

Untitled

April 20, 2016

1 In-Class Exercise

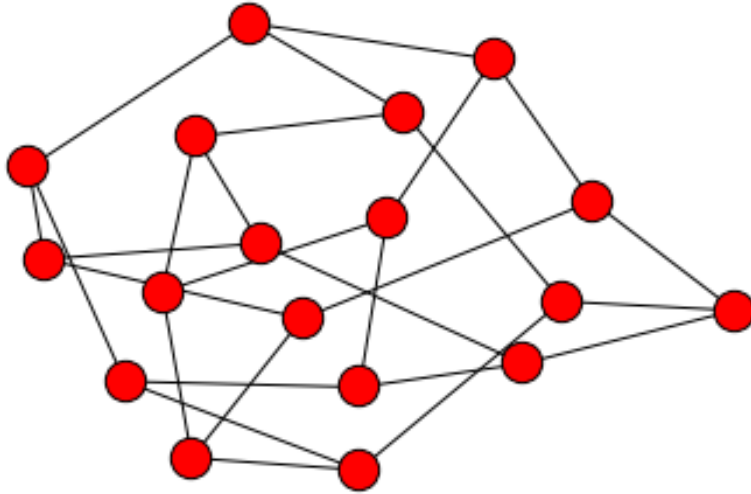
Dinara Assan and Nurdaulet Kenges

```
In [2]: import networkx as nx
import matplotlib.pyplot as plt
F = nx.powerlaw_cluster_graph (9, 1, 0.4)
G = nx.barabasi_albert_graph (100, 2)
H = nx.grid_2d_graph (10, 10)
I = nx.complete_graph (10)
J = nx.cycle_graph (10)
K = nx.erdos_renyi_graph (100, 0.01)
```

```
In [3]: import networkx as nx
import matplotlib.pyplot as plt
import numpy as np
%matplotlib inline

L = nx.pappus_graph ()
nx.draw(L)
plt.show()

a = nx.adjacency_matrix(L)
print(a)
l = nx.laplacian_matrix(L)
l = l.todense ()
w, v = np.linalg.eig(l)
print(w)
```



| | |
|---------|---|
| (0, 1) | 1 |
| (0, 5) | 1 |
| (0, 17) | 1 |
| (1, 0) | 1 |
| (1, 2) | 1 |
| (1, 8) | 1 |
| (2, 1) | 1 |
| (2, 3) | 1 |
| (2, 13) | 1 |
| (3, 2) | 1 |
| (3, 4) | 1 |
| (3, 10) | 1 |
| (4, 3) | 1 |
| (4, 5) | 1 |
| (4, 15) | 1 |
| (5, 0) | 1 |
| (5, 4) | 1 |
| (5, 6) | 1 |
| (6, 5) | 1 |
| (6, 7) | 1 |
| (6, 11) | 1 |
| (7, 6) | 1 |
| (7, 8) | 1 |
| (7, 14) | 1 |
| (8, 1) | 1 |
| : | : |
| (9, 16) | 1 |

```

(10, 3)      1
(10, 9)      1
(10, 11)     1
(11, 6)      1
(11, 10)     1
(11, 12)     1
(12, 11)     1
(12, 13)     1
(12, 17)     1
(13, 2)      1
(13, 12)     1
(13, 14)     1
(14, 7)      1
(14, 13)     1
(14, 15)     1
(15, 4)      1
(15, 14)     1
(15, 16)     1
(16, 9)      1
(16, 15)     1
(16, 17)     1
(17, 0)      1
(17, 12)     1
(17, 16)     1
[ 6.00000000e+00 -3.53883589e-16  3.00000000e+00  3.00000000e+00
 4.73205081e+00  3.00000000e+00  4.73205081e+00  4.73205081e+00
 3.00000000e+00  1.26794919e+00  1.26794919e+00  4.73205081e+00
 4.73205081e+00  1.26794919e+00  1.26794919e+00  1.26794919e+00
 1.26794919e+00  4.73205081e+00]

```

```

In [25]: import networkx as nx
import matplotlib.pyplot as plt
import numpy as np
%matplotlib inline

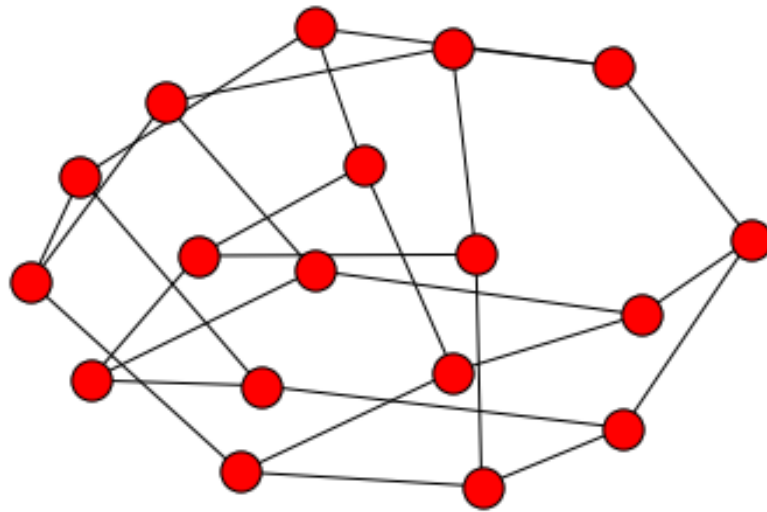
L = nx.pappus_graph ()
nx.draw(L)
plt.show()

a = nx.adjacency_matrix(L)

l = nx.laplacian_matrix(L)
l = l.todense ()
w, v = np.linalg.eig(l)

count=0
for i in range(len(w)):
    if(w[i]==0):
        count+=1
print("The number of zeros", count)

```

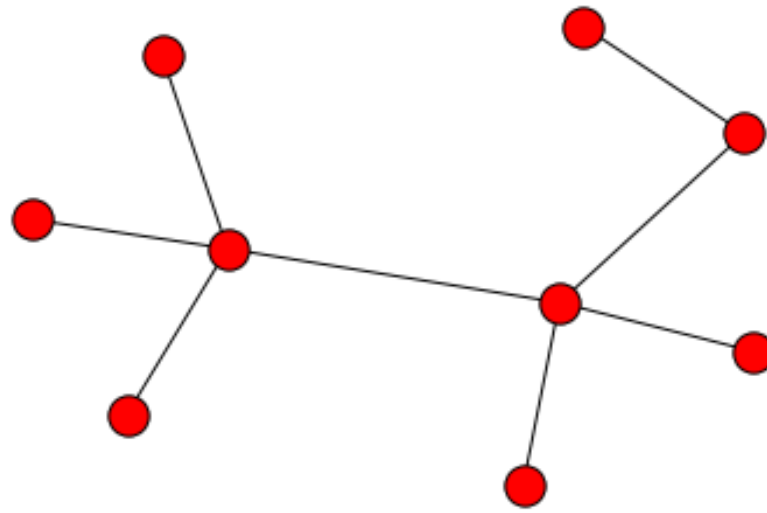


The number of zeros 0

```
In [4]: def draw_comp(L):
        nx.draw(L)
        plt.show()

        a = nx.adjacency_matrix(L)
        print("The Adjacent Matrix")
        print(a)
        l = nx.laplacian_matrix(L)
        l = l.todense ()
        w, v = np.linalg.eig(l)
        print("The Laplacian Matrix")
        print(w)
        count=0
        for i in range(len(w)):
            if(w[i]==0):
                count+=1
        print("The number of zeros", count)

In [27]: draw_comp(F)
```



The Adjacent Matrix

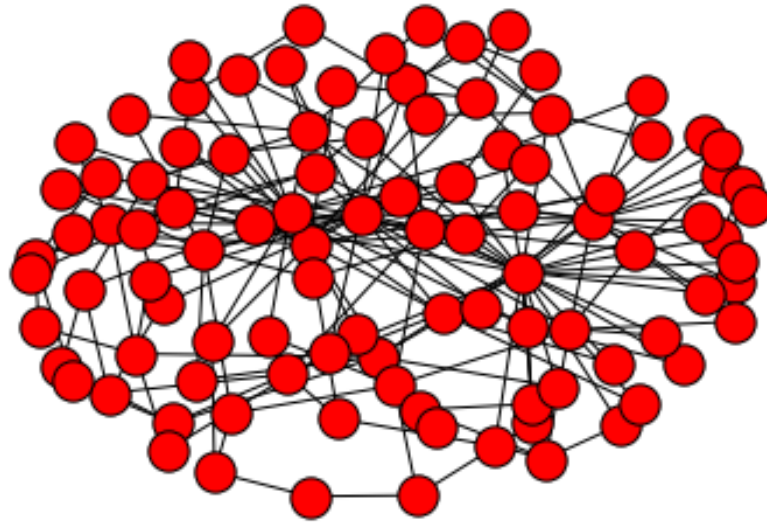
| | |
|--------|---|
| (0, 1) | 1 |
| (0, 3) | 1 |
| (0, 4) | 1 |
| (0, 8) | 1 |
| (1, 0) | 1 |
| (1, 2) | 1 |
| (2, 1) | 1 |
| (3, 0) | 1 |
| (3, 5) | 1 |
| (3, 6) | 1 |
| (3, 7) | 1 |
| (4, 0) | 1 |
| (5, 3) | 1 |
| (6, 3) | 1 |
| (7, 3) | 1 |
| (8, 0) | 1 |

The Laplacian Matrix

| | | | | |
|---|-----------------|----------------|----------------|----------------|
| [| 5.67925111e+00 | 4.08635154e+00 | 2.37349122e+00 | 3.34408019e-16 |
| | 2.82470428e-01 | 5.78435710e-01 | 1.00000000e+00 | 1.00000000e+00 |
| | 1.00000000e+00] | | | |

The number of zeros 0

In [28]: draw_comp(G)



The Adjacent Matrix

| | |
|---------|---|
| (0, 2) | 1 |
| (0, 3) | 1 |
| (0, 4) | 1 |
| (0, 6) | 1 |
| (0, 7) | 1 |
| (0, 12) | 1 |
| (0, 16) | 1 |
| (0, 23) | 1 |
| (0, 41) | 1 |
| (0, 43) | 1 |
| (0, 45) | 1 |
| (0, 54) | 1 |
| (0, 60) | 1 |
| (0, 74) | 1 |
| (0, 76) | 1 |
| (0, 77) | 1 |
| (0, 84) | 1 |
| (0, 86) | 1 |
| (0, 96) | 1 |
| (1, 2) | 1 |
| (1, 7) | 1 |
| (1, 17) | 1 |
| (1, 48) | 1 |
| (1, 50) | 1 |
| (1, 69) | 1 |
| : | : |

(88, 43) 1
 (89, 2) 1
 (89, 56) 1
 (90, 44) 1
 (90, 55) 1
 (91, 4) 1
 (91, 13) 1
 (92, 13) 1
 (92, 53) 1
 (92, 95) 1
 (92, 97) 1
 (93, 53) 1
 (93, 56) 1
 (94, 41) 1
 (94, 76) 1
 (95, 13) 1
 (95, 92) 1
 (96, 0) 1
 (96, 77) 1
 (97, 18) 1
 (97, 92) 1
 (98, 9) 1
 (98, 37) 1
 (99, 10) 1
 (99, 51) 1

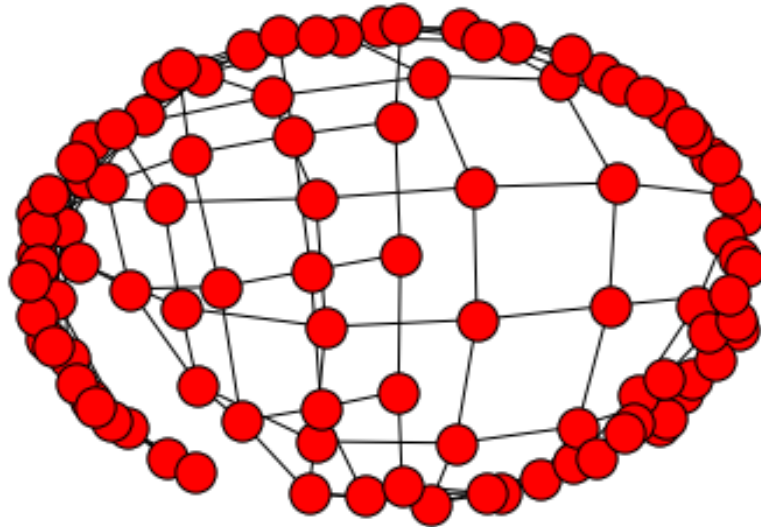
The Laplacian Matrix

| | |
|-----------------------------------|---------------------------------|
| [2.91334650e+01 +0.00000000e+00j | 2.09521573e+01 +0.00000000e+00j |
| 1.92419123e+01 +0.00000000e+00j | 1.63040537e+01 +0.00000000e+00j |
| 1.49420109e+01 +0.00000000e+00j | 1.08061380e+01 +0.00000000e+00j |
| 9.96363774e+00 +0.00000000e+00j | 8.97967437e+00 +0.00000000e+00j |
| 8.02739615e+00 +0.00000000e+00j | 7.69883782e+00 +0.00000000e+00j |
| 7.55317222e+00 +0.00000000e+00j | 6.96269794e+00 +0.00000000e+00j |
| 6.81689628e+00 +0.00000000e+00j | 6.62797955e+00 +0.00000000e+00j |
| 6.35695376e+00 +0.00000000e+00j | 5.88139857e+00 +0.00000000e+00j |
| 5.80699200e+00 +0.00000000e+00j | 5.75282787e+00 +0.00000000e+00j |
| 5.68444233e+00 +0.00000000e+00j | 5.62389845e+00 +0.00000000e+00j |
| 5.51903637e+00 +0.00000000e+00j | 5.20662022e+00 +0.00000000e+00j |
| 5.06938643e+00 +0.00000000e+00j | 8.04853255e-15 +0.00000000e+00j |
| 4.89004814e+00 +0.00000000e+00j | 4.61341463e+00 +0.00000000e+00j |
| 4.66363319e+00 +0.00000000e+00j | 4.51864923e+00 +0.00000000e+00j |
| 4.37599901e+00 +0.00000000e+00j | 4.17188051e+00 +0.00000000e+00j |
| 4.07434893e+00 +0.00000000e+00j | 3.97014368e+00 +0.00000000e+00j |
| 3.90802946e+00 +0.00000000e+00j | 3.70786169e+00 +0.00000000e+00j |
| 5.55965651e-01 +0.00000000e+00j | 3.65214130e+00 +0.00000000e+00j |
| 3.59576030e+00 +0.00000000e+00j | 5.91863600e-01 +0.00000000e+00j |
| 3.53740399e+00 +0.00000000e+00j | 3.49944613e+00 +0.00000000e+00j |
| 3.36147417e+00 +0.00000000e+00j | 3.45126251e+00 +0.00000000e+00j |
| 3.38289548e+00 +0.00000000e+00j | 3.13044077e+00 +0.00000000e+00j |
| 3.05678526e+00 +0.00000000e+00j | 2.99011352e+00 +0.00000000e+00j |
| 7.67818804e-01 +0.00000000e+00j | 7.88714691e-01 +0.00000000e+00j |
| 2.75425769e+00 +0.00000000e+00j | 8.33687643e-01 +0.00000000e+00j |
| 8.72572871e-01 +0.00000000e+00j | 8.87214123e-01 +0.00000000e+00j |
| 2.51801908e+00 +0.00000000e+00j | 2.49120049e+00 +0.00000000e+00j |
| 2.44502007e+00 +0.00000000e+00j | 9.88414330e-01 +0.00000000e+00j |

| | | | |
|----------------|------------------|----------------|------------------|
| 9.44208675e-01 | +0.00000000e+00j | 1.06705587e+00 | +0.00000000e+00j |
| 1.10252109e+00 | +0.00000000e+00j | 2.15889469e+00 | +0.00000000e+00j |
| 1.15755715e+00 | +0.00000000e+00j | 1.18883126e+00 | +0.00000000e+00j |
| 1.21863127e+00 | +0.00000000e+00j | 1.23613048e+00 | +0.00000000e+00j |
| 1.29236334e+00 | +0.00000000e+00j | 1.31935600e+00 | +0.00000000e+00j |
| 1.98422751e+00 | +0.00000000e+00j | 1.32925062e+00 | +0.00000000e+00j |
| 1.36626044e+00 | +0.00000000e+00j | 1.44180540e+00 | +0.00000000e+00j |
| 1.95951863e+00 | +0.00000000e+00j | 1.47490733e+00 | +0.00000000e+00j |
| 1.92731384e+00 | +0.00000000e+00j | 1.55079308e+00 | +0.00000000e+00j |
| 1.58311090e+00 | +0.00000000e+00j | 1.90394125e+00 | +0.00000000e+00j |
| 1.64990976e+00 | +0.00000000e+00j | 1.68331756e+00 | +0.00000000e+00j |
| 1.60948535e+00 | +0.00000000e+00j | 1.87272331e+00 | +0.00000000e+00j |
| 1.85894952e+00 | +0.00000000e+00j | 1.81361103e+00 | +0.00000000e+00j |
| 1.78522698e+00 | +0.00000000e+00j | 1.71400018e+00 | +0.00000000e+00j |
| 1.53914223e+00 | +0.00000000e+00j | 1.83198552e+00 | +0.00000000e+00j |
| 1.76872368e+00 | +0.00000000e+00j | 1.70817988e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +7.19506754e-16j |
| 2.00000000e+00 | -7.19506754e-16j | 2.00000000e+00 | +0.00000000e+00j |
| 2.00000000e+00 | +0.00000000e+00j | 2.00000000e+00 | +0.00000000e+00j |

The number of zeros 0

In [29]: draw_comp(H)



The Adjacent Matrix
(0, 61) 1


```

(0, 69)      1
(0, 86)      1
(0, 92)      1
(1, 41)      1
(1, 50)      1
(1, 84)      1
(2, 30)      1
(2, 32)      1
(2, 60)      1
(2, 62)      1
(3, 14)      1
(3, 51)      1
(3, 63)      1
(3, 64)      1
(4, 15)      1
(4, 42)      1
(4, 93)      1
(5, 63)      1
(5, 66)      1
(5, 85)      1
(5, 94)      1
(6, 43)      1
(6, 71)      1
(6, 76)      1
:           :
(92, 77)     1
(93, 4)      1
(93, 56)     1
(93, 82)     1
(94, 5)      1
(94, 33)     1
(94, 45)     1
(94, 83)     1
(95, 63)     1
(95, 64)     1
(95, 66)     1
(96, 35)     1
(96, 38)     1
(96, 65)     1
(96, 68)     1
(97, 13)     1
(97, 36)     1
(97, 58)     1
(98, 9)      1
(98, 35)     1
(98, 38)     1
(98, 59)     1
(99, 39)     1
(99, 60)     1
(99, 62)     1

```

The Laplacian Matrix

```

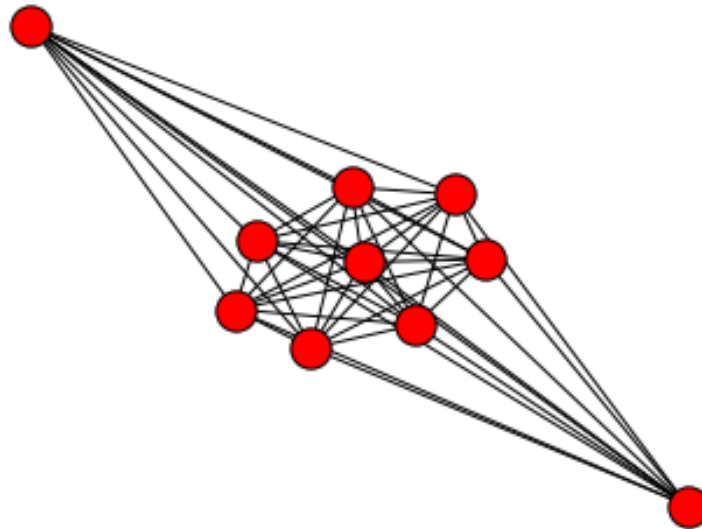
[ 7.80422607e+00  7.52014702e+00  7.23606798e+00 -2.52966051e-15
 1.95773935e-01  7.52014702e+00  6.52014702e+00  7.07768354e+00
 9.78869674e-02  6.79360449e+00  6.35114101e+00  6.23606798e+00

```

| | | | |
|----------------|----------------|----------------|-----------------|
| 7.07768354e+00 | 4.79852979e-01 | 3.81966011e-01 | 6.79360449e+00 |
| 9.78869674e-02 | 8.24429495e-01 | 4.79852979e-01 | 3.81966011e-01 |
| 6.52014702e+00 | 5.90211303e+00 | 6.23606798e+00 | 7.63932023e-01 |
| 8.24429495e-01 | 9.22316463e-01 | 5.90211303e+00 | 1.64885899e+00 |
| 1.20639551e+00 | 5.61803399e+00 | 5.79360449e+00 | 5.79360449e+00 |
| 5.28407904e+00 | 9.22316463e-01 | 1.38196601e+00 | 5.61803399e+00 |
| 1.20639551e+00 | 5.28407904e+00 | 1.47985298e+00 | 1.38196601e+00 |
| 5.17557050e+00 | 1.47985298e+00 | 5.00000000e+00 | 5.23606798e+00 |
| 5.17557050e+00 | 2.00000000e+00 | 1.76393202e+00 | 1.76393202e+00 |
| 5.00000000e+00 | 2.09788697e+00 | 2.20639551e+00 | 4.61803399e+00 |
| 4.72654253e+00 | 2.76393202e+00 | 2.00000000e+00 | 4.72654253e+00 |
| 2.09788697e+00 | 4.55753652e+00 | 4.44246348e+00 | 2.38196601e+00 |
| 4.28407904e+00 | 4.61803399e+00 | 2.20639551e+00 | 4.55753652e+00 |
| 2.38196601e+00 | 4.28407904e+00 | 2.61803399e+00 | 2.82442950e+00 |
| 4.44246348e+00 | 2.61803399e+00 | 4.00000000e+00 | 2.82442950e+00 |
| 3.27345747e+00 | 3.90211303e+00 | 4.00000000e+00 | 3.17557050e+00 |
| 3.55753652e+00 | 3.71592096e+00 | 3.71592096e+00 | 3.61803399e+00 |
| 3.44246348e+00 | 3.38196601e+00 | 3.17557050e+00 | 2.71592096e+00 |
| 2.71592096e+00 | 3.90211303e+00 | 3.38196601e+00 | 3.44246348e+00 |
| 3.61803399e+00 | 3.27345747e+00 | 3.55753652e+00 | 3.00000000e+00 |
| 4.00000000e+00 | 3.00000000e+00 | 4.00000000e+00 | 4.00000000e+00 |
| 4.00000000e+00 | 4.00000000e+00 | 4.00000000e+00 | 4.00000000e+00] |

The number of zeros 0

In [30]: draw_comp(I)



The Adjacent Matrix
(0, 1) 1

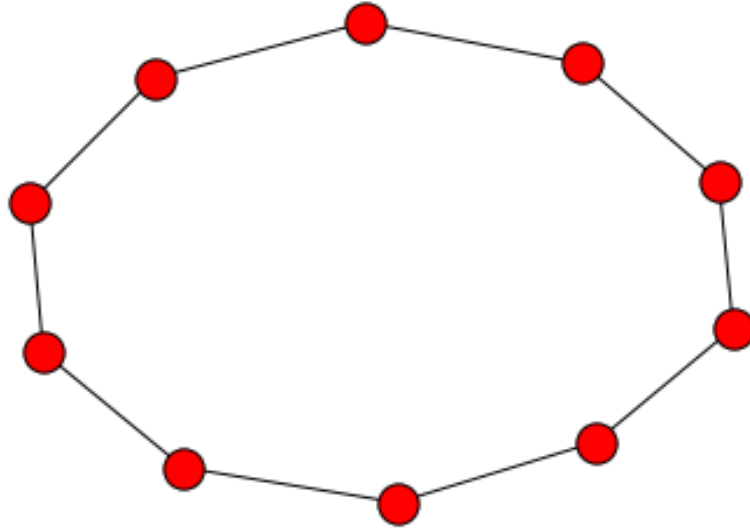
```

(0, 2)      1
(0, 3)      1
(0, 4)      1
(0, 5)      1
(0, 6)      1
(0, 7)      1
(0, 8)      1
(0, 9)      1
(1, 0)      1
(1, 2)      1
(1, 3)      1
(1, 4)      1
(1, 5)      1
(1, 6)      1
(1, 7)      1
(1, 8)      1
(1, 9)      1
(2, 0)      1
(2, 1)      1
(2, 3)      1
(2, 4)      1
(2, 5)      1
(2, 6)      1
(2, 7)      1
:           :
(7, 2)      1
(7, 3)      1
(7, 4)      1
(7, 5)      1
(7, 6)      1
(7, 8)      1
(7, 9)      1
(8, 0)      1
(8, 1)      1
(8, 2)      1
(8, 3)      1
(8, 4)      1
(8, 5)      1
(8, 6)      1
(8, 7)      1
(8, 9)      1
(9, 0)      1
(9, 1)      1
(9, 2)      1
(9, 3)      1
(9, 4)      1
(9, 5)      1
(9, 6)      1
(9, 7)      1
(9, 8)      1
The Laplacian Matrix
[ 1.00000000e+01 -2.22044605e-16 1.00000000e+01 1.00000000e+01
 1.00000000e+01 1.00000000e+01 1.00000000e+01 1.00000000e+01
 1.00000000e+01 1.00000000e+01]

```

The number of zeros 0

```
In [31]: draw_comp(J)
```



The Adjacent Matrix

| | |
|--------|---|
| (0, 1) | 1 |
| (0, 9) | 1 |
| (1, 0) | 1 |
| (1, 2) | 1 |
| (2, 1) | 1 |
| (2, 3) | 1 |
| (3, 2) | 1 |
| (3, 4) | 1 |
| (4, 3) | 1 |
| (4, 5) | 1 |
| (5, 4) | 1 |
| (5, 6) | 1 |
| (6, 5) | 1 |
| (6, 7) | 1 |
| (7, 6) | 1 |
| (7, 8) | 1 |
| (8, 7) | 1 |
| (8, 9) | 1 |
| (9, 0) | 1 |
| (9, 8) | 1 |

The Laplacian Matrix

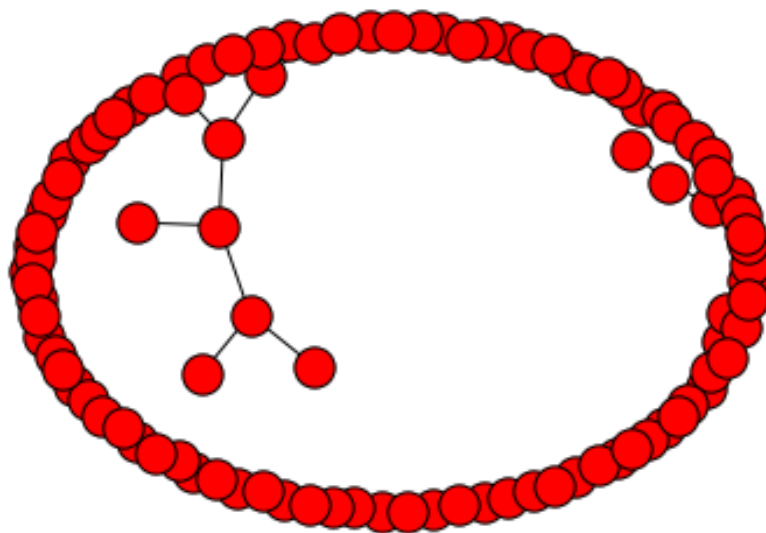
```
[ -2.22044605e-16  3.81966011e-01  1.38196601e+00  2.61803399e+00
```

```

4.00000000e+00  3.61803399e+00  3.61803399e+00  3.81966011e-01
2.61803399e+00  1.38196601e+00]
The number of zeros 0

```

In [32]: draw_comp(K)



The Adjacent Matrix

| | |
|----------|---|
| (0, 23) | 1 |
| (1, 5) | 1 |
| (3, 33) | 1 |
| (3, 94) | 1 |
| (5, 1) | 1 |
| (6, 29) | 1 |
| (6, 43) | 1 |
| (8, 62) | 1 |
| (9, 64) | 1 |
| (10, 48) | 1 |
| (11, 57) | 1 |
| (11, 98) | 1 |
| (18, 39) | 1 |
| (18, 51) | 1 |
| (19, 50) | 1 |
| (20, 83) | 1 |
| (22, 64) | 1 |
| (22, 91) | 1 |
| (23, 0) | 1 |
| (23, 49) | 1 |

```

(23, 90)      1
(27, 59)      1
(29, 6)       1
(29, 94)      1
(30, 46)      1
:             :
(65, 87)      1
(66, 49)      1
(67, 56)      1
(70, 32)      1
(76, 98)      1
(78, 61)      1
(78, 84)      1
(79, 32)      1
(81, 55)      1
(81, 82)      1
(82, 81)      1
(83, 20)      1
(84, 78)      1
(87, 58)      1
(87, 65)      1
(89, 62)      1
(90, 23)      1
(91, 22)      1
(91, 61)      1
(94, 3)       1
(94, 29)      1
(94, 52)      1
(98, 11)      1
(98, 49)      1
(98, 76)      1

```

The Laplacian Matrix

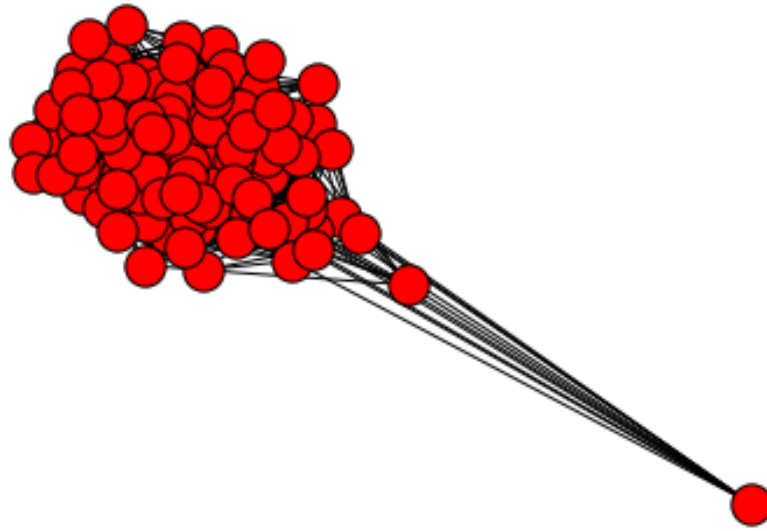
```

[ 4.84677823e+00 +0.00000000e+00j  3.85252385e+00 +0.00000000e+00j
  4.43828324e+00 +0.00000000e+00j  2.73378014e+00 +0.00000000e+00j
  2.07824830e+00 +0.00000000e+00j  3.13856427e+00 +0.00000000e+00j
  2.61803399e+00 +0.00000000e+00j  7.22292395e-01 +0.00000000e+00j
  5.54591229e-01 +0.00000000e+00j  3.80193774e+00 +0.00000000e+00j
  3.24697960e+00 +0.00000000e+00j  1.17975075e+00 +0.00000000e+00j
  2.11785864e-01 +0.00000000e+00j  2.44504187e+00 +0.00000000e+00j
  3.41421356e+00 +0.00000000e+00j  3.00000000e+00 +0.00000000e+00j
  3.81966011e-01 +0.00000000e+00j  1.55495813e+00 +0.00000000e+00j
  3.00000000e+00 +0.00000000e+00j  2.43401746e-01 +0.00000000e+00j
  7.53020396e-01 +0.00000000e+00j  3.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  3.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  1.98062264e-01 +0.00000000e+00j
  1.00000000e+00 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
  5.85786438e-01 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
  3.00000000e+00 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  3.00000000e+00 +0.00000000e+00j
  2.00000000e+00 +0.00000000e+00j  1.00000000e+00 +0.00000000e+00j
 -7.22701989e-16 +0.00000000e+00j -2.27194446e-16 +0.00000000e+00j
 -2.25871106e-16 +4.57122035e-16j -2.25871106e-16 -4.57122035e-16j

```

The number of zeros 46

```
In [33]: K = nx.erdos_renyi_graph (100, 0.2)
In [34]: draw_comp(K)
```



The Adjacent Matrix

| | |
|---------|---|
| (0, 7) | 1 |
| (0, 8) | 1 |
| (0, 12) | 1 |
| (0, 18) | 1 |
| (0, 19) | 1 |
| (0, 24) | 1 |
| (0, 28) | 1 |
| (0, 41) | 1 |
| (0, 49) | 1 |
| (0, 57) | 1 |
| (0, 58) | 1 |
| (0, 59) | 1 |
| (0, 60) | 1 |
| (0, 73) | 1 |
| (0, 82) | 1 |
| (0, 86) | 1 |
| (0, 97) | 1 |
| (0, 98) | 1 |
| (1, 2) | 1 |
| (1, 3) | 1 |
| (1, 5) | 1 |
| (1, 6) | 1 |
| (1, 10) | 1 |
| (1, 23) | 1 |
| (1, 30) | 1 |
| : | : |


```

(98, 63)      1
(98, 66)      1
(98, 69)      1
(98, 80)      1
(98, 96)      1
(98, 97)      1
(99, 3)       1
(99, 5)       1
(99, 11)      1
(99, 12)      1
(99, 18)      1
(99, 26)      1
(99, 29)      1
(99, 38)      1
(99, 42)      1
(99, 43)      1
(99, 52)      1
(99, 61)      1
(99, 63)      1
(99, 69)      1
(99, 70)      1
(99, 78)      1
(99, 80)      1
(99, 86)      1
(99, 96)      1

```

The Laplacian Matrix

```

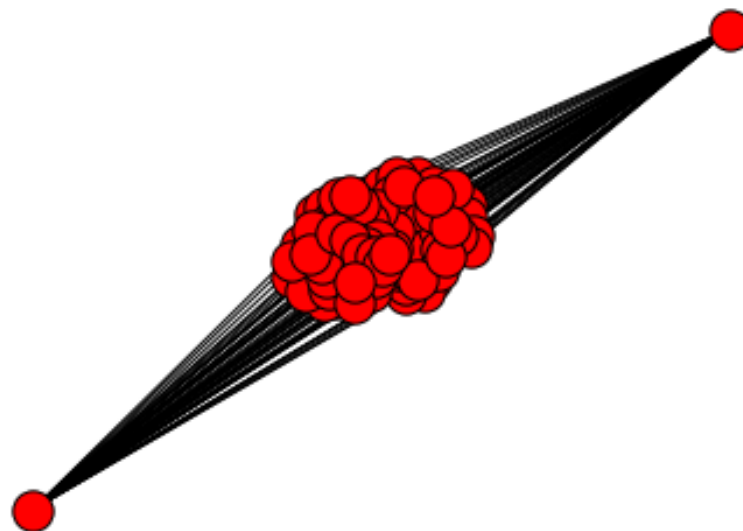
[ -1.80860837e-15  3.27976360e+01  7.66213812e+00  3.14378484e+01
  3.10828355e+01  3.01028691e+01  2.99795091e+01  2.92326962e+01
  9.77506512e+00  1.03914876e+01  2.90404336e+01  2.87293397e+01
  2.88161397e+01  2.80890578e+01  1.07525921e+01  1.10472147e+01
  2.74283312e+01  2.74415941e+01  2.72014889e+01  2.68130051e+01
  1.15416329e+01  1.21560522e+01  1.22457898e+01  2.65758256e+01
  2.62251663e+01  2.63778571e+01  2.58331295e+01  1.25346531e+01
  1.26369030e+01  2.56908191e+01  2.55766631e+01  1.28845285e+01
  2.53535411e+01  2.50135134e+01  1.30448338e+01  2.47312654e+01
  1.33088839e+01  2.46387624e+01  1.36688143e+01  1.37957033e+01
  2.43581575e+01  2.41454590e+01  2.40491857e+01  2.36932021e+01
  1.39808994e+01  1.41554152e+01  2.34315105e+01  1.42866113e+01
  1.45299422e+01  1.47701404e+01  1.45758280e+01  2.31936751e+01
  1.50401966e+01  2.30924344e+01  2.28260960e+01  2.26411985e+01
  1.51832596e+01  2.23458744e+01  2.21910140e+01  1.55432826e+01
  1.56172755e+01  1.56632572e+01  2.20079769e+01  2.18679534e+01
  1.58704567e+01  2.17131248e+01  1.61202290e+01  1.62868010e+01
  1.59537502e+01  1.65449211e+01  1.65336158e+01  2.14049825e+01
  2.12073656e+01  1.69938917e+01  1.70714673e+01  1.71660221e+01
  1.74202860e+01  1.75426209e+01  2.10321262e+01  2.09119115e+01
  1.77360499e+01  1.79994515e+01  1.82810491e+01  2.07805420e+01
  1.96935262e+01  1.96046910e+01  1.78274159e+01  1.98770923e+01
  1.92378794e+01  2.04643686e+01  1.87081801e+01  1.89202354e+01
  1.99972227e+01  1.90481712e+01  1.87812208e+01  2.00913266e+01
  2.03093196e+01  2.03601865e+01  1.85384306e+01  1.91246025e+01]

```

The number of zeros 0

In [35]: K = nx.erdos_renyi_graph (100, 0.5)

`draw_comp(K)`



The Adjacent Matrix

| | |
|---------|---|
| (0, 1) | 1 |
| (0, 3) | 1 |
| (0, 6) | 1 |
| (0, 8) | 1 |
| (0, 10) | 1 |
| (0, 11) | 1 |
| (0, 12) | 1 |
| (0, 17) | 1 |
| (0, 18) | 1 |
| (0, 21) | 1 |
| (0, 22) | 1 |
| (0, 24) | 1 |
| (0, 25) | 1 |
| (0, 26) | 1 |
| (0, 27) | 1 |
| (0, 31) | 1 |
| (0, 33) | 1 |
| (0, 34) | 1 |
| (0, 35) | 1 |
| (0, 37) | 1 |
| (0, 38) | 1 |
| (0, 40) | 1 |
| (0, 41) | 1 |
| (0, 42) | 1 |

```

(0, 44)      1
:           :
(99, 59)     1
(99, 60)     1
(99, 62)     1
(99, 63)     1
(99, 64)     1
(99, 65)     1
(99, 66)     1
(99, 67)     1
(99, 69)     1
(99, 70)     1
(99, 71)     1
(99, 73)     1
(99, 75)     1
(99, 76)     1
(99, 78)     1
(99, 80)     1
(99, 82)     1
(99, 83)     1
(99, 84)     1
(99, 85)     1
(99, 89)     1
(99, 91)     1
(99, 93)     1
(99, 94)     1
(99, 97)     1

```

The Laplacian Matrix

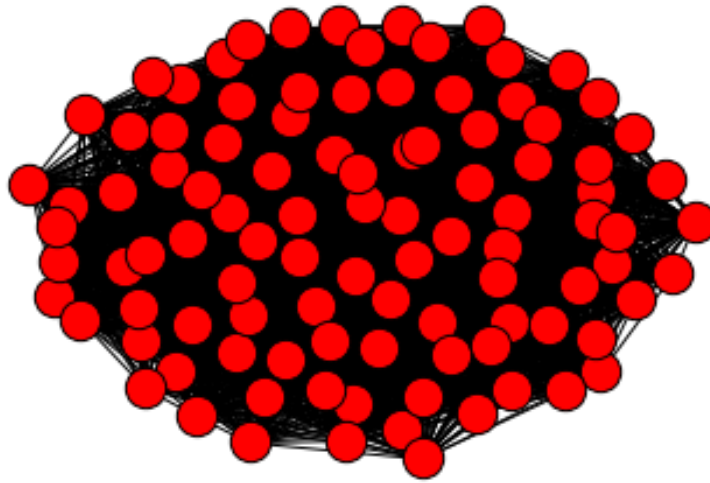
```

[ 2.68661538e-14  3.37224622e+01  3.61702641e+01  6.37307471e+01
  3.69100220e+01  3.77670853e+01  6.23261187e+01  6.17281833e+01
  6.14847443e+01  6.03461747e+01  6.01717683e+01  6.02197813e+01
  3.86090309e+01  3.90601781e+01  5.95787835e+01  5.93614652e+01
  3.94083424e+01  5.89707039e+01  3.97643732e+01  5.87201772e+01
  3.99510947e+01  4.02743764e+01  5.83216658e+01  5.80541703e+01
  5.78159545e+01  5.76673504e+01  4.10219459e+01  5.72456917e+01
  5.69757106e+01  5.68265166e+01  4.09614297e+01  4.14896006e+01
  4.16175900e+01  4.17819544e+01  5.62522657e+01  4.22647606e+01
  5.60894310e+01  4.24482965e+01  5.58782068e+01  4.26071990e+01
  5.55446152e+01  5.55066932e+01  4.28954071e+01  5.52448477e+01
  5.50290372e+01  4.31426140e+01  4.35535627e+01  4.34341176e+01
  4.37856473e+01  5.46633580e+01  5.45177075e+01  4.40925614e+01
  4.44073146e+01  5.44445701e+01  5.41209669e+01  5.39216726e+01
  4.45674614e+01  4.47877643e+01  4.46939258e+01  4.50969866e+01
  5.34781310e+01  5.34030620e+01  5.32514246e+01  4.55216545e+01
  5.30996669e+01  4.57146021e+01  5.26383567e+01  4.61238985e+01
  5.24029939e+01  4.62902504e+01  4.65006188e+01  5.21179315e+01
  5.19923831e+01  5.16796306e+01  5.14048246e+01  4.65616330e+01
  5.13176870e+01  5.20531676e+01  4.69168481e+01  4.68322561e+01
  5.09538398e+01  4.73492923e+01  5.06931187e+01  4.94557163e+01
  5.02240684e+01  4.78736593e+01  4.80567188e+01  4.81706146e+01
  4.76535306e+01  4.99793154e+01  4.91149225e+01  5.03846083e+01
  4.75680744e+01  4.87195277e+01  4.99484768e+01  4.91986815e+01
  5.04444948e+01  4.85610400e+01  4.86439075e+01  4.86589239e+01]

```

The number of zeros 0

```
In [5]: K = nx.erdos_renyi_graph (100, 0.7)
        draw_comp(K)
```



The Adjacent Matrix

| | |
|---------|---|
| (0, 1) | 1 |
| (0, 2) | 1 |
| (0, 3) | 1 |
| (0, 5) | 1 |
| (0, 7) | 1 |
| (0, 8) | 1 |
| (0, 10) | 1 |
| (0, 11) | 1 |
| (0, 12) | 1 |
| (0, 14) | 1 |
| (0, 15) | 1 |
| (0, 16) | 1 |
| (0, 17) | 1 |
| (0, 21) | 1 |
| (0, 22) | 1 |
| (0, 24) | 1 |
| (0, 27) | 1 |
| (0, 28) | 1 |
| (0, 30) | 1 |
| (0, 32) | 1 |
| (0, 33) | 1 |
| (0, 34) | 1 |
| (0, 37) | 1 |

```

(0, 38)      1
(0, 39)      1
:           :
(99, 70)     1
(99, 71)     1
(99, 73)     1
(99, 74)     1
(99, 75)     1
(99, 77)     1
(99, 78)     1
(99, 79)     1
(99, 80)     1
(99, 81)     1
(99, 82)     1
(99, 83)     1
(99, 84)     1
(99, 86)     1
(99, 88)     1
(99, 89)     1
(99, 90)     1
(99, 91)     1
(99, 92)     1
(99, 93)     1
(99, 94)     1
(99, 95)     1
(99, 96)     1
(99, 97)     1
(99, 98)     1

```

The Laplacian Matrix

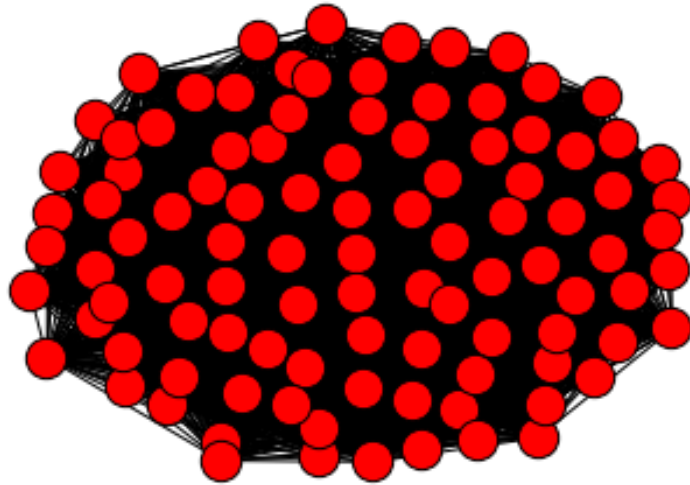
```

[ 3.81040686e-14  5.61745660e+01  8.40385579e+01  5.72253283e+01
 5.81745896e+01  5.87131797e+01  5.95084540e+01  8.22085002e+01
 8.15212326e+01  8.12101382e+01  8.10097383e+01  6.02266349e+01
 8.08222179e+01  8.05556154e+01  8.00226625e+01  6.05374900e+01
 6.08735259e+01  6.10891827e+01  6.13574945e+01  7.90488010e+01
 7.89026760e+01  7.87385021e+01  6.17428859e+01  6.18592913e+01
 6.21374431e+01  6.22478092e+01  7.83568353e+01  7.82491839e+01
 6.25692821e+01  7.78886898e+01  7.75742551e+01  7.73736280e+01
 7.70242775e+01  6.32261464e+01  6.34610693e+01  6.37956489e+01
 7.68162727e+01  6.39569036e+01  7.65836562e+01  7.64740991e+01
 7.63940560e+01  7.58957007e+01  6.44685306e+01  6.43058161e+01
 6.43492642e+01  6.48301604e+01  7.57393440e+01  6.50410097e+01
 7.56016788e+01  6.53519158e+01  7.53076336e+01  7.52712990e+01
 6.54767695e+01  7.50834947e+01  7.49561478e+01  7.46712929e+01
 6.61953117e+01  6.61830279e+01  6.64799536e+01  7.41541555e+01
 7.41081064e+01  6.66723167e+01  6.68023810e+01  7.38677600e+01
 7.37340423e+01  6.69558051e+01  7.35033829e+01  6.73950922e+01
 6.76412121e+01  7.32331787e+01  7.36176870e+01  6.73431172e+01
 6.77636050e+01  6.80136131e+01  6.84238460e+01  6.85552617e+01
 7.27378727e+01  7.26654014e+01  6.89567278e+01  6.90642816e+01
 6.94307622e+01  7.17799795e+01  7.16967804e+01  7.20154094e+01
 6.96590324e+01  7.13249287e+01  7.00676707e+01  7.10857290e+01
 7.03257656e+01  7.22657771e+01  7.24937795e+01  7.07222582e+01
 6.98612459e+01  6.81736068e+01  6.72121568e+01  7.23245673e+01
 7.04457032e+01  7.06072852e+01  6.91892367e+01  7.12106074e+01]

```

The number of zeros 0

```
In [6]: K = nx.erdos_renyi_graph (100, 0.9)
        draw_comp(K)
```



The Adjacent Matrix

| | |
|---------|---|
| (0, 1) | 1 |
| (0, 2) | 1 |
| (0, 4) | 1 |
| (0, 5) | 1 |
| (0, 6) | 1 |
| (0, 7) | 1 |
| (0, 8) | 1 |
| (0, 9) | 1 |
| (0, 10) | 1 |
| (0, 11) | 1 |
| (0, 12) | 1 |
| (0, 14) | 1 |
| (0, 15) | 1 |
| (0, 16) | 1 |
| (0, 17) | 1 |
| (0, 19) | 1 |
| (0, 20) | 1 |
| (0, 21) | 1 |
| (0, 22) | 1 |
| (0, 23) | 1 |
| (0, 24) | 1 |

```

(0, 25)      1
(0, 26)      1
(0, 27)      1
(0, 28)      1
:            :
(99, 70)     1
(99, 71)     1
(99, 72)     1
(99, 73)     1
(99, 74)     1
(99, 75)     1
(99, 76)     1
(99, 77)     1
(99, 78)     1
(99, 79)     1
(99, 80)     1
(99, 81)     1
(99, 85)     1
(99, 86)     1
(99, 87)     1
(99, 88)     1
(99, 89)     1
(99, 90)     1
(99, 92)     1
(99, 93)     1
(99, 94)     1
(99, 95)     1
(99, 96)     1
(99, 97)     1
(99, 98)     1

```

The Laplacian Matrix

```

[ 3.43771508e-14  7.95556597e+01  8.00544626e+01  9.91293352e+01
  8.14268760e+01  9.71829214e+01  8.20344632e+01  8.22118313e+01
  8.27658602e+01  8.30201071e+01  8.32802357e+01  8.33877362e+01
  8.37102962e+01  9.67580188e+01  9.66962199e+01  9.65678616e+01
  8.42184424e+01  8.42696282e+01  9.62750799e+01  8.44541270e+01
  8.46270914e+01  9.60309024e+01  9.60632126e+01  9.60719338e+01
  8.50043154e+01  8.51605038e+01  9.56455403e+01  9.54782454e+01
  8.53809356e+01  9.53368538e+01  8.54489113e+01  8.58280854e+01
  8.57930936e+01  8.61074994e+01  9.51231629e+01  9.50494680e+01
  9.49259840e+01  9.48886061e+01  8.63953150e+01  9.46724528e+01
  9.44808658e+01  9.42345695e+01  8.65121889e+01  8.65943033e+01
  8.66766328e+01  8.68352757e+01  9.41372732e+01  9.40554426e+01
  8.70266916e+01  8.72964413e+01  9.39551674e+01  9.37931595e+01
  9.36313633e+01  9.39129572e+01  8.74590610e+01  9.33838796e+01
  9.32339798e+01  9.31732708e+01  8.76125187e+01  8.77333490e+01
  8.78290532e+01  8.79856848e+01  8.80825764e+01  9.29582862e+01
  9.29007418e+01  9.27537756e+01  8.83078662e+01  9.26611191e+01
  8.84066253e+01  8.82252191e+01  9.25044664e+01  9.24263251e+01
  8.86659271e+01  8.88411429e+01  9.23043281e+01  9.21096530e+01
  8.89929724e+01  8.90759705e+01  8.92842087e+01  8.92296694e+01
  9.17712801e+01  9.17641503e+01  8.95405781e+01  9.04681356e+01
  9.03591980e+01  8.99307557e+01  9.14190262e+01  9.00679363e+01
  9.13584764e+01  9.06088138e+01  8.97663018e+01  8.98157587e+01

```

```
9.01482448e+01  9.16116978e+01  9.12409518e+01  9.08186978e+01
9.11478704e+01  9.09185456e+01  9.07475516e+01  9.11807512e+01]
The number of zeros 0
```

As we can see, Erdos Renyi graph takes into argument the probability of connection between nodes. The higher probability, the connections gets more, this can be seen in previous plotted graphs.

In []: