

# 1. Nuclear Force-Solutions

### **Practice Set 1 Solutions**

1. The range of the nuclear force between two nucleons due to the exchange of pions is 1.40fm. If the mass of pion is  $140 \text{MeV/c}^2$  and the mass of the rho-meson is  $770 \text{MeV/c}^2$ , then the range of the force due to exchange of rho-mesons is

**[NET JUNE 2017]** 

**A.** 1.40fm

C. 0.25fm 7 JOUND. 0.18fm 7 C

**Solution:** Range for nuclear force between nucleon will be  $R = c\Delta t = \frac{\hbar c}{mc^2}$  and  $\hbar c = 199 \text{MeVfm}$  $\Rightarrow R = \frac{199 \text{MeV fm}}{770 \frac{\text{MeV}}{.2} \times c^2} \approx 0.25 \text{fm}$ 

2. The reaction  ${}_{1}^{2}D + {}_{1}^{2}D \rightarrow {}_{2}^{4}He + \pi^{0}$  cannot proceed via strong interactions because it violates the conserva-

[ NET/JRF (JUNE-2015)]

a. Angular momentum

b. Electric charge

c. Baryon number

d. Isospin

### Solution:

$$_1D^2 + _1D^2 \rightarrow {}_2\mathrm{He}^4 + \pi^0$$
 (Not conserved)  
 $I: 0 \longrightarrow 0 \rightarrow 1$ 

This isopin is not conserved in above reaction.

3. A deuteron d captures a charged pion  $\pi^-$  in the l=1 state, and subsequently decays into a pair of neutrons (n) via strong interaction. Given that the intrinsic parities of  $\pi^-$ , d and n are -1, +1 and +1 respectively, the spin wavefunction of the final state neutrons is

[NET/JRF (JUNE-2018)]

a. Linear combination of a singlet and a triplet

**b.** Singlet

c. Triplet

d. Doublet

#### **Solution:**

Parity must conserve intersections

$$\pi + d \rightarrow n + n$$

The parity of the initial state is

$$(-1)^{l}P_{\pi}P_{d} = (-1)^{1}(-1)(+1) = +1$$

The parity of the final state is

$$(-1)^l P_n P_n = (-1)^l (+1)(+1) = (-1)^l = 1$$
 :  $l = 0, 2, \dots$ 

word or phrase

So the correct answer is **Option** (b)

- 4. The strong nuclear force between a neutron and a proton in a zero orbital angular momentum state is denoted by  $F_{np}(r)$ , where r is the separation between them. Similarly,  $F_{nn}(r)$  and  $F_{pp}(r)$  denote the forces between a pair of neutrons and protons, respectively, in zero orbital momentum state. Which of the following is true on average if the inter-nucleon distance is 0.2 fm < r < 2 fm?
  - **a.**  $F_{np}$  is attractive for triplet spin state, and  $F_{nn}$ ,  $F_{pp}$  are always repulsive
  - **b.**  $F_{nn}$  and  $F_{np}$  are always attractive and  $F_{pp}$  is repulsive in the triplet spin state
  - **c.**  $F_{pp}$  and  $F_{np}$  are always attractive and  $F_{nn}$  is always repulsive
  - d. All three forces are always attractive

**Solution:** Inside the nucleus the interaction between neutron neutron and newtran-proton is always attractive due to nuclear force whereas between proton-proton it is repulsive due to coulombic interaction: Thus  $F_{nn}$  and  $F_{np}$  are always attractive and  $F_{pp}$  is repulsive So the correct answer is **Option (b)** 

Answer key				
Q.No.	Answer	Q.No.	Answer	
1	0.25	2		
3	b	4	b	
5		6		

# **Practice Set-2 Solutions**

1. The ground state wavefunction of deuteron is in a superposition of *s* and *d* states. Which of the following is NOT true as a consequence?

[GATE 2010]

- A. It has a non-zero quadruple moment
- **B.** The neutron-proton potential is non-central
- **C.** The orbital wavefunction is not spherically symmetric
- **D.** The Hamiltonian does not conserve the total angular momentum

Solution: So the correct answer is Option (d)

2. Deuteron has only one bound state with spin parity 1<sup>+</sup>, isospin 0 and electric quadrupole moment 0.286efm<sup>2</sup>. These data suggest that the nuclear forces are having

[GATE 2012]

- A. Only spin and isospin dependence
- **B.** No spin dependence and no tensor components
- C. Spin dependence but no tensor components
- **D.** Spin dependence along with tensor components

Solution: So the correct answer is **Option** (d)

3. Which of the following statements is NOT correct?

[GATE 2016]

- **A.** A deuteron can be disintegrated by irradiating it with gamma rays of energy 4MeV.
- **B.** A deuteron has no excited states.
- **C.** A deuteron has no electric quadrupole moment.
- **D.** The  ${}^{1}S_{0}$  state of deuteron cannot be formed.

**Solution:** So the correct answer is **Option** (c)

Answer key				
Q.No.	Answer	Q.No.	Answer	
1	d	2	d	
3	С	4		
5		6		

