

A Study on Mental State Classification using EEG-based Brain-Machine Interface

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Abstract—This work aims to find discriminative EEG-based features and appropriate classification methods that can categorise brainwave patterns based on their level of activity or frequency for mental state recognition useful for human-machine interaction. By using the Muse headband with four EEG sensors (TP9, AF7, AF8, TP10), we categorised three possible states such as relaxing, neutral and concentrating based on a few states of mind defined by cognitive behavioural studies. We have created a dataset with five individuals and sessions lasting one minute for each class of mental state in order to train and test different methods. Given the proposed set of features extracted from the EEG headband five signals (alpha, beta, theta, delta, gamma), we have tested a combination of different features selection algorithms and classifier models to compare their performance in terms of recognition accuracy and number of features needed. Different tests such as 10-fold cross validation were performed. Results show that only 44 features from a set of over 2100 features are necessary when used with classical classifiers such as Bayesian Networks, Support Vector Machines and Random Forests, attaining an overall accuracy over 87%.

Keywords—*EEG, brain-machine interface, machine learning, mental states classification*

I. INTRODUCTION

The ability to autonomously detect mental states, whether cognitive or affective, is useful for multiple purposes in many domains such as robotics, health care, education, neuroscience, etc. The importance of efficient human-machine interaction mechanisms increases with the number of real life scenarios where smart devices, including autonomous robots, can be applied. One of the many alternatives that can be used to interact with machines is through superficial brain activity signals. These signals, called electroencephalograms or EEG for short, convey information regarding the voltage measured by electrodes (dry or wet) placed around the scalp of an individual. In addition to regular non-invasive electroencephalography there can also be found invasive alternatives which can monitor brain activity placing the electrodes directly inside the skull of the subject [35]. This technique is known as intracranial electroencephalography (iEEG). Despite iEEG can yield better signal acquisition, it is invasive and therefore more complex to apply. Extracranial electroencephalography techniques include

wearable and non-wearable technologies. The fact that extracranial devices used to acquire EEG signals are non-invasive, are becoming easier to wear, and their price is decreasing widens the range of applications for which they are suitable.

A major challenge in brain-machine interface applications is inferring how momentary mental states are mapped into a particular pattern of brain activity. One of the main issues of classifying EEG signals is the amount of data needed to properly describe the different states, since the signals are complex, non-linear, non-stationary, and random in nature. The signals are considered stationary only within short intervals, that is why the best practice is to apply short-time windowing technique in order to detect local discriminative features to meet this requirement. The paper at hand focuses on selecting a subset of highly discriminative features and comparing to state-of-the-art classification methods that can categorise EEG signals into different mental states, taking into consideration the performance in terms of accuracy and computational cost. The application considered herein is to distinguish among three different mental states (e.g. relaxed, neutral and highly concentrated) of an individual using an EEG device with dry electrodes that can interface a range of applications, such as to control the movement of a robot.

The remainder of the paper proceeds as follows. Related works are summarised in section II. The experimental setup, including information regarding the device used, and details about the data acquisition are described in section III. The methods tested to perform feature selection and the criteria used to compare the different classifiers are presented in section IV. Preliminary results are presented in section V. A discussion on the conclusions drawn from the experimental results is provided in section VI.

II. RELATED WORK

Statistical features derived from EEG data are commonly used alongside machine learning techniques to classify mental states [18], [19]. These nominal states can then be used for finite points of control as a Brain-Computer Interface. A Muse headband has been recognised by neuroscientists for its effectiveness and relatively low cost as well as its accuracy

effects of a relaxed or concentrative mental state. Finally, for concentration, the subjects were instructed to follow the “shell game” in which a ball was hidden under one of three cups, which were then switched, the task was to try and follow which cup hid the ball. Future work arises in the implementation of a standard experiment for each state, for proper comparison to similar experiment. After a short amount of time into the stimulus starting, as to not gather data with an inaccurate class, the EEG data from the Muse Headband was automatically recorded for sixty seconds. The data was observed to be streaming at a variable frequency within the range of 150 - 270 Hz. BlueMuse [5] was used for interfacing the device to a computer, and Muselsl [6] was used to convert the Muse signals to MicroVolts and record the data into a preliminary dataset ready for feature extraction. Fig 2. shows a live stream of EEG data, blinking can be seen in the troughs of TP9 and TP10 (forehead sensors). At each point in the data stream (150 - 270 Hz), all signals were recorded along with a UNIX timestamp which was further used for down sampling the data to produce a uniform stream frequency. The measured voltages on the graph can be mapped to the EEG placements seen in Fig 1. Before the features extraction we have down sampled the data. The sampling rate was decimated to 200 Hz based on fast Fourier transformations along a given axis. The resampled signal starts at the same value as x , but it is sampled with a spacing of $\text{len}(x) / \text{num} * (\text{spacing of } x)$. Because a Fourier method is used, the signal is assumed to be periodic. This is a realistic down-sampling as the dominant energy is concentrated in the range of 20 - 500Hz, even though the frequency range of the EEG sensor is superior.

IV. METHODS

A. Proposed Set of Features for EEG signals

Feature extraction and classification of EEG signals are core issues in brain computer interface (BCI) applications. One challenging problem when it comes to EEG feature extraction is the complexity of the signal, since it is non-linear, non-stationary, and random in nature. The signals are considered stationary only within short intervals, that is why the best practice is to apply short-time windowing technique to meet this requirement. However, it is still considered an assumption that holds during a normal brain condition. Non-stationary signals can be observed during the change in alertness and wakefulness, during eye blinking, and also during transitions of mental states. Thus, this subsection describes the set of features considered in this work to adequately discriminate different classes of mental states. These features rely on statistical techniques, time-frequency based on fast Fourier transform (FFT), Shannon entropy, max-min features in temporal sequences, log-covariance and others. All features proposed to classify the mental states are computed in terms of the temporal distribution of the signal in a given time window. This slide window is defined as a period of 1 second at 250 Hz, i.e. all features are computed within this time instant. An overlap of 0.5 second is used when moving the window, i.e. the temporal window 1 (w_1) starts at 0 sec. and finishes at 1 sec.; w_2 starts at 1.5 sec. and finishes at 2.5 sec.; w_3 starts at 2 sec. and finishes at 3 sec.; w_4 starts at 2.5 sec. and finishes at 3.5 sec., and so on. Another important point to compute the features is the signals from the EEG Muse headband. Since it returns five types of signal

frequencies $\{\alpha, \beta, \theta, \delta, \gamma\}$, then we compute all proposed set of features for each signal. Thus, the total number of feature values extracted from these signals is 2147 values.

Statistical Features: In order to have a compact representation of the raw sensor data in a given time range, we are using a set of classical statistical features since they are useful with proven efficiency to complement set of multiples features in order to recognise patterns in time series. The statistical features are: (i) given a set of data values $\{x_1, x_2, \dots, x_N\}$ acquired in each temporal window, the mean value $\mu = \frac{1}{N} \sum_{i=1}^N x_i$ of that sequence is computed; (ii) the standard deviation $\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2}$; (iii) statistical moments of 3rd and 4th order, which gives us the skewness to measure the asymmetry of the data, and also the kurtosis to measure the peakedness of the probability distribution of the data, respectively. The statistical moments employed are computed as follows:

$$y = \frac{\mu^k}{\sigma^k}, \quad (1)$$

$$\mu^k = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^k, \quad (2)$$

where μ^k is the $k = \{3^{\text{rd}}, 4^{\text{th}}\}$ moment about the mean and $y = \{\text{skewness}, k = 3; \text{kurtosis}, k = 4\}$. Another type of statistical features computed was the autocorrelation of the signals at each time window for each of the five signals from the EEG. The correlation of the signal with a delayed copy of itself as a function of delay was employed similarly to [22] and [23], where the implementation details and parameters are described.

Max, Min and Derivatives: Given a time window of 1 sec., the maximum and minimum values are computed to increase the diversity of the features types. Derivatives are also computed as temporal features. For each time window, we split the time window by 2, such $w/2 = 0.5$ sec. and $w = 1$ sec., resulting in two sequences of data at ~ 125 Hz, then we compute:

$$uv = \frac{\mu^w - \mu^{w/2}}{2}, \quad (3)$$

where w and $w/2$ indicates the first and second half of the sequence of data in a time window of 1 sec. The same strategy is employed to get the derivative given the *max* and *min* features in sub time windows:

$$\text{max}_t = \frac{\text{max}^w - \text{max}^{w/2}}{2}, \quad (4)$$

$$\text{min}_t = \frac{\text{min}^w - \text{min}^{w/2}}{2}. \quad (5)$$

The next temporal features are extracted after splitting the initial time window of one second into 4 batches of 0.25 sec. each. Then we computed the mean, max and min values of each batch, $\{\mu_1, \mu_2, \mu_3, \mu_4\}$, $\{\text{max}_1, \text{max}_2, \text{max}_3, \text{max}_4\}$ and $\{\text{min}_1, \text{min}_2, \text{min}_3, \text{min}_4\}$. Then we compute the 1D Euclidean distance among all mean values, $\delta\mu_{12} = |\mu_1 - \mu_2|$, $\delta\mu_{13} = |\mu_1 - \mu_3|$, $\delta\mu_{14} = |\mu_1 - \mu_4|$, $\delta\mu_{23} = |\mu_2 - \mu_3|$, $\delta\mu_{24} = |\mu_2 - \mu_4|$, $\delta\mu_{34} = |\mu_3 - \mu_4|$, the same for the minimum and maximum values, so that in the end we got 18 features based on distances. Using the four mean values, and the four max and four min values, and adding the previous 18, we got 30 features for each

signal in the short time window, so that counting the 5 signals we have 150 temporal features per second.

Log-covariance features: Given the previous 150 temporal features, we then discard the last 6 features in order to attain 144 features, so that we could build a 12×12 square matrix to compute the log-covariance as follows:

$$lcM = U(\logm(cov(M))), \quad (6)$$

where lcM is a resulting vector containing the upper triangular elements (78 features) of the matrix after computing the matrix logarithm over the covariance matrix M ; $U(\cdot)$ is a function to return the upper triangular elements; $\logm(\cdot)$ is the matrix logarithm function; and the covariance matrix is given by $cov(M) = cov_{ij} = 1/N \sum_k (x_{ik} - \mu_i)(x_{jk} - \mu_j)$. The rationale behind of log-covariance is the mapping of the convex cone of a covariance matrix to the vector space by using the matrix logarithm so that it does not lie in Euclidean space, i.e., the covariance matrix space is not closed under multiplication with negative scalars.

Shannon entropy and log-energy entropy: non-linear analysis such as Shannon entropy has proven its efficiency in signal processing and time series since randomness of non-linear data is well embodied by calculating entropies over the time series. Entropy is an uncertainty measure and in brain-machine interface applications, it is used to measure the level of chaos of the system, since it is a non-linear measure quantifying the degree of complexity of the data. In information theory, the Shannon entropy is given by:

$$h = -\sum_j S_j \times \log(S_j), \quad (7)$$

where h is a feature computed in every time window of 1 sec. and S_j is each element (normalized) of this temporal window. Then, given the same time window, we split into two to compute the log-energy entropy as follows:

$$loge = \sum_i \log(S_i^2) + \sum_j \log(S_j^2), \quad (8)$$

where i represents an index for the elements of the first sub window (0 - 0.5 sec.) and j represents an index for the second sub window (0.5 - 1 sec.).

Frequency domain: The FFT is an advantageous method to analyse the spectrum of a given time-series. At every time window we compute it as follows:

$$X_k = \sum_{n=0}^{N-1} S_n^t e^{-i2\pi k \frac{n}{N}}, \quad k = 0, \dots, N-1. \quad (9)$$

Accumulative features as energy model: An accumulative value was obtained frame-by-frame given a time window, for each individual feature, duplicating the number of features. We compute the difference between the values of the current frame to the previous frame and accumulate it over time as follows:

$$y_{icum}^t = \begin{cases} y_i^t, & t = 1. \\ \sum_{z=2}^t (y_i^z - y_i^{z-1})^2, & t > 1 \end{cases}, \quad (10)$$

where y_{icum}^t is the resulting energy model for the current time instant given a specific type of feature y_i^k , $i = \{1, \dots, N\}$ at a time instant z representing a specific frame within a time window.

B. Feature Selection Algorithms

Feature selection aims to remove data which has no useful application and only serves to unneededly increase the demand for resources. Five datasets were generated using different algorithms. Each retained the same data points, but which had a reduced number of attributes selected by the algorithm. The evaluators used were as follows:

1. *OneR*: calculates error rate of each prediction based on one rule and selects the lowest risk classification [24].
2. *Information Gain*: assigns a worth to each individual attribute by measuring the information gain with respect to the class (difference of entropy) [25].
3. *Correlation*: measures the correlation of the attribute and class via their *Pearson's* coefficient which is used to rank attributes' worth comparable to all others. [26].
4. *Symmetrical Uncertainty*: measures the uncertainty of an attribute with respect to the class and bases selection on lower uncertainties [27].
5. *Evolutionary Algorithm*: creates a population of attribute subsets and ranks their effectiveness with a fitness function to measure their predictive ability of the class. At each generation, solutions are bred to create offspring, and weakest solutions are killed off in a tournament of fitness [34].

C. Machine Learning Algorithms

As a benchmark, a ZeroR classifier was first run on each dataset. This simplistic classifier chooses one single class to apply to all of the data to reduce inaccurate classifications, it is expected that an accuracy of one third is achieved with a fair distribution of the three mental states. Two models were trained on Bayes Theorem, a formula of conditional probability based on hypothesis H and evidence E . The theorem states that the probability of the hypothesis being true before evidence $P(H)$ is related to the probability of the hypothesis after reading the evidence $P(H|E)$ and is given as follows [29]:

$$P(H|E) = \frac{P(E|H)P(H)}{\sum_j P(E|H)P(H)}. \quad (11)$$

Naivety arises due to the unverified assumption of non-consideration of the relationships between the absence of attributes. A Bayesian Network (Bayes Net) model was also trained. This method generates a probabilistic graphical model via representing probabilities of variables to classes on a Directed Acyclic Graph (DAG) [28] as follows:

$$P(C^{t-1:t-T} | X^{t:t-T}) = \frac{1}{\beta} \prod_{k=t}^{t-T} P(X^k | C^k) P(C^k). \quad (12)$$

TABLE I. TABLE TO SHOW ACCURACY OF TRAINED MODELS

Dataset	Model Accuracy % (2dp)						
	<i>Naive Bayes</i>	<i>Bayes Net</i>	<i>J48</i>	<i>Random Tree</i>	<i>Random Forest</i>	<i>MLP</i>	<i>SVM</i>
<i>OneR</i>	56.21	<u>73.67</u>	80	<u>76.21</u>	<u>87.16</u>	74.27	61.18
<i>Information Gain</i>	54.2	71.64	76.85	65.02	78.02	72.22	64.1
<i>Correlation</i>	<u>56.3</u>	72.69	77.05	75.85	84.17	80.82	<u>75.24</u>
<i>Symmetrical Uncertainty</i>	51.49	71.41	76.29	74.35	82.96	72.25	60.1
<i>Evolutionary Algorithm</i>	55.04	70.31	<u>80.65</u>	72.62	85.29	<u>80.85</u>	67.65

TABLE II. NUMBER OF ATTRIBUTES SELECTED BY FIVE EVALUATORS OF THE ORIGINAL 2147 STATISTICAL ATTRIBUTES

Attribute Selection Evaluator	Ranker Search Cut-off	No. of attributes selected
OneR	60.0	44
Information Gain	0.5	31
Correlation	0.3	26
Symmetrical Uncertainty	0.25	36
Evolutionary Algorithm	N/A	99

The goal is to infer the current time value of C_t given the data $X_{t:t-T} = \{X_t, X_{t-1}, \dots, X_{t-T}\}$ and the prior knowledge of the class, which is attained by the a-posteriori probability $P(C_t | C_{t-1:t-T}, X_{t:t-T})$. The superscript notation denotes the set of values over a time interval.

Three decision trees were developed. Generated by the C4.5 algorithm [2], a J48 tree splits each decision based on information gain, due to the measure of entropy in a leaf node.

A Random Tree is generated through a stochastic process that will consider a random number of attributes at each node. A Random Forest is the process of generating multiple Random Trees [3]. A Multilayer Perceptron (MLP) model was generated, a feedforward Neural Network in that cycles are not formed by neurons. An MLP was implemented due to its ability to classify data points that are not linearly separable in Euclidean space [30]. A model was also trained using a Support Vector Machine (SVM), which classifies labelled data through a process of supervised learning, where examples are mapped out in space and classification is performed by the closest area in which the unknown class

data falls [31]. In particular, an improved version of Platt's Sequential Minimal Optimization (SMO) was used to train the SVM [32], [33].

V. PRELIMINARY RESULTS

The five generated sets from the original dataset are shown in Table I. Five different algorithms were chosen, and their results ranked by their individual scores. Arbitrary cut off points were implemented where the scores closed in on either 0 or the lowest score present if there were no zero values. The values given are incomparable between algorithms due to their unique methods of giving score. The MLP was given 2000 epochs to train with the number of nodes on layers set to the default "a" setting, dynamically calculated by $n = (\text{attributes} + \text{classes})/2$ for each dataset it was trained on. A Zero Rules classifier was run as a benchmark, and with close to equally distributed data, set a model accuracy of 33.36% on all datasets for comparison. We can observe from when compared to all other classifiers which are not naive. The most effective model was a Random Forest classifier along with the dataset created by the OneR Attribute Selector, which had a high accuracy of 87.16% when classifying the data into one of the three mental states. Preliminary results for each of the datasets and their trained models are presented in Table II. For each test, 10-fold cross validation was used to train the model. All random seeds were set to their default value of 1. Table II that all of the models far outperformed the benchmarks set by the Zero Rules classifier, the lowest being 51.49% (Symmetrical Uncertainty dataset with a Naive Bayes classifier). It is reasonable to assume that the naivety in not considering attribute relationships has led to poorer results.

VI. CONCLUSION

This paper presented a study on mental state classification based on EEG signals, it proposed a set of features using a short-term windowing extracted from five signals from an EEG sensor to categorise three different states: *neutral*, *relaxed* and *concentrated*. A dataset was created using data

from five individuals in sessions lasting one minute for each state. The primary goal of this work was to find appropriate set of features by testing multiple feature selection algorithms and classification models that provide acceptable accuracy performance on the dataset that can be useful for human-machine interaction. From the multiple feature sets and models produced, the most accurate is a Random Forest classifier on an attribute selected by the *OneR* ruleset, with a prediction accuracy of 87.16%. Future work will be focused on comparing our best results with deep learning strategies and implementing a real-time application to: (i) control devices, such as robots; and (ii) detect positive and negative moods useful for applications in mental health care.

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