

① Let  $m$ : match score  
 $d$ : mismatch penalty  
 $g$ : gap penalty, where  $m > 0$  and  $g, d < 0$

And  $F(i, j)$  is the element in the  $i^{\text{th}}$  row and  $j^{\text{th}}$  column of the matrix.

$$\text{Let } X(i, j) = \begin{cases} F(i-1, j-1) + m & \text{if } F(i, j) = F(i-1, j-1) \\ F(i-1, j-1) + d & \text{if } F(i, j) \neq F(i-1, j-1) \end{cases}$$

$$\text{and } F(i, j) = \max \{ X(i, j), F(i-1, j) + g, F(i, j-1) + g \}$$

$$\text{Consider } F(3, 6) = 3.$$

$$F(3, 6) = \max \{ F(2, 5) + d, F(2, 6) + g, F(3, 5) + g \}$$

If it is  $F(2, 5) + d$ , which is a mismatch, the following must be true:  $0 + d = 3$  where  $d \in \mathbb{Z}^-$ . Since this is not possible, consider a gap penalty:

$$F(2, 6) + g \text{ or } F(3, 5) + g. \text{ So it is either}$$

$$7 + g = 3 \text{ or } 7 = g = 3. \rightarrow \boxed{g = -4}. \text{ That is, } \underline{\text{gap penalty} = -4}.$$

$$\text{Now, consider } F(6, 6) = \max \{ 14 + d, 10 + g, 10 + g \} = 8$$

$$\text{Knowing } g = -4, 10 + g = -6 \neq 8. \text{ Then } 14 + d = 8, \underline{d = -6}$$

So mismatch penalty is -6.

$$\text{Now, consider } F(2, 6) = \max \{ 0 + m, 0 + g, 0 + g \} = 7.$$

$$\text{Knowing } g = -4, 0 - 4 \neq 7. \text{ So } 0 + m = 7. \rightarrow \underline{m = 7}$$

Matching score = 7.

	-	M	I	M	A	G	E	D	I	L
-	0	0	0	0	0	0	0	0	0	0
G	0	0	0	0	0	0	7	3	0	0
A	0	0	0	0	7	3	1	0	0	0
M	0	7	3	7	3	1	0	0	0	0
A	0	3	1	3	14	10	6	2	0	0
E	0	0	0	0	10	8	17	13	9	5
D	0	0	0	0	6	4	13	24	20	16
K	0	0	0	0	2	0	9	20	18	14

M | A | G | E | D  
 M | A | - | E | D

} is the best local  
 alignment.  
 (1st question)

(2)

	-	M	C	G	A	C	M	E	L
-	0	-4	-8	-12	-16	-20	-24	-28	-32
M	-4	-3	-7	-6	-10	-14	-18	-22	-26
C	-8	1	-3	-6	-5	-9	-13	-17	
G	-12	-3	10	6	2	0	4	0	-4
A	-16	-7	6	7	11	7	4	15	9
C	-24	-11	2	4	7	9	5	9	16
M	-28	-15	-2	1	3	6	5	16	16
E	-32	-19	-6	-3	7	2	5	8	10
L									20

$\left. \begin{array}{c} C \\ G \end{array} \right| \begin{array}{c} G \\ G \end{array} \left| \begin{array}{c} M \\ M \end{array} \right| \begin{array}{c} - \\ - \end{array} \left| \begin{array}{c} C \\ C \end{array} \right| \begin{array}{c} M \\ M \end{array} \left| \begin{array}{c} L \\ L \end{array} \right| \begin{array}{c} E \\ - \end{array} \left| \begin{array}{c} L \\ L \end{array} \right\} \text{best alignment of the sequences.}$