```
 1: from numpy import arange
 2: from pylab import *
 3:
 4:
 5: def trapazoidal(f, ax, bx, ay, by, h=0.001):
 6:     h2 = h**2
 7:     Nx = int(abs(bx - ax) / h)
 8:     Ny = int(abs(by - ay) / h)
 9:     corner = 0.25 * (f(ax, ay) + f(ax, by) + f(bx, ay) + f(bx, by))
10:     edge = 0.5 * (sum([f(ax, ay + i * h) for i in range(1, Ny)]) + sum([
11:         f(bx, ay + i * h) for i in range(1, Ny)
12:     ]) + sum([f(ax + i * h, ay) for i in range(1, Nx)]) + sum(
13:         [f(ax + i * h, by) for i in range(1, Nx)]))
14:     inner = sum([
15:         sum([f(ax + i * h, ay + k * h)
16:              for k in range(1, Ny)])
17:         for i in range(1, Nx)
18:     ])
19:     return (h**2) * (corner + edge + inner)
20:
21: def p2():
22:     ep = 8.854187871e-12
23:
24:     def dist(p1, p2):
25:         return sqrt((p1[0] - p2[0])**2 + (p1[1] - p2[1])**2 +
26:                     (p1[2] - p2[2])**2)
27:
28:     def diff(a, b):
29:         return abs(a - b) >= 1e-5
30:
31:     def V(q, r):
32:         return q / (4 * pi * ep * r)
33:
34:     def E(q, r):
35:         return q / (4 * pi * ep * r**2)
36:
37:     def potential(x, y, z):
38:         return V(-1, dist([-0.05, 0, 0], [x, y, z])) + V(
39:             1, dist([0.05, 0, 0], [x, y, z]))
40:
41:     def Ex(x, y, z):
42:         return (potential(x + 1e-8, y, z) - potential(x, y, z)) / 1e-8
43:
44:     def Ey(x, y, z):
45:         return (potential(x, y + 1e-8, z) - potential(x, y, z)) / 1e-8
46:
47:     def a():
48:         data = [[potential(x, y, 0)
49:                  for x in arange(-0.5, 0.5, 0.01)]
50:                 for y in arange(-0.5, 0.5, 0.01)]
51:         imshow(data, vmax=1e10, vmin=-1e10)
52:         show()
53:
54:     def b():
55:         vec_u = [[-Ex(x, y, 0)
56:                   for x in arange(-0.5, 0.5, 0.01)]
57:                  for y in arange(-0.5, 0.5, 0.01)]
58:         vec_v = [[-Ey(x, y, 0)
59:                   for x in arange(-0.5, 0.5, 0.01)]
60:                  for y in arange(-0.5, 0.5, 0.01)]
61:         for i in range(len(vec_u)):
62:             for j in range(len(vec_u[i])):
63:                 if abs(vec_u[i][j]) > 1e12 or abs(vec_v[i][j]) > 1e12:
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   64:                     vec_u[i][j] = 0
   65:                     vec_v[i][j] = 0
   66:         quiver(vec_u, vec_v)
   67:         show()
   68:
   69:     def c():
   70:         L = .1
   71:         sigma = lambda x, y, z: 100 * sin(2 * pi * x / L) * sin(2 * pi * y / L)
   72:
   73:         def gen(a, b, c):
   74:             return lambda x, y: 0 if (b-y) == (a-x) == 0 else (sigma(x, y, 0) / (4 * pi
 * ep * sqrt((a - x)**2 + (b - y)**2 + (c - 0)**2)))
   75:
   76:         potential = [[ trapazoidal(gen(a, b, 0), -0.05, 0.05, -0.05, 0.05, 0.01) for a
in arange(-0.05, 0.05, 0.01) ] for b in arange(-0.05, 0.05, 0.01)]
   77:
   78:         vec_u = [[(potential[i + 1][j] - potential[i][j]) / 0.01 if i != (len(potential
[j])) - 1 else (potential[i-1][j]-potential[i][j])/0.01
   79:                   for i in range(len(potential[j]))]
   80:                  for j in range(len(potential) - 1)]
   81:         vec_v = [[(potential[i][j + 1] - potential[i][j]) / 0.01 if i != (len(potential
[j])) - 1 else (potential[i-1][j]-potential[i][j])/0.01
   82:                   for i in range(len(potential[j]))]
   83:                  for j in range(len(potential) - 1)]
   84:         imshow(potential)
   85:         quiver(vec_u, vec_v)
   86:         show()
   87:
   88:     a()
   89:     b()
   90:     c()
   91:
   92: if __name__ == "__main__":
   93:     p2()
```