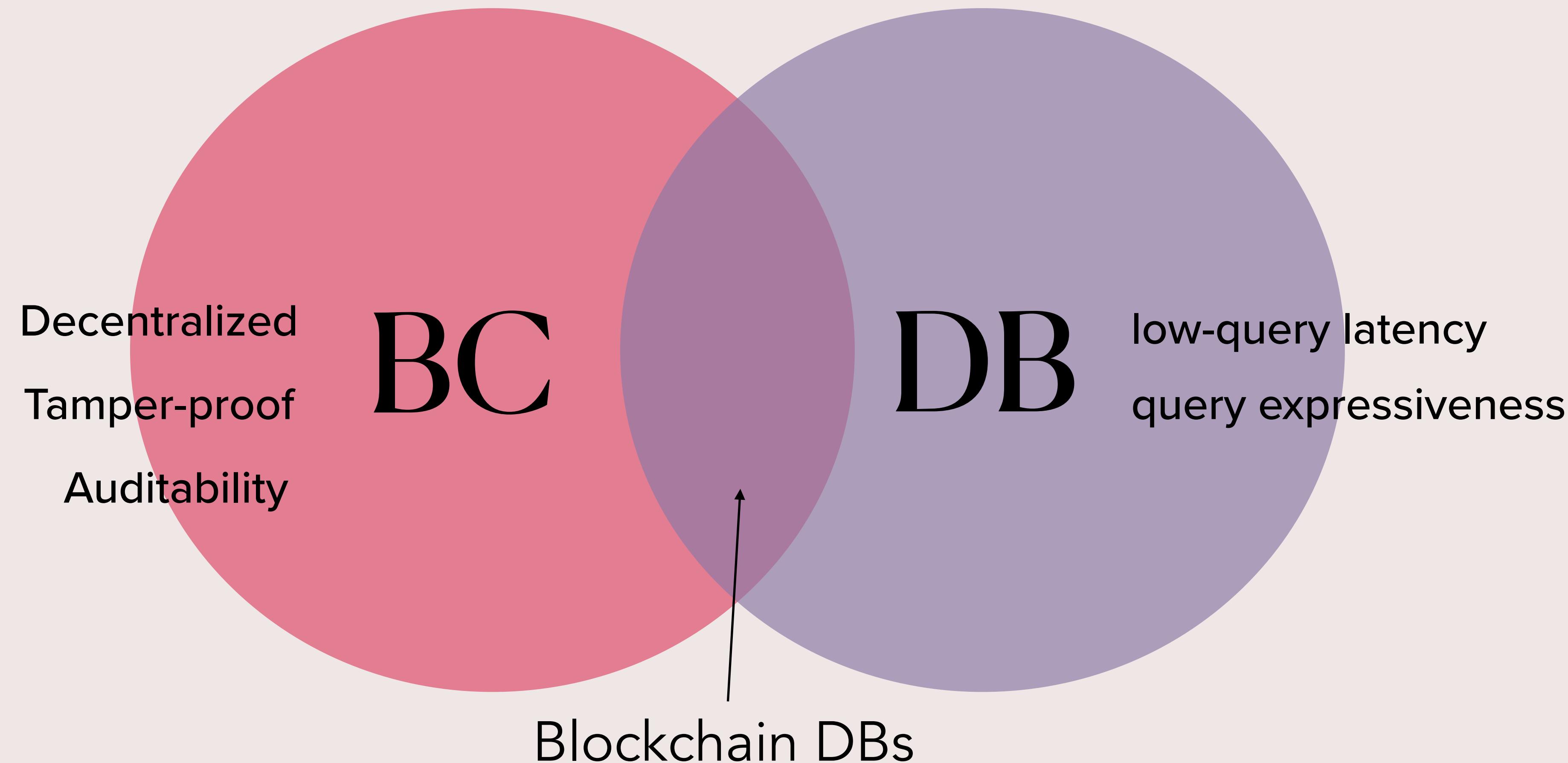


# Encrypted Blockchain Databases

**Daniel Adkins, Archita Agarwal, Seny Kamara, Tarik Moataz**



# Blockchain DBs

# Blockchain DBs



# Blockchain DBs



- electronic healthcare records
- financial records
- legal documents
- customer data

# Blockchain DBs



## CONFIDENTIALITY?

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- financial records
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# Blockchain DBs



## CONFIDENTIALITY?



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In this work ...

How to store Encrypted  
Multi-Maps on BCs

In this work ...

# How to store Encrypted Multi-Maps on BCs

a kind of NoSQL Databases, like Key-Value Stores

# What are Multimaps?

Set of label/value tuples

$\ell_1$	$(v_1, v_2)$
$\ell_2$	$(v_1, v_2, v_3)$
$\ell_3$	$(v_3)$
$\ell_4$	$(v_4, v_5)$
$\ell_5$	$(v_2, v_5, v_7, v_8)$

Varying lengths

*Encrypted*

# What are <sup>✓</sup>Multimaps?

Set of label/value tuples

$\ell_1$	$(v_1, v_2)$
$\ell_2$	$(v_1, v_2, v_3)$
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# What are <sup>✓</sup> Multimaps?

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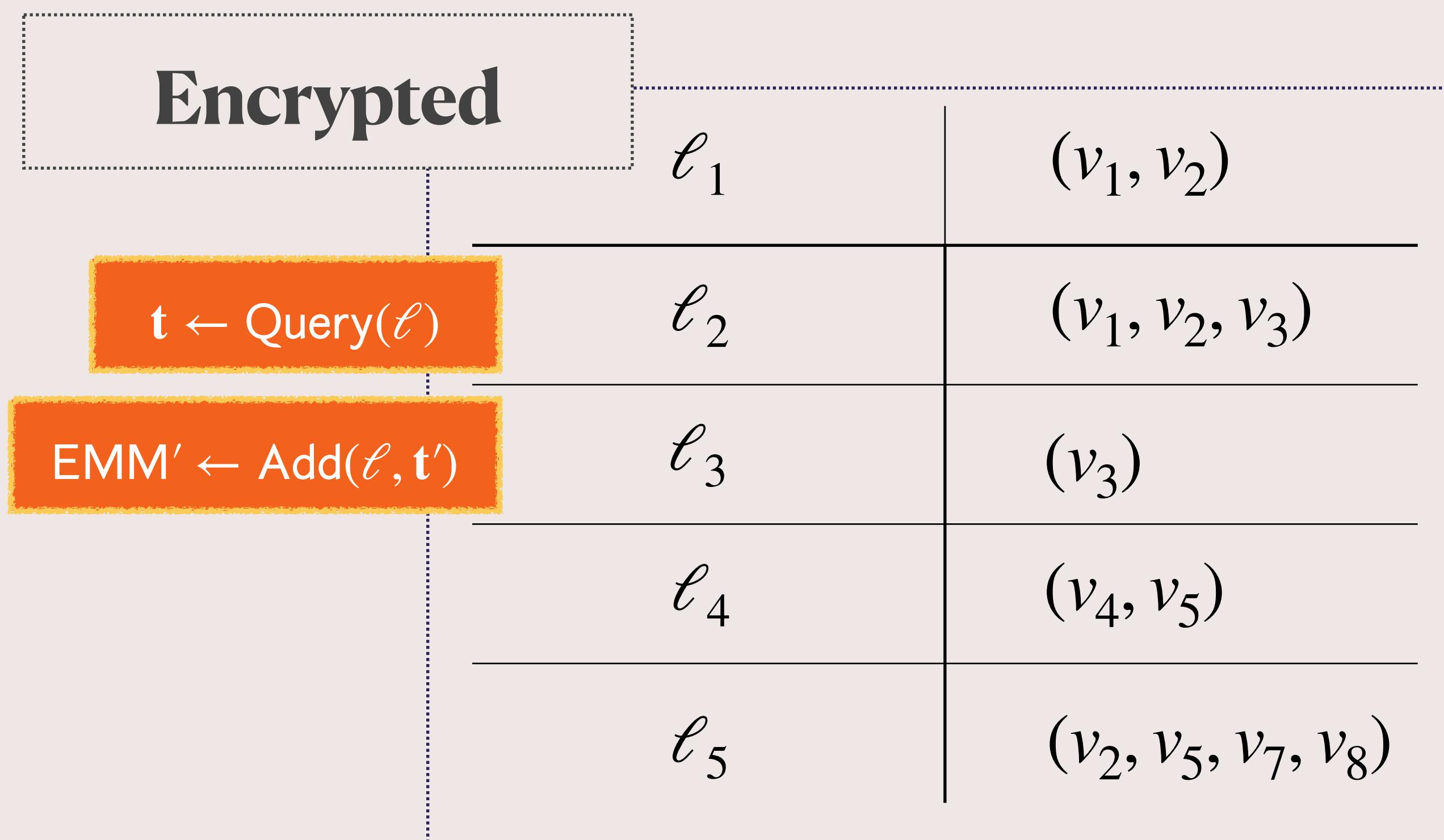
# What are <sup>✓</sup> Multimaps?

Set of label/value tuples

Encrypted	
$\ell_1$	$(v_1, v_2)$
$\ell_2$	$(v_1, v_2, v_3)$
$\ell_3$	$(v_3)$
$\ell_4$	$(v_4, v_5)$
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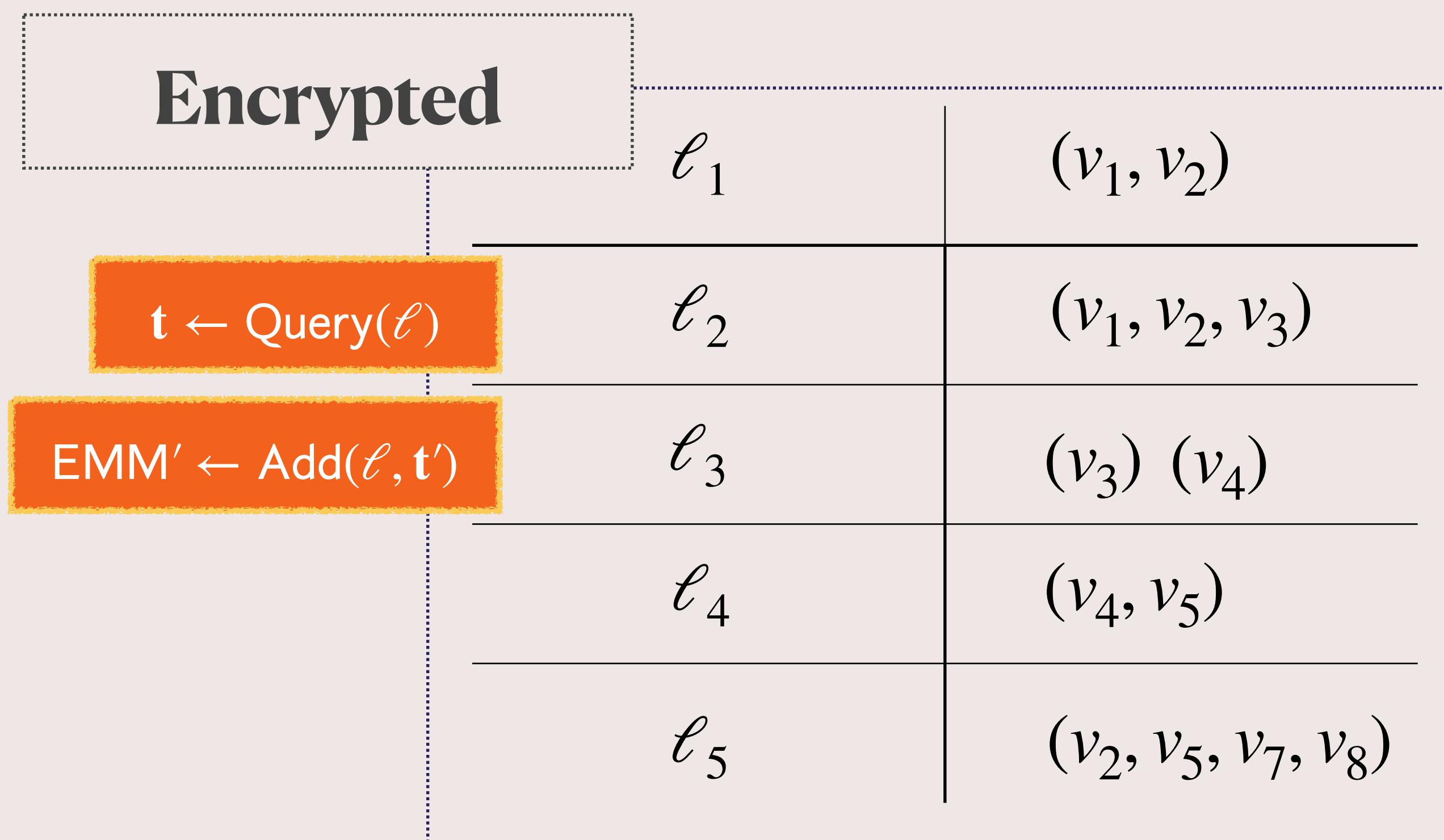
# What are <sup>✓</sup> Multimaps?

Set of label/value tuples



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Set of label/value tuples



# What are <sup>✓</sup> Multimaps?

Set of label/value tuples

Encrypted		
$t \leftarrow \text{Query}(\ell)$	$\ell_1$	$(v_1, v_2)$
$\text{EMM}' \leftarrow \text{Add}(\ell, t')$	$\ell_2$	$(v_1, v_2, v_3)$
$\text{EMM}' \leftarrow \text{Delete}(\ell, t')$	$\ell_3$	$(v_3) (v_4)$
	$\ell_4$	$(v_4, v_5)$
	$\ell_5$	$(v_2, v_5, v_7, v_8)$

# In our work

**LSX**

**List-Based**

**TRX**

**Tree-Based**

**PAX**

**Patch-Based**



# In our work

**LSX**

**List-Based**

**TRX**

**Tree-Based**

**PAX**

**Patch-Based**



# In our work

**LSX**

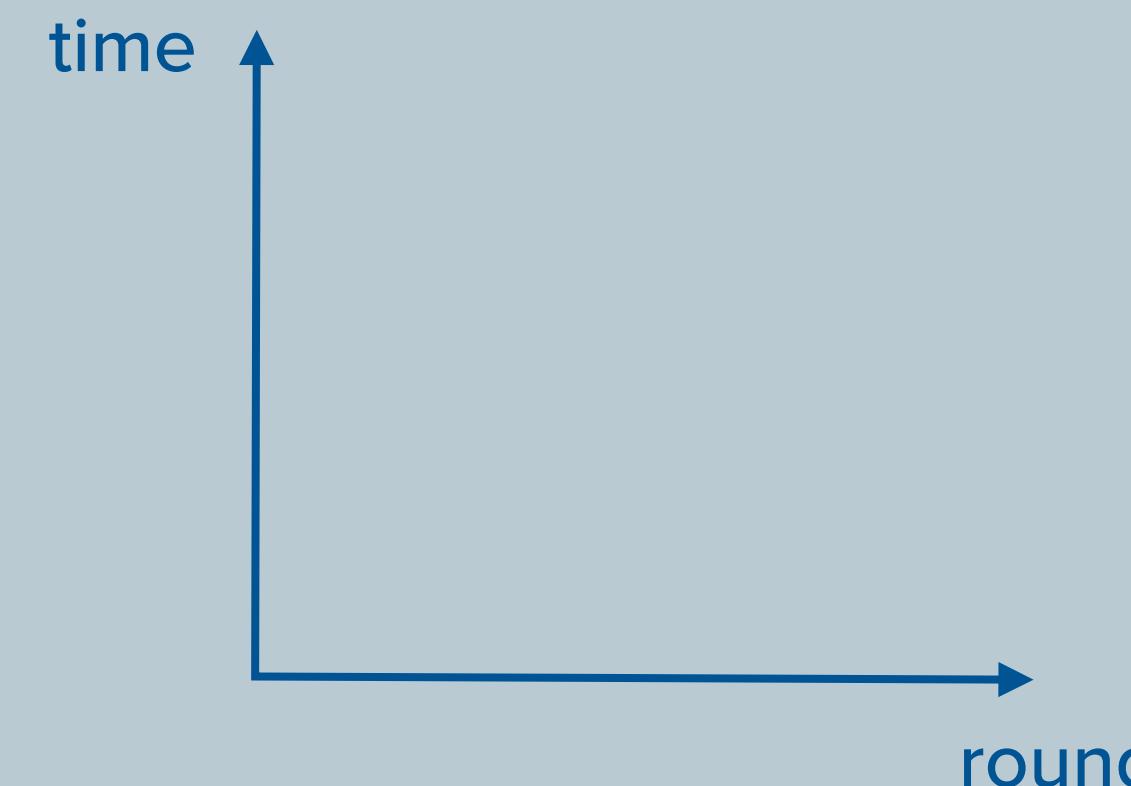
**List-Based**

**TRX**

**Tree-Based**

**PAX**

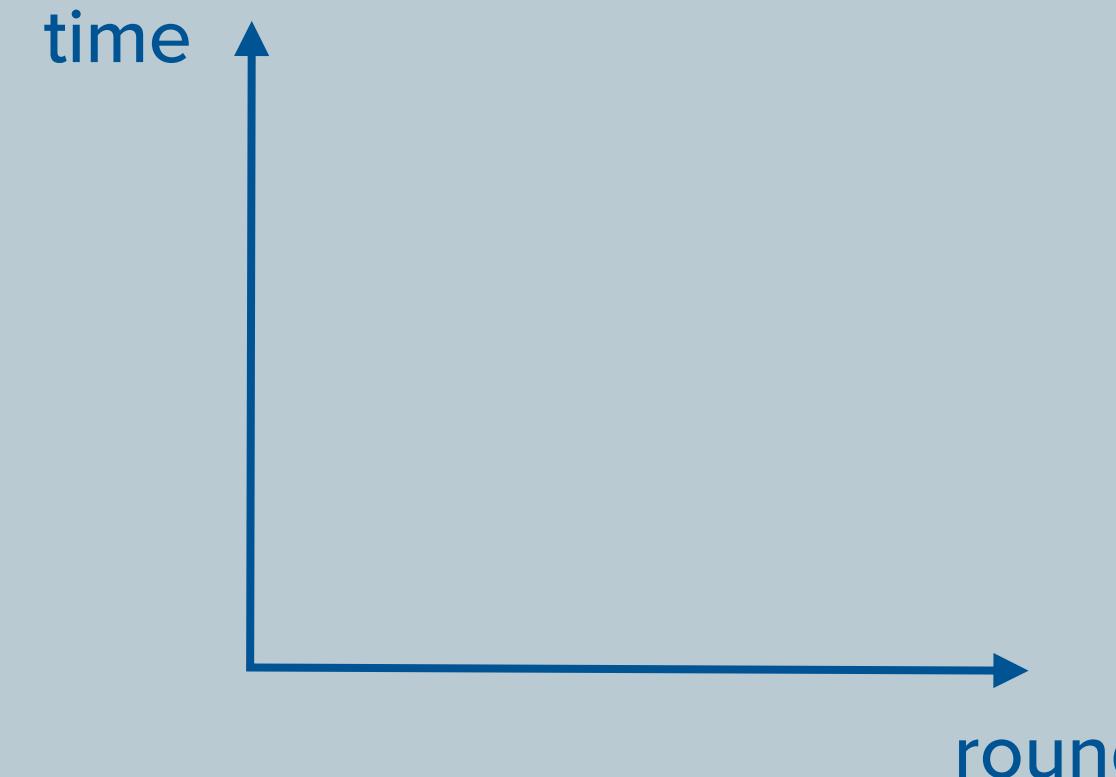
**Patch-Based**



# In our work

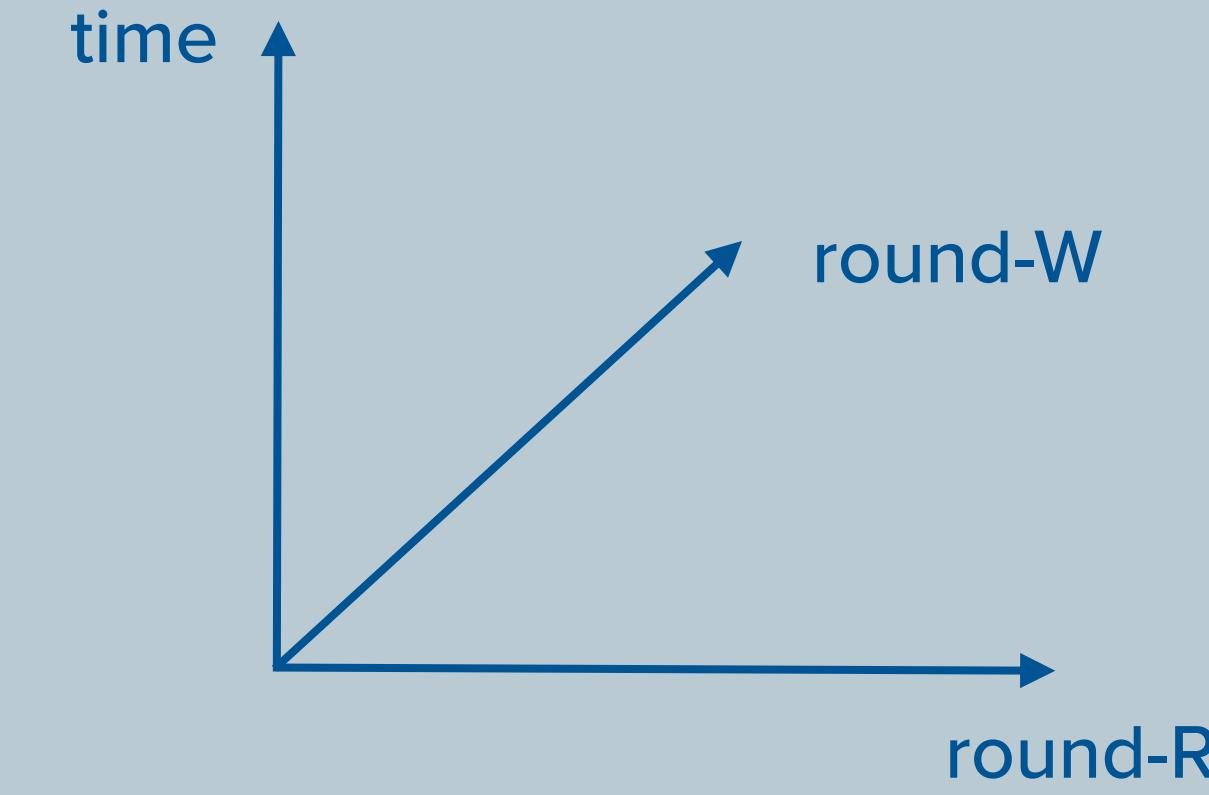
**LSX**

**List-Based**



**TRX**

**Tree-Based**



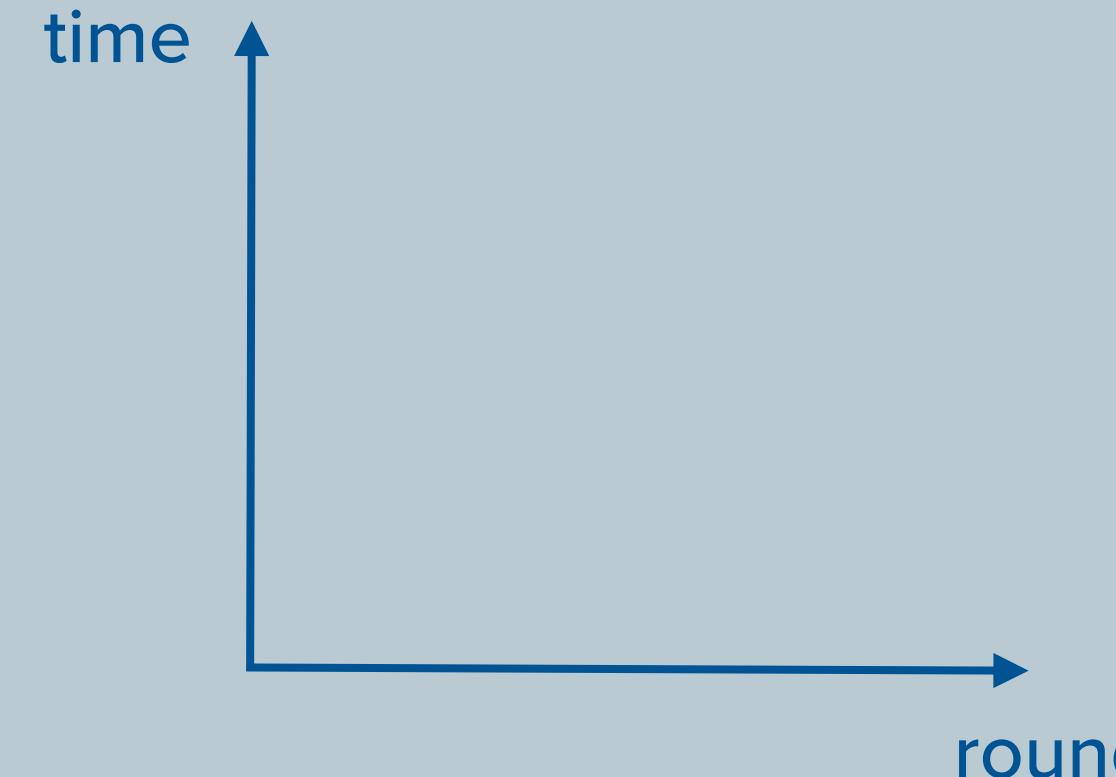
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# In our work

**LSX**

**List-Based**

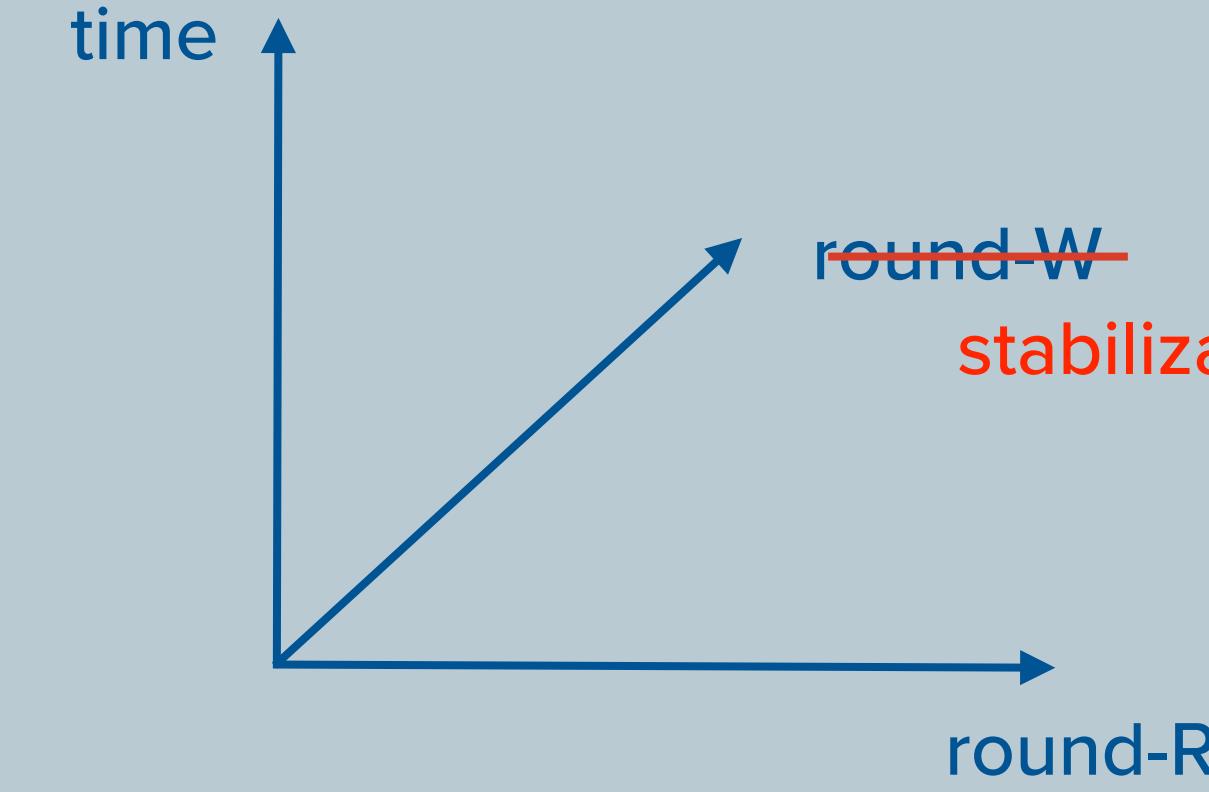


**TRX**

**Tree-Based**

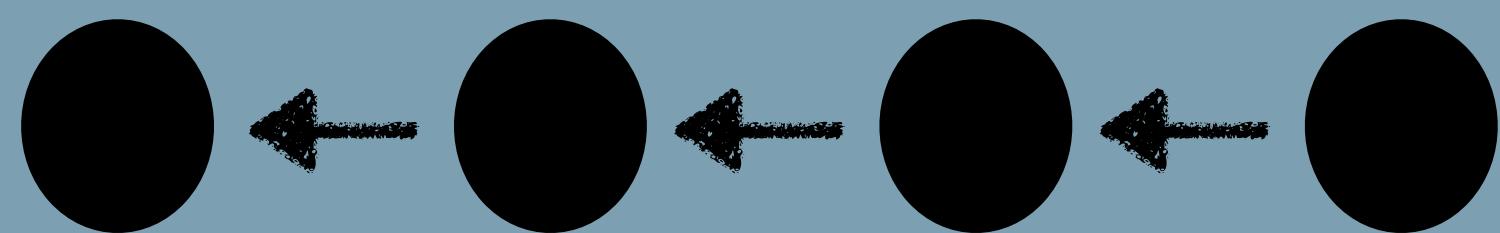
**PAX**

**Patch-Based**

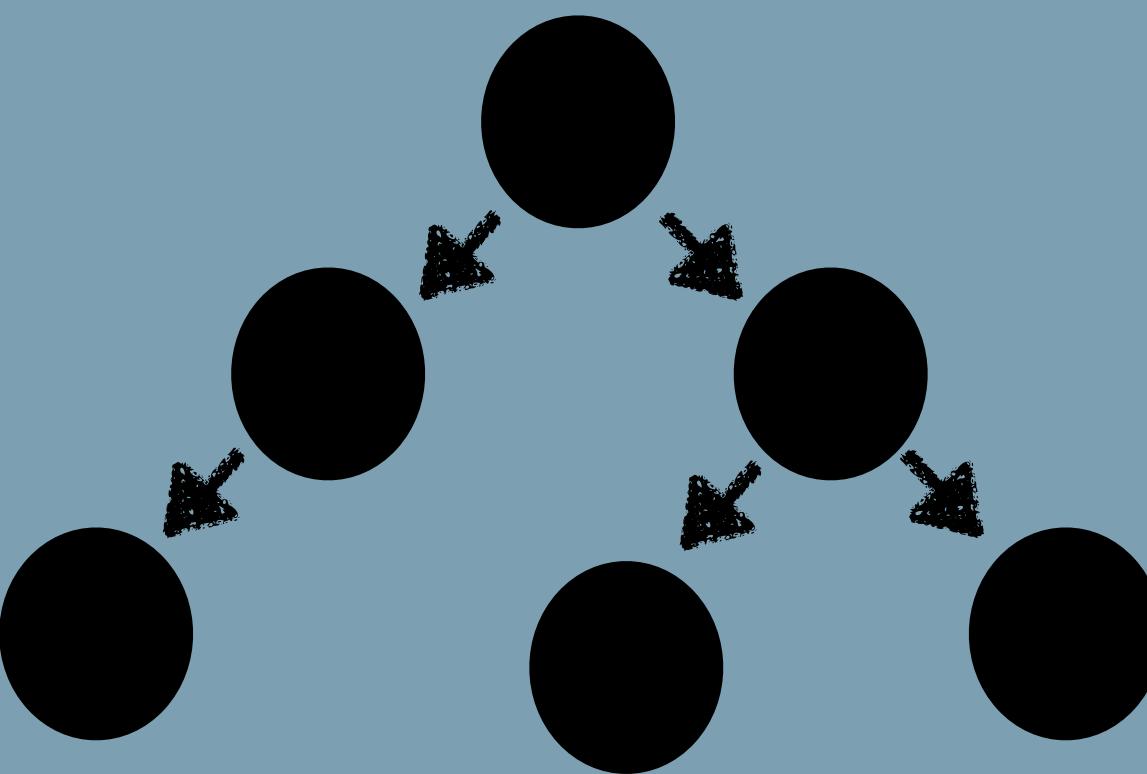
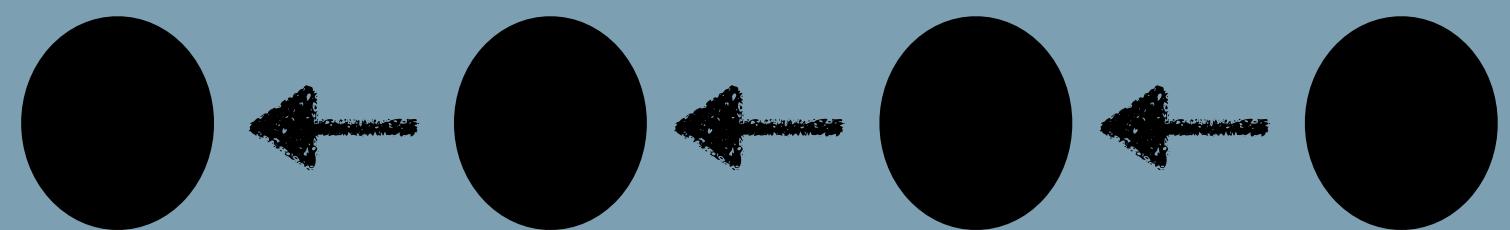


# Storing data structures on BCs

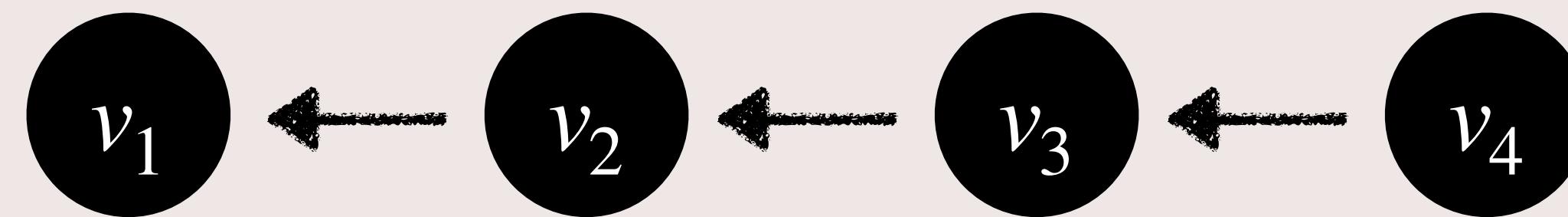
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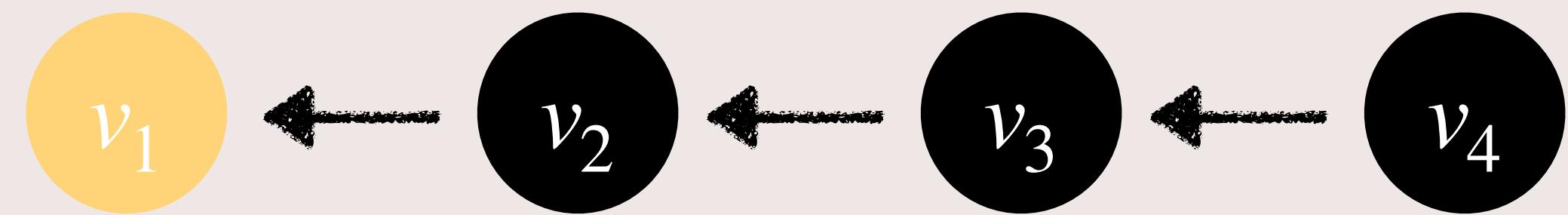
# Storing data structures on BCs



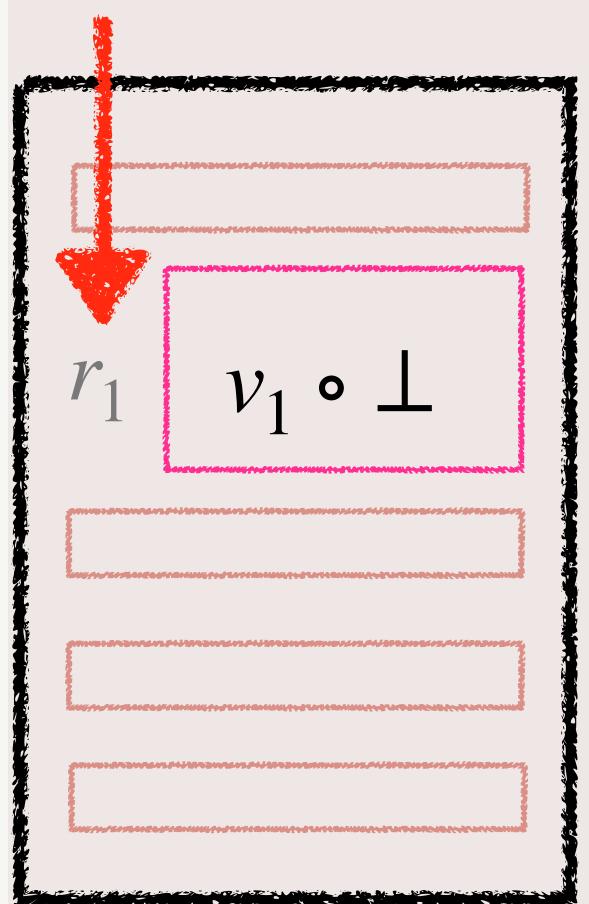
# Storing linked-list on BCs



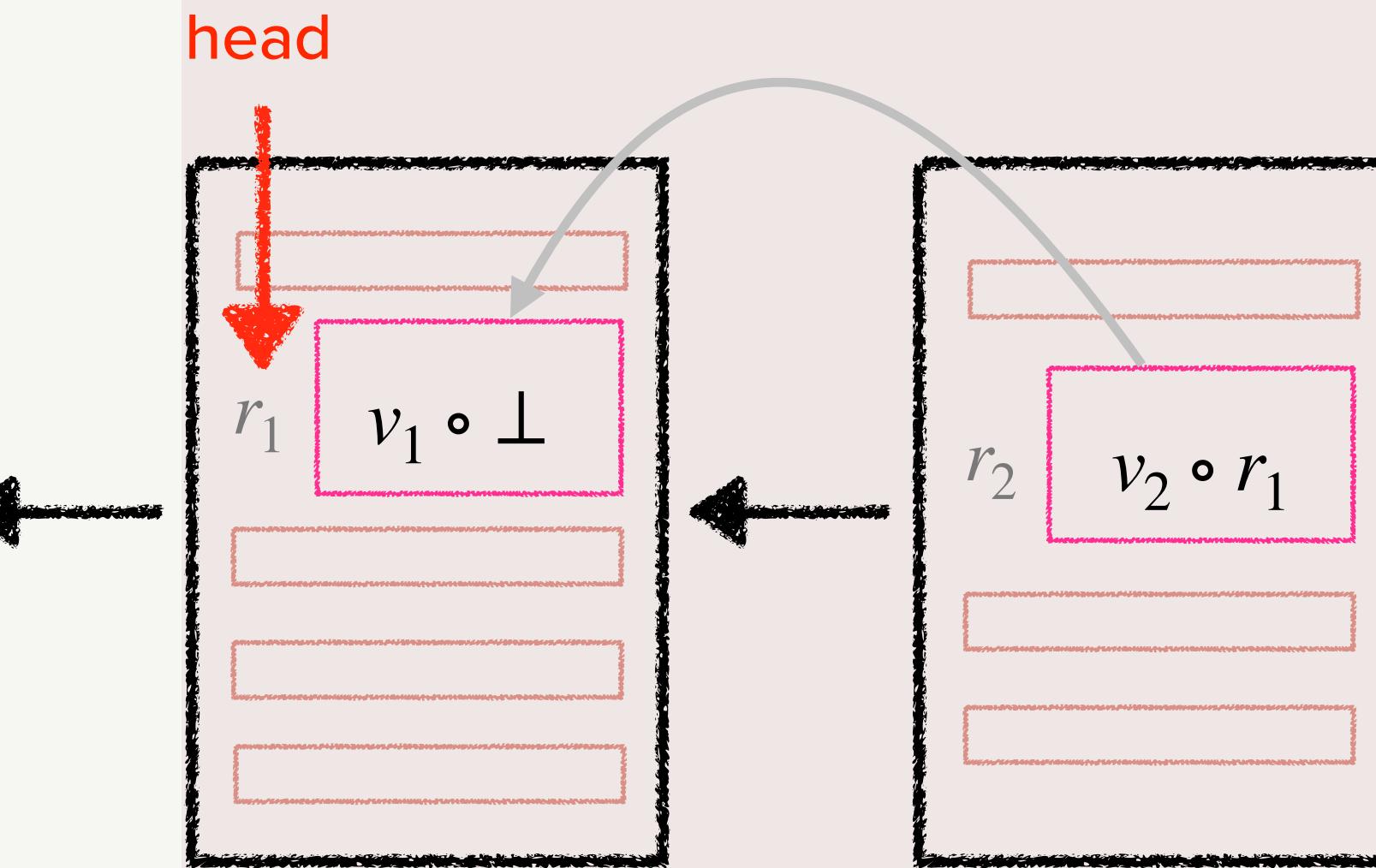
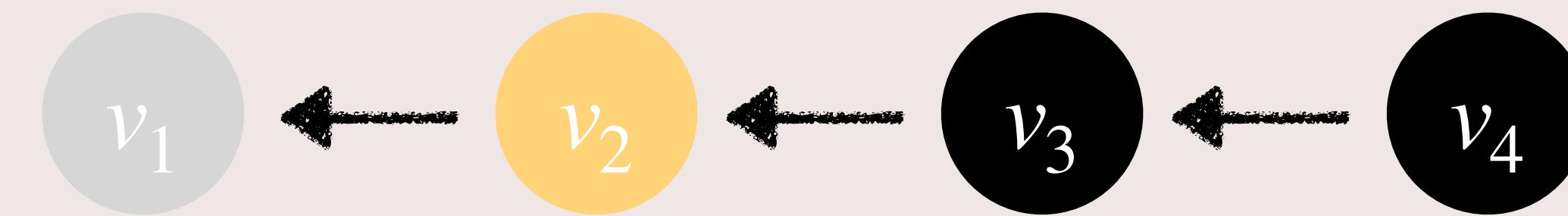
# Storing linked-list on BCs



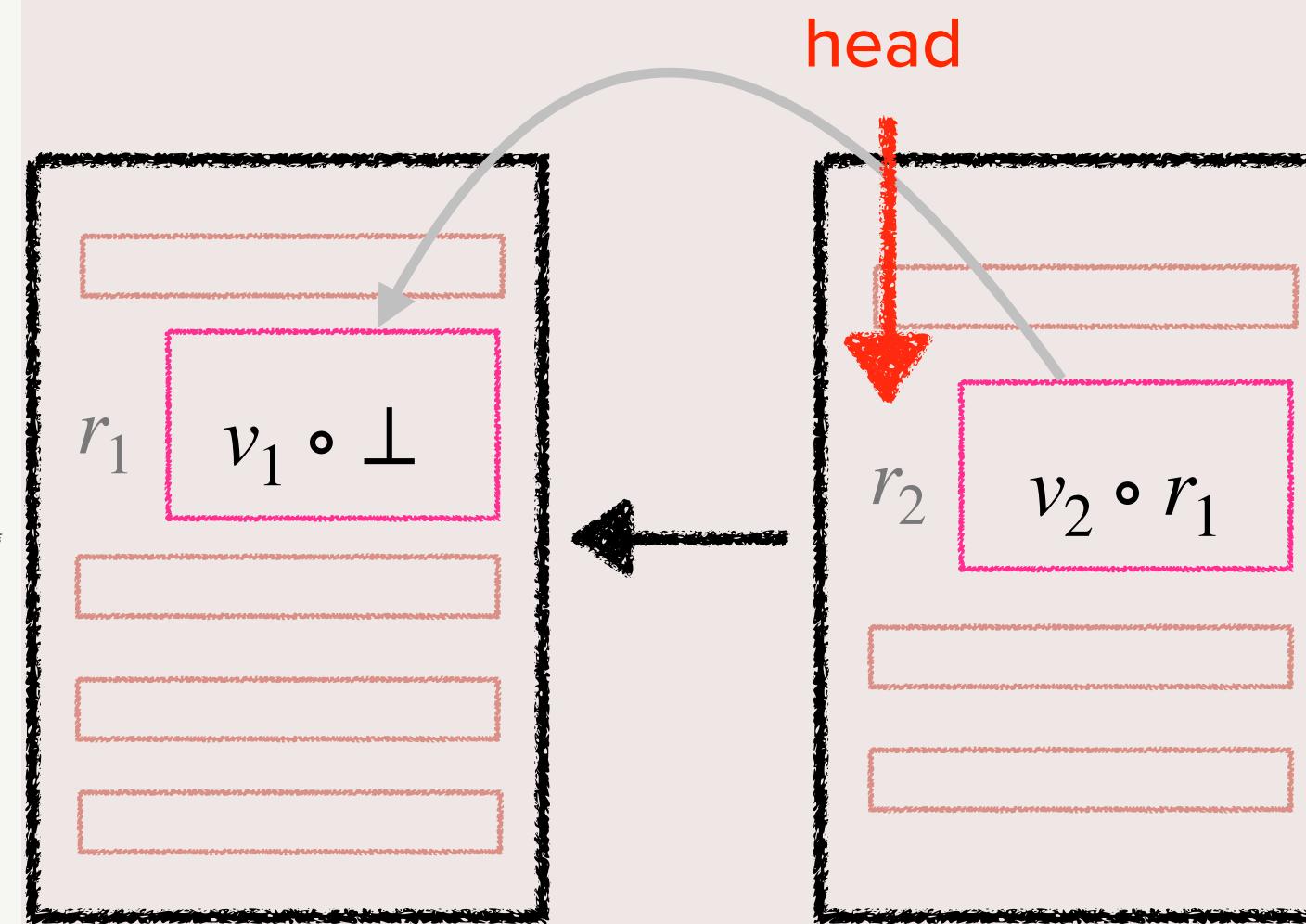
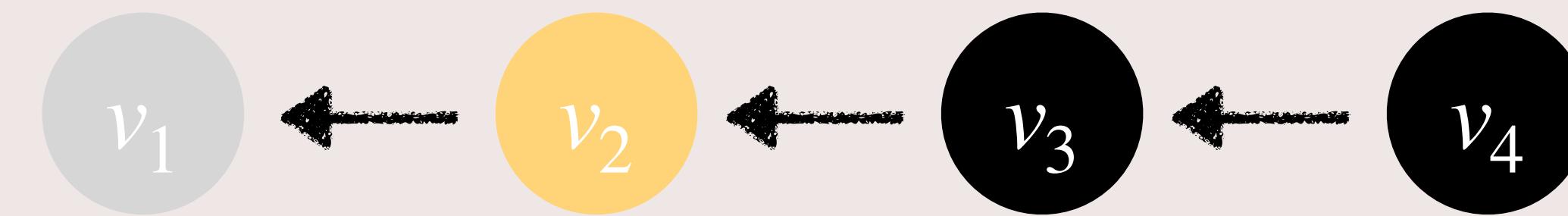
head



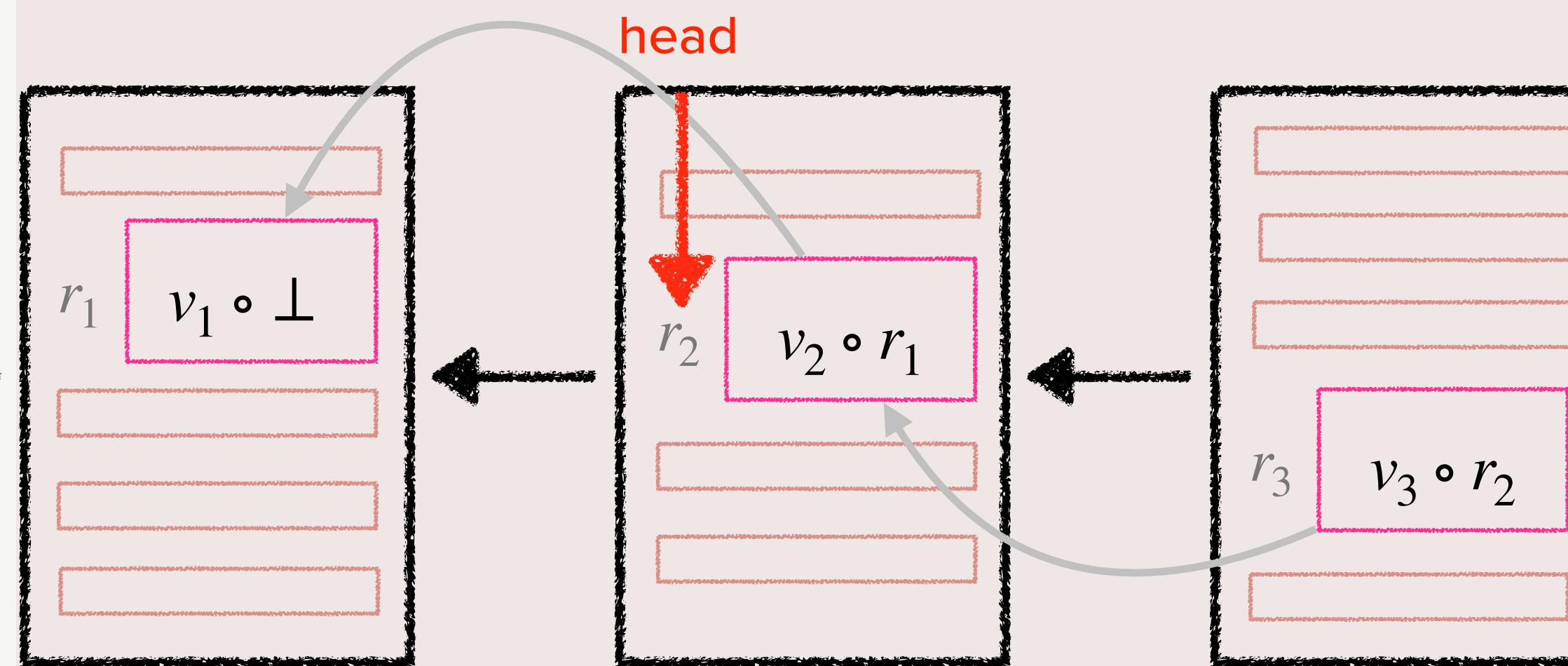
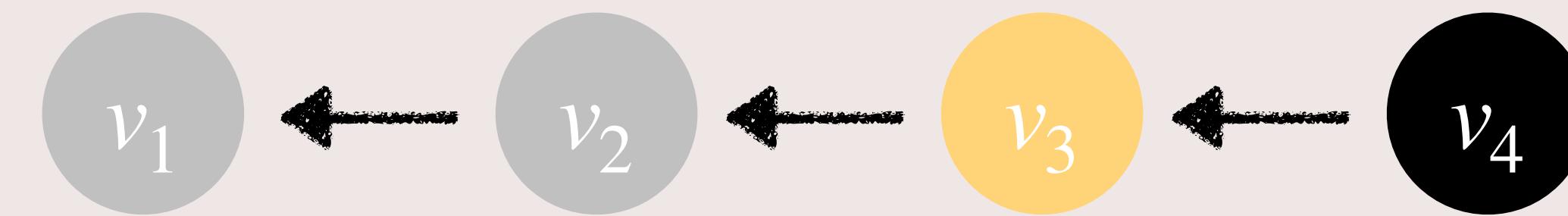
# Storing linked-list on BCs



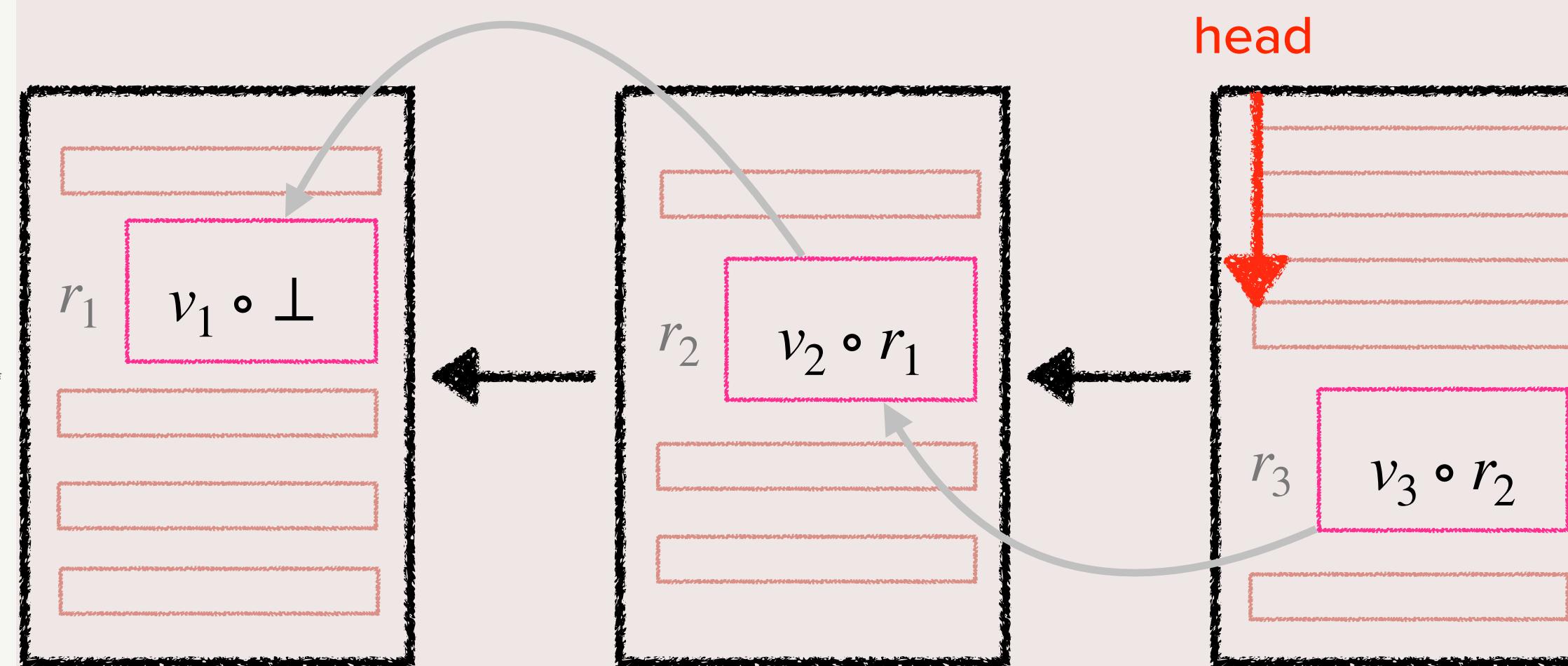
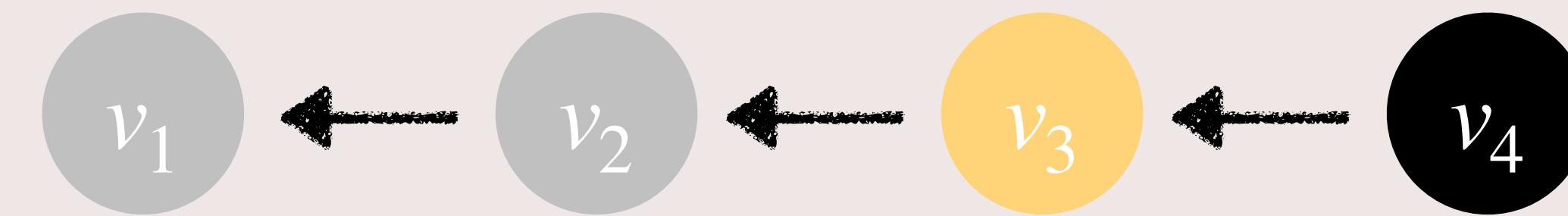
# Storing linked-list on BCs



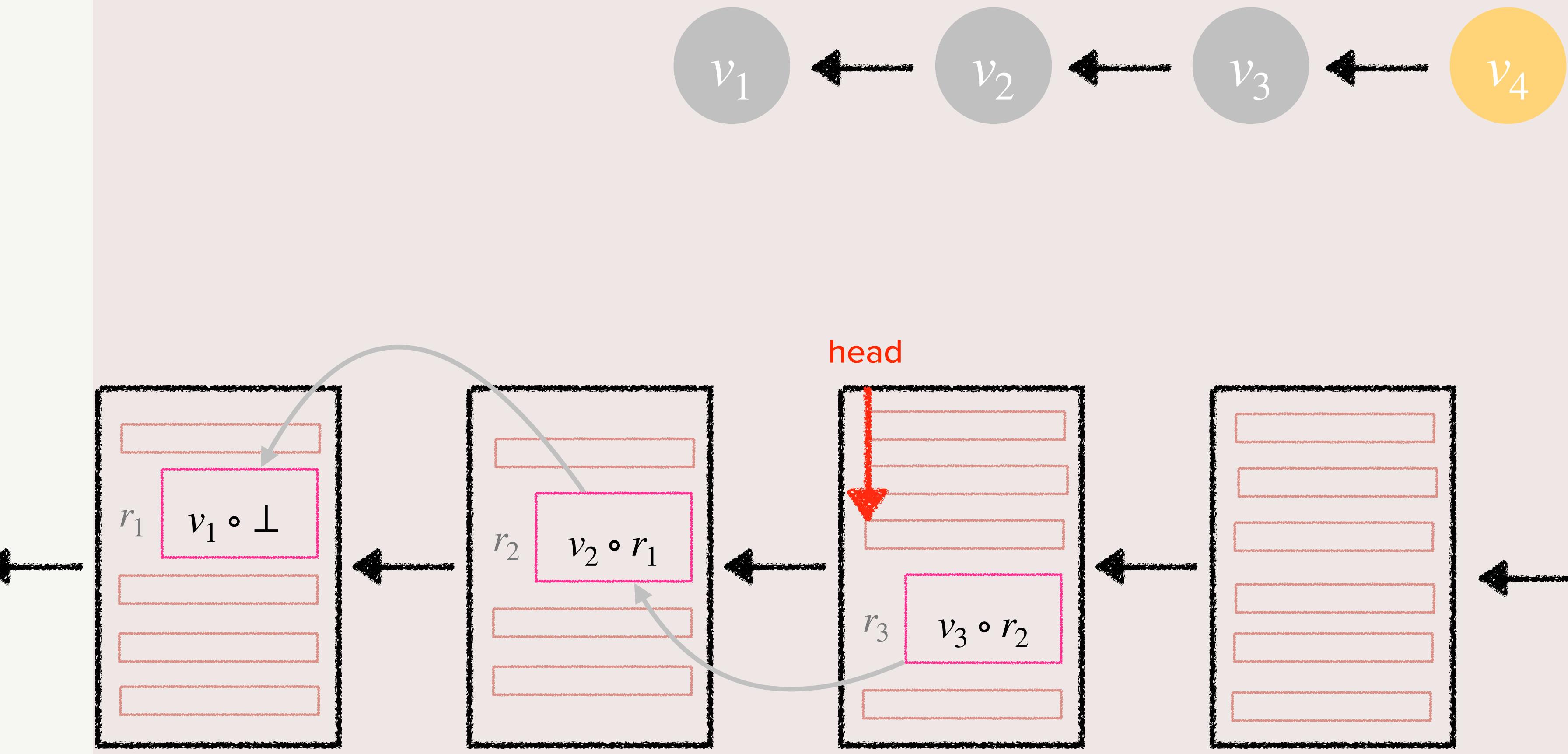
# Storing linked-list on BCs



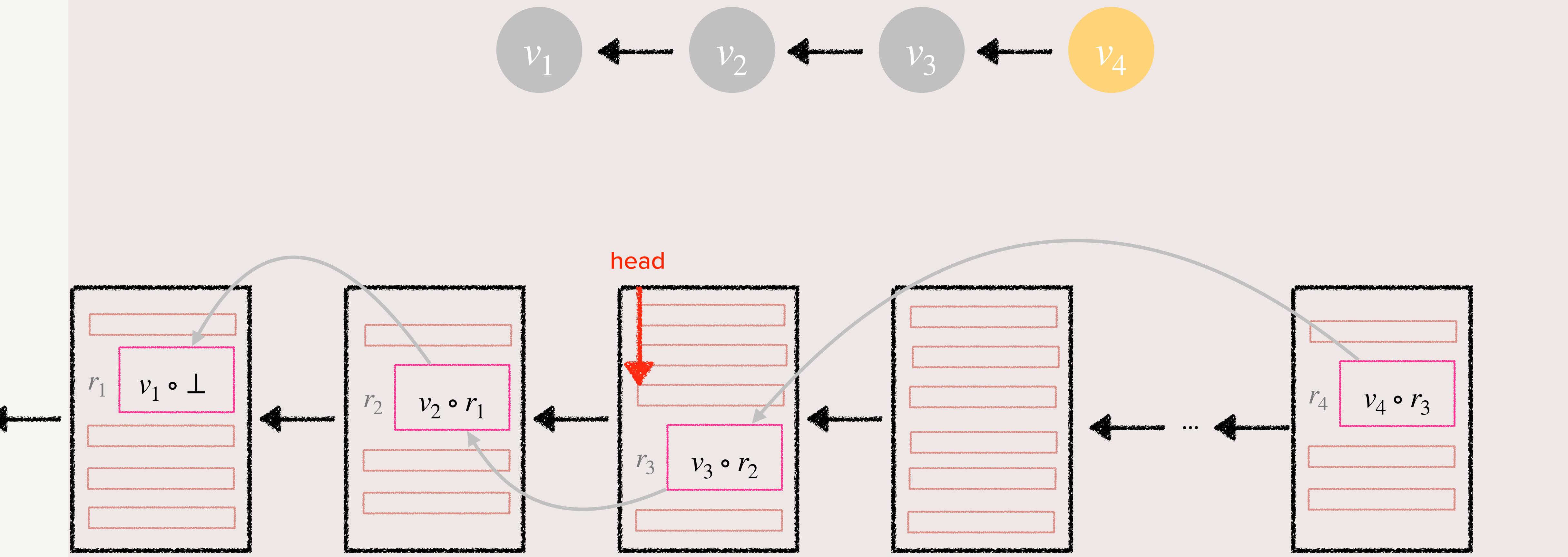
# Storing linked-list on BCs



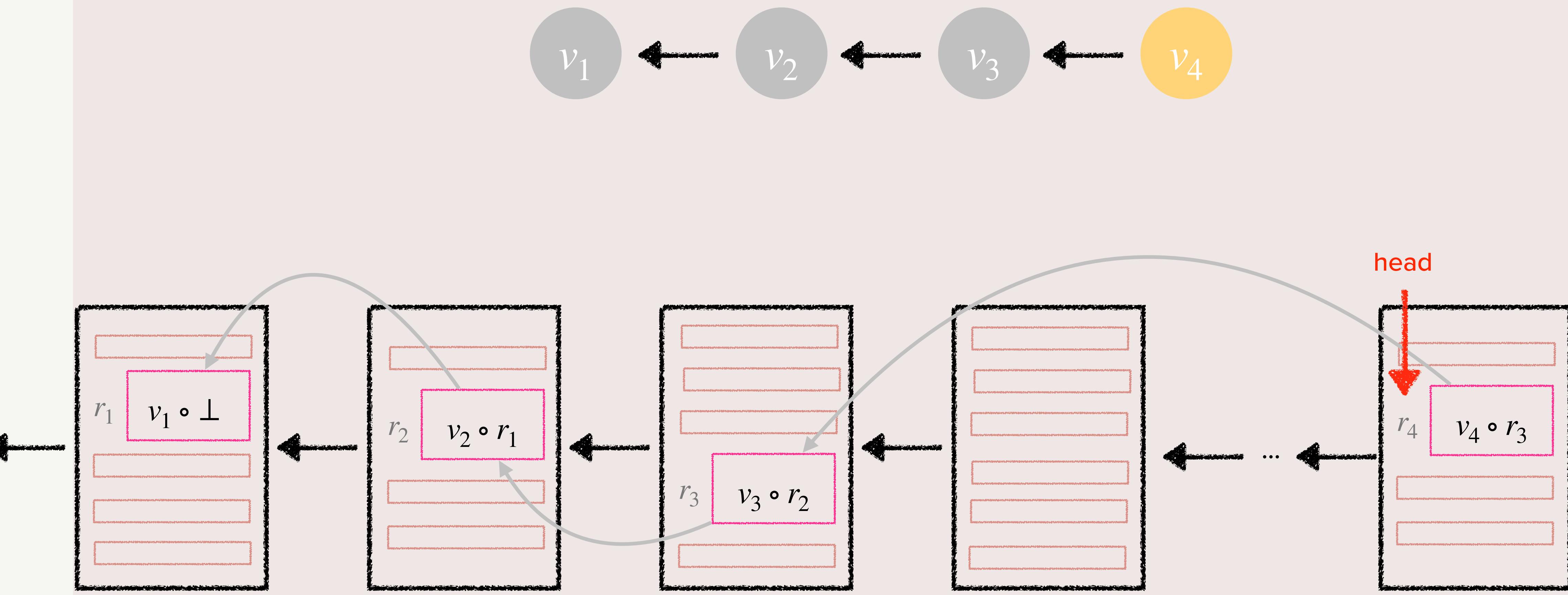
# Storing linked-list on BCs



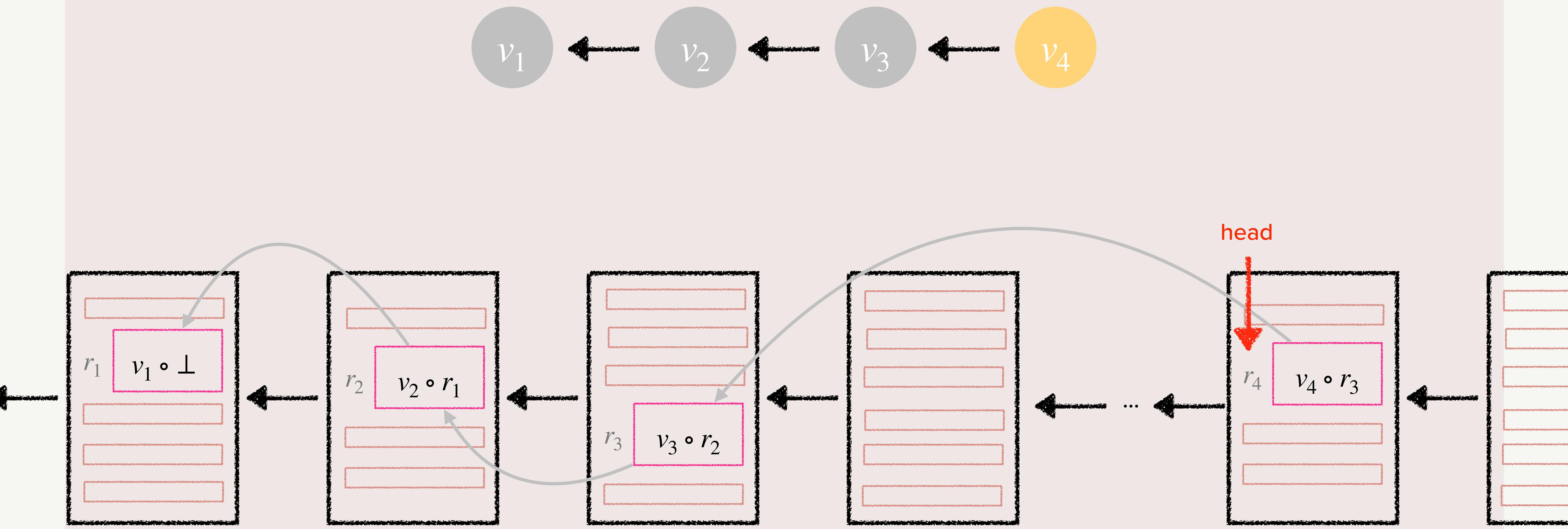
# Storing linked-list on BCs



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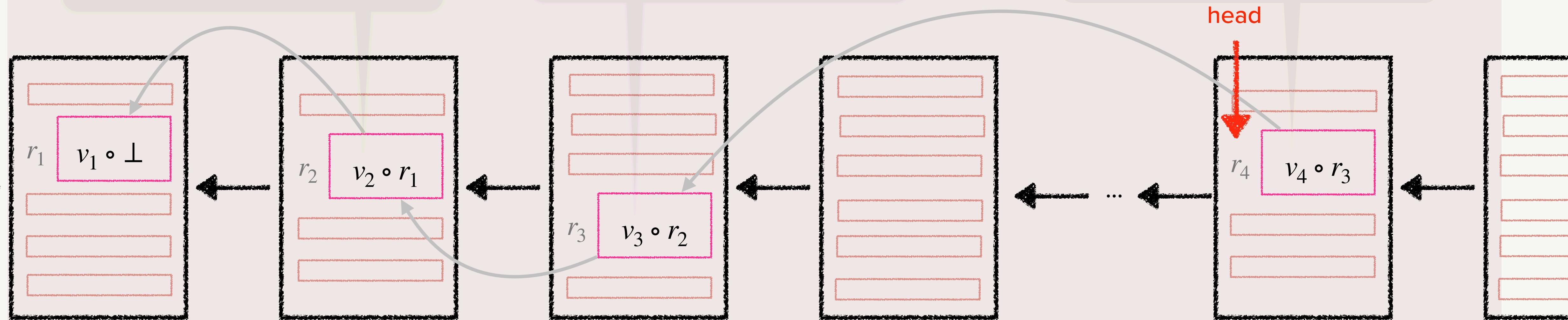
# Storing linked-list on BCs



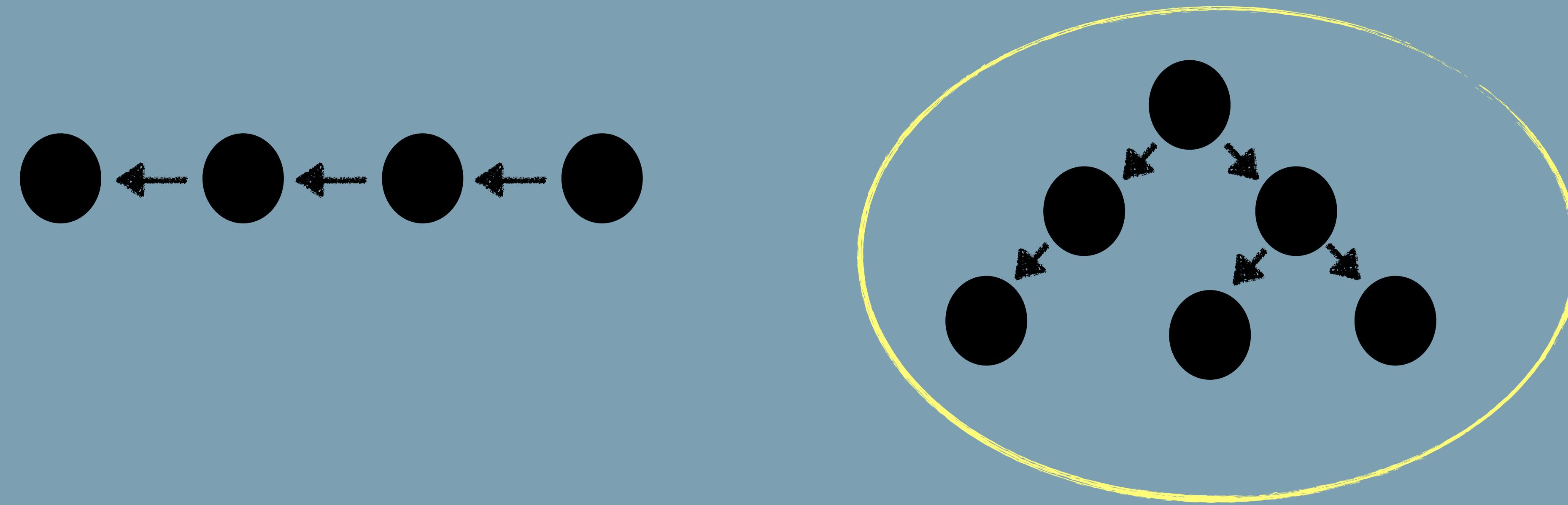
# Stabilization Complexity

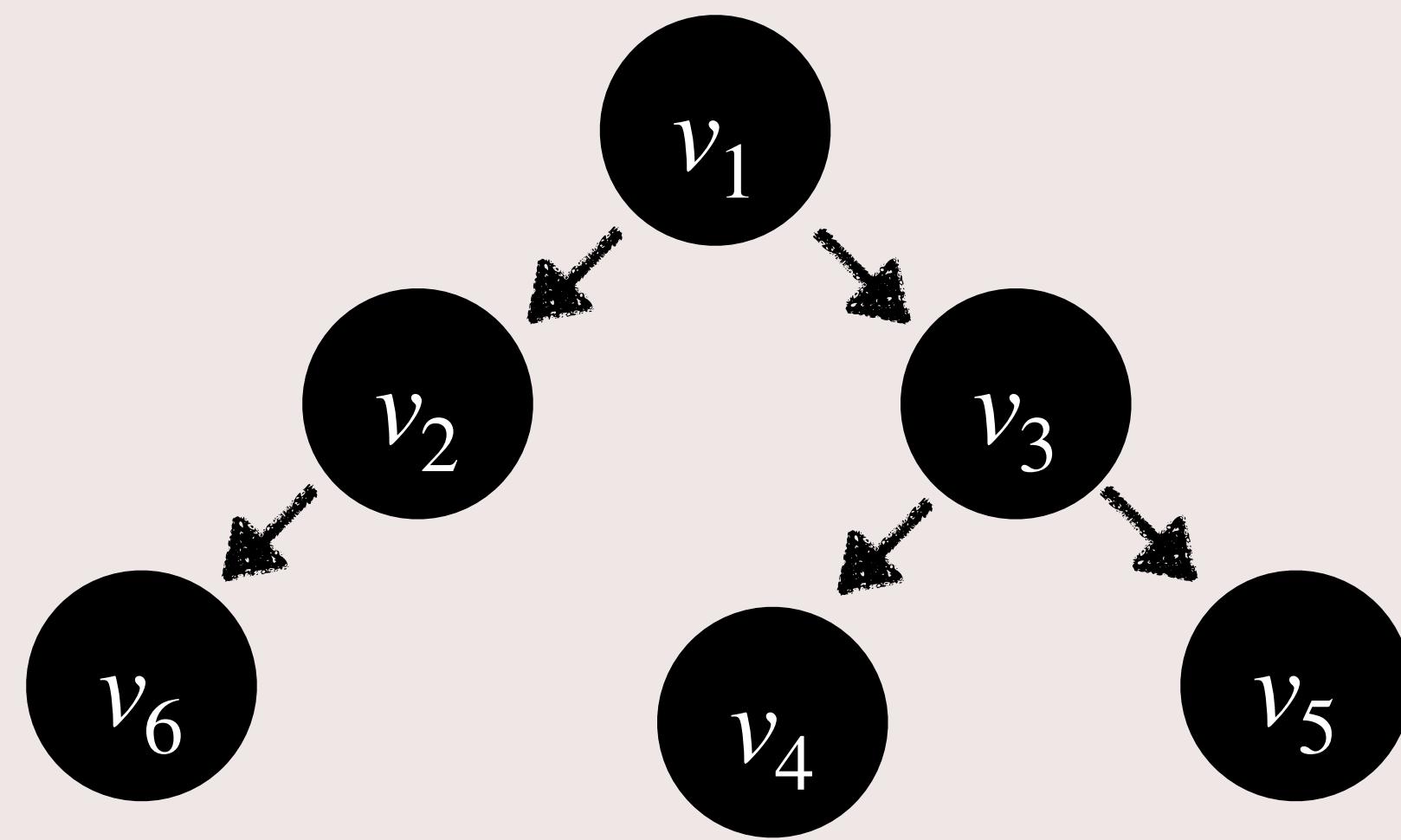
(aka number of write rounds)

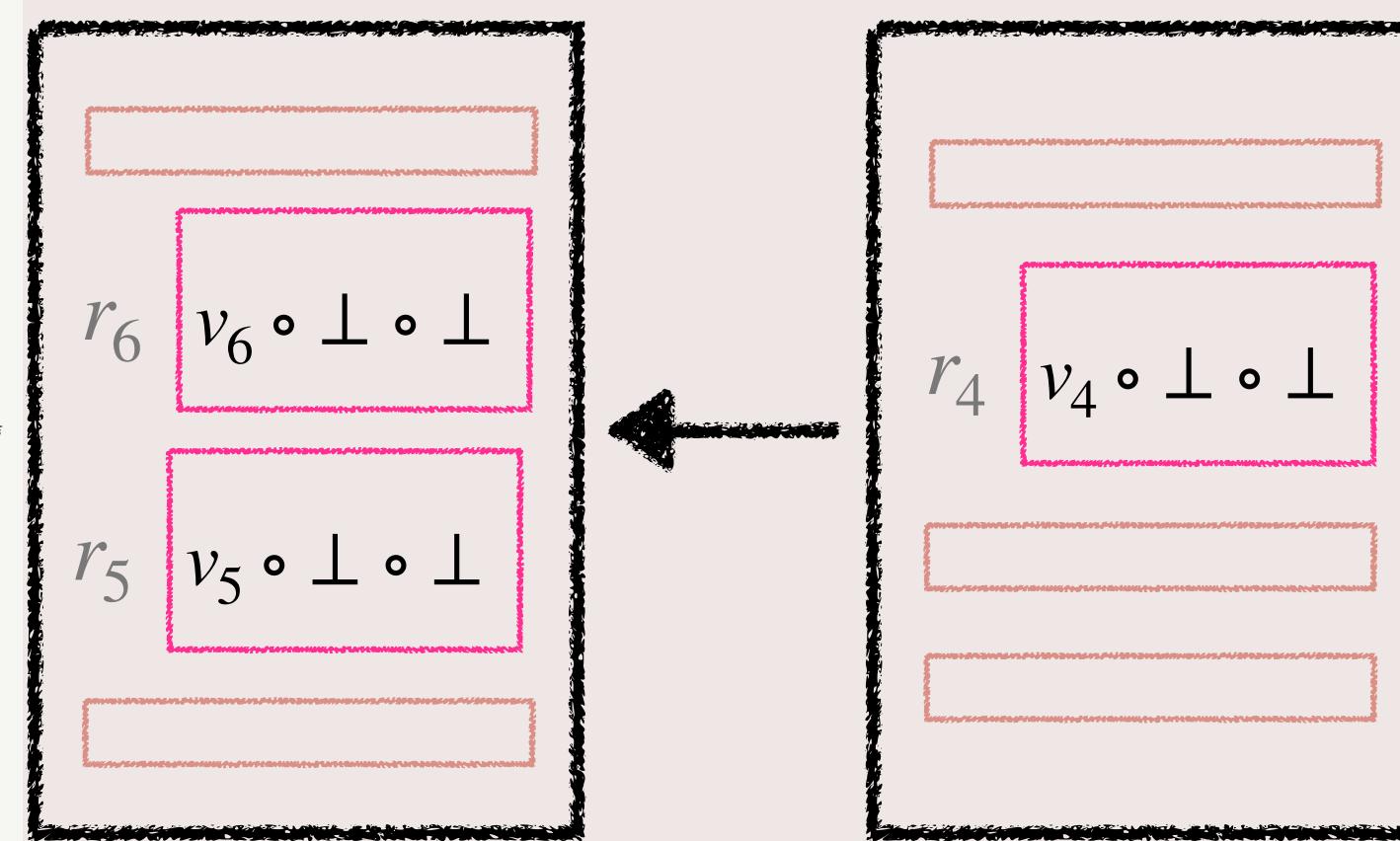
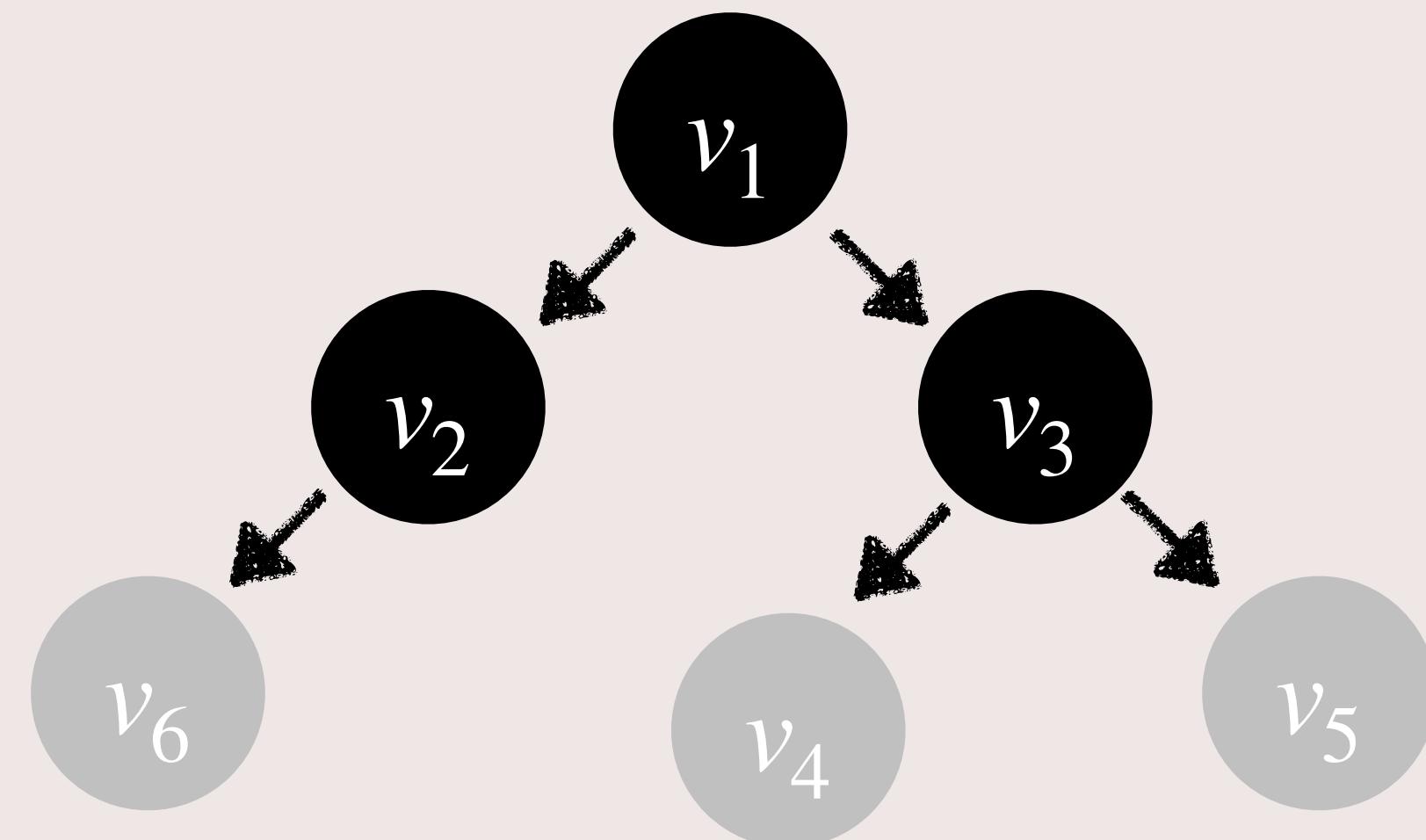
number of values in linked-list

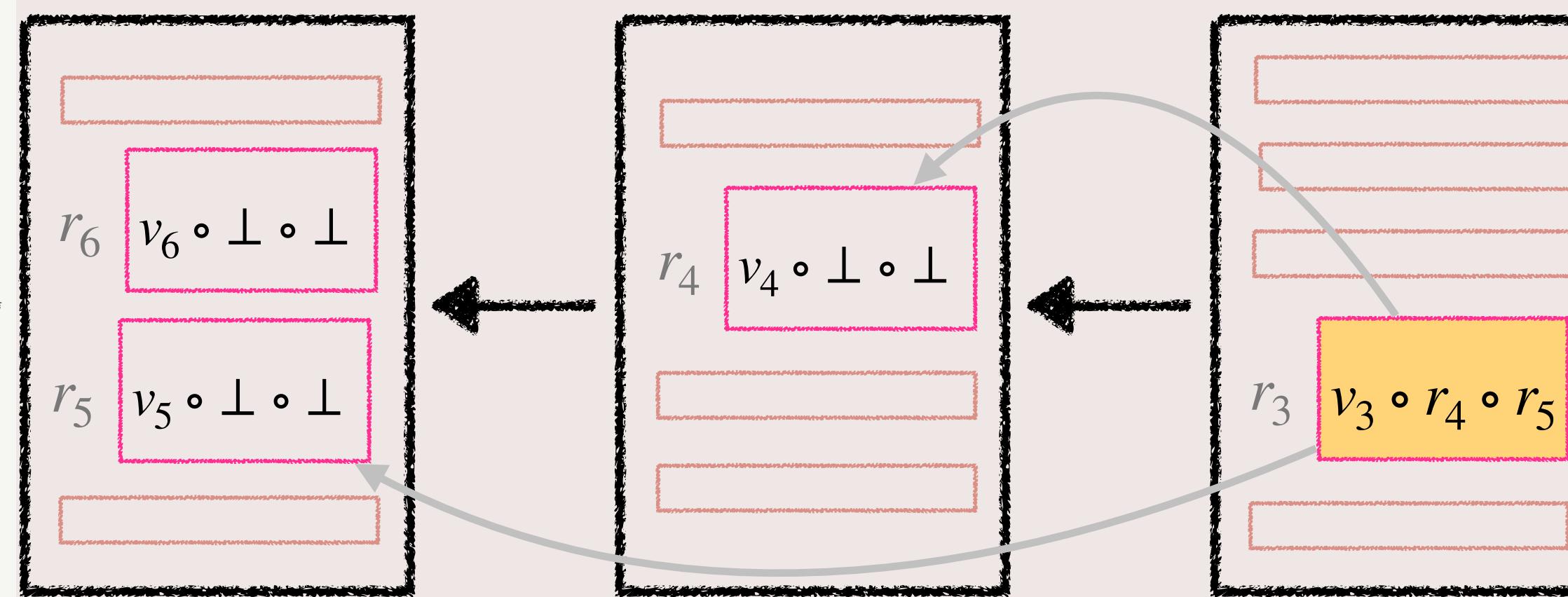
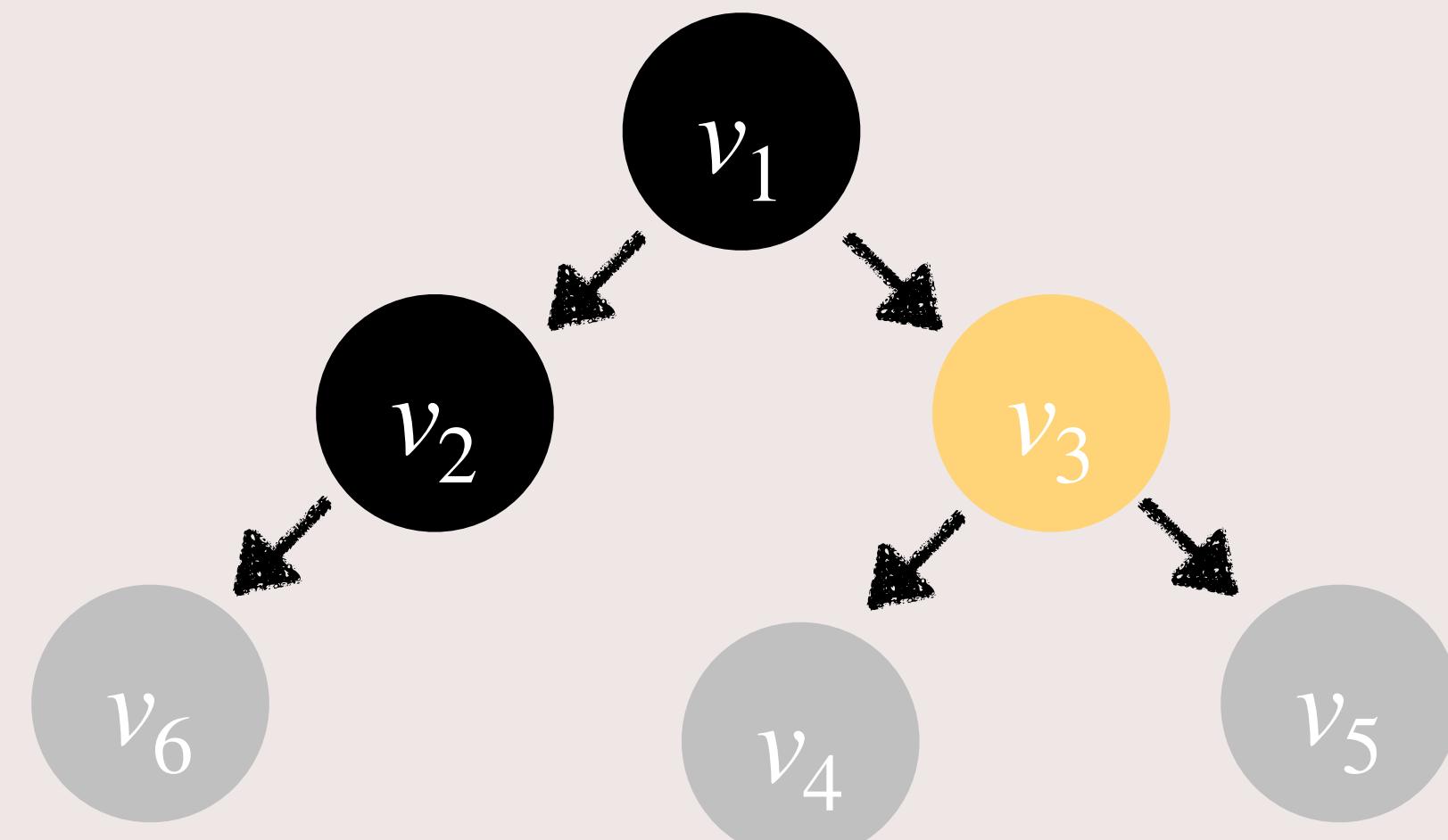


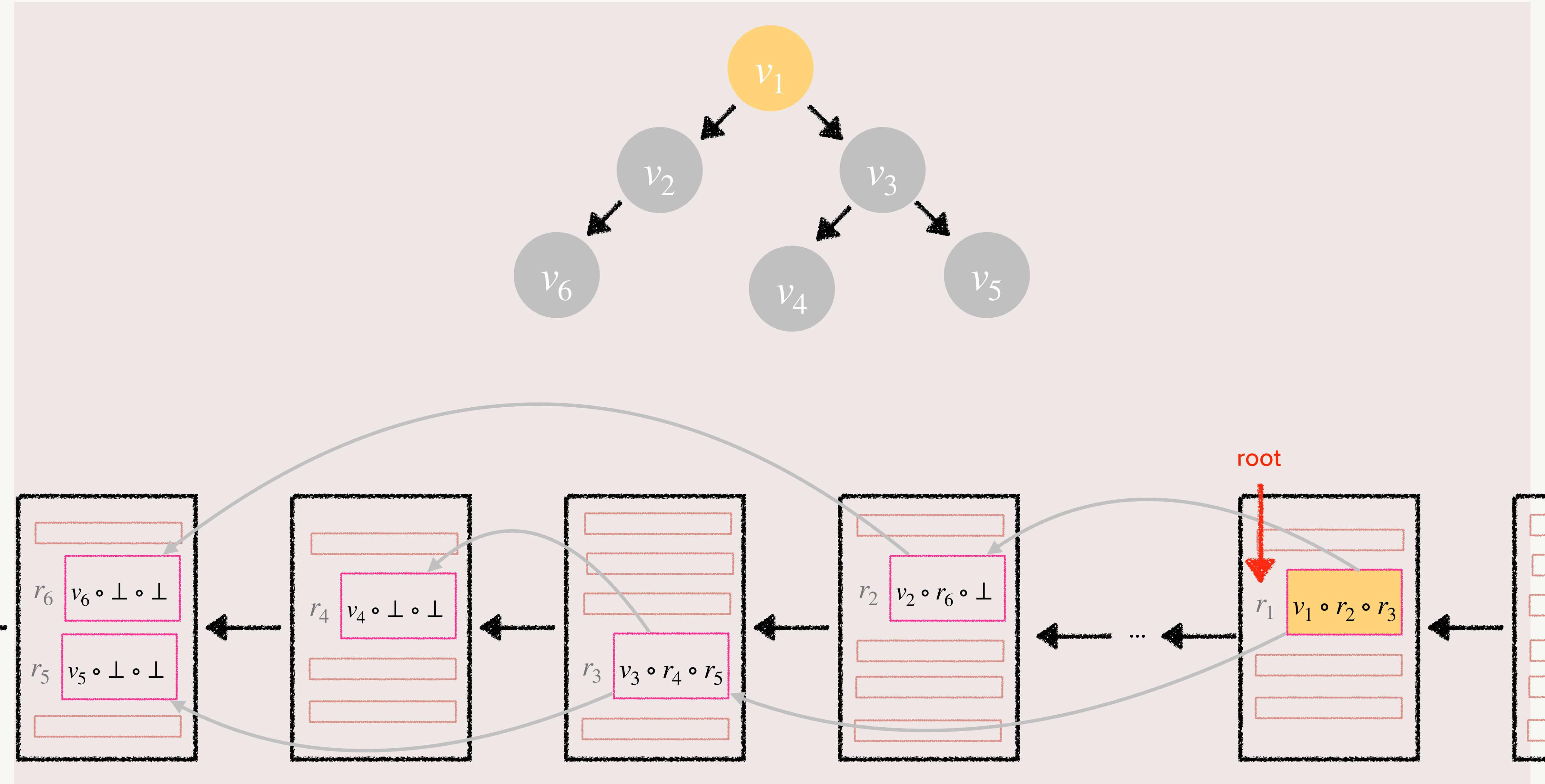
# Storing data structures on BCs

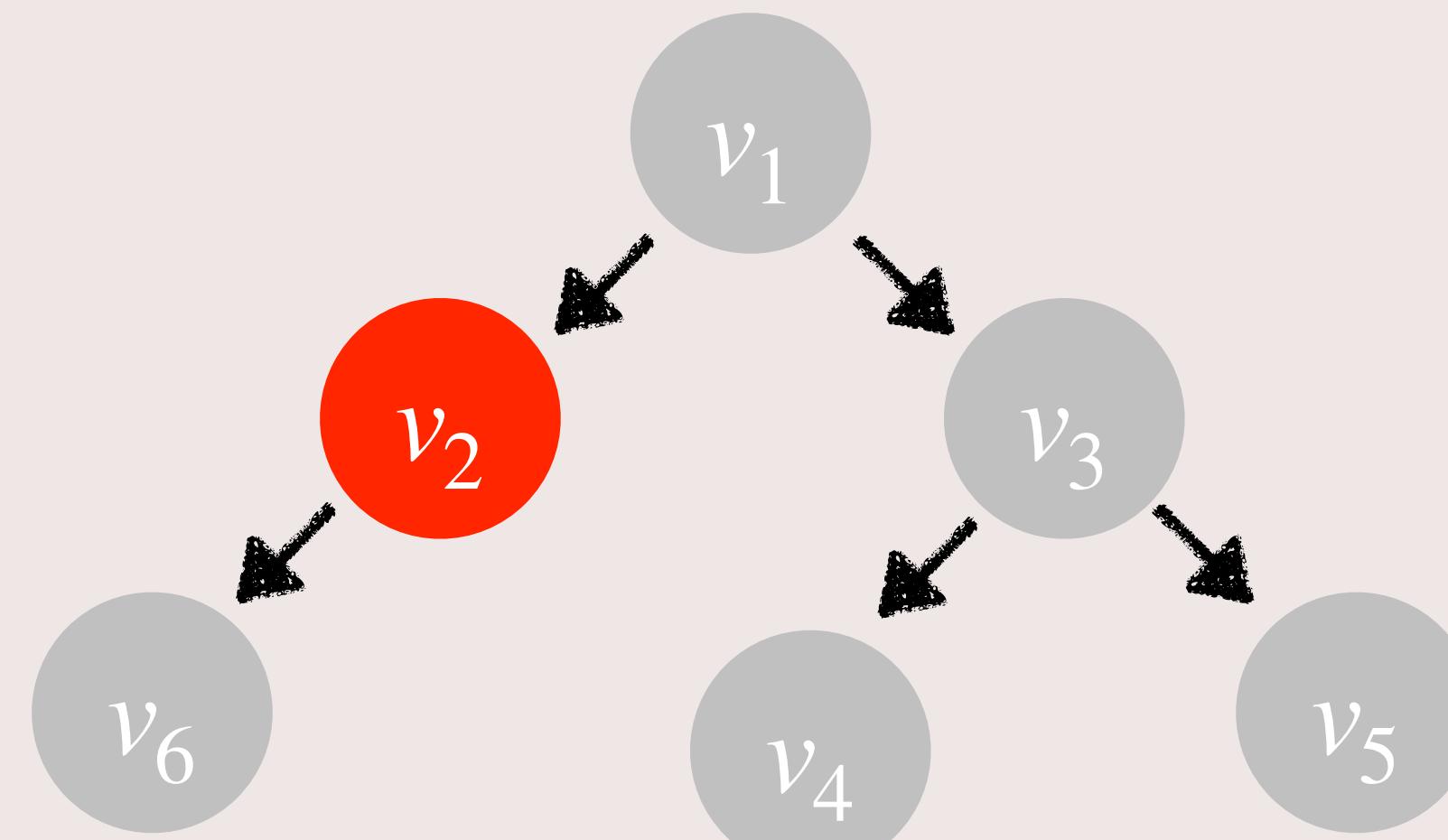




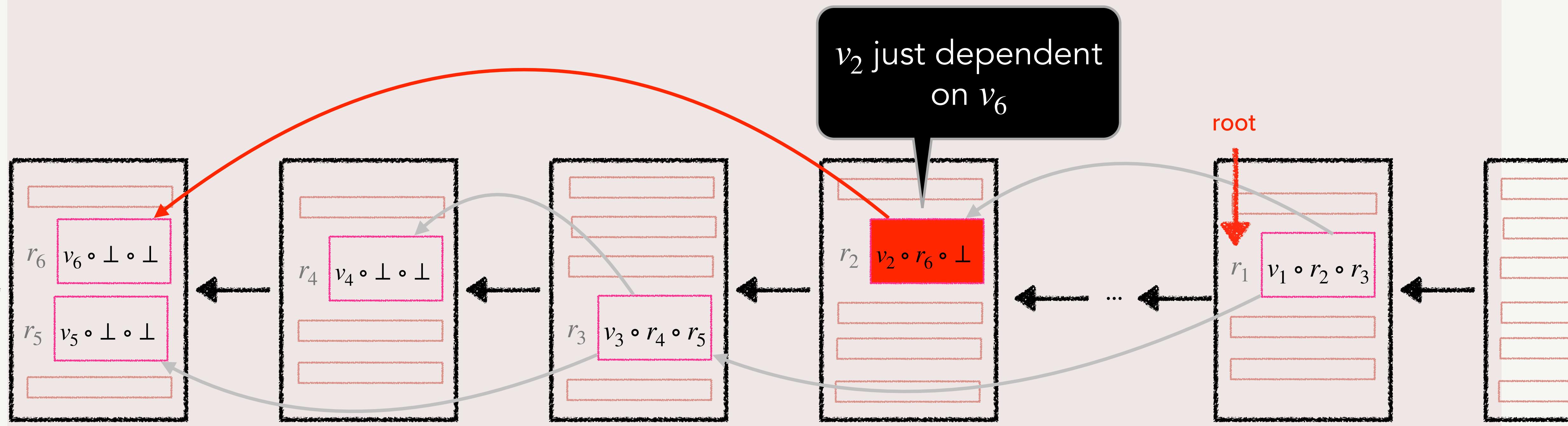




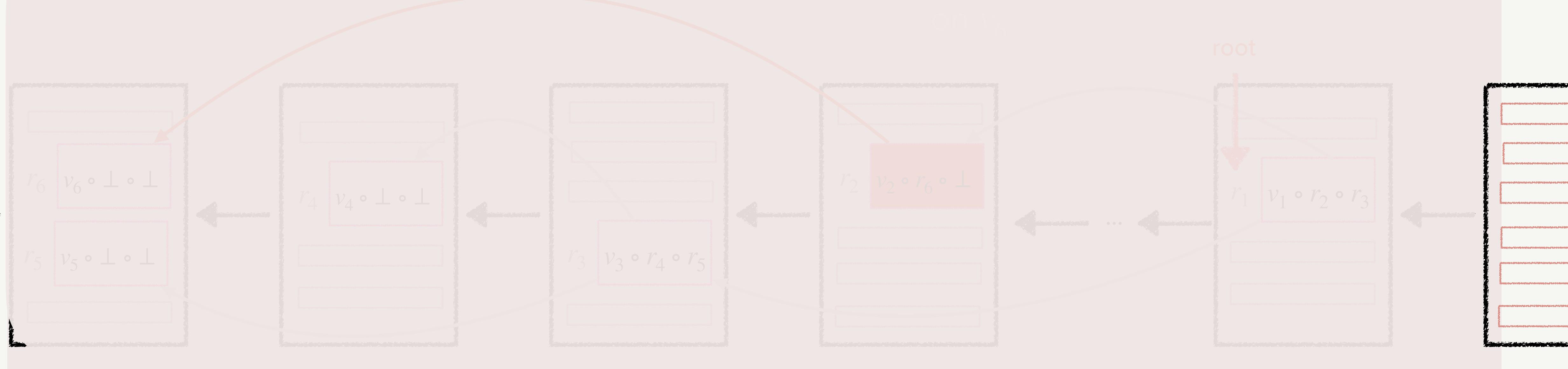
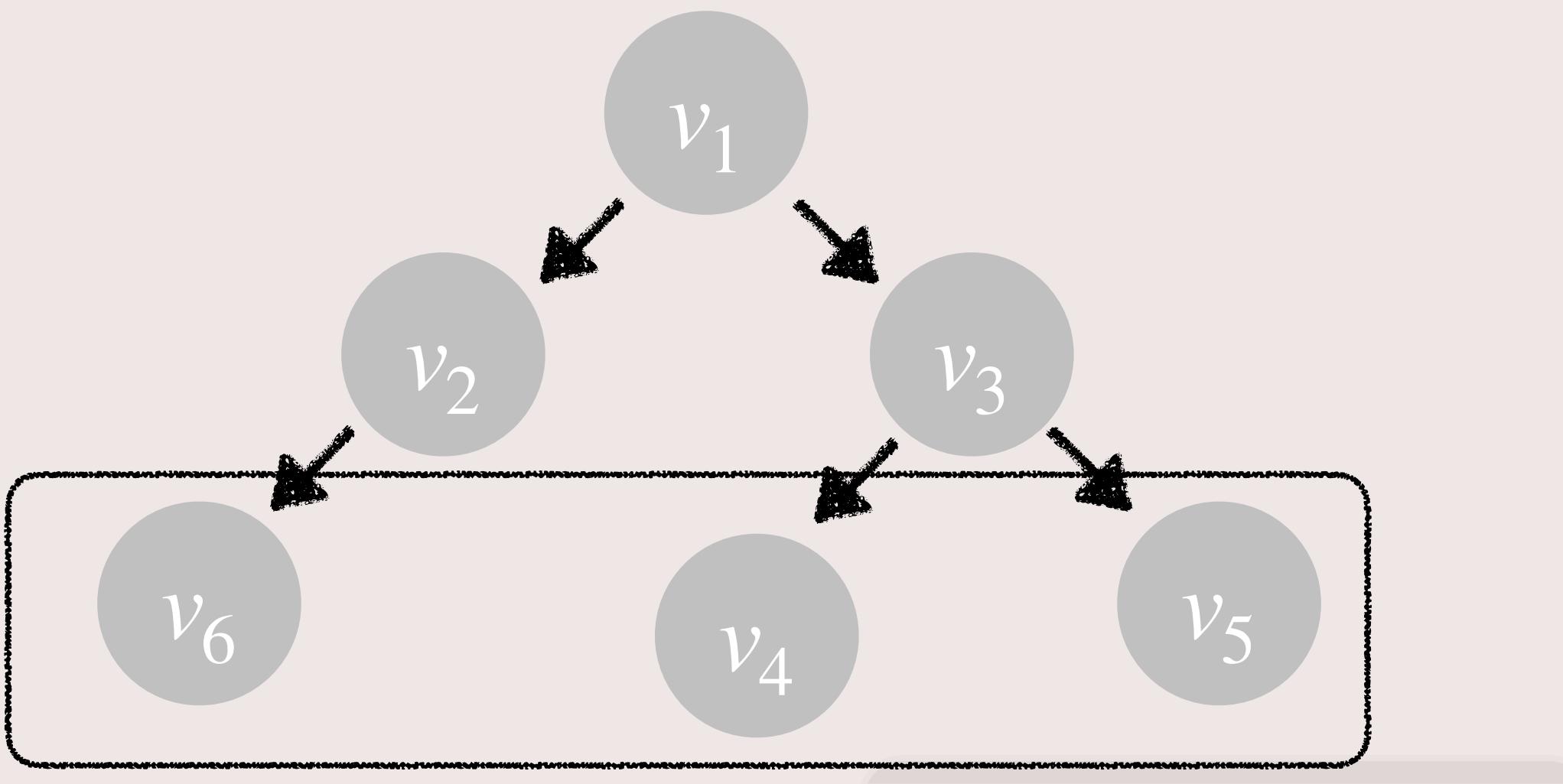


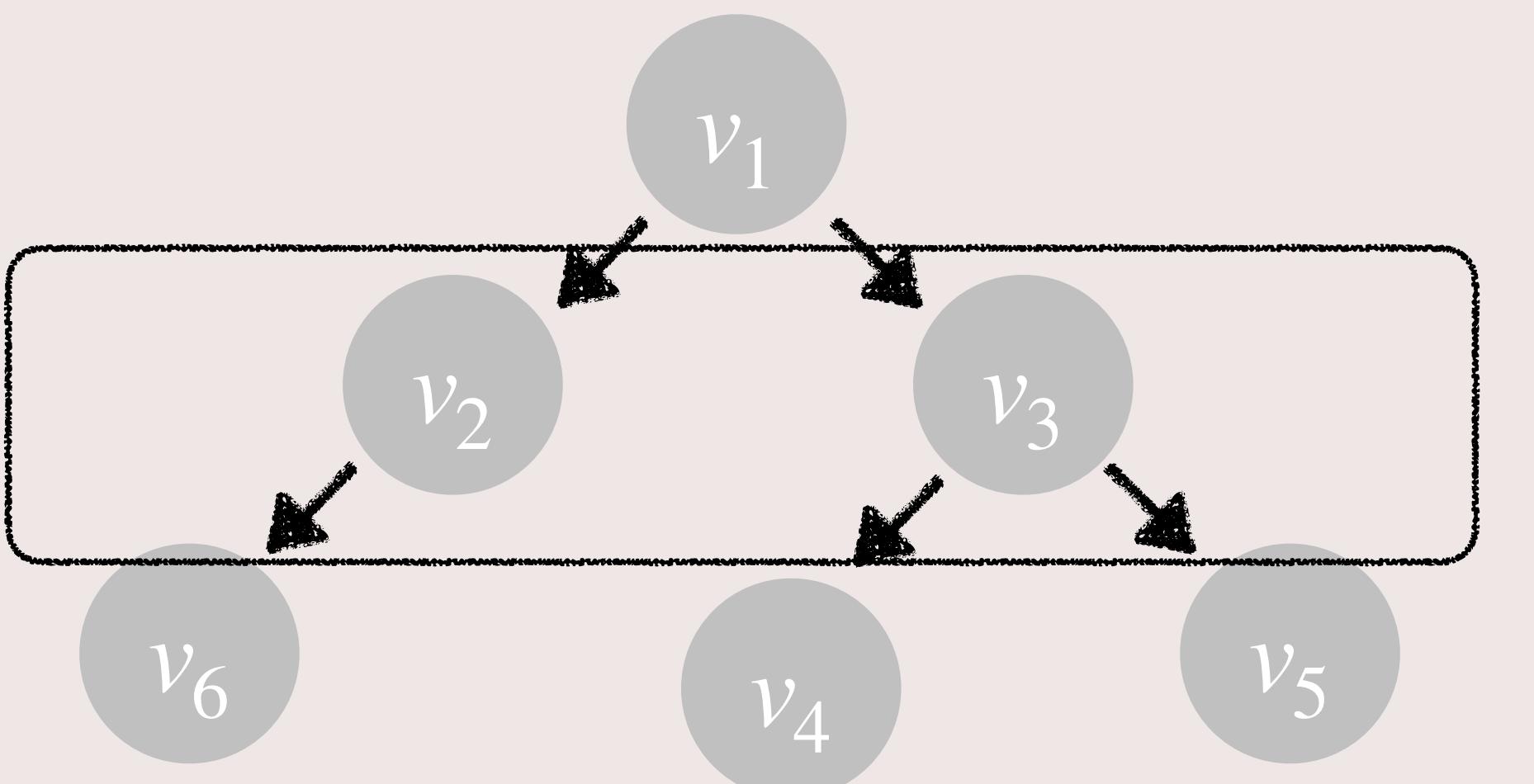


$v_2$  just dependent  
on  $v_6$



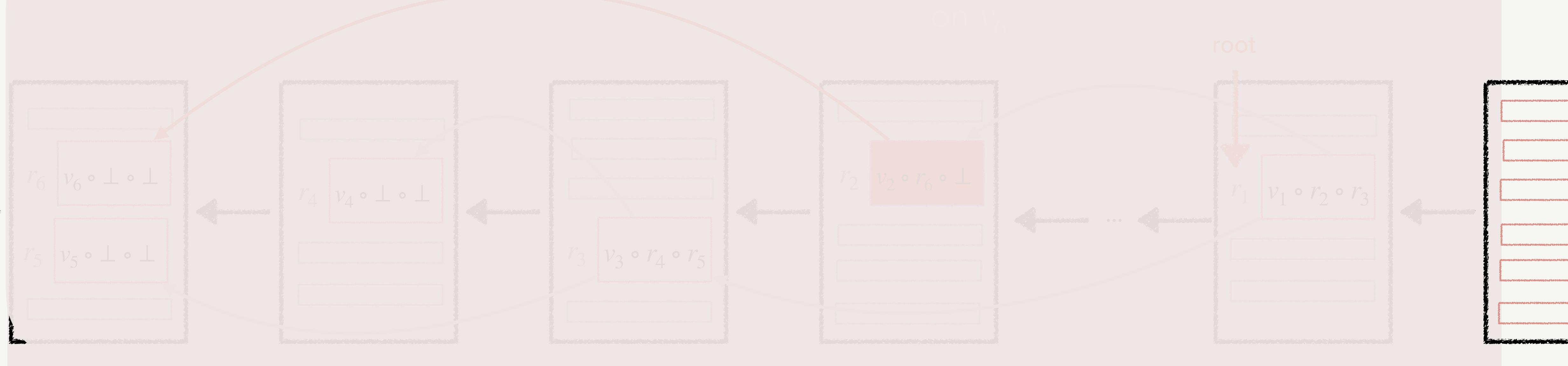
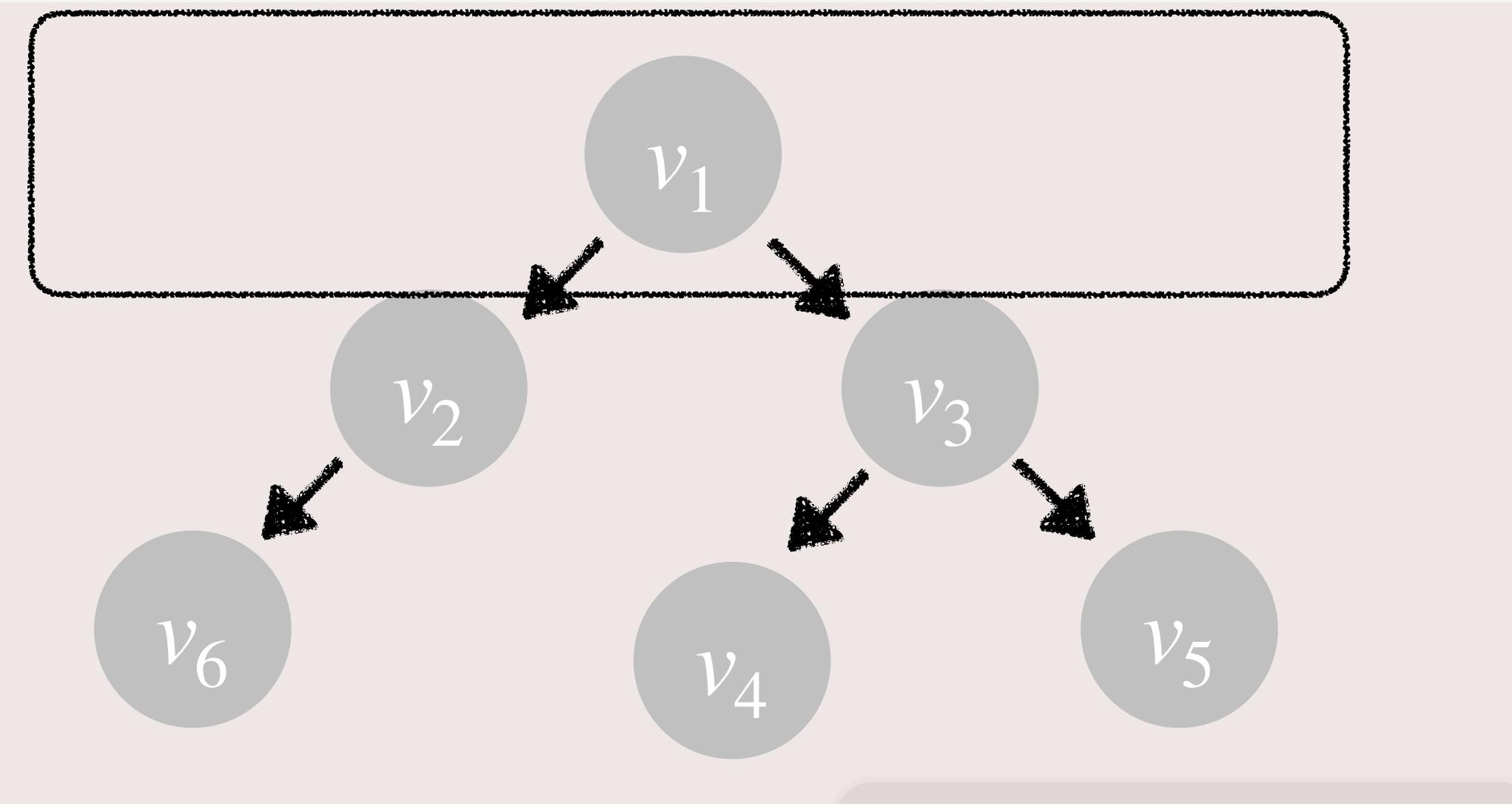
Written in parallel



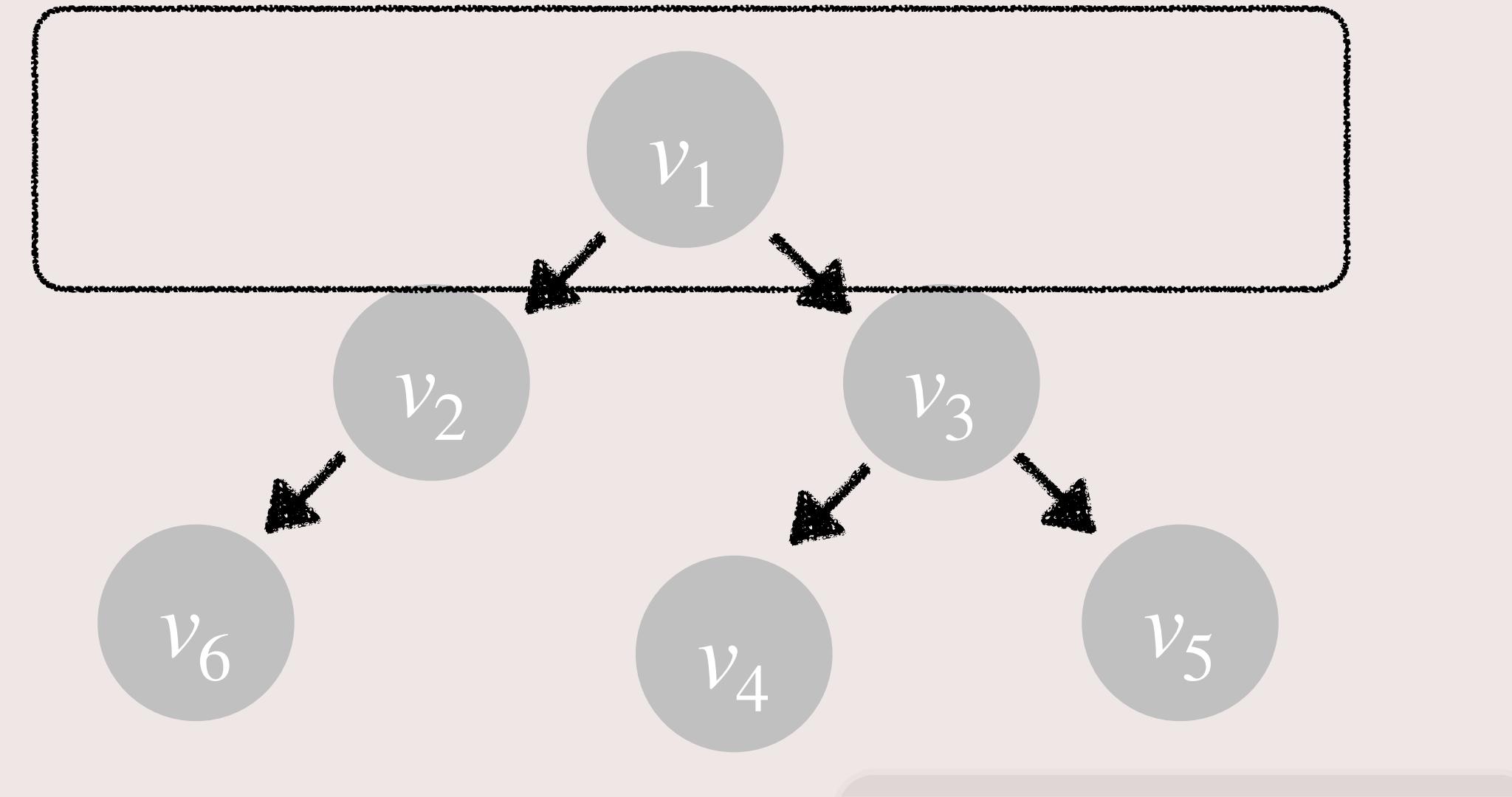


# Written in parallel

Written in parallel



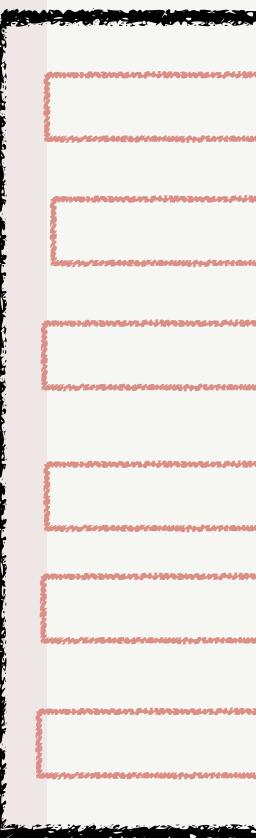
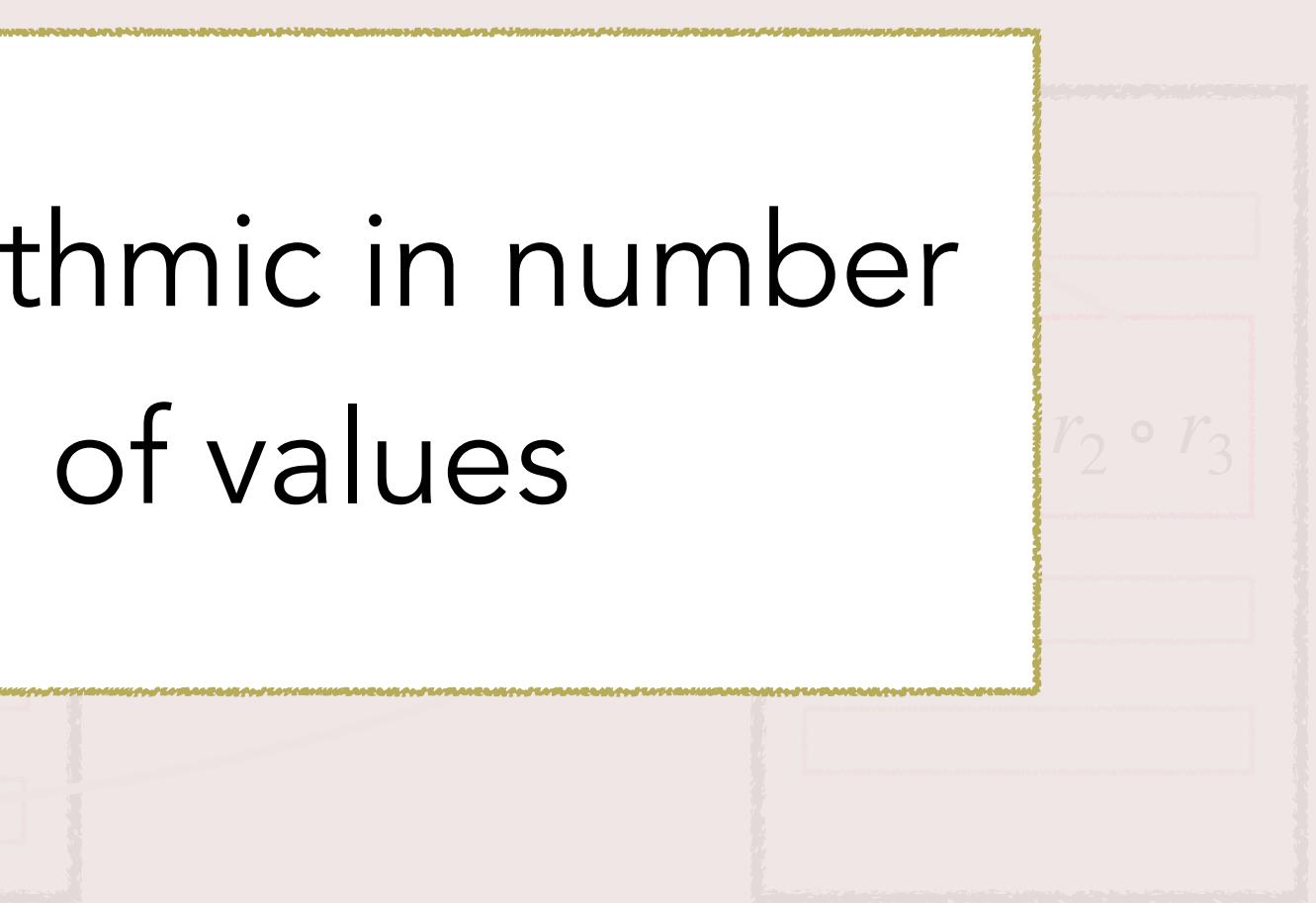
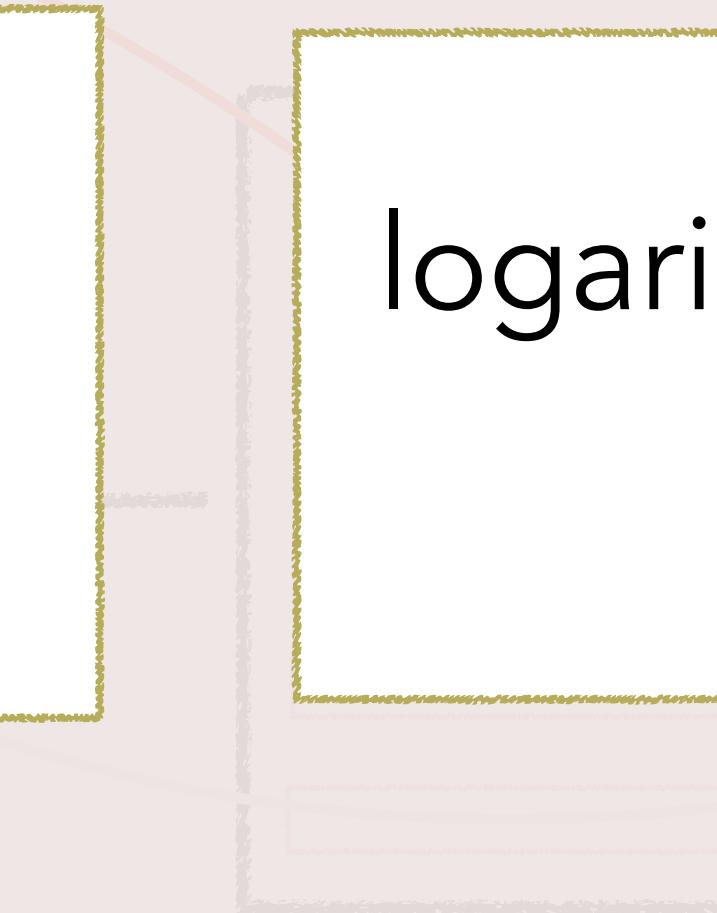
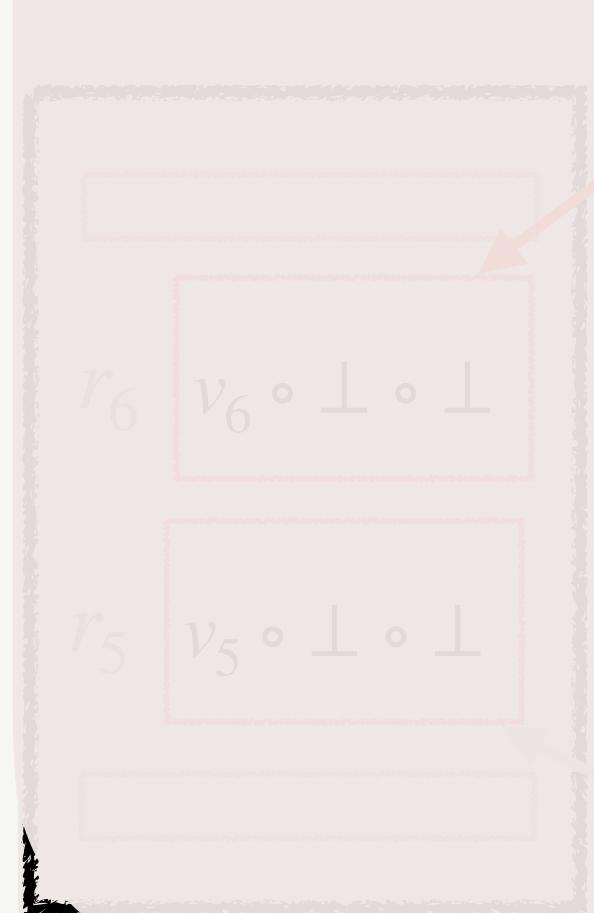
Written in parallel



Stabilization  
Complexity

logarithmic in number  
of values

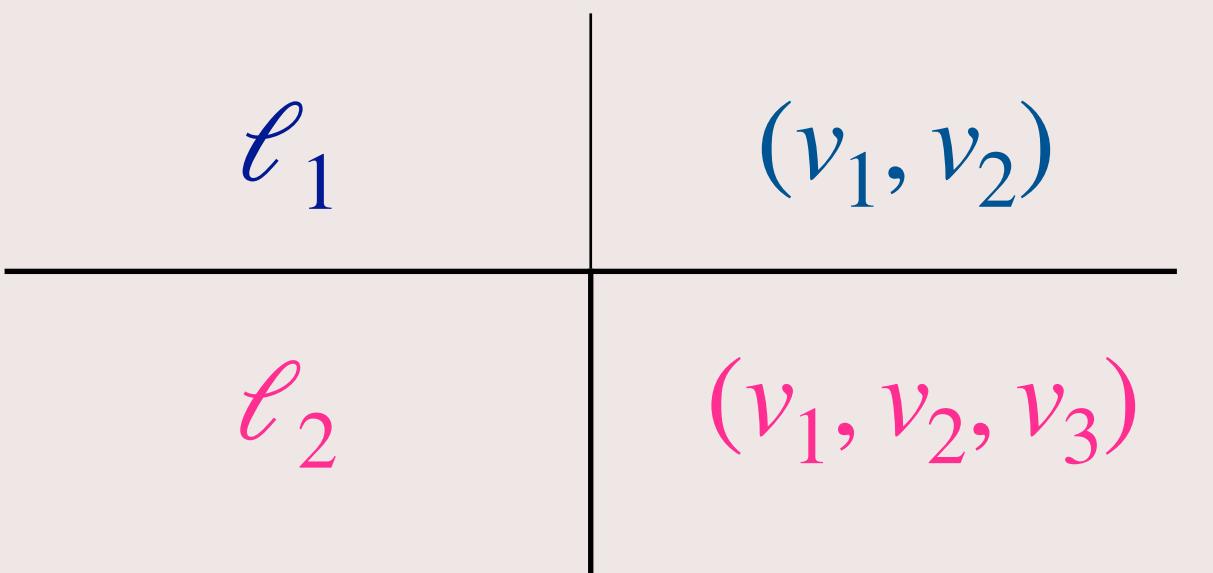
root



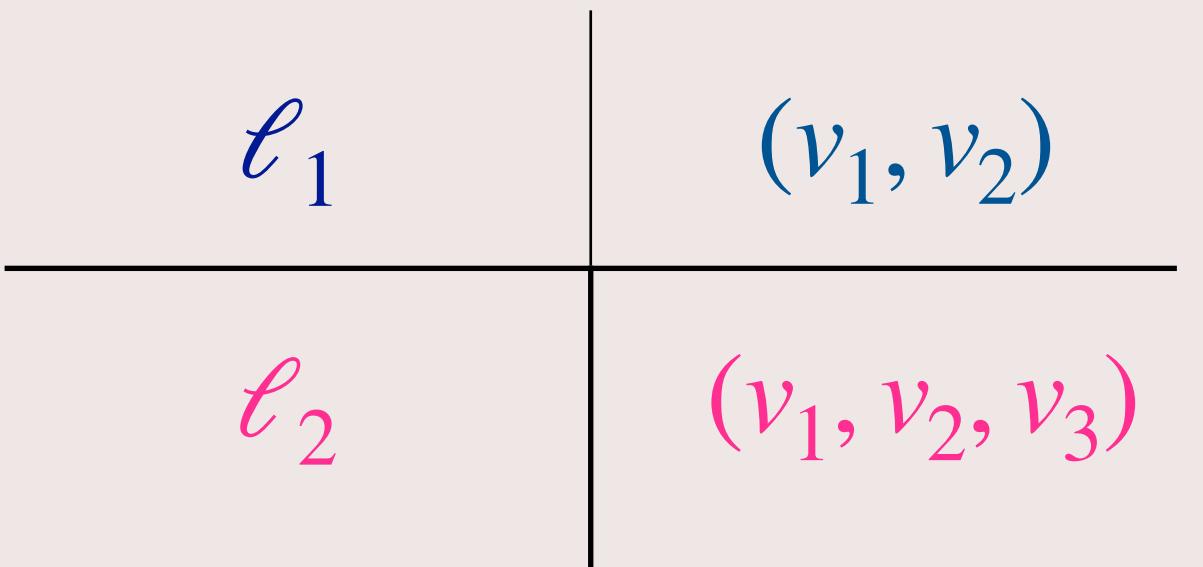
- What are Multi-Maps (MMs)
- What are Encrypted Multi-Maps (EMMs)
- **How to store EMMs on Blockchains**
- LSX
- TRX
- PAX
- Real World Deployment

# LSX

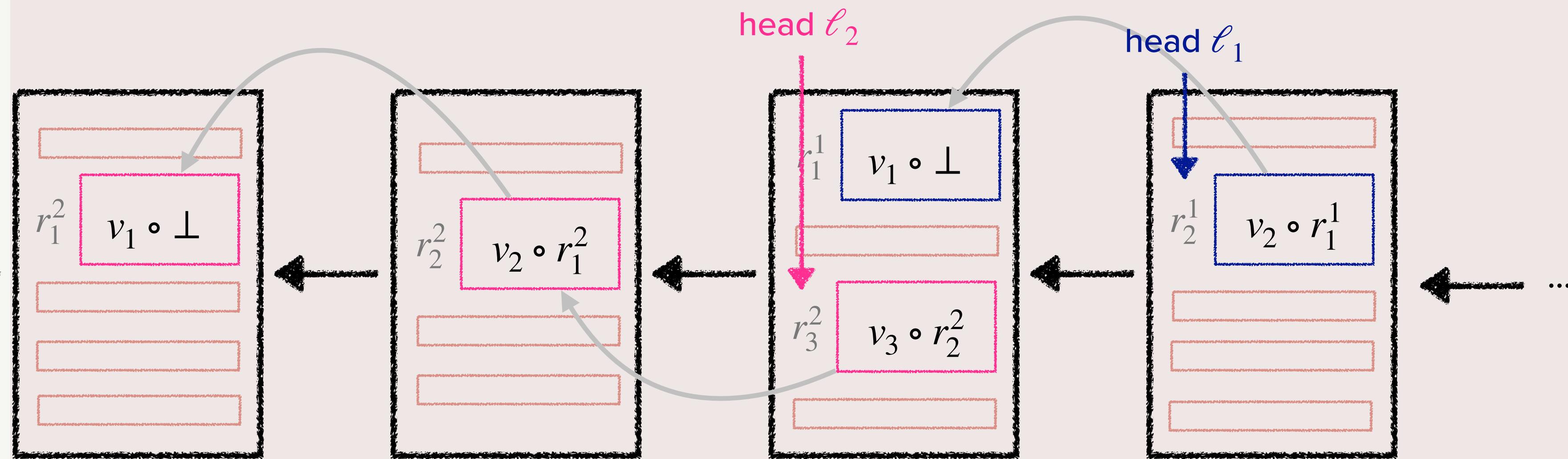
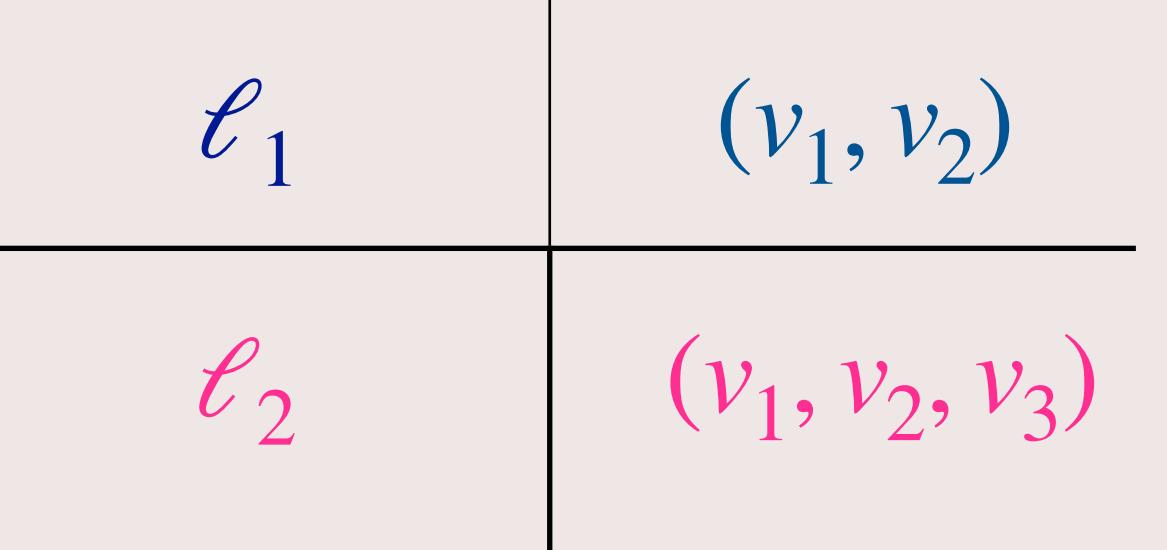
**A list-based EMM**



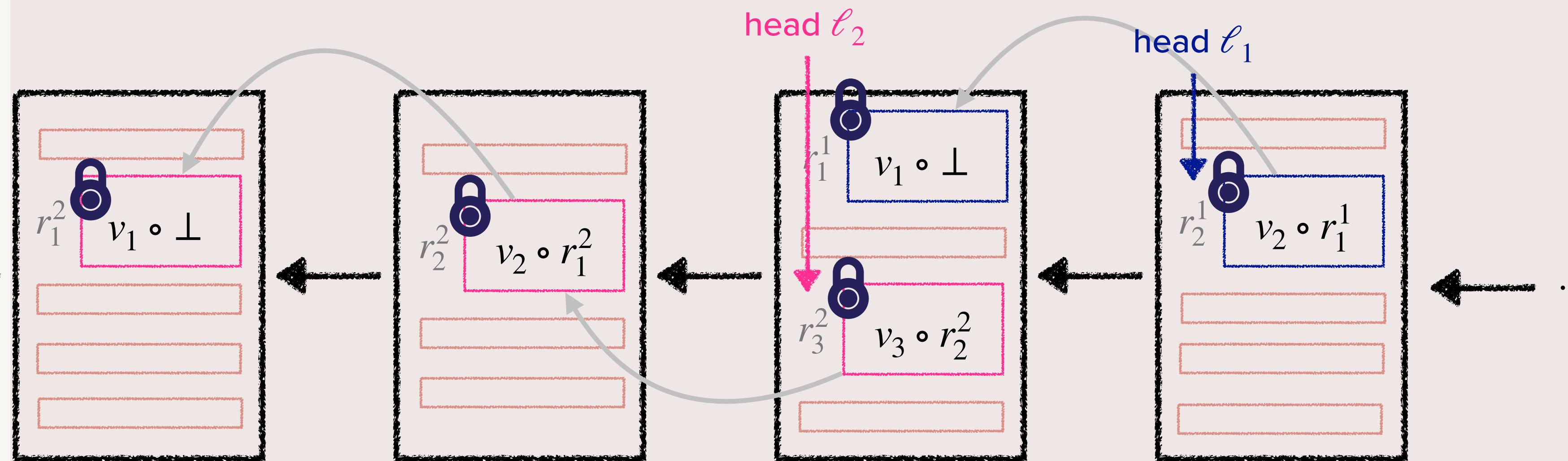
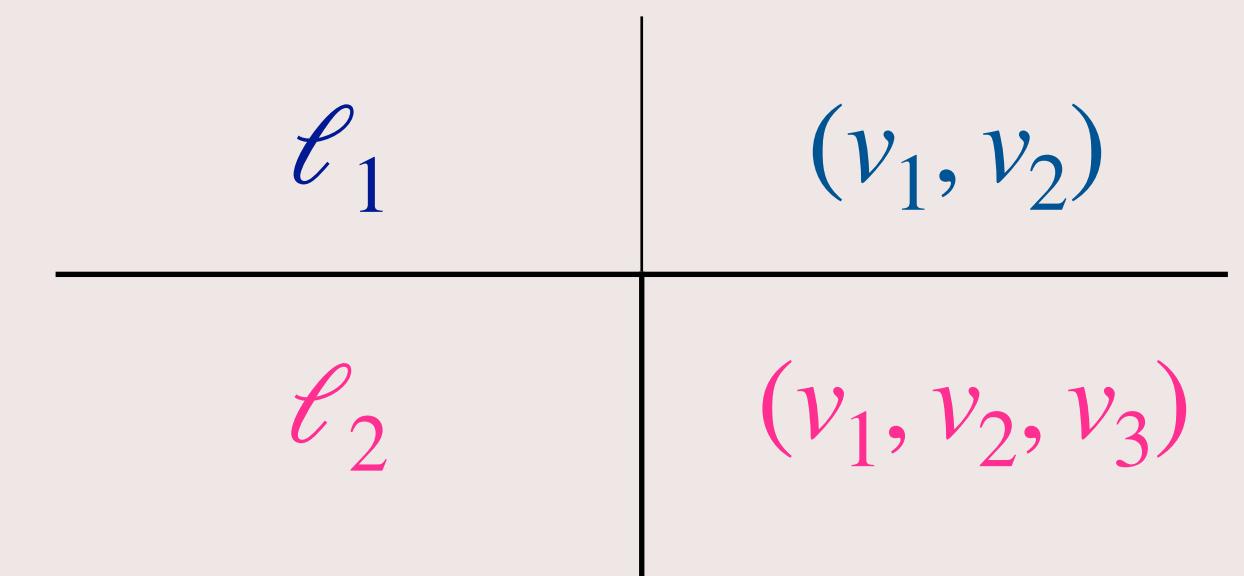
- Represent each label as separate list on BC



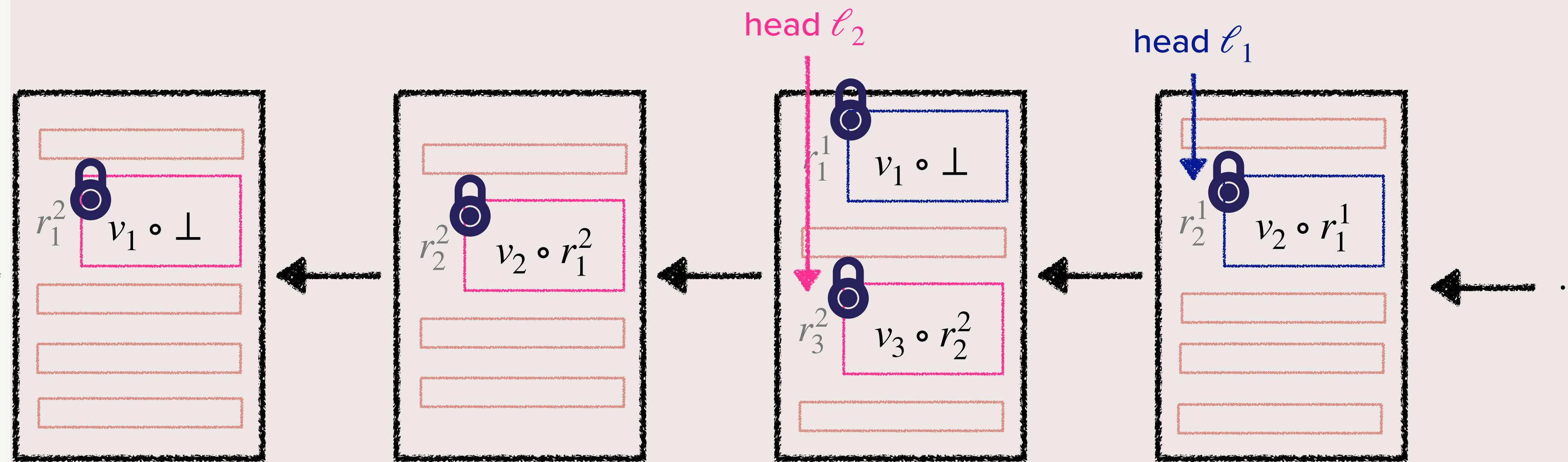
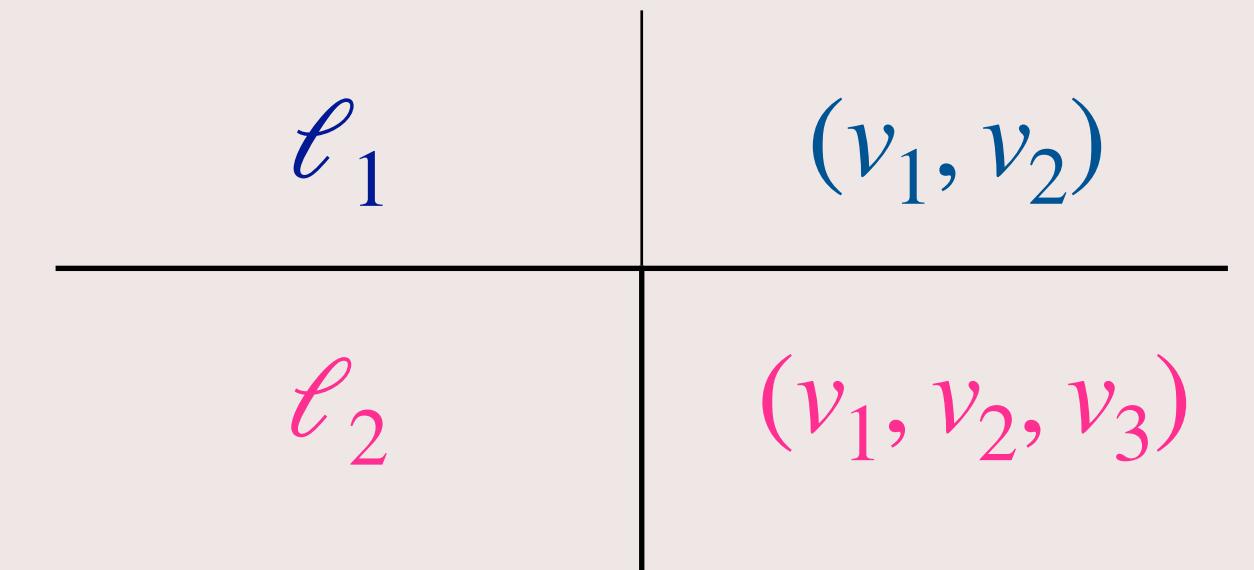
- Represent each label as separate list on BC



- Represent each label as separate list on BC
- Encrypt each value before storing on BC



- Represent each label as separate list on BC
- Encrypt each value before storing on BC

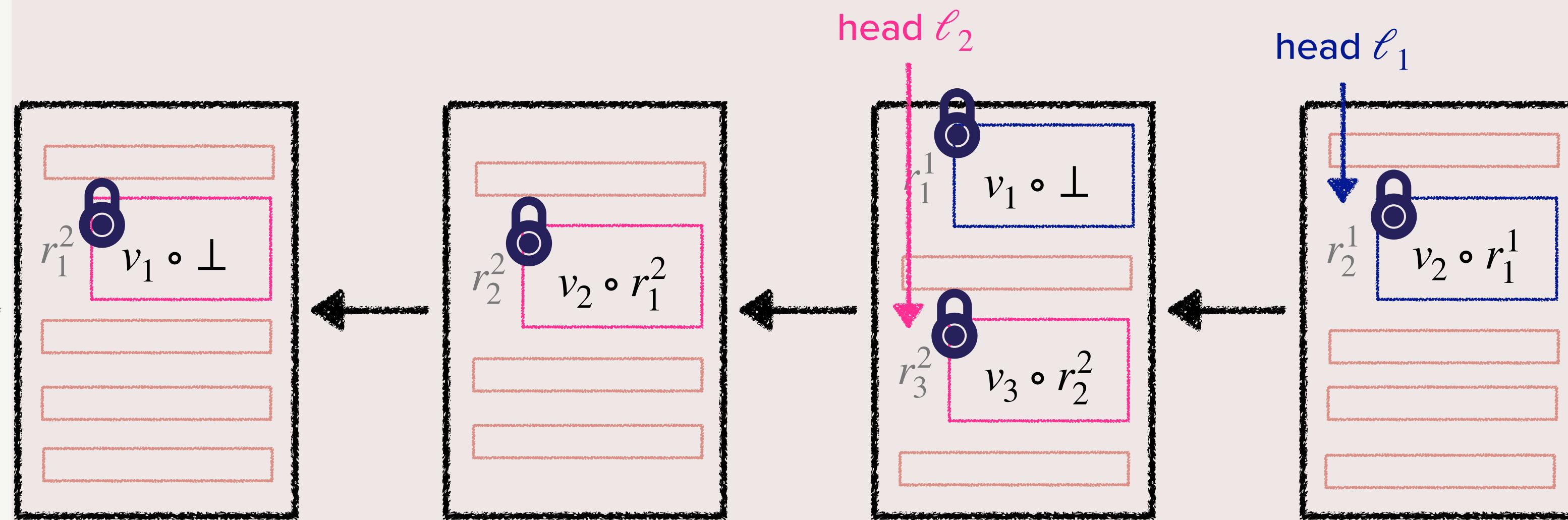


# LSX

Add( $\ell_2, v_4$ )

Delete( $\ell_1, v_1$ )

Query( $\ell_1$ )



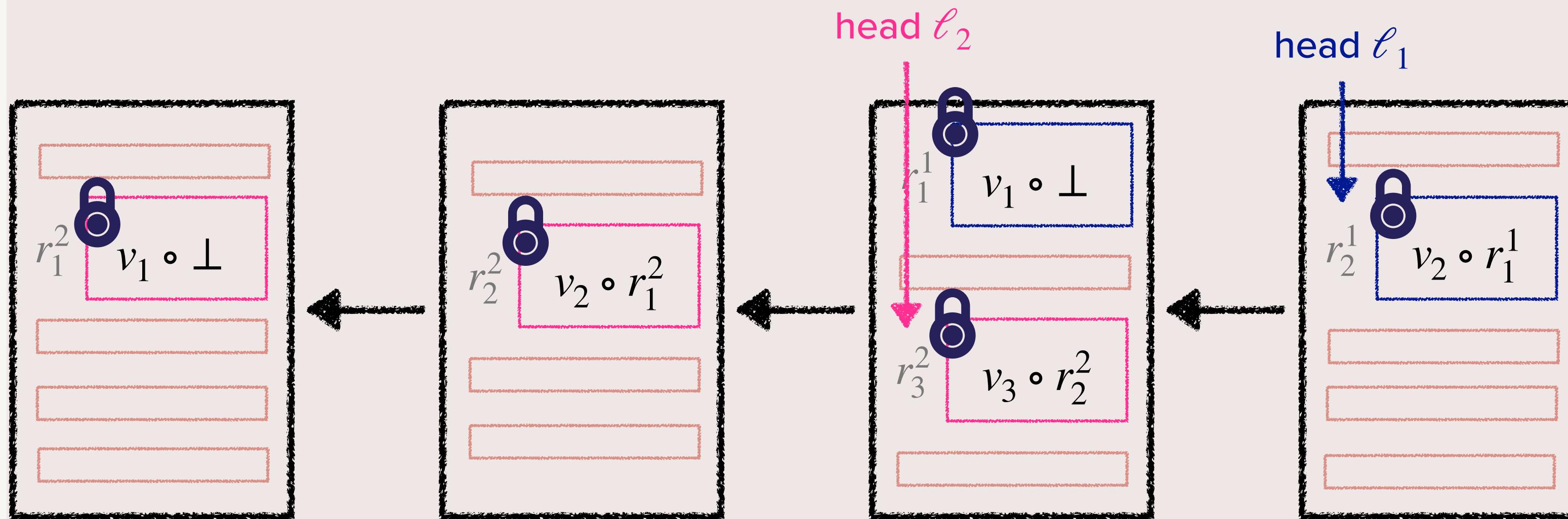
# LSX

Add( $\ell_2, v_4$ )

- Append Enc( $v_4, r_3^2$ ) at head of  $\ell_2$
- Update the head

Delete( $\ell_1, v_1$ )

Query( $\ell_1$ )



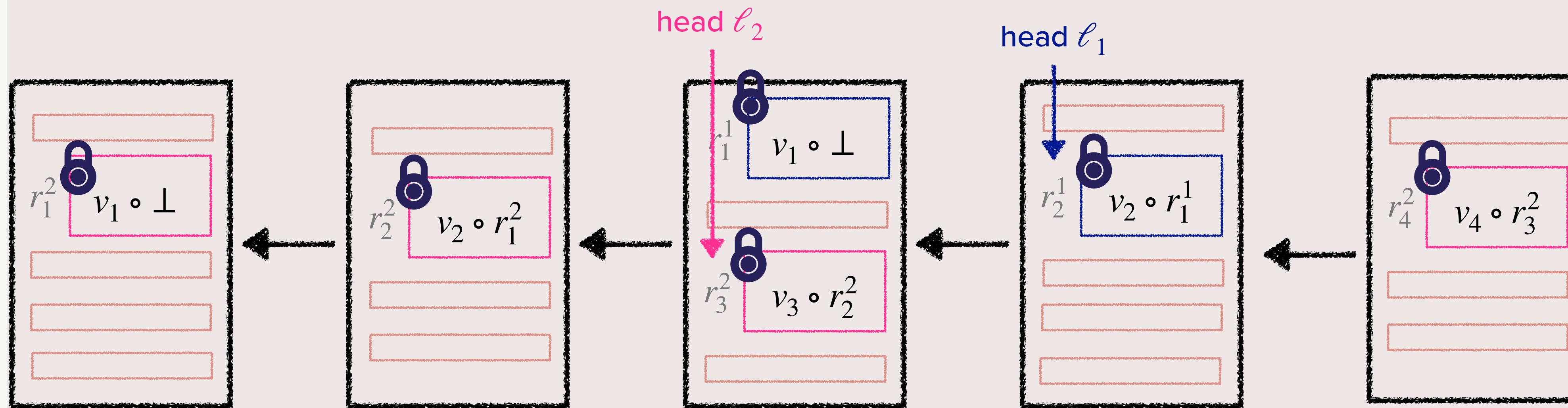
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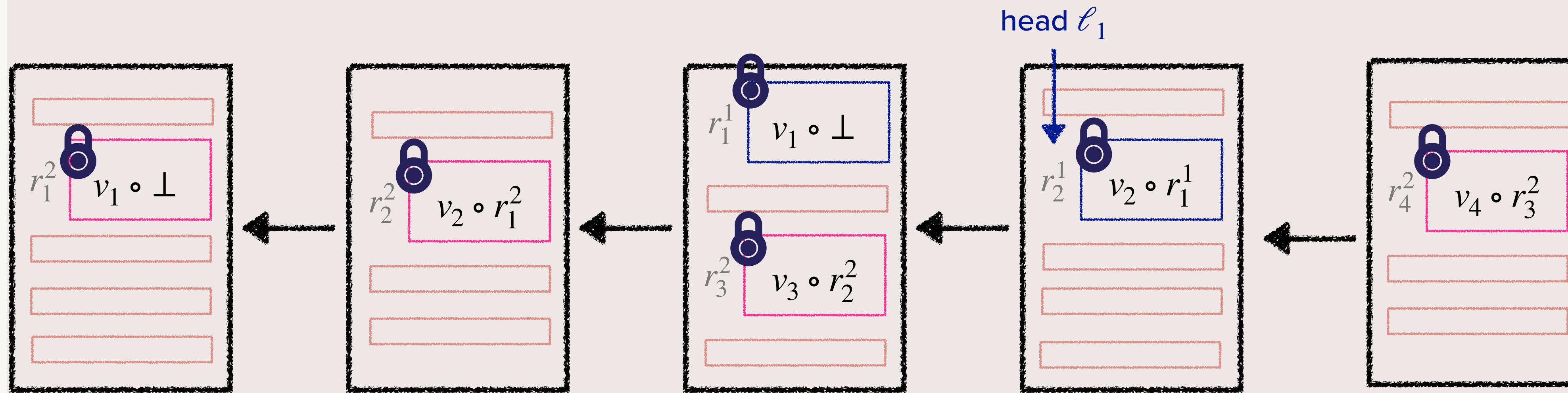
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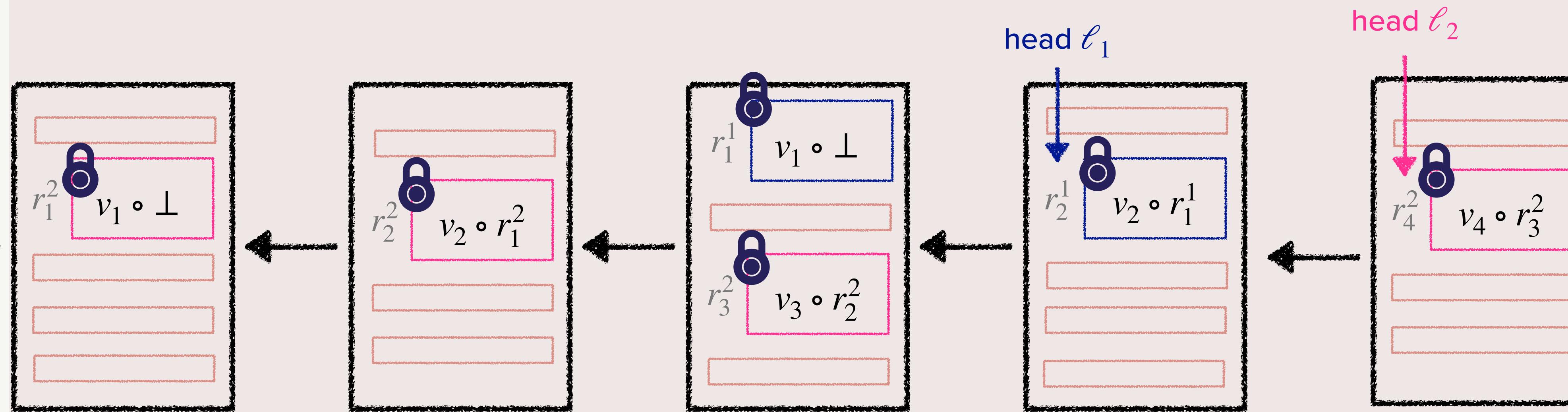
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# LSX

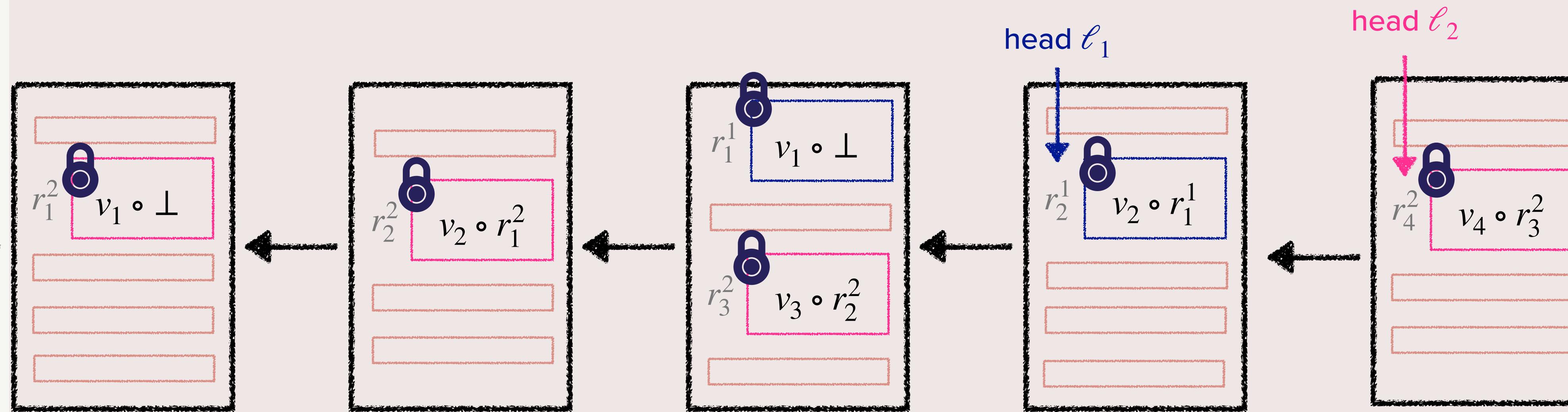
Add( $\ell_2, v_4$ )

- Append Enc( $v_4, r_3^2$ ) at head of  $\ell_2$
- Update the head

Delete( $\ell_1, v_1$ )

- Same as Add
- Append a DEL flag to the value

Query( $\ell_1$ )



# LSX

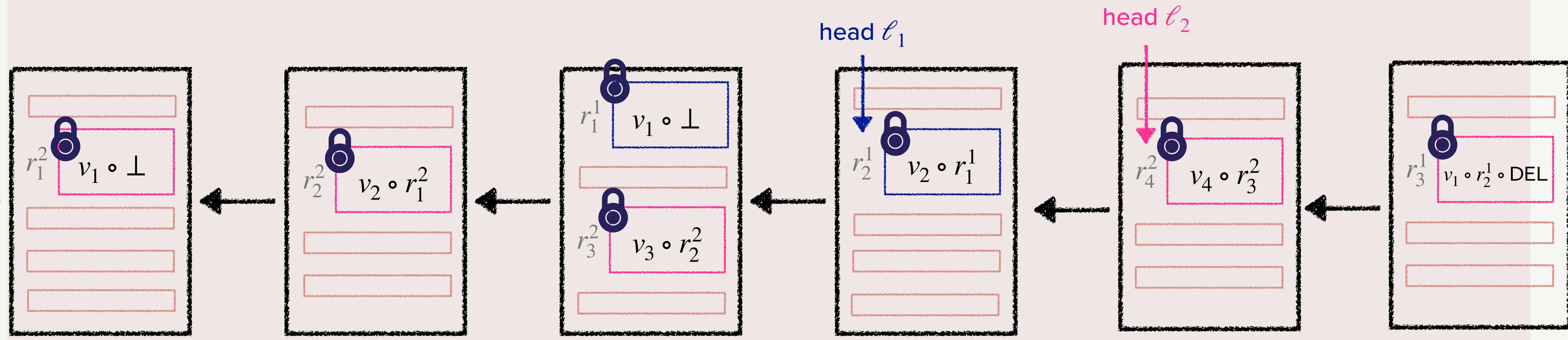
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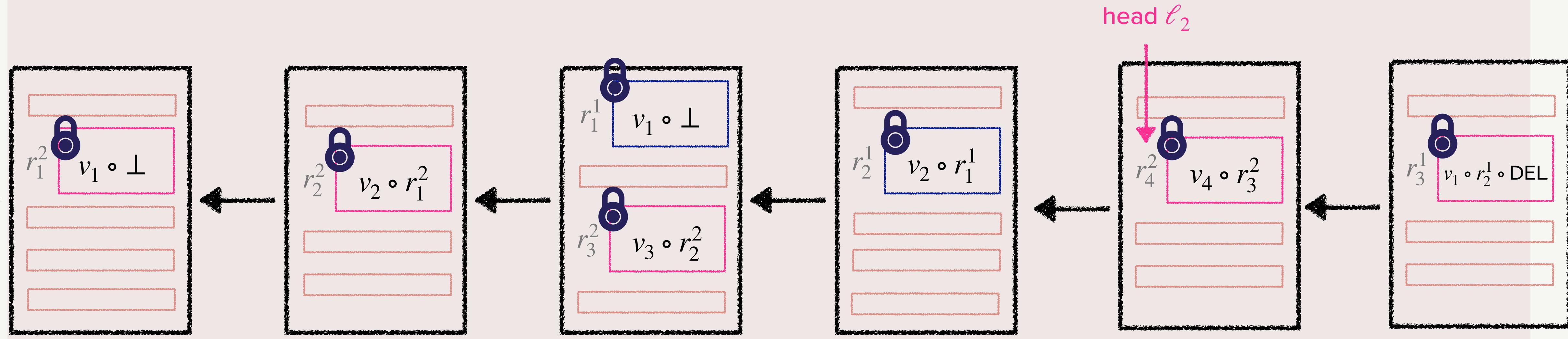
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# LSX

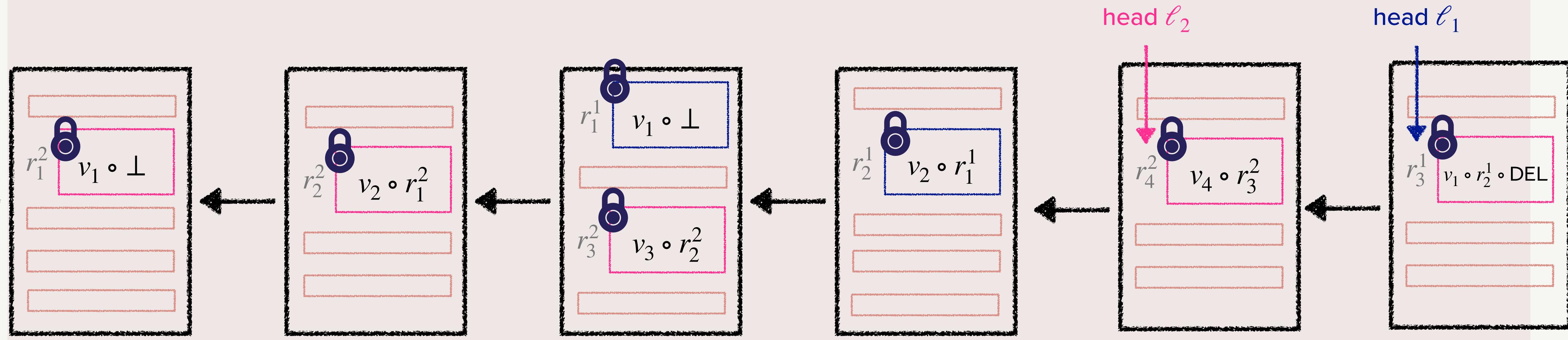
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Query( $\ell_1$ )



# LSX

Add( $\ell_2, v_4$ )

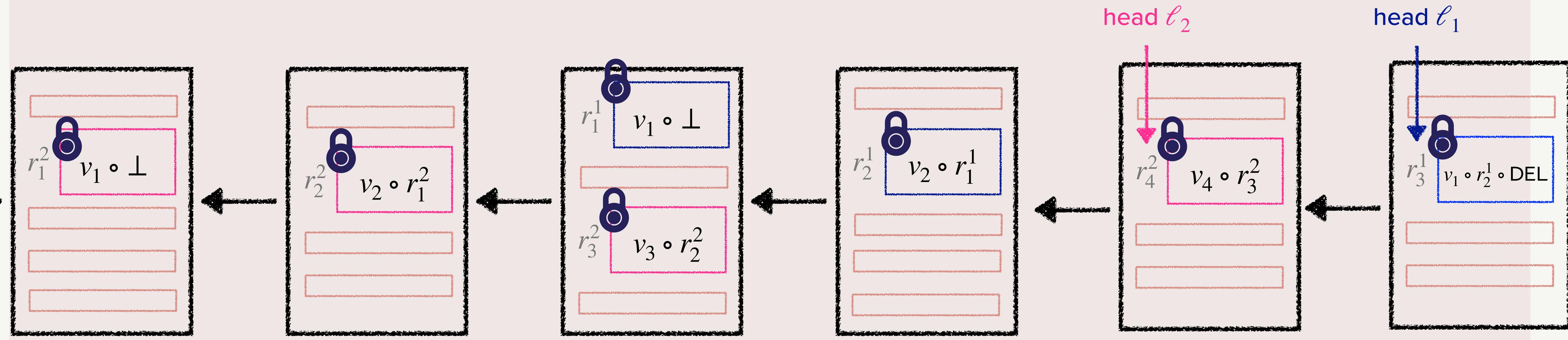
- Append Enc( $v_4, r_3^2$ ) at head of  $\ell_2$
- Update the head

Delete( $\ell_1, v_1$ )

- Same as Add
- Append a DEL flag to the value

Query( $\ell_1$ )

- Read all values from the list
- Output un-deleted values



# LSX

Add( $\ell_2, v_4$ )

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$
- Update the head

time

Optimal:  $O(|t|)$

Delete( $\ell_1, v_1$ )

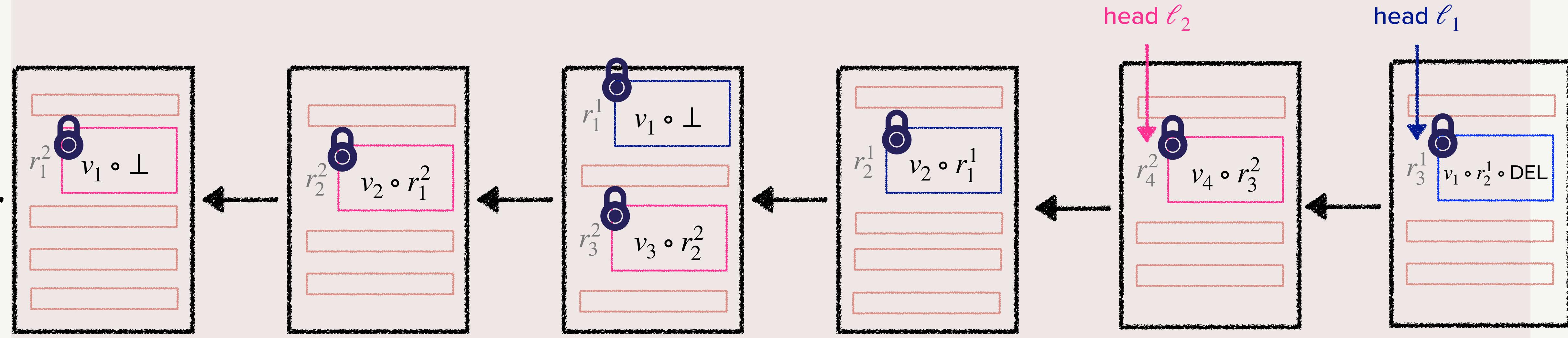
- Same as Add
- Append a DEL flag to the value

time

Optimal:  $O(|t|)$

Query( $\ell_1$ )

- Read all values from the list
- Output un-deleted values



# LSX

Add( $\ell_2, v_4$ )

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$
- Update the head

Optimal:  $O(|t|)$

Delete( $\ell_1, v_1$ )

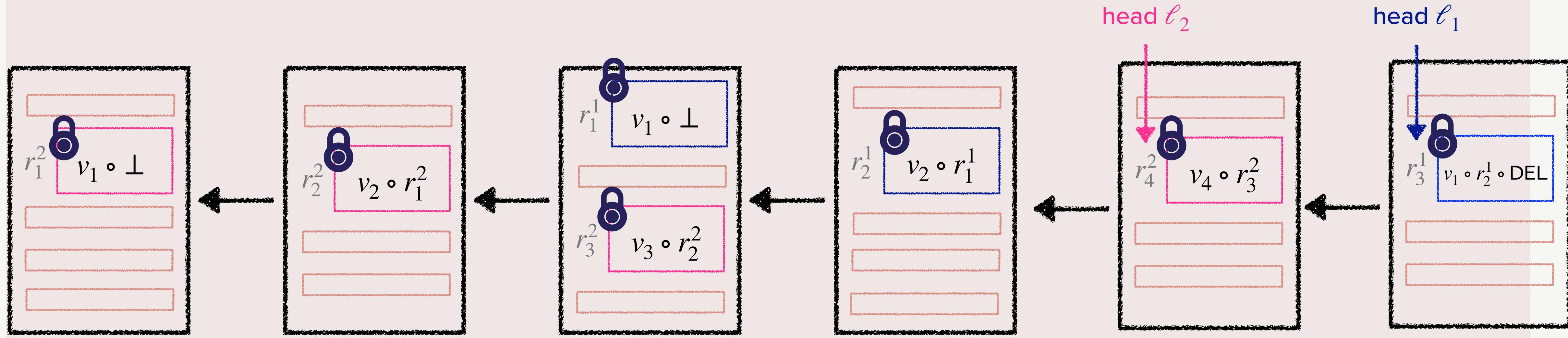
- Same as Add
- Append a DEL flag to the value

Optimal:  $O(|t|)$

Query( $\ell_1$ )

- Read all values from the list
- Output un-deleted values

# values ever added/  
deleted



# LSX

Add( $\ell_2, v_4$ )

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$
- Update the head

Optimal:  $O(|t|)$

stabilization

$O(|t|)$

Delete( $\ell_1, v_1$ )

- Same as Add
- Append a DEL flag to the value

Optimal:  $O(|t|)$

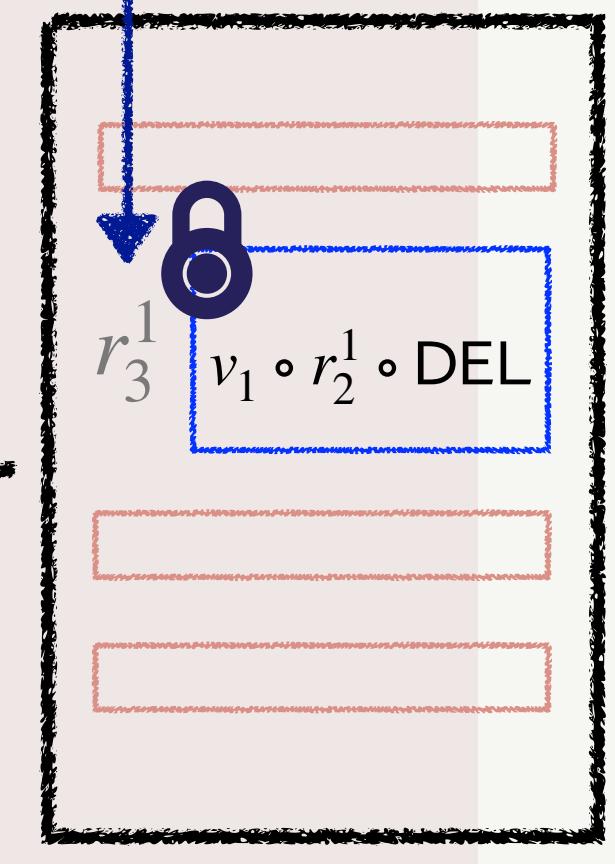
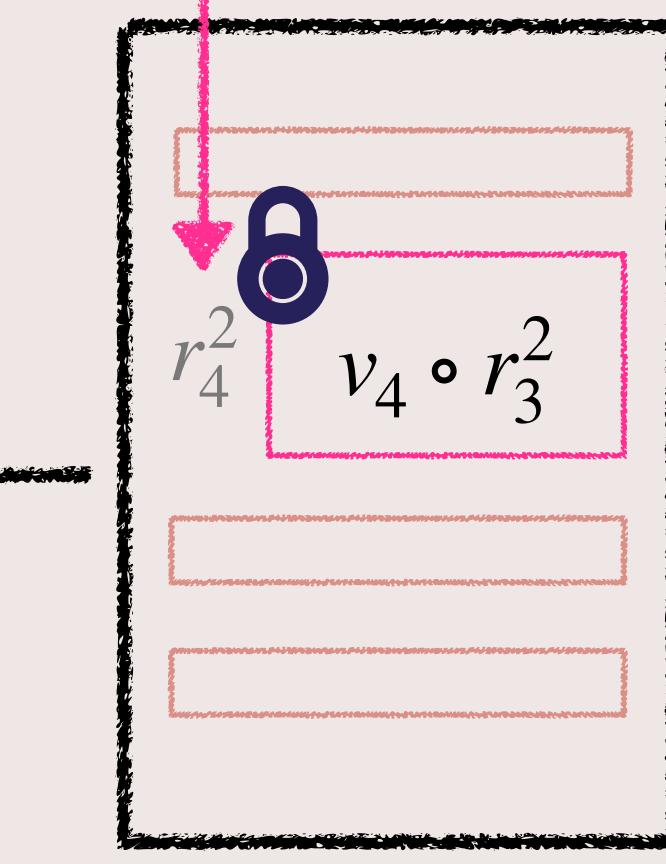
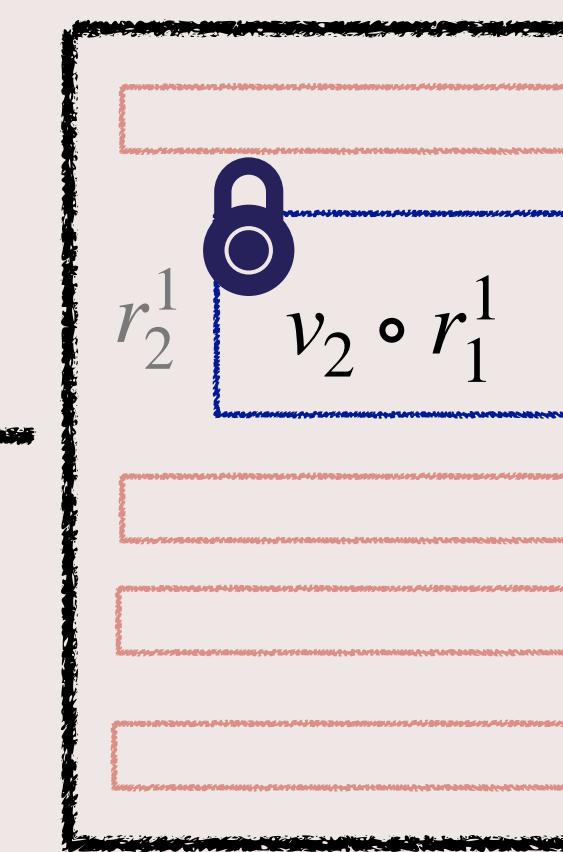
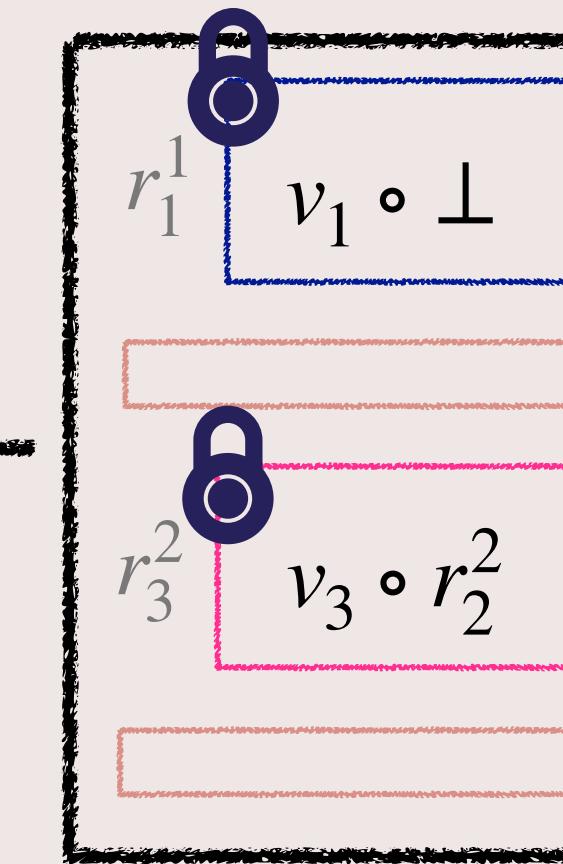
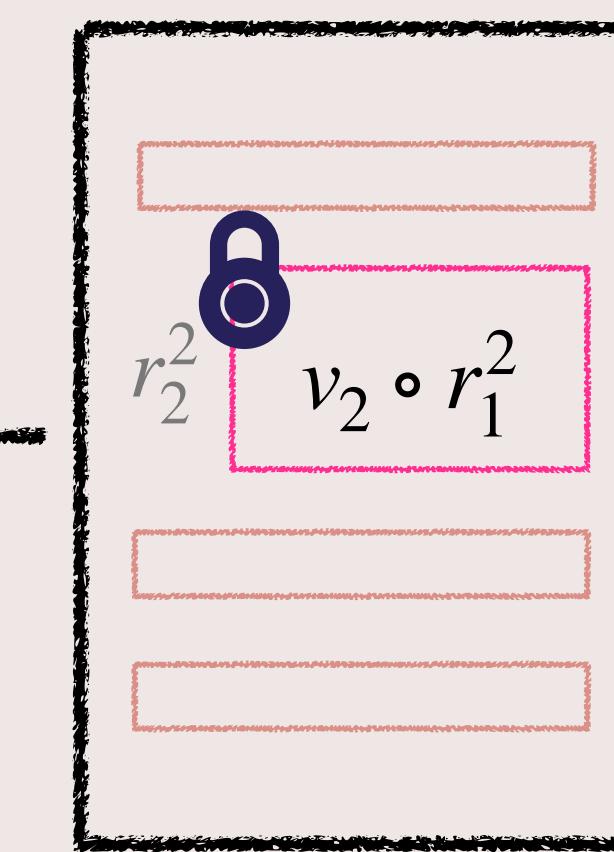
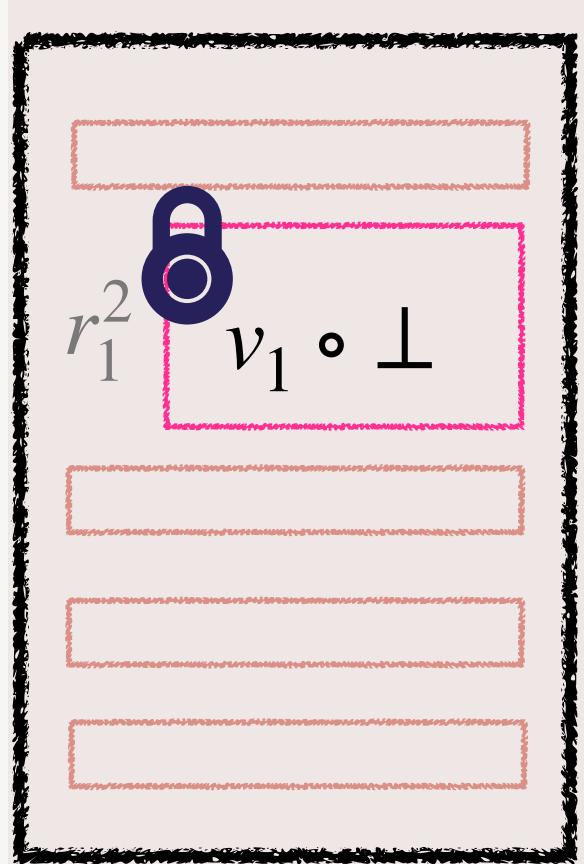
stabilization

$O(|t|)$

Query( $\ell_1$ )

- Read all values from the list
- Output un-deleted values

# values ever added/  
deleted



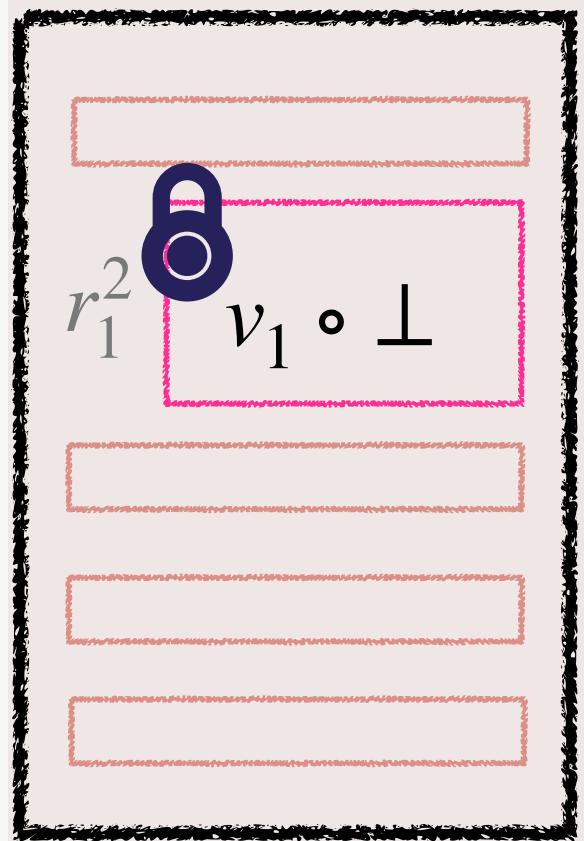
# LSX

Add( $\ell_2, v_4$ )

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$
- Update the head

Optimal:  $O(|t|)$

*stabilization*:  $O(|t|)$

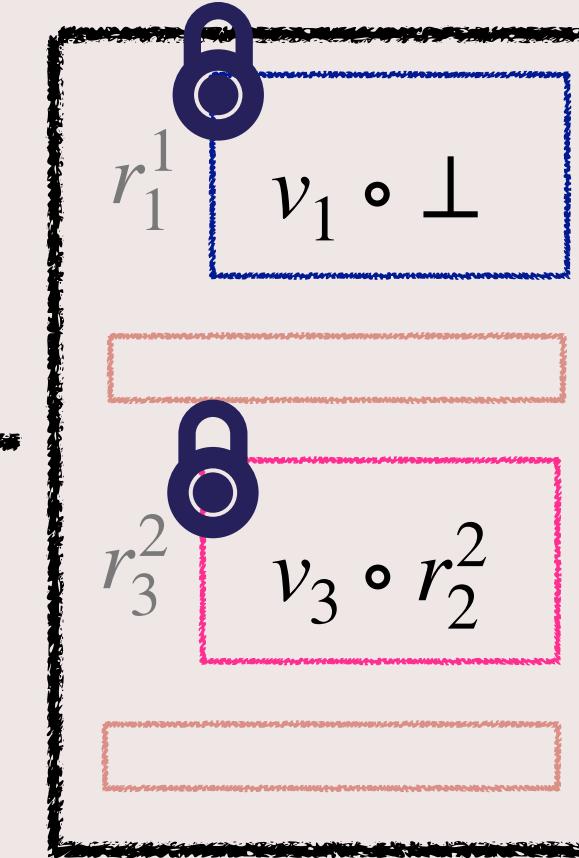


Delete( $\ell_1, v_1$ )

- Same as Add
- Append a DEL flag to the value

Optimal:  $O(|t|)$

*stabilization*:  $O(|t|)$

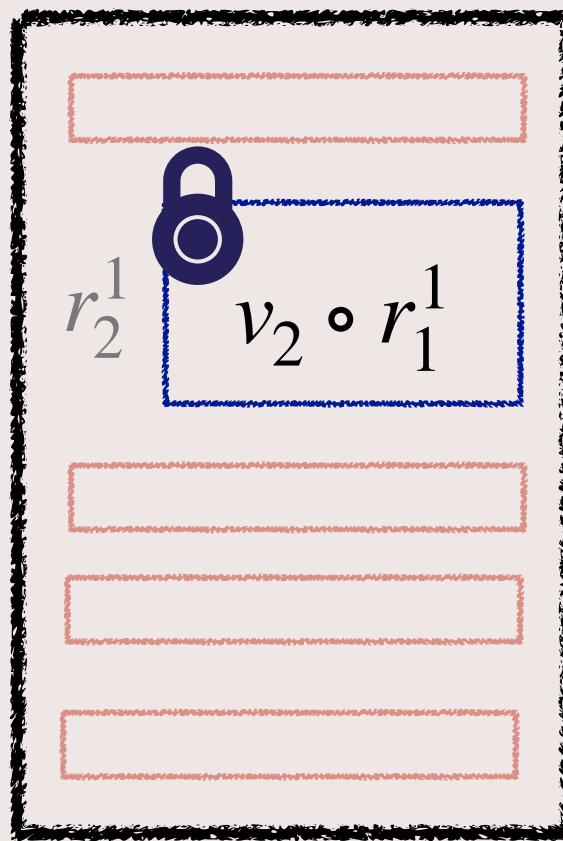


Query( $\ell_1$ )

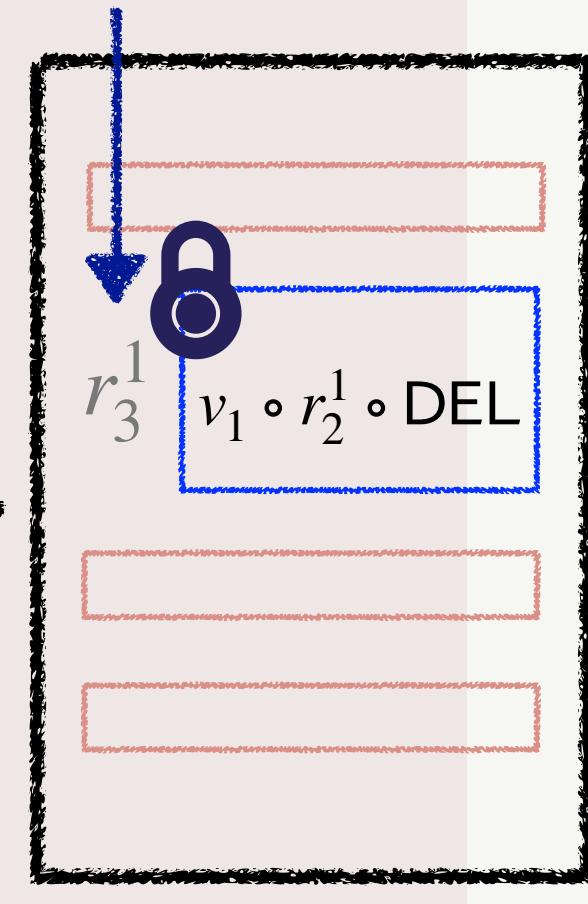
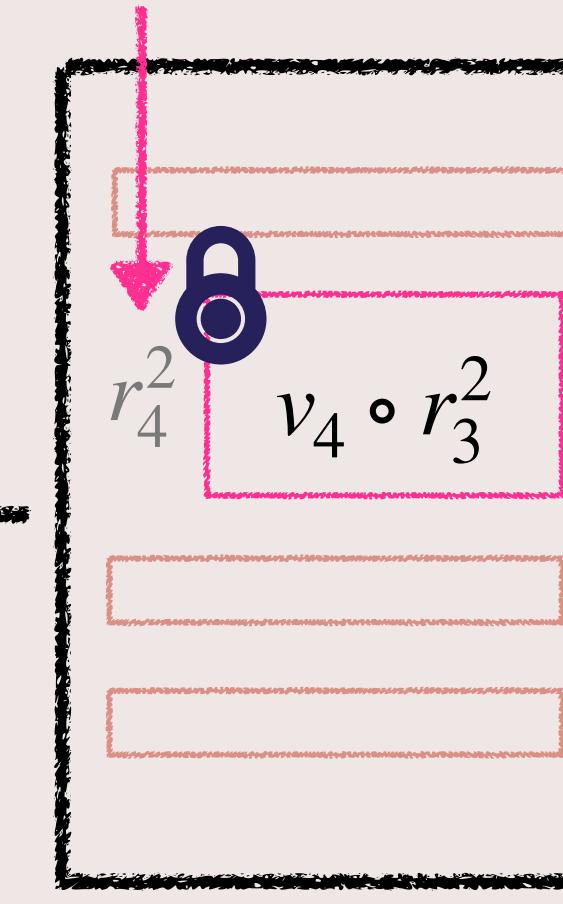
- Read all values from the list
- Output un-deleted values

# values ever added/  
deleted

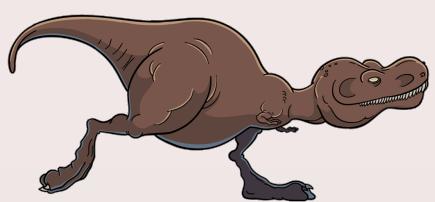
head  $\ell_2$



head  $\ell_1$



LSX



# TRX

## A tree-based EMM

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$

- Update the head

Optimal:  $O(|t|)$

time

stabilization

~~$O(|t|)$~~

time

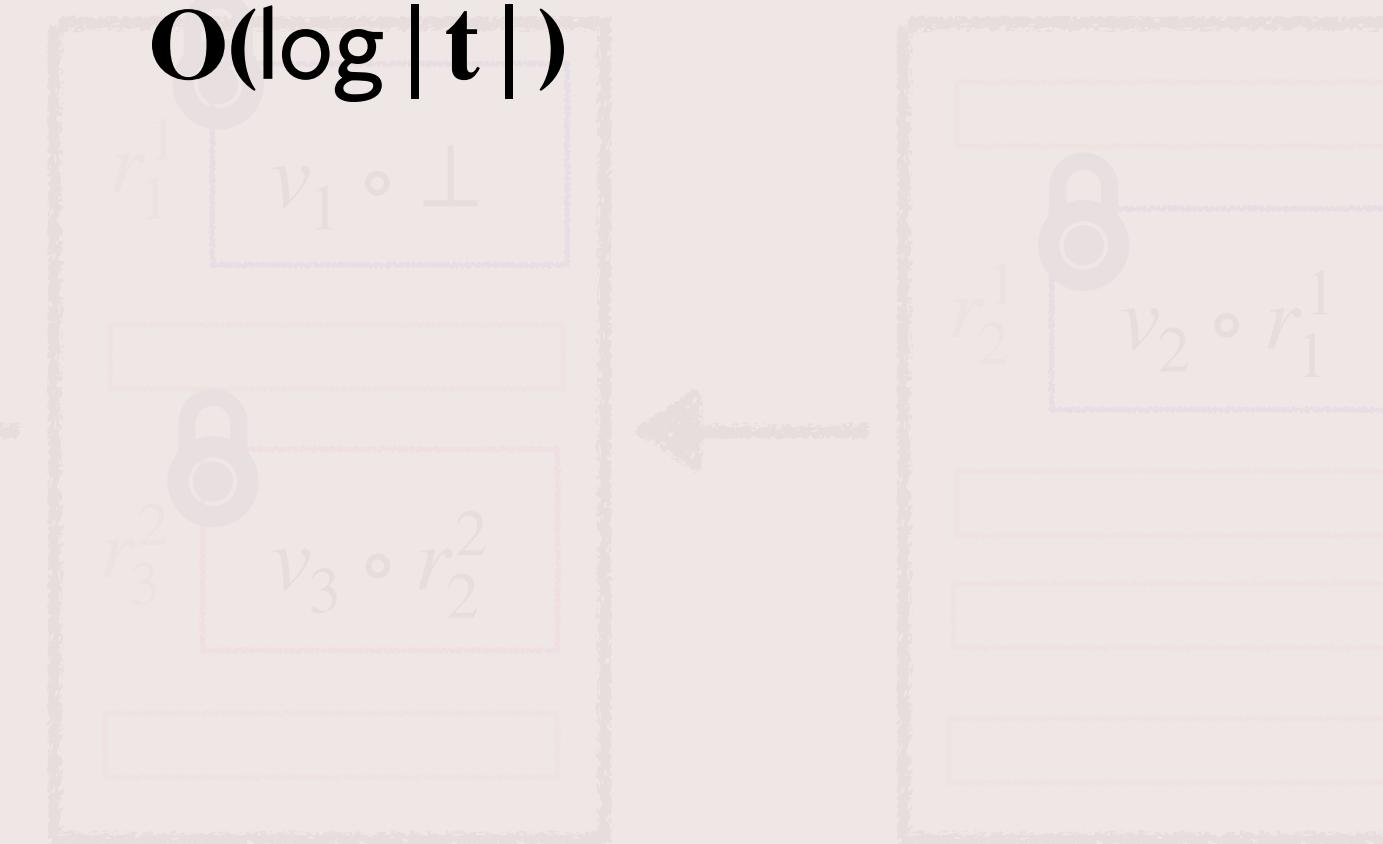
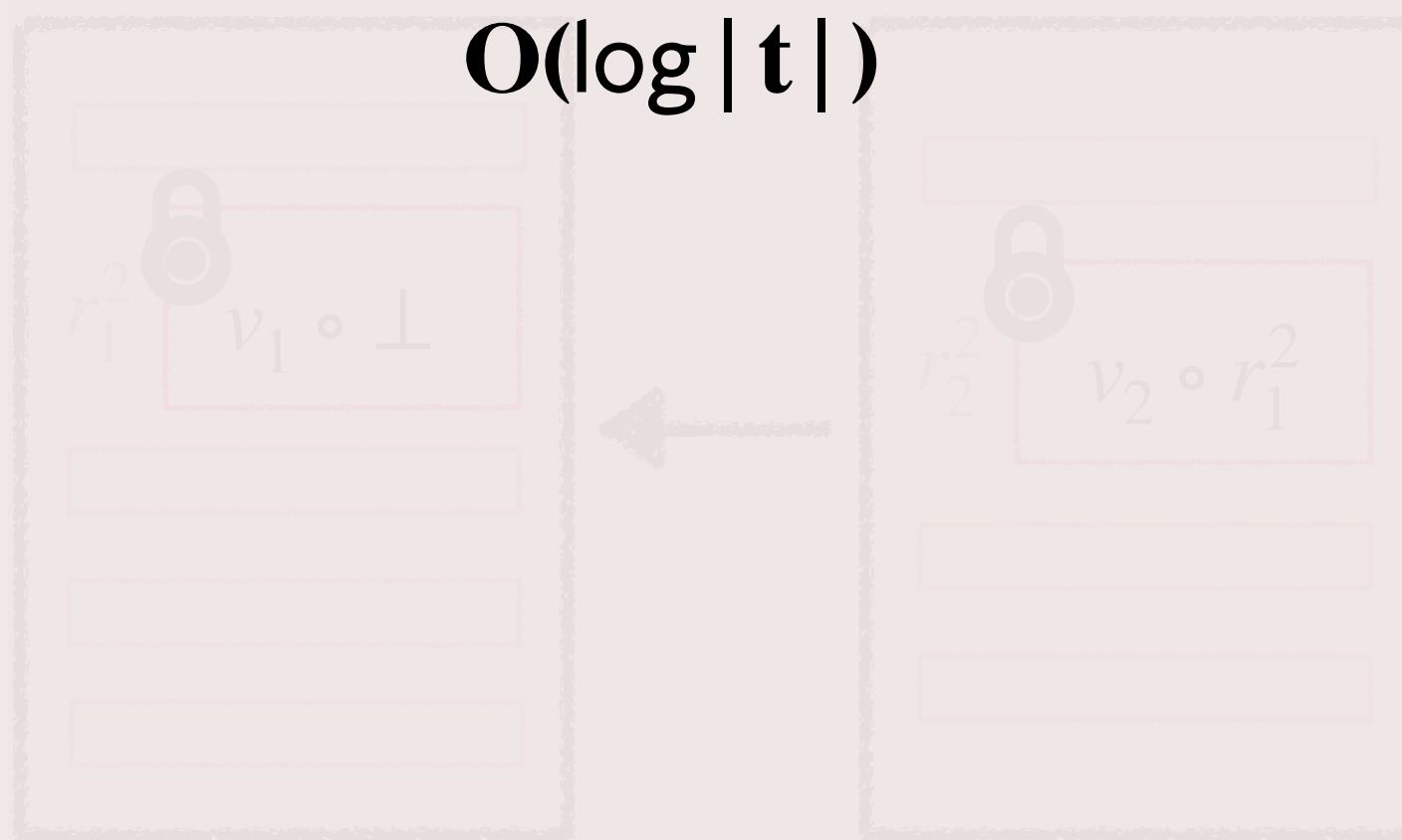
Optimal:  $O(|t|)$

stabilization

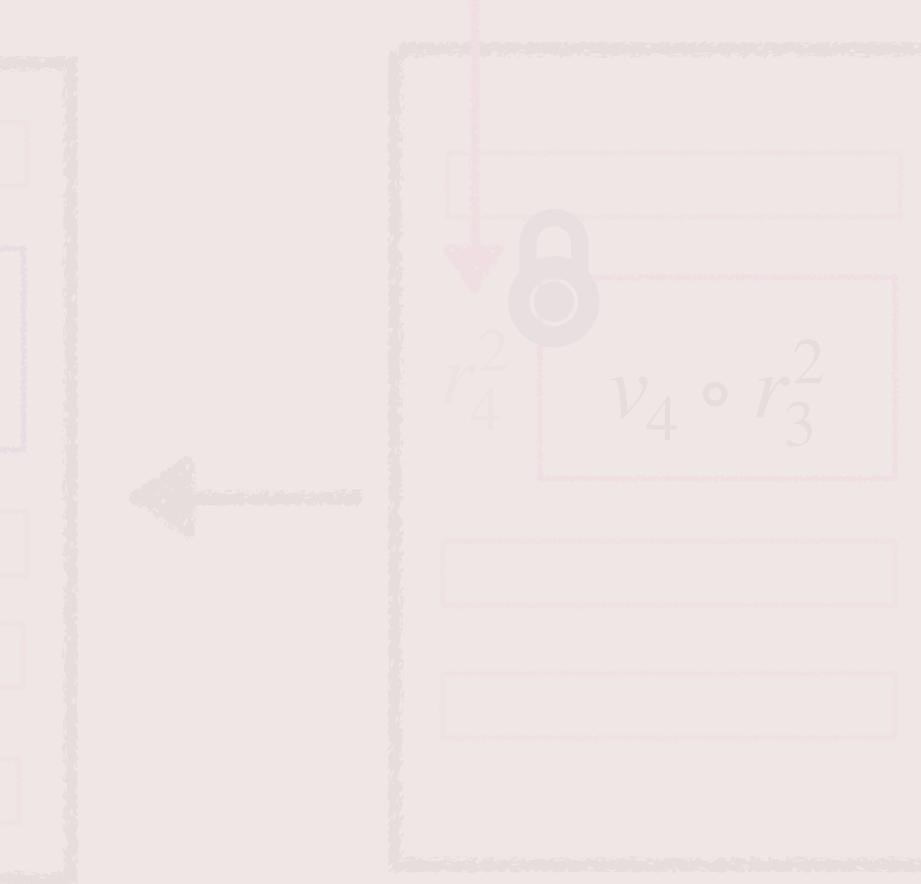
~~$O(|t|)$~~

time

# values ever added/  
deleted



head  $\ell_2$



head  $\ell_1$



LSX

# TRX

## A tree-based EMM

Add( $\ell_2, v_4$ )

- Append  $\text{Enc}(v_4, r_3^2)$  at head of  $\ell_2$

- Update the head

Optimal:  $O(|t|)$

~~$O(|t|)$~~

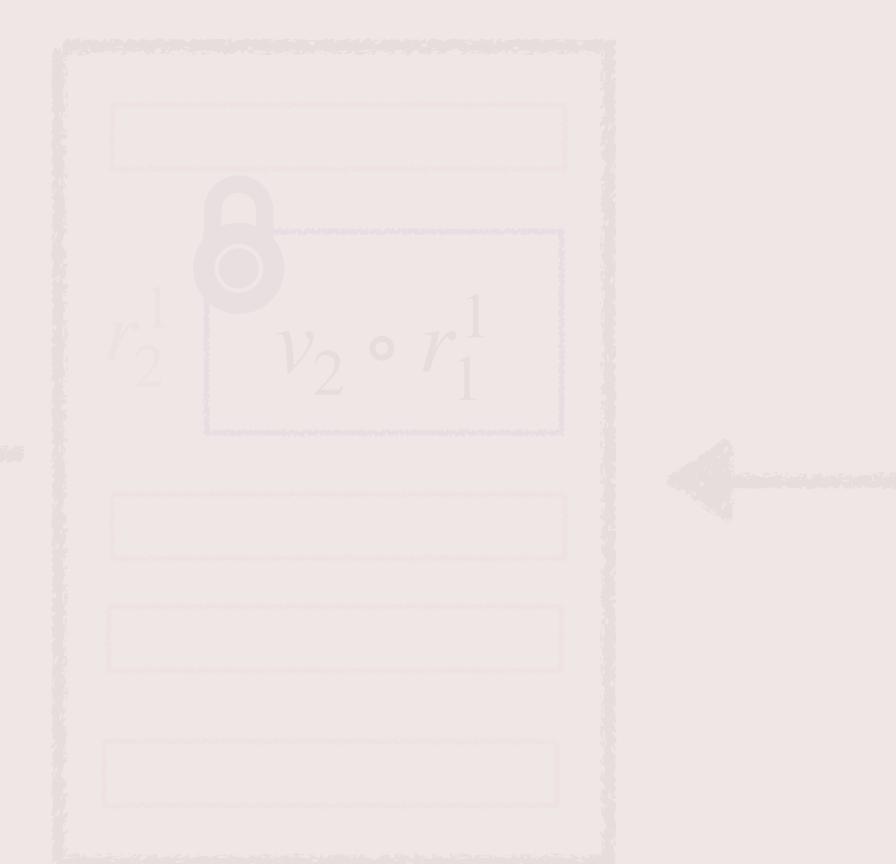
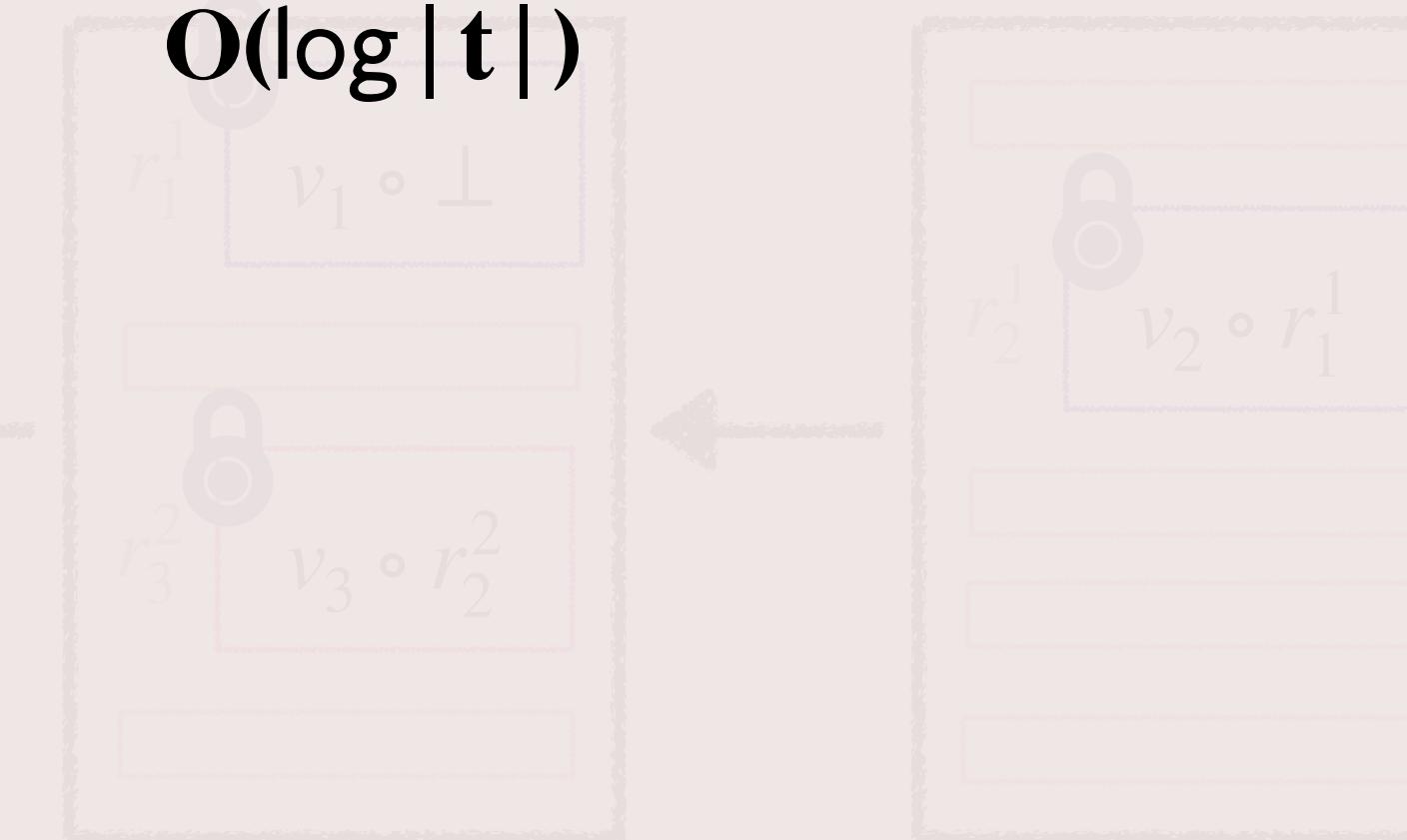
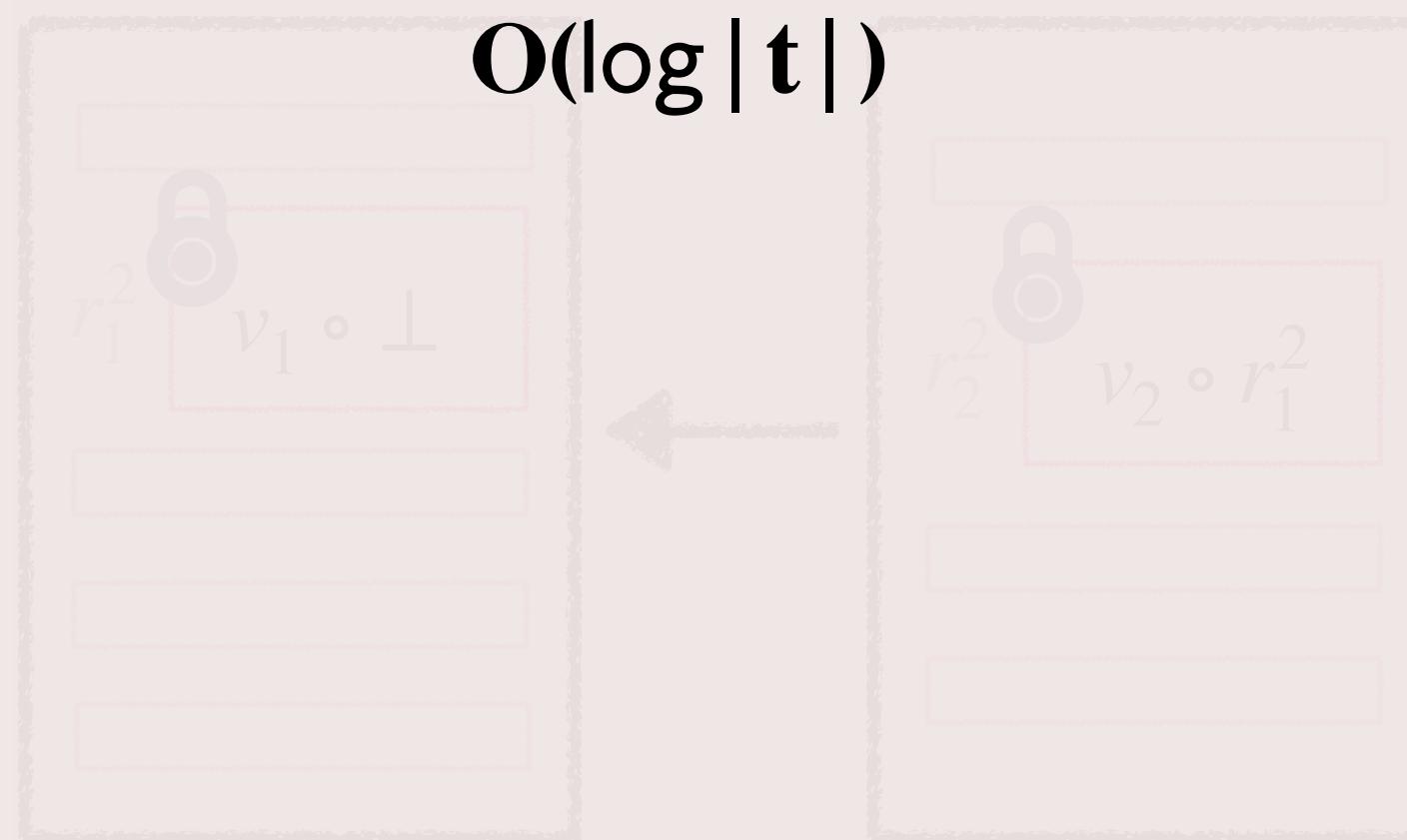
Optimal:  $O(|t|)$

~~$O(|t|)$~~

Query( $\ell_1$ )

- Read all values from the list
- Output un-deleted values

# values ever added/  
deleted



head  $\ell_2$

head  $\ell_1$



# PAX

A patched EMM

Add( $\ell_2, v_4$ )

time

Optimal:  $O(|t|)$

stabilization

$O(|t|)$

Delete( $\ell_1, v_1$ )

time

Optimal:  $O(|t|)$

stabilization

$O(|t|)$

Query( $\ell_1$ )

time

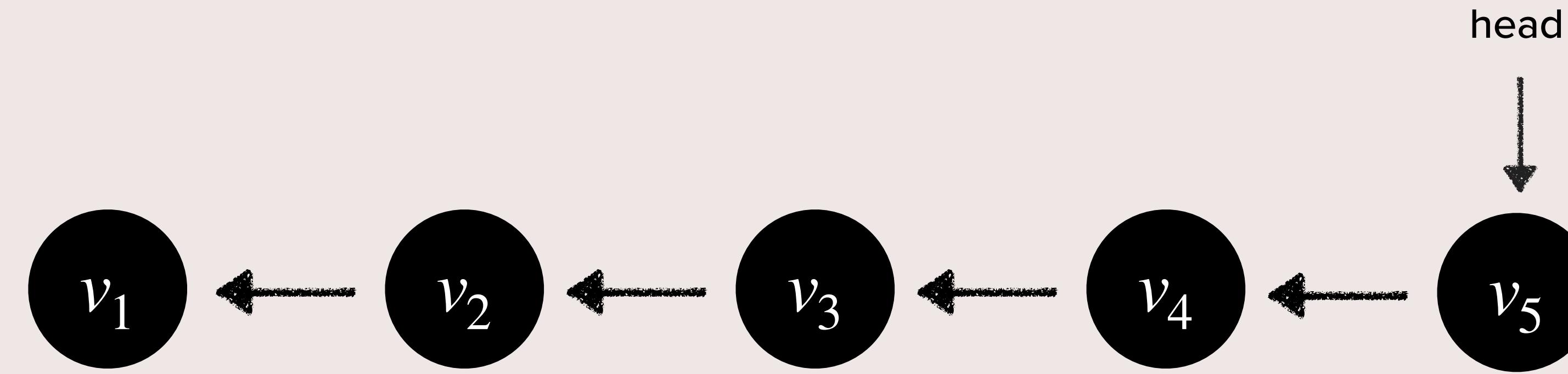
# values ever added/  
deleted

# PAX

Query( $\ell_1$ )

time

# values ever added/  
deleted

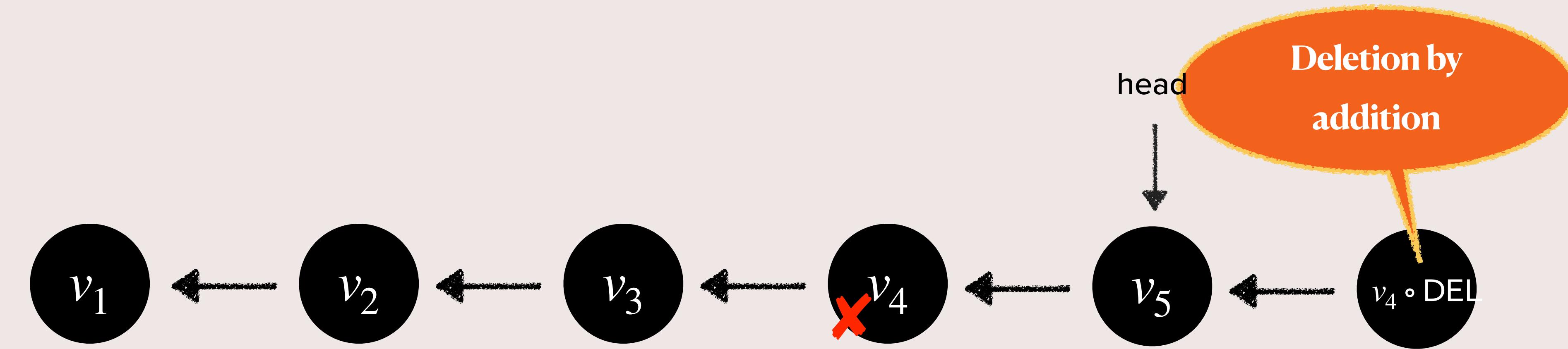


# PAX

Query( $\ell_1$ )

time

# values ever added/  
deleted

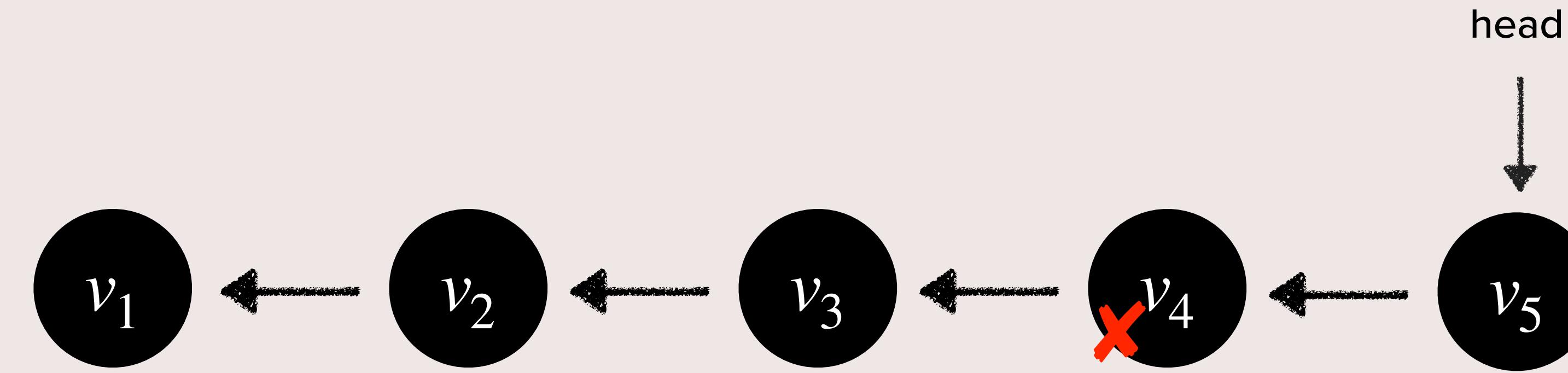


# PAX

Query( $\ell_1$ )

time

# values ever added/  
deleted

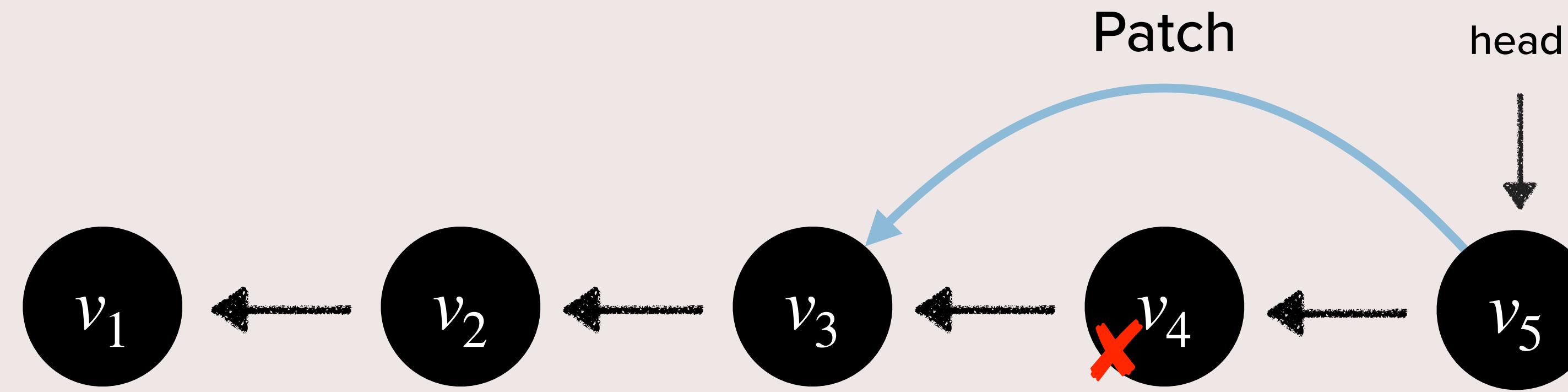


# PAX

time

Query( $\ell_1$ )

# values ever added/  
deleted



# PAX

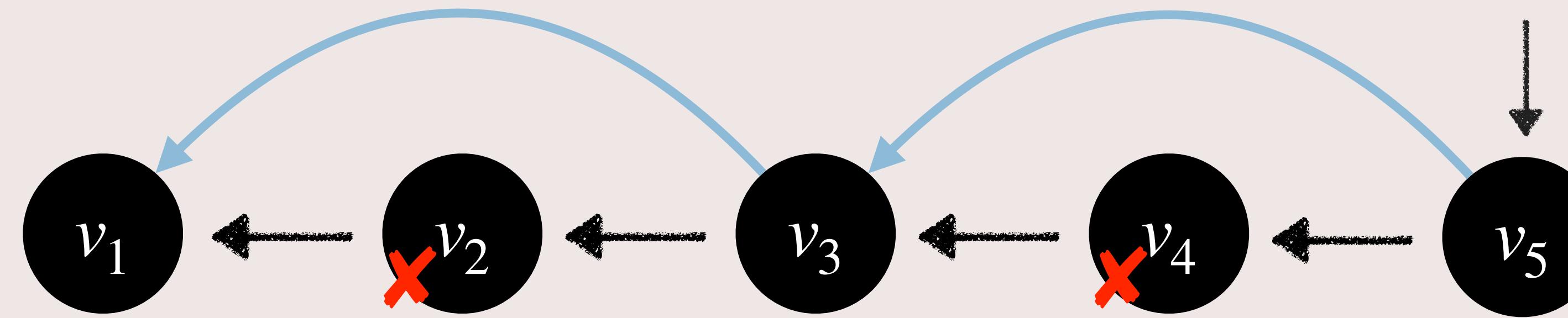
time

Query( $\ell_1$ )

# values ever added/  
deleted

Patch

head

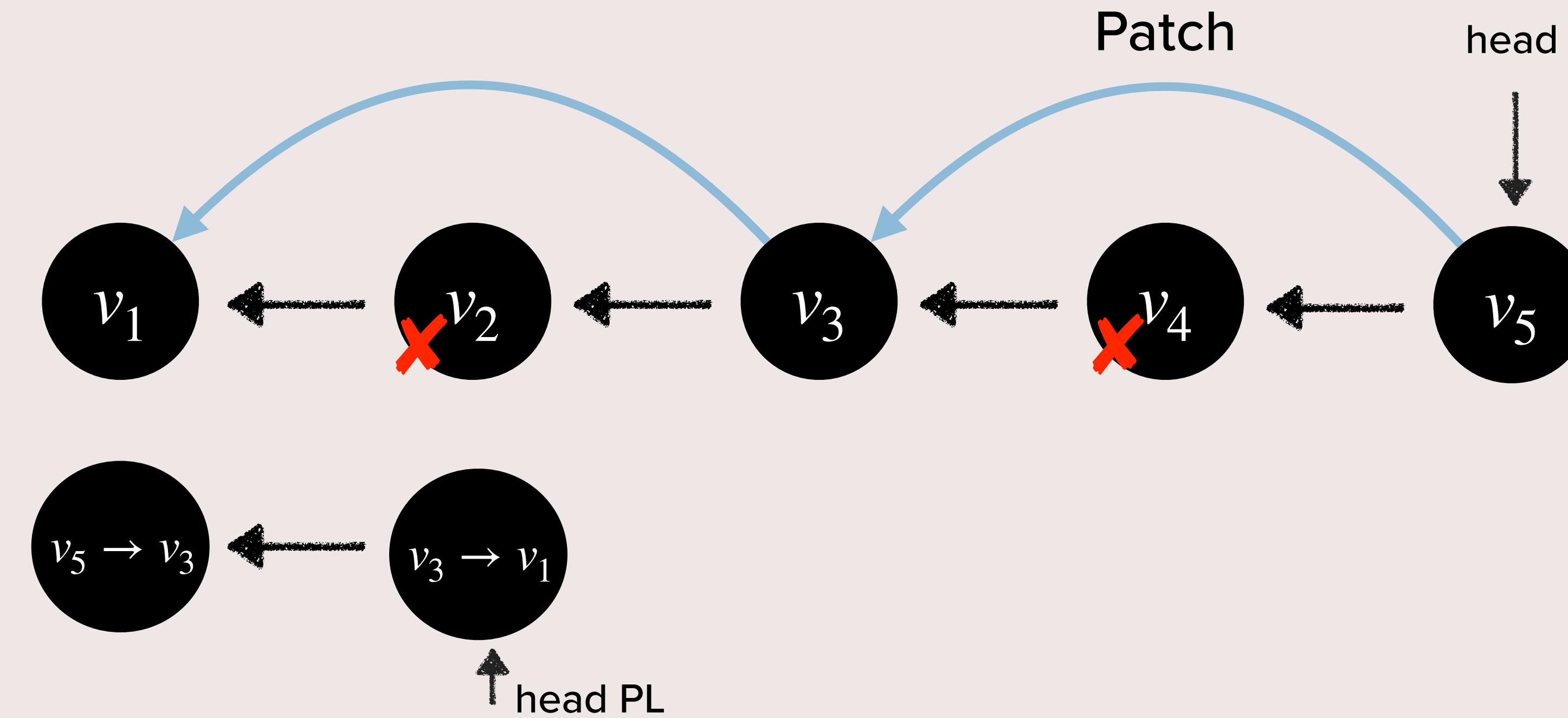


# PAX

time

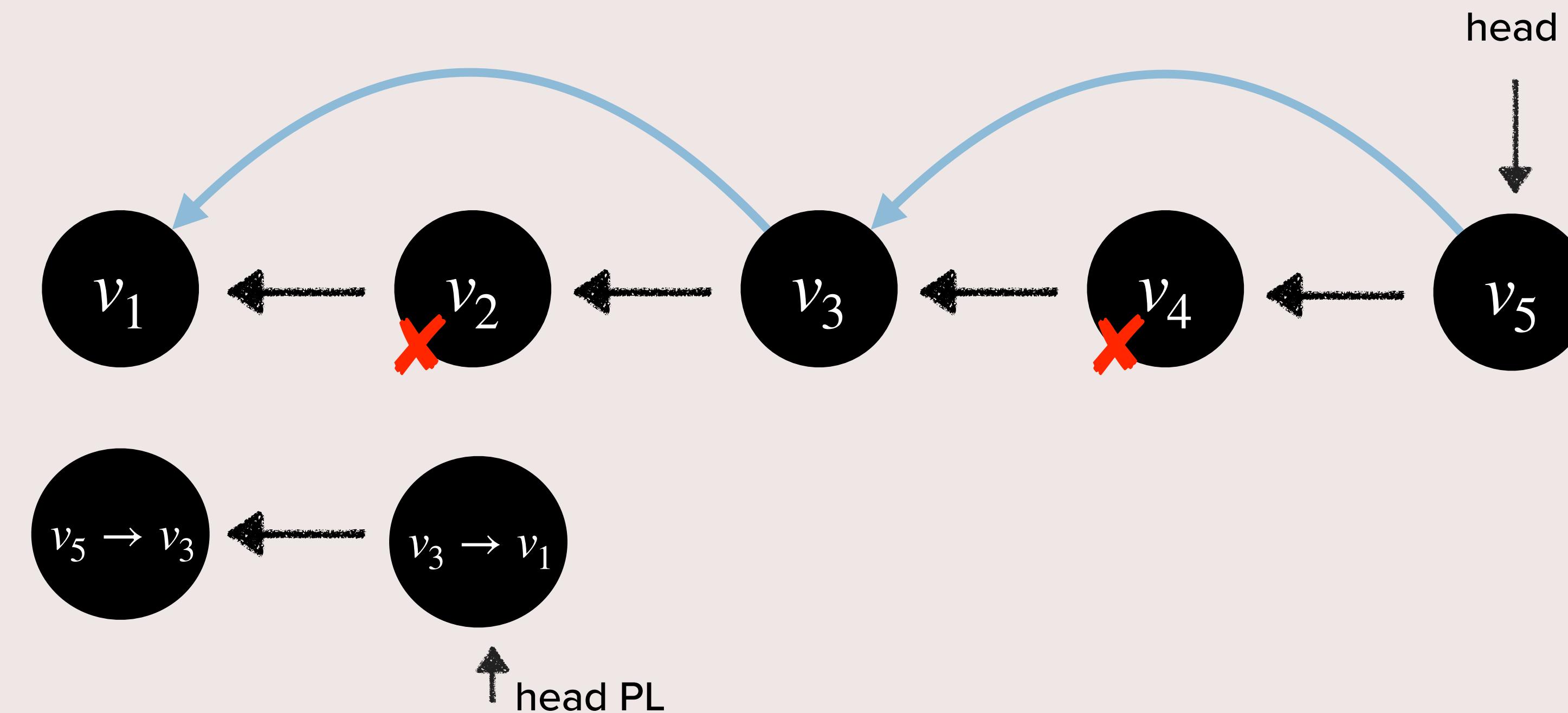
Query( $\ell_1$ )

# values ever added/  
deleted



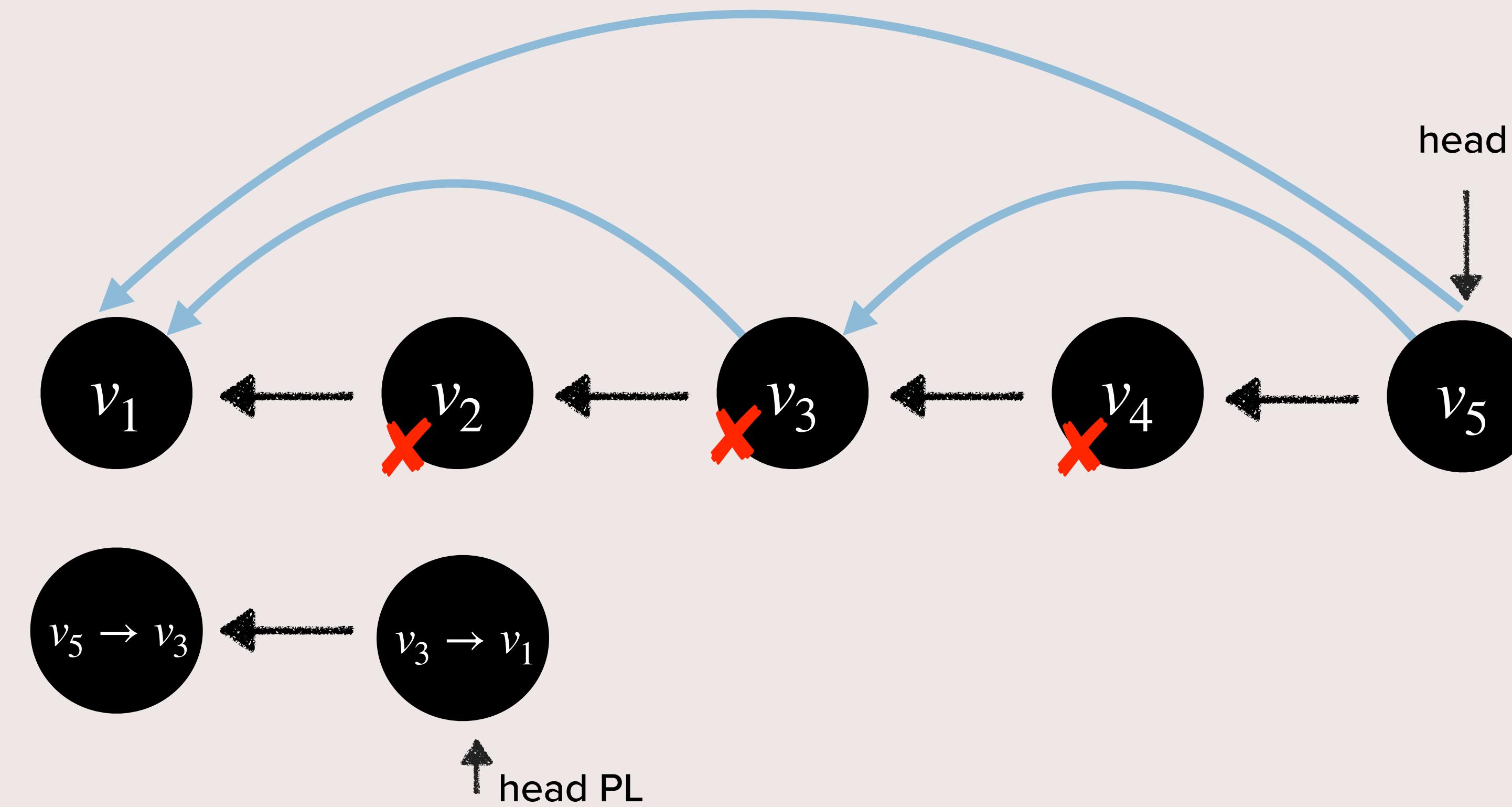
PAX

Let's delete  $v_3$



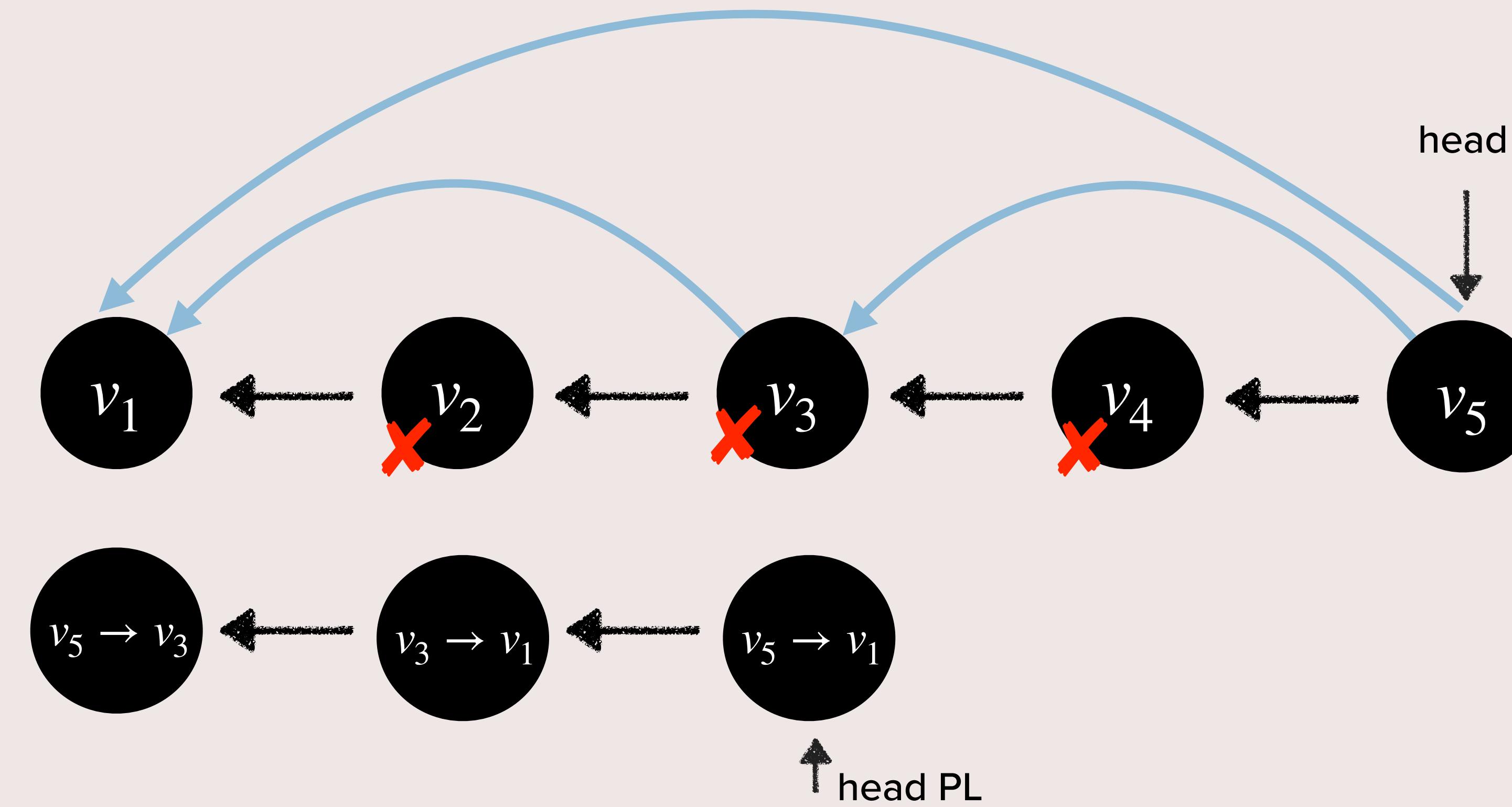
PAX

Let's delete  $v_3$



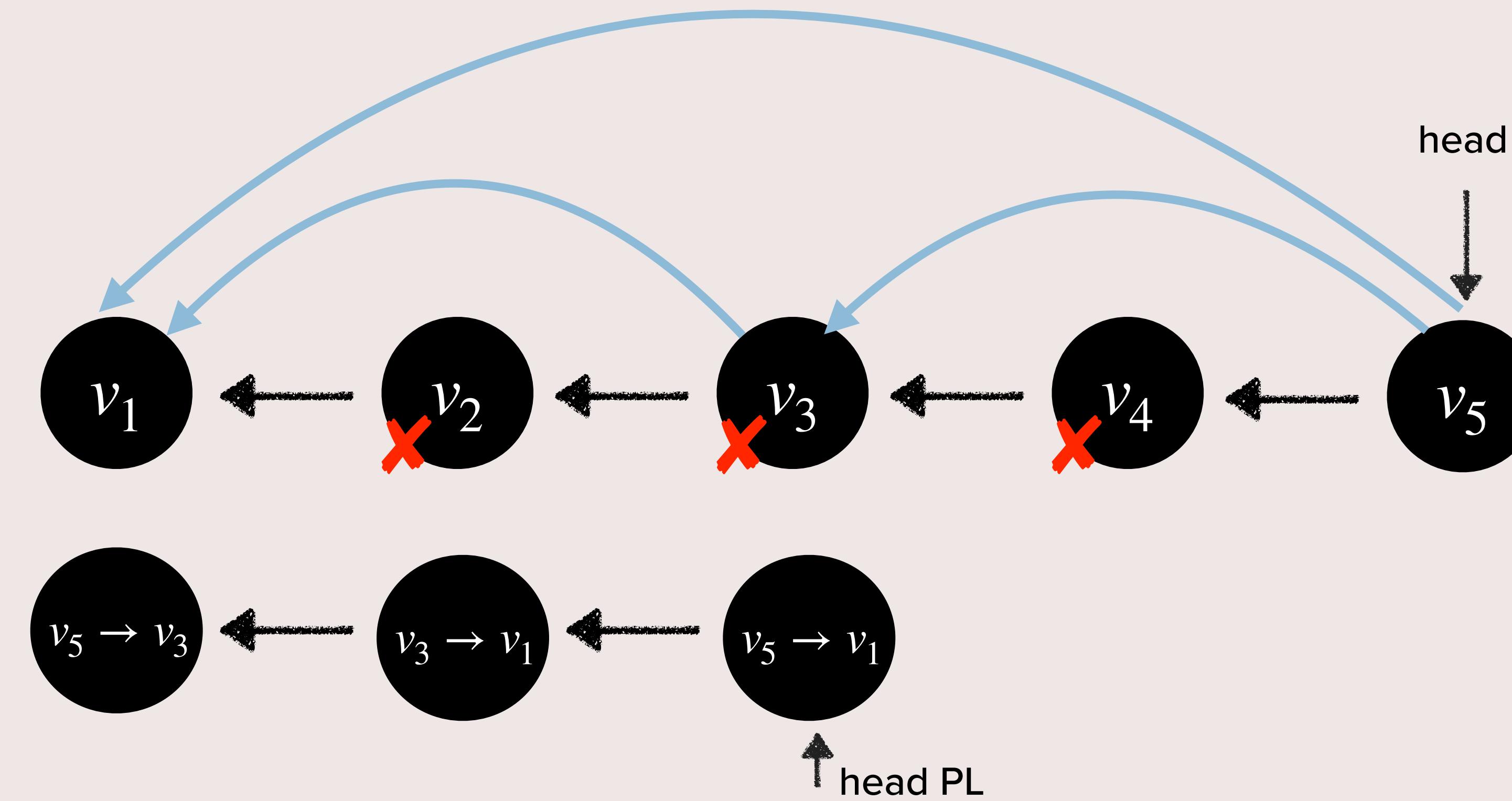
PAX

Let's delete  $v_3$



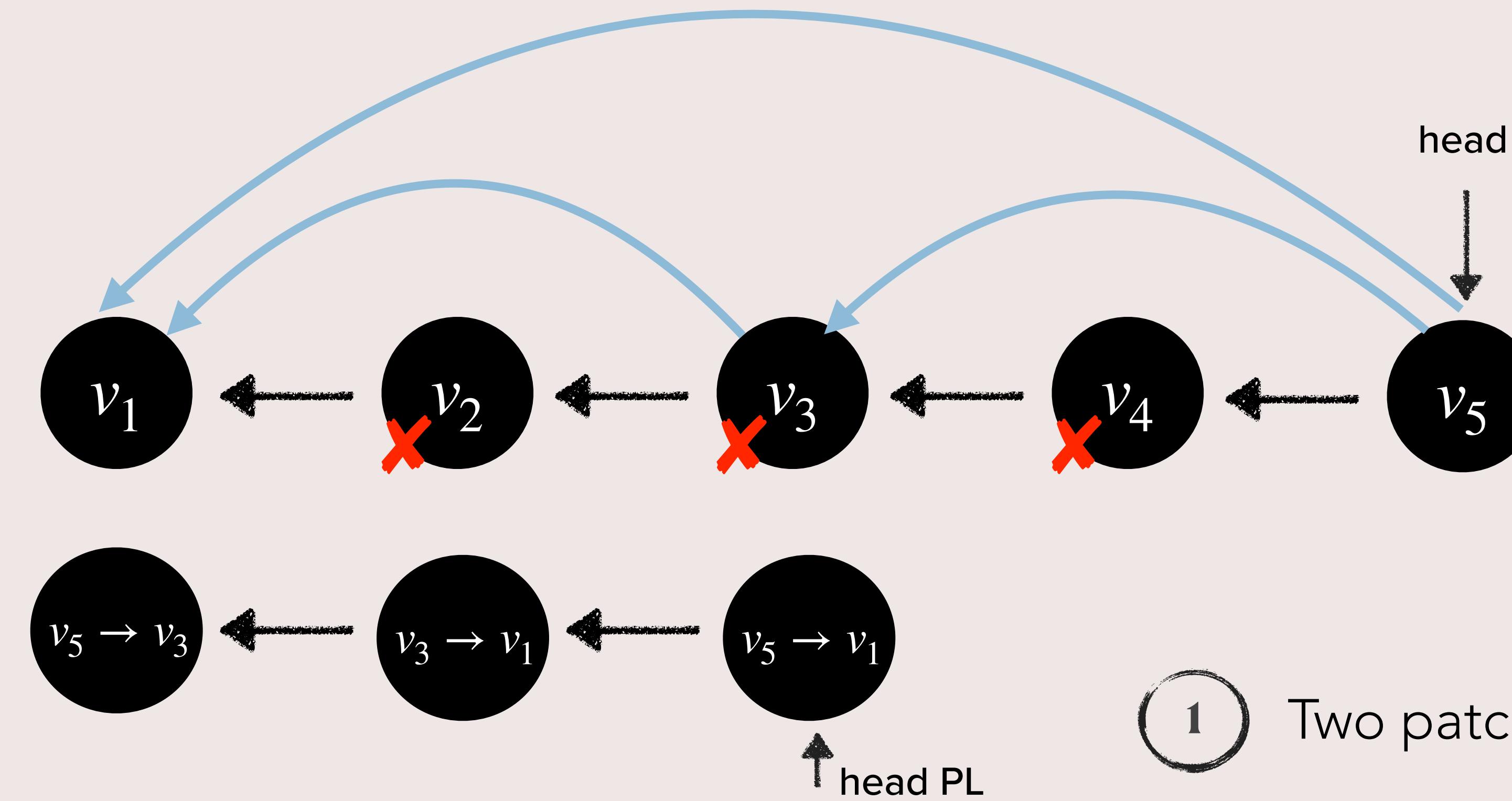
PAX

Let's delete  $v_3$



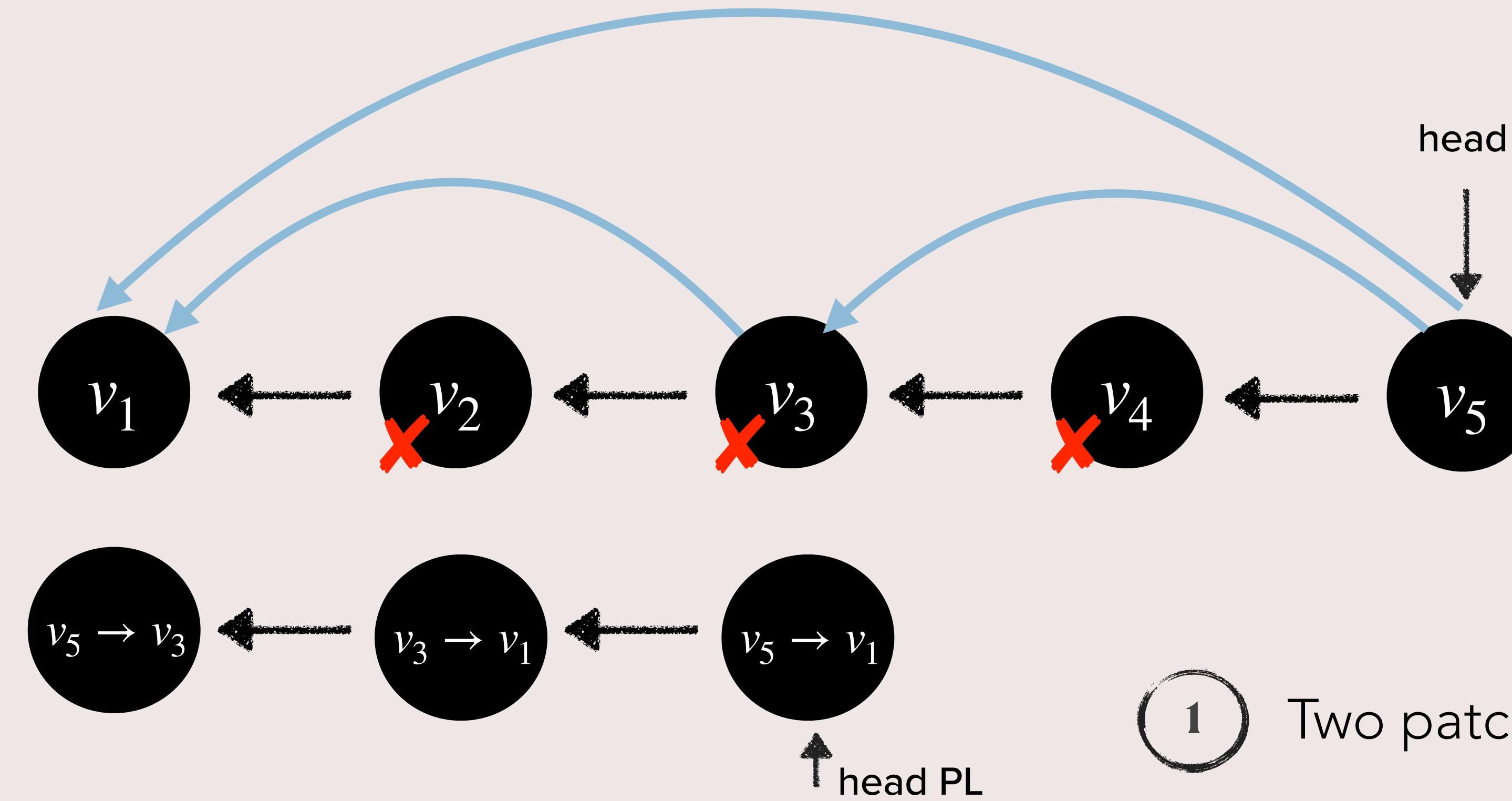
PAX

# Let's delete $v_3$

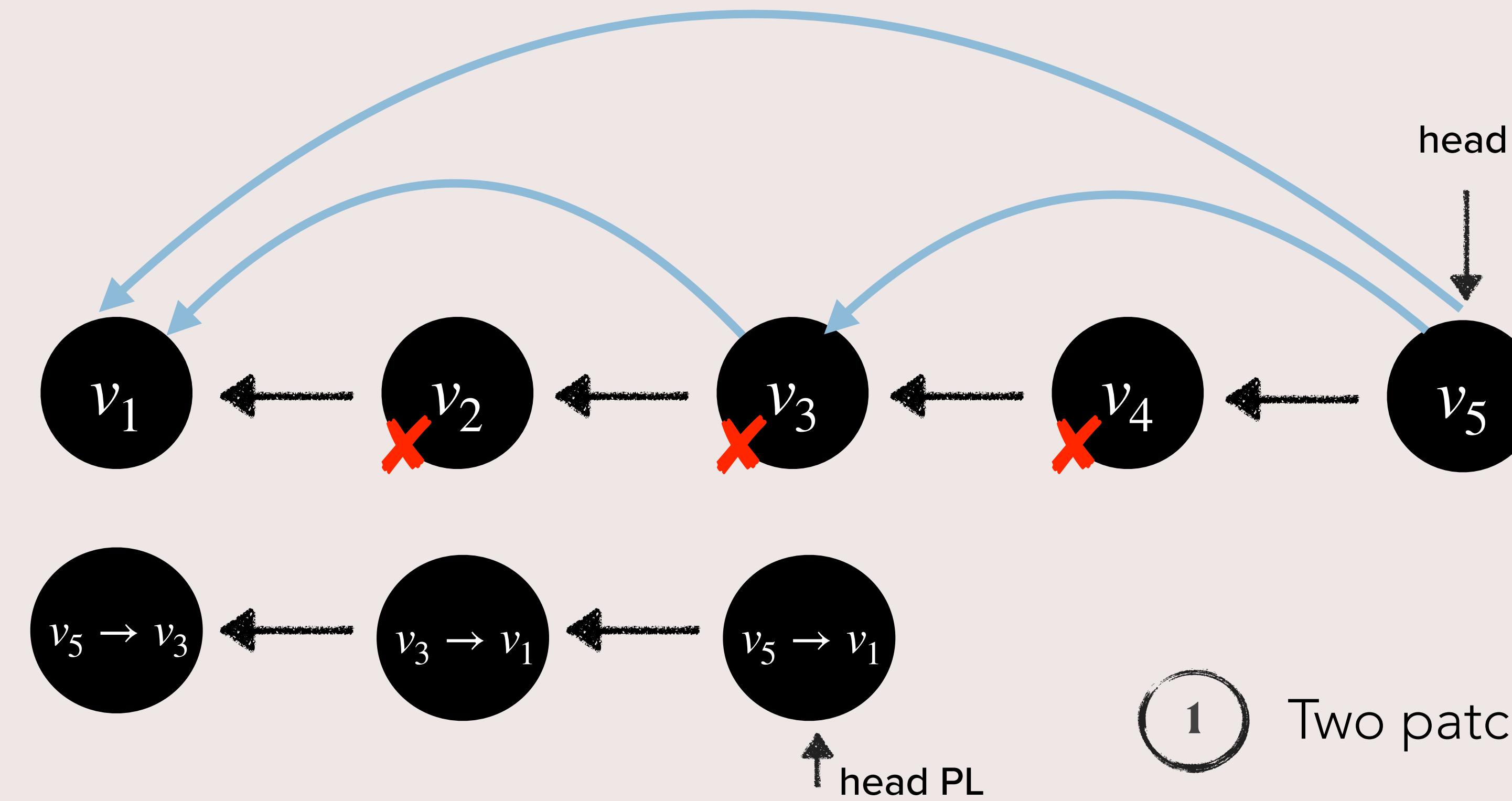


PAX

# Let's delete $v_3$



# Let's delete $v_3$



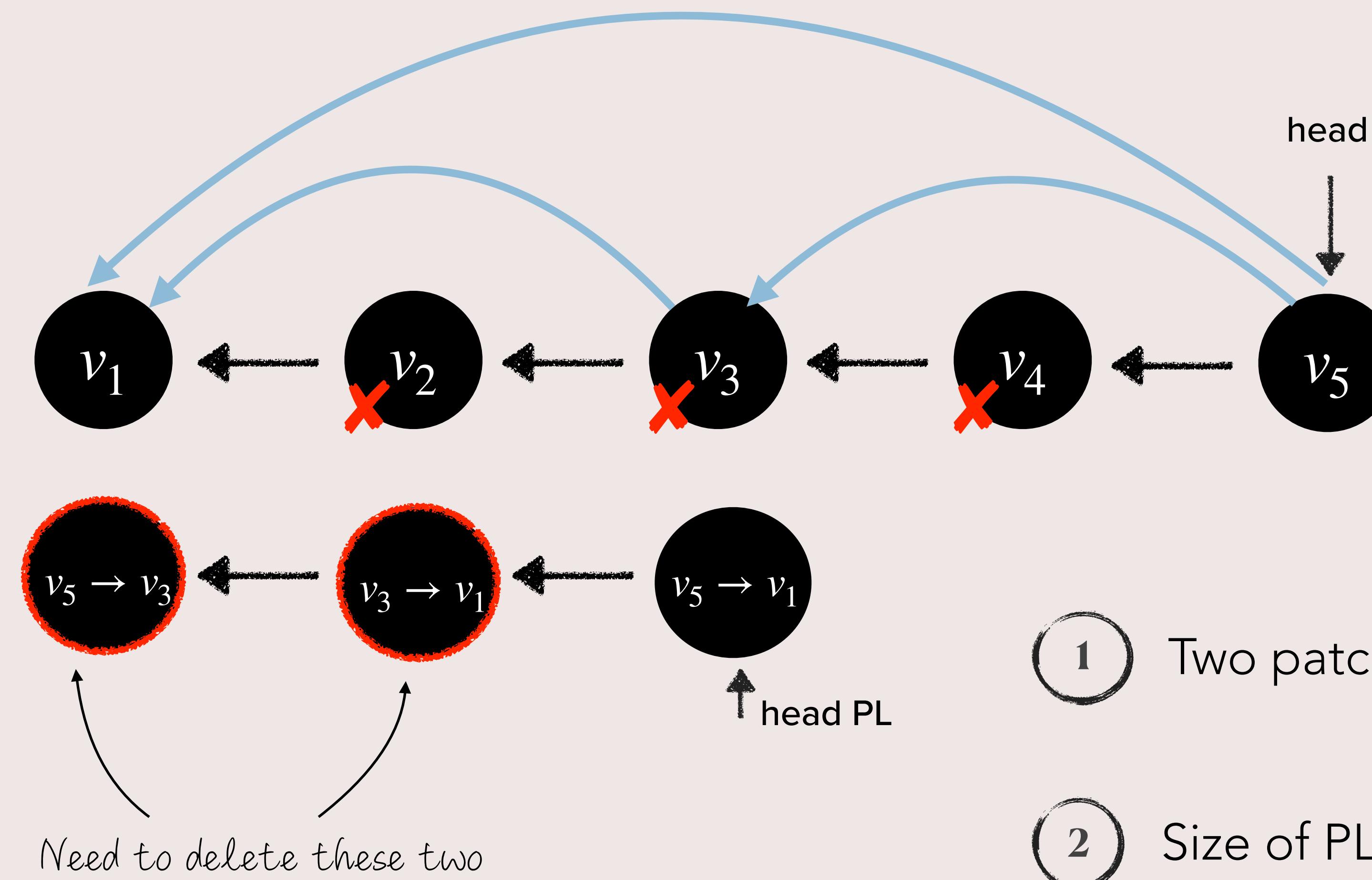
1 Two patches from  $v_5$

Bad for correctness

2 Size of PL = # values deleted

Bad for efficiency

# Let's delete $v_3$



1 Two patches from  $v_5$

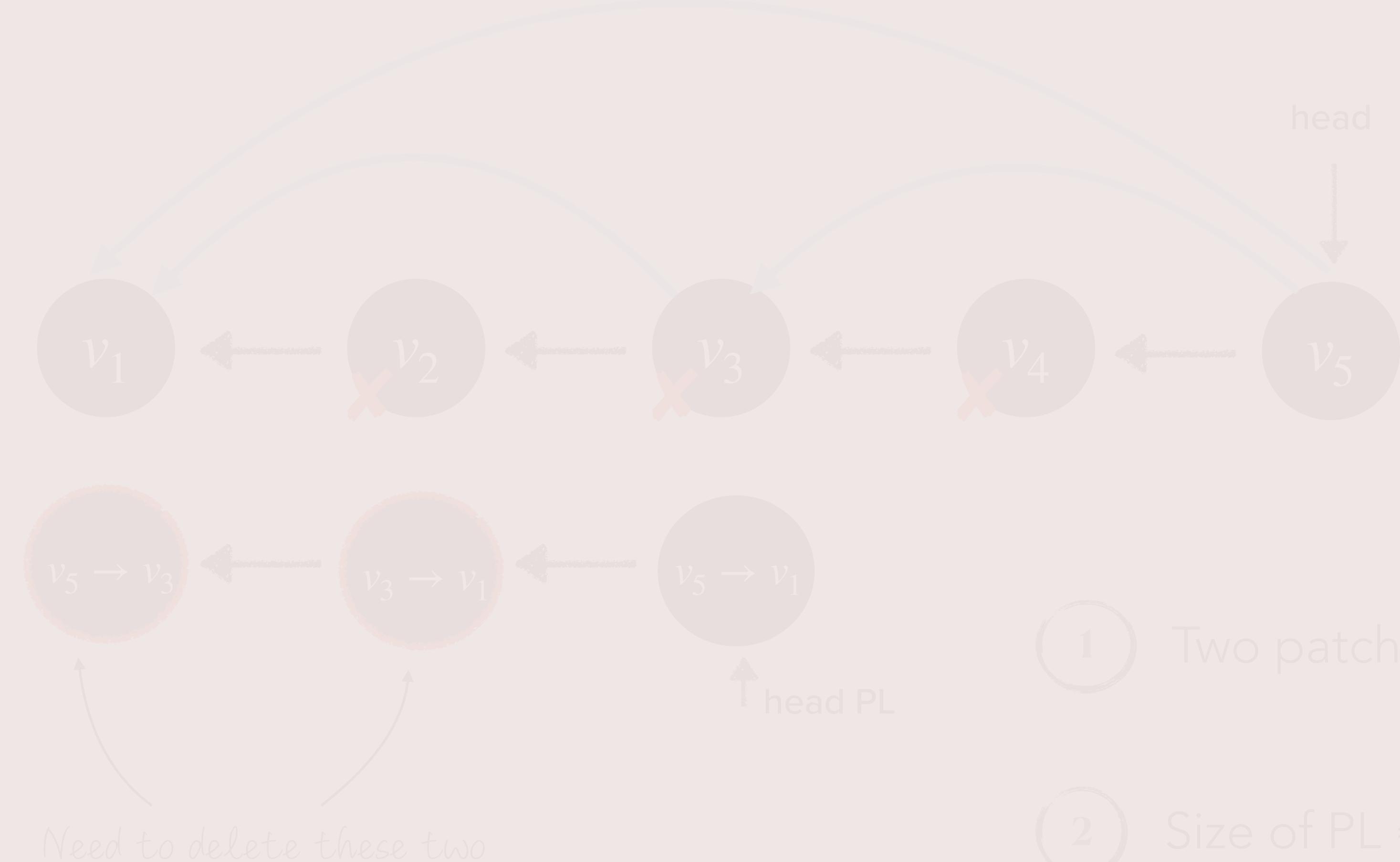
Bad for correctness

2 Size of PL = # values deleted

Bad for efficiency

# PAX

## Let's delete $v_3$



① Two patches from  $v_5$

Bad for correctness

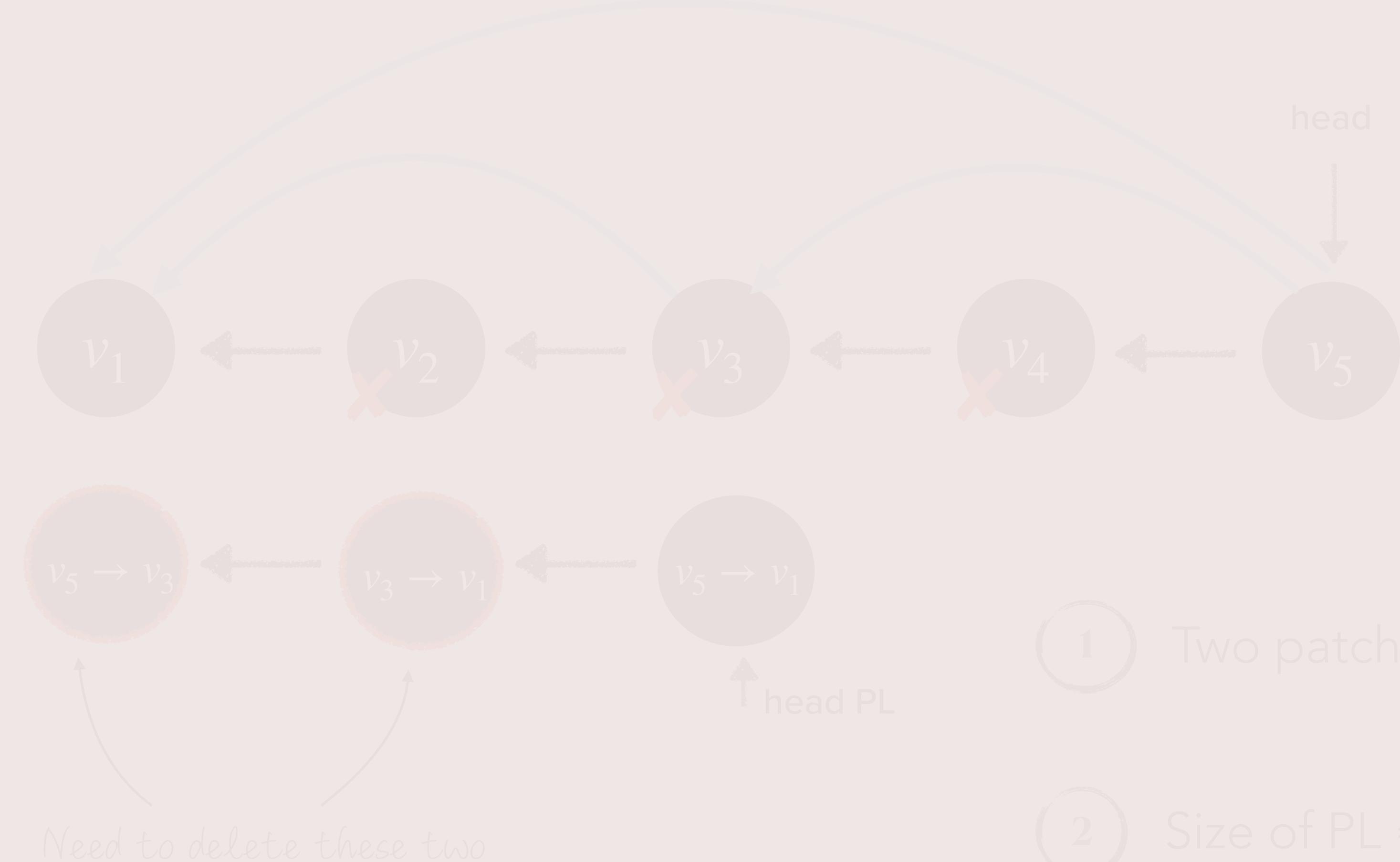
② Size of PL = # vertices deleted

Bad for efficiency



# PAX

## Let's delete $v_3$



① Two patches from  $v_5$

Bad for correctness

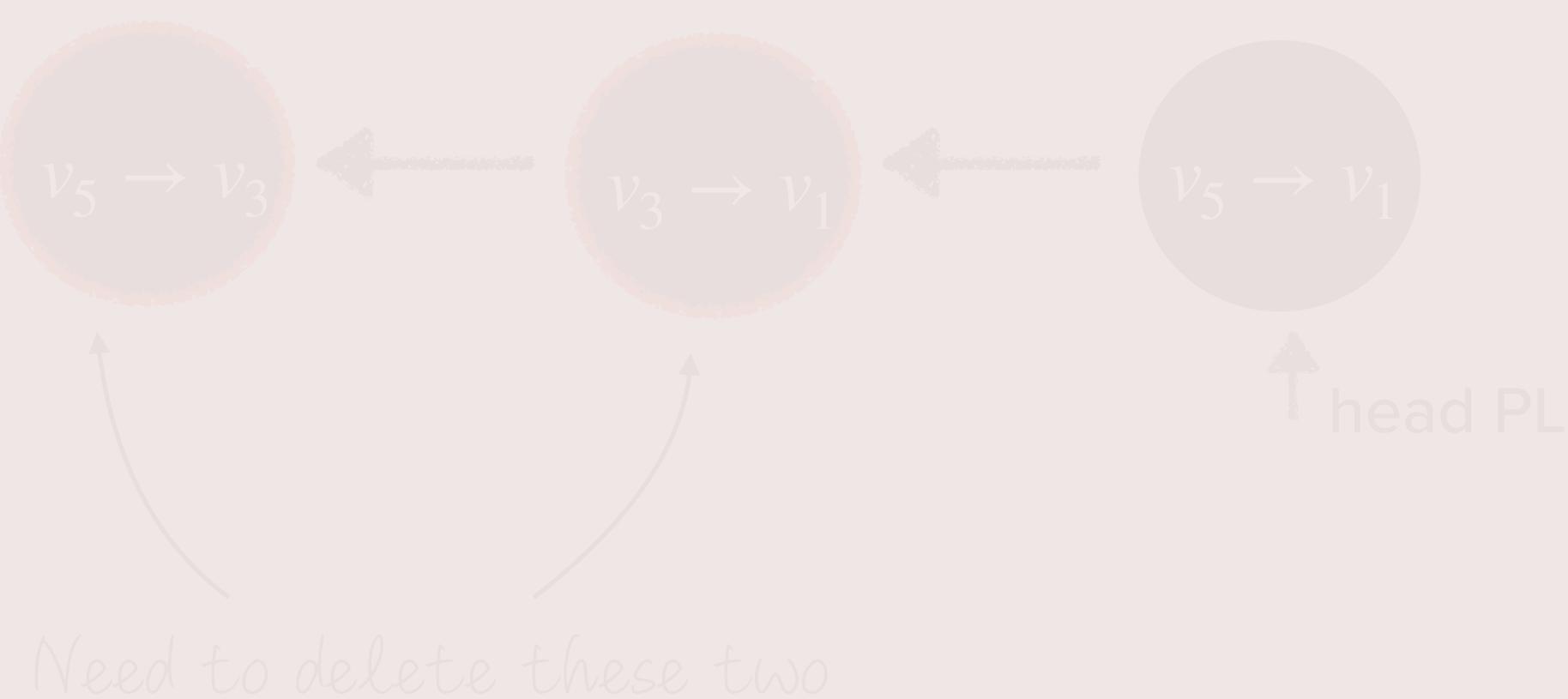
② Size of PL = # vertices deleted

Bad for efficiency



Let's delete  $v_3$

# Copy On Write



① Two patches from  $v_5$

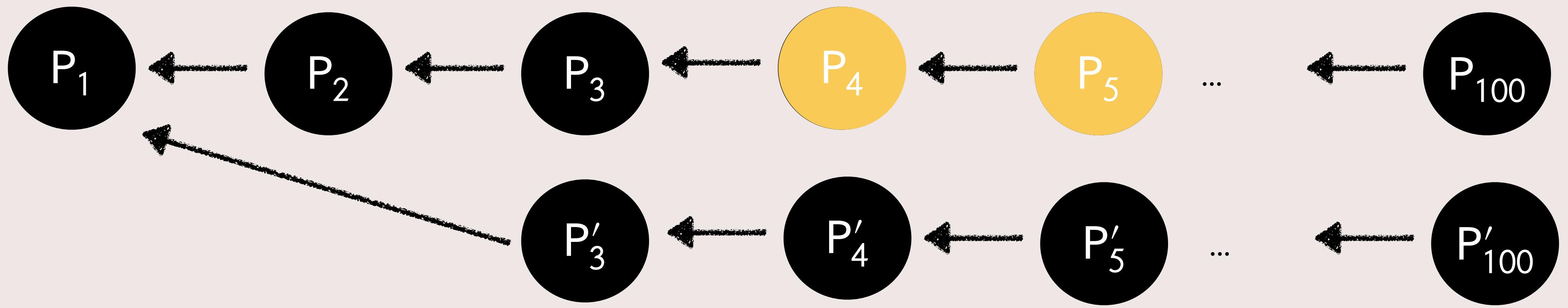
Bad for correctness

② Size of PL = # vertices deleted

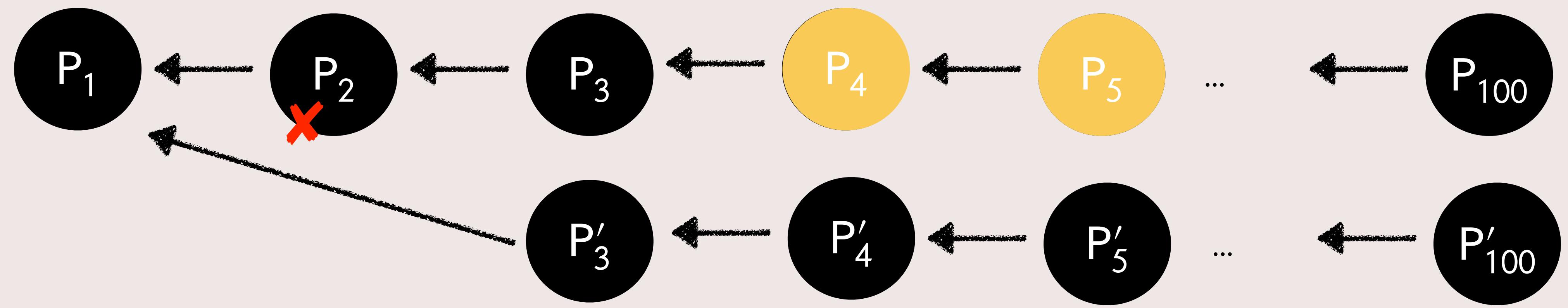
Bad for efficiency



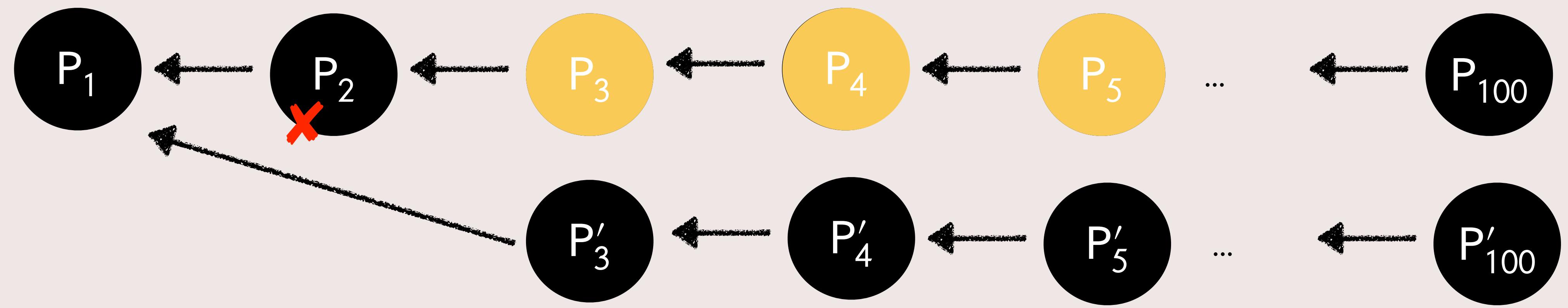
PAX



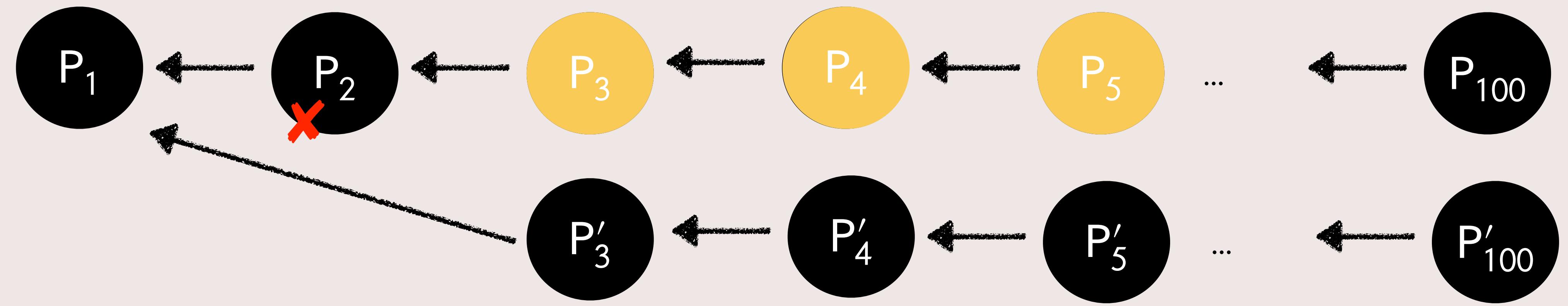
# PAX



# PAX

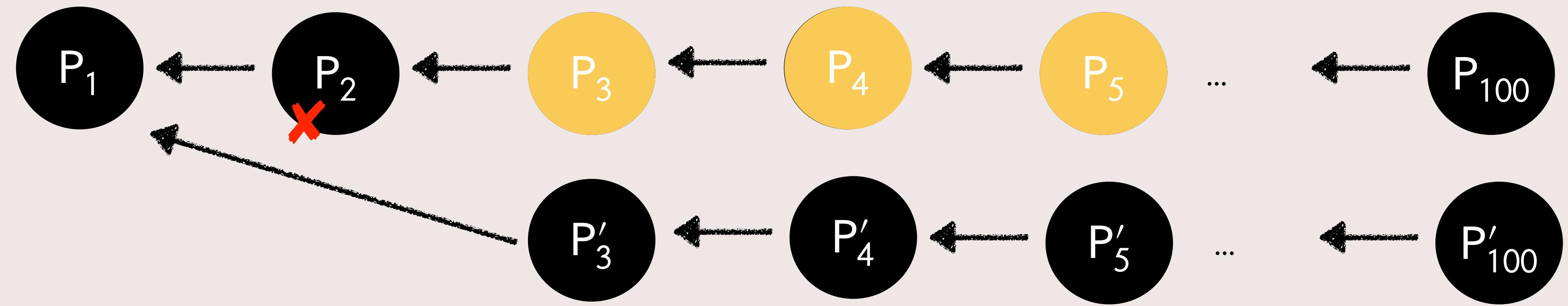


PAX

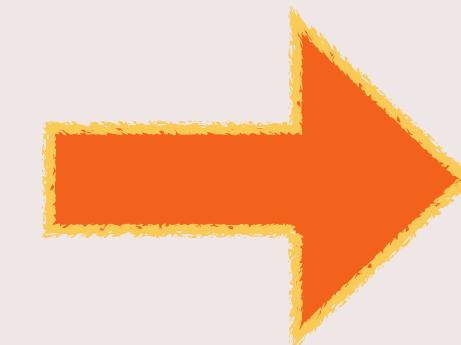


Expensive!

PAX

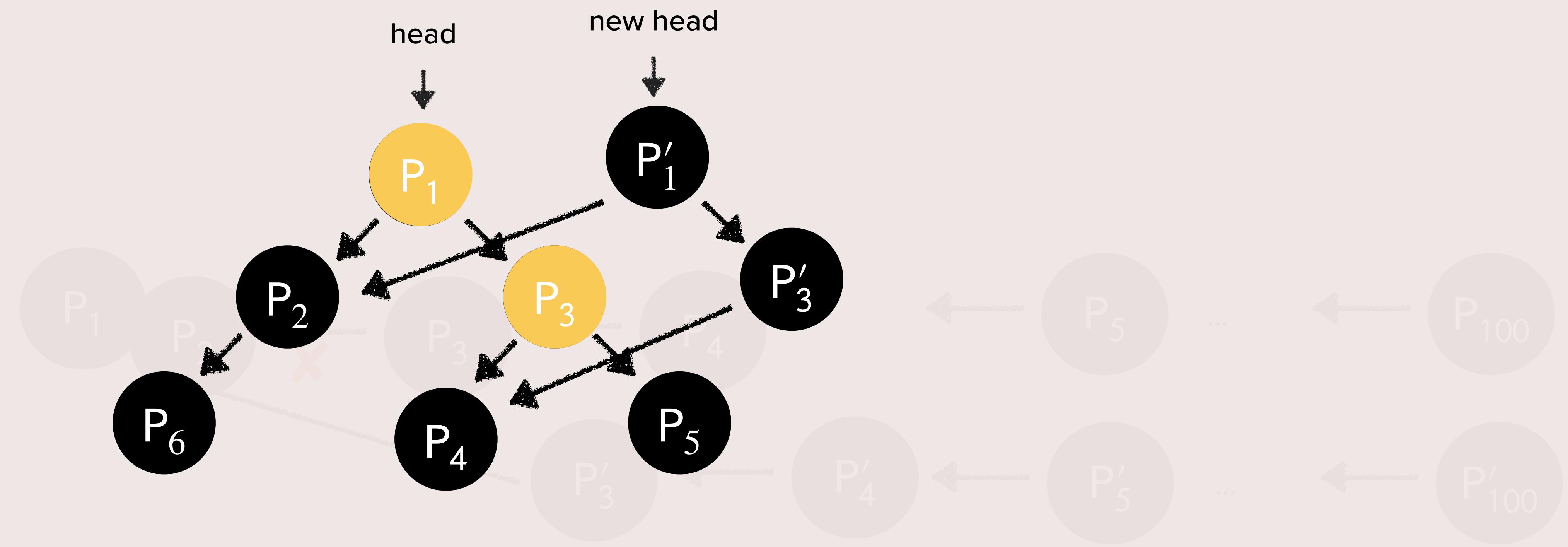


Expensive!

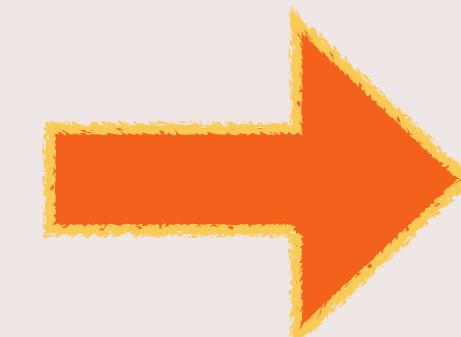


Organize patches in a BST

# PAX

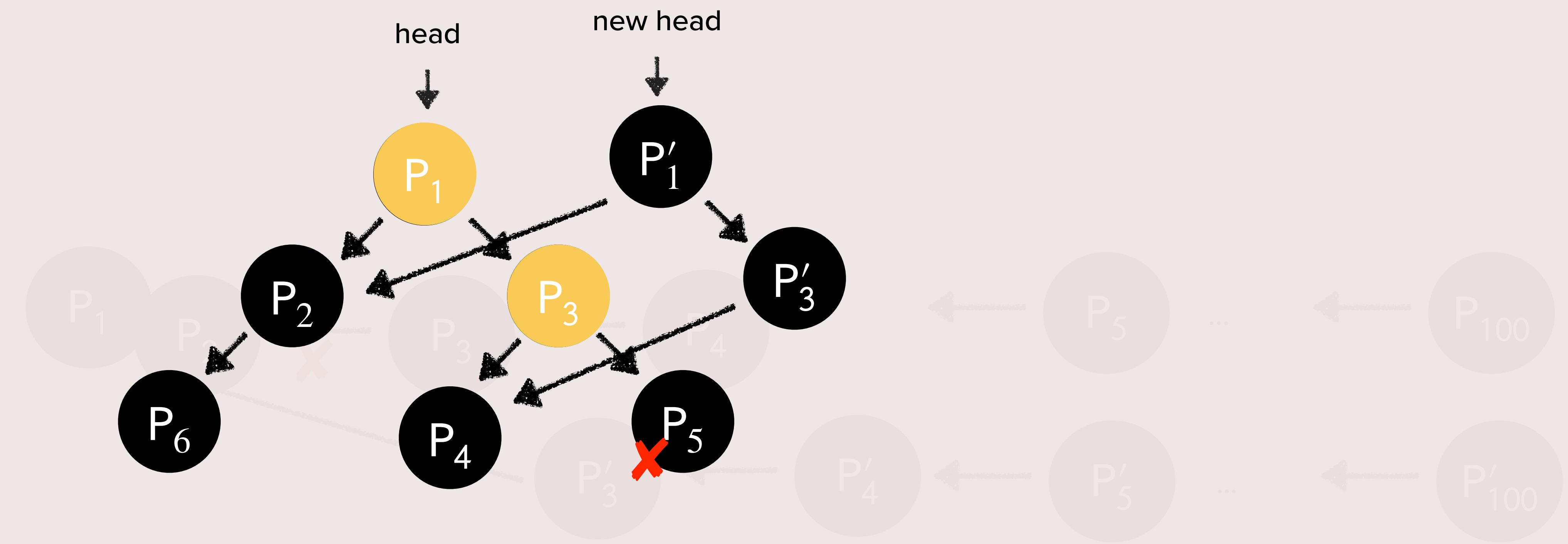


Expensive!

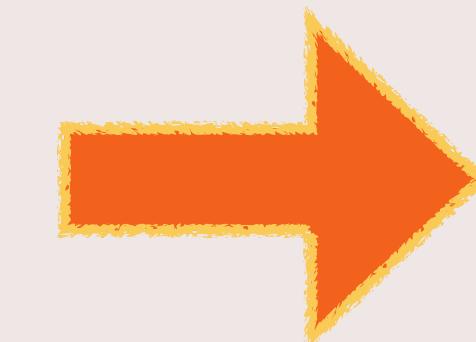


Organize patches in a BST

# PAX

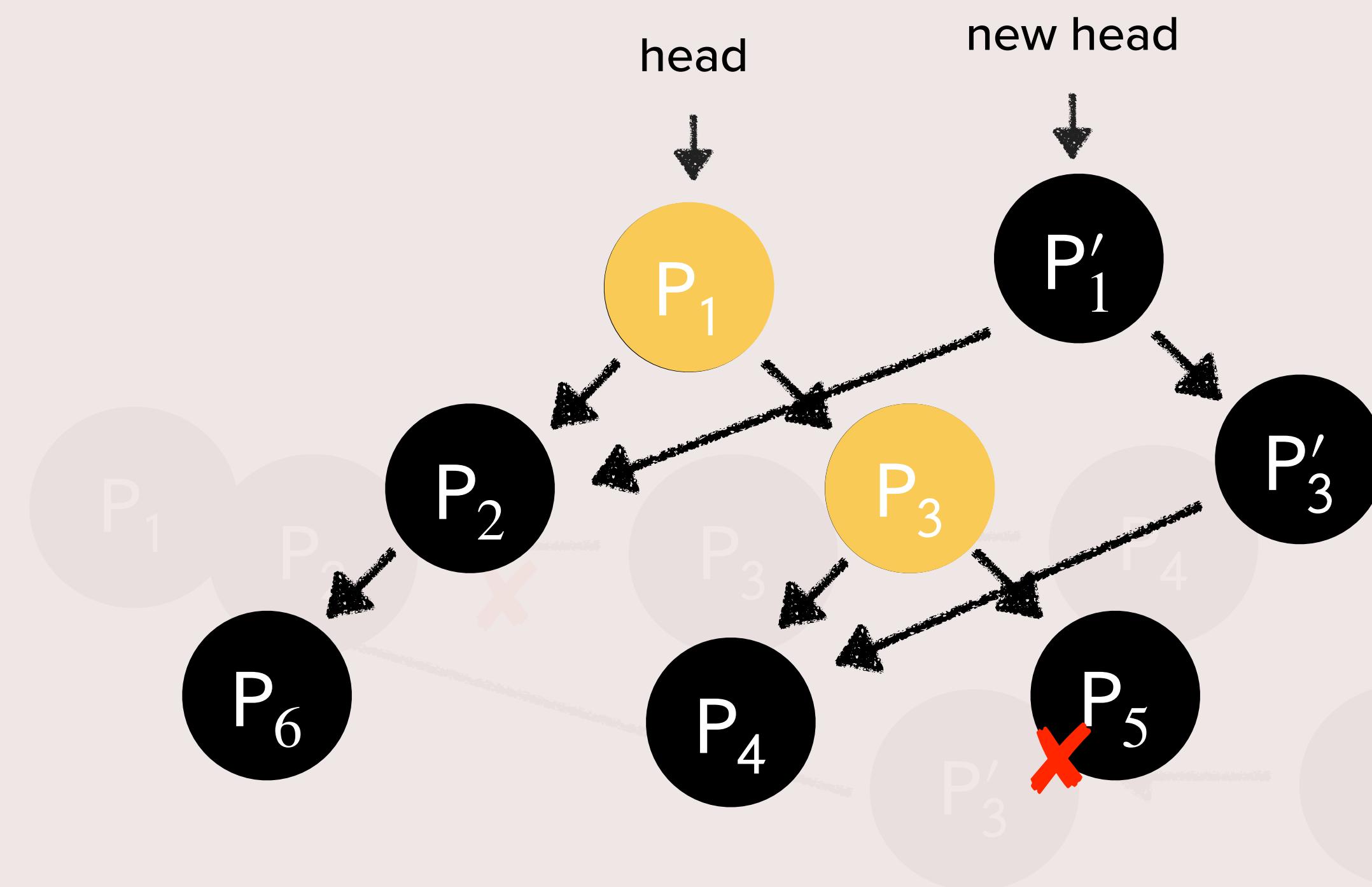


Expensive!



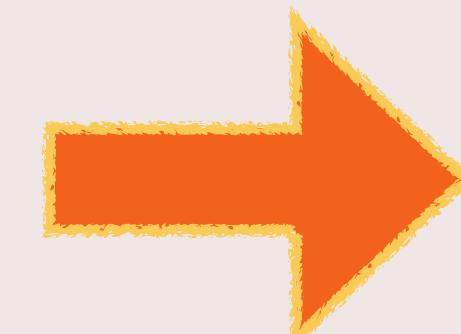
Organize patches in a BST

# PAX



Show  
# nodes in BST  
 $\leq$  # values in multi-map

Expensive!



Organize patches in a BST

# PAX

Add

time

stabilization

time LSX

stabilization LSX

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Delete

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Query

$O(\# \text{ values ever added/deleted})$

# PAX

Add

time

$O(|\mathbf{t}|)$

stabilization

time LSX

$O(|\mathbf{t}|)$

stabilization LSX

$O(|\mathbf{t}|)$

Delete

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Query

$O(\# \text{ values ever added/deleted})$

# PAX

Add

time

stabilization

time LSX

stabilization LSX

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Delete

$O(|\mathbf{t}| \log (\text{size of MM}))$

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Query

$O(\# \text{ values ever added/deleted})$

# PAX

Add

time

stabilization

time LSX

stabilization LSX

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Delete

$O(|\mathbf{t}| \log (\text{size of MM}))$

$O(|\mathbf{t}|)$

$O(|\mathbf{t}|)$

Query

$O(\text{size of MM})$

$O(\# \text{ values ever added/deleted})$

# PAX

Add

time

stabilization

time LSX

stabilization LSX

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

Delete

$$O(|\mathbf{t}| \log (\text{size of MM}))$$

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

$$O(|\mathbf{t}|)$$

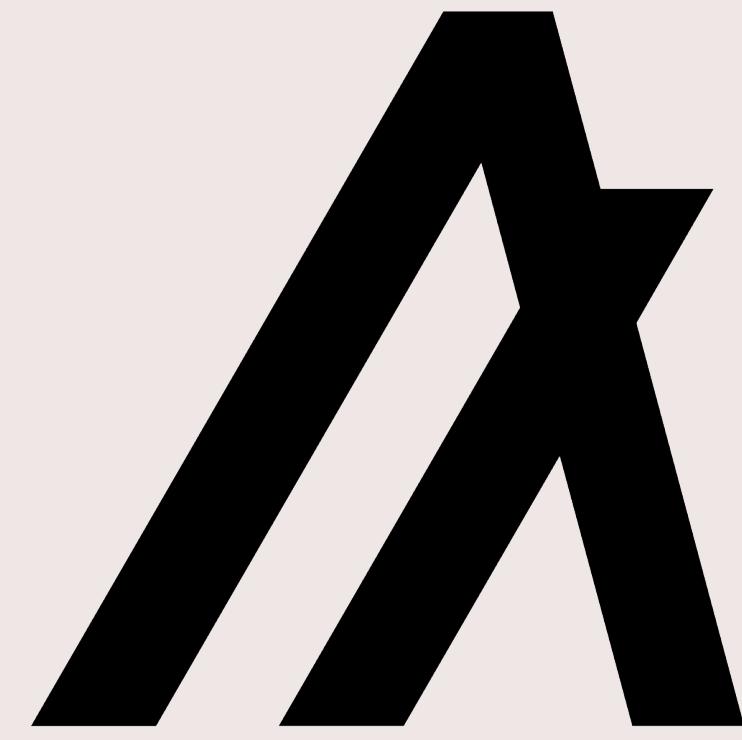
Query

$$O(\text{size of MM})$$

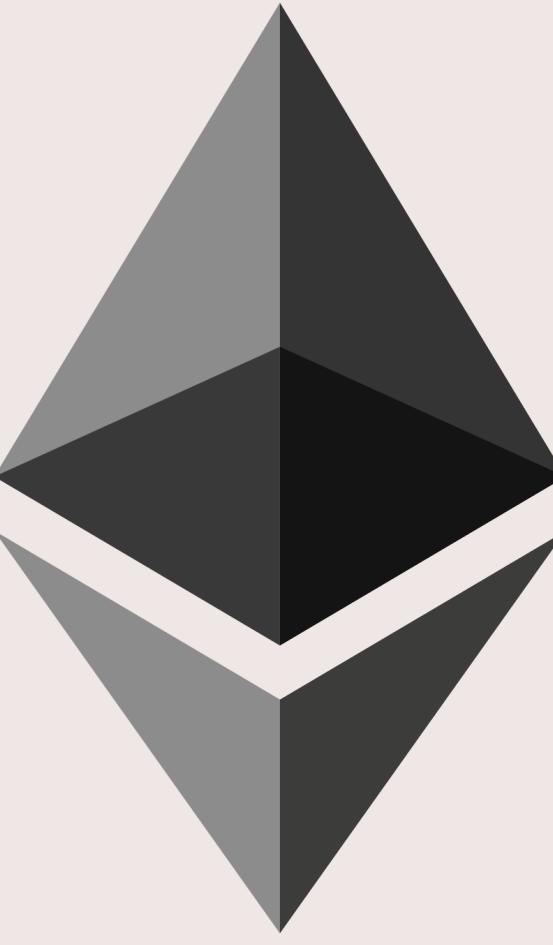
$O(\# \text{ values ever added/deleted})$

- What are Multi-Maps (MMs)
- What are Encrypted Multi-Maps (EMMs)
- How to store EMMs on Blockchains
  - LSX
  - TRX
  - PAX
- Real World Deployment

# Real World Deployments

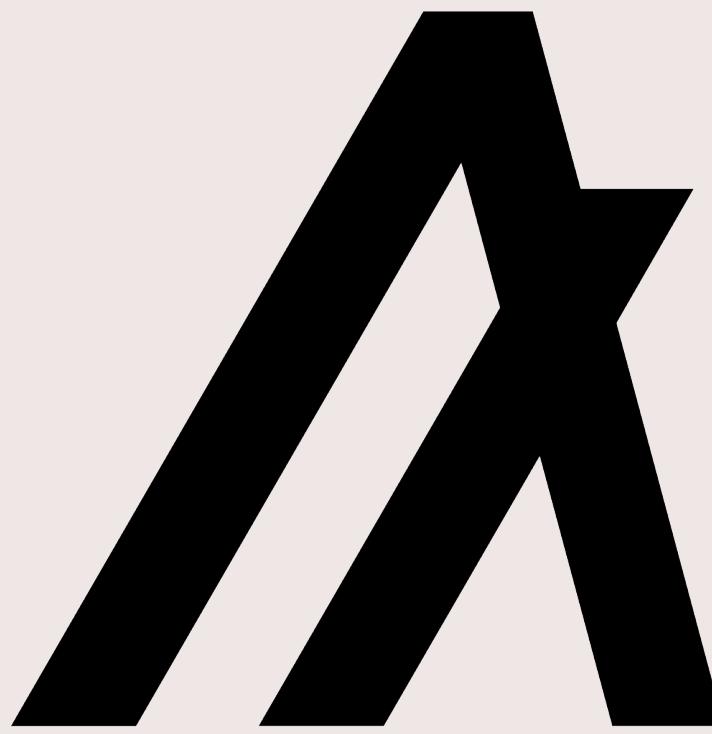


Algorand

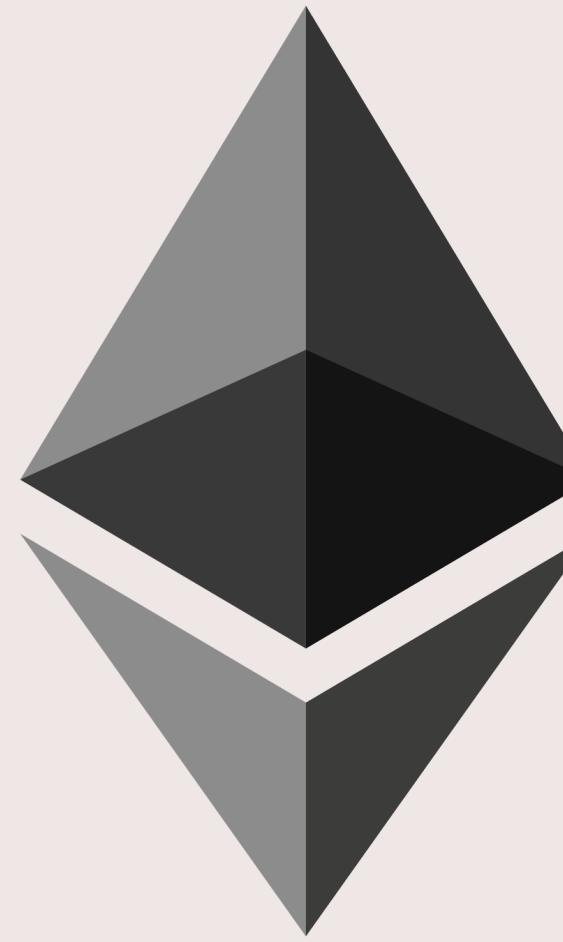


Ethereum

# Real World Deployments



Algorand

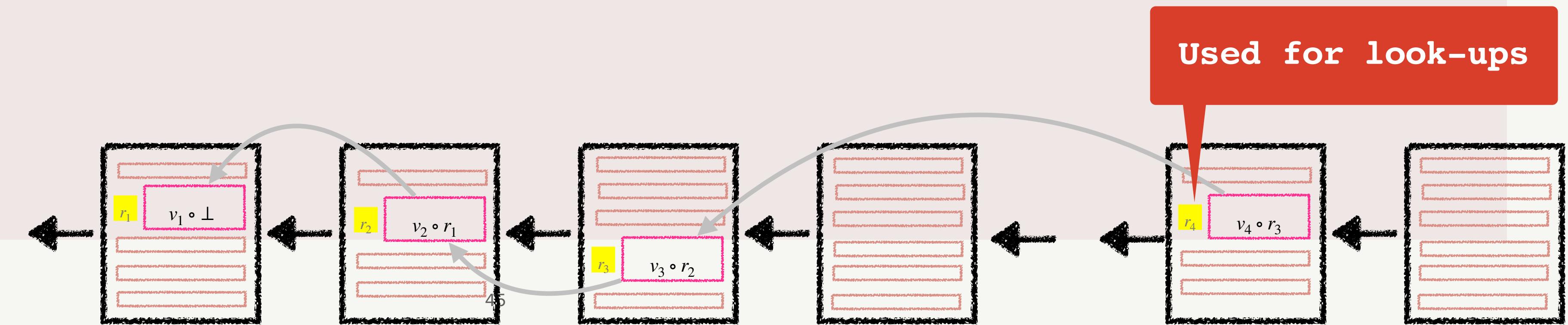


Ethereum

Some things to think about ...

①

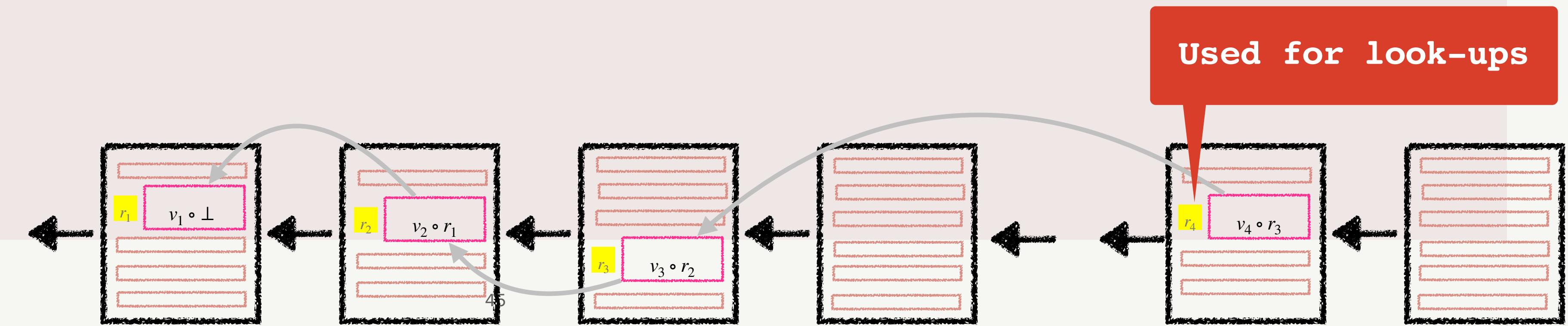
# What should we use as addresses?



①

# What should we use as addresses?

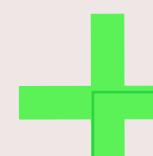
TX hashes



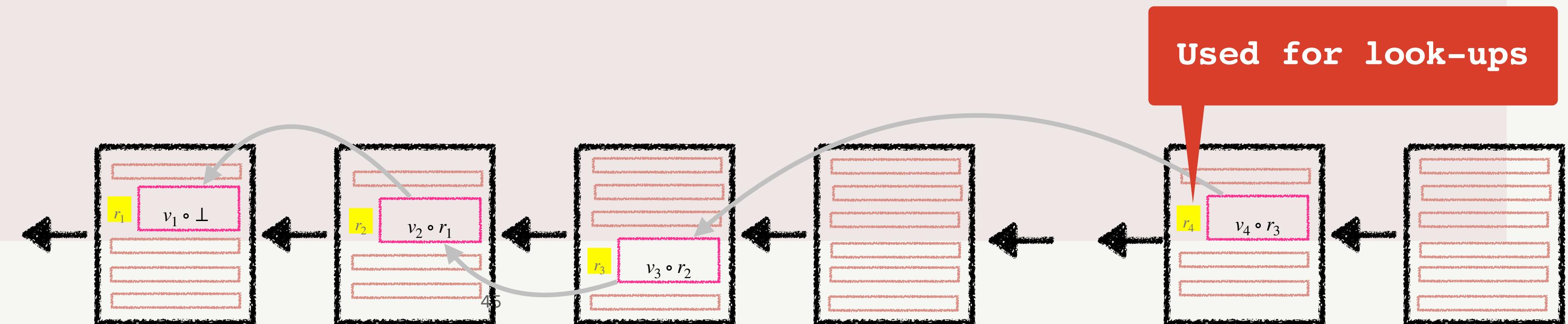
1

# What should we use as addresses?

TX hashes



- All writes can be sent in parallel
  - LSX = TRX
  - Stabilization complexity =  $O(1)$



1

# What should we use as addresses?

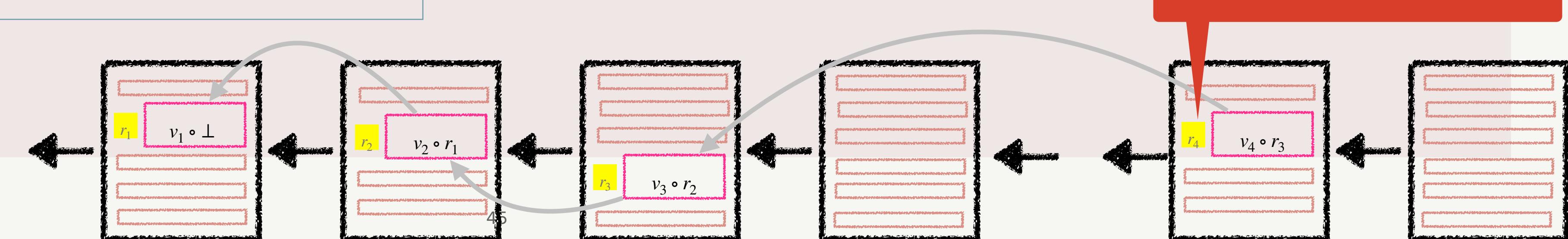
TX hashes



- All writes can be sent in parallel
  - LSX = TRX
  - Stabilization complexity =  $O(1)$



- Might require database indexing
- Many BCs do not support this



1

# What should we use as addresses?

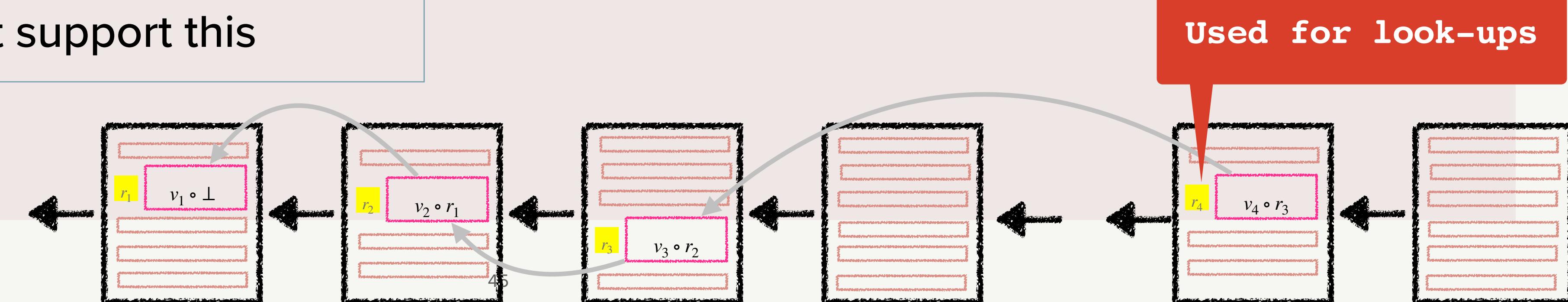
TX hashes

Block numbers + TX hashes



- All writes can be sent in parallel
  - LSX = TRX
  - Stabilization complexity =  $O(1)$

- Might require database indexing
- Many BCs do not support this



1

# What should we use as addresses?

TX hashes

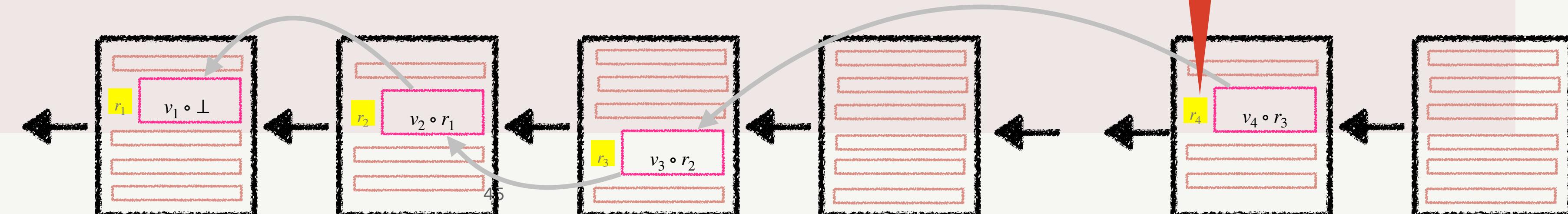
Block numbers + TX hashes

- All writes can be sent in parallel
  - LSX = TRX
  - Stabilization complexity =  $O(1)$

- BCs support fast lookup by block numbers

- Might require database indexing
- Many BCs do not support this

Used for look-ups



1

# What should we use as addresses?

TX hashes

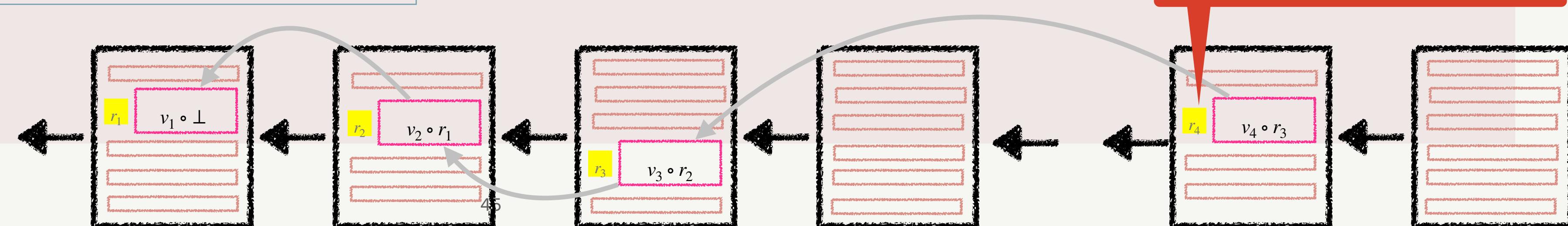
- All writes can be sent in parallel
  - LSX = TRX
  - Stabilization complexity =  $O(1)$

Block numbers + TX hashes

- BCs support fast lookup by block numbers
  - Higher bandwidth required

- Might require database indexing
- Many BCs do not support this

Used for look-ups

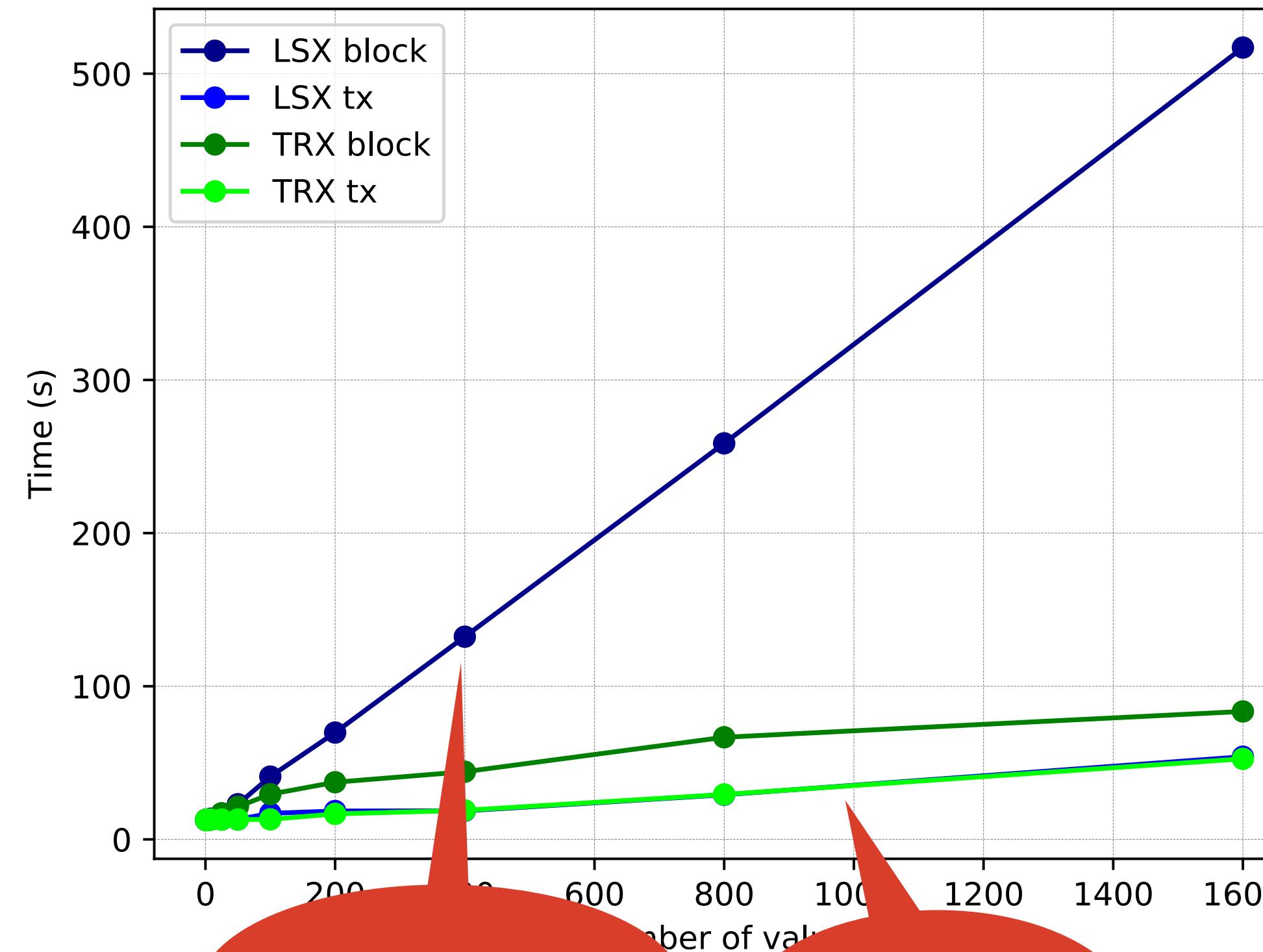


1

# What should we use as addresses?

Add on  
Algorand

- LSX = TRX
- Stabilization con
- Might require data
- Many BCs do not s



LSX (block)

LSX (tx)

Used for look-ups

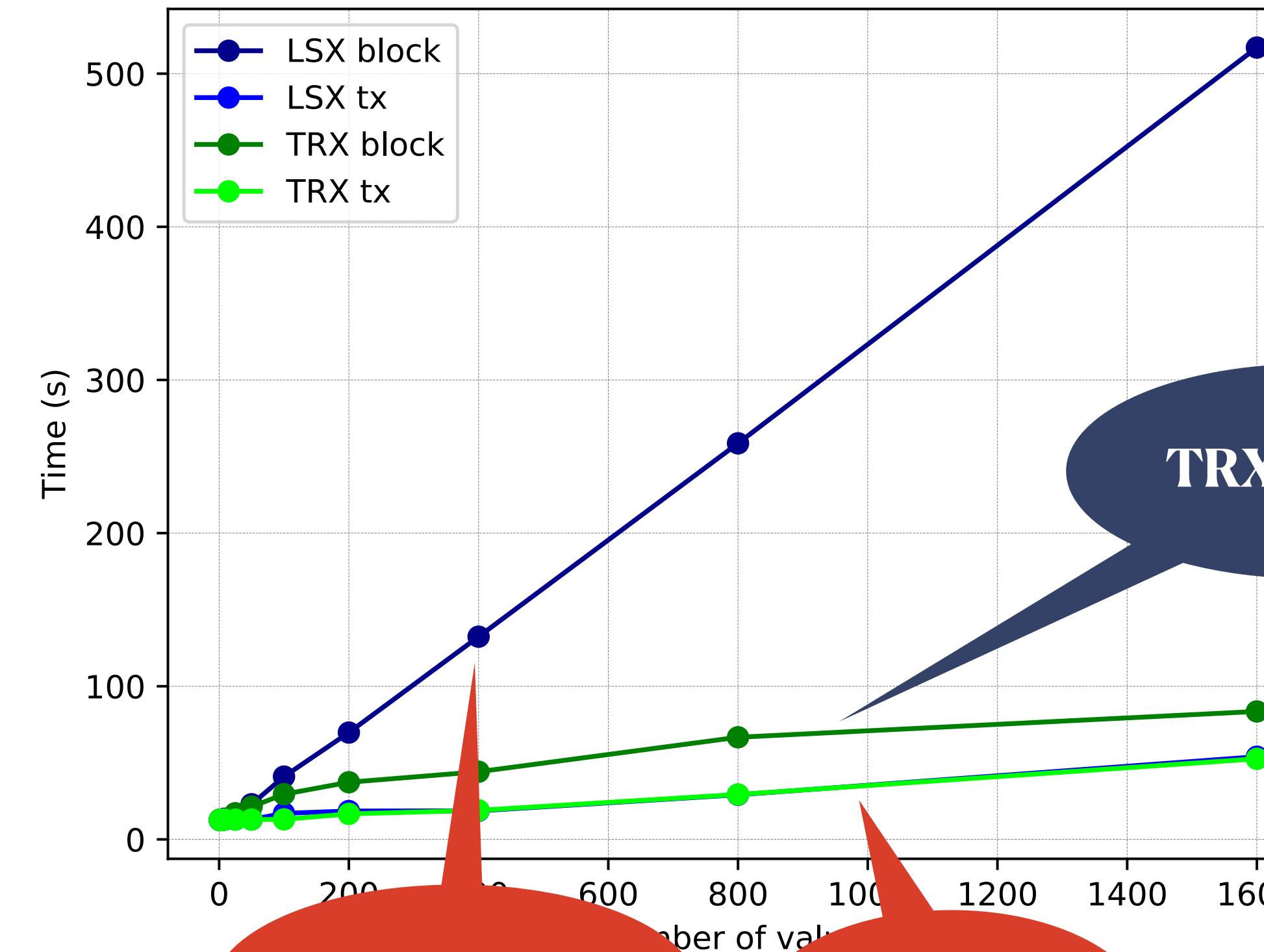


1

# What should we use as addresses?

Add on  
Algorand

- LSX = TRX
- Stabilization con
- Might require data
- Many BCs do not s



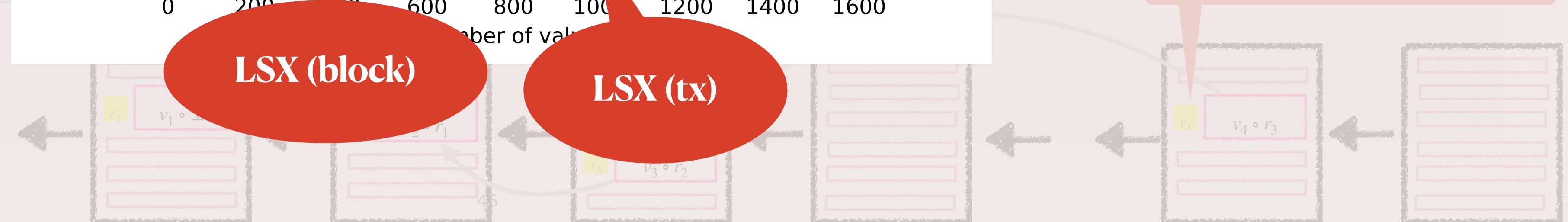
TRX (block)

TRX (tx)

LSX (block)

LSX (tx)

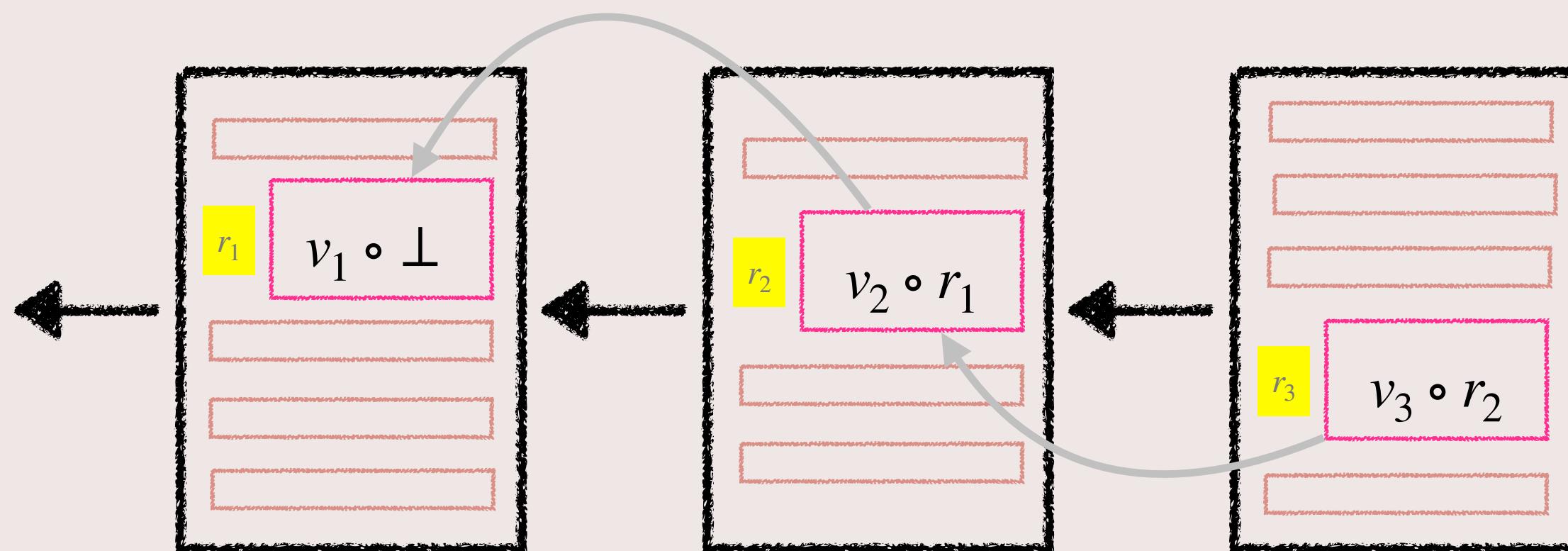
Used for look-ups



# ②

# Packing

Saves time & money



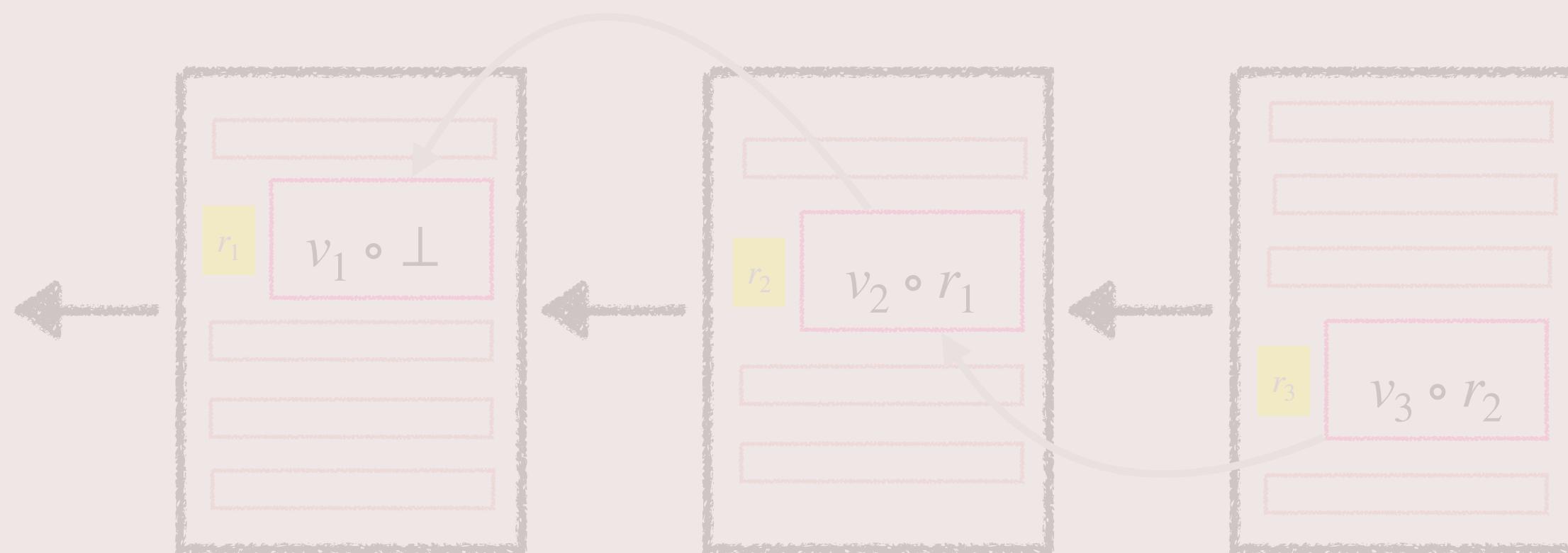
$v_1 \circ v_2 \circ v_3 \perp$

**Store multiple  
values in a tx**

# ②

# Packing

PAX doesn't support packing



$v_1 \circ v_2 \circ v_3 \perp$

Store multiple  
values in a tx

# 2

# Packing

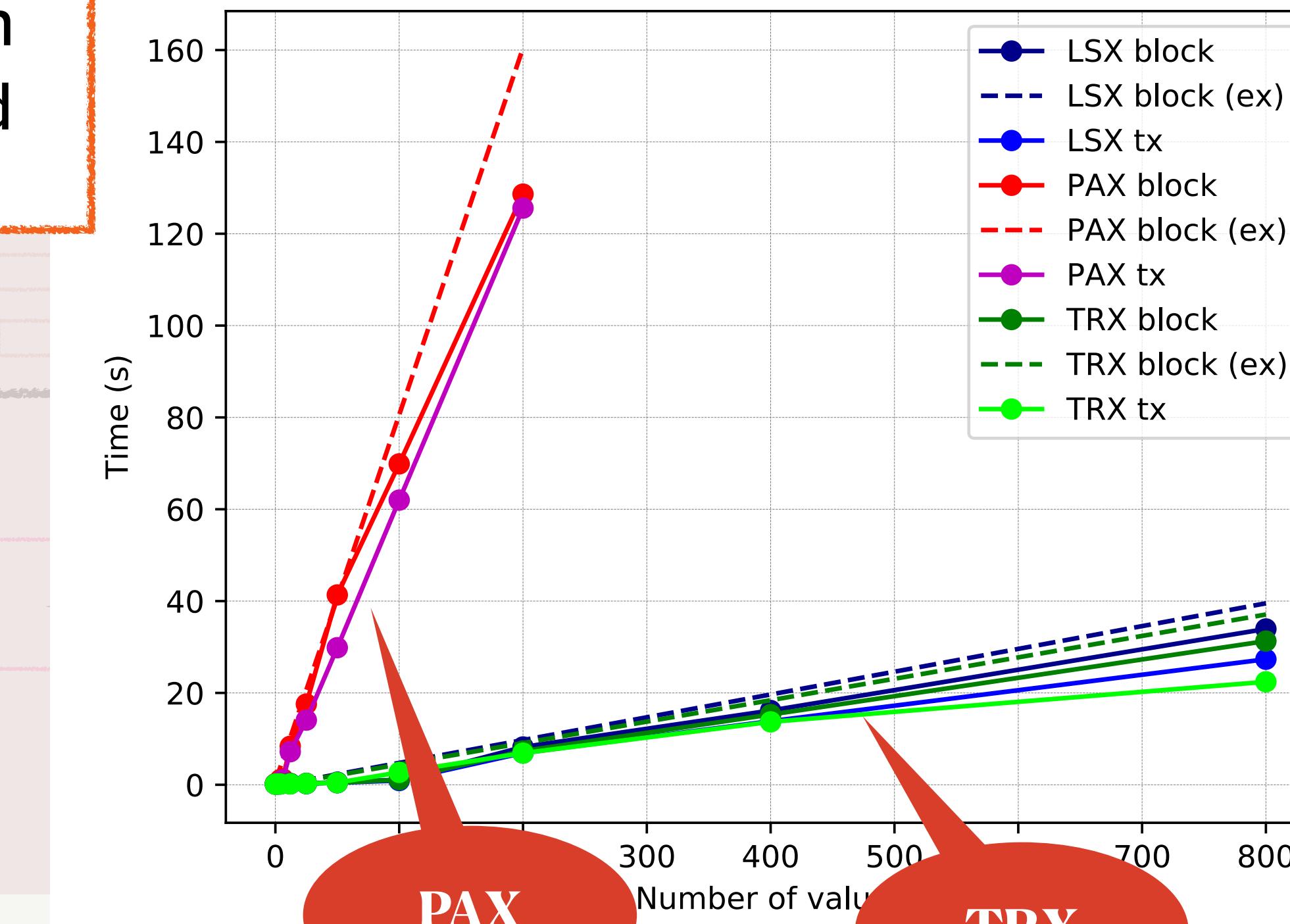
PAX doesn't support packing

Query on  
Algorand

$O(\text{size of MM})$

time PAX

$O(\# \text{ values ever added/deleted})$



# 2

# Packing

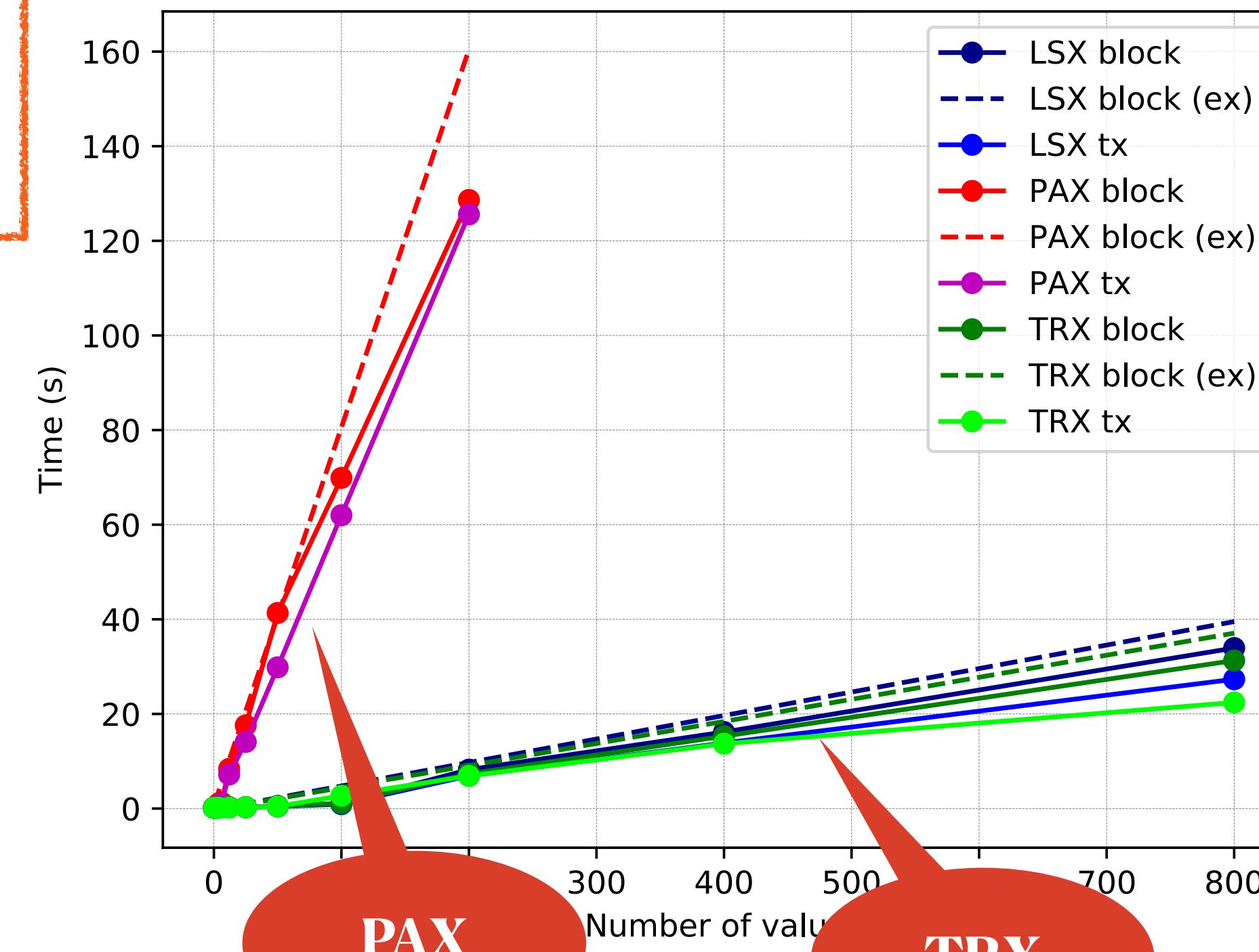
PAX doesn't support packing



Query on  
Algorand

time PAX  
 $O(\text{size of MM})$

time TRX  
 $O(\# \text{ values ever added/deleted})$



PAX

TRX

# 2

# Packing

PAX doesn't support packing



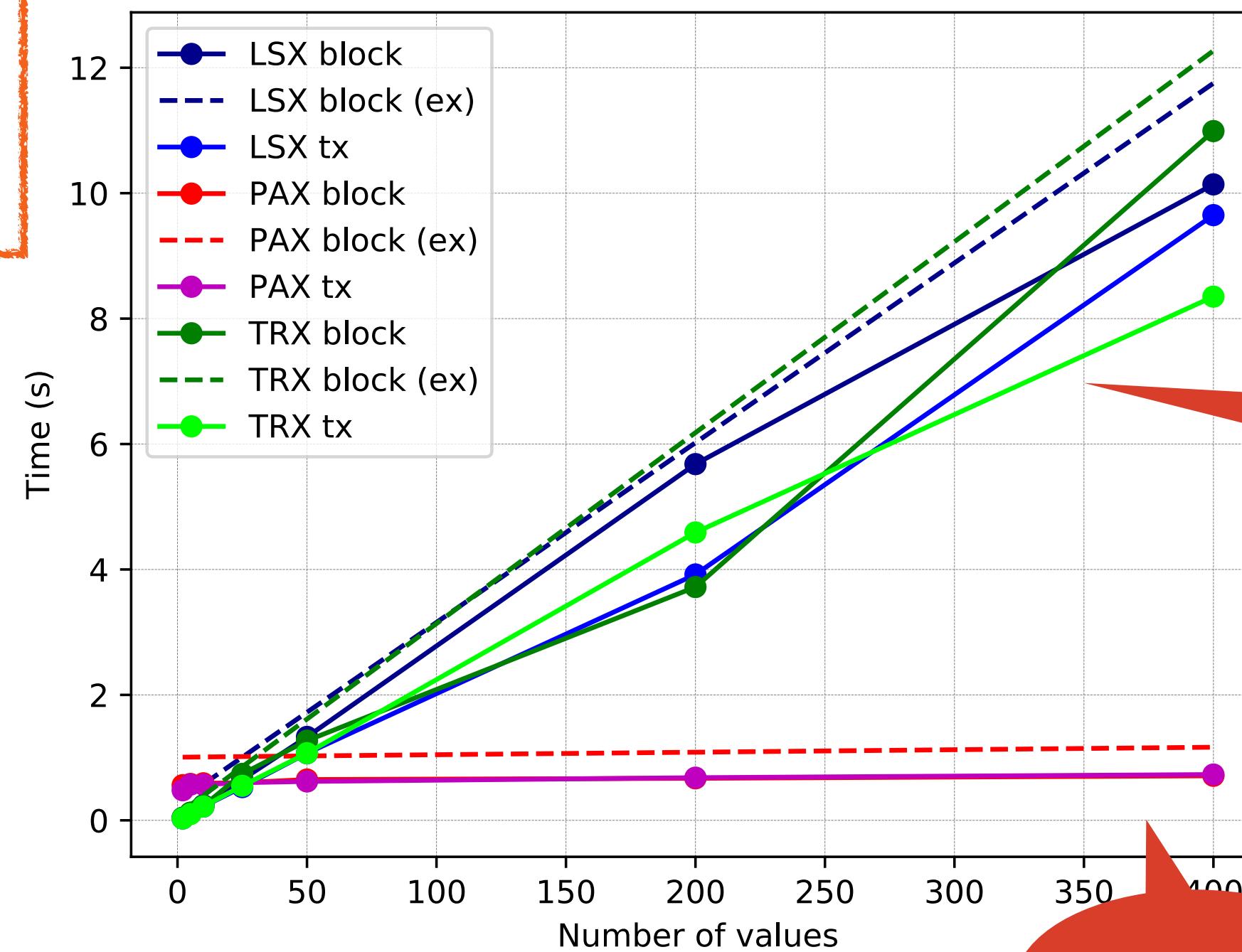
Query on Algorand

(after most values have been deleted)

$O(\text{size of MM})$

time PAX

$O(\# \text{ values ever added/deleted})$



TRX

PAX



