

COMP6453 Assignment I: Q4

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July 9, 2025

Q4)

a) The maximum number of calls to the SHA-1 function is if we take the first 40 bits (5 bytes) and try to find a collision for $H(m_1) = H(m_k)$. This is the worst case scenario and 2^{40} calls will be required

b) But By using the birthday attack we can use the fact that the actual bits of security will be $2^{n/2}$ where n is the number of bits, until we find a collision with probability of 50%. Thus we will need to compare 2^{20} bits instead.

c) Pseudocode:

Algorithm 1 Find Colliding Hash

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1: Define function:
2:   Define HashTable {hash table stores (hash, message) pairs}
3:    $(m_1, h_1) \leftarrow \text{get40BitsFromSha1}()$ 
4:   didFindHash  $\leftarrow$  HashTable.get( $h_1$ )
5:   if didFindHash  $\neq$  null then
6:     HashTable.add( $h_1$ )
7:   else if  $m_1 == \text{val}$  then
8:     skip
9:   else
10:     $m_2 \leftarrow$  didFindHash
11:   end if
12:   return ( $h_1, m_1, m_2$ )
```
