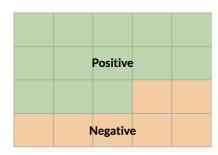
### 1. Probability and Bayes' Rule

You learned about probabilities and Bayes' rule.

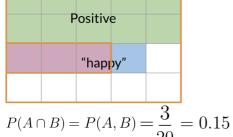
#### Corpus of tweets



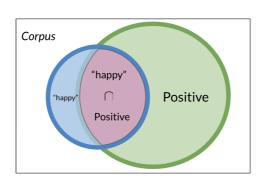
A → Positive tweet

$$P(A) = N_{pos} / N = 13 / 20 = 0.65$$

To calculate a probability of a certain event happening, you take the count of that specific event and you divide by the sum of all events. Furthermore, the sum of all probabilities has to equal 1.



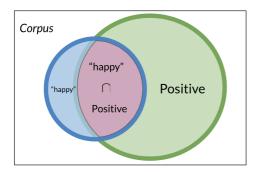
$$P(A \cap B) = P(A, B) = \frac{3}{20} = 0.15$$



To compute the probability of 2 events happening, like "happy" and "positive" in the picture above, you would be looking at the intersection, or overlap of events. In this case red and blue boxes overlap in 3 boxes. So the answer is  $\frac{3}{20}$ .

# 2. Bayes' Rule

Conditional probabilities help us reduce the sample search space. For example given a specific event already happened, i.e. we know the word is happy:



$$P(\text{Positive} | \text{"happy"}) =$$

$$P(\text{Positive} \cap \text{"happy"})$$

$$P(\text{"happy"})$$

Then you would only search in the blue circle above. The numerator will be the red part and the denominator will be the blue part. This leads us to conclude the following:

$$P(\text{Positive} | \text{``happy''}) = \frac{P(\text{Positive} \cap \text{``happy''})}{P(\text{``happy''})}$$
$$P(\text{``happy''} | \text{Positive}) = \frac{P(\text{``happy''} \cap \text{Positive})}{P(\text{Positive})}$$

Substituting the numerator in the right hand side of the first equation, you get the following:

$$P(\text{Positive}|\text{"happy"}) = P(\text{"happy"}|\text{Positive}) \times \frac{P(\text{Positive})}{P(\text{"happy"})}$$

Note that we multiplied by P(positive) to make sure we don't change anything. That concludes Bayes Rule which is defined as:

$$P(X|Y) = P(Y|X)P(X) / P(Y)$$

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$

#### 3. Naïve Bayes Introduction

- It is "naïve" because it assumes that all the features for classification are independent (which in reality may not be)
- Still works nicely for sentiment analysis

To build a classifier, we will first start by creating conditional probabilities given the following table:

| Positive 1                           | tweets   |  |  |
|--------------------------------------|--|--|--|
| I am happy because I am learning NLP |  |  |  |
| I am hap                             | ppy, not sad.  |  |  |
|                                      | Negative tweets  |  |  |
|                                      | I am sad, I am not learning NLP<br>I am sad, not happy |  |  |

| word               | Pos | Neg |
|--------------------|-----|-----|
| 1                  | 3   | 3   |
| am                 | 3   | 3   |
| happy              | 2   | 1   |
| because            | 1   | 0   |
| learning           | 1   | 1   |
| NLP                | 1   | 1   |
| sad                | 1   | 2   |
| not                | 1   | 2   |
| N <sub>class</sub> | 13  | 12  |

• Note: The sum for "Neg" should also 13

This allows us compute the following table of probabilities:

| word     | Pos  | Neg  |
|----------|------|------|
|          | 0.24 | 0.25 |
| am       | 0.24 | 0.25 |
| happy    | 0.15 | 0.08 |
| because  | 0.08 | 0    |
| learning | 0.08 | 0.08 |
| NLP      | 0.08 | 0.08 |
| sad      | 0.08 | 0.17 |
| not      | 0.08 | 0.17 |
|          |      |      |

Once you have the probabilities, you can compute the likelihood score as follows:

Tweet: I am happy today; I am learning.

$$\prod_{i=1}^{m} \frac{P(w_i|pos)}{P(w_i|neg)} = \frac{0.14}{0.10} = 1.4 > 1$$

$$\frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.14}{0.10} * \frac{0.20}{0.20} * \frac{0.20}{0.20} * \frac{0.10}{0.10}$$

| word     | Pos  | Neg  |
|----------|------|------|
|          | 0.20 | 0.20 |
| am       | 0.20 | 0.20 |
| happy    | 0.14 | 0.10 |
| because  | 0.10 | 0.05 |
| learning | 0.10 | 0.10 |
| NLP      | 0.10 | 0.10 |
| sad      | 0.10 | 0.15 |
| not      | 0.10 | 0.15 |

- The product formulae is the Naïve Bayes inference condition rule for binary classification
- The 1.4 calculation is for the word "happy"
- Words that have occurred equally in Pos and Neg do not have any effect on even new (unseen) sentences, even if those words occur a lot of time in the new unseen sentence.

A score greater than 1 indicates that the class is positive, otherwise it is negative.

# 4. Laplacian Smoothing

• Laplacian smoothing to avoid P(wi|class) = 0 case

We usually compute the probability of a word given a class as follows:

$$P\left(\mathbf{w_{i} \mid \ class} \; 
ight) = rac{\mathrm{freq}\left(\mathbf{w_{i}}, \, \mathrm{class} \; 
ight)}{\mathrm{N_{class}}} \quad \ \mathrm{class} \; \in \left\{ \; \mathrm{Positive}, \, \mathrm{Negative} \; 
ight\}$$

However, if a word does not appear in the training, then it automatically gets a probability of 0, to fix this we add smoothing as follows

$$P\left(\mathbf{w_i} \mid \text{class}\right) = \frac{\text{freq}(\mathbf{w_i}, \text{class}) + 1}{(N_{\text{class}} + V)}$$

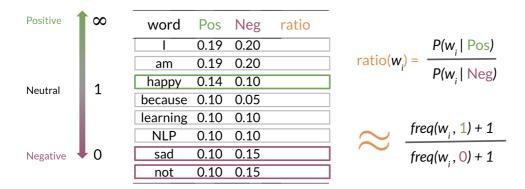
Note that we added a 1 in the numerator, and since there are V words to normalize, we add V in the denominator.

N\_{class}: frequency of all words in class

V: number of unique words in vocabulary

### 5. Log Likelihood, Part 1

To compute the log likelihood, we need to get the ratios and use them to compute a score that will allow us to decide whether a tweet is positive or negative. The higher the ratio, the more positive the word is:



To do inference, you can compute the following:

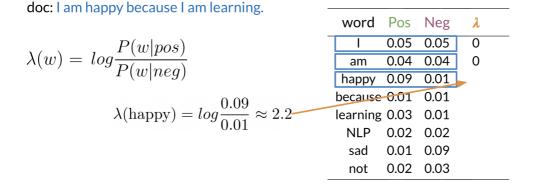
$$rac{P(pos)}{P(neg)}\prod_{i=1}^{m}rac{P(w_i|pos)}{P(w_i|neg)}>1$$

P(pos) / P(neg) 
$$\Pi$$
 i=1 to m [ P(w\_i | pos) / P(w\_i | neg) ] > 1

As m gets larger, we can get numerical flow issues, so we introduce the log, which gives you the following equation:

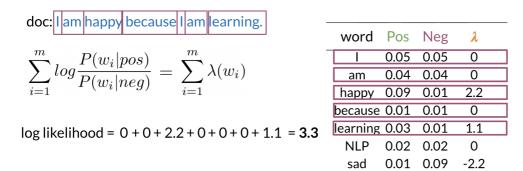
$$\log\left(\frac{P(pos)}{P(neg)}\prod_{i=1}^{n}\frac{P(w_{i}|pos)}{P(w_{i}|neg)}\right)\Rightarrow\log\frac{P(pos)}{P(neg)}+\sum_{i=1}^{n}\log\frac{P(w_{i}|pos)}{P(w_{i}|neg)}$$

The first component is called the log prior and the second component is the log likelihood. We further introduce  $\lambda$  as follows:



#### 6. Log Likelihood, Part 2

Once you computed the  $\lambda$  dictionary, it becomes straightforward to do inference:



As you can see above, since 3.3 > 0, we will classify the document to be positive. If we got a negative number we would have classified it to the negative class.

not

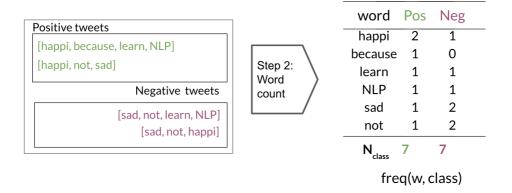
0.02 0.03

-0.4

### 7. Training Naïve Bayes

To train your naïve Bayes classifier, you have to perform the following steps:

- 1. Get or annotate a dataset with positive and negative tweets
- 2. Preprocess the tweets: process\_tweet(tweet)  $\rightarrow$  [w1, w2, w3, ...]:
  - Lowercase
  - Remove punctuation, urls, names
  - Remove stop words
  - Stemming
  - Tokenize sentences
- 3. Compute freq(w, class):



4. Get P(w|pos), P(w|neg)

You can use the table above to compute the probabilities.

5. Get 
$$\lambda(\mathrm{w})$$
  $\lambda(w) = \log rac{P(\mathrm{w}|\mathrm{pos})}{P(\mathrm{w}|\mathrm{neg})}$ 

6. Compute 
$$logprior = \log(P(pos)/P(neg))$$
  $\log prior = \log \frac{D_{pos}}{D_{neg}}$  where  $D_{pos}$  and  $D_{neg}$  correspond to the number of positive and negative documents respectively.

# 8. Testing Naïve Bayes

$$\bullet \quad \text{log-likelihood dictionary } \lambda(w) = log \frac{P(w|pos)}{P(w|neg)} \quad ---$$

$$\begin{array}{l} \bullet \quad logprior = log \frac{D_{pos}}{D_{neg}} = 0 \\ \bullet \quad \text{Tweet: [I] pass, the NLP interview]} \end{array}$$

$$score = -0.01 + 0.5 - 0.01 + 0 + log prior = 0.48$$

$$pred = score > 0$$

| word    | λ     |
|---------|-------|
|         | -0.01 |
| the     | -0.01 |
| happi   | 0.63  |
| because | 0.01  |
| pass    | 0.5   |
| NLP     | 0     |
| sad     | -0.75 |
| not     | -0.75 |
|         |       |

The example above shows how you can make a prediction given your  $\lambda$  dictionary. In this example the logprior is 0 because we have the same amount of positive and negative documents (i.e. log(1) = 0).

# 9. Applications of Naïve Bayes

There are many applications of naive Bayes including:

- Author identification
- Spam filtering
- Information retrieval
- Word disambiguation

This method is usually used as a simple baseline. It's also really fast.

### 10. Naïve Bayes Assumptions

Naïve Bayes makes the independence assumption and is affected by the word frequencies in the corpus. For example, if you had the following:





"It is sunny and hot in the Sahara desert."

"It's always cold and snowy in \_\_\_\_."

In the first image, you can see the word sunny and hot tend to depend on each other and are correlated to a certain extent with the word "desert". Naive Bayes assumes independence throughout. Furthermore, if you were to fill in the sentence on the right, this naive model will assign equal weight to the words "spring, summer, fall, winter".

#### Relative frequencies in corpus



On Twitter, there are usually more positive tweets than negative ones. However, some "clean" datasets you may find are artificially balanced to have to the same amount of positive and negative tweets. Just keep in mind, that in the real world, the data could be much noisier.

# 11. Error Analysis

There are several mistakes that could cause you to misclassify an example or a tweet. For example,

- Removing punctuation
- Removing words

**Tweet:** This is not good, because your attitude is not even close to being nice.

processed\_tweet: [good, attitude, close, nice]

Tweet: My beloved grandmother:(

processed\_tweet: [belov, grandmoth]

Word order

Tweet: I am happy because I did not go.



Tweet: I am(not happy because I did go.



Adversarial attacks

These include sarcasm, irony, euphemisms.