```
    1: """
    2: The Magnetic Field from Current Distribution
    3: """
    4:
    5: from math import *
    6: from pylab import show, imshow
    7: import numpy as np
    8:
    9:
   10: def simpson(func, a, b, h=0.001):
   11:     """Approximates integral using simpson method"""
   12:     n = int(abs(b - a) / h)
   13:     n -= 1 if n % 2 == 1 else 0
   14:     return (h / 3.0) * (
   15:         func(a) + func(b) +
   16:         (4.0 * sum([func(a + (k * h)) for k in range(1, n, 2)])) +
   17:         (2.0 * sum([func(a + (k * h)) for k in range(2, n - 1, 2)])))
   18:
   19: def adaptive(func, a, b, h=0.001, delta=10e-4):
   20:     """Approximates integral using adaptive method"""
   21:     n = int(abs(b - a) / h)
   22:     i0 = h * ((0.5 * (func(a) + func(b))) + sum(
   23:         [func(a + k * h) for k in range(1, int((b - a) / h))]))
   24:     epsilon = delta + 10
   25:     while epsilon > delta:
   26:         h /= 2
   27:         n *= 2
   28:         i1 = (0.5 * i0) + (h * sum([func(a + k * h) for k in range(1, n, 2)]))
   29:         epsilon = abs(i1 - i0) / 3
   30:         i0 = i1
   31:     return i1
   32:
   33:
   34: def B(x, y, z):
   35:     func_x = lambda theta: (2 * z * sin(theta)) / pow((x - 3 * cos(theta))**2 + (y - 2
* sin(theta))**2 + z**2, 3 / 2)
   36:     func_y = lambda theta: -(3 * z * cos(theta)) / pow((x - 3 * cos(theta))**2 + (y - 2
 * sin(theta))**2 + z**2, 3 / 2)
   37:     func_z = lambda theta: (3 * y * cos(theta) - 2 * x * sin(theta)) / pow((x - 3 * cos
(theta))**2 + (y - 2 * sin(theta))**2 + z**2, 3 / 2)
   38:     comp_x = simpson(func_x, 0, 2 * pi, 0.1)
   39:     comp_y = simpson(func_y, 0, 2 * pi, 0.1)
   40:     comp_z = simpson(func_z, 0, 2 * pi, 0.1)
   41:     return (comp_x, comp_y, comp_z)
   42:
   43: def B_adaptive(x, y, z):
   44:     func_x = lambda theta: (2 * z * sin(theta)) / pow((x - 3 * cos(theta))**2 + (y - 2
* sin(theta))**2 + z**2, 3 / 2)
   45:     func_y = lambda theta: -(3 * z * cos(theta)) / pow((x - 3 * cos(theta))**2 + (y - 2
 * sin(theta))**2 + z**2, 3 / 2)
   46:     func_z = lambda theta: (3 * y * cos(theta) - 2 * x * sin(theta)) / pow((x - 3 * cos
(theta))**2 + (y - 2 * sin(theta))**2 + z**2, 3 / 2)
   47:     comp_x = adaptive(func_x, 0, 2 * pi, 0.1, 10e-4)
   48:     comp_y = adaptive(func_y, 0, 2 * pi, 0.1, 10e-4)
   49:     comp_z = adaptive(func_z, 0, 2 * pi, 0.1, 10e-4)
   50:     return (comp_x, comp_y, comp_z)
   51:
   52:
   53: def main():
   54:
   55:     def a():
   56:         print(B(1, 4, 7))
   57:
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```
    def b():
        print(B_adaptive(1,2,5))
    def c():
        data = []
        for y in np.arange(-5, 5, 0.1):
            row = []
            for x in np.arange(-5, 5, 0.1):
                b = B_adaptive(x, y, 1)
                row.append(np.sqrt(b[0]**2+b[1]**2+b[2]**2))
            data.append(row)
        imshow(data)
        show()

    a()
    b()
    c()


if __name__ == "__main__":
    main()
```