

# Physics 152 Review

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24 March 2017

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# 1 Chapter 14

## 1.1 Simple Harmonic Motion

$$F_x = ma_x = -kx \quad (1)$$

$$x(t) = A \cos[\omega t + \delta] \quad (2)$$

$$\omega_{spring} = \sqrt{\frac{k}{m}} \quad (3)$$

$$\omega_{pendulum} = \sqrt{\frac{g}{l}} \quad (4)$$

$$E = K + U \quad (5)$$

$$= \frac{1}{2}kA^2 \quad (6)$$

$$\omega = 2\pi f \quad (7)$$

$$= \frac{2\pi}{T} \quad (8)$$

- (1) The equation for the linear restoring force, where  $k$  is the spring constant.
- (2) The basic position equation, where  $x$  is the positions,  $A$  is the amplitude,  $\omega$  is the angular frequency,  $t$  is the time, and  $\delta$  is the phase offset.
- (3) The  $\omega$  for a spring, where  $k$  is the spring constant, and  $m$  is the mass at the end of the spring.
- (4) The  $\omega$  for a simple pendulum, where  $g$  is gravity, and  $l$  is the length of the pendulum.
- (5) The mechanical energy equation for a wave, where  $E$  is total energy,  $K$  is the kinetic energy, and  $U$  is the potential energy.
- (6) The mechanical energy equation for a wave, where  $k$  is the spring constant, and  $A$  is the amplitude.
- (7) The angular frequency equation, where  $\omega$  is the angular frequency, and  $f$  is the frequency.
- (8) The angular frequency equation, where  $T$  is the period.

## 1.2 Damped Harmonic Motion

$$A = A_0 e^{\frac{t}{2\tau}} \quad (9)$$

$$E = E_0 e^{\frac{-t}{\tau}} \quad (10)$$

$$\tau = \frac{m}{b} \quad (11)$$

$$Q = \omega_0 \tau \quad (12)$$

$$\omega' = \omega_0 \sqrt{1 - \frac{1}{4Q^2}} \quad (13)$$

$$Q = \frac{1\pi}{\left(\frac{|\Delta E|}{E}\right)_{cycle}} \quad \text{When } \left(\frac{|\Delta E|}{E}\right)_{cycle} \ll 1 \quad (14)$$

- (9) Amplitude equation, where  $A_0$  is the initial amplitude,  $t$  is the time, and  $\tau$  is the decay time.
- (10) Energy equation, where  $E_0$  is the initial energy,  $t$  is the time, and  $\tau$  is the decay time.
- (11) Decay time equation, where  $\tau$  is the decay time,  $m$  is the mass, and  $b$  is the damping constant.
- (12) Q factor definition, where  $Q$  is the Q factor,  $\omega_0$  is the initial angular frequency, and  $\tau$  is the decay time.
- (13) Frequency for a damped oscillation, where  $\omega'$  is the angular frequency,  $\omega_0$  is the initial angular frequency, and  $Q$  is the Q factor.
- (14) Q factor of weak dampining, where  $Q$  is the Q factor, and  $\left(\frac{|\Delta E|}{E}\right)_{cycle}$  is the percentage change of energy per cycle.

## 2 Chapter 15

### 2.1 Traveling Waves

$$v_{string} = \sqrt{\frac{F_T}{\mu}} \quad (15)$$

$$v_{sound} = \sqrt{\frac{B}{\rho}} \quad (16)$$

$$v_{sound} = 343 \frac{m}{s} \quad (17)$$

$$c = 3.00 \times 10^8 \frac{m}{s} \quad (18)$$

$$r = \frac{v_2 - v_1}{v_2 + v_1} \quad (19)$$

$$\tau = \frac{2v_2}{v_2 + v_1} \quad (20)$$

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} * \frac{\partial^2 y}{\partial t^2} \quad (21)$$

- (15) Speed of wave on a string, where  $v$  is the velocity of the wave,  $F_T$  is the tension force, and  $\mu$  is the linear density of the string.
- (16) Speed of sound wave in a fluid, where  $v$  is the velocity of the wave,  $B$  is the Bulk Modulus, and  $\rho$  is the volume density of the fluid.
- (17) Constant of the speed of sound in air.
- (18) Constant of the speed of light/electromagnetic waves in vacuum.
- (19) Reflection coefficient equation, where  $r$  is the reflection coefficient,  $v_1$  is the wave velocity in the first region, and  $v_2$  is the wave velocity in the second region.
- (20) Transmission coefficient equation, where  $\tau$  is the transmission coefficient,  $v_1$  is the wave velocity in the first region, and  $v_2$  is the wave velocity in the second region.
- (21) Wave equation for a traveling wave.

## 2.2 Harmonic Traveling Waves

$$y(x, t) = A \sin(kx \pm \omega t) \quad (22)$$

$$= A \sin(k(x \pm vt)) \quad (23)$$

$$k = \frac{2\pi}{\lambda} \quad (24)$$

$$v = f\lambda \quad (25)$$

$$= \frac{\omega}{k} \quad (26)$$

$$\omega = 2\pi f \quad (27)$$

$$= \frac{2\pi}{T} \quad (28)$$

$$P_{avg} = \frac{1}{2} \mu v \omega^2 A^2 \quad (29)$$

$$I = \frac{P_{avg}}{A} \quad (30)$$

$$\beta = (10 \text{ dB}) \log_{10} \left( \frac{I}{I_0} \right) \quad (31)$$

$$I_0 = 10^{12} \frac{\text{W}}{\text{m}^2} \quad (32)$$

- (22) Wave equation, where  $y$  is the height,  $x$  is the position,  $t$  is the time,  $A$  is the amplitude,  $k$  is the wave number, and  $\omega$  is the angular frequency. Use  $+$  for waves traveling in the  $+x$  direction, and use  $-$  for waves traveling in the  $-x$  direction.
- (23) Wave equation, where  $A$  is the amplitude,  $k$  is the wave number,  $x$  is the position,  $v$  is the wave speed, and  $t$  is the time.
- (24) Wave number equation, where  $k$  is the wave number, and  $\lambda$  is the wave length.
- (25) Wave speed equation, where  $v$  is the wave speed,  $f$  is the frequency, and  $\lambda$  is the wavelength.
- (26) Wave speed equation, where  $\omega$  is the angular frequency, and  $k$  is the wave number.
- (27) Angular frequency equation, where  $\omega$  is the angular frequency, and  $f$  is the frequency.
- (28) Angular frequency equation, where  $T$  is the period.
- (29) Average power for a harmonic wave on a string, where  $P_{avg}$  is average power,  $\mu$  is the linear density of the string,  $v$  is the velocity of the string,  $\omega$  is the angular frequency, and  $A$  is the amplitude.

- (30) Intensity of a harmonic wave, where  $I$  is the intensity,  $P_{avg}$  is the average power, and  $A$  is the amplitude.
- (31) Intensity of a wave in dB, where  $\beta$  is the intensity in dB,  $I$  is the intensity, and  $I_0$  is a constant.
- (32) Constant of  $I_0$ .

## 2.3 Doppler Shifts

$$f_r = \frac{v \pm u_r}{\lambda} \quad (33)$$

$$\lambda = \frac{v \pm u_s}{f_s} \quad (34)$$

$$f_r = \frac{v \pm u_r}{v \pm u_s} f_s \quad (35)$$

$$\frac{f_r}{v \pm u_r} = \frac{f_s}{v \pm u_s} \quad (36)$$

$$u \ll v \quad \text{Where } u = u_s \pm u_r \quad (37)$$

$$\frac{\Delta f}{f_s} \approx \pm \frac{u}{v} \quad (38)$$

- (33) Frequency received when the receiver is moving, where  $f_r$  is the frequency,  $v$  is the speed of the wave,  $u_r$  is the speed of the receiver, and  $\lambda$  is the wavelength.
- (34) Wavelength of wave when the source is moving, where  $\lambda$  is the wavelength,  $v$  is the speed of the wave, and  $u_s$  is the speed of the source.
- (35) Frequency if either the source or receiver is moving, where  $f_r$  is the frequency received,  $v$  is the speed of the wave,  $u_r$  is the speed of the receiver,  $u_s$  is the speed of the source, and  $f_s$  is the frequency emitted by the source. Choose signs that give and up-shift in frequency for an approaching source or receiver, and vice versa.
- (36) Equation relating frequency of source and receiver, where  $f_r$  is the frequency received,  $v$  is the speed of the wave,  $u_r$  is the speed of the receiver,  $f_s$  is the frequency emitted by the source, and  $u_s$  is the speed of the source.
- (37) For small speed of the source and receiver comparatively to the wave, the estimation is true, where  $u$  is the speed of the source and receiver,  $v$  is the speed of the wave,  $u_s$  is the speed of the source, and  $u_r$  is the speed of the receiver.
- (38) This approximation only holds if (37) is true, then this is true, where  $\Delta f$  is the change in frequency,  $f_s$  is the frequency emitted by the source,  $u$  is the velocity of the source and receiver from (37), and  $v$  is the velocity of the wave.

### 3 Chapter 16

#### 3.1 Superposition and Standing waves

$$y = y_1 + y_2 \quad (39)$$

$$= y_0 \sin(kx - \omega t) + y_0 \sin(kx - \omega t + \delta) \quad (40)$$

$$= \left( 2y_0 \cos\left(\frac{\delta}{2}\right) \right) \sin\left(kx - \omega t + \frac{\delta}{2}\right) \quad (41)$$

$$\delta = k\Delta x \quad (42)$$

$$= 2\pi \frac{\Delta x}{\lambda} \quad (43)$$

$$\lambda_n = \frac{2L}{n} \quad n = 1, 2, 3, 4... \quad (44)$$

$$\lambda_n = \frac{4L}{n} \quad n = 1, 3, 5, 7... \quad (45)$$

The superposition of two waves with the same amplitude, wave number, and frequency, but phase difference  $\delta$ , results in a harmonic wave of the same wave number and frequency, but differing in phase and amplitude from each of the two waves.

- (39) The amplitude of the wave is the sum of the amplitudes of each wave, where  $y$  is the resultant value,  $y_1$  is the value of the first wave, and  $y_2$  is the value of the second wave.
- (40) Superposition of two waves, where  $y_0$  is the amplitude of the source,  $k$  is the wave number,  $x$  is the position,  $\omega$  is the angular frequency,  $t$  is the time, and  $\delta$  is the phase difference.
- (41) Superposition of two waves, where  $y_0$  is the amplitude of the source,  $\delta$  is the phase difference,  $k$  is the wave number,  $x$  is the position,  $\omega$  is the angular frequency, and  $t$  is the time.
- (42) Phase difference due to path difference, where  $\delta$  is the phase difference,  $k$  is the wave number, and  $\Delta x$  is the difference between distances from the two sources.
- (43) Phase difference due to path difference, where  $\Delta x$  is the difference between the distances from the two sources, and  $\lambda$  is the wavelength.
- (44) Wavelength for standing wave fixed at both ends, where  $n$  is the wave number,  $\lambda_n$  is the wavelength for that wave number, and  $L$  is the length of string.
- (45) Wavelength for standing wave fixed at one end, where  $n$  is the wave number,  $\lambda_n$  is the wavelength for that wave number, and  $L$  is the length of string.



## 4 Chapter 31

### 4.1 Speed of Light

$$c = 299,792,458 \frac{m}{s} \quad (46)$$

$$v = \frac{c}{n} \quad (47)$$

(46) Speed of light in a vacuum.

(47) Speed of light in a transparent medium, where  $n$  is the index of refraction.

### 4.2 Reflection and Refraction

$$\theta_1 = \theta'_1 \quad (48)$$

$$I = \left( \frac{n_1 - n_2}{n_1 + n_2} \right)^2 I_0 \quad (49)$$

$$n = \frac{c}{v} \quad (50)$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \quad (51)$$

$$n_1 \sin \theta_c = n_2 \sin 90 \quad (52)$$

$$\theta_c = \sin^{-1} \left( \frac{n_2}{n_1} \right) \quad (53)$$

$$r = \frac{n_2 - n_1}{n_2 + n_1} \quad (54)$$

(48) Law of reflection.

(49) Reflected intensity.

(50) Index of refraction for a medium.

(51) Snell's Law(Law of refraction).

(52) Total internal reflection for critical angle.

(53) Critical angle for total internal reflection.

(54) Reflection coefficient.

### 4.3 Polarization

$$I = I_0 \cos^2 \theta \quad (55)$$

$$\theta_p = \tan^{-1} \left( \frac{n_2}{n_1} \right) \quad (56)$$

- (55) Malus's Law, for intensity of transmitted light through angled polarizers.
- (56) Angle of polarization from reflection.

## 5 Chapter 32

### 5.1 Mirrors

$$\frac{1}{s} + \frac{1}{s'} = \frac{1}{f} \quad (57)$$

$$f = \frac{r}{2} \quad (58)$$

$$m = \frac{y'}{y} = -\frac{s'}{s} \quad (59)$$

(57) Mirror equation, where  $s$  is the position of the object, and  $s'$  is the position of the image.

(58) Definition of focal length.

(59) Equation for lateral magnification.

### 5.2 Lenses

$$\frac{1}{f} = (n - 1) \left( \frac{1}{f_1} - \frac{1}{f_2} \right) \quad (60)$$

(60) Lense-Maker's Equation. if  $f > 0$  then the lense is converging, if  $f < 0$  then the lense is diverging.

## 6 Chapter 33

### 6.1 Interference

$$\delta = k\Delta x = s\pi \frac{\Delta x}{\lambda} \quad (61)$$

(62)

(61) Phase shift from path difference.

### 6.2 Diffraction

$$d\sin(\theta_m) = m\lambda \quad m = 0, 1, 2, \dots \quad (63)$$

$$a\sin(\theta_m) = m\lambda \quad m = 0, 1, 2, \dots \quad (64)$$

$$d\sin(\theta_m) = m\lambda \quad m = 0, 1, 2, \dots \quad (65)$$

$$\alpha_c = 1.22 \frac{\lambda}{D} \quad (66)$$

(63) Diffraction grating maxima.

(64) Single slit interference minima.

(65) Two slit interference maxima.

(66) Rayleigh's criterion.