

Math 215 – Fall 2017

Practice Homework # 3 – Assigned September 14th, due September 18th

Note: Remember that you must show your work to get full credit for a problem.

1. A grocery store in a small town has 600 lottery tickets for sale. Since the town only has a population of 1200 people, the store has stated that no person may get more than 1 ticket.

- (a) How many ways are there to distribute all the tickets among the town residents? Explain your reasoning.
- (b) Suppose the store changes its policy so that no person may get more than 2 tickets. How many ways are there to distribute all the tickets.

2. For each of the following logical statements state if it is a tautology, contradiction, or neither.

- (a)
$$(A \rightarrow B) \leftrightarrow (\neg B \rightarrow \neg A).$$

- (b)
$$(A \rightarrow B) \rightarrow (B \rightarrow A).$$

- (c)
$$(C \rightarrow (A \vee B)) \rightarrow (A \rightarrow B).$$

- (d)
$$(((A \vee B) \rightarrow C) \wedge A) \rightarrow C.$$

- (e)
$$(Q \rightarrow (P \wedge \neg Q)) \wedge Q.$$

3. Create a true table for every part of the following logical statements.

- (a)
$$(A \vee B) \rightarrow (B \rightarrow A).$$

- (b)
$$A \rightarrow (B \rightarrow (A \wedge B)).$$

4. Reduce the following logical statements to disjunctive normal form using De Morgan's and the distributive laws.

- (a)
$$(A \vee B) \wedge (C \vee D)$$

- (b)
$$(A \rightarrow B) \wedge C$$