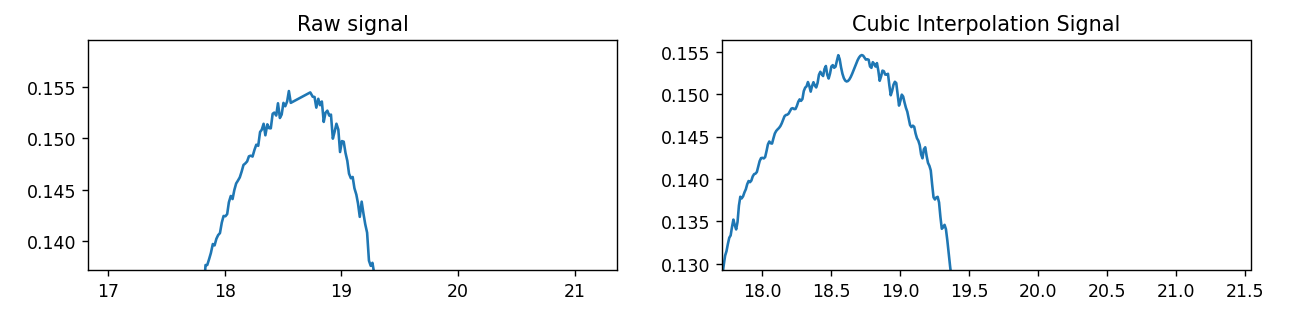
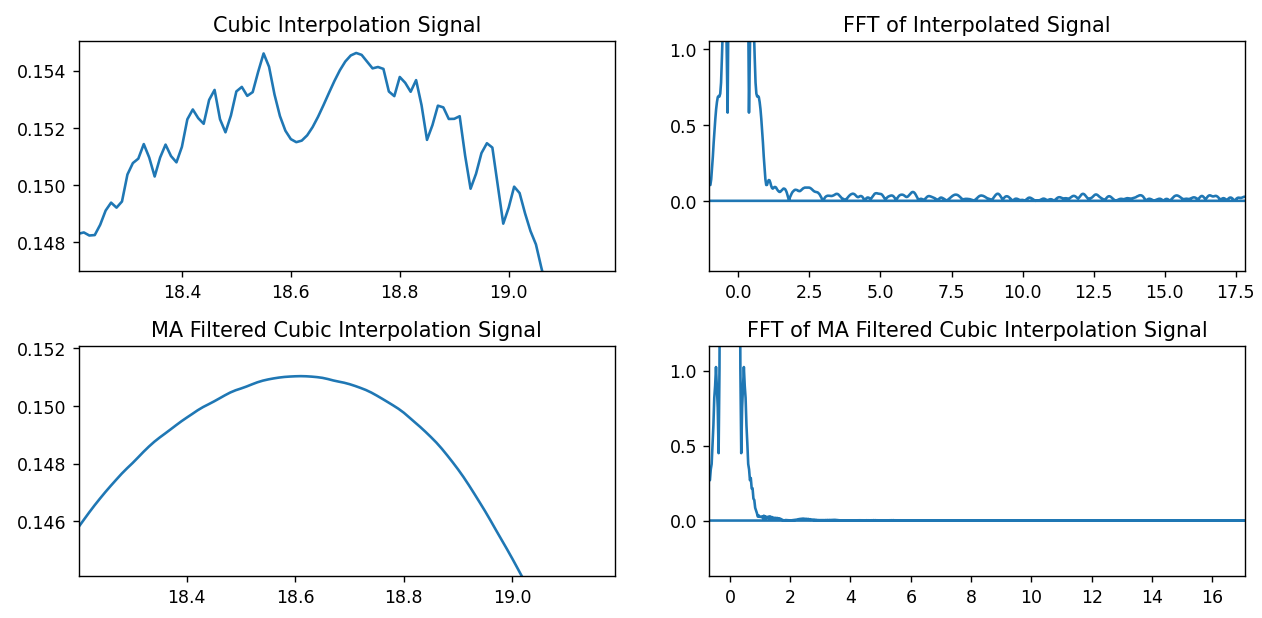
**Mapping Mirror Coordinates to Target Plane Coordinates**

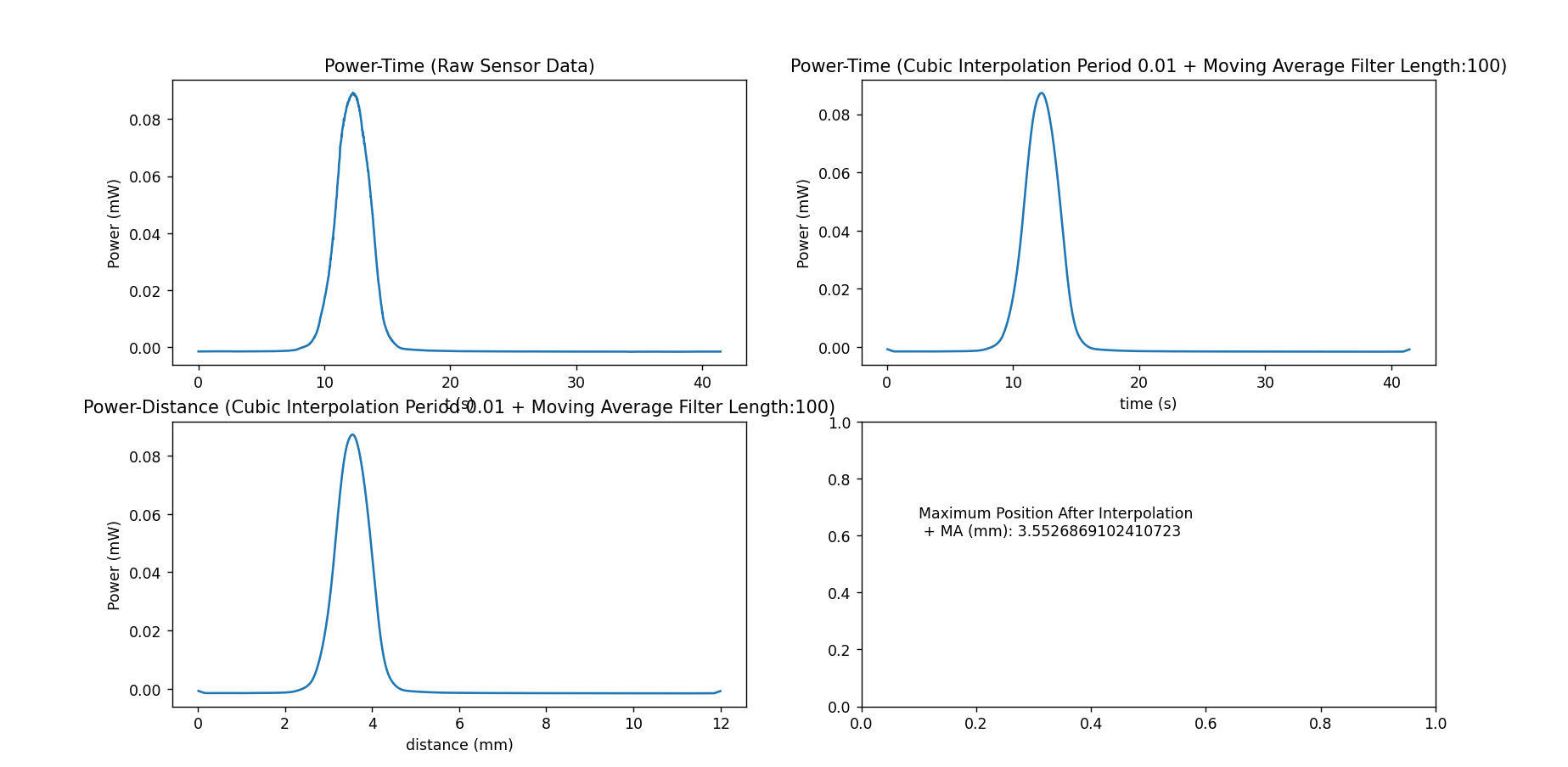
**Measurement System**

Measurements are done with a 2-dimensional servo motor system with a PM400 power meter attached. Measurements are performed by pointing the laser to a specified target position and then sweeping the power meter in a linear trajectory. Power recordings are recorded with recording times and plotted to find the instance with maximum power. This point gives the center position of the laser. Power measurements are performed by a Python script which has a loop with a period of around 0.01s. This sampling period is not constant throughout the measurements and might deviate from 0.01s. For this reason, after the measurement, cubic interpolation is performed to get a uniformly sampled signal.

****

Interpolation solves the nonuniform sampling problem. Obtained signal still has noise in it which might alter the maximum position. To remove the noise a low pass filter in the form of a moving average filter is applied. The figure below depicts the signal before and after the low pass filter. High-frequency noise components are removed from the signal while keeping the original signal mostly intact. This operation produced a smoother signal which is more suitable for peak finding operation.

****The recorded power signal is plotted with respect to distance in order to find the position of the laser’s center. This method gives the position of the laser relative to the initial position of the servo motor. The figure below shows the power levels with respect to time and position. Position with maximum power is written in the fourth graph in millimeters.



Measurements are performed with different parameters such as the distance between the mirror and target plane, different sweep locations.

**Horizontal Measurements D=410mm (actual distance 425mm)**

Table 1: Distance between mirror and target plane: 410mm. Mirror input y coordinate: -5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input x (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | -5 | 2.322 | -3.096 |
| -2.5 | -5 | 2.853 | -2.565 |
| -2 | -5 | 3.372 | -2.046 |
| -1.5 | -5 | 3.868 | -1.550 |
| -1 | -5 | 4.392 | -1.026 |
| -0.5 | -5 | 4.905 | -0.513 |
| 0 | -5 | 5.418 | 0 |
| 0.5 | -5 | 5.921 | 0.503 |
| 1 | -5 | 6.446 | 1.028 |
| 1.5 | -5 | 6.923 | 1.505 |
| 2 | -5 | 7.427 | 2.009 |
| 2.5 | -5 | 7.937 | 2.519 |
| 3 | -5 | 8.452 | 3.034 |

Table 2: Distance between mirror and target plane: 410mm. Mirror input y coordinate: 0mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 0 | 2.278 | -3.089 |
| -2.5 | 0 | 2.792 | -2.575 |
| -2 | 0 | 3.311 | -2.056 |
| -1.5 | 0 | 3.829 | -1.538 |
| -1 | 0 | 4.327 | -1.040 |
| -0.5 | 0 | 4.860 | -0.507 |
| 0 | 0 | 5.367 | 0 |
| 0.5 | 0 | 5.878 | 0.511 |
| 1 | 0 | 6.379 | 1.012 |
| 1.5 | 0 | 6.880 | 1.513 |
| 2 | 0 | 7.392 | 2.025 |
| 2.5 | 0 | 7.880 | 2.513 |
| 3 | 0 | 8.390 | 3.023 |

Table 3: Distance between mirror and target plane: 410mm. Mirror input y coordinate: 5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 5 | 2.391 | -3.097 |
| -2.5 | 5 | 2.909 | -2.579 |
| -2 | 5 | 3.424 | -2.064 |
| -1.5 | 5 | 3.949 | -1.539 |
| -1 | 5 | 4.468 | -1.020 |
| -0.5 | 5 | 4.974 | -0.514 |
| 0 | 5 | 5.488 | 0 |
| 0.5 | 5 | 6.013 | 0.525 |
| 1 | 5 | 6.534 | 1.046 |
| 1.5 | 5 | 7.042 | 1.554 |
| 2 | 5 | 7.547 | 2.059 |
| 2.5 | 5 | 8.052 | 2.564 |
| 3 | 5 | 8.561 | 3.073 |

**Horizontal Measurements D=425mm (actual distance 425mm)**

Table 4: Distance between mirror and target plane: 425mm. Mirror input y coordinate: -5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input x (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | -5 | 6.723 | -2.999 |
| -2.5 | -5 | 7.225 | -2.497 |
| -2 | -5 | 7.727 | -1.995 |
| -1.5 | -5 | 8.218 | -1.504 |
| -1 | -5 | 8.716 | -1.007 |
| -0.5 | -5 | 9.228 | -0.494 |
| 0 | -5 | 9.722 | 0.0 |
| 0.5 | -5 | 10.212 | 0.49 |
| 1 | -5 | 10.695 | 0.973 |
| 1.5 | -5 | 11.191 | 1.469 |
| 2 | -5 | 11.673 | 1.951 |
| 2.5 | -5 | 12.151 | 2.429 |
| 3 | -5 | 12.653 | 2.931 |

Table 5: Distance between mirror and target plane: 425mm. Mirror input y coordinate: 0mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 0 | 6.788 | -2.956 |
| -2.5 | 0 | 7.275 | -2.469 |
| -2 | 0 | 7.777 | -1.967 |
| -1.5 | 0 | 8.289 | -1.455 |
| -1 | 0 | 8.758 | -0.986 |
| -0.5 | 0 | 9.248 | -0.496 |
| 0 | 0 | 9.744 | 0.0 |
| 0.5 | 0 | 10.225 | 0.481 |
| 1 | 0 | 10.711 | 0.967 |
| 1.5 | 0 | 11.207 | 1.463 |
| 2 | 0 | 11.666 | 1.922 |
| 2.5 | 0 | 12.156 | 2.412 |
| 3 | 0 | 12.654 | 2.91 |

Table 6: Distance between mirror and target plane: 425mm. Mirror input y coordinate: 5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 5 | 6.849 | -2.978 |
| -2.5 | 5 | 7.364 | -2.463 |
| -2 | 5 | 7.867 | -1.959 |
| -1.5 | 5 | 8.359 | -1.468 |
| -1 | 5 | 8.843 | -0.984 |
| -0.5 | 5 | 9.34 | -0.487 |
| 0 | 5 | 9.826 | 0.0 |
| 0.5 | 5 | 10.308 | 0.481 |
| 1 | 5 | 10.824 | 0.998 |
| 1.5 | 5 | 11.304 | 1.478 |
| 2 | 5 | 11.793 | 1.967 |
| 2.5 | 5 | 12.279 | 2.453 |
| 3 | 5 | 12.781 | 2.954 |

**Horizontal Measurements D=210mm (actual distance 225mm)**

Table 7: Distance between mirror and target plane: 210mm. Mirror input y coordinate: -5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | -5 | 3.387 | -3.230 |
| -2.5 | -5 | 3.913 | -2.704 |
| -2 | -5 | 4.454 | -2.163 |
| -1.5 | -5 | 5.000 | -1.617 |
| -1 | -5 | 5.533 | -1.084 |
| -0.5 | -5 | 6.082 | -0.535 |
| 0 | -5 | 6.617 | 0 |
| 0.5 | -5 | 7.170 | 0.553 |
| 1 | -5 | 7.700 | 1.083 |
| 1.5 | -5 | 8.233 | 1.616 |
| 2 | -5 | 8.765 | 2.148 |
| 2.5 | -5 | 9.296 | 2.679 |
| 3 | -5 | 9.843 | 3.226 |

Table 8: Distance between mirror and target plane: 210mm. Mirror input y coordinate: 0mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 0 | 3.359 | -3.204 |
| -2.5 | 0 | 3.888 | -2.675 |
| -2 | 0 | 4.416 | -2.147 |
| -1.5 | 0 | 4.954 | -1.609 |
| -1 | 0 | 5.490 | -1.073 |
| -0.5 | 0 | 6.026 | -0.537 |
| 0 | 0 | 6.563 | 0 |
| 0.5 | 0 | 7.104 | 0.541 |
| 1 | 0 | 7.647 | 1.084 |
| 1.5 | 0 | 8.179 | 1.616 |
| 2 | 0 | 8.692 | 2.129 |
| 2.5 | 0 | 9.221 | 2.658 |
| 3 | 0 | 9.754 | 3.191 |

Table 9: Distance between mirror and target plane: 210mm. Mirror input y coordinate: 5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 5 | 3.553 | -3.189 |
| -2.5 | 5 | 4.077 | -2.665 |
| -2 | 5 | 4.604 | -2.138 |
| -1.5 | 5 | 5.158 | -1.584 |
| -1 | 5 | 5.679 | -1.063 |
| -0.5 | 5 | 6.212 | -0.529 |
| 0 | 5 | 6.742 | 0.0 |
| 0.5 | 5 | 7.27 | 0.528 |
| 1 | 5 | 7.807 | 1.065 |
| 1.5 | 5 | 8.343 | 1.601 |
| 2 | 5 | 8.873 | 2.131 |
| 2.5 | 5 | 9.404 | 2.662 |
| 3 | 5 | 9.934 | 3.192 |

**Horizontal Measurements D=225mm (actual distance 225mm)**

Table 10: Distance between mirror and target plane: 225mm. Mirror input y coordinate: -5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | -5 | 4.985 | -3.044 |
| -2.5 | -5 | 5.503 | -2.526 |
| -2 | -5 | 6.007 | -2.023 |
| -1.5 | -5 | 6.505 | -1.524 |
| -1 | -5 | 7.034 | -0.995 |
| -0.5 | -5 | 7.536 | -0.494 |
| 0 | -5 | 8.029 | 0.0 |
| 0.5 | -5 | 8.539 | 0.509 |
| 1 | -5 | 9.045 | 1.016 |
| 1.5 | -5 | 9.546 | 1.517 |
| 2 | -5 | 10.045 | 2.015 |
| 2.5 | -5 | 10.529 | 2.499 |
| 3 | -5 | 11.009 | 2.98 |

Table 11: Distance between mirror and target plane: 225mm. Mirror input y coordinate: 0mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 0 | 4.989 | -2.992 |
| -2.5 | 0 | 5.493 | -2.488 |
| -2 | 0 | 5.999 | -1.982 |
| -1.5 | 0 | 6.49 | -1.491 |
| -1 | 0 | 6.998 | -0.984 |
| -0.5 | 0 | 7.459 | -0.523 |
| 0 | 0 | 7.981 | 0.0 |
| 0.5 | 0 | 8.461 | 0.479 |
| 1 | 0 | 8.952 | 0.971 |
| 1.5 | 0 | 9.485 | 1.503 |
| 2 | 0 | 9.976 | 1.994 |
| 2.5 | 0 | 10.464 | 2.483 |
| 3 | 0 | 10.956 | 2.975 |

Table 12: Distance between mirror and target plane: 225mm. Mirror input y coordinate: 5mm

|  |  |  |  |
| --- | --- | --- | --- |
| **Mirror Input (mm)** | **Mirror Input y (mm)** | **Peak Power Position (mm)** | **Relative Distance (mm)** |
| -3 | 5 | 5.156 | -2.982 |
| -2.5 | 5 | 5.664 | -2.475 |
| -2 | 5 | 6.153 | -1.986 |
| -1.5 | 5 | 6.649 | -1.49 |
| -1 | 5 | 7.154 | -0.985 |
| -0.5 | 5 | 7.64 | -0.498 |
| 0 | 5 | 8.138 | 0.0 |
| 0.5 | 5 | 8.634 | 0.496 |
| 1 | 5 | 9.126 | 0.988 |
| 1.5 | 5 | 9.635 | 1.497 |
| 2 | 5 | 10.126 | 1.988 |
| 2.5 | 5 | 10.609 | 2.47 |
| 3 | 5 | 11.103 | 2.965 |

**Mapping Camera Coordinates to Laser Coordinates**

The coordinates that are used in the laser and the coordinates that are recorded by the camera are rotated and translated versions of each other. In the figure below, the laser is pointed at 30 different positions in a plane 500 cm away from the mirror center. Each point is extracted from the color images and their 3D coordinates are extracted and plotted. Laser points are named and camera points are named . Both matrices have the shape 3xN. To find the mapping between these points, the optimal rotation matrix and optimal translation vector should be found. The mapping is modeled as:

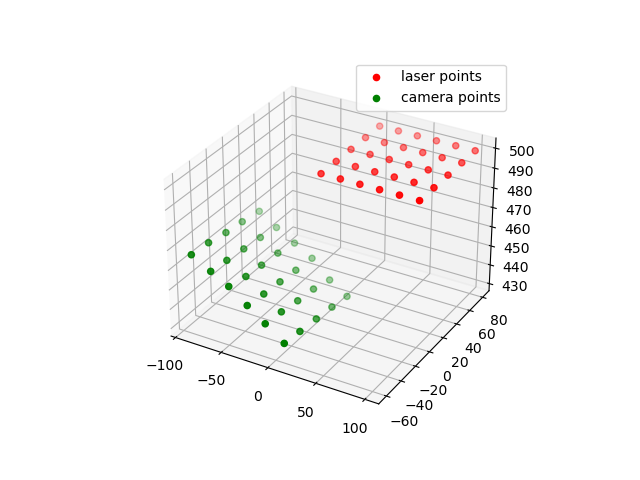


Figure 1: Recording of the same points in laser and camera coordinate systems

Optimal and t are found by the following algorithm [1] [2] [3]:

To find the rotation matrix R

To find the translation vector t

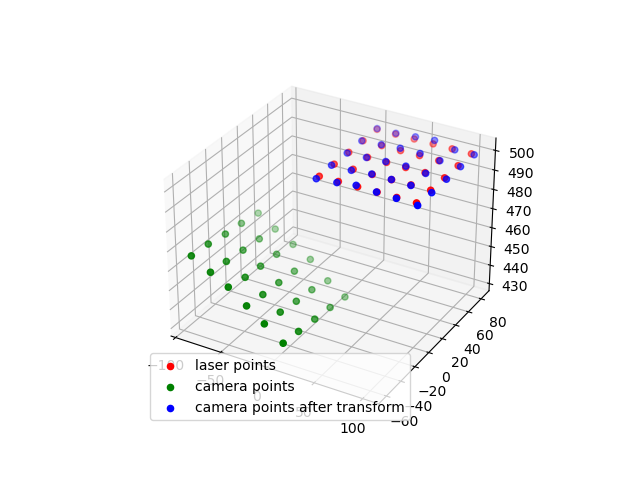


Figure 2: Camera points after the transformation

**Object Tracking Algorithms to Try:**

* ARuCO
* ChromaTag
* Skeleton tracking from Microsoft Kinect
* WHYCon

# References

|  |  |
| --- | --- |
| [1] | C. Simon, "simonensemble," [Online]. Available: https://simonensemble.github.io/posts/2018-10-27-orthogonal-procrustes/. |
| [2] | N. Ho, "FINDING OPTIMAL ROTATION AND TRANSLATION BETWEEN CORRESPONDING 3D POINTS," [Online]. Available: https://nghiaho.com/?page\_id=671. |
| [3] | "Kabsch algorithm," [Online]. Available: https://en.wikipedia.org/wiki/Kabsch\_algorithm. |