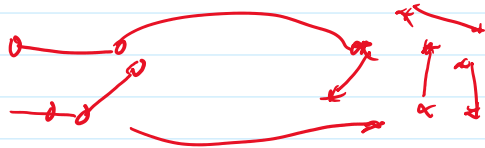


Homophily - Assortative Mixing.



What is the prob. that kids interact w' kids.

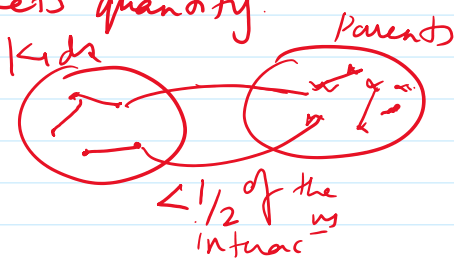
$k - k \rightarrow$
 $\{k - P\} \rightarrow \frac{1}{2}$
 $P - P \rightarrow$

Tossing a coin twice

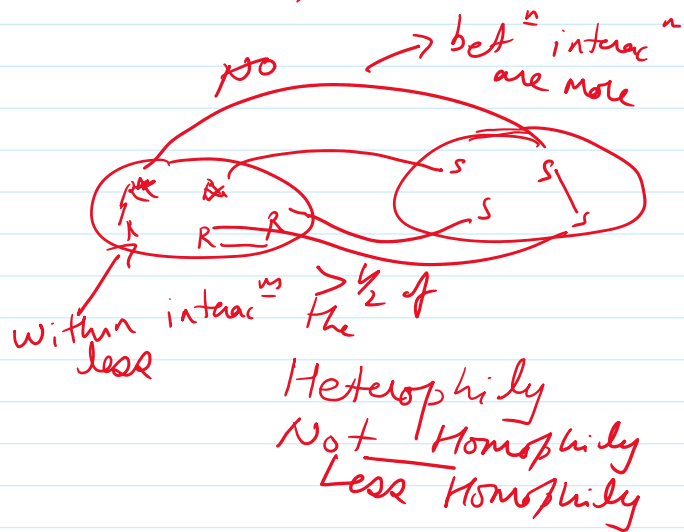
$H H \rightarrow \frac{1}{4}$
 $H T \rightarrow \frac{1}{4}$
 $T H \rightarrow \frac{1}{4}$
 $T T \rightarrow \frac{1}{4}$
 $\frac{1}{2}$

Homophily

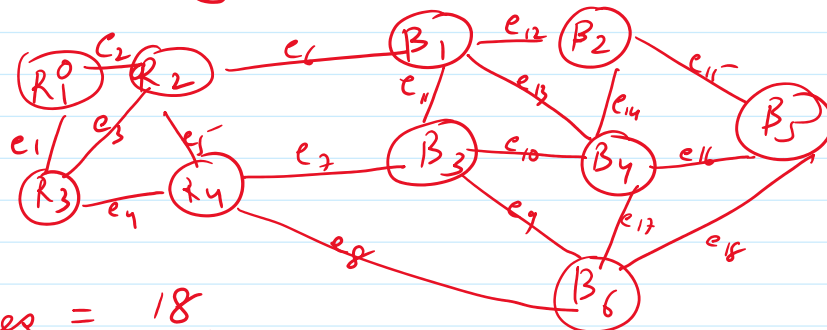
Let's quantify.



Homophily
Assortative Mixing



Heterophily
Not Homophily
Less Homophily



Total edges = 18

Expected edges betⁿ R & S $\Rightarrow 9$

Actual edges = 3.

$$\frac{A_c}{\text{Expected}} \Rightarrow \frac{3}{9} = \frac{1}{3}$$

$$1 - \frac{A_c}{\text{exp}} = 1 - \frac{1}{3} \Rightarrow \text{Value } \uparrow, \text{ homophily } \uparrow$$

$$1 - \frac{A_c}{\text{ex} = A_c} = 0 \Rightarrow \text{Random}$$

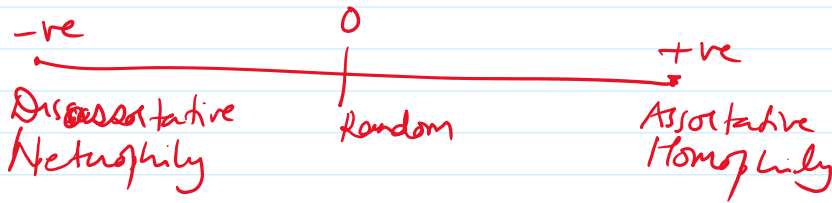
\rightarrow Assortative
 \rightarrow Not homophily
 \rightarrow Disassortative

$$1 - \frac{A_c}{E_c} = 0 \Rightarrow \text{Random}$$

Disassortative

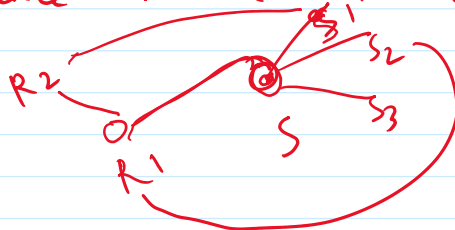
When $A_c > E_c$

$1 - \frac{A_c}{E_c}$ is -ve \rightarrow Non-Homophily
Heterophily / Disassortative



\rightarrow Similar nodes interact \checkmark

\rightarrow Influence Nodes influence other nodes



Link predicⁿ.

\rightarrow Categorical attributes
race, hair, city

age? \rightarrow numerical
Salary? \rightarrow numerical

$$\gamma = \frac{\sum_{i,j} e_{ij} - \sum_i a_i^2}{1 - \sum_i a_i^2}$$

e_{ij} = fracⁿ of edges betⁿ nodes w' same attrⁿ

a_i = fracⁿ of edges having at least one end w' attrⁿ

	s_1	s_2	s_3	s_4	a_i
s_1	0.3	0.05	0.1	0.05	0.5
s_2	0.05	0.05	0	0	0.1
s_3	0.1	0	0.2	0	0.3
s_4	0.05	0	0	0.05	0.1
a_i	0.5	0.1	0.3	0.1	1

fracⁿ of edges betⁿ s_1 & s_4 students

fracⁿ of edges betⁿ s_2 & s_4 students

\rightarrow actual

\rightarrow

$$\gamma = (0.3 + 0.05 + 0.2 + 0.5) - (0.5^2 + 0.1^2 + 0.3^2 + 0.1^2)$$

$$\gamma = \frac{(0.3 + 0.05 + 0.2 + 0.5) - (0.5^2 + 0.1^2 + 0.3^2 + 0.1^2)}{1 - (0.5^2 + 0.1^2 + 0.3^2 + 0.1^2)}$$

→ actual "

exp.

$$1 - \frac{Ac}{Exp}$$

=
Homophily / Assortative index value of the n/w.
in the context of sem attribute