Data Mining Classification: Alternative Techniques

Thanks to [Tan,Steinbach, Kumar]

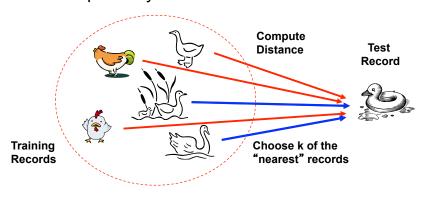
Instance-Based Classifiers Set of Stored Cases Store the training records Use training records to Atr1 AtrN Class predict the class label of A unseen cases В В Unseen Case C AtrN A С В

Instance Based Classifiers

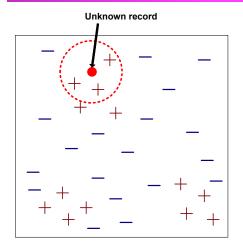
- Examples:
 - Rote-learner
 - Memorizes entire training data and performs classification only if attributes of record match one of the training examples exactly
 - Nearest neighbor
 - ◆ Uses k "closest" points (nearest neighbors) for performing classification

Nearest Neighbor Classifiers

- Basic idea:
 - If it walks like a duck, quacks like a duck, then it's probably a duck



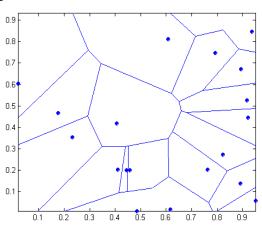
Nearest-Neighbor Classifiers



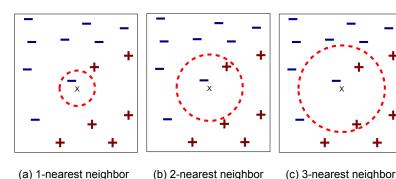
- Requires three things
 - The set of stored records
 - Distance Metric to compute distance between records
 - The value of k, the number of nearest neighbors to retrieve
- To classify an unknown record:
 - Compute distance to other training records
 - Identify k nearest neighbors
 - Use class labels of nearest neighbors to determine the class label of unknown record (e.g., by taking majority vote)

1 nearest-neighbor

Voronoi Diagram



Definition of Nearest Neighbor



K-nearest neighbors of a record x are data points that have the k smallest distance to x

Nearest Neighbor Classification

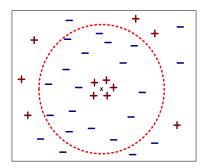
- Compute distance between two points:
 - Euclidean distance

$$d(p,q) = \sqrt{\sum_{i} (p_{i} - q_{i})^{2}}$$

- Determine the class from nearest neighbor list
 - take the majority vote of class labels among the k-nearest neighbors
 - Weigh the vote according to distance
 - ◆ weight factor, w = 1/d²

Nearest Neighbor Classification...

- Choosing the value of k:
 - If k is too small, sensitive to noise points
 - If k is too large, neighborhood may include points from other classes

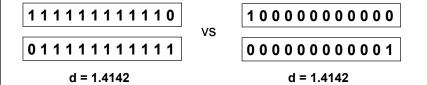


Nearest Neighbor Classification...

- Scaling issues
 - Attributes may have to be scaled to prevent distance measures from being dominated by one of the attributes
 - Example:
 - height of a person may vary from 1.5m to 1.8m
 - weight of a person may vary from 90lb to 300lb
 - income of a person may vary from \$10K to \$1M

Nearest Neighbor Classification...

- Problem with Euclidean measure:
 - High dimensional data
 - curse of dimensionality
 - Can produce counter-intuitive results



◆ Solution: Normalize the vectors to unit length

Nearest neighbor Classification...

- k-NN classifiers are lazy learners
 - It does not build models explicitly
 - Unlike eager learners such as decision tree induction and rule-based systems
 - Classifying unknown records are relatively expensive

Example: PEBLS

- PEBLS: Parallel Examplar-Based Learning System (Cost & Salzberg)
 - Works with both continuous and nominal features
 - ◆For nominal features, distance between two nominal values is computed using modified value difference metric (MVDM)
 - Each record is assigned a weight factor
 - Number of nearest neighbor, k = 1

Example: PEBLS

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

Distance between nominal attribute values:

d(Single, Married)

= | 2/4 - 0/4 | + | 2/4 - 4/4 | = 1

d(Single,Divorced)

= | 2/4 - 1/2 | + | 2/4 - 1/2 | = 0

d(Married, Divorced)

= |0/4 - 1/2| + |4/4 - 1/2| = 1

d(Refund=Yes,Refund=No)

= |0/3 - 3/7| + |3/3 - 4/7| = 6/7

Class	Marital Status				
Class	Single	Married	Divorced		
Yes	2	0	1		
No	2	4	1		

١		Refund		
١	Class	Yes	No	
Ī	Yes	0	3	
Ī	No	3	4	

$$d(V_1, V_2) = \sum_{i} \left| \frac{n_{1i}}{n_1} - \frac{n_{2i}}{n_2} \right|$$

Example: PEBLS

Tid	Refund	Marital Status	Taxable Income	Cheat
Х	Yes	Single	125K	No
Υ	No	Married	100K	No

Distance between record X and record Y:

$$\Delta(X,Y) = w_X w_Y \sum_{i=1}^d d(X_i, Y_i)^2$$

where:

 $w_X = \frac{\text{Number of times X is used for prediction}}{\text{Number of times X predicts correctly}}$

 $W_X \cong 1$ if X makes accurate prediction most of the time

 $w_X > 1$ if X is not reliable for making predictions

Bayes Classifier

- A probabilistic framework for solving classification problems
- Conditional Probability:

$$P(C \mid A) = \frac{P(A, C)}{P(A)}$$

$$P(A \mid C) = \frac{P(A,C)}{P(C)}$$

Bayes theorem:

$$P(C \mid A) = \frac{P(A \mid C)P(C)}{P(A)}$$

Example of Bayes Theorem

- Given:
 - A doctor knows that meningitis causes stiff neck 50% of the time
 - Prior probability of any patient having meningitis is 1/50,000
 - Prior probability of any patient having stiff neck is 1/20
- If a patient has stiff neck, what's the probability he/she has meningitis?

$$P(M \mid S) = \frac{P(S \mid M)P(M)}{P(S)} = \frac{0.5 \times 1/50000}{1/20} = 0.0002$$

Bayesian Classifiers

- Consider each attribute and class label as random variables
- Given a record with attributes (A₁, A₂,...,A_n)
 - Goal is to predict class C
 - Specifically, we want to find the value of C that maximizes P(C| A₁, A₂,...,A_n)
- Can we estimate P(C| A₁, A₂,...,A_n) directly from data?

Bayesian Classifiers

- Approach:
 - compute the posterior probability $P(C \mid A_1, A_2, ..., A_n)$ for all values of C using the Bayes theorem

$$P(C \mid A_1 A_2 \dots A_n) = \frac{P(A_1 A_2 \dots A_n \mid C) P(C)}{P(A_1 A_2 \dots A_n)}$$

- Choose value of C that maximizes
 P(C | A₁, A₂, ..., A_n)
- Equivalent to choosing value of C that maximizes $P(A_1, A_2, ..., A_n|C) P(C)$
- How to estimate $P(A_1, A_2, ..., A_n \mid C)$?

Naïve Bayes Classifier

- Assume independence among attributes A_i when class is given:
 - $P(A_1, A_2, ..., A_n | C) = P(A_1 | C_j) P(A_2 | C_j)... P(A_n | C_j)$
 - Can estimate P(A_i| C_i) for all A_i and C_i.
 - New point is classified to C_j if $P(C_j)$ Π $P(A_i|C_j)$ is maximal.

How to Estimate Probabilities from Data?

Tid	Refund	Marital Status	Taxable Income	Evade
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

- Class: $P(C) = N_c/N$
 - e.g., P(No) = 7/10, P(Yes) = 3/10
- For discrete attributes:

$$P(A_i \mid C_k) = |A_{ik}| / N_{c_k}$$

- where $|A_{ik}|$ is number of instances having attribute A, and belongs to class C_k
- Examples:

P(Status=Married|No) = 4/7 P(Refund=Yes|Yes)=0

How to Estimate Probabilities from Data?

- For continuous attributes:
 - Discretize the range into bins
 - one ordinal attribute per bin
 - violates independence assumption
 - Two-way split: (A < v) or (A > v)
 - choose only one of the two splits as new attribute
 - Probability density estimation:
 - Assume attribute follows a normal distribution.
 - Use data to estimate parameters of distribution (e.g., mean and standard deviation)
 - Once probability distribution is known, can use it to estimate the conditional probability P(A_i|c)

How to Estimate Probabilities from Data?

Tid	Refund	Marital Status	Taxable Income	Evade
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

Normal distribution:

$$P(A_{i} \mid c_{j}) = \frac{1}{\sqrt{2\pi\sigma_{ij}^{2}}} e^{\frac{(A_{i} - \mu_{ij})^{2}}{2\sigma_{ij}^{2}}}$$

- One for each (A_i,c_i) pair
- For (Income, Class=No):
 - If Class=No.
 - ◆ sample mean = 110
 - ◆ sample variance = 2975

$$P(Income = 120 \mid No) = \frac{1}{\sqrt{2\pi}(54.54)} e^{\frac{(120-110)^2}{2(2975)}} = 0.0072$$

Example of Naïve Bayes Classifier

Given a Test Record:

X = (Refund = No, Married, Income = 120K)

naive Bayes Classifier:

P(Refund=Yes|No) = 3/7

P(Refund=NolNo) = 4/7P(Refund=Yes|Yes) = 0 P(Refund=NolYes) = 1 P(Marital Status=Single|No) = 2/7 P(Marital Status=Divorced|No)=1/7 P(Marital Status=MarriedINo) = 4/7 P(Marital Status=Single|Yes) = 2/7 P(Marital Status=DivorcedlYes)=1/7 P(Marital Status=Married|Yes) = 0

For taxable income:

sample mean=110 sample variance=2975

sample mean=90 If class=Yes:

sample variance=25

- P(X|Class=No) = P(Refund=No|Class=No) × P(Married| Class=No) × P(Income=120Kl Class=No) $= 4/7 \times 4/7 \times 0.0072 = 0.0024$
- P(X|Class=Yes) = P(Refund=No| Class=Yes) × P(Marriedl Class=Yes) × P(Income=120KI Class=Yes) $= 1 \times 0 \times 1.2 \times 10^{-9} = 0$

Since P(X|No)P(No) > P(X|Yes)P(Yes)Therefore P(No|X) > P(Yes|X)

=> Class = No

Naïve Bayes Classifier

- If one of the conditional probability is zero, then the entire expression becomes zero
- Probability estimation:

Original:
$$P(A_i \mid C) = \frac{N_{ic}}{N_c}$$

Laplace:
$$P(A_i \mid C) = \frac{N_{ic} + 1}{N_c + k}$$

m-estimate:
$$P(A_i \mid C) = \frac{N_{ic} + mp}{N_c + m}$$

 N_{ic} : number of objects with value A_i in class c

N_c: number of objects in class c

k: number of distinct values of A

p: prior probability

m: parameter

Naïve Bayes (Summary)

- Robust to isolated noise points
- Handle missing values by ignoring the instance during probability estimate calculations
- Robust to irrelevant attributes
- Independence assumption may not hold for some attributes
 - Use other techniques such as Bayesian Belief Networks (BBN)

Example of Naïve Bayes Classifier

Name	Give Birth	Can Fly	Live in Water	Have Legs	Class
human	yes	no	no	yes	mammals
python	no	no	no	no	non-mammals
salmon	no	no	yes	no	non-mammals
whale	yes	no	yes	no	mammals
frog	no	no	sometimes	yes	non-mammals
komodo	no	no	no	yes	non-mammals
bat	yes	yes	no	yes	mammals
pigeon	no	yes	no	yes	non-mammals
cat	yes	no	no	yes	mammals
leopard shark	yes	no	yes	no	non-mammals
turtle	no	no	sometimes	yes	non-mammals
penguin	no	no	sometimes	yes	non-mammals
porcupine	yes	no	no	yes	mammals
eel	no	no	yes	no	non-mammals
salamander	no	no	sometimes	yes	non-mammals
gila monster	no	no	no	yes	non-mammals
platypus	no	no	no	yes	mammals
owl	no	yes	no	yes	non-mammals
dolphin	yes	no	yes	no	mammals
eagle	no	yes	no	ves	non-mammals

- A: attributes
- M: mammals
- N: non-mammals

$$P(A|M) = \frac{6}{7} \times \frac{6}{7} \times \frac{2}{7} \times \frac{2}{7} = 0.06$$

$$P(A|N) = \frac{1}{13} \times \frac{10}{13} \times \frac{3}{13} \times \frac{4}{13} = 0.0042$$

$$P(A \mid M)P(M) = 0.06 \times \frac{7}{20} = 0.021$$

$$P(A|N)P(N) = 0.004 \times \frac{13}{20} = 0.0027$$

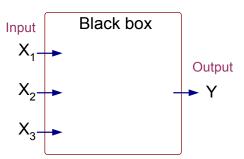
Give Birth	Can Fly	Live in Water	Have Legs	Class
yes	no	yes	no	?

P(A|M)P(M) > P(A|N)P(N)

=> Mammals

Artificial Neural Networks (ANN)

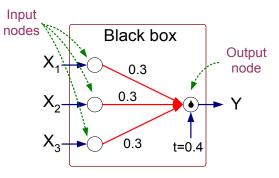
X_1	X_2	X_3	Υ
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	0
0	1	0	0
0 0	1	1	1
0	0	0	0



Output Y is 1 if at least two of the three inputs are equal to 1.

Artificial Neural Networks (ANN)

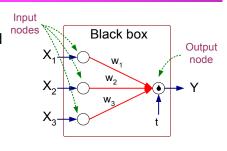
X_1	X_2	X_3	Υ
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1
0	0	1	0
0	1	0	0
0	1	1	1
0	0	0	0



$$Y = I(0.3X_1 + 0.3X_2 + 0.3X_3 - 0.4 > 0)$$
where $I(z) = \begin{cases} 1 & \text{if } z \text{ is true} \\ 0 & \text{otherwise} \end{cases}$

Artificial Neural Networks (ANN)

- Model is an assembly of inter-connected nodes and weighted links
- Output node sums up each of its input value according to the weights of its links
- Compare output node against some threshold t

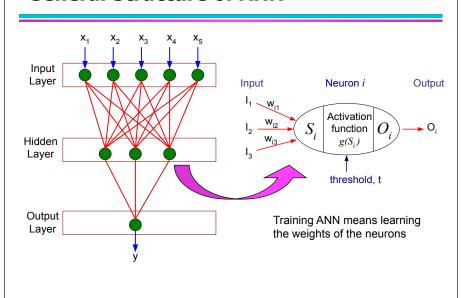


Perceptron Model

$$Y = I(\sum_{i} w_{i}X_{i} - t) \text{ or}$$

$$Y = sign(\sum_{i} w_{i}X_{i} - t)$$

General Structure of ANN



Algorithm for learning ANN

- Initialize the weights (w₀, w₁, ..., w_k)
- Adjust the weights in such a way that the output of ANN is consistent with class labels of training examples
 - Objective function: $E = \sum_{i} [Y_i f(w_i, X_i)]^2$
 - Find the weights w_i's that minimize the above objective function
 - e.g., backpropagation algorithm (see lecture notes)