][2] == ch)  
        return true;  
  
    // right diagonals  
    if(board[0][2] == ch && board[1][1] == ch && board[2][0] == ch)  
        return true;  
  
    return false;  
}
```

↳ Constant $O(1)$

Work
case
9
 $\Rightarrow O(1)$

```
public String tictactoe(int[][] moves) {  
    char ch = 'X';  
    char[][] board = new char[3][3];  
  
    for(int[] move: moves){  
        int row = move[0];  
        int col = move[1];  
        board[row][col] = ch;  
  
        if(isWinner(board, row, col, ch) == true){  
            if(ch == 'X') return "A";  
            else return "B";  
        }  
  
        if(ch == 'X') ch = '0';  
        else ch = 'X';  
    }  
  
    if(moves.length == 9) return "Draw";  
    else return "Pending";  
}
```

LC 36) Valid Sudoku

Determine if a 9×9 Sudoku board is valid. Only the filled cells need to be validated **according to the following rules**:

- # Each row must contain the digits $1-9$ without repetition.
- # Each column must contain the digits $1-9$ without repetition.
- # Each of the nine 3×3 sub-boxes of the grid must contain the digits $1-9$ without repetition.

Note:

- A Sudoku board (partially filled) could be valid but is not necessarily solvable.
- Only the filled cells need to be validated according to the mentioned rules.

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

```

public boolean isRowValid(char[][] board, int row){
    int[] freq = new int[10];
    for(int col = 0; col < 9; col++){
        int val = board[row][col] - '0';
        freq[val]++;
        if(freq[val] > 1) return false;
    }
    return true;
}

public boolean isColValid(char[][] board, int col){
    int[] freq = new int[10];
    for(int row = 0; row < 9; row++){
        int val = board[row][col] - '0';
        freq[val]++;
        if(freq[val] > 1) return false;
    }
    return true;
}

```

```

public boolean isSubGridValid(char[][] board){
}

public boolean isValidSudoku(char[][] board) {
    for(int row = 0; row < 9; row++){
        if(isRowValid(board, row) == false) return false;
    }

    for(int col = 0; col < 9; col++){
        if(isColValid(board, col) == false) return false;
    }

}

```

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	3	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

(0,0) (1,0) (2,0)
(0,1) (1,1) (2,1)
(0,2) (1,2) (2,2)
(0,3) (1,3) (2,3)
(0,4) (1,4) (2,4)
(0,5) (1,5) (2,5)

5	3		7		6
6		1	9	5	
9	8				6
8		3,3	6	3,6	3
4		8	3		1
7		2			6
6	6	4,3	5	6,8	8
	7,4	1	9		5
	8	8		7	9

```

public boolean isRowValid(char[][] board, int row){
    int[] freq = new int[10];
    for(int col = 0; col < 9; col++){
        if(board[row][col] == '.') continue;
        int val = board[row][col] - '0';
        freq[val]++;
        if(freq[val] > 1) return false;
    }
    return true;
}

public boolean isColValid(char[][] board, int col){
    int[] freq = new int[10];
    for(int row = 0; row < 9; row++){
        if(board[row][col] == '.') continue;
        int val = board[row][col] - '0';
        freq[val]++;
        if(freq[val] > 1) return false;
    }
    return true;
}

```

$O(g)$

```

public boolean isSubGridValid(char[][] board, int row, int col){
    int[] freq = new int[10];
    for(int r = row; r < row + 3; r++){
        for(int c = col; c < col + 3; c++){
            if(board[r][c] == '.') continue;
            int val = board[r][c] - '0';
            freq[val]++;
            if(freq[val] > 1) return false;
        }
    }
    return true;
}

public boolean isValidSudoku(char[][] board) {
    for(int row = 0; row < 9; row++){
        if(isRowValid(board, row) == false) return false;
    }

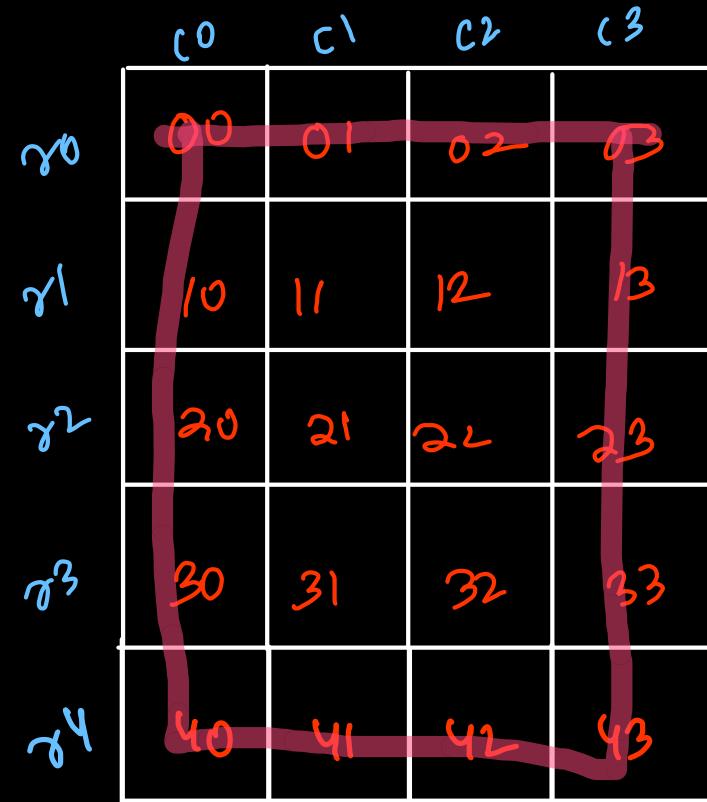
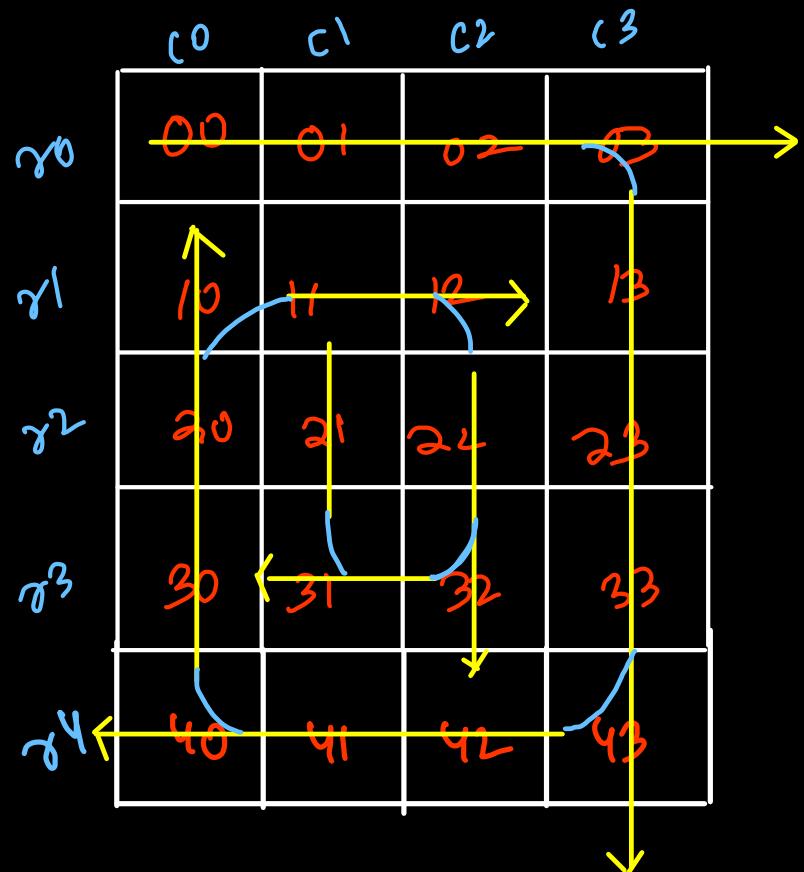
    for(int col = 0; col < 9; col++){
        if(isColValid(board, col) == false) return false;
    }

    for(int row = 0; row < 9; row += 3){
        for(int col = 0; col < 9; col += 3){
            if(isSubGridValid(board, row, col) == false)
                return false;
        }
    }
    return true;
}

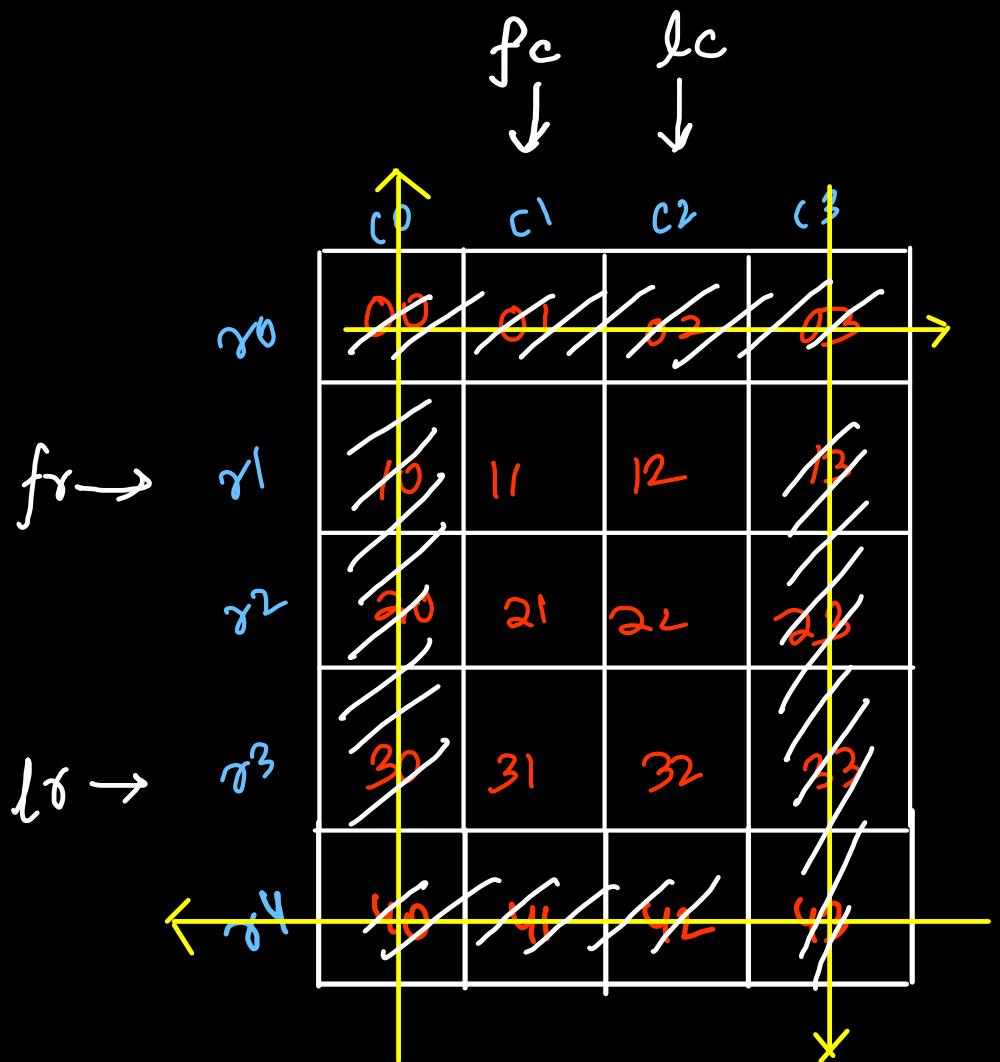
```

$\# \underline{O(3 \times 9 \times 9)}$

L(54) Spiral matrix



boundary
traversal



$f_r = 0, f_c = 0, l_r = m-1, l_c = n-1;$
 // top wall (left to right)
 for(int c = fc; c <= lc; c++)
 Sys0(mat[r][c]); } fr++;

// right wall (top to bottom)
 for(int r = fr; r <= lr; r++)
 Sys0(mat[r][lc]); } lc--;

// bottom wall (right to left)
 for(int c = lc; c >= fc; c--)
 Sys0(mat[lr][c]); } lr--;

// left wall (bottom to top)
 for(int r = lr; r >= fr; r--) { f++
 Sys0(mat[r][fc]); }

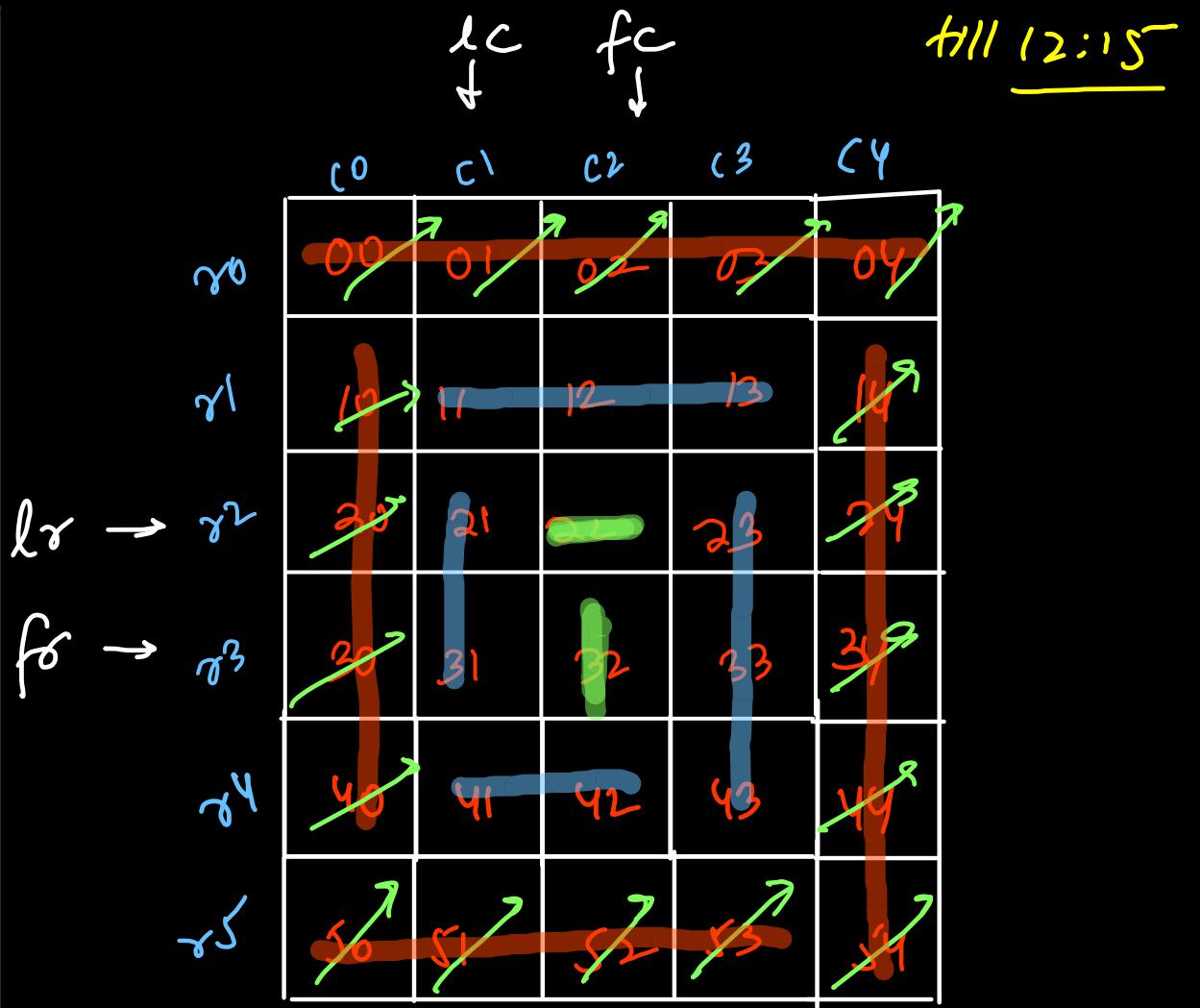
```

public List<Integer> spiralOrder(int[][] mat) {
    List<Integer> spiral = new ArrayList<>();
    int fr = 0, fc = 0, lr = mat.length - 1, lc = mat[0].length - 1;

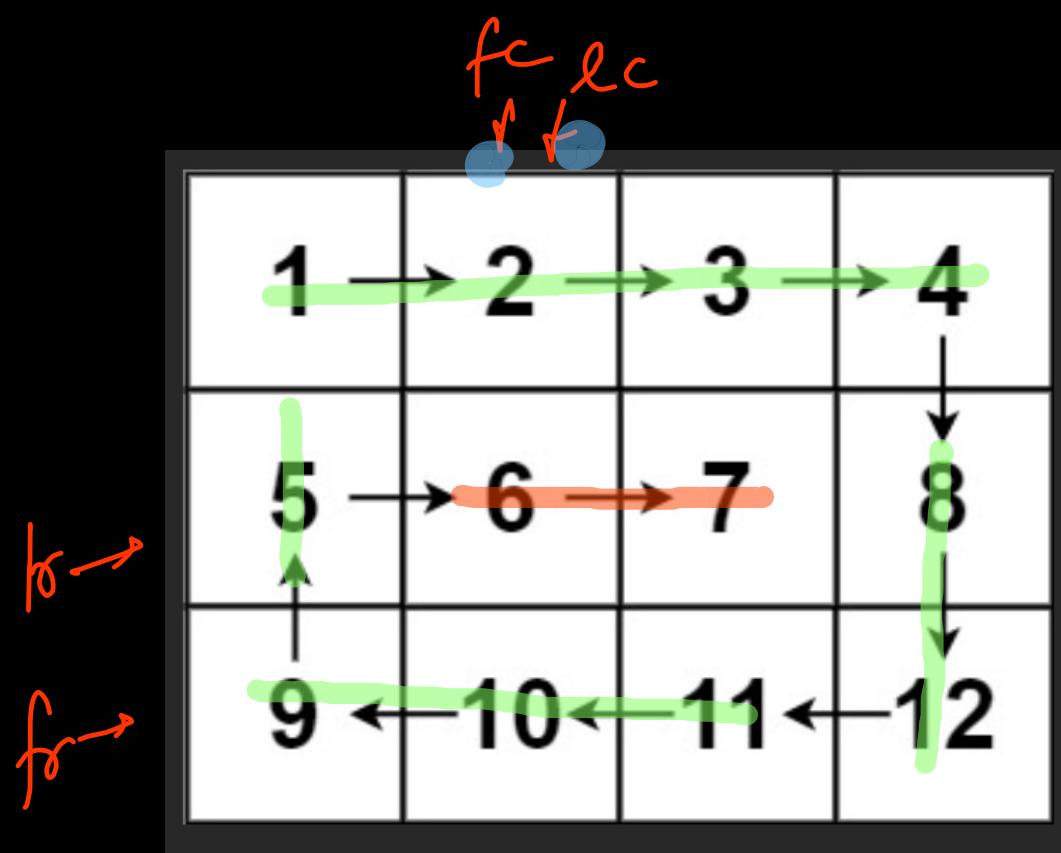
    while(true){ → all shells
        // top wall (left to right)
        for(int c = fc; c <= lc; c++){
            spiral.add(mat[fr][c]);
        }
        fr++; → ignore top wall
        if(fr > lr) break;
        ← no row remaining
        // right wall (top to bottom)
        for(int r = fr; r <= lr; r++){
            spiral.add(mat[r][lc]);
        }
        lc--; → ignore
        if(fc > lc) break;
        ← no column remaining
        // bottom wall (right to left)
        for(int c = lc; c >= fc; c--){
            spiral.add(mat[lr][c]);
        }
        lr--; → ignore
        if(fr > lr) break;
        ← no row rem
        // left wall (bottom to top)
        for(int r = lr; r >= fr; r--){
            spiral.add(mat[r][fc]);
        }
        fc++; → ignore
        if(fc > lc) break;
        ← no col rem
    }

    return spiral;
}

```



Time : $O(m \times n)$
Space = $O(1)$
quadratic ,
inplace



```

public List<Integer> spiralOrder(int[][] mat) {
    List<Integer> spiral = new ArrayList<>();
    int fr = 0, fc = 0, lr = mat.length - 1, lc = mat[0].length - 1;

    while(true){
        // top wall (left to right)
        for(int c = fc; c <= lc; c++){
            spiral.add(mat[fr][c]);
        }
        fr++;
        if(fr > lr) break;

        // right wall (top to bottom)
        for(int r = fr; r <= lr; r++){
            spiral.add(mat[r][lc]);
        }
        lc--;
        if(fc > lc) break;

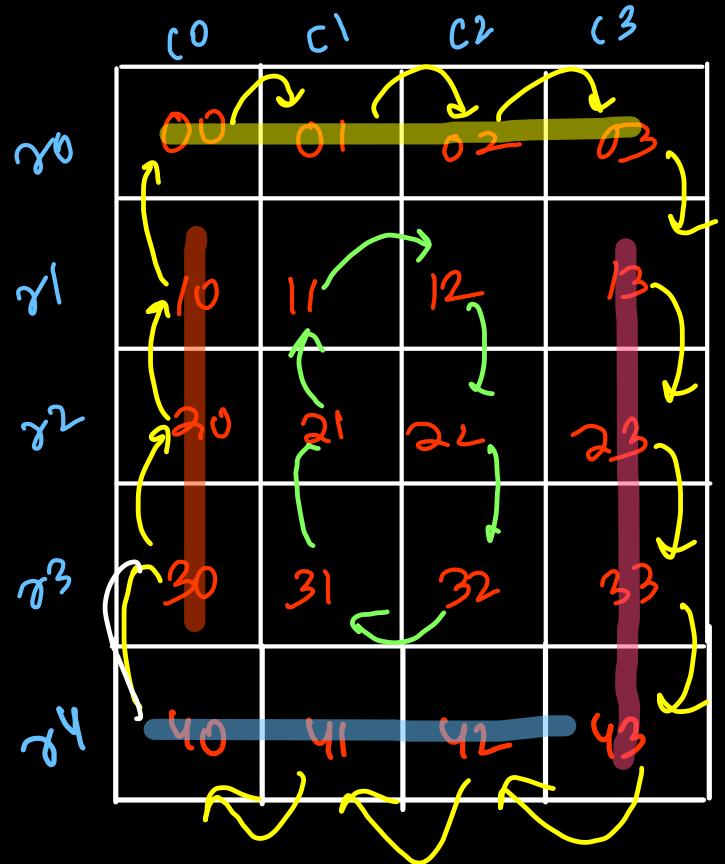
        // bottom wall (right to left)
        for(int c = lc; c >= fc; c--){
            spiral.add(mat[lr][c]);
        }
        lr--;
        if(fr > lr) break;

        // left wall (bottom to top)
        for(int r = lr; r >= fr; r--){
            spiral.add(mat[r][fc]);
        }
        fc++;
        if(fc > lc) break;
    }

    return spiral;
}

```

homework



GFG

Rotate shells of matrix

shell by shell



⇒ top wall \Rightarrow arraylist
↳ right shift

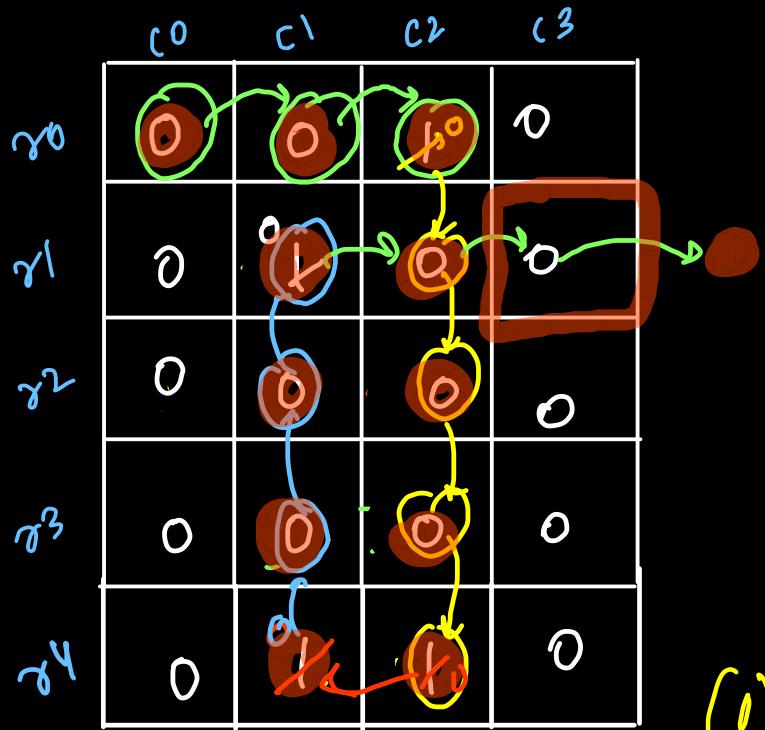
⇒ right wall \Rightarrow arraylist
↳ downshift

⇒ bottom wall \Rightarrow arraylist
↳ left shift

⇒ left wall \Rightarrow arraylist
↳ top shift

	c^0	c^1	c^2	c^3
r^0	10	00	01	02
r^1	20	21	11	03
r^2	30	31	12	13
r^3	40	32	22	23
r^4	41	42	43	33

Exit Point Matrix

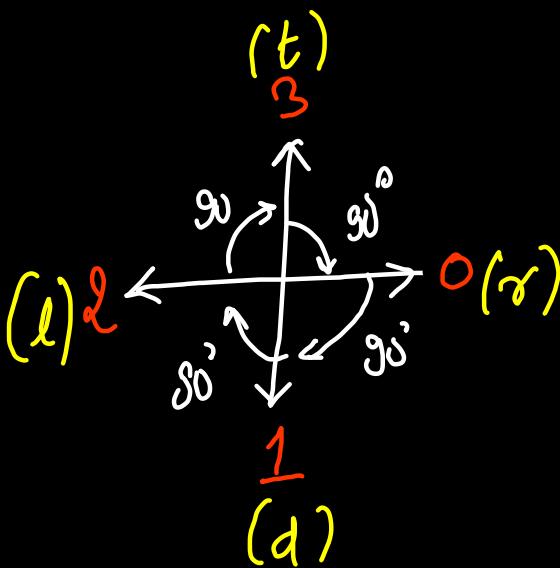


starting cell $\Rightarrow (0, 0)$

starting directn \Rightarrow left to right

0 \Rightarrow same directn

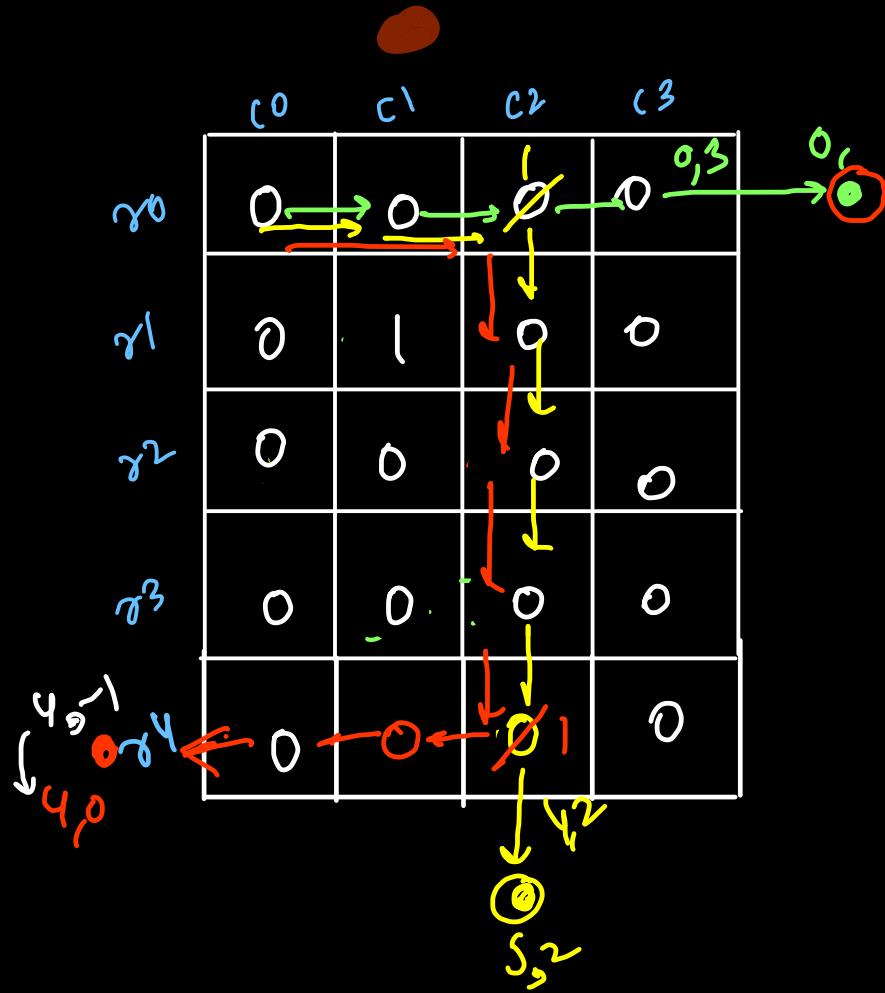
1 \Rightarrow directn $\Rightarrow 90^\circ$ rightwards
change value to 0.



```
// direction = 0 -> right, 1 -> down, 2 -> left, 3 -> top
public int[] FindExitPoint(int[][] mat)
{
    int row = 0, col = 0, direction = 0;

    while(row >= 0 && col >= 0 && row < mat.length && col < mat[0].length){
        if(mat[row][col] == 1){
            mat[row][col] = 0; // set 1 to 0
            direction = (direction + 1) % 4; // rotate the direction
        }

        if(direction == 0){
            // right
            col++;
        } else if(direction == 1){
            // down
            row++;
        } else if(direction == 2){
            // left
            col--;
        } else {
            // top
            row--;
        }
    }
}
```



```

// direction = 0 -> right, 1 -> down, 2 -> left, 3 -> top
public int[] FindExitPoint(int[][] mat)
{
    int row = 0, col = 0, direction = 0;

    while(row >= 0 && col >= 0 && row < mat.length && col < mat[0].length){
        if(mat[row][col] == 1){
            mat[row][col] = 0; // set 1 to 0
            direction = (direction + 1) % 4; // rotate the direction
        }

        if(direction == 0){
            // right
            col++;
        } else if(direction == 1){
            // down
            row++;
        } else if(direction == 2){
            // left
            col--;
        } else {
            // top
            row--;
        }
    }
}

```

```

if(row < 0){
    // top wall
    return new int[]{row + 1, col};
} else if(col < 0){
    // left wall
    return new int[]{row, col + 1};
} else if(row == mat.length){
    // bottom wall
    return new int[]{row - 1, col};
} else {
    // right wall
    return new int[]{row, col - 1};
}

```

calculate last cell within matrix

Time \rightarrow
 $O(n \times m)$

Space \rightarrow
 $O(1)$ inplace