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1: import numpy as np
2: from matplotlib import animation
3: import pylab
4:
5: def RungeKutta(f1, f2, f3, f4, a_init, b_init, c_init, d_init, t0, tf, h=0.1):
6:     A = []
7:     B = []
8:     C = []
9:     D = []
10:    T = np.arange(t0, tf, h)
11:    a = a_init
12:    b = b_init
13:    c = c_init
14:    d = d_init
15:    for t in T:
16:        A.append(a)
17:        B.append(b)
18:        C.append(c)
19:        D.append(d)
20:        k1 = h*f1(a,b,c,d,t)
21:        l1 = h*f2(a,b,c,d,t)
22:        m1 = h*f3(a,b,c,d,t)
23:        n1 = h*f4(a,b,c,d,t)
24:        k2 = h*f1(a+k1/2,b+l1/2,c+m1/2,d+n1/2,t+h/2)
25:        l2 = h*f2(a+k1/2,b+l1/2,c+m1/2,d+n1/2,t+h/2)
26:        m2 = h*f3(a+k1/2,b+l1/2,c+m1/2,d+n1/2,t+h/2)
27:        n2 = h*f4(a+k1/2,b+l1/2,c+m1/2,d+n1/2,t+h/2)
28:        k3 = h*f1(a+k2/2,b+l2/2,c+m2/2,d+n2/2,t+h/2)
29:        l3 = h*f2(a+k2/2,b+l2/2,c+m2/2,d+n2/2,t+h/2)
30:        m3 = h*f3(a+k2/2,b+l2/2,c+m2/2,d+n2/2,t+h/2)
31:        n3 = h*f4(a+k2/2,b+l2/2,c+m2/2,d+n2/2,t+h/2)
32:        k4 = h*f1(a+k3,b+l3,c+m3,d+n3,t+h)
33:        l4 = h*f2(a+k3,b+l3,c+m3,d+n3,t+h)
34:        m4 = h*f3(a+k3,b+l3,c+m3,d+n3,t+h)
35:        n4 = h*f4(a+k3,b+l3,c+m3,d+n3,t+h)
36:        a += (k1+2*k2+2*k3+k4)/6
37:        b += (l1+2*l2+2*l3+l4)/6
38:        c += (m1+2*m2+2*m3+m4)/6
39:        d += (n1+2*n2+2*n3+n4)/6
40:    return T, A, B, C, D
41:
42: def main():
43:     MsG = 4*np.pi**2
44:     f1 = lambda x, y, vx, vy, t: vx
45:     f2 = lambda x, y, vx, vy, t: vy
46:     f3 = lambda x, y, vx, vy, t: -MsG*x/pow(x**2+y**2, 3/2)
47:     f4 = lambda x, y, vx, vy, t: -MsG*y/pow(x**2+y**2, 3/2)
48:     T, X, Y, Vx, Vy = RungeKutta(f1,f2,f3,f4, 1, 0, 0, 2*np.pi, 0.0, 10, 0.01)
49:     print("Calculated")
50:     fig, ax = pylab.subplots()
51:     line, = ax.plot(X[0], Y[0], 'ko')
52:     pylab.ylim((-1.1, 1.1))
53:     pylab.xlim((-1.1, 1.1))
54:     def init():
55:         line.set_data(X[0], Y[0])
56:         return line,
57:     def anim(i):
58:         line.set_data(X[i], Y[i])
59:         return line,
60:     ani = animation.FuncAnimation(fig, anim, init_func=init, interval=20, frames=range(
len(T)))
61:     pylab.show()
62:
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63: if __name__ == "__main__":  
64:     main()
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