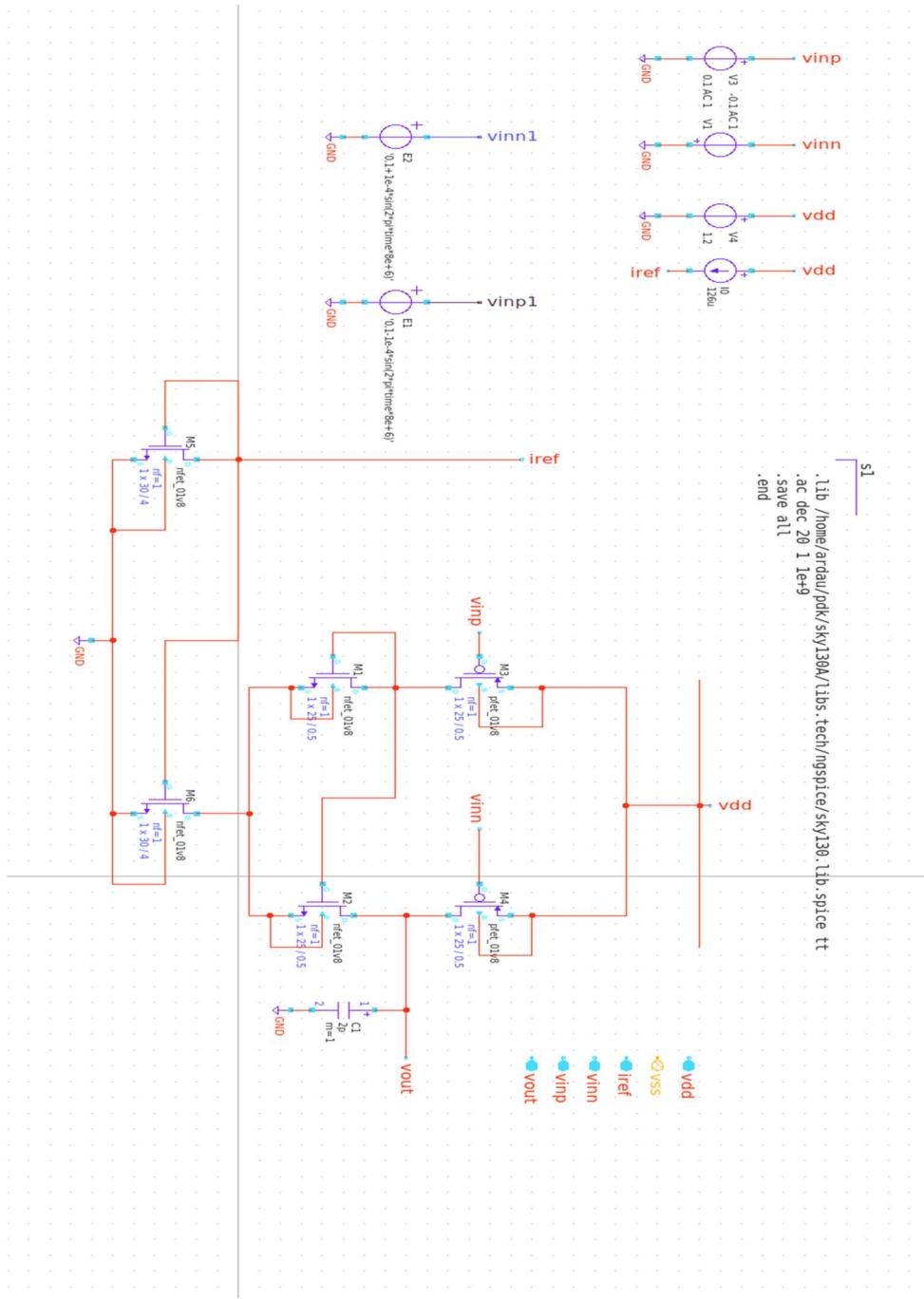
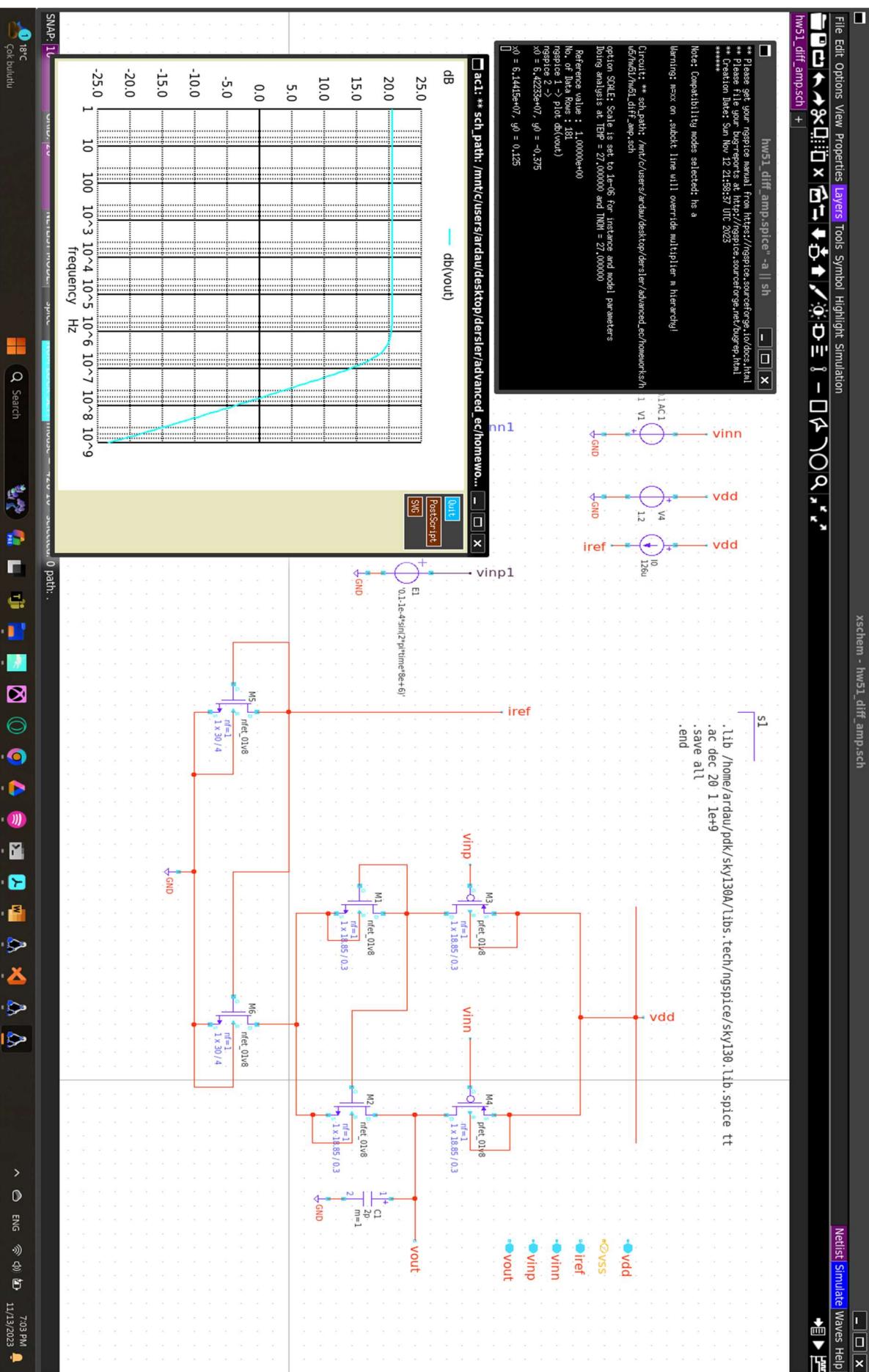


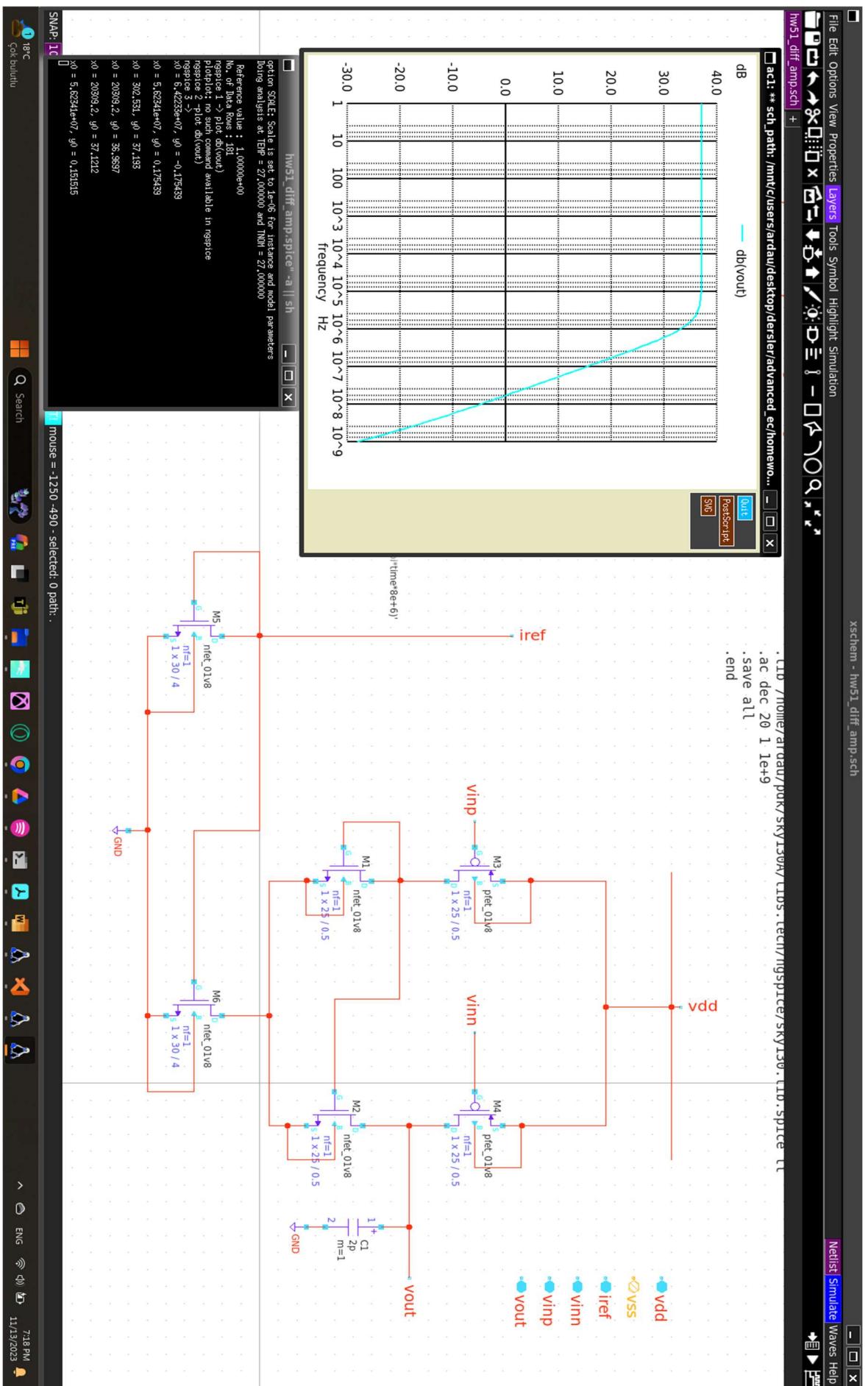
HOMEWORK 5

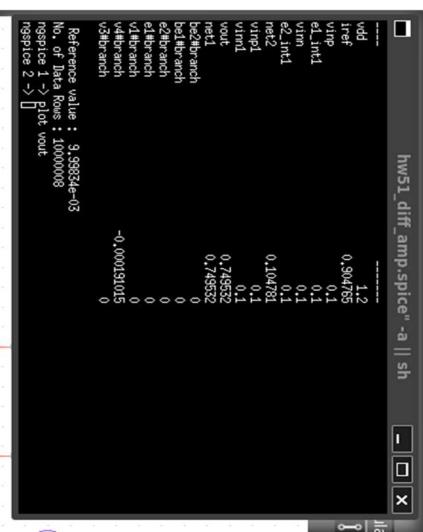
ARDA ÜNAL

1)





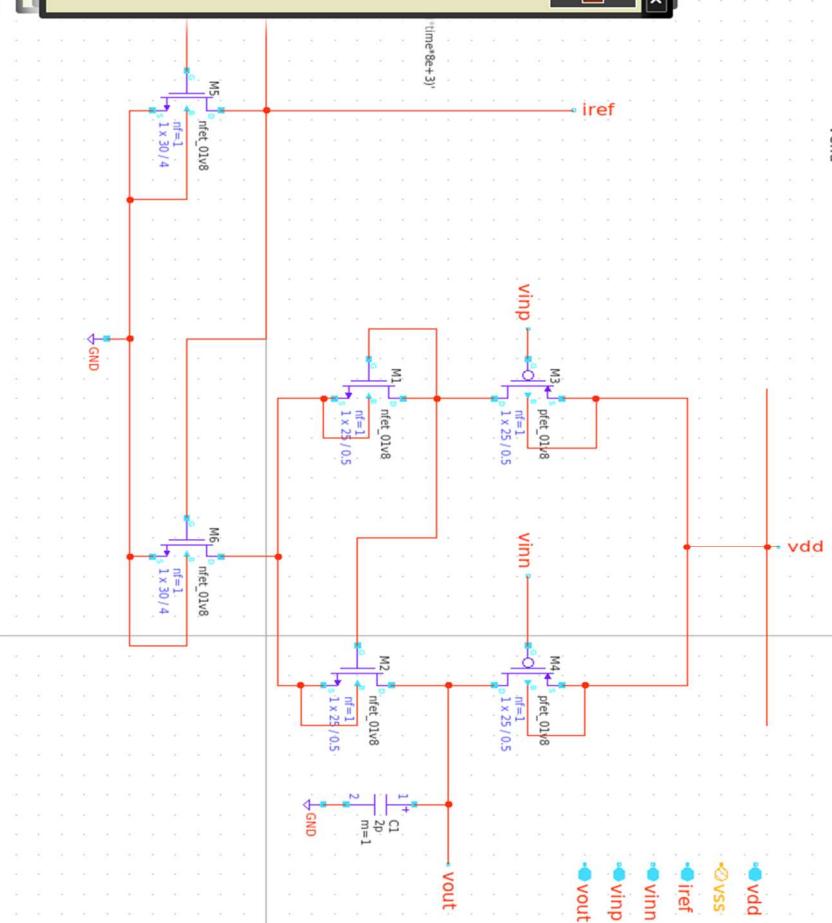
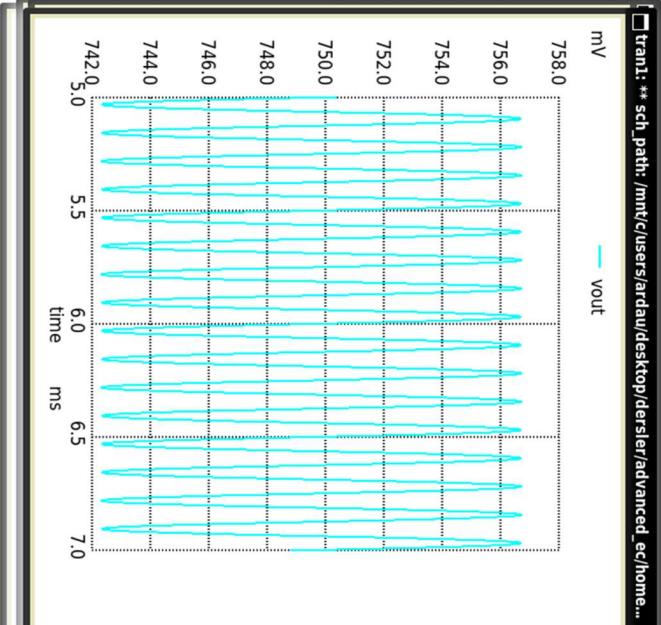




vdd

51

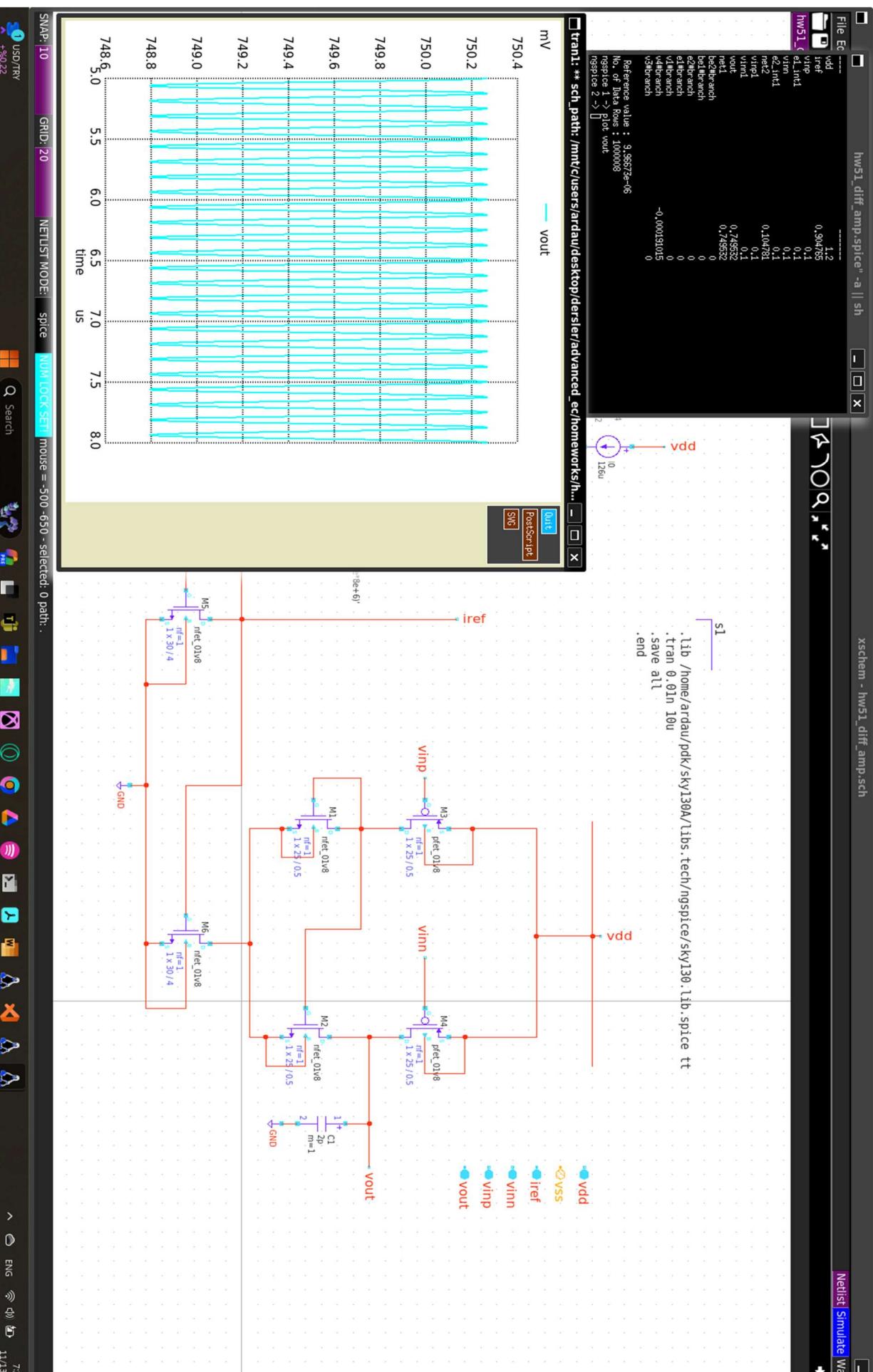
51



Snap-10 GRID-20 NETLIST MODE: spice
Çok bulutlu 17°C     

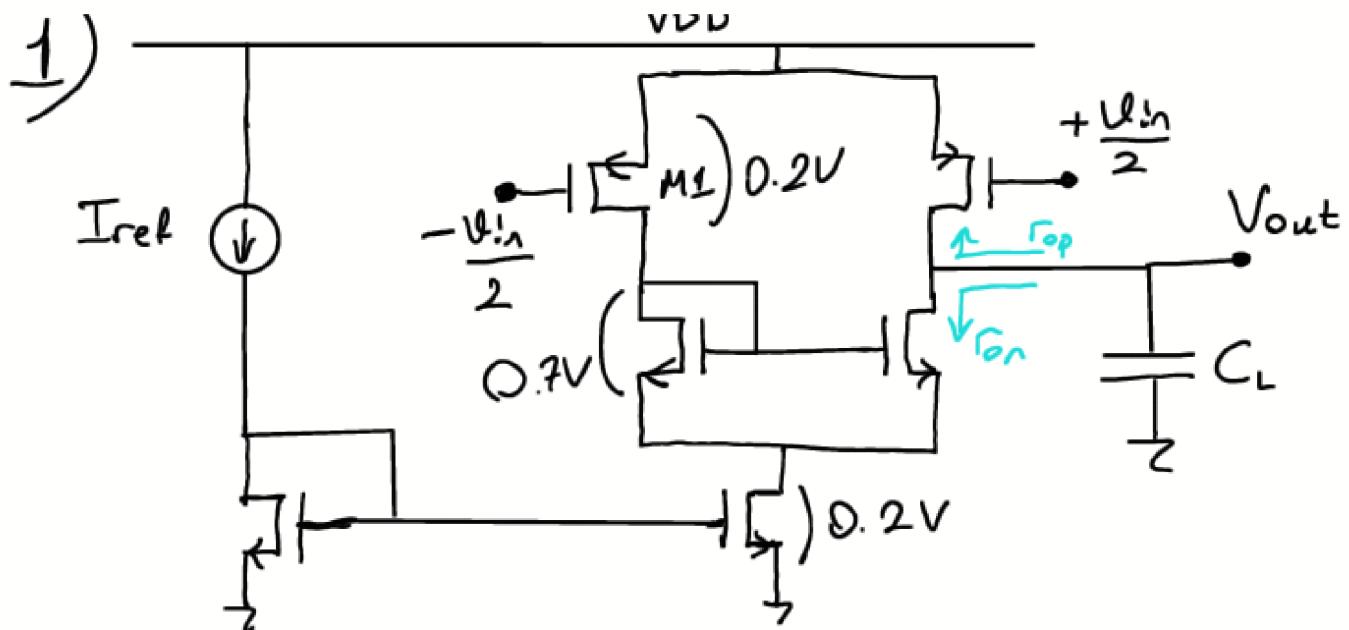
ouse = -1370 -690 - Selected: 0 path: .

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11/13/2023



hw51

Today 02:01 Uncategorized ▾



$$A_v = g_m R_{out} \quad GBW = \frac{g_m}{2\pi C_L}$$

$$\Rightarrow g_m = 2\pi \times 2 \times 10^{-12} \times 50 \times 10^6 \\ = 6.2832 \times 10^{-4} \text{ S}$$

→ From design perspective,

$$g_m = \frac{2I_D}{V_{GS} - V_T} \Rightarrow I_D = 62.832 \mu\text{A}$$

$$\Rightarrow I_{ref} = 2 \times I_D = 125.664 \mu\text{A}$$

$$\text{Since } g_m = \sqrt{2k' \frac{W}{L} I_D} \Rightarrow \frac{W}{L} = 62.832$$

$$R_{out} = r_{on} // r_{op} \Rightarrow A_v = g_m \frac{R_{out}}{2} = 70$$

$$\Rightarrow R_{out} = 55.7 k\Omega \Rightarrow r_{op} \approx 111 k\Omega$$

$r_{on} > r_{op}$ for some L , we just need to decide r_{op} and we can use same L for NMOS as well.

$$r_{op} = \frac{V_{A_p}}{I_D} \Rightarrow V_{A_p} = 7 \rightarrow \text{Thus we need to find } L_p \text{ for this } V_{A_p}.$$

\rightarrow When $V_{GS} = -3V$, $V_A = 3.5$ for $L = 0.15 \mu m$ PMOS and $I_D = 0.22567 \text{ mA}$ at $V_{DS} = 3V$

$$\Rightarrow V_{T_p} = -0.8V, \text{ so } \frac{\mu_p C_{ox}}{2} = 1.088 \times 10^{-4}$$

$$V_{OV_p} = 0.2V \Rightarrow V_{GS} + 0.8 = 0.2V$$

$$\Rightarrow V_{GS} = -0.6V, \text{ so } V_{GS} = 0.1V \rightarrow \text{For our circuit.}$$

\rightarrow So V_{DD} must be at least $1.1V$, thus let us choose $V_{DD} = 1.2V$.

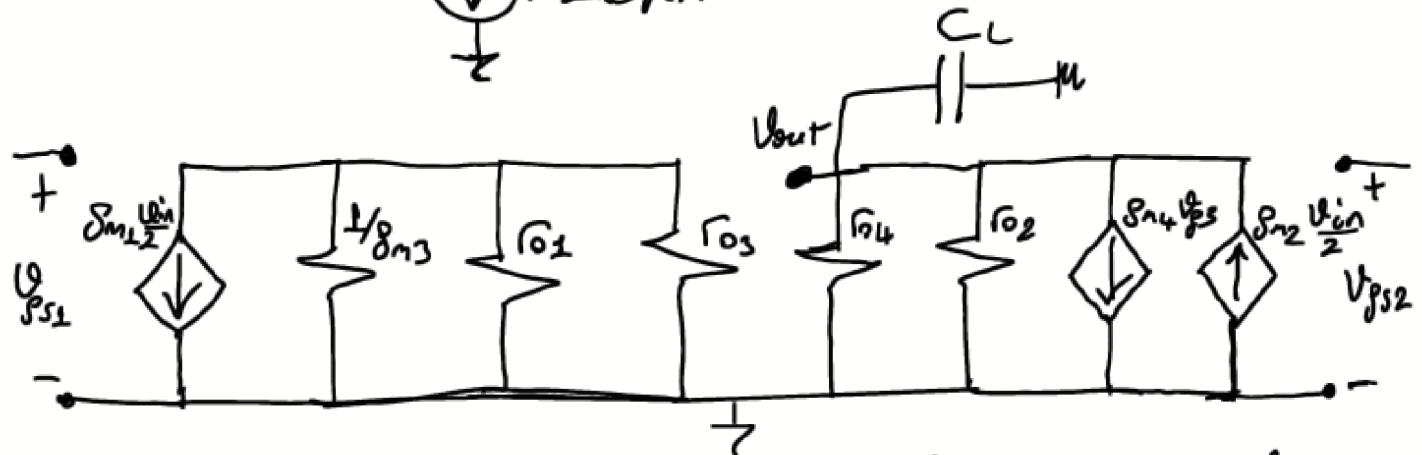
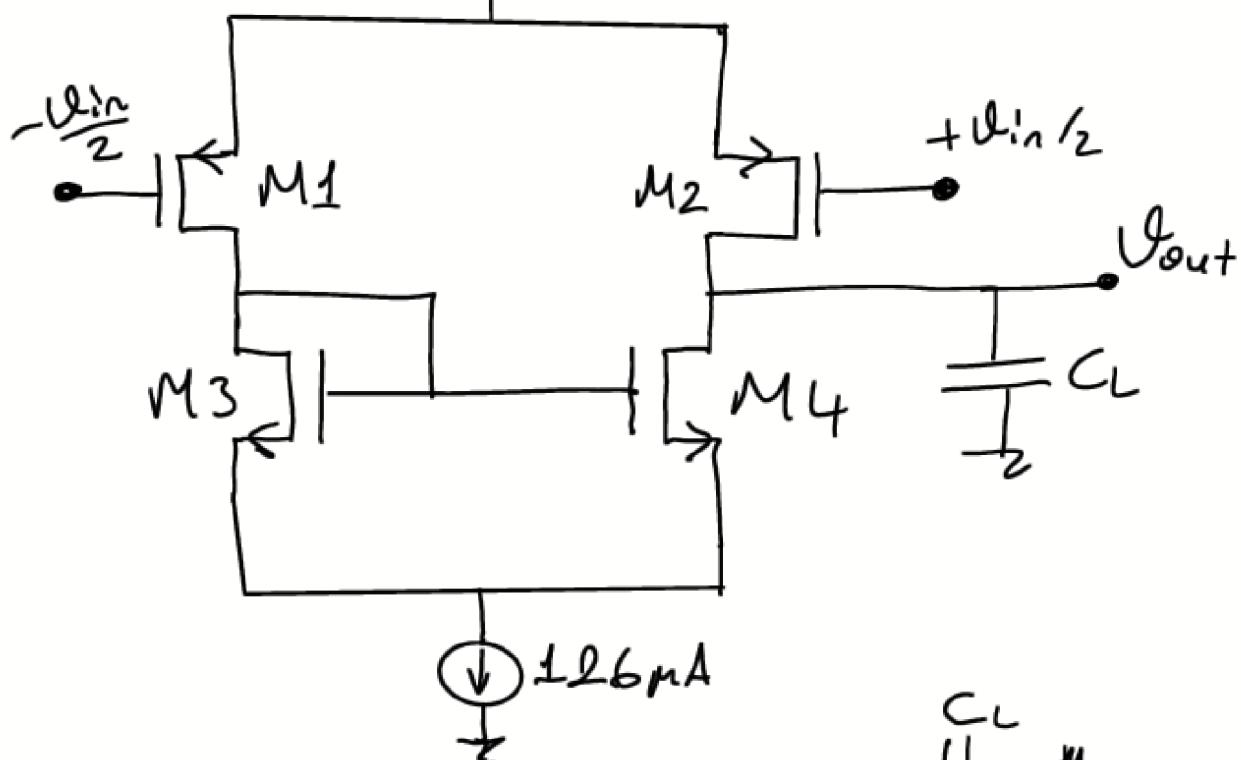
$$V_{A_p} = 7 = V_E L \text{ since } V_E = 23.3 \times 10^6$$

$$\Rightarrow L = 0.3 \mu m \Rightarrow W = 18.85 \mu m$$

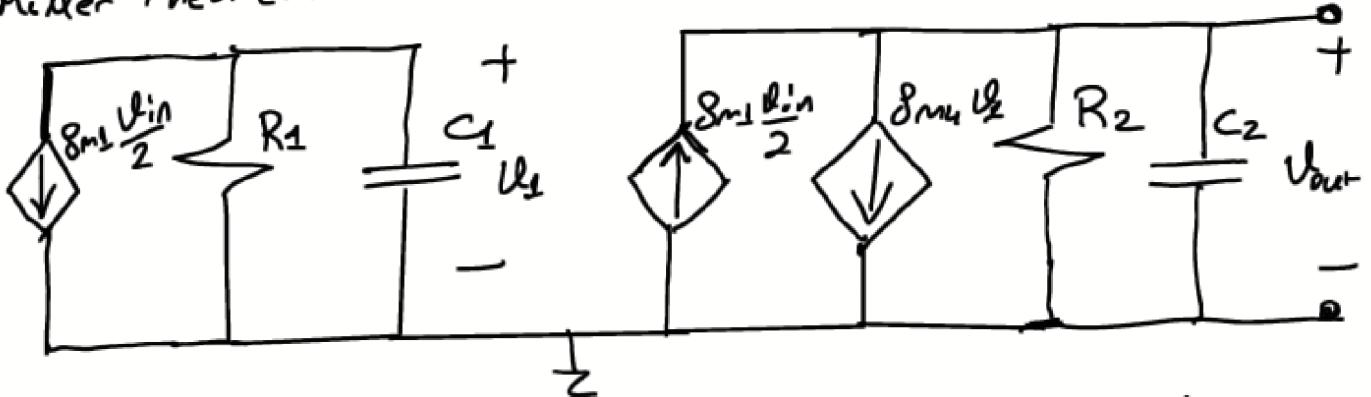
\rightarrow To catch specifications, let say

$$L = 0.5 \mu m \text{ and } W = 25 \mu m$$

2) Small Signal Equivalent Circuit



→ by including capacitances, above circuit becomes "Miller Theorem"



$$R_1 = C_1 / \delta m_1 \quad R_2 = C_2 / \delta m_2 \quad R_1 = \frac{1}{\delta m_1} / (R_{O1} // R_{O3}) \approx \frac{1}{\delta m_2}$$

$$C_1 = C_{gd1} + C_{gs3} + C_{gs4} + C_{bd1} + C_{bd3}$$

$$C_2 = C_{gd2} + C_{gd4} + C_{bd2} + C_{bd4} + C_L$$

$$C_{gs,p} = C_{gs,n} = \frac{2}{3} WL C_{ox} + WC_{ov}$$

$$C_{gd,p} = C_{gd,n} = WC_{ov}, \text{ and } C_{bd,n,p} = C_j$$

→ Since I do not know exactly how to calculate Cov and C_j , I will assume that they are zero, so

$$C_{gs} = \frac{2}{3} WL C_{ox} \approx 4.1667 \times 10^{-18} F$$

$$\Rightarrow C_1 = 0.04 \mu F \text{ and } C_2 = 2 \mu F$$

$$V_1 = -8m_1 \frac{V_{in}}{2} \left(\frac{1}{8m_3 + sC_1} \right)$$

$$i_o = -8m_4 V_1 + 8m_1 \frac{V_{in}}{2} \quad \text{and}$$

$$V_{out} = - \left(R_2 \parallel \frac{1}{sC_2} \right) i_o$$

$$= - \left(R_2 \parallel \frac{1}{sC_2} \right) \left(-8m_4 V_1 + 8m_1 \frac{V_{in}}{2} \right)$$

$$= - \frac{R_2}{1 + sC_2 R_2} \left[+8m_4 8m_1 \frac{V_{in}}{2} \left(\frac{1}{8m_3 + sC_1} + 8m_1 \frac{V_{in}}{2} \right) \right]$$

$$\Rightarrow V_{out} = - \frac{R_2}{1 + sC_2 R_2} 8m_1 \frac{V_{in}}{2} \left(\frac{8m_4}{8m_3 + sC_1} + 1 \right)$$

$$\Rightarrow A_v = \frac{V_{in}}{V_{out}} = \frac{-8m_1 R_2}{2(1 + sC_2 R_2)} \left(\frac{8m_4}{8m_3 + sC_1} + 1 \right)$$

→ Now let us define 2 frequency variables (poles):

$$\omega_n = \frac{1}{\sqrt{C_1 C_2}} \quad \text{and} \quad \omega_d = \frac{1}{\sqrt{sC_1}}$$

$$\omega_2 = \frac{1}{R_2 C_2}$$

$$\Rightarrow A_v = \frac{-g_{m1} R_2 \omega_2}{2(s + \omega_2)} \left[1 + \frac{g_{m4} R_L \omega_L}{s + \omega_L} \right]$$

Since $R_L C_1$ is too small, the dominant freq.
is $\omega_2 = \frac{1}{R_2 C_2} = \frac{1}{R_{out} C_L} = \frac{1}{55.7k \times 2p} \approx 9 \text{ MHz}$

and $\omega_L = \frac{1}{0.06 \times 10^{-12} \times (5.8 \times 10^{-4})^{-1}}$
 \hookrightarrow by using $g_m = \sqrt{2k'W I_D}$

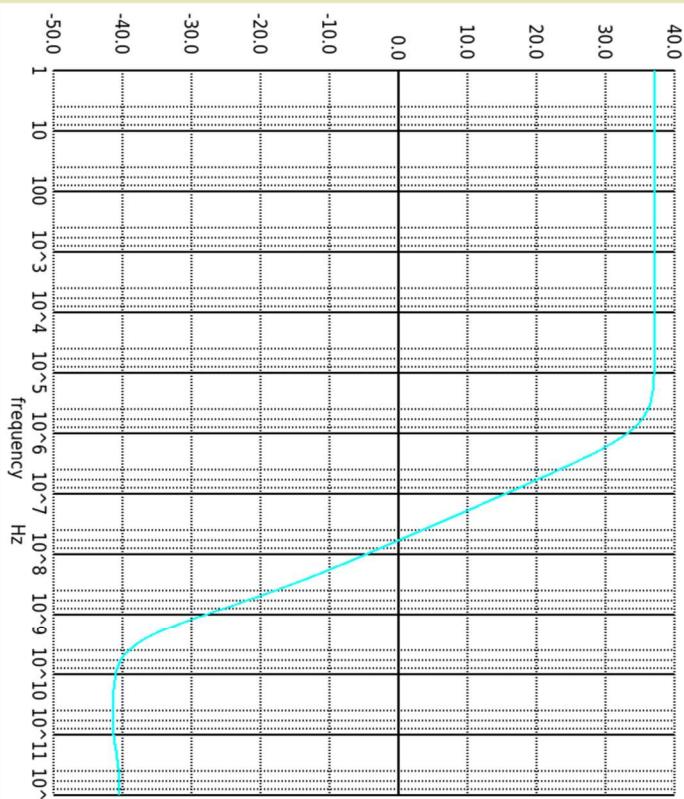
$$\Rightarrow \omega_L = 14.5 \text{ GHz}$$

$$\Rightarrow A_v = \frac{-g_{m1} R_2 \omega_2}{2(s + \omega_2)} - \frac{g_{m1} g_{m4} R_L R_2 \omega_1 \omega_2}{2(s + \omega_2)(s + \omega_L)}$$

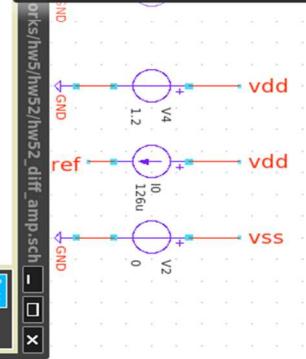
$$\Rightarrow A_v = - \frac{g_{m1} R_2 \omega_2 (s + \omega_1) + g_{m1} g_{m4} R_L R_2 \omega_1 \omega_2}{2(s + \omega_2)(s + \omega_L)}$$

Zero: $s + \omega_1 + g_{m4} R_L \omega_L = 0 \Rightarrow \omega_0 \approx 2\omega_1$

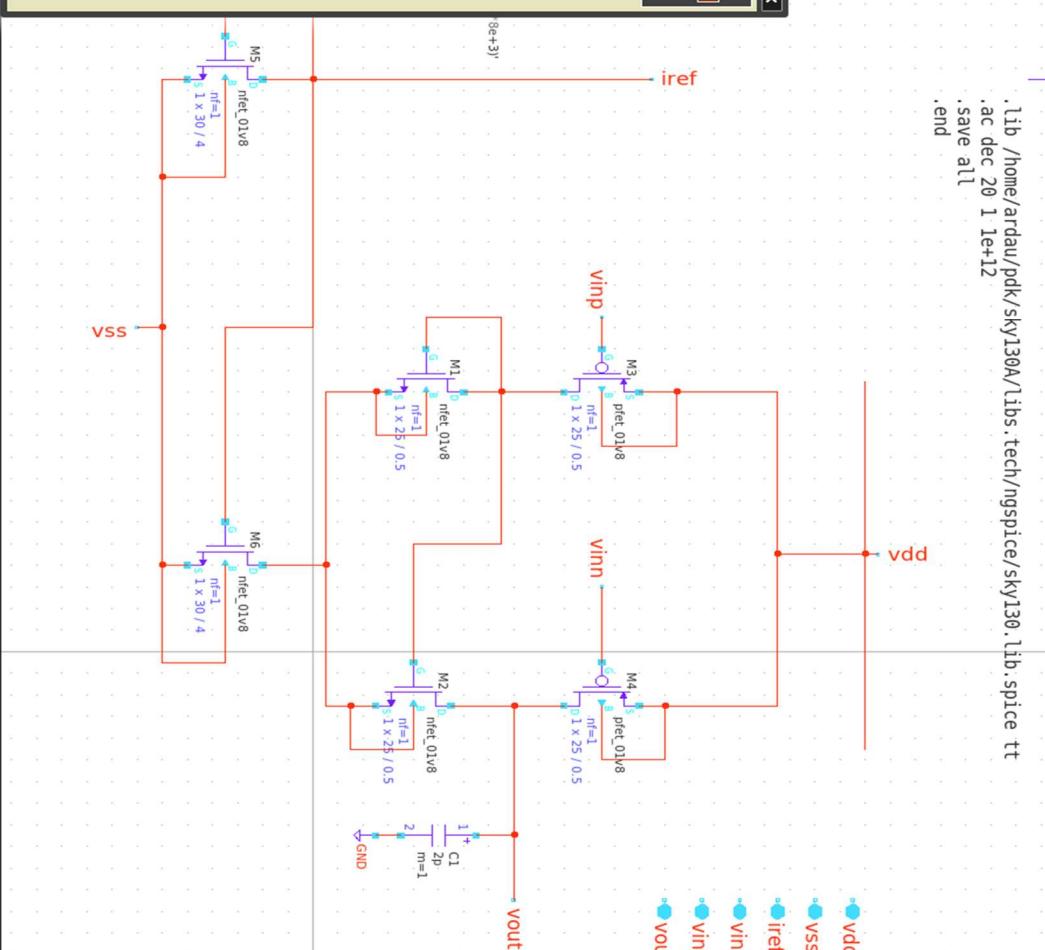
$$\Rightarrow \omega_0 = 29.5 \text{ GHz}$$



```
File Edit Option
# nsimcice-41 : Circuit level simulation program
#   ** The U. C. Berkeley GRD Group
#   ** Copyright 1985-1994, Regents of the University of California,
#   ** Please see your nsimcice manual from https://nsimcice.sourceforge.net/bugrep.html
#   ** Please file your bug-reports at https://nsimcice.sourceforge.net/bugrep.html
#   *** Creation Date: Sun Nov 12 21:58:37 UTC 2023
*****  
  
Note: Compatibility modes selected; no a  
  
Warning: nsimcice on .subckt line will override multiplier in hierarchy!  
  
Circuit: ** sch-path: /mnt/c/users/danlu/desktop/derlayer/advanced_ec/homework/s/h  
w5/nm22/nm22_difff_amp.sch  
option STOLEN; Scale is set to 1e-06 for instance and model parameters  
Doing analysis at Tmp = 27.000000 and TNOM = 27.000000  
Reference value : 1.00000e+00  
No. of Data Rows : 241  
nsimcice 1 > plot db(out)  
nsimcice 2 > |
```



```
.lib /home/ardau/pdk/sky130A/libs.tech/ngspice/sky130.lib.spice tt  
.ac dec 20 1 le12  
.save all  
.end
```



SNAP: 10 GRID: 20 NETLIST MODE: spice NUM LOCK SET! mouse = -1120 -510 - selected: 0 path: .
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11/13/2023

hw53

Today 02:01 Uncategorized ▾

3) Common mode gain can be found by using CMRR which is used in lesson slides:

Since $CMRR = \left| \frac{A_d}{A_c} \right|$, so

$A_d = g_{mp} (r_o \parallel r_{op})$ and CMRR was given as

$$CMRR \approx \left(2g_m(d_p) r_{tail} \right) g_m(m_i_r) \left(r_o(d_p) \parallel r_o(m_i_r) \right)$$

$$\Rightarrow A_c = \frac{g_m(d_p) r_o(d_p)}{\left(2g_m(d_p) r_{tail} \right) g_m(m_i_r) \left(r_o(d_p) \parallel r_o(m_i_r) \right)}$$

$$\Rightarrow = r_o(d_p) / \left[2g_m(m_i_r) r_{tail} \left(r_o(d_p) \parallel r_o(m_i_r) \right) \right]$$

$$r_{tail} = r_o, r_o(m_i_r) = 1/g_m(m_i_r), r_o(d_p) = R_{out}$$

$$\Rightarrow A_c = \frac{R_{out} (R_{out} + 1/g_m(m_i_r))}{2 g_m(m_i_r) r_o \frac{R_{out}}{g_m(m_i_r)}}$$

$$\Rightarrow A_c = \frac{R_{out} + 1/g_m(m_i_r)}{2 r_o} \quad \text{found via Python script}$$

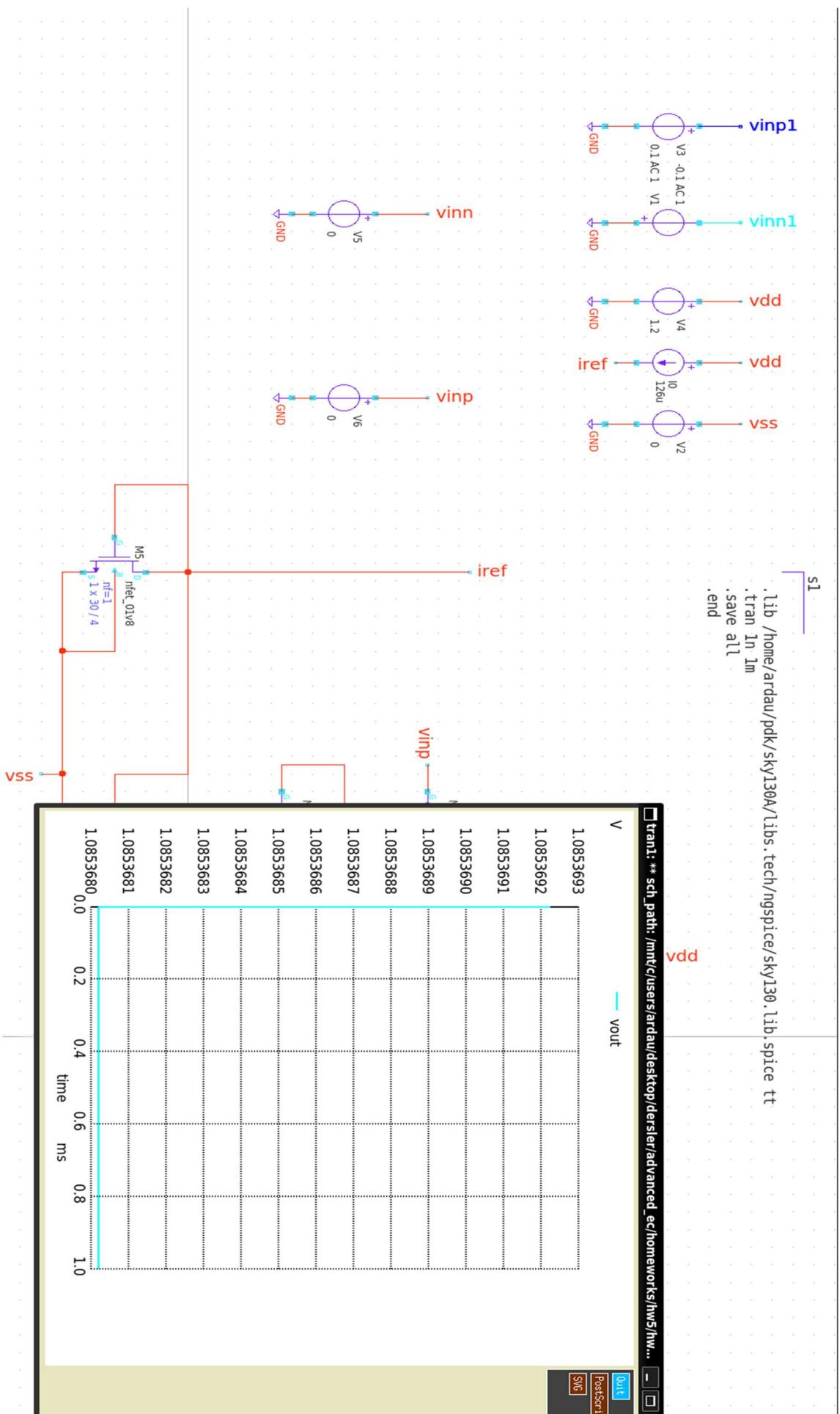
$$R_{out} = 55.7k, r_o = \frac{V_E L}{I_D} \approx 115k$$

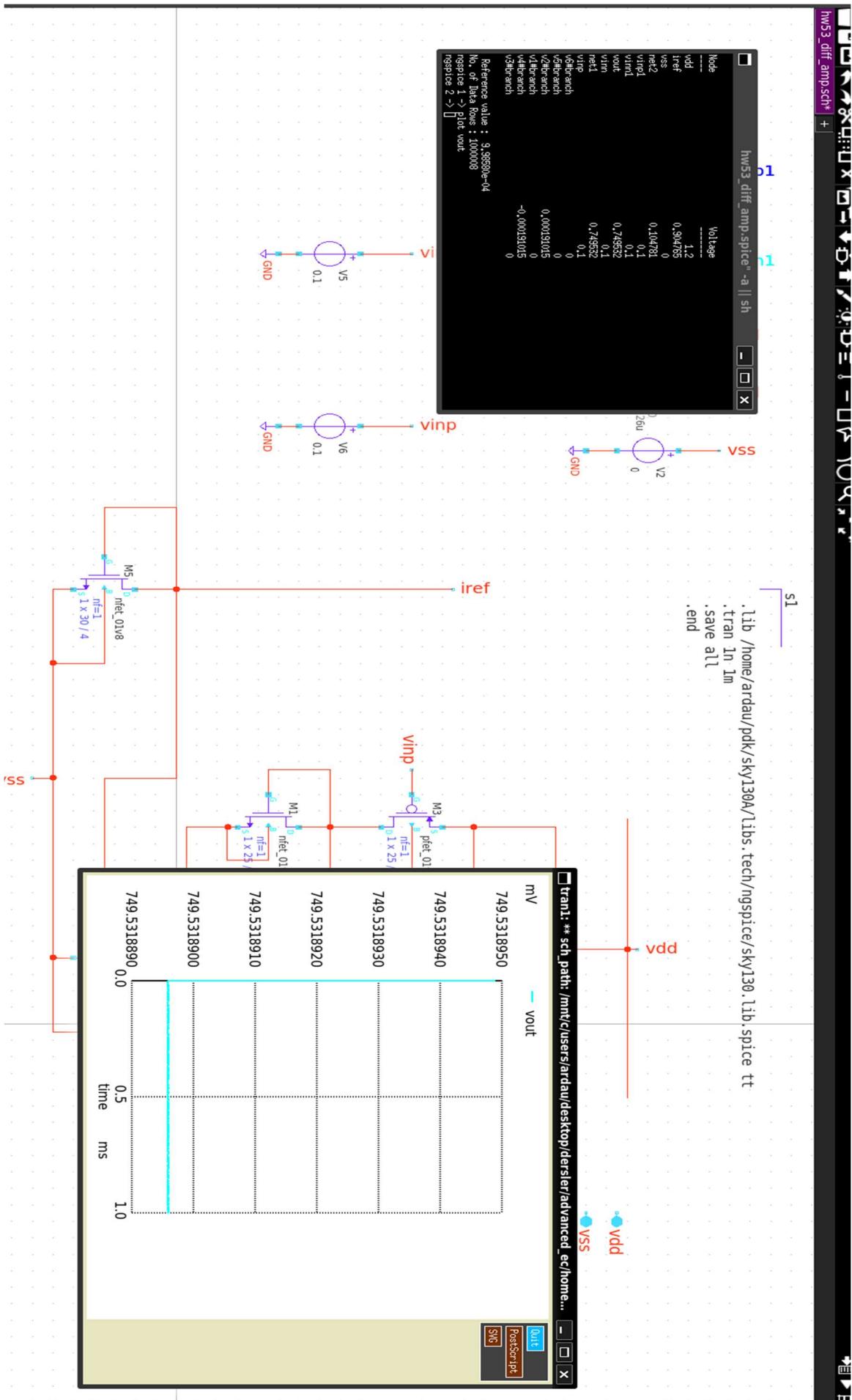
This is equal to
1 for our case

$$M_1 \boxed{M_2} M_2; g_m(m_i_r) = \frac{g_{m_L}}{r_o + 1/r} \frac{(W_2/L_2)}{(W_1/L_1)}$$

$$\Rightarrow S_m(\text{mir}) \approx \frac{3.165 \times 10^{-4}}{\frac{1}{80k} + \frac{3.165 \times 10^{-4}}{S_m}} = 9.962$$

$$\Rightarrow A_c \approx 0.242 // \quad \begin{array}{l} \text{Simulation} = 3.355 \\ \text{Result} \end{array}$$



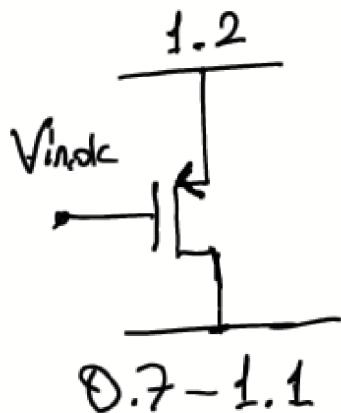
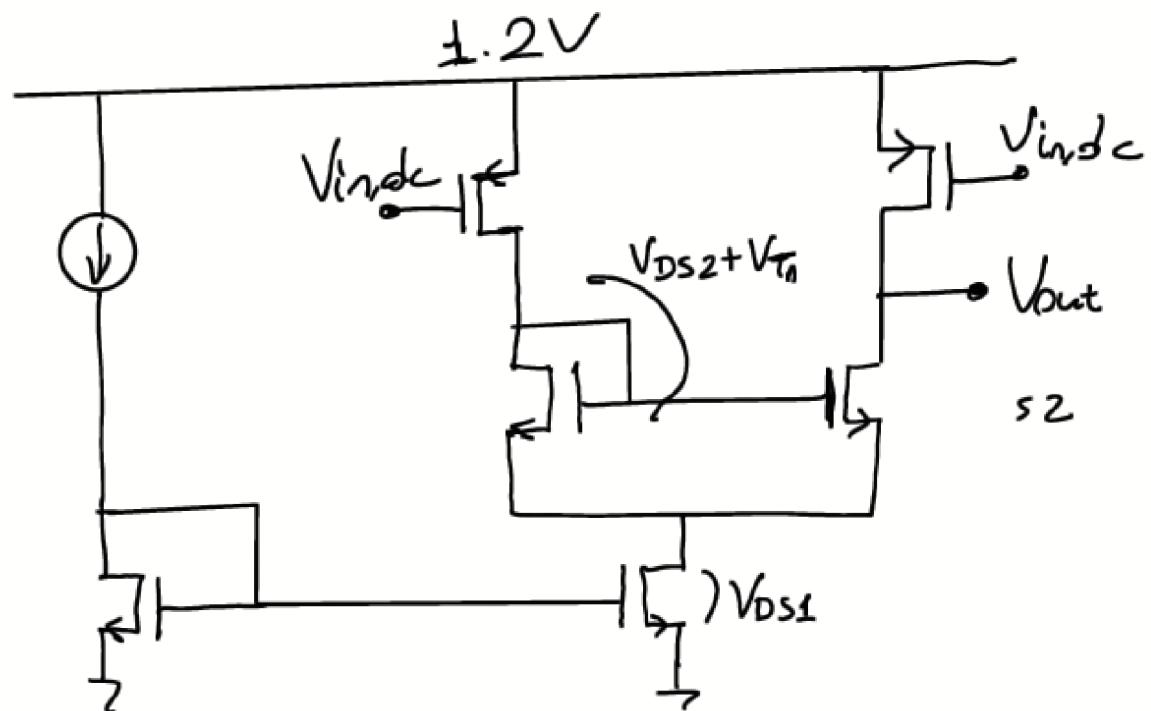


hw54

Today 02:01

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4)

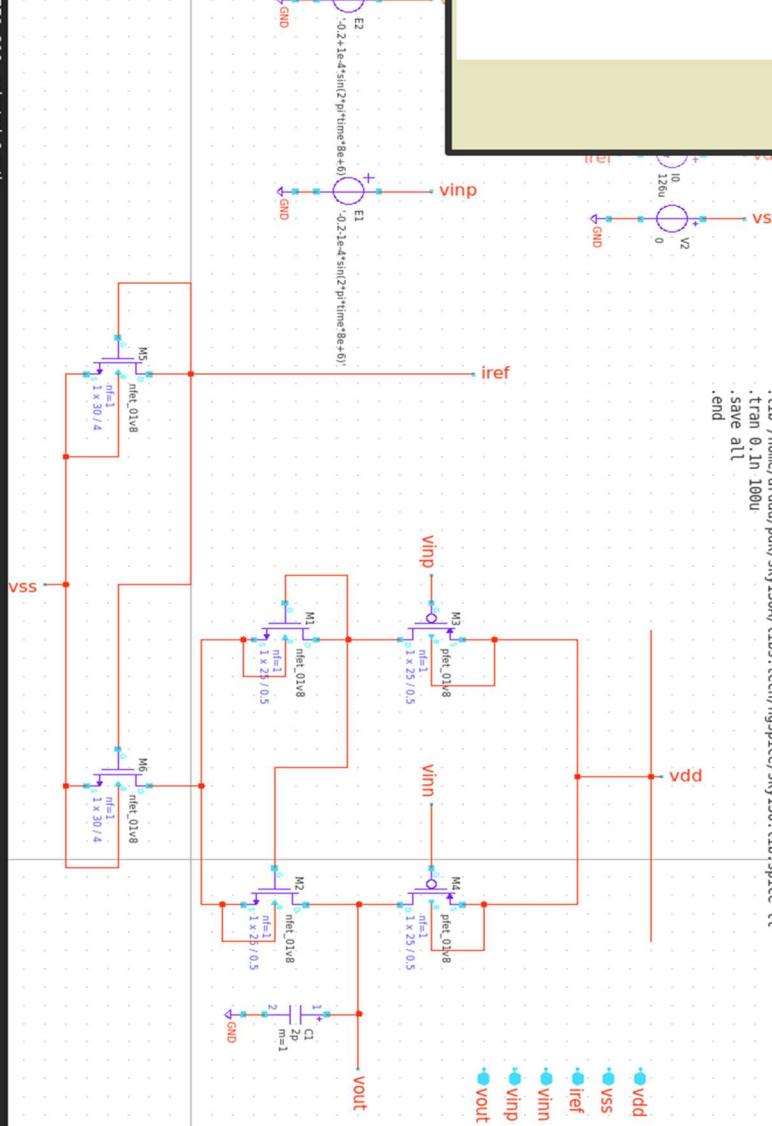


$$V_{T,P} = -0.8V$$

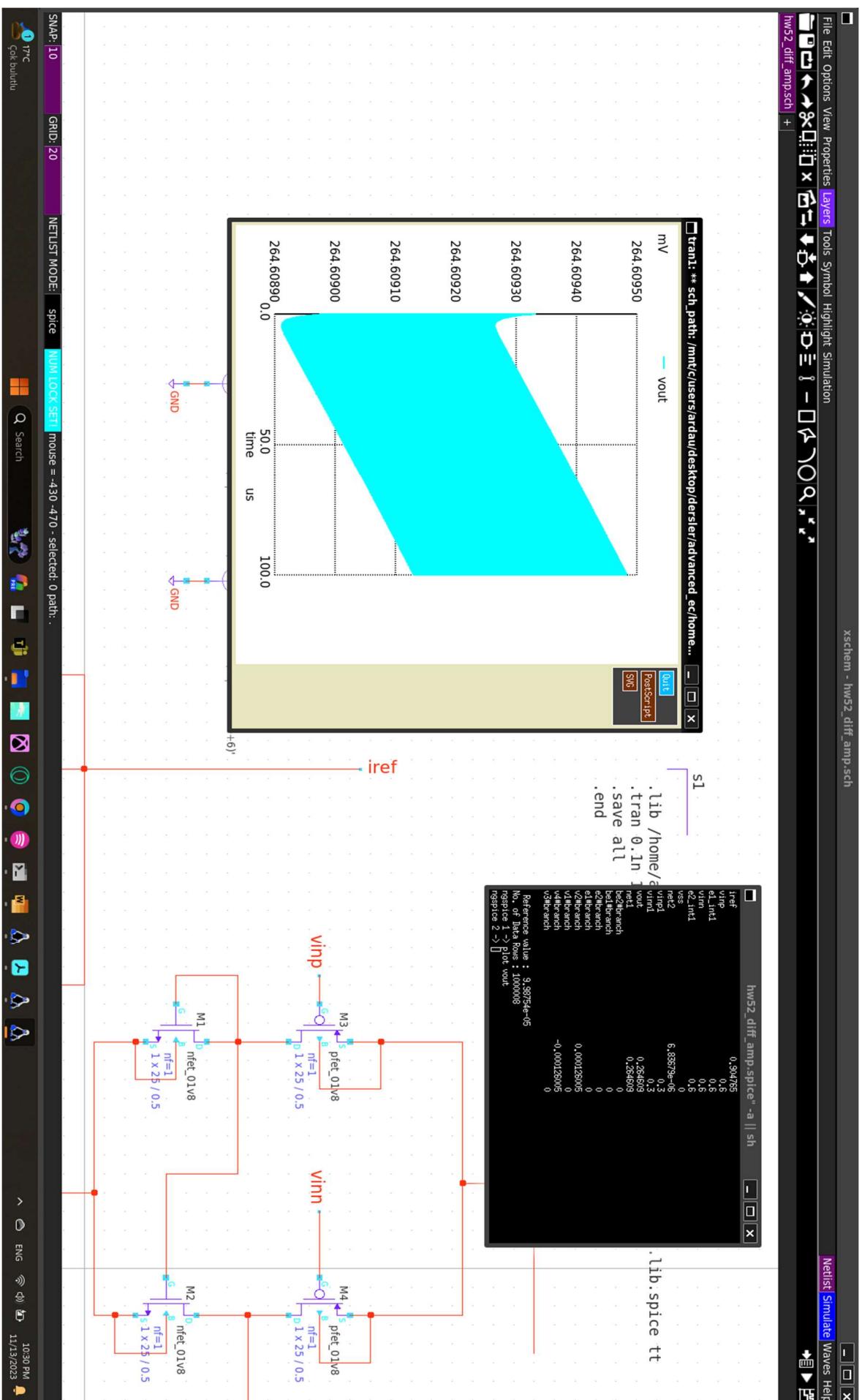
$$V_{DS1} = V_{DS2} = 0.1V, V_{T,N} = 0.5V$$

$$V_{in,max} = 0.3V, V_{in,min} = -0.1V$$

→ I found $V_{T,P} = -0.8V$ from my analysis
but it seems that it is $-0.5V$ for this circuit,
 $V_{in,max} = 0.55V, V_{in,min} = -0.2V$



Snap: 10 Grid: 20 Netlist Mode: spice Num Lock Set! mouse = -770 -210 - selected: 0 path: .

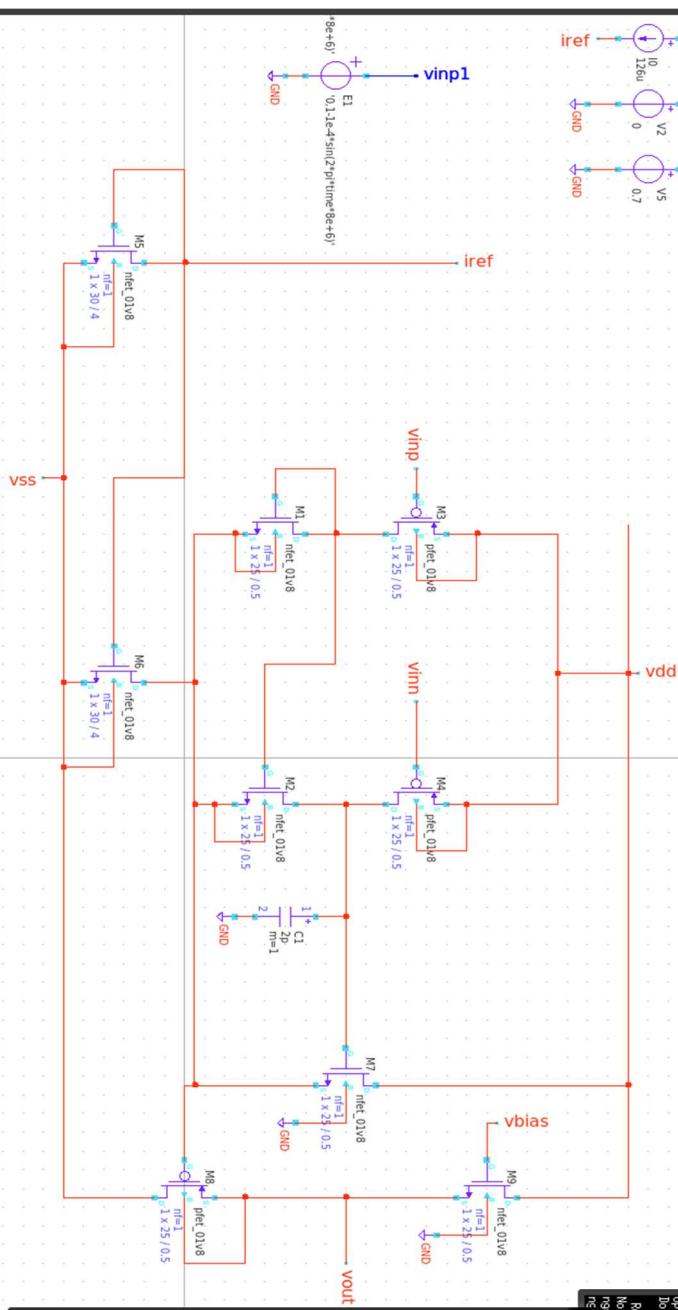
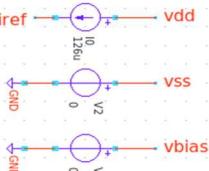


xschem - hw52_diff_amp.sch

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hw52_diff_amp.sch +

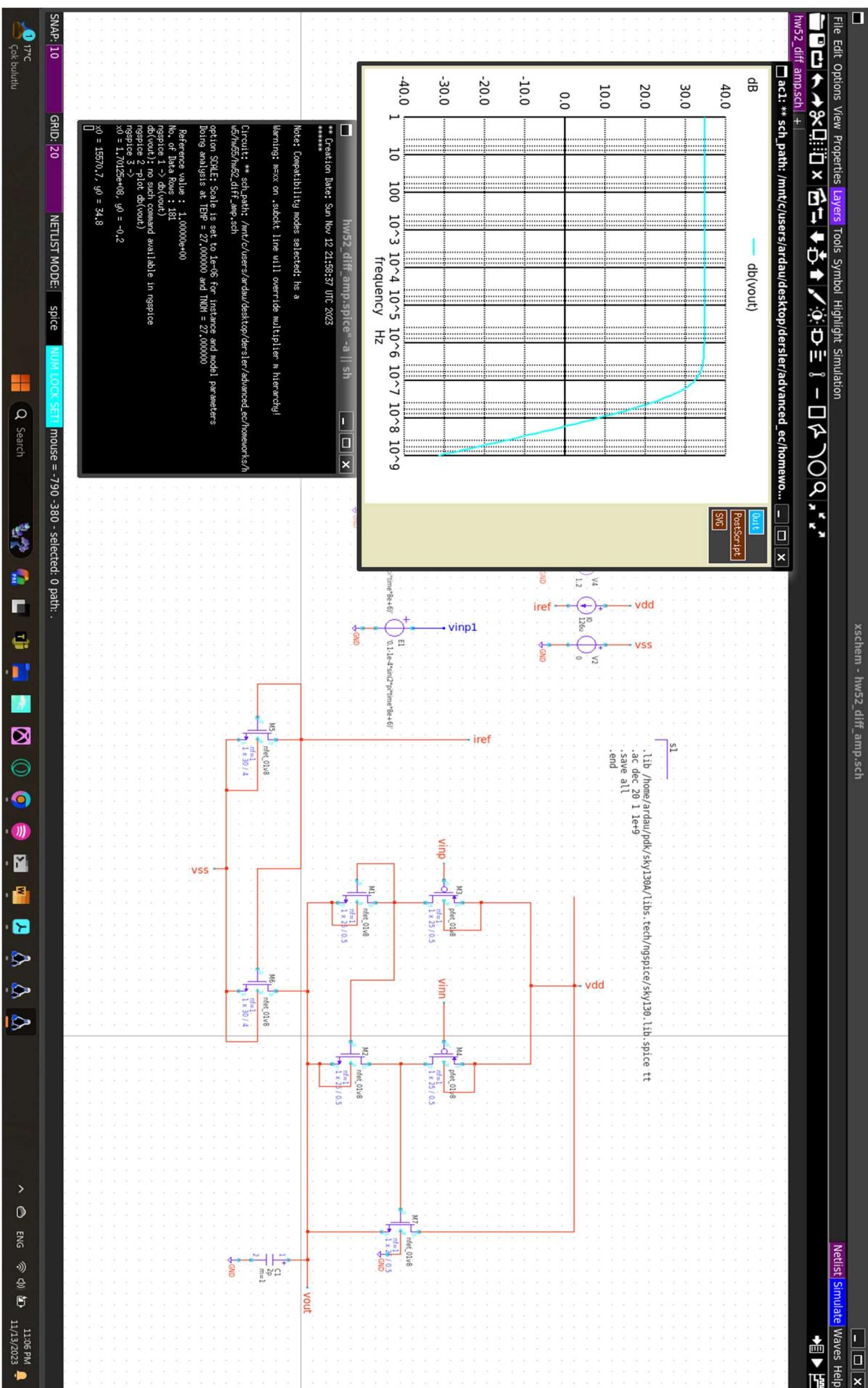
```
.lib /home/ardau/pdk/sky130A/libs.tech/ngspice/sky130.lib.spice tt
.ac dec 20 1 1e+9
.save all
.end
```



SWAP: 10 GRID: 20 NETLIST MODE: spice NUM LOCK SET: mouse = -500 -520 - selected: 0 path: -



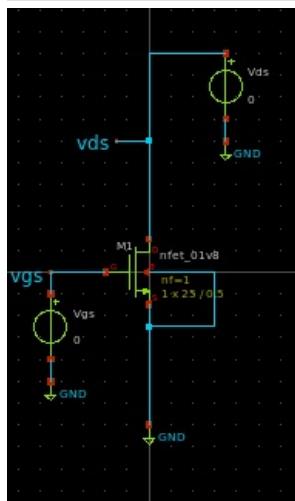
11:02 PM 1/13/2023



```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import warnings
warnings.filterwarnings("ignore")
sns.set_theme()
```

```
In [2]: from IPython import display
display.Image("hw53_nmos.png")
```

Out[2]:



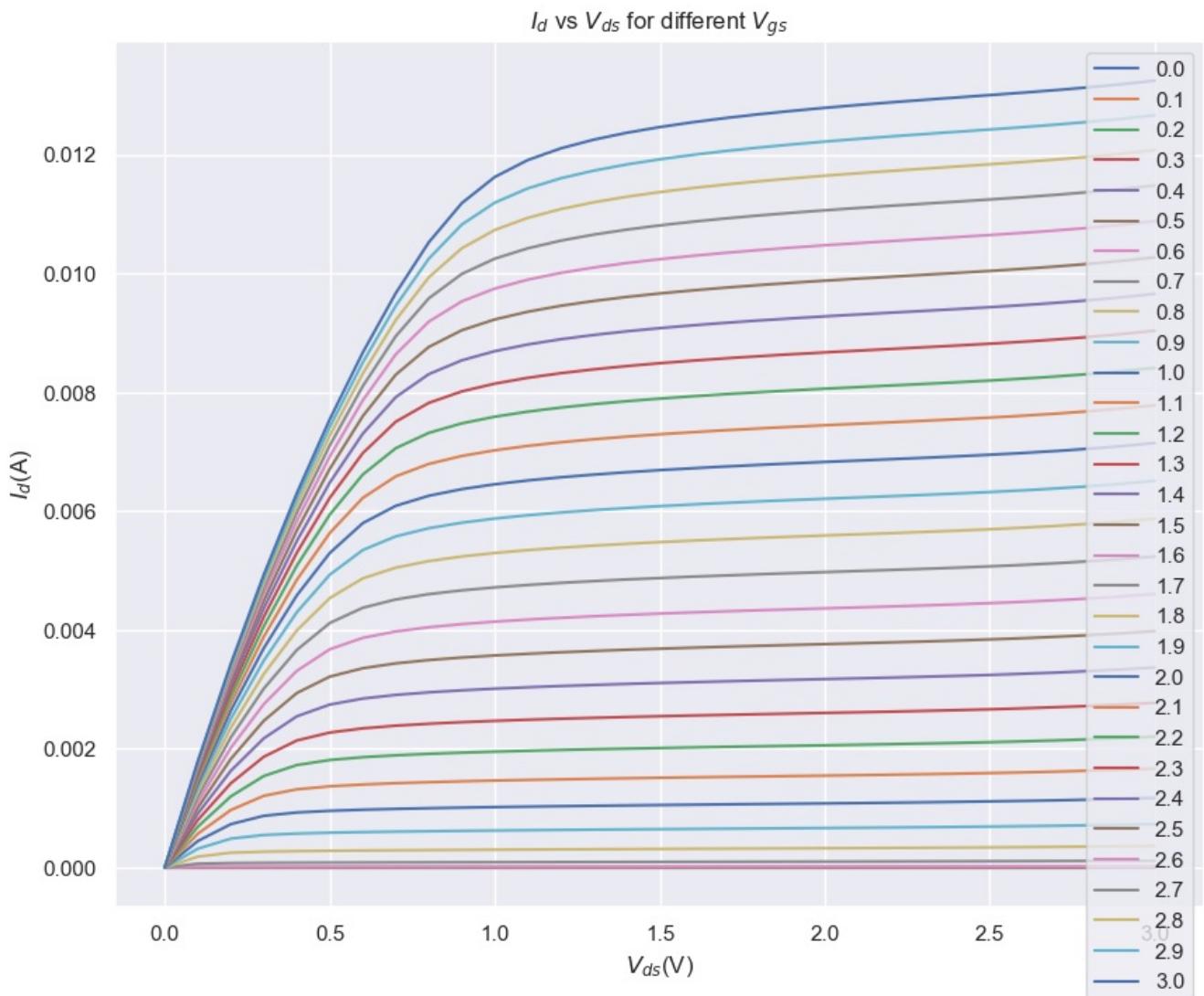
```
In [3]: data = pd.read_csv("hw53_nmos.txt", delimiter=",")
data.head()
```

```
Out[3]:   undefined  v-sweep  v(vds)  v(vgs)      i(vds)  undefined2
0       NaN      0.0      0.0      0.0 -5.948255e-40      NaN
1       NaN      0.1      0.1      0.0 -2.007283e-12      NaN
2       NaN      0.2      0.2      0.0 -2.245315e-12      NaN
3       NaN      0.3      0.3      0.0 -2.437162e-12      NaN
4       NaN      0.4      0.4      0.0 -2.607692e-12      NaN
```

```
In [4]: data["v(vgs)"] = [float(i) for i in data["v(vgs)"]]
data["v(vds)"] = [float(i) for i in data["v(vds)"]]
data["i(vds)"] = [-1*float(i) for i in data["i(vds)"]]
```

```
In [5]: Id_list = []
Vds_list = []
vgs_vals = data["v(vgs)"].unique()
for val in vgs_vals:
    df = data[data["v(vgs)"] == val]
    Id_list.append(list(df["i(vds)"]))
    Vds_list.append(list(df["v(vds)"]))
```

```
In [6]: plt.figure(figsize = (10, 8))
for count in range(len(vgs_vals)):
    plt.plot(Vds_list[count], Id_list[count], '--', label = str(vgs_vals[count]))
    plt.title("$I_d$ vs $V_{ds}$ for different $V_{gs}$")
    plt.ylabel("$I_d(A)$")
    plt.xlabel("$V_{ds}(V)$")
    plt.legend()
    plt.grid("on")
```



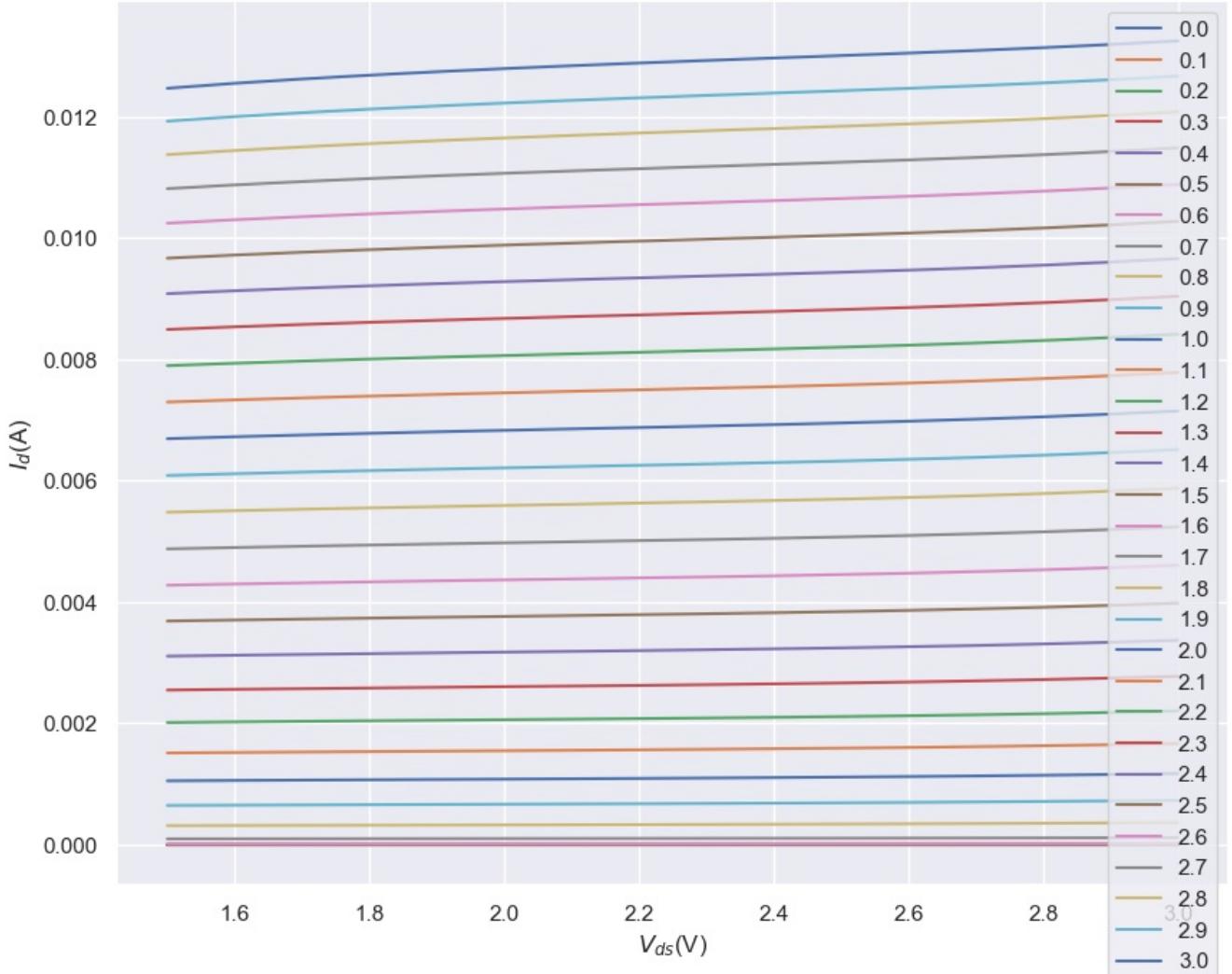
```
In [7]: from sklearn.linear_model import LinearRegression
linear_regression = LinearRegression()

plt.figure(figsize = (10, 8))

for val in vgs_vals:
    df = data[data["v(vgs)"] == val]
    df = df[(df["v(vds)"] >= 1.5)]
    Id_list2 = df["i(vds)"]
    vds_list2 = df["v(vds)"]
    x = vds_list2.values.reshape(-1, 1)
    y = Id_list2.values.reshape(-1, 1)
    linear_regression.fit(x, y)
    b0 = linear_regression.intercept_
    b1 = linear_regression.coef_
    #  $y = b1*x + b0$ , so  $x = -b0/b1$  at  $y = 0$ 
    Va = -float(b0)/float(b1)
    Ve = Va/(0.15e-6)
    plt.plot(x, y, '-', label = str(val))
plt.title("$I_d$ vs $V_{ds}$ at Active Region")
plt.ylabel("$I_d$(A)")
plt.xlabel("$V_{ds}$(V)")
plt.legend()
plt.grid("on")
print("Va = {} and Ve = {} at Vgs = {}".format(Va, Ve, val))
```

$V_a = -0.9666269368762943$ and $V_e = -6444179.579175295$ at $V_{gs} = 0.0$
 $V_a = -1.9942064586468284$ and $V_e = -13294709.72431219$ at $V_{gs} = 0.1$
 $V_a = -2.1711597787096477$ and $V_e = -14474398.524730986$ at $V_{gs} = 0.2$
 $V_a = -2.197746894502127$ and $V_e = -14651645.963347513$ at $V_{gs} = 0.3$
 $V_a = -2.237384633907754$ and $V_e = -14915897.559385026$ at $V_{gs} = 0.4$
 $V_a = -2.411923453567197$ and $V_e = -16079489.69044798$ at $V_{gs} = 0.5$
 $V_a = -3.2673549641982$ and $V_e = -21782366.427988$ at $V_{gs} = 0.6$
 $V_a = -5.475802508137886$ and $V_e = -36505350.05425258$ at $V_{gs} = 0.7$
 $V_a = -8.204654192871953$ and $V_e = -54697694.619146354$ at $V_{gs} = 0.8$
 $V_a = -10.557391641259205$ and $V_e = -70382610.94172804$ at $V_{gs} = 0.9$
 $V_a = -12.454477524869494$ and $V_e = -83029850.16579664$ at $V_{gs} = 1.0$
 $V_a = -14.0312889854532$ and $V_e = -93541926.569688$ at $V_{gs} = 1.1$
 $V_a = -15.387040126893304$ and $V_e = -102580267.51262203$ at $V_{gs} = 1.2$
 $V_a = -16.578600341327792$ and $V_e = -110524002.27551863$ at $V_{gs} = 1.3$
 $V_a = -17.64063812423988$ and $V_e = -117604254.16159922$ at $V_{gs} = 1.4$
 $V_a = -18.59651566090382$ and $V_e = -123976771.07269213$ at $V_{gs} = 1.5$
 $V_a = -19.462877014122366$ and $V_e = -129752513.42748244$ at $V_{gs} = 1.6$
 $V_a = -20.251643384690805$ and $V_e = -135010955.8979387$ at $V_{gs} = 1.7$
 $V_a = -20.971044669674086$ and $V_e = -139806964.4644939$ at $V_{gs} = 1.8$
 $V_a = -21.626283637138332$ and $V_e = -144175224.2475889$ at $V_{gs} = 1.9$
 $V_a = -22.220028493308988$ and $V_e = -148133523.2887266$ at $V_{gs} = 2.0$
 $V_a = -22.752824407429678$ and $V_e = -151685496.0495312$ at $V_{gs} = 2.1$
 $V_a = -23.223454392571043$ and $V_e = -154823029.28380695$ at $V_{gs} = 2.2$
 $V_a = -23.629275780947825$ and $V_e = -157528505.20631886$ at $V_{gs} = 2.3$
 $V_a = -23.966548914338958$ and $V_e = -159776992.76225972$ at $V_{gs} = 2.4$
 $V_a = -24.230760561264187$ and $V_e = -161538403.74176127$ at $V_{gs} = 2.5$
 $V_a = -24.41695301055837$ and $V_e = -162779686.7370558$ at $V_{gs} = 2.6$
 $V_a = -24.52005521393628$ and $V_e = -163467034.75957522$ at $V_{gs} = 2.7$
 $V_a = -24.535195484225124$ and $V_e = -163567969.89483416$ at $V_{gs} = 2.8$
 $V_a = -24.45802269699003$ and $V_e = -163053484.64660022$ at $V_{gs} = 2.9$
 $V_a = -24.28494402729102$ and $V_e = -161899626.8486068$ at $V_{gs} = 3.0$

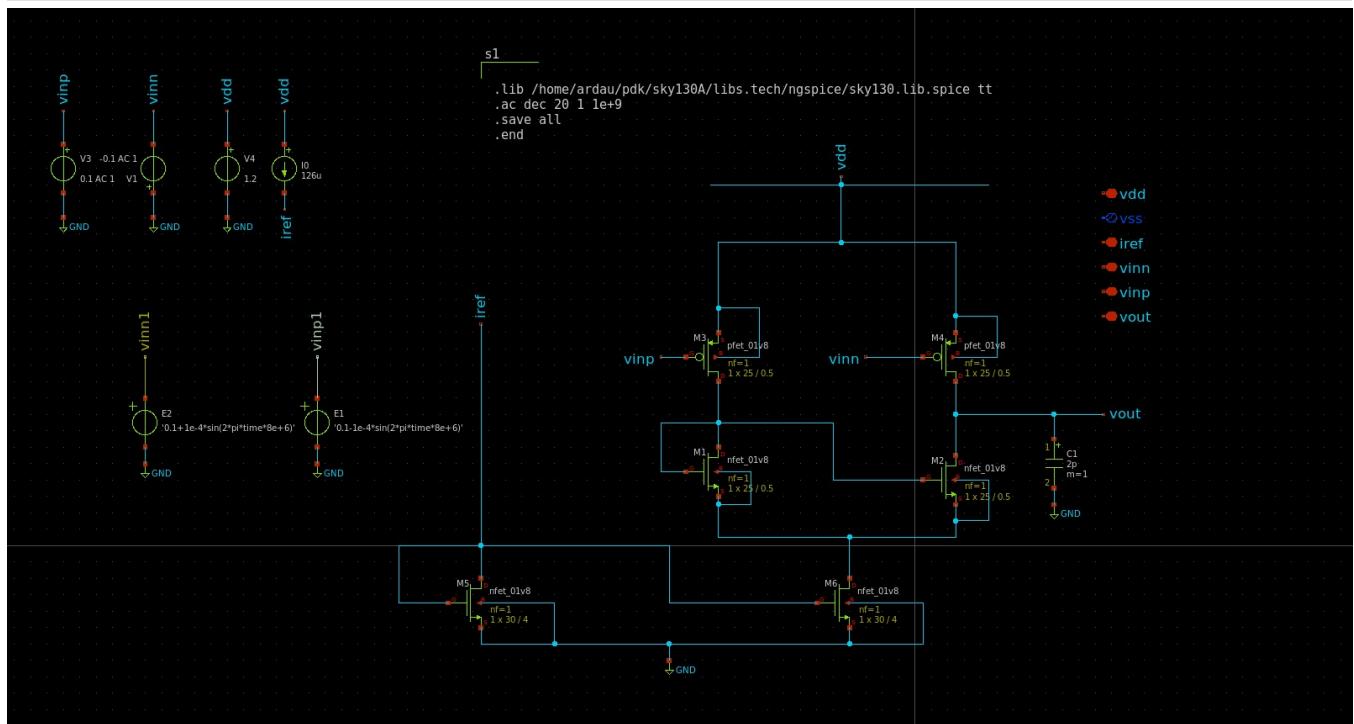
I_d vs V_{ds} at Active Region



```
In [1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import warnings
warnings.filterwarnings("ignore")
sns.set_theme()
```

```
In [2]: from IPython import display
display.Image("hw51_circuit.png")
```

Out[2]:



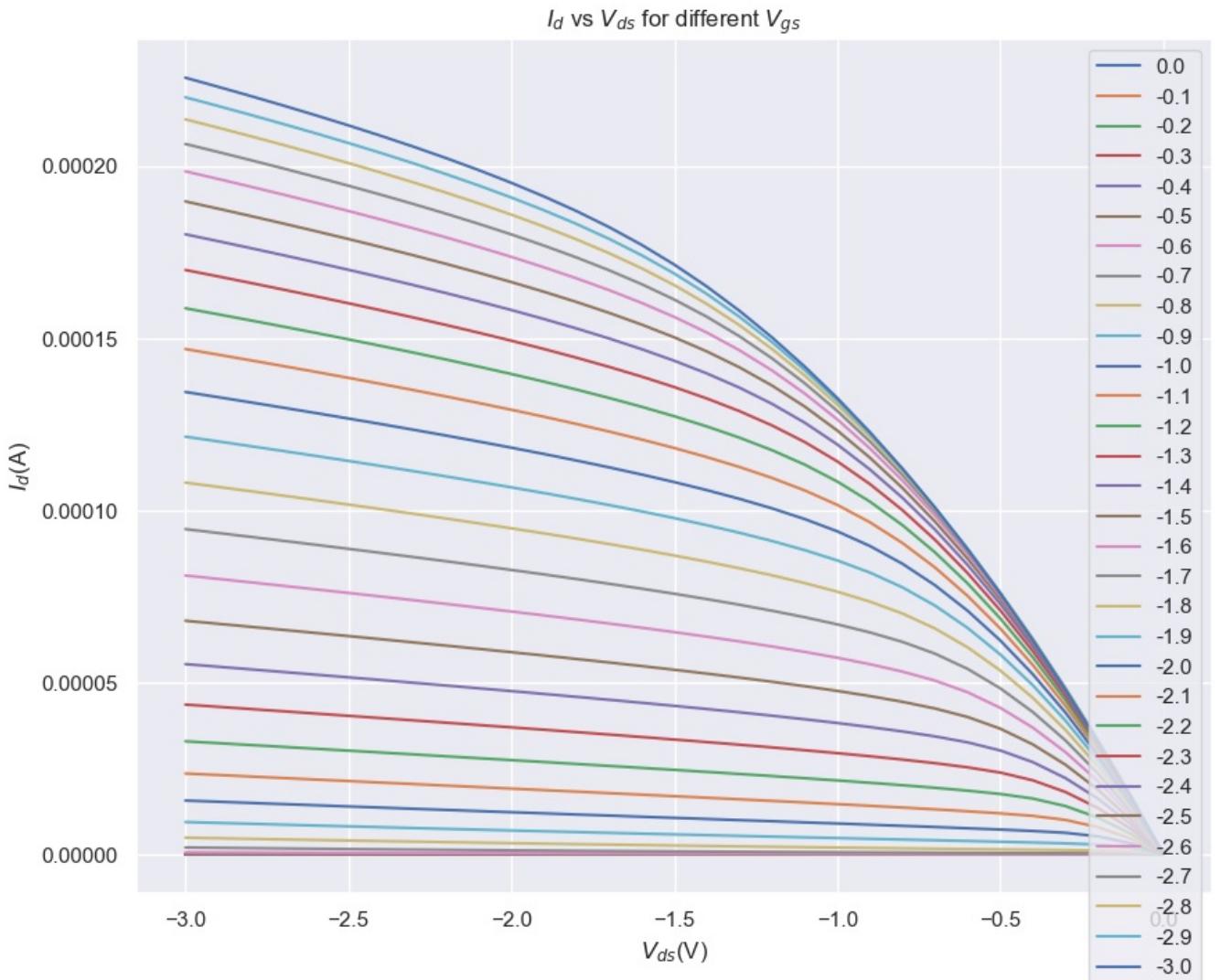
```
In [3]: data = pd.read_csv("hw51_pmos.txt", delimiter=",")
data.head()
```

```
Out[3]:   undefined2  v-sweep  v(vds)  v(vgs)      i(vds)  undefined2.1
0     NaN        0.0       0.0       0.0  6.098593e-38      NaN
1     NaN        0.1      -0.1       0.0 -2.419759e-12      NaN
2     NaN        0.2      -0.2       0.0 -2.962852e-12      NaN
3     NaN        0.3      -0.3       0.0 -3.522738e-12      NaN
4     NaN        0.4      -0.4       0.0 -4.133915e-12      NaN
```

```
In [4]: data["v(vgs)"] = [float(i) for i in data["v(vgs)"]]
data["v(vds)"] = [float(i) for i in data["v(vds)"]]
data["i(vds)"] = [-1*float(i) for i in data["i(vds)"]]
```

```
In [5]: Id_list = []
Vds_list = []
vgs_vals = data["v(vgs)"].unique()
for val in vgs_vals:
    df = data[data["v(vgs)"] == val]
    Id_list.append(list(df["i(vds)"]))
    Vds_list.append(list(df["v(vds)"]))
```

```
In [6]: plt.figure(figsize = (10, 8))
for count in range(len(vgs_vals)):
    plt.plot(Vds_list[count], Id_list[count], '-', label = str(vgs_vals[count]))
    plt.title("$I_d$ vs $V_{ds}$ for different $V_{gs}$")
    plt.ylabel("$I_d(A)$")
    plt.xlabel("$V_{ds}(V)$")
    plt.legend()
    plt.grid("on")
```



```
In [7]: from sklearn.linear_model import LinearRegression
linear_regression = LinearRegression()

plt.figure(figsize = (10, 8))

for val in vgs_vals:
    df = data[data["v(vgs)"] == val]
    df = df[(df["v(vds)"] <= -1.5)]
    Id_list2 = df["i(vds)"]
    vds_list2 = df["v(vds)"]
    x = vds_list2.values.reshape(-1, 1)
    y = Id_list2.values.reshape(-1, 1)
    linear_regression.fit(x, y)
    b0 = linear_regression.intercept_
    b1 = linear_regression.coef_
    #  $y = b1*x + b0$ , so  $x = -b0/b1$  at  $y = 0$ 
    Va = -float(b0)/float(b1)
    Ve = Va/(0.15e-6)
    plt.plot(x, y, '-', label = str(val))
plt.title("$I_d$ vs $V_{ds}$ at Active Region")
plt.ylabel("$I_d$(A)")
plt.xlabel("$V_{ds}$(V)")
plt.legend()
plt.grid("on")
print("Va = {} and Ve = {} at Vgs = {}".format(Va, Ve, val))
```

$V_a = -1.6733889059687133$ and $V_e = -11155926.039791422$ at $V_{gs} = 0.0$
 $V_a = -1.3052078354556458$ and $V_e = -8701385.569704305$ at $V_{gs} = -0.1$
 $V_a = -1.018310297240141$ and $V_e = -6788735.314934273$ at $V_{gs} = -0.2$
 $V_a = -0.8872011916105759$ and $V_e = -5914674.610737173$ at $V_{gs} = -0.3$
 $V_a = -0.8465933448359222$ and $V_e = -5643955.632239481$ at $V_{gs} = -0.4$
 $V_a = -0.8289125836662976$ and $V_e = -5526083.891108651$ at $V_{gs} = -0.5$
 $V_a = -0.7345569281852217$ and $V_e = -4897046.187901478$ at $V_{gs} = -0.6$
 $V_a = -0.407958017164422$ and $V_e = -2719720.11442948$ at $V_{gs} = -0.7$
 $V_a = 0.18263460624847927$ and $V_e = 1217564.0416565286$ at $V_{gs} = -0.8$
 $V_a = 0.9144204281477727$ and $V_e = 6096136.187651819$ at $V_{gs} = -0.9$
 $V_a = 1.6605566579722564$ and $V_e = 11070377.719815044$ at $V_{gs} = -1.0$
 $V_a = 2.3505677769729085$ and $V_e = 15670451.846486058$ at $V_{gs} = -1.1$
 $V_a = 2.954863513736966$ and $V_e = 19699090.091579773$ at $V_{gs} = -1.2$
 $V_a = 3.4644157581953796$ and $V_e = 23096105.054635864$ at $V_{gs} = -1.3$
 $V_a = 3.880048486852222$ and $V_e = 25866989.912348147$ at $V_{gs} = -1.4$
 $V_a = 4.207527965412073$ and $V_e = 28050186.436080486$ at $V_{gs} = -1.5$
 $V_a = 4.455038889866701$ and $V_e = 29700259.26577801$ at $V_{gs} = -1.6$
 $V_a = 4.631656562728734$ and $V_e = 30877710.418191563$ at $V_{gs} = -1.7$
 $V_a = 4.746377398055929$ and $V_e = 31642515.987039533$ at $V_{gs} = -1.8$
 $V_a = 4.807552663315228$ and $V_e = 32050351.088768188$ at $V_{gs} = -1.9$
 $V_a = 4.8226192291816865$ and $V_e = 32150794.861211244$ at $V_{gs} = -2.0$
 $V_a = 4.798031648869598$ and $V_e = 31986877.659130655$ at $V_{gs} = -2.1$
 $V_a = 4.739311335018513$ and $V_e = 31595408.90012342$ at $V_{gs} = -2.2$
 $V_a = 4.651155391598578$ and $V_e = 31007702.610657185$ at $V_{gs} = -2.3$
 $V_a = 4.537572788804766$ and $V_e = 30250485.258698445$ at $V_{gs} = -2.4$
 $V_a = 4.4020312699445014$ and $V_e = 29346875.132963344$ at $V_{gs} = -2.5$
 $V_a = 4.247620387175554$ and $V_e = 28317469.24783703$ at $V_{gs} = -2.6$
 $V_a = 4.077239182509167$ and $V_e = 27181594.550061118$ at $V_{gs} = -2.7$
 $V_a = 3.893816458816539$ and $V_e = 25958776.392110262$ at $V_{gs} = -2.8$
 $V_a = 3.7005224312228107$ and $V_e = 24670149.541485406$ at $V_{gs} = -2.9$
 $V_a = 3.5008484128258734$ and $V_e = 23338989.418839157$ at $V_{gs} = -3.0$

I_d vs V_{ds} at Active Region

