$$\rho = a \frac{z}{\varphi + d\varphi} = \beta$$