$$\rho = a \frac{z}{\varphi} = \beta$$