

# Symmetric Encryption

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## Encryption Schemes

### Definition

An Encryption Scheme is a tuple  $(X, K, E, D)$  with:

- $X \subseteq \{0, 1\}^*$  Plaintexts
- $K \subseteq \{0, 1\}^*$  the finite Set of keys
- $E$  is a probabilistic encryption algorithm with  $x \in X; k \in K$  as inputs, so that  $E(x, k) = y \in \{0, 1\}^*$
- $D$  is a deterministic decryption algo. with  $y \in \{0, 1\}^*; k \in K$  as inputs and returns  $x \in X$

The Scheme has to satisfy the "perfect correctness" property:

$$\forall x \in X; k \in K : D(E(x, k), k) = x$$

$y := E(x, k)$  is called a cyphertext.

$Y$  is the set of all possible cyphertexts.

$$Y \subseteq \{0, 1\}^*$$

### Definition

Let  $X, K, E, D$  be an encryption scheme with deterministic encryption.

For  $k \in K$  the function:

$$E(\cdot, k) : X \rightarrow Y; x \mapsto E(x, k)$$

Is called a Cipher.