$Math\ 215-Fall\ 2017$

Practice Homework 14 – Assigned November 2nd, due November 6th **Note:** Remember that you must show your work to get full credit for a problem.

1. Please prove or disprove that each of the following functions is 1-1 and/or onto. (So two carefully written proofs must be given for each part.)

a.
$$f: \mathbb{R} \to \mathbb{R}$$
 given by $f(x) = 4x - 1$

b.
$$f: \mathbb{N} \to \mathbb{N}$$
 given by $f(n) = 4n - 1$

c.
$$f: \mathcal{P}(\{a,b,c,d\}) \to \mathcal{P}(\{a,b,c,d\})$$
 given by $f(S) = S \cap \{a,b\}$

d.
$$f: \mathcal{P}(\{a, b, c, d\}) \to \mathcal{P}(\{a, b, c, d\})$$
 given by $f(S) = S \cup \{a\}$

e.
$$f: \mathbb{R}^2 \to \mathbb{R}$$
 given by $f(x,y) = x^2 + y^2$

f.
$$f: \mathbb{R}^2 \to \mathbb{R}$$
 given by $f(x, y) = xy$